Enigma

## Stem Sentences

## Number, addition and subtraction

- Composition of quantities and measures
- Wholes and parts
- Composition of numbers including place value
- Additive structures: aggregation and partitioning
- Additive structures: augmentation and reduction
- Odd and even
- Rounding
- Negative numbers
- Addition and subtraction strategies
- Written algorithms for addition and subtraction
- Decimals

| Comparison of quantities and measures |  |  |
| :---: | :---: | :---: |
| The $\qquad$ is heavier than the $\qquad$ <br> The $\qquad$ is lighter than the $\qquad$ . | Language | The elephant is heavier than the mouse. The mouse is lighter than the elephant. |
| The $\qquad$ is the same length as the $\qquad$ The $\qquad$ is the same length as the $\qquad$ | Language | The pen is the same length as the pencil. The pencil is the same length as the pen. |
| There are more $\qquad$ than $\qquad$ <br> There are fewer $\qquad$ than $\qquad$ . | Language | There are more people than hats. <br> There are fewer hats than people. |
| Wholes and parts |  |  |
| This is a whole $\qquad$ because I have all of it. | Language/ Structure | This is a whole apple because I have all of it. |
| This is not a whole $\qquad$ because I don't have all of it. | Language/ <br> Structure |  |
| This is not a whole $\qquad$ because I only have part of it. | Language/ <br> Structure | This is not a whole carrot because I don't have all of it. This is not a whole carrot because I only have part of it. |
| A whole can be split into two parts in lots of different ways. | Generalisation |  |

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| A whole is always bigger than a part of the whole. | Generalisation |  |
| :---: | :---: | :---: |
| A part is always smaller than its whole. | Generalisation |  |
| A whole can be split into more than two parts in lots of different ways. | Generalisation |  |
| This is a whole group of $\qquad$ because none are missing; I have all of them. | Structure | This is a whole group of cakes because none are missing; I have all of them. |
| This is not a whole group of $\qquad$ because we don't have all of them; some of them are missing. <br> This is not a whole group of $\qquad$ because only part of the $\qquad$ has $\qquad$ in. | Structure Structure | This is not a whole group of cakes because we don't have all of them; some of them are missing. <br> This is not a whole group of cakes because only part of the tray has cakes in. |
| This is the whole group of $\qquad$ . I have all of them. | Language/ Structure | Charlotte's group of six cars: <br> This is the whole group of Charlotte's cars. I have all of them. <br> There are four pencils in the whole group. There are three pencils in this part of the group |
| There are $\qquad$ in the whole group. There are $\qquad$ in this part of the group. | Structure |  |
| $\qquad$ is the whole; $\qquad$ is a part and $\qquad$ is a part. | Structure | 3 is the whole; <br> 2 <br> 1 is a part and 2 is a part. |
| A whole split into equal parts can be seen as both an additive and a multiplicative structure. <br> A whole split into unequal parts can be seen as an additive structure. | Generalisation | 4 4 43 4 5 |
| The whole minus the known part(s) is equal to the missing part. <br> The sum of the known part(s) plus the missing part is equal to the whole | Generalisation | 360 g   <br> $?$ 125 g 55 g |
| Composition of numbers inc. place value |  |  |
| The $\qquad$ represents all the counters. <br> The $\qquad$ represents the $\qquad$ counters. | Structure |  |



