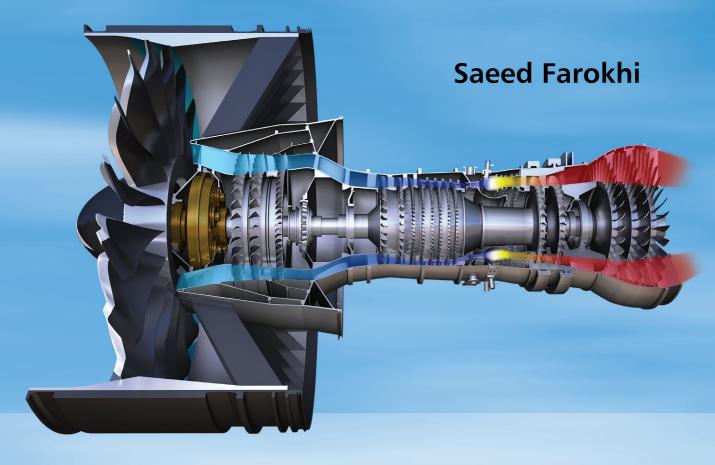
Aircraft Propulsion

Second Edition





Aircraft Propulsion

Aircraft Propulsion

Second Edition

SAEED FAROKHI, PhD

Professor Aerospace Engineering Department The University of Kansas, USA

WILEY

This edition first published 2014 © 2014 John Wiley & Sons Ltd

Registered office

John Wiley & Sons Ltd, The Atrium, Southern Gate, Chichester, West Sussex, PO19 8SQ, United Kingdom

For details of our global editorial offices, for customer services and for information about how to apply for permission to reuse the copyright material in this book please see our website at www.wiley.com.

The right of the author to be identified as the author of this work has been asserted in accordance with the Copyright, Designs and Patents Act 1988.

All rights reserved. No part of this publication may be reproduced, stored in a retrieval system, or transmitted, in any form or by any means, electronic, mechanical, photocopying, recording or otherwise, except as permitted by the UK Copyright, Designs and Patents Act 1988, without the prior permission of the publisher.

Wiley also publishes its books in a variety of electronic formats. Some content that appears in print may not be available in electronic books.

Designations used by companies to distinguish their products are often claimed as trademarks. All brand names and product names used in this book are trade names, service marks, trademarks or registered trademarks of their respective owners. The publisher is not associated with any product or vendor mentioned in this book.

Limit of Liability/Disclaimer of Warranty: While the publisher and author have used their best efforts in preparing this book, they make no representations or warranties with respect to the accuracy or completeness of the contents of this book and specifically disclaim any implied warranties of merchantability or fitness for a particular purpose. It is sold on the understanding that the publisher is not engaged in rendering professional services and neither the publisher nor the author shall be liable for damages arising herefrom. If professional advice or other expert assistance is required, the services of a competent professional should be sought.

Library of Congress Cataloging-in-Publication Data

Farokhi, Saeed.
Aircraft propulsion / Saeed Farokhi. – Second edition. pages cm
Includes bibliographical references and index.
ISBN 978-1-118-80677-7 (hardback)
1. Airplanes–Jet propulsion. 2. Airplanes–Motors–Design and construction. I. Title. TL709.F34 2014
629.134'35–dc23

2014001461

A catalogue record for this book is available from the British Library.

ISBN 9781118806777

Set in 10/12pt Times by Aptara Inc., New Delhi, India

I dedicate this book to my lovely grandchildren:

