| 1 | Scheme | Marks | AOs | Pearson Progression Step and Progress descriptor |
| :---: | :---: | :---: | :---: | :---: |
| (a) | Makes an attempt to substitute $k=1, k=2$ and $k=4$ into $a_{k}=2^{k}+1, k$ Ö 1 | M1 | 1.1b | 5th <br> Understand disproof by counter example. |
|  | Shows that $a_{1}=3, a_{2}=5$ and $a_{4}=17$ and these are prime numbers. | A1 | 1.1b |  |
|  |  | (2) |  |  |
| (b) | Substitutes a value of $k$ that does not yield a prime number. <br> For example, $a_{3}=9$ or $a_{5}=33$ | A1 | 1.1b | 5th <br> Understand disproof by counter example. |
|  | Concludes that their number is not prime. <br> For example, states that $9=3 \times 3$, so 9 is not prime. | B1 | 2.4 |  |
|  |  | (2) |  |  |
| (4 marks) |  |  |  |  |
| Notes |  |  |  |  |


| 2 | Scheme | Marks | AOs | Pearson <br> Progression Step and Progress descriptor |
| :---: | :---: | :---: | :---: | :---: |
|  | Finds $\|a\|=\sqrt{(4)^{2}+(-1)^{2}+(3)^{2}}=\sqrt{26}$ | M1 | 1.1b | 5th <br> Find the magnitude of a vector in 3 dimensions. |
|  | $\text { States } \cos \theta_{y}=-\frac{1}{\sqrt{26}}$ | M1 | 1.1b |  |
|  | Solves to find $\theta_{y}=101.309 \ldots{ }^{\circ}$. Accept awrt $101.3^{\circ}$ | A1 | 1.1b |  |
|  |  | (3) |  |  |
|  | (3 marks) |  |  |  |
| Notes |  |  |  |  |


| 3 | Scheme | Marks | AOs | Pearson Progression Step and Progress descriptor |
| :---: | :---: | :---: | :---: | :---: |
| (a) | Deduces from $3 \sin \left(\frac{x}{6}\right)^{3}-\frac{1}{10} x-1=0$ that $3 \sin \left(\frac{x}{6}\right)^{3}=\frac{1}{10} x+1$ | M1 | 1.1b | Understand the concept of roots of equations. |
|  | States $\left(\frac{x}{6}\right)^{3}=\arcsin \left(\frac{1}{3}+\frac{1}{30} x\right)$ | M1 | 1.1b |  |
|  | Multiplies by $6^{3}$ and then takes the cube root: $x=6\left(\sqrt[3]{\arcsin \left(\frac{1}{3}+\frac{1}{30} x\right)}\right)$ | A1 | 1.1b |  |
|  |  | (3) |  |  |
| (b) | Attempts to use iterative procedure to find subsequent values. | M1 | 1.1b | 6th <br> Solve equations approximately using the method of iteration. |
|  | Correctly finds: $\begin{aligned} & x_{1}=4.716 \\ & x_{2}=4.802 \\ & x_{3}=4.812 \\ & x_{4}=4.814 \end{aligned}$ | A1 | 1.1b |  |
|  |  | (2) |  |  |
| ( 5 marks) |  |  |  |  |
| (b) A | Notes <br> d M1 if finds at least one correct answer. |  |  |  |


| 4 | Scheme | Marks | AOs | Pearson <br> Progression Step <br> and Progress <br> descriptor |
| :---: | :--- | :---: | :---: | :---: |
| Recognises that two subsequent values will divide to give an <br> equal ratio and sets up an appropriate equation. <br> $\frac{2 k^{2}}{4 k}=\frac{4 k}{k+2}$ | M1 | 2.2 a | 4th <br> Understand <br> simple geometric <br> sequences. |  |
|  | Makes an attempt to solve the equation. For example, <br> $2 k^{3}+4 k^{2}=16 k^{2}$ or $2 k^{3}-12 k^{2}=0$ | M1 | 1.1 b |  |
|  | M1 | 1.1 b |  |  |


