

9.2

Solving Quadratic Equations by Graphing

For use with Exploration 9.2

Essential Question How can you use a graph to solve a quadratic equation in one variable?

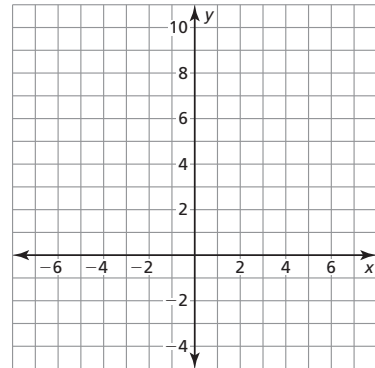
1 EXPLORATION: Solving a Quadratic Equation by Graphing

Go to *BigIdeasMath.com* for an interactive tool to investigate this exploration.

Work with a partner.

a. Sketch the graph of $y = x^2 - 2x$.

b. What is the definition of an x -intercept of a graph? How many x -intercepts does this graph have? What are they?



c. What is the definition of a solution of an equation in x ? How many solutions does the equation $x^2 - 2x = 0$ have? What are they?

d. Explain how you can verify the solutions you found in part (c).

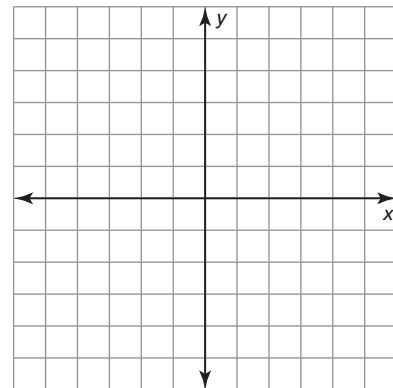
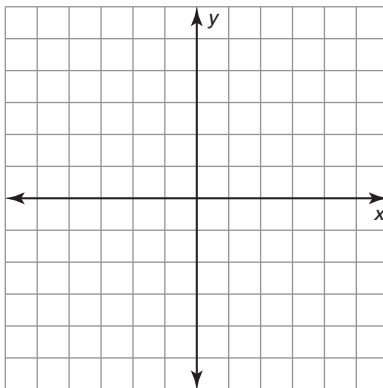
2 EXPLORATION: Solving Quadratic Equations by Graphing

Go to *BigIdeasMath.com* for an interactive tool to investigate this exploration.

Work with a partner. Solve each equation by graphing.

a. $x^2 - 4 = 0$

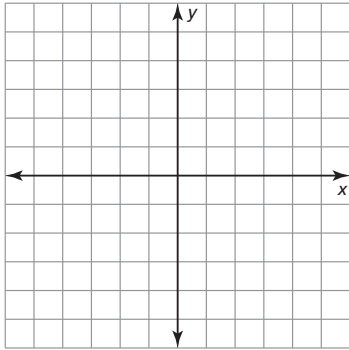
b. $x^2 + 3x = 0$



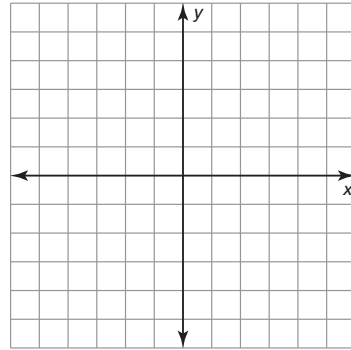
9.2 Solving Quadratic Equations by Graphing (continued)

2 EXPLORATION: Solving Quadratic Equations by Graphing (continued)

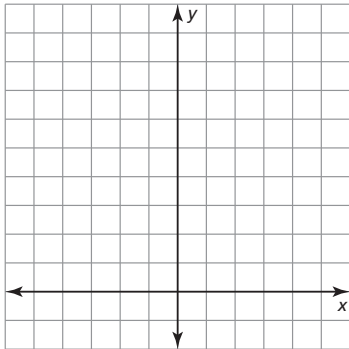
c. $-x^2 + 2x = 0$



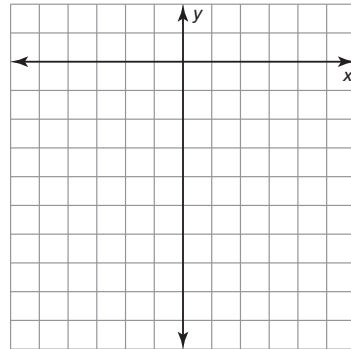
d. $x^2 - 2x + 1 = 0$



e. $x^2 - 3x + 5 = 0$



f. $-x^2 + 3x - 6 = 0$



Communicate Your Answer

3. How can you use a graph to solve a quadratic equation in one variable?

4. After you find a solution graphically, how can you check your result algebraically?
Check your solutions for parts (a)–(d) in Exploration 2 algebraically.

