Name	Period	Date _	



# **Two Lines and a Transversal**

(Warm Up)



Directions: Correctly place an angle number in the correct box. Angle numbers may repeat.

Name	Angles	Transversal <i>p</i> intersects lines <i>q</i> and <i>r</i>
Exterior Angles		
Interior Angles		q $1/2$
Consecutive Interior Angles		4 3
Alternate Exterior Angles		$r \frac{5}{6}$
Alternate Interior Angles		
Corresponding Angles		

Name	Period	Date
Parallel Lines         (Guided P         Directions : Read the column on the lefigure on the right in your p         Complete the conjecture a	By Copyi ractice Constru ft and use your portfolio. t the bottom of	ng an Angle uction) r geometric tools to construct the the page.
1. Use a straight edge to draw $\overrightarrow{MN}$ .	Draw	
point <i>P</i> that is not on $\overrightarrow{MN}$ . Draw $\overrightarrow{PN}$	$\vec{A}$	
		MN
2. Copy $\angle PMN$ (Please refer to notebook on how to copy an angle.) s is the vertex of the new angle. Label t intersection points Q and R.	o your o that P he	P Q Q M N
3. Draw $\overrightarrow{PQ}$		P Q Q
$\angle PMN$ is congruent to $\angle RPQ$ by construction.		M
Conjecture: If corresponding angle transversal, then the lines are	es are congruer	nt when two lines are cut by a



Directions: Using only a compass and straight edge complete the following constructions.

1. Construct a line parallel to line k that passes through point W.



2. Construct a line parallel to line j that passes through point P.



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3. Construct two parallel lines and a traversal such that the corresponding angles are congruent to the angle below:



4. Construct two parallel lines and a traversal such that one pair of alternate interior angles are congruent to the angle below:



5. Construct a line that contains point Q parallel to line *I* such that point Q is exactly apart.

Name:

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Angle Identity (Warm Up)



Line *m* is parallel to line *n* and line *t* is the transversal. Answer the following questions using the diagram to the right.

- a) Name all pairs of alternate interior angles.
- b) Name all pairs of corresponding angles.
- c) Name all pairs of alternate exterior angles.
- d) Name all linear pairs angles.
- e) Name all vertical angles.
- f) Name all consecutive interior angles.





1. Construct a line that is parallel to line k and passes through



2. Construct a line that is parallel to line *n* and passes through point R.



Ν	а	m	۱e	,
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 Construct and label two parallel lines and a traversal such that the distance between the parallel lines is exactly



Date



City Project (High Level Task)



- Overview: City planners and designers must be able to accurately draw parallel and perpendicular lines to create a city map.
- Objective: Draw a city map using only a compass and straightedge that meets conditions below.
- Materials: Poster or blank paper, colored pencils, eraser, compass and straightedge.
- Directions: Assume no two buildings can occupy the same space. Make your constructions lines light so that they can be easily be erased. Draw a city with the following conditions:
  - 1. Use a straight edge to draw and label a street across your paper.
  - 2. Draw and label a street that intersects the previous street drawn.
  - 3. Construct and label three streets that are parallel to one of the streets you just drew.
  - 4. Construct at least two transversal streets that are perpendicular to the parallel streets.
  - 5. Sketch a house and a school on a pair of consecutive interior angles.
  - 6. Sketch a bank and a post office on a pair of corresponding angles.
  - 7. Sketch a grocery store and an electronic store on a pair of alternate interior angles.
  - 8. Sketch a movie theater and a pet store on a pair of alternate exterior angles.
  - 9. Sketch a water tower halfway between the bank and the post office.
  - 10. Sketch a park exactly halfway between the grocery store and the school.
  - 11. Sketch traffic lights on at least four intersections.

Names:			_ Task: Teach	er (/16	=%)
Clear	Asse	essing	the High (Rubric)	n Level	Task
	4	3	2	1	Points
Mathematical Language • •	Appropriate language <b>ALWAYS</b> selected and used properly	Appropriate language selected and used properly MOST OF THE TIME	Appropriate language <b>SOMETIMES</b> selected and used properly	Appropriate language SELDOM OR NEVER selected and used properly	Student Score Teacher Score
<ul> <li>Problem Solving Strategies</li> <li>Used constructions</li> <li>Construction lines are neatly erased.</li> <li>Followed directions</li> <li>Used color</li> <li>Labeled diagrams</li> </ul>	Appropriate strategy or strategies <b>ALWAYS</b> selected and used properly	Appropriate strategy or strategies selected and used properly MOST OF THE TIME	Appropriate strategy or strategies <b>SOMETIMES</b> selected and used properly	Appropriate strategy or strategies <b>SELDOM</b> <b>OR NEVER</b> selected and used properly	Student Score Teacher Score
<ul> <li>Mathematical Reasoning</li> <li>Used logical reasoning</li> <li>Utilized sound algebraic and/or mathematical steps and procedures</li> </ul>	Logical reasoning <b>ALWAYS</b> used to obtain reasonable and correct solutions	Logical reasoning used to obtain reasonable and correct solutions <b>MOST OF</b> <b>THE TIME</b>	Logical reasoning <b>SOMETIMES</b> used to obtain reasonable and correct solutions	Logical reasoning <b>SELDOM</b> <b>OR NEVER</b> used to obtain reasonable and correct solutions	Student Score Teacher Score
Communication <ul> <li>Discussed with group</li> <li>Presented to class</li> <li>Wrote neatly and legibly</li> <li>Easily understood by peers</li> </ul>	Ideas ALWAYS communi- cated clearly and effectively	Ideas communi- cated clearly and effectively <b>MOST OF</b> <b>THE TIME</b>	Ideas SOMETIMES communi- cated clearly and effectively	Ideas SELDOM OR NEVER communi- cated clearly and effectively	Student Score Teacher Score