| 5 | Scheme | Marks | AOs | Pearson <br> Progression Step and Progress descriptor |
| :---: | :---: | :---: | :---: | :---: |
|  | Makes an attempt to set up a long division. <br> For example: $x ^ { 2 } - 2 x - 1 5 \longdiv { x ^ { 4 } + 2 x ^ { 3 } - 2 9 x ^ { 2 } - 4 8 x + 9 0 }$ is seen. | M1 | 2.2a | 6th <br> Decompose algebraic fractions into |
|  | Award 1 accuracy mark for each of the following: $x^{2}$ seen, $4 x$ seen, -6 seen. $\begin{gathered} x^{2}+4 x-6 \\ x ^ { 2 } - 2 x - 1 5 \longdiv { x ^ { 4 } + 2 x ^ { 3 } - 2 9 x ^ { 2 } - 4 7 x + 7 7 } \\ \frac{x^{4}-2 x^{3}-15 x^{2}}{4 x^{3}-14 x^{2}-47 x} \\ \frac{4 x^{3}-8 x^{2}-60 x}{-6 x^{2}+13 x+77} \\ \frac{-6 x^{2}+12 x+90}{x-13} \end{gathered}$ | A3 | 1.1b | three linear factors. |
|  | Equates the various terms to obtain the equation: $x-13=V(x-5)+W(x+3)$ <br> Equating the coefficients of $x: V+W=1$ <br> Equating constant terms: $-5 V+3 W=-13$ | M1 | 2.2a |  |
|  | Multiplies one or or both of the equations in an effort to equate one of the two variables. | M1 | 1.1b |  |
|  | Finds $W=-1$ and $V=2$. | A1 | 1.1b |  |
|  |  |  |  | (7 marks) |
| Notes |  |  |  |  |


| 6 | Scheme | Marks | AOs | Pearson <br> Progression Step and Progress descriptor |
| :---: | :---: | :---: | :---: | :---: |
|  | Use Pythagoras' theorem to show that the length of $O B=2 \sqrt{3}$ or $O D=2 \sqrt{3}$ or states $B D=4 \sqrt{3}$ | M1 | 2.2a | 6th <br> Solve problems involving arc length and sector area in context. |
|  | Makes an attempt to find $\angle D A B$ or $\angle D C B$. <br> For example, $\cos \angle D A O=\frac{2}{4}$ is seen. | M1 | 2.2a |  |
|  | Correctly states that $\angle D A B=\frac{2 \pi}{3}$ or $\angle D C B=\frac{2 \pi}{3}$ | A1 | 1.1b |  |
|  | Makes an attempt to find the area of the sector with a radius of 4 and a subtended angle of $\frac{2 \pi}{3}$ <br> For example, $A=\frac{1}{2} \times 4^{2} \times \frac{2 \pi}{3}$ is shown. | M1 | 2.2a |  |
|  | Correctly states that the area of the sector is $\frac{16 \pi}{3}$ | A1 | 1.1b |  |
|  | Recognises the need to subtract the sector area from the area of the rhombus in an attempt to find the shaded area. <br> For example, $\frac{16 \pi}{3}-8 \sqrt{3}$ is seen. | M1 | 3.2a |  |
|  | Recognises that to find the total shaded area this number will need to be multiplied by 2 . For example, $2 \times\left(\frac{16 \pi}{3}-8 \sqrt{3}\right)$ | M1 | 3.2a |  |
|  | Using clear algebra, correctly manipulates the expression and gives a clear final answer of $\frac{2}{3}(16 \pi-24 \sqrt{3})$ | A1 | 1.1b |  |
|  |  |  |  | (8 marks) |
|  | Notes |  |  |  |


