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Overview



- **Open Channel Flow**
- **O Manning Equation**
- **O Basic Culvert Design**
- Sanitary Sewer
 - Design Flow, Velocity
- Stormwater Sewer
 - Design Flow, Velocity



Open Channel Flow



Fluid passage way that allows part of the fluid to be exposed to the atmosphere

- Natural Waterways
- Canals
- Flumes
- Culverts
- Pipes flowing under the influence of gravity (pressure conduits always flow full.)

Open Channel Flow



Difficulties with Open Channel Flow

- Variations in cross sections and roughness
- More empirical & less exact than pressure conduit flow
- Run-off calculations also imprecise

Parameters Used in Open Channel Flow



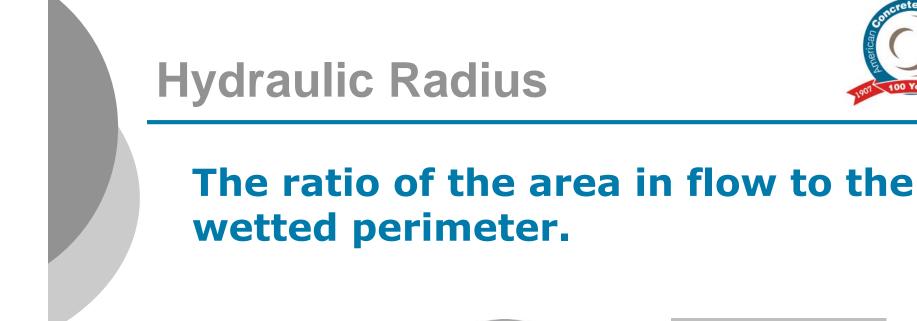
- O Q = Flow Quantity/Volume
- A = Cross-sectional Area of Flow
- o v = Velocity (mean velocity)
- R = Hydraulic Radius
- P = Wetted Perimeter
- **S = Slope**
- o n = Manning Roughness Coefficient

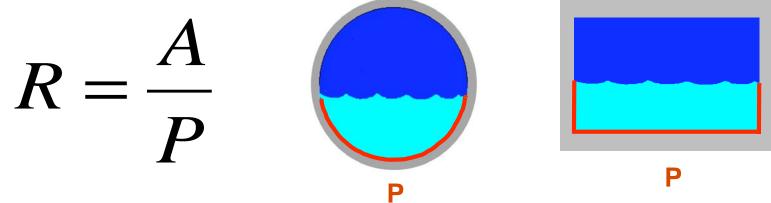
Mean Velocity



Mean velocity (v) multiplied by flow area (A) gives flow quantity (Q).

Q = Av







Hydraulic Radius



• For a circular pipe flowing full or half full:

D R





Governing Equations

• Continuity Equation $A_1v_1 = A_2v_2$ • Chezy Equation - 1768 $v = C\sqrt{RS}$ $C = \sqrt{\frac{8g}{f}}$ • Manning Equation - 1888 $C = (1.49) p^{\frac{1}{2}}$

$$C = \left(\frac{1.49}{n}\right) R^{\frac{1}{6}}$$





Governing Equations

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$$C = \left(\frac{1.49}{n}\right) R^{\frac{1}{6}}$$



