

## LEARNER OUTCOME(S)

- Students will be able to recognize that some expressions can be rewritten utilizing exponents to condense and assist in evaluation.
- Students will be able to simplify independent exponential functions and expressions with exponents.
- Students will be able to demonstrate (85\%) accuracy in simplifying exponential functions and expressions on lesson quiz.


## ASSESSMENT TOOLS/METHODS

## Formative:

- Verbal check-in with students as they are working on warm-up - i.e. circulating the groups as students are working out the problem. Gauge if students are discussing during warm-up or if extra directives are needed.
- Offer individual, group or class assistance if needed. For example, remind students of PEMDAS
- Review concepts as a class for accuracy and areas of difficulty, if need-be.
- Provide more practice problems in form of worksheets if group/individual needs more time. Select and print any worksheet deemed appropriate from www.mathdrills.com.
Summative:
- Collect quizzes and grade/check for accuracy.
- If utilized, collect homework next class and grade.

Next Steps:

- Incorporate exponents into multistep algebraic equations or begin scientific notation.
- Introduce scientific notation (under resources) - optional.


## LEARNER PRIOR KNOWLEDGE:

- Terms: exponents, order of operations.
- Math concepts: PEMDAS; math operations (addition, subtraction, multiplication, division).


## INSTRUCTIONAL ACTIVITIES

1. Warm-up activity: Pair students in groups of 3 or 4 . Pose this problem on the board: $3+2 \times 2 \times 2 \times 2 \times 2-4 \div 2$
2. Have students solve the problem individually then share their solutions with the other members of their group. Groups should discuss and compare their answers and approaches for solving the problem.
3. Student groups should select one answer from the members that they feel is correct (or most likely to be correct). When all groups make a selection, have a student from each group write their selected answer on the board.
4. Teacher identifies correct answers or shares with class correct answer to problem. (The answer is 33 when utilizing order of operations). Provide students the opportunity to voice their misconceptions or issues in the solving process.
5. Using your own knowledge, introduce the term exponent to the students. (Optional definitions: a quantity that is raised by a power; or, a symbol that is written above to the right of a number to indicate how many times the number should be multiplied by itself).
6. Utilize a class volunteer, or do yourself - write an example of an exponent. Then have the class verbally indicate how to write it out. (Example: $4^{3}$ is $4 \times 4 \times 4$ ).
7. Refocus class' attention to original warm-up problem. Inquire to the class if there is any part of the problem that can be re-written utilizing the exponent function. Write out $3+2{ }^{\wedge} 5-4 \div 2$ on the board. Have students individually try to solve the problem. Discuss the difference solving the original problem versus the rewritten problem.
8. Video Lesson - play MuchoMath Exponents video.

Teacher can play video to class via projector or students can watch the video individually on the computer using headphones. Alternatively, students can be paired to watch video together if space allows due to sound.
9. Teacher choice: distribute Optional In-Class Practice Worksheet Exponents (attached) to students and allow them to complete it either individually or, in the interest of differentiating for the varied levels in the

## RESOURCES

White/chalkboard/chart paper (choose one)

Student paper for in-class exercises

Classroom projector with speakers that can hookup to a laptop/computer with internet for MuchoMath video lesson. Or, computer lab with sufficient internet accessible computers and headphones for students to watch MuchoMath video lesson independently or in pairs

MuchoMath Exponents Video Lesson, accessible here: https://www.youtube.com/watch?v=i 1LVdI8MVs

Student copies of Optional In-Class Practice Worksheet (attached)

Student copies of Exponent Quiz (attached)

- Quiz 1 Exponents - Beginner
- Quiz 2 Exponents - Advanced

Answer Key Quiz 1 Exponents - Beginner (attached)
Answer Key Quiz 2 Exponents - Advanced (attached)

Student copies of Teacher-Generated Supplemental Practice worksheets. Retrieved from: http://www.k5learning.com/free-math-worksheets/sixth-grade-6/exponents (Teacher can utilize link to create a class appropriate worksheet. Site allows for teacher to