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| There are $\qquad$ tens which is $\qquad$ and $\qquad$ ones which is $\qquad$ . This makes $\qquad$ altogether. <br> The $\qquad$ represents $\qquad$ tens. It has a value of $\qquad$ <br> The $\qquad$ represents $\qquad$ ones. It has a value of $\qquad$ | Structure | There are two tens which is twenty and three ones which is three. This makes twenty-three altogether: 23. The ' 2 ' represents two tens. It has a value of twenty. The ' 3 ' represents three ones. It has a value of three. |
| :---: | :---: | :---: |
| All multiples of ten end with a zero. | Generalisation | Digits What it <br> means <br> 10 1 ten <br> 20 2 tens <br> 30 3 tens <br> 40 4 tens <br> 50 5 tens |
| We have ___ tens. We call this __. | Language/ structure |  |
| This is the number $\qquad$ . We write the $\qquad$ then the $\qquad$ . | Structure | This is the number forty-two. We write the four then the two. |
| This is $\qquad$ . Ten more than $\qquad$ is $\qquad$ $\qquad$ is ten more than $\qquad$ <br> This is $\qquad$ . Ten less than $\qquad$ is $\qquad$ $\qquad$ is ten less than $\qquad$ - | Structure |  |
| I know that $\qquad$ plus $\qquad$ is equal to $\qquad$ <br> So, $\qquad$ tens plus $\qquad$ tens is equal to $\qquad$ tens. | Structure | I know that 2 plus 5 is equal to 7 . <br> So, 2 tens plus 5 tens is equal to 7 tens. |

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| I know that $\qquad$ minus $\qquad$ is equal to $\qquad$ . <br> So, $\qquad$ tens minus $\qquad$ tens is equal to $\qquad$ tens. | Structure |  |
| :---: | :---: | :---: |
|  |  | I know that 5 minus 2 is equal to 3 . <br> So, 5 tens minus 2 tens is equal to 3 tens. |
| I know that $\qquad$ plus $\qquad$ is equal to ten so $\qquad$ plus $\qquad$ is equal to $\qquad$ . | Structure | I know that 6 plus 4 is equal to 10 so 16 plus 4 is equal to 20. |
| I know that $\qquad$ minus $\qquad$ is equal to ten so $\qquad$ minus $\qquad$ is equal to $\qquad$ | Structure | I know that 10 minus 3 is equal to 7 so 20 minus 3 is equal to 17. |
| To compare two digit numbers, we need to compare the tens digits; if the tens digits are the same, we need to compare the ones digits. | Generalisation structure |  |
| To compare three digit numbers, we need to compare the hundreds digit; if the hundreds digits are the same, we need to compare the tens digits; if the | Generalisation structure |  |


| tens digits are the same, we need to compare the ones digits. |  |  |
| :---: | :---: | :---: |
| To compare two numbers, we compare digits with the same place value, starting with the largest place value digit. | Generalisation |  |
| When we find ten more, the tens digit changes and the ones digit stays the same. <br> When we find ten less, the tens digit changes and the ones digit stays the same. | Generalisation |  |
| We had $\qquad$ tens and $\qquad$ ones. Ten more gives us $\qquad$ tens and $\qquad$ ones. | Structure |  |
| We had $\qquad$ tens and $\qquad$ ones. Ten less gives us $\qquad$ tens and $\qquad$ ones. | Structure |  |
| One part is ten, the other part is $\qquad$ and the whole is $\qquad$ . | Structure | One part is ten, the other part is 36 and the whole is 46. |
| There are one hundred ones in one hundred. | Structure |  |
| There are ten tens in one hundred. | Structure |  |
| One hundred is divided into $\qquad$ equal parts so each part/ division has a value of $\qquad$ _. | Structure | 100     <br> $?$ $?$ $?$ $?$  <br> One hundred is divided into four equal parts so each part has a value of 25 . |
| $\qquad$ plus $\qquad$ is equal to $\qquad$ so $\qquad$ tens plus $\qquad$ tens is equal to $\qquad$ tens. $\qquad$ plus $\qquad$ is equal to 100 . | Structure | 10  <br> 7 310 tens  <br> 7 tens 3 tens <br> 7 plus 3 is equal to 10 so 7 tens plus 3 tens is equal to 10 tens. 70 plus 30 is equal to 100 . |
| Ten minus $\qquad$ is equal to $\qquad$ So ten tens minus $\qquad$ tens is equal to $\qquad$ tens. 100 minus $\qquad$ is equal to $\qquad$ | Structure | 10  <br> 7 310 tens  <br> 7 tens 3 tens <br> 10 minus 3 is equal to 7 . So 10 tens minus 3 tens is equal to 7 tens. 100 minus 30 is 70 . |
| There are $\qquad$ groups of ten. There is $\qquad$ group of 100 and $\qquad$ more tens. There are $\qquad$ altogether. | Structure | There are 14 groups of ten. There is one group of 100 and 4 more tens. There are 140 altogether. |
| I know that $\qquad$ plus $\qquad$ is equal to $\qquad$ . (single digit addends) | Structure | I know that seven plus five is equal to twelve. So seven tens plus five tens is equal to twelve tens. 70 plus 50 is equal to 120 . |