| 7 | Scheme | Marks | AOs | Pearson <br> Progression Step and Progress descriptor |
| :---: | :---: | :---: | :---: | :---: |
| (a) | Makes an attempt to rearrange $x=\frac{1+4 t}{1-t}$ to make $t$ the subject. For example, $x-x t=1+4 t$ is seen. | M1 | 2.2a | 5th <br> Convert between parametric equations and cartesian forms using substitution. |
|  | Correctly states $t=\frac{x-1}{4+x}$ | A1 | 1.1b |  |
|  | Makes an attempt to substitute $t=\frac{x-1}{4+x}$ into $y=\frac{2+b t}{1-t}$ <br> For example, $y=\frac{2+\frac{b x-b}{x+4}}{1-\frac{x-1}{x+4}}=\frac{\frac{2 x+8+b x-b}{x+4}}{\frac{x+4-x+1}{x+4}}$ is seen. | M1 | 2.2a |  |
|  | Simplifies the expression showing all steps. <br> For example, $y=\frac{2 x+8+b x-b}{5}=\left(\frac{2+b}{5}\right) x+\left(\frac{8-b}{5}\right)$ | A1 | 1.1b |  |
|  |  | (4) |  |  |
| (b) | Interprets the gradient of line being -1 as $\frac{2+b}{5}=-1$ and finds $b=-7$ | M1 | 2.2a | 5th <br> Convert between parametric equations and cartesian forms using substitution |
|  | Substitutes $t=-1$ to find $x=-\frac{3}{2}$ and $y=\frac{9}{2}$ And substitutes $t=0$ to find $x=1$ and $y=2$ | M1 | 1.1b |  |
|  | Makes an attempt to use Pythagoras' Theorem to find the length of the line: $\sqrt{\left(\frac{5}{2}\right)^{2}+\left(\frac{5}{2}\right)^{2}}$ | M1 | 1.1b |  |
|  | Correctly finds the length of the line segment, $\frac{5 \sqrt{2}}{2}$ or states $a=\frac{5}{2}$ | A1 | 1.1b |  |
|  |  | (4) |  |  |
|  |  |  |  | (8 marks) |
|  | Notes |  |  |  |


| 8 | Scheme | Marks | AOs | Pearson <br> Progression Step and Progress descriptor |
| :---: | :---: | :---: | :---: | :---: |
| (a) | Differentiates $u=4 t^{\frac{2}{3}}$ obtaining $\frac{\mathrm{d} u}{\mathrm{~d} t}=\frac{8}{3} t^{-\frac{1}{3}}$ and differentiates $v=t^{2}+1$ obtaining $\frac{\mathrm{d} v}{\mathrm{~d} t}=2 t$ | M1 | 1.1b | 6th <br> Differentiate using the product rule. |
|  | Makes an attempt to substitute the above values into the product rule formula: $\frac{\mathrm{d} H}{\mathrm{~d} t}=\frac{v \frac{\mathrm{~d} u}{\mathrm{~d} t}-u \frac{\mathrm{~d} v}{\mathrm{~d} t}}{v^{2}}$ | M1 | 2.2a |  |
|  | Finds $\frac{\mathrm{d} H}{\mathrm{~d} t}=\frac{\frac{8}{3} t^{\frac{5}{3}}+\frac{8}{3} t^{-\frac{1}{3}}-8 t^{\frac{5}{3}}}{\left(t^{2}+1\right)^{2}}$ | M1 | 1.1b |  |
|  | Fully simplfies using correct algebra to obtain $\frac{\mathrm{d} H}{\mathrm{~d} t}=\frac{8\left(1-2 t^{2}\right)}{3 \sqrt[3]{t}\left(t^{2}+1\right)^{2}}$ | A1 | 2.4 |  |
|  |  | (4) |  |  |
| (b) | Makes an attempt to substitute $t=2$ into $\frac{\mathrm{d} H}{\mathrm{~d} t}=\frac{8\left(1-2 t^{2}\right)}{3 \sqrt[3]{t}\left(t^{2}+1\right)^{2}}=\frac{8\left(1-2(2)^{2}\right)}{3 \sqrt[3]{2}\left(2^{2}+1\right)^{2}}$ | M1 ft | 1.1b | 6th <br> Differentiate using the product rule. |
|  | Correctly finds $\frac{\mathrm{d} H}{\mathrm{~d} t}=-0.592 \ldots$ and concludes that as $\frac{\mathrm{d} H}{\mathrm{~d} t}<0$ the toy soldier was decreasing in height after 2 seconds. | B1 ft* | 3.5a |  |
|  |  | (2) |  |  |


