# 1. Plan

#### **Objectives**

- 1 To relate slope and parallel lines
- 2 To relate slope and perpendicular lines

#### **Examples**

- 1 Checking for Parallel Lines
- 2 Determining Whether Lines are Parallel
- 3 Writing Equations of Parallel Lines
- 4 Checking for Perpendicular Lines
- 5 Writing Equations for Perpendicular Lines
- 6 Real-World Connection

# Math Background

Slope is a fixed ratio that characterizes any nonvertical line. It is another example of a pure geometric concept, a line, described by algebraic methods. The product of the slopes of perpendicular lines being -1, although initially surprising, is merely the Pythagorean Theorem in an analytic geometry setting.

#### More Math Background: p. 124D

#### Lesson Planning and Resources

See p. 124E for a list of the resources that support this lesson.



**Check Skills You'll Need** For intervention, direct students to:

#### Slope

Algebra 1 Review, page 165

#### **Graphing Lines**

Lesson 3-6: Example 3 Extra Skills, Word Problems, Proof Practice, Ch. 3



# Slopes of Parallel and Perpendicular Lines

#### What You'll Learn

- To relate slope and parallel lines
- To relate slope and perpendicular lines

#### ... And Why

To write an equation that models part of a leaded glass window, as in Example 6

| of Check Skills You'll Need               | GO for Help                                 | page 165 and Lesson 3-6                      |
|---|---|--|
| Find the slope of the line th             | rough each pair of points.                  |  |
| <b>1.</b> $F(2,5), B(-2,3) = \frac{1}{2}$ | <b>2.</b> $H(0, -5), D(2, 0) = \frac{5}{2}$ | <b>3.</b> <i>E</i> (1, 1), <i>F</i> (2, −4)  |
| Find the slope of each line.              |   | -5   |
| <b>4.</b> $y = 2x - 5$ <b>2</b>           | <b>5.</b> $x + y = 20$ <b>-1</b>            | <b>6.</b> $2x - 3y = 6\frac{2}{3}$           |
| <b>7.</b> $x = y$ <b>1</b>                | 8. $y = 7$ 0                                | <b>9.</b> $y = \frac{2}{3}x + 7 \frac{2}{3}$ |
|   |   |  |

#### Slope and Parallel Lines

The relationship between slope and parallel lines is summarized below and proved in Lesson 7-3.

| Key Concepts | Summary             | Slopes of Parallel Lines  |
|--------------|---------------------|---|
|              | If two nonvertica   | l lines are parallel, their slopes are equal.                   |
|              | If the slopes of tw | o distinct nonvertical lines are equal, the lines are parallel. |
|              | Any two vertical    | lines are parallel.   |
| •            |                     |   |

#### Real-World 🌍 Connection

The ramp and rails are parallel because they have the same slope.



You can test whether nonvertical lines are parallel by comparing their slopes.

#### EXAMPLE Checking for Parallel Lines

Are lines  $\ell_1$  and  $\ell_2$  parallel? Explain.

Find and compare the slopes of the lines.

slope of 
$$\ell_1 = \frac{5 - (-4)}{1 - (-2)} = \frac{9}{3} = 3$$

slope of 
$$\ell_2 = \frac{3 - (-4)}{3 - 1} = \frac{7}{2}$$

Lines  $\ell_1$  and  $\ell_2$  are not parallel because their slopes are not equal.



Quick Check 1 Line  $\ell_3$  contains A(-4, 2) and B(3, 1). Line  $\ell_4$  contains C(-4, 0) and D(8, -2). Are  $\ell_3$  and  $\ell_4$  parallel? Explain. No; the slope of  $\ell_3 = -\frac{1}{7}$ , and the slope of  $\ell_4 = -\frac{1}{6}$ .

174 Chapter 3 Parallel and Perpendicular Lines

#### Differentiated Instruction Solutions for All Learners

#### Special Needs

Some students may have difficulty seeing pairs of perpendicular lines other than vertical and horizontal lines. Have students use a protractor to confirm the perpendicular lines shown in Example 4.