| So $\qquad$ tens plus $\qquad$ tens is equal to $\qquad$ tens. (multiple-of-ten addends) $\qquad$ plus $\qquad$ is equal to one hundred and $\qquad$ . (number names) |  |  |
| :---: | :---: | :---: |
| I know that $\qquad$ minus $\qquad$ is equal to $\qquad$ . (bridging ten) <br> So $\qquad$ tens minus $\qquad$ tens is equal to $\qquad$ tens. (bridging ten tens) ten One hundred and $\qquad$ minus $\qquad$ is equal to $\qquad$ . (number names) | Structure | I know that twelve minus five is equal to seven. So twelve tens minus five tens is equal to seven tens. 120 minus 50 is equal to 70 . |
| There is $\qquad$ group of 100 and $\qquad$ more. There are $\qquad$ | Structure | There is 1 group of 100 and 24 more. There are one hundred and twenty-four. |
| $\qquad$ is $\qquad$ ones. $\qquad$ $\qquad$ hundreds and $\qquad$ ones. $\qquad$ $\qquad$ tens and $\qquad$ ones. $\qquad$ $\qquad$ hundreds, $\qquad$ tens and $\qquad$ ones. | Structure | 243 is 243 ones. <br> 243 is 2 hundreds and 43 ones. 243 is 24 tens and 3 ones. <br> 243 is 2 hundreds, 4 tens and 3 ones. |
| There are ten hundreds in one thousand. <br> There are one hundred tens in one thousand. <br> There are one thousand ones in one thousand. | Structure |  |
| hundred plus $\qquad$ hundred is equal to $\qquad$ hundred. <br> We know there are ten hundreds in one thousand, so $\qquad$ hundred plus $\qquad$ hundred is equal to $\qquad$ thousand $\qquad$ hundred. | Structure | Six hundred plus five hundred is equal to eleven hundred. We know there are ten hundreds in one thousand, so six hundred plus five hundred is equal to one thousand one hundred. |
| We know there are ten hundreds in one thousand, so $\qquad$ thousand $\qquad$ hundred is equal to $\qquad$ hundred. $\qquad$ hundred minus $\qquad$ hundred is equal to $\qquad$ hundred. |  | We know there are ten hundreds in one thousand, so one thousand one hundred is equal to eleven hundred. eleven hundred minus six hundred is equal to five hundred. |
| There are ten one thousands in tenthousand. <br> There are one hundred one hundreds in ten-thousand. <br> There are one thousand tens in tenthousand. <br> There are ten thousand ones in tenthousand. |  |  |

