

A study of the JWL equation of state parameters of dynamite for use in airblast models

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Abstract

Two separate blast tests were conducted inside a conventional, unreinforced, brick building scheduled to be demolished. The small cylindrical explosive charges (less than 9 kg each), composed of dynamite sticks bundled together, were placed inside the building and detonated (in separate events) to study the blast resistance of the structure. The pressures generated by the blasts were recorded using a high speed data acquisition system. To better understand the complex pressure loading caused by the blasts for use in structural response modelling, the authors have undertaken a study to computationally model the explosive detonations. Advanced computational modelling is of interest because most tabular and other simplified blast load analysis techniques are inaccurate for the case of a close-in (but outside the detonation products) blast produced by a cylindrical charge. This paper presents the results of two dimensional airblast simulations performed using CTH, a shock physics hydrocode written by Sandia National Laboratories. The Jones-Wilkins-Lee (JWL) equation of state (EOS) coefficients for dynamite available in the literature are reviewed and then adjusted to reflect the properties of the dynamite used in these tests. CTH simulations are compared to the measured blast pressures and impulses to assess the ability of adjusted EOS parameters to model currently available commercial dynamite.

Keywords: explosives, equation of state, airblast, bomb blast, impact and blast loading characteristics, interaction between computational and experimental results.



1 Introduction

The Department of Civil and Environmental Engineering at the University of North Carolina at Charlotte conducted two blast tests inside a conventional, unreinforced, brick building before its scheduled demolition. The experimental program was designed to serve two purposes. The first purpose was to study the blast performance of a non-purpose-built, conventional brick building that, by definition, possessed representative dead loads, non-ideal boundary conditions, and the inherent characteristics resulting from the design and construction practices in the United States in the 1940s. The second purpose of the experiment was to study the capabilities of various analytical techniques to predict blast pressures for close-in, non-hemispherical (or non-spherical) charges.

This scenario is of interest because it results in non-planar blast waves as opposed to the planar blast waves generated by distant explosions. USACE [1] contains guidance for the analysis of blast loads generated by cylindrical charges, but this data is only tabulated for a few explosives relevant to military weaponry. Data has not been generated for commercial explosives such as the dynamite used in this work. Typically, defense laboratories or the Department of Energy in the United States are tasked with characterizing explosives to support ongoing weapons related programs. Within the government explosives community, the characterization of an explosive is typically project specific, and dynamite is not widely used for military applications because more powerful and stable explosives are readily available. While the use of precisely manufactured TNT would have simplified the airblast modeling effort, logistical considerations led the authors to use dynamite in this experimental program.

This article reports the results of an analytical and experimental program in which sticks of commercial dynamite (Unimax, Dyno Nobel, Salt Lake City, Utah) were bundled together and detonated in two separate blast events. First, JWL EOS coefficients available in the literature for commercial dynamites are reviewed. This data will be modified using a density scaling technique to develop JWL coefficients for a previously uncharacterized dynamite, Unimax. The adjusted JWL coefficients will be used with CTH, a shock physics hydrocode written by Sandia National Laboratories, to simulate the airblasts created by the dynamite charges. The simulations will be used to assess the adequacy of the new JWL coefficients for Unimax by comparing simulated pressures and impulses to those measured during the experiments.

2 Commercial dynamite in the United States

Dyno Nobel is the only manufacturer of nitroglycerin dynamites in North America today. In the 1980s there were still several nitroglycerin dynamite manufacturers as evidenced by Cooper [2]. Of the commercially manufactured dynamites, Unigel (made by Hercules) was widely considered the standard gelatin dynamite. Dyno Nobel acquired Hercules in 1985 and began manufacturing Unigel as its own product. With the rising use of bulk explosives



like ANFO, the demand for dynamites decreased and Dyno Nobel became the sole manufacturer of nitroglycerin dynamites in North America.

Dyno Nobel currently manufactures two main nitroglycerin dynamite products, Unigel and Unimax. Their energetic and chemical properties are shown in Table 1. No test data was available regarding detonation pressure, so eqn (1) was used to compute it assuming the adiabatic gamma (Γ) was equal to 2.49.

$$P_{CJ} = \frac{\rho_0 D_{CJ}^2}{(\Gamma+1)} \quad (1)$$

In this equation ρ_0 is the explosive's unreacted density and D_{CJ} is the detonation velocity. The Unigel currently manufactured by Dyno Nobel is similar in density to that manufactured at the time of previous studies by other authors (see Table 2). In addition to Unigel, Dyno Nobel manufactures a more powerful dynamite called Unimax. Unimax is termed an extra gelatin dynamite by the manufacturer. The designation "extra" means that the composite explosive contains additional oxidizers. The "gelatin" designation refers to the nitroglycerin component which is combined with another agent to form a gel [2].