#### Below Level 12

Review the rules for multiplying and dividing signed numbers before students work with the slopes of perpendicular lines.

learning style: tactile

ALGEBRA

Slope-intercept form allows you to compare slopes easily in order to decide whether lines are parallel.

|   | 2 EXAMPLE Determining Whether Lines are Parallel  |
|---|---|
| 00000   | <b>Multiple Choice</b> Which line is parallel to $4y - 12x = 20$ ?  |
| Test-Taking Tip   | (A) $y = 3x - 1$<br>(B) $y = -\frac{1}{3}x - 1$<br>(C) $4x = -\frac{1}{2}x + 20$<br>(C) $x = -\frac{1}{3}x + 1$   |
| To compare slopes of<br>two lines, write their<br>equations in slope-<br>intercept form,<br>y = mx + b. | Write $4y - 12x + 20$<br>4y - 12x = 20 in slope-intercept form.<br>4y - 12x = 20<br>4y = 12x + 20 Add 12x to each side.<br>y = 3x + 5 Divide each side by 4   |
|   | The line $4y - 12x = 20$ has slope 3. The line $y = 3x - 1$ is the only answer choice<br>with slope 3. The correct choice is A.   |
| 🧭 Quick Check   | 2 Are the lines parallel? Explain. <b>a.</b> $y = -\frac{1}{2}x + 5$ and $2x + 4y = 9$ <b>b.</b> $y = -\frac{1}{2}x + 5$ and $2x + 4y = 20$ <b>Yes; both slopes = <math>-\frac{1}{2}</math>.</b> No; the lines are the same. You can write an equation for a line parallel to a given line.   |
|   | 3 EXAMPLE Writing Equations of Parallel Lines<br>Write an equation for the line parallel to $y = -4x + 3$ that contains $(1, -2)$ .<br>Step 1 Identify the slope of the given line.<br>y = -4x + 3<br>slope<br>Step 2 Use point-slope form to write an equation for the new line.<br>$y - y_1 = m(x - x_1)$<br>$y - (-2) = -4(x - 1)$ Substitute -4 for m and $(1, -2)$ for $(x_1, y_1)$ .<br>y + 2 = -4(x - 1) Simplify. |
| 🧭 Quick Check   | 3 Write an equation for the line parallel to $y = -x + 4$ that contains (-2, 5).<br>y = -x + 3  |

#### Slope and Perpendicular Lines

Summary

The relationship between perpendicular lines and their slopes is summarized below. These statements will be proved in Lessons 6-6 and 6-7.

Key Concepts

#### Slopes of Perpendicular Lines

If two nonvertical lines are perpendicular, the product of their slopes is -1. If the slopes of two lines have a product of -1, the lines are perpendicular. Any horizontal line and vertical line are perpendicular.

#### Lesson 3-7 Slopes of Parallel and Perpendicular Lines 175

| Advanced Learners 4<br>After students complete Example 5, have them work on<br>this problem: Line $y + ax = b$ is perpendicular to line<br>y - ax = b. What are the possible values of a? | <b>English Language Learners ELL</b><br>Review the meaning of <i>positive slope</i> and <i>negative</i><br><i>slope</i> . Then distinguish slope from the <i>product of the</i><br><i>slopes</i> of two lines. The <i>product of the slopes</i> for two<br>nonvertical perpendicular lines is always – 1. |
|---|---|
| learning style: verbal  | learning style: verbal  |

## 2. Teach

#### **Guided Instruction**

#### Careers

Most buildings have walls that are perpendicular to floors, to ceilings, and to each other. Have students investigate how builders construct these.

#### Math Tip

After students read the Key Concepts about parallel lines, ask: *How can you state the two conditionals as a biconditional?* Two distinct nonvertical lines are parallel if and only if their slopes are equal.

#### 2 EXAMPLE Error Prevention

Remind students that they must compare both the slopes and the y-intercepts. Ask: *If the slopes are equal and the y-intercepts are equal, are the lines parallel? Explain.* No; there is only one line.



Line  $\ell_1$  contains P(0, 3) and Q(-2, 5). Line  $\ell_2$  contains R(0, -7) and S(3, -10). Are lines  $\ell_1$  and  $\ell_2$  parallel? Explain. Yes; each has slope -1 and different *y*-intercepts.

**2** Are the lines y = -5x + 4 and x = -5y + 4 parallel? Explain. No; one line has slope -5 and the other line has slope  $-\frac{1}{5}$ .

3 Write an equation in pointslope form for the line parallel to 6x - 3y = 9 that contains (-5, -8). y + 8 = 2(x + 5)

#### **Guided Instruction**

#### 4 EXAMPLE Alternative Method

When lines are perpendicular, their slopes are *negative* reciprocals. Have students check that  $m_1$  and  $m_2$  are negative reciprocals.