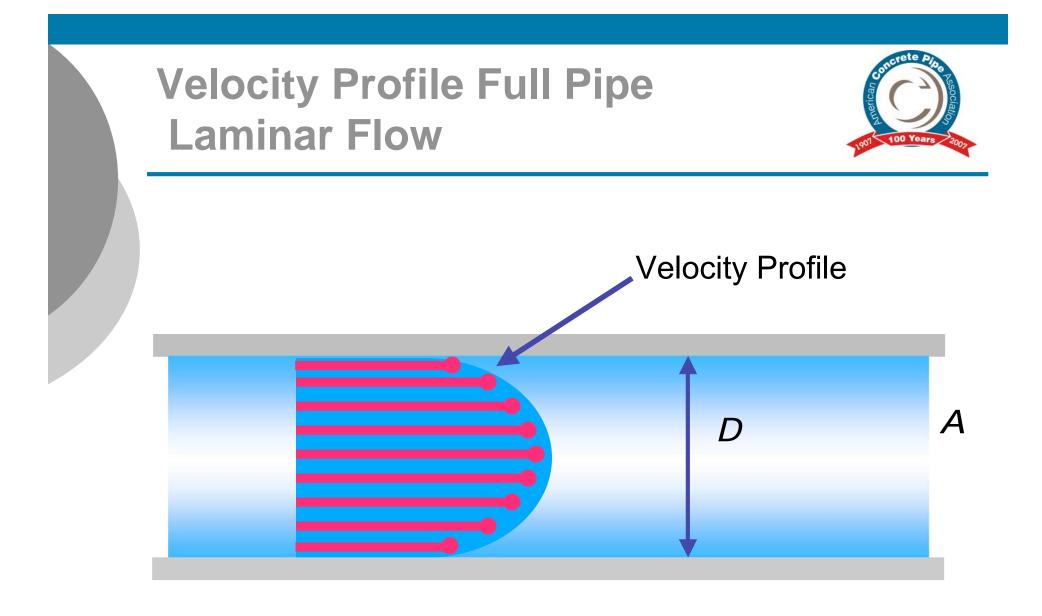


The Manning Equation

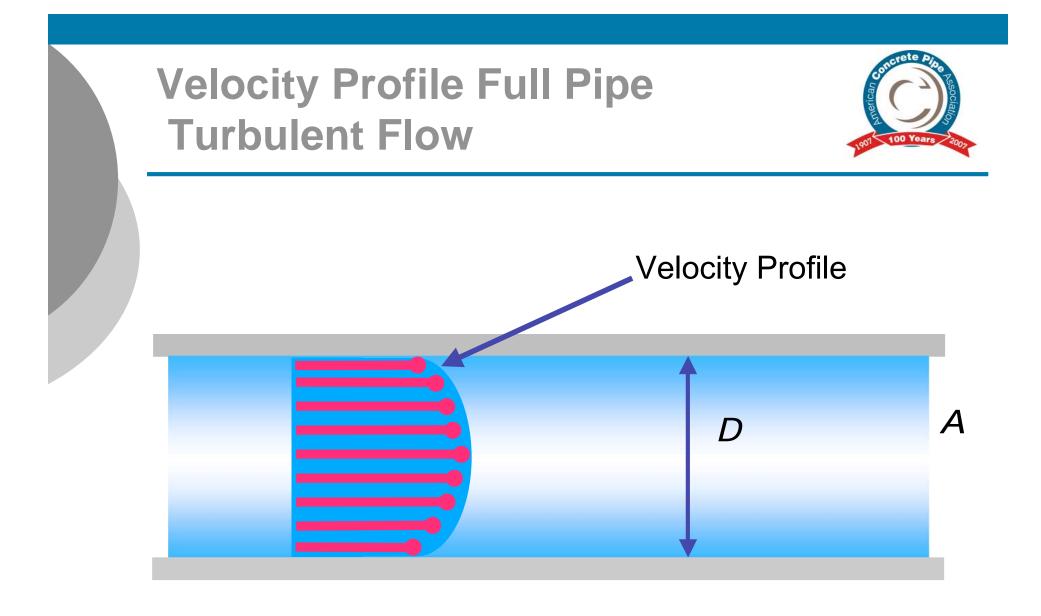
$$Q = vA = \left(\frac{1.49}{n}\right)A R^{\frac{2}{3}}\sqrt{S}$$

$$v = \left(\frac{1.49}{n}\right) R^{\frac{2}{3}} \sqrt{S}$$

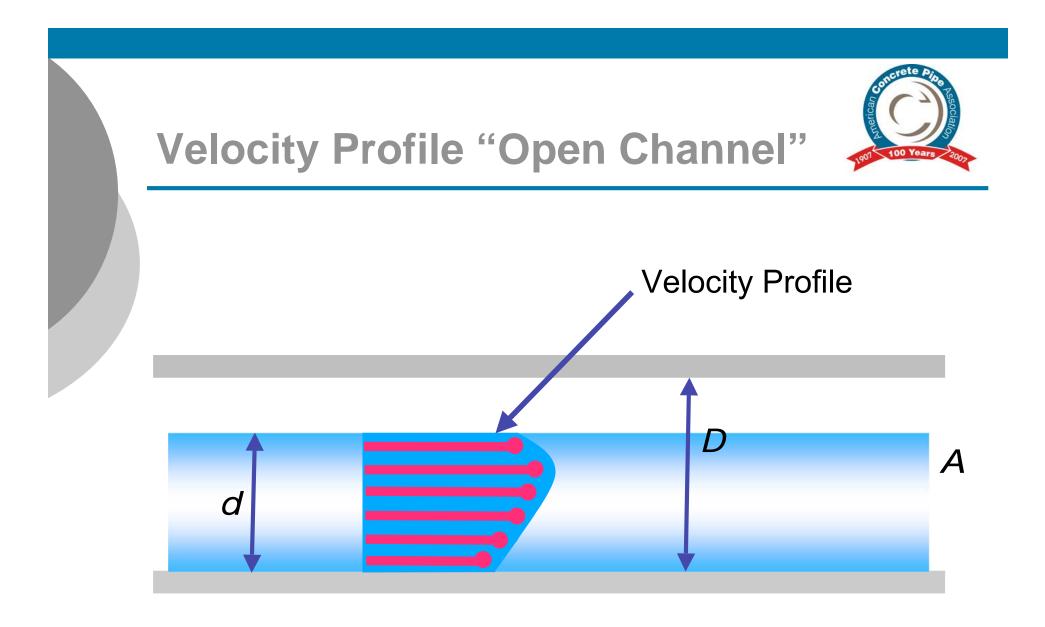














Manning Coefficient (n)

Judgment is used in selecting *n* values. Additional Design Data - <u>click here</u> *n* varies with depth of flow
For most calculations *n* is assumed to be constant.
To consider variable *n* - use tables or graphs for *n*.

Additional Info in the Concrete Design Manual - <u>click here</u>



Manning Equation Manning Coefficient (*n*)



Circular Channel Ratios

d	Q	V
D	Q _{full}	V _{full}
0.1	0.02	0.31
0.2	0.07	0.48
0.3	0.14	0.61
0.4	0.26	0.71
0.5	0.41	0.80
0.6	0.56	0.88
0.7	0.72	0.95
0.8	0.87	1.01
0.9	0.99	1.04
0.95	1.02	1.03
1.00	1.00	1.00



Manning Coefficient (n)



- For smooth wall pipes (concrete, plastic) laboratory tests have shown that "n" range between 0.009 and 0.010.
- Engineers typically use 0.012 or 0.013 to account for differences between laboratory and installed conditions.