| (c) | $\frac{\mathrm{d} H}{\mathrm{~d} t}=\frac{8\left(1-2 t^{2}\right)}{3 \sqrt[3]{t}\left(t^{2}+1\right)^{2}}=0$ or $8-16 t^{2}=0$ at a turning point. <br> Solves $8-16 t^{2}=0$ to find $t=\frac{1}{\sqrt{2}}$ <br> Can also state $t \neq-\frac{1}{\sqrt{2}}$ | M1 ft <br> A1 ft | 1.1b | 6th <br> Differentiate using the product rule. |
| :---: | :---: | :---: | :---: | :---: |
|  |  | (2) |  |  |
| (8 marks) |  |  |  |  |
| Notes <br> (b) Award ft marks for a correct answer using an incorrect answer from part a. <br> B1: Can also state $\frac{\mathrm{d} H}{\mathrm{~d} t}<0$ as the numerator of $\frac{\mathrm{d} H}{\mathrm{~d} t}$ is negative and the denominator is positive. Award ft marks for a correct answer using an incorrect answer from part a. |  |  |  |  |


| 9 | Scheme | Marks | AOs | Pearson <br> Progression Step and Progress descriptor |
| :---: | :---: | :---: | :---: | :---: |
| (a) | Recognises the need to write $\tan ^{4} x \equiv \tan ^{2} x \tan ^{2} x$ | M1 | 2.2a | 6th <br> Integrate using trigonometric identities. |
|  | Recognises the need to write $\tan ^{2} x \tan ^{2} x \equiv\left(\sec ^{2} x-1\right) \tan ^{2} x$ | M1 | 2.2a |  |
|  | Multiplies out the bracket and makes a further substitution $\begin{aligned} & \left(\sec ^{2} x-1\right) \tan ^{2} x \\ & \equiv \sec ^{2} x \tan ^{2} x-\tan ^{2} x \\ & \equiv \sec ^{2} x \tan ^{2} x-\left(\sec ^{2} x-1\right) \end{aligned}$ | M1 | 2.2a |  |
|  | States the fully correct final answer $\sec ^{2} x \tan ^{2} x+1-\sec ^{2} x$ | A1 | 1.1b |  |
|  |  | (4) |  |  |
| (b) | States or implies that $\int \sec ^{2} x \mathrm{~d} x=\tan x$ | M1 | 1.1b | 6th <br> Integrate using the reverse chain rule. |
|  | States fully correct integral $\int \tan ^{4} x \mathrm{~d} x=\frac{1}{3} \tan ^{3} x+x-\tan x+C$ | M1 | 2.2a |  |
|  | Makes an attempt to substitute the limits. For example, $\left[\frac{1}{3} \tan ^{3} x+x-\tan x\right]_{0}^{\frac{\pi}{4}}=\left(\frac{1}{3}\left(\tan \frac{\pi}{4}\right)^{3}+\frac{\pi}{4}-\tan \frac{\pi}{4}\right)-(0) \text { is seen. }$ | M1 ft | 1.1b |  |
|  | Begins to simplify the expression $\frac{1}{3}+\frac{\pi}{4}-1$ | M1 ft | 1.1b |  |
|  | States the correct final answer $\frac{3 \pi-8}{12}$ | A1 ft | 1.1b |  |
|  |  | (5) |  |  |
| (9 marks) |  |  |  |  |
| Notes <br> (b) Student does not need to state ' $+C$ ' to be awarded the second method mark. <br> (b) Award ft marks for a correct answer using an incorrect initial answer. |  |  |  |  |