Table 1: Properties of Dyno Nobel dynamites from LeVan [3].

	Unimax	Unigel
Detonation Velocity (D_{CJ})	5856 m/s	4300 m/s*
Detonation Pressure (P_{CJ})	14.7 GPa**	6.89 GPa**
Unreacted Density (ρ_0)	1.50 g/cc	1.30 g/cc
Relative Weight Strength	1.20	1.09
Nitroglycerin Ether Extract	26.2 %	19.5 %
Ammonium Nitrate	39.2 %	67.0 %
Sodium Nitrate	25.6 %	7.40 %
Heat of Explosion (\approxenergy)	6.322 kJ/cc	5.191 kJ/cc

*Unigel's detonation velocity from Dyno Nobel proprietary computer code

**Values computed using eqn (1)

The primary quantities of interest when characterizing any explosive are the unreacted density and the two Chapman Jouguet (CJ) state parameters: detonation velocity (D_{CJ}) and detonation pressure (P_{CJ}). Table 2 shows that while Unigel's density has not varied considerably, there is a discrepancy between the manufacturer's detonation velocity (shown in Table 1) and that reported by other researchers. It should be noted that Unigel's detonation velocity in Table 1 was provided by the manufacturer as a minimum while Unimax's detonation velocity was experimentally determined by the manufacturer. This could partially explain the discrepancy between the two tables.

In addition to knowing the CJ state parameters for an explosive, an equation of state (EOS) is required to computationally model a blast. The Jones-Wilkins-Lee (JWL) EOS is one of the most commonly used due to its simplicity. The JWL EOS describes the adiabatic expansion of gaseous detonation products from

Table 2: Summary of CJ parameters for dynamites from other researchers.

Product Description	ρ_0 (g / cc)	P_{CJ} (GPa)	D_{CJ} (m / s)	Diameter (mm)	Ref.
Unigel	1.26	12.8	5760	Not Listed	[4]
Unigel	1.294	12.0	5477	Not Listed	[5]
Unigel	1.262	12.0	5760	Not Listed	[6]
Gelatin Dynamite	1.50	15.9*	6090	100	[7]
Permissible Dynamite	1.10	2.26*	2680	45	[7]
Ammonia Gelatin Dynamite	1.50	15.4*	5980	100	[8]
Extra Dynamite	1.36	6.55*	4100	100	[8]

*Value computed using eqn (1)

the CJ state. Although the JWL EOS is a mathematical abstraction of the thermochemical processes of detonation, it is sufficient for many engineering analyses and is easily implemented in hydrocodes. The standard form of the JWL EOS is given by Lee *et al.* [9]

$$P(V, E) = A \left[1 - \frac{\omega}{R_1 V} \right] e^{-R_1 V} + B \left[1 - \frac{\omega}{R_2 V} \right] e^{-R_2 V} + \frac{\omega E}{V} \quad (2)$$

In this equation, P is the pressure and A , B , R_1 , R_2 , and ω are the JWL coefficients, V is the relative volume which can be computed as ρ_0/ρ , where ρ is the density of the detonation products, and E is the energy. The coefficients for this EOS are derived from tests in which a cylinder of explosive encased in copper is detonated at one end. The cylinder wall velocity time history is recorded and compared to simulations, typically performed using LS-DYNA (LSTC, Livermore, CA). The simulations are performed iteratively, adjusting the input JWL coefficients until the simulated cylinder wall velocity or displacement matches the test data. Table 3 shows some of the JWL coefficients for Unigel dynamite found in the literature. In the table, all variables are as defined above and E_0 is the explosive's available chemical energy.

It is worth briefly discussing the notion of ideality. Penn *et al.* [6] define an ideal explosive as one in which there is a constant rate of energy release over a wide range of diameters while Souers *et al.* [10] defines an ideal explosive as one which follows Zel'dovich-von Neumann-Doring (ZND) theory and possesses a true CJ point under heavy confinement. Powerful military explosives like PETN are ideal explosives. Composite explosives like dynamite and ANFO typically do not display these characteristics. Penn *et al.* [6] noted that, while ANFO's behavior was highly complex and would require a more complex EOS, dynamite could be approximated as an ideal explosive and thus the JWL EOS could be used.

