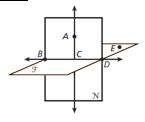
Pre-AP Geometry Fall 2015 Semester Exam REVIEW

*Chapter 1.1 Points Lines Planes

Use the figure to name each of the following:

1) three non-collinear points

(A, C, B) or (A, C, D) or any two points listed with E.



- 2) one line in three different ways \overrightarrow{BD} , \overrightarrow{DB} , \overrightarrow{BC} , \overrightarrow{CB} , \overrightarrow{CD} , or \overrightarrow{DC}
- 3) the intersection of the two planes
- 4) the intersection of the two lines

Draw and label each of the following:

5) a segment with endpoints S and T with midpoint, M



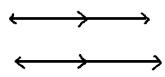
6) three coplanar lines that intersect in a common point



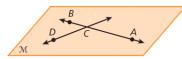
7) ray with endpoint F that passes through G



8) two lines that do not intersect



Use the figure to name each of the following:



9) a pair of opposite rays

 \overrightarrow{CB} and \overrightarrow{CA}

10) the plane in two different ways Plane *M* or *DCA* (3 non-collinear points)

*Chapter 1.2 Line Segments and Distance

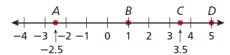
Find the length of the following:

11) Segment AB

12) Segment BC

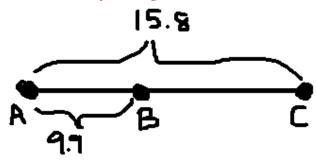
3.5

2.5



13) B is a point between points A and C, segment AC = 15.8, and segment AB = 9.9. Find the length of segment BC. (Draw a picture).

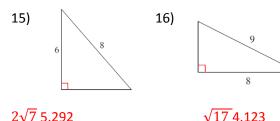
BC = 5.9 units by the Segment Addition Postulate



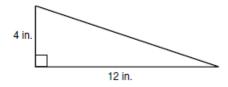
14) Find the length of segment NP.



Find the missing side for each triangle in simplest radical form AND as a decimal rounded to the nearest hundredth.

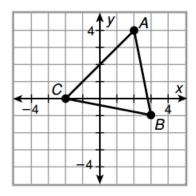


17) Determine the length of the given triangle's hypotenuse. The answer should be given both rounded to the nearest tenth and in simplest radical form.



12.649 or $4\sqrt{10}$

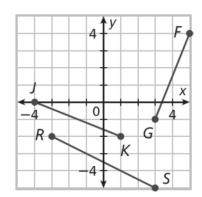
18) Find the lengths below and leave your answer in simplest radical form.



- a. Find $AB \sqrt{26}$
- b. Find $BC \sqrt{26}$
- c. Find $CA = 4\sqrt{2}$

Use the Distance formula or Pythagorean theorem to find the length of each segment. Round answers to the nearest tenth.

19) Segment JK 5.385 or $\sqrt{29}$

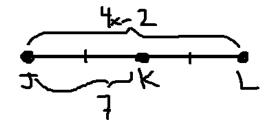


20) Segment RS 6.708 or $3\sqrt{5}$

21) Segment GF 5.385 or $\sqrt{29}$

*Chapter 1.3 Locating Points and Midpoints

22) K is the **midpoint** of segment JL, JL = 4x - 2, and JK = 7. Find x, the length of KL, and JL. x = 4



23) Y is the midpoint of \overline{XZ} . X has coordinates (2, 4), and Y has coordinates (-1, 1). Find the coordinates of Z.

$$(-4, -2)$$

24) \overline{TU} has endpoints T(5a, -1b) and U(1a, -5b). Find the midpoint.

$$(3a, -3b)$$

Find the coordinates of the <u>midpoin</u>t of each segment:

25) *AB* with endpoints *A* (4, -6) and *B* (-4, 2) (0, -2)

26) CD with endpoints C (0, -8) and D (3, 0)

(1.5, -4)

*Chapter 1.4 and 1.5 Angle Measure and Angle Relationships

27) $\angle A$ is an acute angle. $\angle O$ is an obtuse angle. $\angle R$ is a right angle. Put $\angle A$, $\angle O$, and $\angle R$ in order from least to greatest by measure.

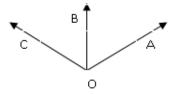
 $\angle A$, $\angle R$, and $\angle O$

28) **a.** Which point is the vertex of $\angle BCD$? *C*

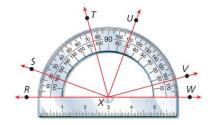
b. Which rays form the sides of $\angle BCD$? \overrightarrow{CB} and \overrightarrow{CD}

29) Correctly name all 3 angles in the diagram.