|  | classroom, in structured pairs which allow advanced students to work with struggling students. <br> 10. Practice quiz: pass out Exponents Quiz (attached) based upon student comfort with concepts (either Beginner or Advanced). Allow students to complete quiz individually to gauge acquisition of knowledge. <br> 11. Optional: pass out Teacher-Generated Supplemental Practice homework worksheets, which can be tailored to the class's unique needs on the website http://www.k5learning.com/free-math-worksheets/sixth-grade6/exponents as extra take-home practice or homework. <br> 12. Collect homework and grade/check for accuracy and understanding of new concepts. <br> 13. Next step: Introduce the concept of Scientific Notation by having class view Khan Academy Scientific Notation video. | level worksheets based upon student/class abilities) <br> Student copies of Vocabulary Sheet - Exponents (attached) <br> Khan Academy Video: Scientific Notation Introduction. Retrieved from: <br> https://www.khanacademy.org/math/pre- <br> algebra/exponents-radicals/scientific- <br> notation/v/scientific-notation-old <br> Student copies of Scientific Notation Practice Worksheet (attached) |
| :---: | :---: | :---: |
|  | DIFFERENTIATION (options) <br> - Distribute Vocabulary Sheet - Exponents with terms and definitions to students who appear to be struggling. <br> - Video lesson: teacher can play video on large screen for entire class; students can watch video individually on a computer. <br> - Pairing: students can be paired to watch the lesson together; (teacher preference to pair same level or low with high-level). <br> - Higher level option: advanced quiz, homework options via website in resources. <br> - Circulate room to provide additional assistance throughout activities/exercises. |  |

## In-Class Practice Worksheet

## Exponents

## The rule of exponents

1. $2^{2} \times 2^{3}=2 \times 2 \times 2 \times 2 \times 2=$
2. $2^{5} \div 2^{3}=\frac{2 \times 2 \times Z \times Z \times Z}{Z \times Z \times Z}=2 \times 2=$
3. $\left(2^{2}\right)^{3}=2^{2} \times 2^{2} \times 2^{2}=$

Rule:

Rule:

Rule:

The number being raised to a power ( 2 in this case) is called the base.
Note: You can only apply these rules to numbers involving the same base.
So, for example, you cannot apply the rules of exponents to $3^{2}+2^{3}$

Try these:
Ex1

Ex2
$3^{9} \div 3^{4}=$

Ex5
Ex6

Negative Exponents
$2^{-1}=$
$3^{-2}=$
$2^{-4}=$
$4^{-3}=$

Now consider $2^{3} \times 2^{-3}=$
So,

And generally,

## QUIZ 1: EXPONENTS

Name: $\qquad$

Powers and Exponents
Express the following as an exponent: 9•9•9•9•9
a) $9^{9}$
b) $9^{5}$
c) $5^{9}$
d) $5^{5}$
1.

Powers and Exponents
Express the following as an exponent:
$-12 \cdot 12 \cdot a \cdot a \cdot a$
a) $-12^{2} \cdot a^{3}$
b) $(-12)^{2} \cdot a^{3}$
c) $-(12 a)^{5}$
d) $-12^{3} \cdot a^{5}$
2.

## QUIZ 1 EXPONENTS

Powers and Exponents
Express the following as a product of terms:
$(-z)^{3} \cdot 19^{3}$
a) $-z \cdot-z \cdot-z \cdot 19 \cdot 19 \cdot 19$
b) $-z \cdot z \cdot z \cdot 19 \cdot 19 \cdot 19$
c) $-3 z \cdot 19 \cdot 19 \cdot 19$
d) $-z \cdot z \cdot 19 \cdot 19$
3.

## Powers and Exponents

Express the following as a product of terms:
$8^{2} \cdot x^{2} \cdot 11^{4}$
a) $8 \cdot 8 \cdot x \cdot x \cdot 11 \cdot 11 \cdot 11 \cdot 11 \cdot 11$
b) $8 \cdot x \cdot 11 \cdot 11 \cdot 11 \cdot 11$
c) $8 \cdot 8 \cdot 8 \cdot x \cdot x \cdot 11 \cdot 11 \cdot 11 \cdot 11$
d) $8 \cdot 8 \cdot x \cdot x \cdot 11 \cdot 11 \cdot 11 \cdot 11$
4.

## QUIZ 1 EXPONENTS

Powers and Exponents
Simplify the following:
$6^{4} \cdot 6^{6}$
a) $6^{24}$
b) $6^{10}$
c) $6^{3}$
-d) $10^{6}$
5.

Powers and Exponents
Simplify the following:
$z^{2} \cdot z^{3} \cdot y^{2}$
a) $z^{5} \cdot y^{2}$
b) $z^{6} \cdot y^{2}$
c) $5 z \cdot 2 y$

- d) $(z y)^{7}$

6. 

## QUIZ 1 EXPONENTS

Powers and Exponents
Simplify the following:
$\frac{31^{5}}{31^{4}}$
a) $31^{2}$
b) $31^{20}$
c) $31^{9}$
d) 31
7.

1. $B$
2. $A$
3. A
4. D
5. B
6. D
7. B

MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.
Simplify the expression. Use positive exponents. Assume variables represent nonzero real numbers.