• Recommended *n* values:

0.012 for storm sewer applications

0.013 for sanitary sewers applications



Hazen-Williams 1920s



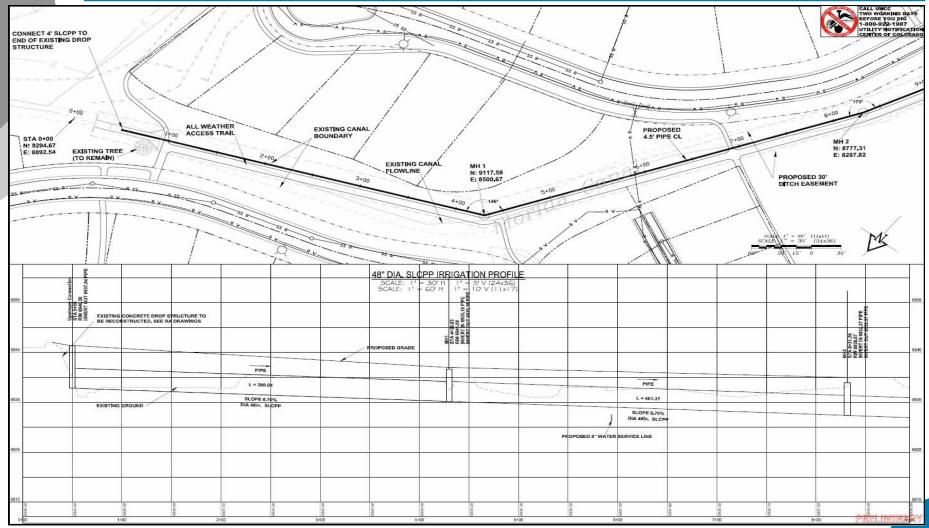
$$v = 1.318 \cdot CR^{0.63}S^{0.54}$$

- Water flows with high Reynolds Number.
- Occasionally used fire, irrigation & water distribution systems.
- Only for water within "normal" ambient conditions.
- Primarily Advantage: C depends only on the roughness, not the fluid characteristics.
- Primarily Disadvantage: C depends only on the roughness, not the fluid characteristics – professional judgment required when choosing C.





Examples







Example No. 1 48-inch Diameter RCP pipe invert out = 6932.37 ft pipe invert in = 6937.84 ft length = 781.41 ft

Use n = 0.012

Find Q_{full}

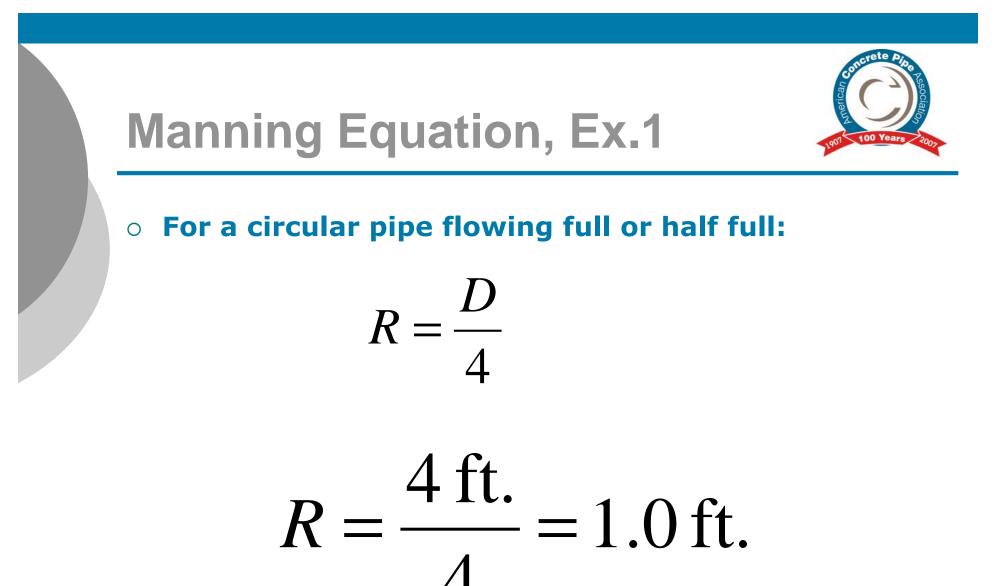




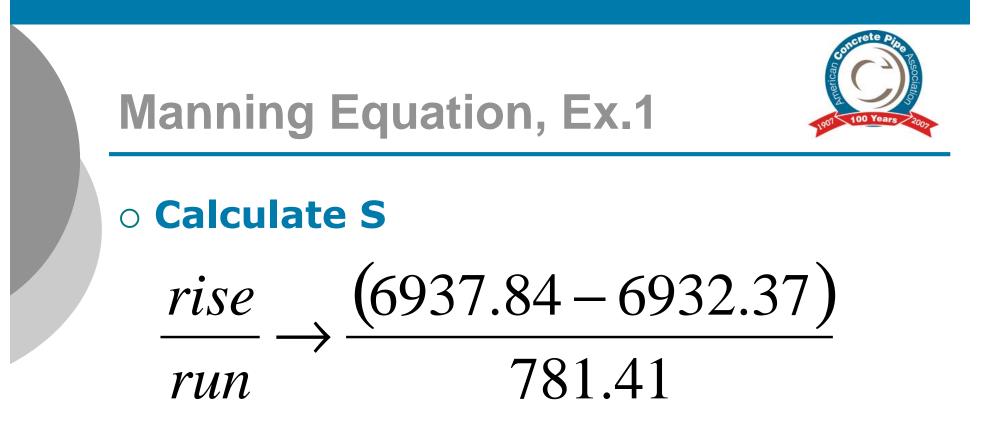
$$Q_{full} = \left(\frac{1.49}{n}\right) A R^{\frac{2}{3}} \sqrt{S}$$

○ n=0.012 ○ 48" Dia = 12.57 ft²









S = 0.007





• Result:

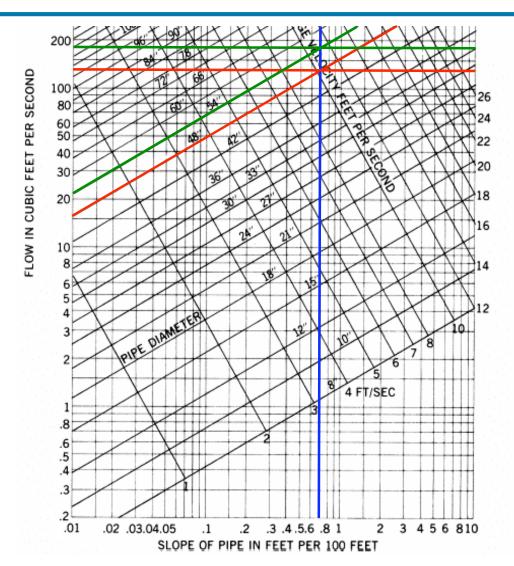
$$Q_{\text{full}} = \left(\frac{1.49}{0.012}\right) \cdot (12.57) \cdot (1.0)^{\frac{2}{3}} \cdot (\sqrt{0.007})$$

$= 130.6 \, cfs$



Flow for Circular Pipe Flowing Full Based on Manning's Equation n=0.012









Using a 54-inch pipe for the 150 cfs flow what is the depth of flow and velocity?





Example No. 2 54-inch Diameter RCP length = 781.41 ft n = 0.012 S = 0.007

R = (4.5/4) = 1.13 ftA = 15.90 ft² Find Q_{full}





$$Q_{full} = \left(\frac{1.49}{n}\right) A R^{\frac{2}{3}} \sqrt{S}$$

$$Q_{\text{full}} = \left(\frac{1.49}{0.012}\right) \cdot (15.90) \cdot (1.13)^{\frac{2}{3}} \cdot (\sqrt{0.007})$$

 $= 179.2 \, cfs$





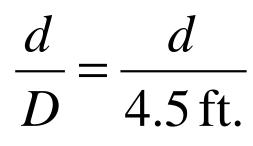
Circular Channel Ratios

d	Q	V
D	Q _{full}	V _{full}
0.1	0.02	0.31
0.2	0.07	0.48
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0.4	0.26	0.71
0.5	0.41	0.80
0.6	0.56	0.88
0.7	0.72	0.95
0.8	0.87	1.01
0.9	0.99	1.04
0.95	1.02	1.03
1.00	1.00	1.00





Find the depth of flow in the pipe



 $\frac{Q}{Q_{\rm full}} = \frac{150.0\,{\rm cfs}}{179.2\,{\rm cfs}} = 0.84$





Circular Channel Ratios

d	Q	V
D	Q _{full}	V _{full}
0.1	0.02	0.31
0.2	0.07	0.48
0.3	0.14	0.61
0.4	0.26	0.71
0.5	0.41	0.80
0.6	0.56	0.88
0.7	0.72	0.95
0.8	0.87	1.01
0.9	0.99	1.04
0.95	1.02	1.03
1.00	1.00	1.00





$$\frac{y - y_0}{y_1 - y_0} = \frac{x - x_0}{x_1 - x_0}$$
$$\frac{\left(\frac{d}{D}\right) - 0.7}{0.8 - 0.7} = \frac{0.84 - 0.72}{0.87 - 0.72}$$

$$\frac{d}{D} = 0.78$$
; D = 4.5 ft. \rightarrow d = 3.51 ft.





• Find the velocity: $v_{\text{full}} = \frac{Q_{\text{full}}}{A} = \frac{179.2 \text{ cfs}}{15.90 \text{ ft}^2} = 11.27 \text{ ft/s}$

$$\frac{v}{v_{\rm full}} = \frac{v}{11.27 \, \rm ft/s}$$

$$\frac{Q}{Q_{\rm full}} = \frac{150.0\,{\rm cfs}}{179.2\,{\rm cfs}} = 0.84$$





Circular Channel Ratios

d	Q	V
D	Q _{full}	V _{full}
0.1	0.02	0.31
0.2	0.07	0.48
0.3	0.14	0.61
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0.8	0.87	1.01
0.9	0.99	1.04
0.95	1.02	1.03
1.00	1.00	1.00





$$\frac{y - y_0}{y_1 - y_0} = \frac{x - x_0}{x_1 - x_0}$$

$$\frac{\left(\frac{v}{v_{\text{full}}}\right) - 0.95}{1.01 - 0.95} = \frac{0.84 - 0.72}{0.87 - 0.72}$$

$$\frac{v}{v_{\text{full}}} = 0.998$$
; $v_{\text{full}} = 11.27 \text{ ft/s} \rightarrow v = 11.25 \text{ ft/s}$





 Conduit passing water under or around an obstructing feature (usually manmade).

 Used to restore a water natural path that has become obstructed.

Additional Design Data – <u>click here</u>





• Headwater - <u>click here</u>

 Depth of water at the upstream face of the culvert

O Outlet velocity - <u>click here</u>

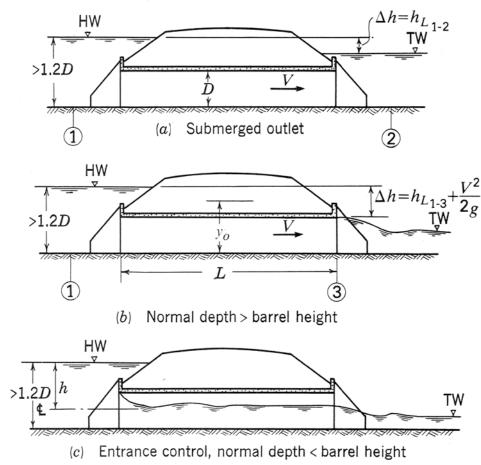
- Similar to channel velocity to protect downstream end
- O Tailwater <u>click here</u>
 - Depth of water downstream of the culvert measured from the outlet culvert