5. How can you determine graphically that a quadratic equation has no solution?

9.2**Notetaking with Vocabulary**

For use after Lesson 9.2

In your own words, write the meaning of each vocabulary term.

quadratic equation

Core Concepts**Solving Quadratic Equations by Graphing**

Step 1 Write the equation in standard form, $ax^2 + bx + c = 0$.

Step 2 Graph the related function $y = ax^2 + bx + c$.

Step 3 Find the x -intercepts, if any.

The solutions, or *roots*, of $ax^2 + bx + c = 0$ are the x -intercepts of the graph.

Notes:

Number of Solutions of a Quadratic Equation

A quadratic equation has:

- two real solutions when the graph of its related function has two x -intercepts.
- one real solution when the graph of its related function has one x -intercept.
- no real solutions when the graph of its related function has no x -intercepts.

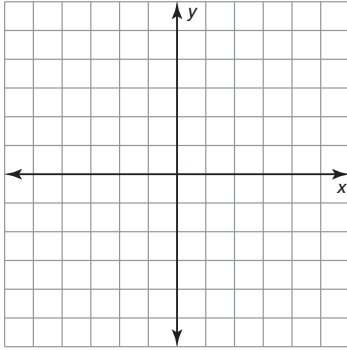
Notes:

9.2 Notetaking with Vocabulary (continued)

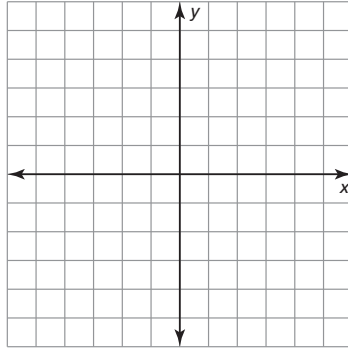
Extra Practice

In Exercises 1–9, solve the equation by graphing.