| 10 | Scheme | Marks | AOs | Pearson Progression Step and Progress descriptor |
| :---: | :---: | :---: | :---: | :---: |
|  | Begins the proof by assuming the opposite is true. <br> 'Assumption: given a rational number $a$ and an irrational number $b$, assume that $a-b$ is rational.' | B1 | 3.1 | 7th <br> Complete proofs using proof by contradiction. |
|  | Sets up the proof by defining the different rational and irrational numbers. The choice of variables does not matter. <br> Let $a=\frac{m}{n}$ <br> As we are assuming $a-b$ is rational, let $a-b=\frac{p}{q}$ <br> So $a-b=\frac{p}{q} \Rightarrow \frac{m}{n}-b=\frac{p}{q}$ | M1 | 2.2a |  |
|  | Solves $\frac{m}{n}-b=\frac{p}{q}$ to make $b$ the subject and rewrites the resulting expression as a single fraction: $\frac{m}{n}-b=\frac{p}{q} \Rightarrow b=\frac{m}{n}-\frac{p}{q}=\frac{m q-p n}{n q}$ | M1 | 1.1b |  |
|  | Makes a valid conclusion. <br> $b=\frac{m q-p n}{n q}$, which is rational, contradicts the assumption $b$ is an irrational number. Therefore the difference of a rational number and an irrational number is irrational. | B1 | 2.4 |  |
|  |  |  |  | (4 marks) |
| Notes |  |  |  |  |


| 11 | Scheme |  | Marks | AOs | Pearson <br> Progression Step and Progress descriptor |
| :---: | :---: | :---: | :---: | :---: | :---: |
| (a) | Figure 1 | Graph has a distinct V-shape. | M1 | 2.2a | 5th <br> Sketch the graph of the modulus function of a linear function. |
|  |  | Labels vertex $\left(-\frac{3}{2},-4\right)$ | A1 | 2.2a |  |
|  |  | Finds intercept with the $y$-axis. | M1 | 1.1b |  |
|  |  | Makes attempt to find $x$-intercept, for example states that $\|2 x+3\|-4=0$ | M1 | 2.2a |  |
|  |  | Successfully finds both $x$-intercepts. | A1 | 1.1b |  |
|  |  |  | (5) |  |  |
| (b) | Recognises that there are two solutions. For example, writing$2 x+3=-\frac{1}{4} x+2 \text { and }-(2 x+3)=-\frac{1}{4} x+2$ |  | M1 | 2.2a | 5th <br> Solve equations involving the modulus function. |
|  | Makes an attempt to solve both questions for $x$, by manipulating the algebra. |  | M1 | 1.1b |  |
|  | Correctly states $x=-\frac{4}{9}$ or $x=-\frac{20}{7}$. Must state both answers. |  | A1 | 1.1b |  |
|  | Makes an attempt to substitute to find $y$. |  | M1 | 1.1b |  |
|  | Correctly finds $y$ and states both sets of coordinates correctly$\left(-\frac{4}{9},-\frac{17}{9}\right) \text { and }\left(-\frac{20}{7},-\frac{9}{7}\right)$ |  | A1 | 1.1b |  |
|  |  |  | (5) |  |  |
|  |  |  |  |  | (10 marks) |
| Notes |  |  |  |  |  |


| 12 | Scheme | Marks | AOs | Pearson <br> Progression Step and Progress descriptor |
| :---: | :---: | :---: | :---: | :---: |
| (a) | $\text { Writes } \begin{aligned} (\sin 3 \theta+\cos 3 \theta)^{2} & \equiv(\sin 3 \theta+\cos 3 \theta)(\sin 3 \theta+\cos 3 \theta) \\ & \equiv \sin ^{2} 3 \theta+2 \sin 3 \theta \cos 3 \theta+\cos ^{2} 3 \theta \end{aligned}$ | M1 | 1.1b | 7th <br> Use addition formulae and/or double-angle formulae to solve equations. |
|  | Uses $\sin ^{2} 3 \theta+\cos ^{2} 3 \theta \equiv 1$ and $2 \sin 3 \theta \cos 3 \theta \equiv \sin 6 \theta$ to write: $(\sin 3 \theta+\cos 3 \theta)^{2} \equiv 1+\sin 6 \theta$ <br> Award one mark for each correct use of a trigonometric identity. | A2 | 2.2a |  |
|  |  | (3) |  |  |
| (b) | States that: $1+\sin 6 \theta=\frac{2+\sqrt{2}}{2}$ | B1 | 2.2a | 7th <br> Use addition formulae and/or double-angle formulae to solve equations. |
|  | Simplifies this to write: $\sin 6 \theta=\frac{\sqrt{2}}{2}$ | M1 | 1.1b |  |
|  | Correctly finds $6 \theta=\frac{\pi}{4}, \frac{3 \pi}{4}, \frac{9 \pi}{4}, \frac{11 \pi}{4}$ <br> Additional answers might be seen, but not necessary in order to award the mark. | M1 | 1.1b |  |
|  | States $\theta=\frac{\pi}{24}, \frac{3 \pi}{24}$ <br> Note that $\theta \neq \frac{9 \pi}{24}, \frac{11 \pi}{24}$. For these values $3 \theta$ lies in the third quadrant, therefore $\sin 3 \theta$ and $\cos 3 \theta$ are both negative and cannot be equal to a positive surd. | A1 | 1.1b |  |
|  |  | (4) |  |  |
| (7 marks) |  |  |  |  |
| Notes |  |  |  |  |
| 6b |  |  |  |  |