Table 3: Summary of available JWL coefficients for dynamite in literature.

	Unigel Penn <i>et al.</i> [6]	Unigel Hornberg [5]	Unigel Edwards <i>et al.</i> [4]
ρ_o (g/cc)	1.262	1.294	1.26
P_{CJ} (GPa)	12.0	12.0	12.8
D_{CJ} (m / s)	5760	5477	5760
E_o (kJ / cc)	5.1	5.1	4.04
Γ	2.49	Not Reported	2.49
A (GPa)	190.7	121.831	109.70
B (GPa)	7.58	1.857	7.58
R_1	4.4	3.60150	4.4
R_2	1.4	0.86185	1.4
ω	0.23	0.20	0.23
C (GPa)	0.627	0.549	Not Reported

It is interesting to note that the energy (or heat of explosion) provided by Dyno Nobel for Unigel in Table 1 is similar to the E_o value for two of the coefficient sets listed in Table 3. Penn *et al.* [6] explicitly state that their E_o value was based on the heat of formation of the detonation products at the CJ state, but Hornberg [5] and Edwards *et al.* [4] do not provide a clear indication of how they arrived at their energy values. E_o is important to the JWL formulation because it is used to make the energy of the JWL EOS consistent with the explosive's available energy and is directly correlated to the airblast output.

3 Density scaling JWL coefficients

The experimental program described in this paper made use of Unimax, for which no well developed EOS coefficients exist. One simple method of generating JWL coefficients for an uncharacterized explosive like Unimax is to use its density to scale the JWL coefficients of another similar explosive. There are, however, very few methods available for engineers to perform such a scaling procedure. For very small adjustments, one density based adjustment method, as presented in Souers *et al.* [10], may be used. Small density adjustments of this type are typically required when analyzing multiple shots of the same explosive during a test series. In Lee *et al.* [9], where the JWL EOS is first presented, the authors provide another method of scaling JWL coefficients based on density for changes on the order of 10%. While the density scaling used in this article is approximately 15%, this latter method was still employed to investigate its applicability. Although it would be possible to use advanced thermochemical equilibrium codes as another method of generating JWL coefficients, such tools are not generally available to the public.

The scaling procedure can be described as follows. The original Γ value, the new unreacted density, and the new detonation velocity are used to compute the new CJ pressure. The original E_o is linearly scaled by the ratio of new to original density to obtain the new E_o . The original values of R_1 , R_2 , Γ , and ω are used in

conjunction with the new values of E_o and P_{CJ} to solve three simultaneous equations that relate pressure, relative volume, and energy. The results of the solution of this system of equations are new values of A , B , and C . The full procedure is well documented in Lee *et al.* [9].

The three sets of JWL coefficients from the literature listed in Table 3 were compared to the Unigel currently manufactured by Dyno Nobel (see Table 1). The first two have similar energies (E_o) while the third is significantly lower. The third set was therefore discarded. The second set of coefficients from Hornberg [5] had unusual values for R_1 and R_2 , and this caused the adjustment method to produce a negative value for B , which was unacceptable. The second set was also discarded. The adjustment scheme described above was therefore directly applied to the JWL coefficients from Penn *et al.* [6]. While the manufacturer supplied heat of explosion and the JWL E_o for Unigel compare favourably, there is no indication that Unimax's E_o should also be closely related to the heat of explosion. Without any further knowledge, the original E_o for Unigel was scaled based on the density ratio, rather than directly specifying the energy. The results of the JWL coefficient scaling procedure are provided in Table 4. This set of adjusted JWL parameters will be used to model the airblast from the experimental program.

Table 4: Original and adjusted JWL coefficients.