- 1. **∠***COB*
- 2. **∠***BOA*
- 3. **∠***COA*

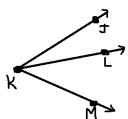


Use the protractor to find the measure of each angle. Then classify each as acute, right, or obtuse.



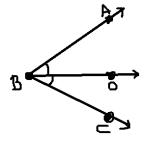
30) $\angle VXW$ 31) $\angle TXW$ 32) $\angle RXU$ 15°; acute 105°; obtuse 110°; obtuse

33) L is in the interior of \angle JKM, $m\angle$ JKL = 42°, and $m\angle$ LKM = 28°. Draw and label the diagram and use it to find $m\angle$ JKM.



70° by the Angle Addition Postulate

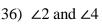
34) Ray BD bisects $\angle ABC$, $m\angle ABD = (6x + 4)^{\circ}$, and $m\angle DBC = (8x - 4)^{\circ}$. Draw and label the diagram and use it to find $m\angle ABD$.



28° by the definition of angle bisector

Tell whether the angles are only adjacent, adjacent and form a linear pair, or not adjacent.

35) ∠1 and ∠2 adjacent and Linear Pair



not adjacent

37) $\angle 1$ and $\angle 3$

not adjacent

38) $\angle 2$ and $\angle 3$

adjacent only

For Exercises 39 - 44, use the figure at the right. Name an angle or angle pair that satisfies each condition.

39) Name two acute vertical angles.

∠EKH and ∠FKG

40) Name two obtuse vertical angles.

∠HKG and ∠EKF

41) Name a linear pair.

∠FKG and ∠GKH (multiple answers here)

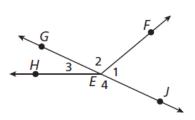
42) Name two acute adjacent angles.

∠JKG and ∠GKF

43) Name an angle complementary to ∠EKH.

∠GKI

44) Name an angle supplementary to ∠FKG. ∠GKH



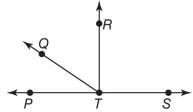
45) Find the measures of an angle and its complement if one angle measures 24 degrees more than the other.

33° and 57°

46) The measure of the supplement of an angle is 36 less than the measure of the angle. Find the measures of the angles..

108° and 72°

For Exercises 47 - 48, use the figure below.



47) If $m \angle RTS = 8x + 18$, find the value of x so that $\overline{TR} \perp \overline{TS}$ x = 13.5

48) If $m \angle PTQ = 3y - 10$ and $m \angle QTR = y$, find the value of y so that $\angle PTR$ is a right angle. y = 25

*Chapter **2.1** Inductive Reasoning

- 49) Inductive Reasoning is used to draw a conclusion from specific cases and/or patterns.
- 50) A statement you believe to be true based on Inductive Reasoning is called a ______. conjecture.
- 51) To show that a conjecture is true, you must

prove it using deductive reasoning.

- 52) To show that a conjecture is false, you can give a counterexample.
- 53) Complete each conjecture:
- **a.** A pair of complementary angles have a sum of 90 degrees.

- **b.** The square of any negative number is always positive.
- 54) Show that each conjecture is false by providing a counterexample:
- **a.** Two angles that have the same *vertex* are adjacent.

 Counterexample: vertical angles

b. If x + 1 > 5, then x = 8Counterexample: x = 5

*Chapter 2.4 Deductive Reasoning

55) Deductive Reasoning is used to draw conclusions from given facts, definitions, and theorems/properties/postulates.

*Chapter **2.6** Algebraic Proofs

State which property, postulate, definition, or theorem supports each statement below.

56) If R is in the interior of $\angle PQS$, then $m\angle PQR + m\angle RQS = m\angle PQS$. Angle Addition Postulate

57) If $\angle 1$ and $\angle 2$ are supplementary, then $m\angle 1 + m\angle 2 = 180^{\circ}$.

Definition of Supplementary Angles

58) If $m\angle 1 = m\angle 2$ and $m\angle 2 = m\angle 3$, then $m\angle 1 = m\angle 3$. Transitive Property of Equality

59) If M is the midpoint of \overline{AB} , then $\overline{AM} \cong \overline{MB}$. Definition of Midpoint

- 60) If AB = CD, then AB + EF = CD + EF. Addition Property of Equality
- 61) ∠1 and ∠2 form a linear pair, then they are supplementary.

 Linear Pair Theorem

62) If $m\angle A + m\angle B = 90$,

then $\angle A$ and $\angle B$ are complementary.

Definition of Complementary Angles

63) If \overrightarrow{BX} bisects $\angle ABC$, then m \angle ABX = m \angle XBC. Definition of Angle Bisector

64) If AM = MB, then
$$\overline{AM} \cong \overline{MB}$$
. Definition of Congruence

65) Complete the following Algebraic Proof by listing each step and providing its justification.