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| There are $\qquad$ and $\qquad$ . <br> We can write this as $\qquad$ plus $\qquad$ <br> The $\qquad$ represents the $\qquad$ <br> The $\qquad$ represents the $\qquad$ . | Structure | There are four open umbrellas and five closed umbrellas. We can write this as four plus five. <br> The four represents the four open umbrellas. <br> The five represents the five closed umbrellas. |
| :---: | :---: | :---: |
| $\qquad$ is equal to $\qquad$ plus $\qquad$ $\qquad$ plus $\qquad$ is equal to $\qquad$ $\qquad$ and $\qquad$ are the addends. $\qquad$ is the sum. | Structure | Five is equal to four plus one. Four plus one is equal to five. Four and one are the addends. Five is the sum. |
| Addend plus addend equals sum. Sum equals addend plus addend. | Language |  |
| Additive structures: augmentation and reduction |  |  |
| First... then... now... <br> See: <br> ncetm_mm_sp1_y1_se06_teach.pdf for lots more examples of how to use 'first... then... now' in the context of augmentation and reduction. | Language | First, four children were sitting on the bus. Then three more children got on the bus. Now seven children are sitting on the bus. <br> First, there were four children in the car. Then one child got out. Now there are three children in the car. |
| Odd and even numbers |  |  |
| $\qquad$ is made of pairs; it is an even number. $\qquad$ is not made of pairs; it is an odd number. | Structure/ Language | 6 is made of pairs; it is an even number. 7 is not made of pairs; it is an odd number. |
| Numbers that can be made out of groups of two are even numbers. Numbers that cannot be made out of groups of two are odd numbers. | Generalisa |  |

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| Even numbers can be partitioned into <br> two odd parts or two even parts. | Generalisation |
| :--- | :--- | :--- | :--- |


| ' $a$ ' is between $\qquad$ and $\qquad$ . <br> The previous multiple of one ten/ hundred/ thousand is $\qquad$ . The next multiple of one ten/ hundred/ thousand is $\qquad$ . ' $a$ ' is nearest to $\qquad$ ten/ hundred/ thousand. ' $a$ ' is $\qquad$ when rounded to the nearest ten/ hundred/ thousand. | Structure | previous <br> mutulio ef <br> 1,000 next <br> mutitio of <br> 1,000 <br> $1,000<1,321<2,000$  <br> 1321 is between 1000 and 2000. <br> The previous multiple of one thousand is 1000 . The next multiple of one thousand is 2000. <br> 1321 is nearest to 1000 . <br> 1321 is 1000 when rounded to the nearest thousand. |
| :---: | :---: | :---: |
| $\qquad$ is between $\qquad$ and $\qquad$ . $\qquad$ is the previous whole number. $\qquad$ is the next whole number. $\qquad$ is nearest to $\qquad$ $\qquad$ rounded to the nearest whole number is $\qquad$ | Structure | 3.4 is between 3 and 4. <br> 3 is the previous whole number. <br> 4 is the next whole number. <br> 3.4 is nearest to 3 . <br> 3.4 rounded to the nearest whole number is 3 . |
| When rounding to the nearest $\qquad$ , if the $\qquad$ digit is 4 or less we round down. If the $\qquad$ digit is 5 or more, we round up. | Generalisation | When rounding to the nearest thousand, if the hundreds digit is 4 or less we round down. If the hundreds digit is 5 or more, we round up. |
| The midpoint between/ of $\qquad$ and $\qquad$ is $\qquad$ , so the midpoint between/ of $\qquad$ thousand and $\qquad$ thousand is $\qquad$ . | Structure | The midpoint between ten and twenty is fifteen, so the midpoint <br> between ten-thousand and twenty-thousand is fifteen thousand. |
| $\qquad$ is greater/ less than $\qquad$ so $\qquad$ thousand is greater/ less than $\qquad$ thousand. | Structure | $\begin{aligned} & 54<58 \\ & 54000<58000 \end{aligned}$ <br> 58 is greater than 54 , so 58 thousand is greater than 54 thousand. |
| Negative numbers |  |  |
| Negative numbers are below/ less than zero. <br> Positive numbers are above/ greater than zero. | Generalisation |  |
| Negative numbers are to the left of zero. <br> Positive numbers are to the right of zero. | Generalisation |  |
| Zero is neither negative nor positive | Generalisation |  |
| For both positive and negative numbers, the larger the value of the number, the further away it is from zero. | Generalisation |  |
| For negative temperatures, the further away from zero it is, the colder the temperature. <br> For positive temperatures, the further away from zero it is, the warmer the temperature. (Can be adapted to other contexts) | Generalisation |  |