Additional Info in the Concrete Design Manual





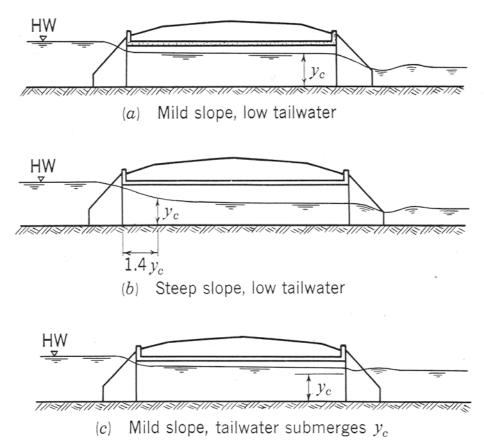
o Submerged Entrance







• Free Entrance





Parameters Used in Culvert Design



- *HW_i* = headwater depth above the inlet control section invert (ft)
- **D** = interior height of the culvert barrel (ft)
- O Q = discharge (cfs)
- A = full cross-sectional area of the culvert barrel (ft²)
- c, Y, M = constants based on shape and material
- Z = term for culvert barrel slope correction factor (ft/ft).
 For mitered inlets use Z=0.7S
 For all other conditions use Z=-0.5S





Characteristics of Flow

- Inlet Control <u>click here</u>
- Outlet Control <u>click here</u>
- Outlet Velocity

Additional Info in the Concrete Design Manual





Inlet Control

- Barrel hydraulic capacity is higher than that of the inlet.
- Typical flow condition is critical depth near the inlet and supercritical flow in the culvert barrel.
- Due to constriction at entrance, the inlet configuration has a significant effect on hydraulic performance.

Additional Design Data – click here

Outlet Control

- Barrel hydraulic capacity has a smaller hydraulic than the inlet does.
- Typical flow condition is that the full or partially full culvert barrel for all or part of its length.
- Flow regime is always subcritical, so the control of flow is either at the downstream end of the culvert or further downstream of the culvert outlet.





o Inlet Control

Submerged Condition (orifice)

$$\left[\frac{HW_i}{D}\right] = c \left[\frac{Q}{AD^{0.5}}\right]^2 + Y + Z \rightarrow \text{for}\left[\frac{Q}{AD^{0.5}}\right] \ge 4.0$$

Unsubmerged Condition (weir)

$$\left[\frac{HW_i}{D}\right] = \left[\frac{Q}{AD^{0.5}}\right]^M \to \text{for}\left[\frac{Q}{AD^{0.5}}\right] \le 3.5$$





Inlet Control Continued

Unsubmerged Condition (weir)
 Based on the specific head at critical depth

$$\left[\frac{HW_i}{D}\right] = \left[\frac{H_c}{D}\right] + K \left[\frac{Q}{AD^{0.5}}\right]^M + Z \to \text{for}\left[\frac{Q}{AD^{0.5}}\right] \le 3.5$$





Outlet Control

 $h_{o} = \max[TW, (d_{c} + D)/2]$ $d_c = \sqrt[3]{\frac{q^2}{q}}$





Outlet Control

Losses h_{ex}+h_e+h_f

$$H = \left(1 + k_e + \frac{29n^2L}{R^{1.33}}\right) \cdot \left(\frac{V^2}{2g}\right)$$

$$HW_{out} = H + h_o - S_o L$$





- Once the inlet control headwater, HW_i and the outlet control headwater, HW_{out} are computed, the controlling headwater is determined by comparing HW_i and HW_{out}
 - if HW_i>HW_{out}, the culvert is inlet controlled
 - if HW_{out}>HW_i, the culvert is outlet controlled



Basic Culvert Design



• Culvert Design Procedures (AASHTO)

- Establishment of Hydrology
- Design of downstream channel
- Assumption of a trial configuration
- Computation of inlet control headwater
- Computation of outlet control headwater at inlet
- Evaluation of the controlling headwater
- Computation of discharge over the roadway & total discharge
- Computation of outlet velocity and normal depth





Design a reinforced concrete box culvert for a roadway crossing to pass a 50-year discharge of 400 cfs.

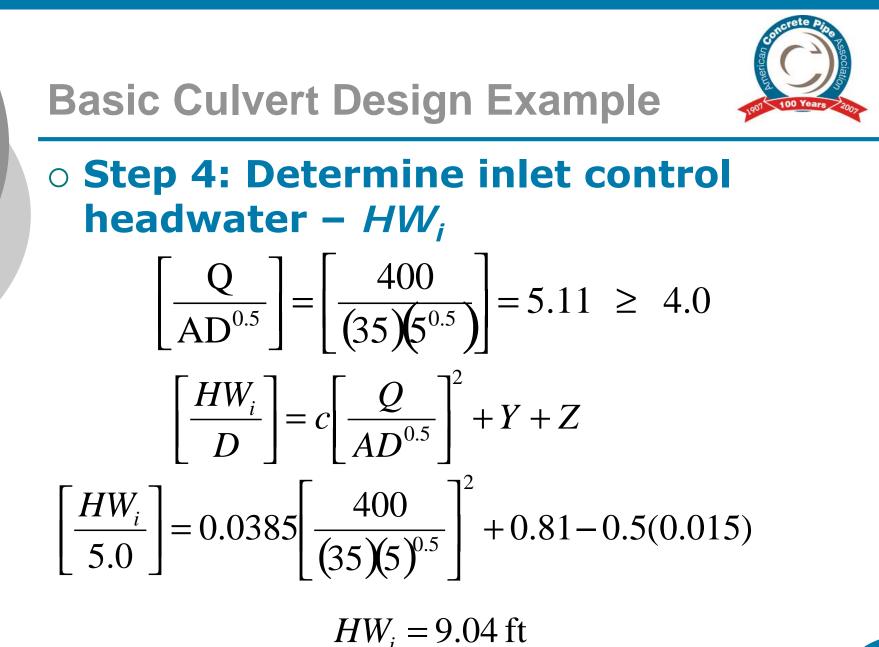
- Shoulder elevation = 155 ft.
- Streambed elevation at culvert face = 140 ft.
- Natural stream slope = 1.5%
- Tailwater depth -= 3.0 ft.
- Culvert length = 200 ft.
- Downstream channel approximate 10' x 10'
- Inlet is not depressed