Directions: Use your conjectures about parallel lines and analyze each figure.

6. First Ave. and Main St. are parallel lines. Explain what is wrong with this picture?



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7. 9<sup>th</sup> St. and 10<sup>th</sup> St. are parallel lines. Explain what is wrong with this picture?



Directions: Use the figure below. Lines X and Y are parallel. Lines L and M are parallel.



Name	Period	Date_
(C)	What's My Measure (Warm-Up)	SA:P

If line A and B are parallel, find the measures of the numbered angles in the figures below.



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NSpiring Parallels (Guided Practice)



- Draw a line in the box below using a straight edge and label points A and B.
- Create a line parallel to the first line using a straight edge and compass.
- > Draw a transversal using a straight edge and label all the points the same as the teacher.
- Use a protractor to measure angle FGD.
- > Use a protractor to measure angle GHB and form a conjecture about what you observe. Make sure you use the correct name for the angle pair.
- > Measure the rest of the angles on your paper and record the answers.
- > Form conjectures for alternate interior, alternate exterior and consecutive interior angles.



then write the special angle names.

∠1&∠3,	∠6&∠7,	∠4&∠8,	∠7&∠8,
∠5&∠7,	∠2&∠3,	∠2&∠6,	∠1&∠7,
∠3&∠7,	∠6&∠8,	∠1&∠5,	∠3&∠5

Congruent	Supplementary	Name of special angles

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We have learned that when two lines are cut by a transversal, special pairs of angles are formed. Practice identifying these special pairs of angles and look for any relationships among the pairs of angles formed.

1. According to the diagram, lines *a* and *b* are parallel and cut by transversal line *c*.

- a. Identify all pairs of corresponding angles.
- b. Identify all pairs of alternate interior angles.
- c. Identify all pairs of alternate exterior angles.



d. Identify all pairs of consecutive interior angles.

Name Date Period Date	Name	Period	Date
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2. According to the diagram, lines *s* and *t* are parallel and cut by transversal line *r*.

a. Identify all pairs of corresponding angles.

b. Identify all pairs of alternate interior angles.

c. Identify all pairs of alternate exterior angles.



d. Identify all pairs of consecutive interior angles.

- 3. Considering both problems, what have you observed?
- 4. Can we make some generalizations?

Therefore a conjecture can be:

5. If two parallel lines are cut by a transversal, then: corresponding angles

are \_\_\_\_\_, alternate interior angles are

\_\_\_\_\_, alternate exterior angles are \_\_\_\_\_,

consecutive interior angles are \_\_\_\_\_.

Name	Period	Date

### Extension: TI Nspiring Calculator

Now use your handheld calculations to create the diagram on the right. Measure any one angle with the commands on the calculator.

6. Choose any one angle to measure.  $m \angle \underline{\phantom{a}} = \underline{\phantom{a}}$ 

Based on that one measurement, calculate the remaining seven measures.

m∠1 =	m∠5 =
m∠2 =	m∠6 =
m∠3 =	m∠7 =
m∠4 =	m∠8 =



7. Are lines f and g parallel? \_\_\_\_\_

How do you know?

Be specific.





Find the measure of the other angles.

m 
$$\angle$$
 GFD =

m  $\angle$  HFE =

m 
$$\angle$$
 FDE =

m 
$$\angle$$
 DEF =



1. What is the special angle relationship between  $\angle$  AED and  $\angle$  CFG?

#### Solve for x.

m ∠ AED = m ∠\_\_\_\_\_

=	
=	
=	
=	
=	
X =	

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Name		Period	Date
3. Find the m	$\scriptstyle \angle$ AED using the va	lue of x.	
m ∠ AED = 1	8x - 14		
= _ = _ = _			
m ∠AED =		N	К
4. Find x so	that JK ∥ MN	-	T S U (9x - 5) (7x+ 3) J
m ∠ HSJ = r	n∠ STM		М
Solve fo	or x.		
<u>7x + 3</u>	= _ <u>9x - 5</u>	V — re a	Vhat is the special angle elationship between ∠HSJ nd ∠STM?
	=		
	=		
	=		
	=		
What is the m	heasure of $\angle$ HSJ?		
What is the m	easure of ∠KSH?		