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| The difference between two numbers is always a positive number, regardless of whether the numbers are negative or positive. | Generalisation |  |
| :---: | :---: | :---: |
| If we add a positive number, the number gets higher/ greater. If we subtract a positive number, the number gets lower/ smaller. If we add a negative number, the number gets smaller/ lower. If we subtract a negative number, the number gets higher/ greater. | Generalisation | The Happiometer! <br> Add something positive (like chocolate!) Mood goes UP! <br> Take away something positive (like a break time) Mood goes down. <br> Add something negative (like a telling off) Mood goes down <br> Take away something negative (like the rain going away) Mood goes UP! |
| Addition and subtraction strategies |  |  |
| If we change the order of the addends, the sum remains the same. We can change the order of the addends and the sum remains the same. | Structure |  |
| Adding one gives one more. | Generalisation |  |
| Subtracting one gives one less. | Generalisation |  |
| Consecutive numbers have a difference of one. | Generalisation |  |
| When zero is added to a number, the number remains unchanged. | Generalisation |  |
| When zero is subtracted from a number, the number remains unchanged. | Generalisation |  |
| Subtracting a number from itself gives a difference of zero. | Generalisation |  |
| There are $\qquad$ and $\qquad$ <br> Altogether there are . $\qquad$ | Language | There are two red marbles, three blue marbles and five yellow marbles. Altogether, there are ten marbles. |
| When we add three numbers, the total will be the same whichever pair we add first. | Generalisation |  |

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| We can look for pairs of addends which sum to ten. | Generalisation |  |
| :---: | :---: | :---: |
| $\qquad$ plus $\qquad$ is equal to ten, then ten plus $\qquad$ is equal to $\qquad$ . | Structure | $7+3+4$ <br> Seven plus three is equal to ten, then ten plus four is equal to fourteen. |
| First I partition the $\qquad$ : $\qquad$ plus $\qquad$ is equal to $\qquad$ <br> Then $\qquad$ plus $\qquad$ is equal to ten... ...and ten plus $\qquad$ is equal to $\qquad$ . | Structure | First I partition the five: three plus 2 is equal to five. Then seven plus three is equal to ten... ...and ten plus two is equal to twelve. |
| There are $\qquad$ more $\qquad$ than $\qquad$ <br> There are $\qquad$ fewer $\qquad$ than $\qquad$ . | Structure | There are two more red cars than blue cars. There are two fewer blue cars than red cars. |
| The difference between the number of $\qquad$ and the number of $\qquad$ is $\qquad$ -. | Structure | The difference between the number of blue cars and the number of red cars is two. |
| The more we subtract, the less we are left with. <br> The less we subtract, the more we are left with. | Generalisation |  |
| The $\qquad$ represents the number of $\qquad$ <br> The $\qquad$ represents the number of $\qquad$ The $\qquad$ represents the difference between the number of $\qquad$ and the number of $\qquad$ , | Structure | $\square$ <br> The 8 represents the number of children. The 3 represents the number of pencils. The 5 represents the difference between the number of children and the number of pencils. |
| Subtraction is not commutative | Generalisation | 6-3 is not equal to 3-6. |
| To subtract $\qquad$ , we can subtract the $\qquad$ then subtract the $\qquad$ . | Structure |  <br> To subtract 23 . We can subtract the 20 then subtract the 3. |
| For a subtraction calculation where both numbers have the same ones | Generalisation |  |