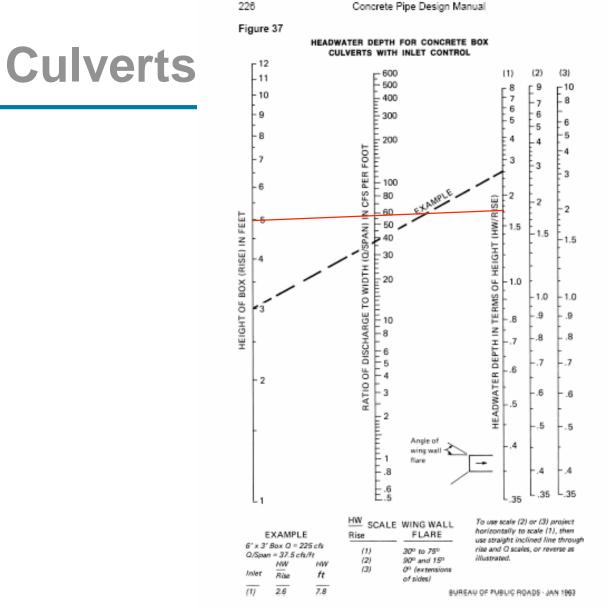
- Step 1: 50-year design discharge is given as 400/cfs.
- Step 2: Downstream geometry is given 10' x 10' rectangular
- Step 3: Use a 7' x 5' reinforced concrete box culvert with 45 degree wing wall flares, <u>beveled edges</u> <u>entrance loss coefficient of 0.2</u>
 Constants for inlet control 30-70 degree wing wall flares: c=0.0385, Y=0.81











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• Step 5 Determine the outlet control headwater depth at inlet.

• Tailwater is given = 3.0 ft.

Find Critical Depth

q(ft³/s/ft), unit discharge = total discharge/culvert width

 $g = gravitational acceleration, 32.2 ft/s^2$

$$d_c = \sqrt[3]{\frac{q^2}{g}} = \sqrt[3]{\frac{(400/7)^2}{32.2}} = 4.7 \text{ ft.}$$





 \circ h₀=is bigger value of tailwater or (D+d_c)/2.

- Tailwater is 3.0 ft.
- (4.7+5)/2=4.85 ft.

Use h₀=4.85 ft.





$\circ\,$ Find H

- A=(7)(5)=35 ft²
- V=400/35=11.4 ft/s
- R=A/P=35/(7+7+5+5)=1.46 ft

$$H = \left(1 + k_e + \frac{29n^2L}{R^{1.33}}\right) \cdot \left(\frac{V^2}{2g}\right)$$

$$H = \left(1 + 0.2 + \frac{29(0.012)^2(200)}{(1.46)^{1.33}}\right) \cdot \left(\frac{(11.4)^2}{2(32.2)}\right) = 3.44 \text{ ft}$$



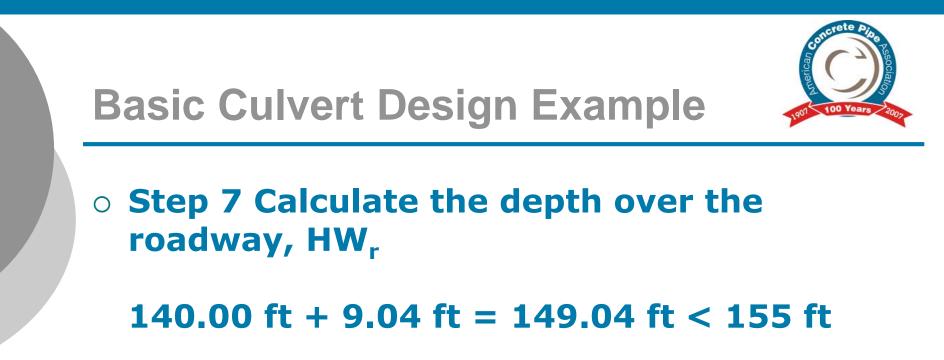


Step 6 Compute controlling headwater

$$HW_{out} = H + h_o - S_o L$$
$$HW_{out} = 3.44 + 4.85 - (0.015)(200) = 5.29 \text{ ft}$$
$$HW_i = 9.04 \text{ ft}$$

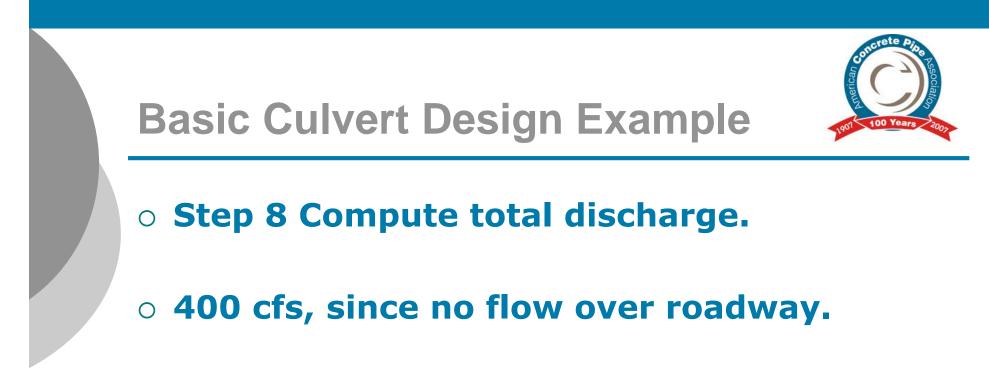
 HW_i controls, so culvert is inlet control