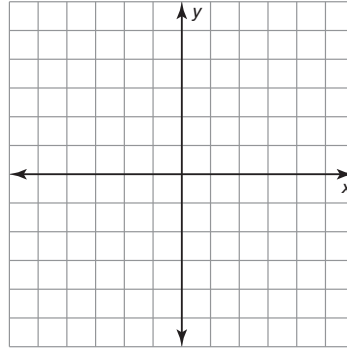
1. $x^2 + 4x = 0$



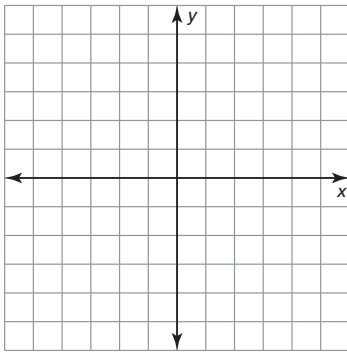
2. $-x^2 = -2x + 1$



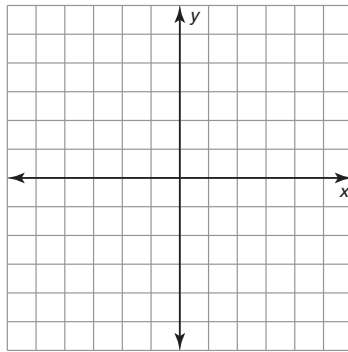
3. $x^2 + 2x + 4 = 0$



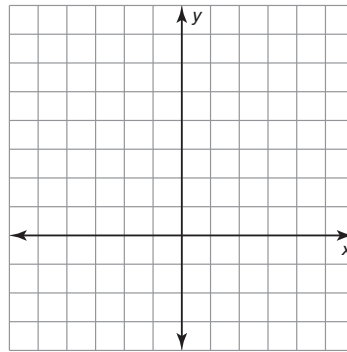
4. $x^2 - 5x + 4 = 0$



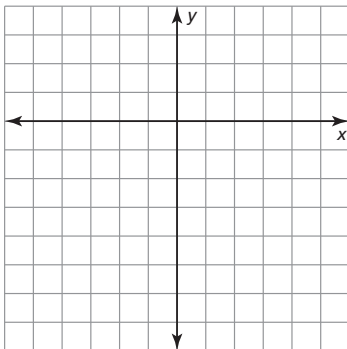
5. $x^2 + 6x + 9 = 0$



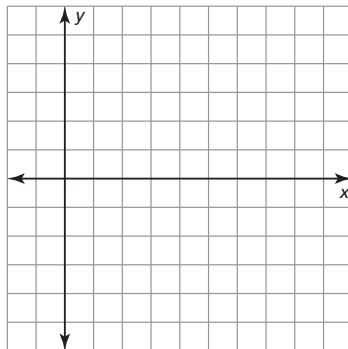
6. $x^2 = 2x - 6$



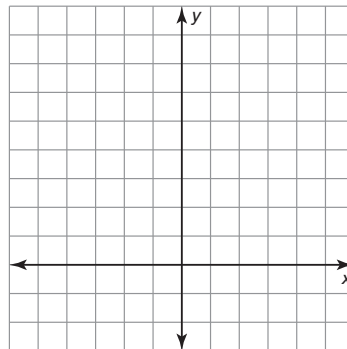
7. $x^2 - x - 12 = 0$



8. $x^2 - 10x + 25 = 0$



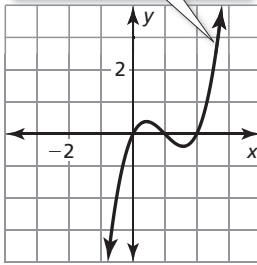
9. $x^2 + 4 = 0$



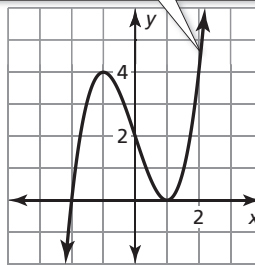
9.2 Notetaking with Vocabulary (continued)

In Exercises 10–15, find the zero(s) of f .

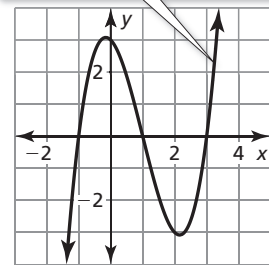
10. $f(x) = (x - 2)(x^2 - x)$



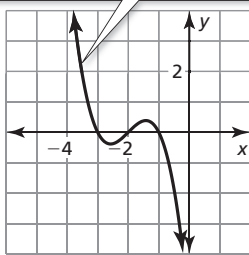
11. $f(x) = (x + 2)(x^2 - 2x + 1)$



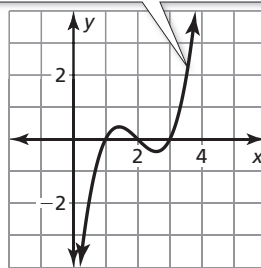
12. $f(x) = (x + 1)(x^2 - 4x + 3)$



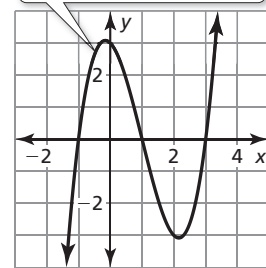
13. $f(x) = (x + 3)(-x^2 - 3x - 2)$



14. $f(x) = (x - 1)(x^2 - 5x + 6)$

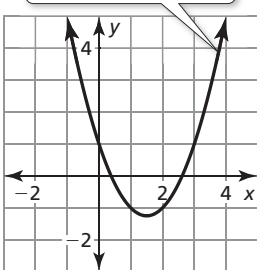


15. $f(x) = (x - 3)(x^2 - 1)$

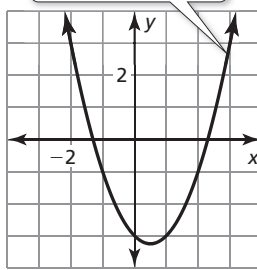


In Exercises 16–18, approximate the zeros of f to the nearest tenth.

16. $f(x) = x^2 - 3x + 1$



17. $f(x) = x^2 - x - 3$



18. $f(x) = -x^2 - 8x - 13$