Na	ame	Period	Date	
5.	Find x and the measure of $\angle I$ $I \parallel m$ . What is the relationship betw $\angle F$ and $\angle K$ .	F so that /een	K	m
	Solve for x.		(7x + 0	3)
<b>X</b> :	=			
Th	ne measure of ∠ F is	·	t	1
6.	Find x so that $s \parallel t$ .		(3)	( + 5) H
	What is the relationship betw ∠A and ∠H.	/een	(2x) A	
	Solve for x.			
<b>X</b> :	=	·		
Th Th	ne measure of ∠A is ne measure of ∠H is	 		

Name	Period	_ Date
	Mix and Match (Independent Practice)	
If there are <u>corresponding</u> <u>angles</u> , then $m \ge 1 = (9X - 4)^{\circ}$ and $m \ge 2 = (31X + 16)^{\circ}$ . Find the value of X and the measure of the angles.	If there are <u>vertical angles</u> , then $m \angle 1 = (3x - 5)^\circ$ and $m \angle 2$ = $(2x + 35)^\circ$ . Find the value of x and the measure of the angles.	If there are <u>alternate</u> <u>exterior angles</u> , then $m \angle 1 = 57^{\circ}$ and $m \angle 2 =$ $(\frac{1}{2}x + 35)^{\circ}$ . Find the value of x and the measure of the angles.
If there are <u>consecutive</u> <u>interior angles</u> , then $m \ge 1 = 45^{\circ}$ and $m \ge 2 = (25x + 10)^{\circ}$ . Find the value of x and the measure of the angles.	If there are <u>alternate interior</u> angles, then $m \ge 1 = 92^{\circ}$ and $m \ge 2 = (4x - 8)^{\circ}$ . Find the value of x and the measure of the angles.	If there are <u>linear pairs</u> , then $m \angle 1 =$ $(2x + 15)^{\circ}$ and $m \angle 2 =$ $135^{\circ}$ . Find the value of x and the measure of the angles.





Name\_\_\_\_\_Period \_\_\_\_ Date \_\_\_\_\_

# Mix and Match Answer Template

(Independent Practice)

Parallel lines diagrams	Names of the special angles	Value of x and the angles' measurements

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Parallel lines diagrams	Names of the special angles	Value of x and the angles' measurements

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If  $m \ge 2 = 25y - 20$  and  $m \ge 7 = 13y + 4$ , find the value for y and the measure of the indicated angles.

- 1. The value of y =\_\_\_\_\_
- 2. The measure of the following angles.

a) *m*∠2 = \_\_\_\_\_ c) *m*∠5 = \_\_\_\_\_

b)  $m \ge 3 =$  \_\_\_\_\_ d)  $m \ge 8 =$  \_\_\_\_\_

	Where's My Parallel? (Group Task)	
Group Members:		
Period:		

Each team member solves an equation corresponding with their assigned letter (A - E). The solution of the equation is the measure of the angle in the parallel lines figure with the corresponding letter. After each team member has solved for their angle, the whole group works together to determine which lines are parallel from the angles <u>given</u> in the figure. If the lines are parallel, justification <u>must</u> be given (Example: Line 1 is parallel to line 2 because angles A and B are congruent corresponding angles).











Equation 1A	Equation 2A	Equation 3A
-3a + 63 = -2(30 + a)	-2(63 – a) = 3(a – 88) + 29	3(a – 64) + 458 = 5a
Equation 1B	Equation 2B	Equation 3B
-2(15 – b) + 12 = 224	4b – 84 = 6(171 – b)	-5b + 462 +2b = 3(b + 64)
Equation 1C	Equation 2C	Equation 3C
4(c - 10) = 2C + 206	3(c + 64) + 39 = 5c + 9	4(64 - c) = 123 - 3c
Equation 1D	Equation 2D	Equation 3D
-3d + 838 = 5(d – 26)	4(76 - d) = -2(d - 22) + 38	6d − 3d = -2(11 − d) + 67
<b></b>		<b></b>
Equation 1E	Equation 2E	Equation 3E
3e – 189 = 174	3e – 160 = 167	4e - 302 = 230

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Equation 4A	Equation 5A	
6a – 418 = 4(a – 64) + 112	3a + 27 = 2(a + 45)	
Equation 4B	Equation 5B	
4(b – 97) + 2b = 422	201 – 3(b + 28) = -2b	
Equation 4C	Equation 5C	
86 – 4c = -2(c + 92)	-4c + 819 = -2c + 5c	
Equation 4D	Equation 5D	
-3(d + 164) + 4d = -2d - 363	3(d + 74) = 342 + 2d	
Equation 4E	Equation 5E	
-4e = -2e - 86	-2e + 78 = 3e - 522	
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