Sophia Sasha Sydney Melody

Table of Contents

	Preface to the Second Edition Preface		
Noi	mencl	ature	xxiii
1			
∎ Intr	oduct	tion	1
1.1	Histor	ry of the Airbreathing Jet Engine, a Twentieth-Century	
	Inven	tion—The Beginning	1
1.2	Innov	ations in Aircraft Gas Turbine Engines	4
	1.2.1	Multispool Configuration	4
	1.2.2	Variable Stator	5
	1.2.3	Transonic Compressor	5
	1.2.4	Low-Emission Combustor	6
	1.2.5	Turbine Cooling	7
	1.2.6	Exhaust Nozzles	8
	1.2.7	Modern Materials and Manufacturing Techniques	8
1.3		Engine Concepts	10
	1.3.1	Advanced Turboprop (ATP) and Geared Turbofan (GTF)	10
	1.3.2	Advanced Airbreathing Rocket Technology	11
	1.3.3	Wave Rotor Topping Cycle	12
		1.3.3.1 Humphrey Cycle versus Brayton Cycle	12
	1.3.4	8 ()	14
	1.3.5	Millimeter-Scale Gas Turbine Engines: Triumph of MEMS and Digital Fabrication	14
	1.3.6	Combined Cycle Propulsion: Engines from Takeoff to Space	14
1.4		Vehicles	16
1.5	Summary		
1.6		map for the Second Edition	16 18
	rences		19
Prob			20

2 Compressible Flow with Friction and Heat: A Review 21 2.1 Introduction 21 2.2 A Brief Review of Thermodynamics 22 2.3 Isentropic Process and Isentropic Flow 27 2.4 28 Conservation Principles for Systems and Control Volumes 2.5 Speed of Sound & Mach Number 35 Stagnation State 2.6 38 2.7 Quasi-One-Dimensional Flow 41 2.8 Area-Mach Number Relationship 44 2.9 Sonic Throat 45 2.10 Waves in Supersonic Flow 49 2.11 50 Normal Shocks 2.12 **Oblique Shocks** 54 2.13 **Conical Shocks** 60 2.14 **Expansion Waves** 63 2.15 Frictionless, Constant-Area Duct Flow with Heat Transfer 67 2.16 Adiabatic Flow of a Calorically Perfect Gas in a Constant-Area Duct 77 with Friction Friction (Drag) Coefficient $C_{\rm f}$ and D'Arcy Friction Factor $f_{\rm D}$ Dimensionless Parameters 91 2.17 2 18 01

2.18	Dimensionless Parameters	91
2.19	Fluid Impulse	95
2.20	Summary of Fluid Impulse	102
Refere	ences	103
Problems		103

Engine Thrust and Performance Parameters			113
3.1	Introc	luction	113
	3.1.1	Takeoff Thrust	119
3.2	Instal	led Thrust—Some Bookkeeping Issues on Thrust and Drag	119
3.3	Engin	e Thrust Based on the Sum of Component Impulse	124
3.4	Rocke	et Thrust	128
3.5	Airbreathing Engine Performance Parameters		
	3.5.1	Specific Thrust	129
	3.5.2	Specific Fuel Consumption and Specific Impulse	130
	3.5.3	Thermal Efficiency	131
	3.5.4	Propulsive Efficiency	134
	3.5.5	Engine Overall Efficiency and Its Impact on Aircraft Range and	
		Endurance	137
3.6	Mode	rn Engines, Their Architecture and Some Performance	
	Chara	icteristics	140
3.7	Sumn	nary	143
Refer	ences		144
Proble	ems		144

s Turb	ine En	igine Cycle Analysis
Intro	luction	
The (Gas Gene	rator
Aircr	aft Gas T	'urbine Engines
4.3.1	The Tu	rbojet Engine
	4.3.1.1	The Inlet
	4.3.1.2	The Compressor
	4.3.1.3	The Burner
	4.3.1.4	The Turbine
	4.3.1.5	The Nozzle
	4.3.1.6	Thermal Efficiency of a Turbojet Engine
	4.3.1.7	Propulsive Efficiency of a Turbojet Engine
	4.3.1.8	The Overall Efficiency of a Turbojet Engine
	4.3.1.9	Performance Evaluation of a Turbojet Engine
4.3.2		rbojet Engine with an Afterburner
	4.3.2.1	Introduction
	4.3.2.2	Analysis
	4.3.2.3	Optimum Compressor Pressure Ratio for Maximum (Ideal) Thrust Turbojet Engine with Afterburner
4.3.3	The Tu	rbofan Engine
	4.3.3.1	Introduction
	4.3.3.2	Analysis of a Separate-Exhaust Turbofan Engine
	4.3.3.3	Thermal Efficiency of a Turbofan Engine
	4.3.3.4	Propulsive Efficiency of a Turbofan Engine
4.3.4	Ultra-H	ligh Bypass (UHB) Turbofan Engines
Anal	ysis of a l	Mixed-Exhaust Turbofan Engine with an Afterburner
4.4.1	Mixer	
4.4.2	Cycle A	Analysis
	4.4.2.1	Solution Procedure
The 7	Turboproj	p Engine
4.5.1	Introdu	ction
4.5.2	Propelle	er Theory
	4.5.2.1	Momentum Theory
	4.5.2.2	Blade Element Theory
4.5.3	Turbop	rop Cycle Analysis
	4.5.3.1	The New Parameters
	4.5.3.2	Design Point Analysis
	4.5.3.3	Optimum Power Split Between the Propeller and the Jet
Sumr	nary	
rences		