1.
$$-2(x+5) = -6$$

Given

2.
$$-2x - 10 = -6$$

2. Distribution

$$3. -2x = 4$$

3. Addition P.O.E.

4.
$$x = -2$$

4. Division P.O.E.

*Chapter 2.7 and 2.8 Geometric Proofs

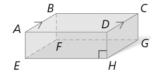
PRACTICE ANY AND ALL PROOFS!!

Places to find proofs on Wroblewski's Website:

- *Writing Algebraic Proofs and Proof Practice 09/29
- *Geometric Proof Notes and Practice 10/01
- *Test Review for Test 2 10/15
- *Test 2

*Chapter **3.1** Parallel Lines and Transversals

Identify each of the following using the figure:



66) a pair of perpendicular segments

 \overline{DH} and \overline{EH} (answers will vary)

67) a pair of skew segments

 \overline{AB} and \overline{EH} (answers will vary)

68) a pair of parallel segments

 \overline{AB} and \overline{DC} (answers will vary)

69) a pair of parallel planes

ABCD and EFGH (answers will vary)

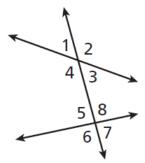
Write <u>all</u> possible answers for each of the following:

70) alternate interior angles

 $\angle 3$ and $\angle 5$; $\angle 4$ and $\angle 8$

71) alternate exterior angles

 $\angle 1$ and $\angle 7$; $\angle 2$ and $\angle 6$



72) corresponding angles

 $\angle 1$ and $\angle 5$; $\angle 2$ and $\angle 8$

 $\angle 4$ and $\angle 6$; $\angle 3$ and $\angle 7$

73) same-side interior angles

 $\angle 4$ and $\angle 5$; $\angle 3$ and $\angle 8$

Identify the type of angle pair given:

(corresponding, alternate interior, alternate exterior, same side interior)

74) ∠6 and ∠8 alternate exterior angles

75) $\angle 2$ and $\angle 3$ same side interior angles

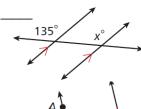
 $\begin{array}{c|c}
 & 6 & 2 \\
 & 1 \angle 3 & \\
 & \text{nterior} & \end{array}$

76) ∠2 and ∠4
alternate interior angles
77) ∠5 and ∠4

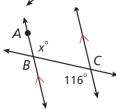
corresponding angles

*Chapter 3.2 Angles and Parallel Lines

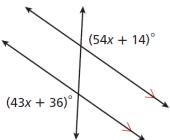
78) x = ___135 degrees_



79) x = __116 degrees __

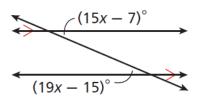


80) Solve for x and find the missing angle:



x = 2, $m \angle = 122$ by the Alternate Exterior Angles Theorem

81) Solve for x and find the missing angle:



x = 2, $m\angle = 23$ by the Alternate Interior Angles Theorem

Use the figure to find the value of all the missing angles:

83)
$$\angle 2 = 60$$

84)
$$\angle 3 = 60$$

85)
$$\angle 4 = 120$$

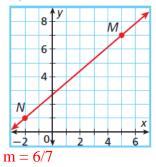
86)
$$\angle 5 = 60$$

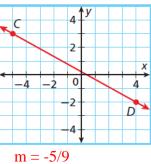
87)
$$\angle 6 = 60$$

88)
$$\angle 7 = 120$$

*Chapter **3.3** Slopes of Lines

89) Find the slope of each given line. Say if it is positive, negative, zero or undefined.





Determine if the lines are parallel, perpendicular or neither by comparing their slopes.

*Chapter 3.4 Equations of Lines

Sketch and write the equation of the line that: 92) passes through (4, 7) and (-2, 1) in <u>slope-intercept</u> form.

$$y = x + 3$$

93) passes through (-4, 2) with slope ³/₄ in <u>point-slope</u> form.

$$y - 2 = 3/4 (x + 4)$$

For problems 94-96, determine whether the lines are parallel, intersect, or coincide.

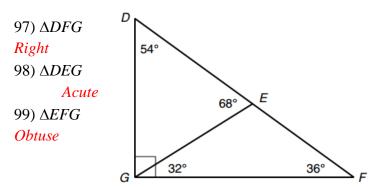
94)
$$y = -3x + 4$$
 and $y = -3x + 1$

95)
$$6x - 12y = -24$$
 and $3y = 2x + 18$
Intersect

96)
$$4x + 2y = 10$$
 and $y = -2x + 15$ Parallel

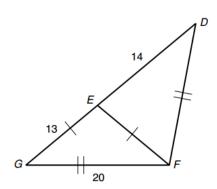
*Chapter 4.1 Classifying Triangles

For problems 97-99, classify each triangle based upon its angle measures:



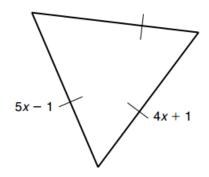
For problems 101-103, classify each triangle based upon its side lengths:

100) ΔEGF Isosceles 101) ΔDEF Scalene 102) ΔDFG Isosceles



103) Find the side lengths of each triangle:

a.