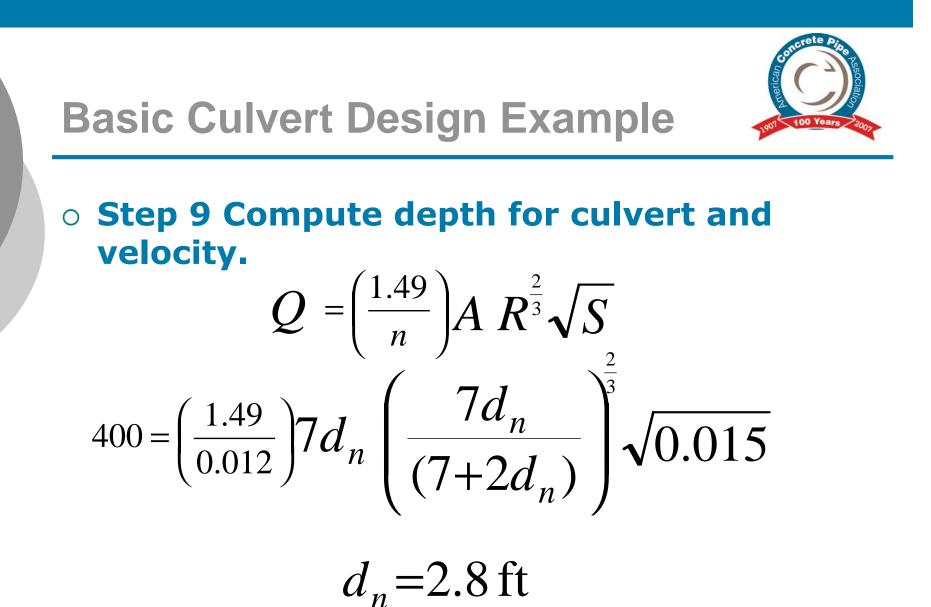


does not flow over the roadway, depth = 0

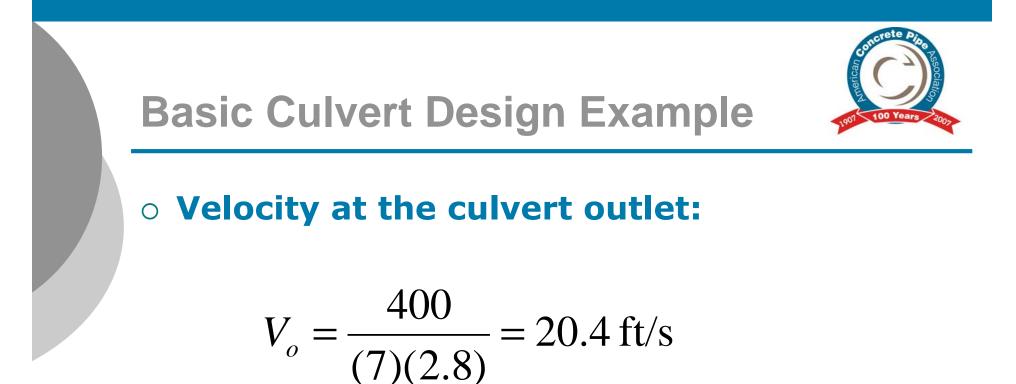
















- Average Flow
- Peak Flow

Additional Design Data – <u>click here</u>

- O Design Velocity <u>click here</u>
 - Minimum Velocity
 Full Flow 2 ft/s

Additional Info in the Concrete Design Manual







- Average Flow
 - Design based on existing data or state/local agencies will specify minimum average flows.
- Peak Flow
 - Peaking factor
- Minimum Flow
 - Is the self cleaning velocity of 2 ft/s maintained?





- Needs to include I & I
- Different for wet and dry months







- 3:1 for large sewers serving stable populations
- 20:1 for small sewers serving growing populations where domestic wastewater is major component of the total flow.







- 10.5 acre site for retail space
- Floor Area Ratio (FAR) of 0.25
- What is the wastewater flow that could be expected to be produced?









Retail space available: (10.5 acre)(0.25)=114345.5 ft²

Worst case = restaurant



Total Population		Equivalent pop/1,000 sq-ft	Population /unit	COMMERCIAL/INDUSTRIAL UNITS
-	-		3.0 2.5	Single-Family Multi-Family
-	-	1.17		COMMERCIAL/INDUSTRIAL UNITS Office, Warehouse
240.14	114.35	2.1	0.5	Retail (includes restaurant) Hotel
240.14	Population (EP)	Total Equivalent I		
	ther Flow, gpcd	r Capita Dry Wea	Pe	
16,809.45	low, gpd (x 70)	ge Dry Weather F	Avera	
11.67	v, gpm (/ 1440)	Dry Weather Flow	Average	
4.12	-(EP/1000)^0.5]	EP/1000)^0.5]/[4+	ctor, PF=[18+	Peak Flow Fac
69,221.57 48.07		vlaximum Dry Wea laximum Dry Wea		
0.15	EP/1000)^0.198	actor, MF = 0.2*(E	imum Flow F	Min
2,534.62 1.76		Minimum Dry Wea Ainimum Dry Wea		
16,600.00	16.60	ting area in acres	gpd; contribu	Infiltration/inflow to sewer,
85,821.57 59.60		laximum Wet Wea aximum Wet Wea		









• **Design Flow -** <u>click here</u>

The Rational Method: Q=CiA

O Design Velocity

- Minimum Velocity
 - o Full Flow 3 ft/s

Additional Info in the Concrete Design Manual



Storm Sewer



 Rational method assumes that the maximum rate of runoff for a given intensity occurs when the duration of the storm is long enough such that all parts of the watershed are contributing to runoff at the interception point.