	Unigel Penn <i>et al.</i> [6]	Adjusted Unimax
ρ_o (g/cc)	1.262	1.50
P_{CJ} (GPa)	12.0	14.7
D_{CJ} (m / s)	5760	5856
E_o (kJ / cc)	5.1	6.1
Γ	2.49	2.49
A (GPa)	190.7	234.4
B (GPa)	7.58	9.51
R_1	4.4	4.4
R_2	1.4	1.4
ω	0.23	0.23
C (GPa)	0.627	0.716

4 Blast tests

The dynamite charges were detonated in two separate rooms of an unreinforced brick masonry building. Figures 1 and 2 show plan views of Blast Chambers A and B, respectively. The drawings show the locations of the charge and sensors in each blast chamber; sensor elevations are measured relative to the finished floor of the chambers. In both locations, the chamber walls were instrumented with piezoelectric pressure transducers manufactured by PCB Piezotronics

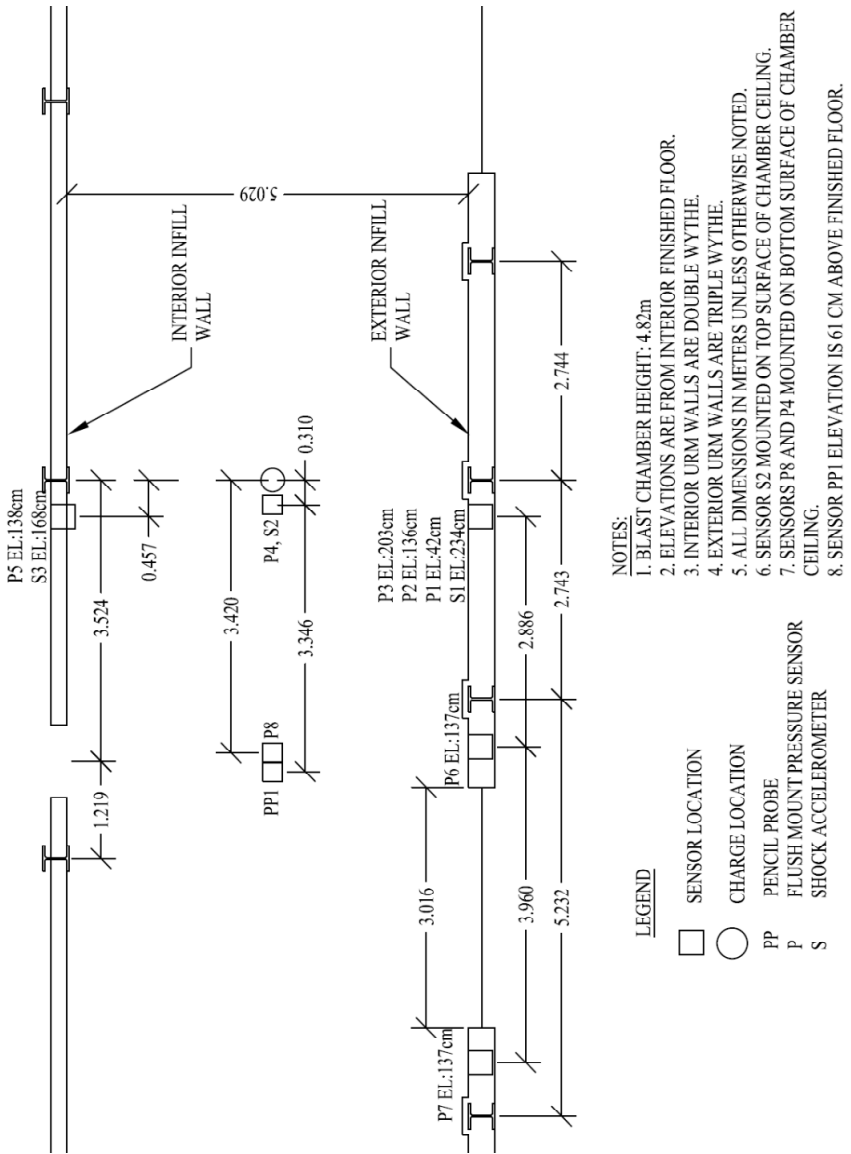


Figure 1: Plan view of Blast Chamber A.