| 13 | Scheme | Marks | AOs | Pearson <br> Progression Step and Progress descriptor |
| :---: | :---: | :---: | :---: | :---: |
| (a) | Correctly writes $6(2+3 x)^{-1}$ as: $6\left(2^{-1}\left(1+\frac{3}{2} x\right)^{-1}\right) \text { or } 3\left(1+\frac{3}{2} x\right)^{-1}$ | M1 | 2.2a | 6th <br> Understand the binomial theorem for rational n . |
|  | Completes the binomial expansion: $3\left(1+\frac{3}{2} x\right)^{-1}=3\left(1+(-1)\left(\frac{3}{2}\right) x+\frac{(-1)(-2)\left(\frac{3}{2}\right)^{2} x^{2}}{2}+\ldots\right)$ | M1 | 2.2a |  |
|  | Simplifies to obtain $3-\frac{9}{2} x+\frac{27}{4} x^{2}+\ldots$ | A1 | 1.1b |  |
|  | Correctly writes $4(3-5 x)^{-1}$ as: $4\left(3^{-1}\left(1-\frac{5}{3} x\right)^{-1}\right) \text { or } \frac{4}{3}\left(1-\frac{5}{3} x\right)^{-1}$ | M1 | 2.2a |  |
|  | Completes the binomial expansion: $\frac{4}{3}\left(1-\frac{5}{3} x\right)^{-1}=\frac{4}{3}\left(1+(-1)\left(-\frac{5}{3}\right) x+\frac{(-1)(-2)\left(-\frac{5}{3}\right)^{2} x^{2}}{2}+\ldots\right)$ | M1 | 2.2a |  |
|  | Simplifies to obtain $\frac{4}{3}+\frac{20}{9} x+\frac{100}{27} x^{2}+\ldots$ | A1 | 1.1b |  |
|  | Simplifies by subtracting to obtain $\frac{5}{3}-\frac{121}{18} x+\frac{329}{108} x^{2}+\ldots$ <br> Reference to the need to subtract, or the subtracting shown, must be seen in order to award the mark. | A1 | 1.1b |  |
|  |  | (7) |  |  |


| (b) | Makes an attempt to substitute $x=0.01$ into $\mathrm{f}(x)$. <br> For example, $\frac{6}{2+3(0.01)}-\frac{4}{3-5(0.01)}$ is seen. | M1 | 1.1 b | 6th <br> Understand the binomial theorem for rational n . |
| :---: | :---: | :---: | :---: | :---: |
|  | States the answer 1.5997328 | A1 | 1.1b |  |
|  |  | (2) |  |  |
| (c) | Makes an attempt to substitute $x=0.01$ into $\frac{5}{3}-\frac{121}{18} x-\frac{329}{108} x^{2}+\ldots$ <br> For example $\frac{5}{3}-\frac{121}{18}(0.01)+\frac{329}{108}(0.01)^{2}+\ldots$ is seen. | M1 ft | 1.1 b | 6th <br> Understand the binomial theorem for rational n . |
|  | States the answer 1.59974907... Accept awrt 1.60. | M1 ft | 1.16 |  |
|  | Finds the percentage error: $0.0010 \%$ | A1 ft | 1.16 |  |
|  |  | (3) |  |  |
| (12 marks) |  |  |  |  |
| Notes <br> (a) If one expansion is correct and one is incorrect, or both are incorrect, award the final accuracy mark if they are subtracted correctly. <br> (c) Award all 3 marks for a correct answer using their incorrect answer from part (a). |  |  |  |  |