Additional Info in the Concrete Design Manual - <u>click here</u>



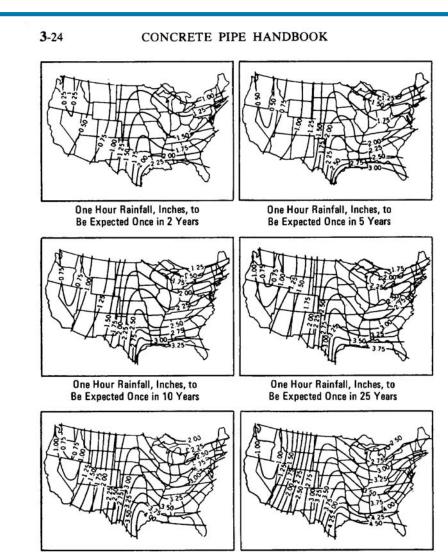


• **Q=C***i***A**

- C is the ratio of the average rate of rainfall on an area to the maximum rate of run off.
- i is the amount of rainfall measured in inches/hr that would be expected in a storm event of a certain duration and frequency.
- A is drainage area in acres contributing to watershed
- Time of Concentration time required for a drop of water to fall at the most remote part of the drainage area and flow to a point in the system











- Highly absorbent surfaces = little runoff
- Occurs when rainfall intensity exceeds infiltration rate into the surface
- Topographic variables
 - Land use
 - Type of soil
 - Area
 - Land shape or form
 - Elevation
 - Slope
 - Orientation

 Estimated by hydrographs or rational method





- **o Instantaneous peak runoff**
- For areas less than 1 to 2 miles²
- \circ **Q** = **C I A**
 - A is area in acres
 - Q is in ac. in./hr. or ft³/sec.
 - C is run off co-efficient
 - Typical values of C

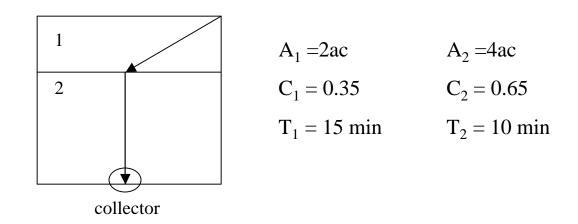
forest	0.059 - 0.2
asphalt	0.7 - 0.95
concrete	0.895
farmland	0.05 - 0.3
unimproved	0.1 - 0.3
downtown	0.7 - 0.95
RESIDENTIAL:	
single family	0.3 - 0.5
apartments	0.5 - 0.7







Given: Two adjacent fields, contribute runoff to a collector whose capacity is to be determined. The intensity after 25 min is 3.9 in / hr.



Find: The peak flow using the rational method





Solution:

Total time: $t = 15 \min + 10 \min = 25 \min$

Total runoff coefficient: Use contributing areas

$$C = (2ac)(0.35) + (4ac)(0.65) = 0.55$$

2ac + 4ac

Total Area: A = 2 ac + 4 ac = 6 ac

Peak Flow: Q = CIA Q = (0.55)(3.9 in/hr)(6ac) $Q = 12.9 \text{ ac-in/hr} (ft^3 / sec)$





Please see remaining slides for the exam questions and submittal form.

PDH for this course: 1.0 Non member fee: \$99.00 Member & Non Industry Engineer Fee: No charge

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Instructions for Submitting Exam

- $\circ~$ Print out the exam submittal form and test.
- Complete the exam by circling the answers on the form.
- Complete submittal form.
- Mail your exam, submittal form and payment (if applicable) to:

American Concrete Pipe Association

, ((),: fYYdcfh[·]D_k mž Suite 3) \$

Irving, TX 750* '

Attn: Professional Membership – Online Exam

• Your exam will be graded by the ACPA and the results provided to you within 60 days.



Hydraulics Exam Submittal Form

Required Contact Information:

	et Addre	ss:								
Maili	ng Addro	ess:								
City:						Stat	e:		Zip Code:	
Telephone:						Fax:				
Website: www										
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Exam

What are the difficulties of Open Channel Flow?

- Solution Station Statistics St
- More empirical and less exact than pressure conduit flow
- **Imprecise run-off calculations**
- All of the above

True or False: Due to constriction at entrance, the inlet configuration has a significant effect on hydraulic performance of basic culverts.

- 💿 True
- 🔊 🛛 False

What is headwater?

- Depth of water downstream of the culvert measured from the outlet culvert
- **Depth of water at the upstream face of the culvert**
- Similar to channel velocity to protect downstream end
- Velocity at the downstream face of the culvert

Name one of the basic culvert uses dealing with hydraulics?

- Restoration of a natural waterway that has become obstructed
- 80 Sanitary Sewer
- **Reinforcing Foundation**
- Tunnel





Exam (cont.)

Which control has the smaller Barrel hydraulic capacity?

- Inlet
- **Outlet**
- **What range of numbers is used by engineers as the manning coefficient, n, for smooth wall pipes?**
 - 0.005 or 0.008
 - **0.009 or 0.010**
 - 10.012 or 0.013
 - **____** 0.015 or 0.025
- What is the time required for a drop of water to fall at the most remote part of the drainage area and flow to a point in the system called?
 - Time of Concentration
 - 10 Time of Flow
 - No Average Flow
 - Design Flow

How is Average Flow calculated?

- Rational Method
- **Product of the manning coefficient and Peak Flow**
- m Based on existing data or specified
- Product of the Peaking Factor and Inlet Headwater





For more information: <u>http://www.fhwa.dot.gov/engineering/hydraulics/</u>

Thank you for participating in ACPA's online training.

Please send us an email at <u>info@concretepipe.org</u> if you would like to suggest a training topic to be added in the future. In the subject line include "online training topic."



Concrete Pipe Association

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