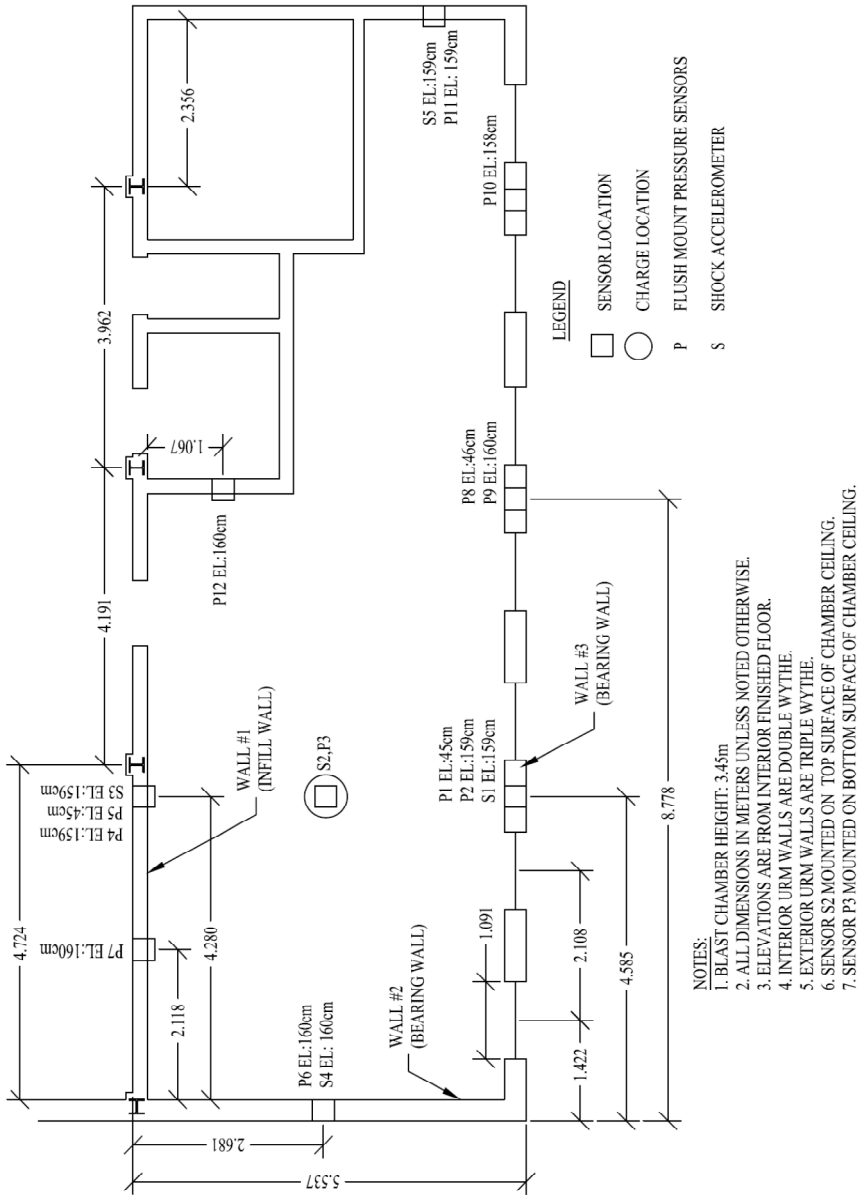


Figure 2: Plan view of Blast Chamber B.

(Depew, New York). The transducers were flush mounted on prefabricated metal plates mounted to the interior surface of the chamber walls. The instruments were powered with 4 milliamps of ICP excitation and data recorded

by National Instruments 4472 modules sampling at 100 kHz with 24 bit resolution.

The charge in Blast Chamber A was 6.53 kg and the charge in Blast Chamber B was 8.71 kg of Unimax sticks formed into upright cylinders. The charges were designed to damage, but not totally collapse the walls in each chamber. The height of both charges was approximately 41 cm. At detonation, the bottoms of the charges were at a height of 30 cm relative to the finished floor of the blast chamber. Both charges were detonated at their centers of mass with two instant electric blasting caps.

5 Airblast modelling

Airblast modelling was performed using CTH, a three dimensional shock physics hydrocode written and maintained by Sandia National Laboratories [11]. Simulations were performed using the built in JWL EOS. The detonation was modelled using the HEBURN feature of CTH. HEBURN allows the user to specify a detonation point and detonation velocity. The code then automatically handles the insertion of energy into the mesh to simulate detonation. In order to use the code's JWL EOS, the user supplies CTH with the constants A , B , ω , R_1 , R_2 , P_{CJ} , D_{CJ} , and ρ_o . The code then computes all other necessary quantities automatically and performs a check to ensure that the specified JWL coefficients are consistent with the specified CJ state.