#### **5** EXAMPLE Special Needs L1

Students who find the procedure complicated can work with partners.

#### 6 EXAMPLE Diversity

Ask students to describe unusual window designs they have seen elsewhere.

# **Additional Examples**

4 Line  $\ell_1$  contains M(0, 8) and N(4, -6). Line  $\ell_2$  contains P(-2, 9)and Q(5, 7). Are lines  $\ell_1$  and  $\ell_2$ perpendicular? Explain. No; the product of their slopes is 1.

5 Write an equation for a line perpendicular to 5x + 2y = 1 that contains (10, 0).  $y = \frac{2}{5}(x - 10)$ 

**6** The equation for a line containing a lead strip is  $y = \frac{1}{2}x - 9$ . Write an equation for a line perpendicular to it that contains (1, 7). y = -2x + 9

#### Resources

Daily Notetaking Guide 3-7 13

• Daily Notetaking Guide 3-7-Adapted Instruction L1

#### Closure

Explain algebraically why two lines cannot be both parallel and perpendicular. The product of the slopes *m* of two parallel lines is  $m^2$ . The product of the slopes of two perpendicular lines is -1. A slope *m* such that  $m^2 = -1$  is not a real number.

You can test whether lines are perpendicular by first noting whether either line is vertical or horizontal. If not, check their slopes. If the product of the slopes is -1, the lines are perpendicular.

#### EXAMPLE **Checking for Perpendicular Lines**

**Algebra** Lines  $\ell_1$  and  $\ell_2$  are neither vertical nor horizontal. Are they perpendicular? Explain.

**Step 1** Find the slope of each line.

**Step 2** Find the product of the slopes.

$$m_1$$
 = slope of  $\ell_1 = \frac{-2}{-3} - \frac{2}{0} = \frac{-4}{-3} = \frac{4}{3}$   
 $m_2$  = slope of  $\ell_2 = \frac{3 - (-3)}{-2 - 6} = \frac{6}{-8} = -\frac{3}{4}$ 

2, 3(0, 2)C 6x(6, -3)

 $m_1 \cdot m_2 = \frac{4}{3} \cdot -\frac{3}{4} = -1$ 

• Lines  $\ell_1$  and  $\ell_2$  are perpendicular because the product of their slopes is -1.

**Vocabulary Tip** 

Numbers with product -1 are opposite reciprocals.

In Example 5, the opposite reciprocal of -3 is  $\frac{1}{3}$ .

Quick Check (a) Are 
$$\ell_3$$
 and  $\ell_4$  perpendicular? Explain.  
No; the slope of  $\ell_3 = \frac{4}{9}$ , and the slope

slope of  $\ell_4 = -\frac{7}{3}$ , and  $\frac{4}{9} \cdot -\frac{7}{3} \neq -1$ .



You can write an equation for a line perpendicular to a given line. If the given line is horizontal, write an equation for a vertical line. If the given line is vertical, write an equation for a horizontal line.

#### EXAMPLE

#### Writing Equations for Perpendicular Lines

Write an equation for the line perpendicular to y = -3x - 5 that contains (-3, 7).

**Step 1** Identify the slope of the given line. y = -3x - 5

**Step 2** Find the slope of the line perpendicular to the given line. Let *m* be the slope of the perpendicular line.

= -1 The product of the slopes of

$$3m = -1$$
 The product of the slopes of perpendicular lines is  $-1$ .

 $m = \frac{1}{3}$  Divide each side by -3.

**Step 3** Use point-slope form to write an equation for the new line.

$$y - y_1 = m(x - x_1)$$
  

$$y - 7 = \frac{1}{3}[x - (-3)]$$
 Substitute  $\frac{1}{3}$  for *m* and (-3, 7) for (x<sub>1</sub>, y<sub>1</sub>)  

$$y - 7 = \frac{1}{3}(x + 3)$$
 Simplify.

**Quick Check (5)** Write an equation for the line perpendicular to 5y - x = 10 that contains (15, -4). y + 4 = -5(x - 15)

176 Chapter 3 Parallel and Perpendicular Lines



#### Real-World < Connection EXAMPLE

The window at the left includes some perpendicular lead strips. The line that contains  $\overline{BC}$  has equation y = -x + 10.  $\overline{AB}$  is perpendicular to  $\overline{BC}$ . Write an equation for  $\overrightarrow{AB}$ , the line that contains  $\overline{AB}$  and point (-1, 5).