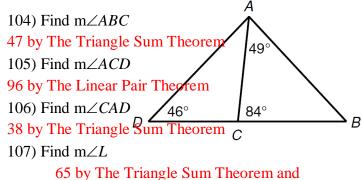


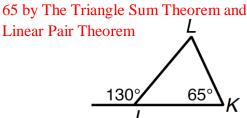
9, 9, and 9 units

b. 2x+2 x+6

7, 7, and 4 units

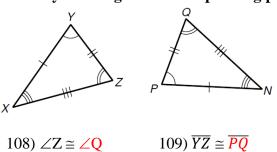
*Chapter **4.2** Angle Relationships in Triangles





*Chapter **4.3** Congruent Triangles

Identify the congruent corresponding parts:



110)
$$\angle P \cong \angle Y$$

111)
$$\angle X \cong \angle N$$

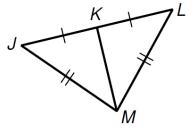
112)
$$\overline{NQ} \cong \overline{XZ}$$

113)
$$\overline{PN} \cong \overline{YX}$$

*Chapter 4.4-4.5 SSS, SAS, ASA, AAS

114) Explain why the two triangles are congruent.

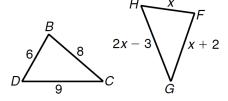
SSS



115) Show that the triangles are congruent when

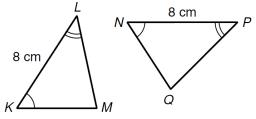
$$x = 6$$

SSS

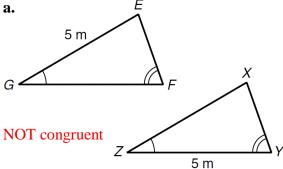


116) Use SSS, ASA, or AAS to determine if the triangles are congruent.

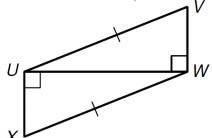
ASA



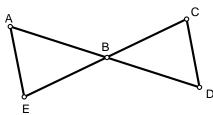
117) Determine if the triangles are congruent based upon the information given. Justify your answer.



b. cannot be determined, SSA

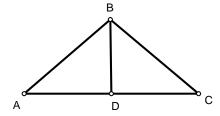


118) Given: $\overline{AE} \parallel \overline{CD}$ and $\overline{AE} \cong \overline{DC}$ Prove: $\Delta AEB \cong \Delta DCB$



We are given $\overline{AE} \parallel \overline{CD}$ and $\overline{AE} \cong \overline{DC}$. Since $\overline{AE} \parallel \overline{CD}$, then $\angle A \cong \angle D$ because they are alternate interior angles. We can also show that $\angle E \cong \angle C$ because they are alternate interior angles. Therefore, $\triangle AEB \cong \triangle DCB$ by ASA.

119) Given: \overline{BD} bisects $\angle ABC$ and $\overline{AB} \cong \overline{BC}$ Prove: $\triangle ABD \cong \triangle CBD$

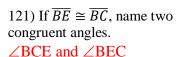


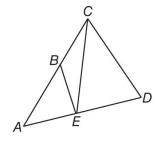
We are given \overline{BD} bisects $\angle ABC$ and $\overline{AB} \cong \overline{BC}$. Since \overline{BD} bisects $\angle ABC$, then we know $\angle ABD \cong \angle CBD$. Finally, the two triangles share side \overline{BD} . Therefore, $\triangle ABD \cong \triangle CBD$ by SAS.

*Chapter **4.6** Isosceles and Equilateral Triangles

For problem 120-123, refer to the figure below.

120) If $\overline{AC} \cong \overline{AD}$, name two congruent angles. $\angle ACD$ and $\angle ADC$



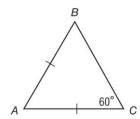


122) If $\angle EBA \cong \angle EAB$, name two congruent segments. $\overline{EA} \cong \overline{EB}$

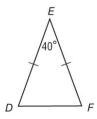
123) If $\angle CED \cong \angle CDE$, name two congruent segments. $\overline{CE} \cong \overline{CD}$

Find each measure.

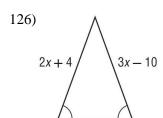
124)
$$m \angle ABC = 60^{\circ}$$

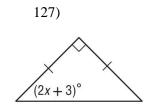






Find the value of each variable.





$$x = 14$$

x = 21