| 14 | Scheme | Marks | AOs | Pearson <br> Progression Step and Progress descriptor |
| :---: | :---: | :---: | :---: | :---: |
| (a) | Uses $a_{n}=a+(n-1) d$ substituting $a=5$ and $d=3$ to get $a_{n}=5+(n-1) 3$ | M1 | 3.1b | 5th <br> Use arithmetic sequences and series in context. |
|  | Simplifies to state $a_{n}=3 n+2$ | A1 | 1.1b |  |
|  |  | (2) |  |  |
| (b) | Use the sum of an arithmetic series to state $\frac{k}{2}[10+(k-1) 3]=948$ | M1 | 3.1b | 5th <br> Use arithmetic sequences and series in context. |
|  | States correct final answer $3 k^{2}+7 k-1896=0$ | A1 | 1.1b |  |
|  |  | (2) |  |  |
|  |  |  |  | (4 marks) |
| Notes |  |  |  |  |


| 15 | Scheme | Marks | AOs | Pearson <br> Progression Step and Progress descriptor |
| :---: | :---: | :---: | :---: | :---: |
|  | Understands that integration is required to solve the problem. <br> For example, writes $\int_{\frac{\pi}{2}}^{\pi}\left(x \sin ^{2} x\right) \mathrm{d} x$ | M1 | 3.1a | 6th <br> Use definite integration to find areas between curves. |
|  | Uses the trigonometric identity $\cos 2 x \equiv 1-2 \sin ^{2} x$ to rewrite $\int_{\frac{\pi}{2}}^{\pi} x \sin ^{2} x \mathrm{~d} x$ as $\int_{\frac{\pi}{2}}^{\pi}\left(\frac{1}{2} x-\frac{1}{2} x \cos 2 x\right) \mathrm{d} x$ o.e. | M1 | 2.2a |  |
|  | Shows $\int_{\frac{\pi}{2}}^{\pi} \frac{1}{2} x \mathrm{~d} x=\left[\frac{1}{4} x^{2}\right]_{\frac{\pi}{2}}^{\pi}$ | A1 | 1.1b |  |
|  | Demonstrates an understanding of the need to find $\int_{\frac{\pi}{2}}^{\pi} \frac{1}{2} x \cos 2 x \mathrm{~d} x$ using integration by parts. For example, $u=x, \frac{\mathrm{~d} u}{\mathrm{~d} x}=1$ $\frac{\mathrm{d} v}{\mathrm{~d} x}=\cos 2 x, v=\frac{1}{2} \sin 2 x$ o.e. is seen. | M1 | 2.2a |  |
|  | States fully correct integral $\int_{\frac{\pi}{2}}^{\pi}\left(\frac{1}{2} x-\frac{1}{2} x \cos 2 x\right) \mathrm{d} x=\left[\frac{1}{4} x^{2}-\frac{1}{4} x \sin 2 x-\frac{1}{8} \cos 2 x\right]_{\frac{\pi}{2}}^{\pi}$ | A1 | 1.1b |  |
|  | Makes an attempt to substitute the limits $\left(\frac{\pi^{2}}{4}-\frac{1}{4}(0)-\frac{1}{8}(1)\right)-\left(\frac{\pi^{2}}{16}-\frac{1}{4}(0)-\frac{1}{8}(-1)\right)$ | M1 | 2.2a |  |
|  | States fully correct answer: either $\frac{3 \pi^{2}}{16}-\frac{1}{4}$ or $\frac{3 \pi^{2}-4}{16}$ o.e. | A1 | 1.1b |  |
|  |  |  |  |  |
| Notes <br> Integration shown without the limits is acceptable for earlier method and accuracy marks. Must correctly substitute limits at step 6 |  |  |  |  |
|  |  |  |  |  |  |