The line that contains  $\overline{BC}$  has slope -1. Let *m* be the slope of  $\overrightarrow{AB}$ .

```
-1m = -1 The product of the slopes is -1.
  m = 1
```

 $\overrightarrow{AB}$  has slope 1 and can be written in the form y = 1x + b, or y = x + b. y = x + b**AB** has slope 1.

5 = -1 + b Substitute 5 for y and -1 for x.

```
6 = b
               Add 1 to each side.
```

```
• The equation for \overrightarrow{AB} is y = x + 6.
```

**Over Check (6)** If the equation for a line containing a lead strip on a different window is

 $y = -\frac{2}{3}x + 15$ , write an equation for the line perpendicular to it that contains (2, 8).

 $y - 8 = \frac{3}{2}(x - 2)$  or  $y = \frac{3}{2}x + 5$ 

#### For more exercises, see Extra Skill, Word Problem, and Proof Practice.

#### **Practice and Problem Solving**

**EXERCISES** 

| Practice by Example  | In Exercises 1–5, are lines $\ell_1$ and $\ell_2$   | 2 paralle  |
|--|---|--|
| Example 1<br>(page 174)<br>(page 174)<br>2. No; the slope of $\ell_1 = \frac{1}{3}$<br>and the slope of $\ell_2 = \frac{1}{2}$ | <b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b><br><b>1.</b> | x  |
| 3. No; the slope of $\ell_1 = \frac{3}{2}$ ,<br>and the slope of $\ell_2 = 2$ .  | 3.<br>$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$  |  |
| Example 2<br>(page 175)  | 5. Line $\ell_1$ contains $A(-3, 6)$ and $R$<br>Yes; both slopes = 0.<br>$x^2$ Algebra Are the lines parallel?<br>6. $y = 2x + 5$<br>y = 2x<br>7. $y = 2x$  | $B(2, 6), a$ $Explai$ $= \frac{3}{4}x - \frac{3}{4}x + \frac{3}{4}$ |
|  | 9. $y - 7x = 6$ 10. $3x$ $y + 7x = 8$ $6x$ Lesson 3-7   | + 4y =<br>+ 2y =<br>Slopes of  |
| 6. Yes; the lines both l   | have 7. Yes; the lines bot  | h have   |

different y-intercepts.

- a slope of  $\frac{3}{4}$  but different y-intercepts.
- 8. Yes; the lines both have a slope of -1 but different y-intercepts.



and line  $\ell_2$  contains C(0,0) and D(7,0).

#### in. 6–11. See margin.

| y = 2x + 5 | <b>7.</b> $y = \frac{3}{4}x - 10$ | <b>8.</b> $y = -x + 6$    |
|------------|-----------------------------------|---------------------------|
| y = 2x     | $y = \frac{3}{4}x + 2$            | x + y = 20                |
| y - 7x = 6 | <b>10.</b> $3x + 4y = 12$         | <b>11.</b> $2x + 5y = -1$ |
| y + 7x = 8 | 6x + 2y = 6                       | 10y = -4x - 20            |

of Parallel and Perpendicular Lines 177

- 9. No; one slope = 7 and the other slope = -7.
- 10. No; one slope =  $-\frac{3}{4}$  and the other slope = -3.

## 3. Practice

#### **Assignment Guide**

| 🗸 А В                 | 1-15, 29-32, 34, 35, 37 |
|-----------------------|-------------------------|
| 🛛 А В                 | 16-28, 33, 36, 38-44    |
| C Challer             | nge 45-48               |
| Test Prep<br>Mixed Re | 49-52<br>view 53-61     |

#### **Homework Quick Check**

To check students' understanding of key skills and concepts, go over Exercises 6, 18, 34, 36, 40.

#### **Visual Learners**

**Exercises 1–4** Lines that do not intersect on the portion of the coordinate plane shown or that appear parallel may not actually be parallel. The only way to be certain that lines are parallel is to compare their slopes.

Exercises 8–11 Remind students to rewrite equations in slopeintercept form.