| digit, the difference is a multiple of ten. |  |  |
| :---: | :---: | :---: |
| First we add: $\qquad$ plus $\qquad$ is equal to ... then we adjust: $\qquad$ minus $\qquad$ is equal to $\qquad$ |  | First we add: 52 plus 30 is equal to 82 ... then we adjust: 82 minus 1 is 81 . |
| For calculations that involve both additions and subtraction steps, we can add then subtract, or subtract then add; the final answer is the same. | Generalisation |  |
| The value of the expressions on each side of the equals sign must be equal. | Generalisation |  |
| If one addend is increased by an amount and the other addend is decreased by the same amount, the sum remains the same. | Generalisation | $\begin{aligned} & \mathbf{5 2 0}+\mathbf{2 9 0}=810 \\ & 10 \mid \downarrow+10 \\ & \downarrow+\quad+300=810 \\ & 510+ \end{aligned}$ |
| (connected with above) I have added $\qquad$ to this addend so I must subtract $\qquad$ from the other addend to keep the sum the same. | Structure | I have added ten to 520 so I must subtract ten from 290 to keep the sum the same. |
| If one addend is increased/ decreased by an amount and the other addend remains unchanged, the sum is also increased/ decreased by the same amount. | Generalisation |  |
| (connected with above) I've added/ subtracted $\qquad$ to/ from this addend and kept the other addend the same so I must add/ subtract $\qquad$ to/ from the sum. | Structure | I have added ten to 4 and kept the other addend the same so I must add ten to 7 also. |
| If the sum increases/ decreases by an amount and one addend has stayed the same, the other addend must increase/ decrease by the same amount. | Generalisation | $\begin{array}{r} 36+47=83 \\ +2 \\ 36+49=85 \end{array}$ |
| (connected with above) The sum has increased/ decreased by $\qquad$ ; one addend has stayed the same, so the other addend must increase/ decrease by $\qquad$ . | Structure | The sum has increased by 2; one addend has stayed the same, so the other addend must also increase by 2. |

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| If the minuend and the subtrahend are changed by the same amount, the difference remains the same. | Generalisation |  |
| :---: | :---: | :---: |
| I've added/ subtracted $\qquad$ to/ from the minuend and the subtrahend so the difference remains the same. | Structure | I've subtracted 1 from the minuend and the subtrahend so the difference remains the same. |
| In a balanced equation, If I add an amount to the minuend or subtrahend, I need to add the same amount to the subtrahend or minuend to keep the difference the same. In a balanced equation, if I subtract an amount from the minuend or subtrahend, I need to subtract the same amount from the subtrahend or minuend to keep the difference the same. | Generalisation |  |
| I've added $\qquad$ to the minuend/ subtrahend, so I need to add $\qquad$ to the subtrahend/ minuend to keep the difference the same. <br> I've subtracted $\qquad$ from the minuend/ subtrahend so I need to subtract $\qquad$ from the subtrahend/ minuend to keep the difference the same. | Structure | I've added 35 to the minuend so I need to add 35 to the subtrahend to keep the difference the same. |
| If a certain amount is added to the minuend and the subtrahend is kept the same, the difference must be increased by the same amount. | Generalisation |  |
| I've added $\qquad$ to the minuend and kept the subtrahend the same, so I have to add $\qquad$ to the difference. | Structure | I've added ten to the minuend and kept the subtrahend the same, so I have to add ten to the difference. |
| If the minuend is changed by an amount and the subtrahend is kept the same, the difference changes by the same amount. | Generalisation |  |
| I've subtracted $\qquad$ from the minuend and kept the subtrahend the same, so I must subtract $\qquad$ from the difference. | Structure | I've subtracted ten from the minuend and kept the subtrahend the same, so I must subtract ten from the difference. |
| If the minuend is kept the same and the subtrahend is increased/ decreased by an amount, the difference must decrease/ increase by the same amount. | Generalisation |  |
| I've kept the minuend the same and added/subtracted $\qquad$ to/ from the | Structure | I've kept the minuend the same and added ten to the subtrahend so I must subtract ten from the difference. |

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