1) $6^{4} \cdot 6^{5}$
A) 620
B) $6^{9}$
C) $36^{9}$
D) $36^{20}$
2) $\left(-5 p^{4}\right)\left(-8 p^{3}\right)$
A) $40 p^{7}$
B) $40 p^{12}$
C) $-40 p^{12}$
D) $-40 p^{7}$

Use the power rules for exponents to simplify. Write the answer in exponential form.
3) $9(r t)^{5}$

1) $\qquad$
2) $\qquad$
3) $\qquad$
4) $\qquad$
A) $3^{6}$
B) $-3^{9}$
C) $3^{9}$
D) $-3^{6}$
C) $95 r^{5}+5$
D) $9 r^{5} t^{5}$
B) $9 r^{5} t$
A) $9 \mathrm{rt}{ }^{5}$
,
D

Evaluate.
5) $(-11)^{0}+(-3)^{0}$
4) $\left(-3^{3}\right)^{3}$
A) -2
B) -14
C) 0
D) 2

Evaluate the expression.
6) $(-5)^{-4}$
6) $\qquad$
A) $-\frac{1}{625}$
B) 625
C) $\frac{1}{625}$
D) -625

## Perform the division.

7) $\left(6 m^{2}+13 m-15\right) \div(m+3)$
A) $m-5$
B) $6 m+5$
C) $6 m-5$
D) $6 m-5+\frac{4}{m-5}$
8) 
9) $\qquad$
$\qquad$

Perform the indicated operation.
8) $\left(7+6 x^{3}+8 x^{5}-4 x^{4}\right)+\left(-5 x^{4}+2 x^{3}-2+7 x^{5}\right)$
A) $2 x^{5}+2 x^{4}+6 x^{3}+3$
A) $16 x^{9}-7 x^{8}+12 x^{7}+1$
B) $15 x^{5}-9 x^{4}+8 x^{3}+5$
D) $15 x^{10}-9 x^{8}+8 x^{6}+5$
9) $\left(4 x^{7}+7 x^{9}+6-2 x^{8}\right)-\left(-5-5 x^{8}+9 x^{9}+8 x^{7}\right)$
B) $-2 x^{9}+3 x^{8}-4 x^{7}+11$
D) $-2 x^{9}-7 x^{8}+12 x^{7}+1$

## ANSWER KEY - QUIZ 2 ADVANCED

1.B
2.A
3.A
4.D
5.B
6.D
7.B

Variables - a factor or quantity that can vary, or change; represented in math by a letter such as $x$ or $y$

Numbers - an arithmetical value expressed by a symbol or word, represents a quantity

Operators - addition, subtraction, multiplication, and division symbols
Exponents - a quantity representing the power a given number or expression is to be raised

Parenthesis - ( ), a pair of rounded brackets used to mark off a mathematical number or expression

Expression - numbers and symbols with operators ( $+,-, x, /$ ) grouped together to show the value of something

Algebraic Expression - a mathematical phrase that contains numbers, variables and operators

PEMDAS - Acronym for "Please Excuse My Dear Aunt Sally" to help learners remember the order to work through/solve operations. The order of operations should be parenthesis first (); exponents second; multiplication and division third from left to right; and addition and subtraction last from left to right

## MATH HANDBOOK TRANSPARENCY MASTER

## Scientific Notation

Scientists need to express small measurements, such as the mass of the proton at the center of a hydrogen atom ( 0.000000000000000000000000001673 kg ), and large measurements, such as the temperature at the center of the Sun ( 15000000 K ). To do this conveniently, they express the numerical values of small and large measurements in scientific notation, which has two parts.


Thus, the temperature of the Sun, 15 million kelvins, is written as $1.5 \times 10^{7} \mathrm{~K}$ in scientific notation.

Positive Exponents Express 1234.56 in scientific notation.
1234.56

Each time the decimal place is moved one place to the left,

$$
\begin{aligned}
& 1234.56 \times 10^{0}=123.456 \times 10^{1} \\
& 123.456 \times 10^{1}=12.3456 \times 10^{2} \\
& 12.3456 \times 10^{2}=1.23456 \times 10^{3} \\
& 1.23456 \times 10^{3}
\end{aligned}
$$

the exponent is increased by one.

Negative Exponents Express 0.00657 in scientific notation.
0.00657

Each time the decimal place is moved one place to the right, $0.00657 \times 10^{0}=0.0657 \times 10^{-1}$
$0.0657 \times 10^{-1}=0.657 \times 10^{-2}$
$0.657 \times 10^{-2}=6.57 \times 10^{-3}$
$6.57 \times 10^{-3}$
the
exponent is decreased by one.
$\qquad$
$\qquad$