#### Differentiated Instruction Resources

| GF          | S Guided Problem Solving  |
|-------------|---|
| Enr         | ichmentL4   |
| R           | eteaching L2  |
| Ada         | apted Practice  |
| Pi          | ractice L3  |
|             | Practice 3-7 Constructing Parallel and Perpendicular Lines<br>Construct a line perpendicular to line / through point Q.                           |
|             | 1. •Q 2. •Q 3. •Q   |
|             |   |
|             | Construct a line perpendicular to line I at point T.  |
|             | 4. $\qquad \qquad $        |
|             | Construct a line parallel to line <i>l</i> and through point <i>K</i> .   |
|             | 7. • <i>K</i> 8. • <i>K</i> 9. • <i>K</i>   |
|             | ÷ ************************************  |
| povas       | For Evervices 1015 use the segments at the right  |
| n drifte n  | 10. Construct a quadrilateral with one pair of parallel sides of lengths <b>b c</b>   |
| ion, his. A | Construct a quadrilateral with one pair of parallel sides of lengths     b and c.   |
| Educat      | 12. Construct a square with side lengths of b.  |
| ustee       | 13. Construct a right triangle with leg lengths of a and c.   |
| e P.c       | <ol> <li>Construct a right triangle with leg lengths of b and c.</li> <li>Construct an isosceles right triangle with leg lengths of a.</li> </ol> |
|             |   |
| 1           |   |

11. Yes; the lines both have a slope of  $-\frac{2}{5}$  but different y-intercepts.

**Exercise 28** Students must correctly transform equations in standard form to slope-intercept form.

**Exercise 38** Discuss as a class how the truth value of this theorem changes if the phrase *in a plane* is removed. Have students explain why the resulting statement is false.

**Exercise 39** In Chapter 5 students will learn that the shortest distance from a point to a line is along the perpendicular path to that line. Discuss informally why Joe would choose the perpendicular route to the ball.

**Exercises 45, 46** These exercises anticipate the study of quadrilaterals in Chapter 6. If necessary, review the distance and midpoint formulas.

- 12. y 3 = -2(x 0) or y - 3 = -2x
- 13.  $y 0 = \frac{1}{3}(x 6)$  or  $y = \frac{1}{3}(x - 6)$
- 29. slope of  $\overline{AB}$  = slope of  $\overline{CD} = \frac{2}{3}; \overline{AB} \parallel \overline{CD}$ slope of  $\overline{BC}$  = slope of  $\overline{AD} = -3; \overline{BC} \parallel \overline{AD}$
- 30. slope of  $\overline{AB}$  = slope of  $\overline{CD}$  =  $-\frac{3}{4}$ ;  $\overline{AB} \parallel \overline{CD}$ slope of  $\overline{BC}$  = slope of  $\overline{AD}$  = 1;  $\overline{BC} \parallel \overline{AD}$
- 31. slope of  $\overline{AB} = \frac{1}{2}$ ; slope of  $\overline{CD} = \frac{1}{4}$ ;  $\overline{AB} \parallel \overline{CD}$ slope of  $\overline{BC} = -1$ ; slope of  $\overline{AD} = -\frac{1}{2}$ ;  $\overline{BC} \parallel \overline{AD}$
- 32. slope of  $\overline{AB} =$  slope of  $\overline{CD} = 0$ ;  $\overline{AB} \parallel \overline{CD}$ slope of  $\overline{BC} = 3$  and slope of  $\overline{AD} = \frac{3}{2}$ ;  $\overline{BC} \parallel \overline{AD}$
- 45.  $\overline{AC}: d$   $= \sqrt{(7-9)^2 + (11-1)^2}$   $= \sqrt{104}$   $\overline{BD}: d$   $= \sqrt{(13-3)^2 + (7-5)^2}$   $= \sqrt{104}$   $\overline{AC} \cong \overline{BD}$

since  $-5 \cdot \frac{1}{5} = -1$ ,

 $\overline{AC} \perp \overline{BD};$ 



since the midpoints are

the same, the diagonals

bisect each other.

178

35.  $\overline{RS}$  and  $\overline{VU}$  are horizontal with slope = 0;  $\overline{RS} \parallel \overline{VU}$ ; slope of  $\overline{RW}$  = slope of  $\overline{UT}$ = 1;  $\overline{RW} \parallel \overline{UT}$ ; slope of  $\overline{WV}$  = slope of  $\overline{ST}$ = -1;  $\overline{WV} \parallel \overline{ST}$ 



Real-World 🜏 Connection

For a corner kick, the ball is placed within a quarter circle of radius 1 yd.





- **35.** Use slope to show that the opposite sides of hexagon *RSTUVW* at the right are parallel.
- **36.** Use slope to determine whether a triangle
- with vertices G(3,2), H(8,5), and K(0,10) is a right triangle. Explain. No; no pairs of slopes have a product of -1.