The simulation was performed in 2D axisymmetric cylindrical coordinates. Thus the explosive was placed at the center of the mesh, and a symmetric boundary was defined through the center of the charge. This symmetry combined with the use of adaptive mesh refinement (AMR) permitted highly resolved simulations. AMR was controlled using two refinement indicators, one which tracked high pressure gradients and the other which predicted the kinetic energy errors associated with unrefinement. The explosive material and the air shock were both zoned at 0.16 cm. A convergence study showed that this meshing scheme provided reasonably accurate pressures and very accurate impulses. The air used in the simulations was adjusted to account for atmospheric conditions at the time of the test. There was significant venting area in both blast chambers, so gas phase pressures were not observed in the experimental data. Interior shock reflections were however observed. In order to facilitate the 2D modelling effort, pressure and impulse comparisons were made for only the first reflection of the shock front. Furthermore, the slight angle of incidence (approximately 10 degrees) of the sensors in shot A relative to the charge will be ignored as its effect on the results is relatively insignificant.

6 Results

Airblast simulations of the two experiments were performed using the JWL parameters listed in Table 4 and the modelling techniques described in the previous section. Tables 5 and 6 compare experimental and predicted pressures and impulses in each blast chamber. Note that experimental and predicted



impulses were computed as the time integrals of the pressure-time histories. The tables show that, in general, predicted and experimental impulses compared well. The average absolute impulse error was roughly 17 percent considering the comparisons in both blast chambers. Maximum reflected pressures, as expected, did not agree as well. On average, the error between experimental and predicted reflected pressures was 39 percent.

The highest observed impulse error was for sensor P1 in Blast Chamber B. Table 6 shows that CTH predicts almost 1.5 times the impulse recorded during the experiment. If one considers that charge B was almost 2.2 kg larger than charge A and the height of sensor P1 in each location was nearly the same, then it would be logical for the P1 sensor in shot B to record a higher impulse than in shot A. Looking at sensor P1 in Tables 5 and 6, however, this is clearly not the case. This would suggest an incomplete detonation of shot B or a malfunction of the P1 sensor for this shot. However, a definitive conclusion regarding the source of this error cannot be drawn from the experimental data alone.

Table 5: Comparisons of experimental and predicted pressures and impulses from Blast Chamber A. Cell size of 0.16 cm.

Sensor Location	Exp. Pressure (MPa)	Pred. Pressure (MPa)	Exp. Impulse (MPa ms)	Pred. Impulse (MPa ms)
P1	5.44	4.06	1.26	1.39
P2	2.33	1.09	0.628	0.552
P3	0.810	0.386	0.363	0.400
P5	2.30	1.17	0.738	0.572

Table 6: Comparisons of experimental and predicted pressures and impulses from Blast Chamber B. Cell size of 0.16 cm.

Sensor Location	Exp. Pressure (MPa)	Pred. Pressure (MPa)	Exp. Impulse (MPa ms)	Pred. Impulse (MPa ms)
P1	11.0	7.79	1.26	1.90
P2	1.50	1.21	0.593	0.614
P4	1.85	1.21	0.627	0.614
P6	1.06	0.579	0.655	0.496

7 Conclusion

The JWL coefficients for dynamite available in the literature were reviewed and the closest match to currently produced dynamites was selected. This set of JWL coefficients was used along with a density adjustment procedure to arrive at a set of JWL coefficients for a previously uncharacterized dynamite, Unimax. The adequacy of the JWL coefficients adjusted to model Unimax was examined by

pressure and impulse comparisons to the experimental results of two blast tests. Tables 5 and 6 show that experimental and predicted impulses compared well, but reflected pressures did not.

Typically, maximum reflected pressures are more difficult to accurately simulate than reflected impulses since a much finer mesh is required to capture peak reflected pressures. However, a number of other factors could have contributed to the error in pressure comparisons. First, the JWL coefficients for Unimax were based on scaling Unigel's parameters. While Unigel and Unimax are both nitroglycerin dynamites, Table 1 shows that the makeup of their oxidizers (ammonium nitrate and sodium nitrate) varies considerably. The scaling procedure used in this work can only account for the effect of density and thus chemical makeup will not be taken into account unless separately considered. Another possible contributing factor is that the charges were bundled sticks of dynamite, rather than a large diameter monolithic charge. The behaviour of a bundled charge relative to the typical case of a monolithic charge has not been investigated.

Despite the pressure errors observed in these simulations, the use of CTH, coupled with the modified JWL coefficients for Unimax, provided reasonably accurate predictions of the impulses observed during the experimental program. Even though a more accurate JWL definition could better model blast pressures, the JWL coefficients presented in this work are sufficient for engineers to use in computing blast loads for mechanics analyses that are impulse dominated.

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