## MATH HANDBOOK TRANSPARENCY WORKSHEET

## Scientific Notation

Use with Appendix B, Scientific Notation

1. Express each of the following numbers in scientific notation.
a. 230
b. 5601
c. 14100000
d. 56 million
e. $2 / 10$
f. 0.45013
g. 0.089
h. 0.00026
i. 0.000000698
j. 12 thousandth
2. Express each of the following measurements in scientific notation.
a. speed of light in a vacuum, $299792458 \mathrm{~m} / \mathrm{s}$
b. number of seconds in a day, 86400 s
c. mean radius of Earth, 6378 km
d. density of oxygen gas at $0^{\circ} \mathrm{C}$ and pressure of $101 \mathrm{kPa}, 0.00142 \mathrm{~g} / \mathrm{mL}$
e. radius of an argon atom, 0.000000000098 m

## SCIENTIFIC NOTATION

$\qquad$

Scientists very often deal with very small and very large numbers, which can lead to a-pf confusion when counting zeros! We have learned to express these numbers as powers vi 10 . Scientific notation takes the form of $\mathrm{M} \times 10^{n}$ where $1 \leq \mathrm{M}<10$ and " $n$ " represents the number of decimal places to be moved. Positive $n$ indicates the standard form is a large number. Negative n indicates a number between zero and one.

Example 1: Convert 1,500,000 to scientific notation. We move the decimal point so that there is only one digit to its left, a total of 6 places.

$$
1,500,000=1.5 \times 10^{6}
$$

Example 2: Convert 0.000025 to scientific notation. For this, we move the decimal point 5 places to the right.

$$
0.000025=2.5 \times 10^{-5}
$$

(Note that when a number starts out less than one, the exponent is always negative.)

Convert the following to scientific notation.

1. $0.005=$ $\qquad$
2. $5,050=$ $\qquad$
3. $1,000=$ $\qquad$
4. $1,000,000=$ $\qquad$
5. $0.25=$ $\qquad$
6. $0.025=$ $\qquad$
7. $0.0008=$ $\qquad$
8. $0.0025=$
$\qquad$
9. $500=$ $\qquad$
10. $5,000=$ $\qquad$

Convert the following to standard notation.

1. $1.5 \times 10^{3}=$ $\qquad$
2. $1.5 \times 10^{-3}=$ $\qquad$
3. $3.35 \times 10^{-1}=$ $\qquad$
4. $1.2 \times 10^{-4}=$ $\qquad$
5. $3.75 \times 10^{-2}=$ $\qquad$ 8. $1 \times 10^{4}=$ $\qquad$
6. $3.75 \times 10^{2}=$ $\qquad$ 9. $1 \times 10^{-1}=$ $\qquad$
7. $2.2 \times 10^{5}=$ $\qquad$
$\qquad$

## Operations with Scientific Notation

## Addition and Subtraction

Before numbers in scientific notation can be added or subtracted, the exponents must be equal.

$\left(3.4 \times 10^{2}\right)+\left(4.57 \times 10^{3}\right)=\left(0.34 \times 10^{3}\right)+\left(4.57 \times 10^{3}\right)$


The decimal is moved

to the left to increase $=(0.34+4.57) \times 10^{3}$ the exponent.

$$
=4.91 \times 10^{3}
$$

## Multiplication

When numbers in scientific notation are multiplied, only the number is multiplied. The exponents are added.


## Division

When numbers in scientific notation are divided, only the number is divided. The exponents are subtracted.


$$
=6.00 \times 10^{3}
$$

$\qquad$

## Operations with Scientific Notation

## Use with Appendix B, Operations with Scientific Notation

1. Perform the following operations and express the answers in scientific notation.
a. $\left(1.2 \times 10^{5}\right)+\left(5.35 \times 10^{6}\right)$
b. $\left(6.91 \times 10^{-2}\right)+\left(2.4 \times 10^{-3}\right)$
c. $\left(9.70 \times 10^{6}\right)+\left(8.3 \times 10^{5}\right)$
d. $\left(3.67 \times 10^{2}\right)-\left(1.6 \times 10^{1}\right)$
e. $\left(8.41 \times 10^{-5}\right)-\left(7.9 \times 10^{-6}\right)$
f. $\left(1.33 \times 10^{5}\right)-\left(4.9 \times 10^{4}\right)$
2. Perform the following operations and express the answers in scientific notation.
a. $\left(4.3 \times 10^{8}\right) \times\left(2.0 \times 10^{6}\right)$
b. $\left(6.0 \times 10^{3}\right) \times\left(1.5 \times 10^{-2}\right)$
c. $\left(1.5 \times 10^{-2}\right) \times\left(8.0 \times 10^{-1}\right)$
d. $\frac{7.8 \times 10^{3}}{1.2 \times 10^{4}}$
e. $\frac{8.1 \times 10^{-2}}{9.0 \times 10^{2}}$
f. $\frac{6.48 \times 10^{5}}{\left(2.4 \times 10^{4}\right)\left(1.8 \times 10^{-2}\right)}$