**Developing Proof** Use slope to explain why each theorem is true for three lines in the coordinate plane.

- **37.** Theorem 3-9: If two lines are parallel to the same line, then they are parallel to each other. **The lines will have the same slope.**
- 38. Theorem 3-10: In a plane, if two lines are perpendicular to the same line, then they are parallel to each other. When lines are ⊥, the product of their slopes is -1. So, two lines ⊥ to the same line must have the same slope.
- **39.** Soccer The coordinate system at the right is designed for a soccer field. Each unit represents one yard. Joe is at point P(35, -20). The path of the ball from a corner kick is represented by the equation  $y = -\frac{4}{3}x$ . To have the best chance for a shot on goal, Joe wants to run toward the ball so that his path meets the path of the ball at a right angle.



Ò,

6

Exercise 35

**a.** Find an equation for the line on which Joe should run.  $y + 20 = \frac{3}{4}(x - 35)$ 

**b.** Critical Thinking Why is point-slope form the best choice for the equation? because you are given a point and can quickly find the slope

Determine whether  $\overrightarrow{AB}$  and  $\overrightarrow{CD}$  are *parallel*, *perpendicular*, or *neither*.

**40.**  $A(-1,\frac{1}{2}), B(-1,2), C(3,7), D(3,-1)$  **41.**  $A(-2,3), B(-2,5), C(1,4), D(2,4) \perp$ **42.** A(2,4), B(5,4), C(3,2), D(0,8)**43.**  $A(-3,2), B(5,1), C(2,7), D(1,-1) \perp$ neither

- **44. Graphing Calculator** Use your graphing calculator to find the slope of  $\overrightarrow{AB}$  in Exercise 43. Enter the *x*-coordinates of *A* and *B* into the L<sub>1</sub> list of your list editor. Enter the *y*-coordinates into the L<sub>2</sub> list. In your **STAT** CALC menu select LinReg (ax + b). **ENTER** to find the slope *a*. Repeat to find the slope of  $\overrightarrow{CD}$ . Are  $\overrightarrow{AB}$  and  $\overrightarrow{CD}$  parallel, perpendicular, or neither?  $\bot$
- 45. Show that the diagonals of the figure at the right are congruent.
  See margin, p. 178.
- 46. Show that the diagonals of the figure at the right are perpendicular bisectors of each other. See margin, p.178.
- **47. a.** Graph the points P(2, 2), Q(7, 4), and R(3, 5). **a-c. See margin.** 
  - **b.** Find the coordinates of a point *S* that, along with points *P*, *Q*, and *R*, will form the vertices of a quadrilateral whose opposite sides are parallel. Graph the quadrilateral.



- **c.** Repeat part (b), finding a different point *S* and graphing the new quadrilateral.
- **48.** A triangle has vertices L(-5, 6), M(-2, -3), and N(4, 5). Write an equation for the line perpendicular to  $\overline{LM}$  that contains point N.  $y 5 = \frac{1}{3}(x 4)$

Lesson 3-7 Slopes of Parallel and Perpendicular Lines 179

R Q S (6, 1)

# c. The other possible locations for S are (-2, 3) and (8, 7).

# 4. Assess & Reteach



**1.** Are lines  $\ell_1$  and  $\ell_2$  parallel? Explain.



Yes; the lines have the same slope and different *y*-intercepts.

- 2. Are the lines x + 4y = 8 and 2x + 6y = 16 parallel? Explain. No; their slopes are not equal.
- 3. Write an equation in pointslope form for the line parallel to -18x + 2y = 7 that contains (3, 1). y - 1 = 9(x - 3)
- 4. Are the lines  $y = \frac{2}{3}x + 5$ and 3x + 2y = 10 perpendicular? Explain. Yes; the product of their slopes is -1.
- 5. Write an equation in point-slope form for the line perpendicular to  $y = -\frac{1}{6}x - 2$  that contains (-5, -8). y + 8 = 6(x + 5)

#### **Alternative Assessment**

Have students draw a pair of parallel lines and a pair of perpendicular lines on a coordinate plane and then use slopes to prove that the lines are parallel and perpendicular.

#### **Test Prep**

### Resources

For additional practice with a variety of test item formats:

- Standardized Test Prep, p. 193
- Test-Taking Strategies, p. 188
- Test-Taking Strategies with Transparencies

47.a-b. Answers may vary. Sample:

Interpretation of the second design of the secon