5

General Aviation and Uninhabited Aerial Vehicle Propulsion System

5.2	Cycle	Analysi	S	284	
	5.2.1	Otto Cy	vcle	284	
	5.2.2	Real En	ngine Cycles	284	
		5.2.2.1	Four-Stroke Cycle Engines	284	
		5.2.2.2	Diesel Engines	286	
		5.2.2.3	Two-Stroke Cycle Engines	288	
		5.2.2.4	Rotary (Wankel) Engines	290	
5.3	Powe	r and Eff	iciency	293	
5.4	Engin	e Compo	onents and Classifications	295	
	5.4.1	295			
	5.4.2	Recipro	ocating Engine Classifications	296	
		5.4.2.1	Classification by Cylinder Arrangement	296	
		5.4.2.2	Classification by Cooling Arrangement	299	
		5.4.2.3	Classification by Operating Cycle	299	
		5.4.2.4	Classification by Ignition Type	300	
5.5	Scalir	ng of Air	craft Reciprocating Engines	300	
	5.5.1	Scaling	of Aircraft Diesel Engines	306	
5.6	Aircra	aft Engin	e Systems	308	
	5.6.1 Aviation Fuels and Engine Knock				
	5.6.2	Carbure	etion and Fuel Injection Systems	310	
		5.6.2.1	Float-Type Carburetors	310	
		5.6.2.2	Pressure Injection Carburetors	311	
		5.6.2.3	Fuel Injection Systems	311	
		5.6.2.4	Full Authority Digital Engine Control (FADEC)	311	
	5.6.3	Ignition	n Systems	311	
		5.6.3.1	Battery Ignition Systems	312	
		5.6.3.2	High Tension Ignition System	312	
		5.6.3.3	Low Tension Ignition System	312	
		5.6.3.4	Full Authority Digital Engine Control (FADEC)	312	
		5.6.3.5	Ignition Boosters	312	
		5.6.3.6	Spark Plugs	313	
	5.6.4	Lubrica	tion Systems	313	
	5.6.5	Superch	narging	314	
5.7	Electi	ic Engin	es	314	
	5.7.1	Electric	Motors	315	
	5.7.2	Solar ce	ells	316	
	5.7.3	Advanc	ed Batteries	316	
	5.7.4	Fuel cel	lls	318	
	5.7.5	State of	the Art for Electric Propulsion – Future Technology	319	
5.8	Prope	llers and	Reduction Gears	319	
Refer	ences			322	
Probl	Problems				

6 Aircraft Engine Inlets and Nozzles

6.1	Introduction	327
6.2	The Flight Mach Number and Its Impact on Inlet Duct Geometry	328

6.3	Diffusers	329
6.4	An Ideal Diffuser	330
6.5	Real Diffusers and Their Stall Characteristics	331
6.6	Subsonic Diffuser Performance	333
6.7	Subsonic Cruise Inlet	338
6.8	Transition Ducts	348
6.9	An Interim Summary for Subsonic Inlets	349
6.10	Supersonic Inlets	350
	6.10.1 Isentropic Convergent–Divergent Inlets	350
	6.10.2 Methods to Start a Supersonic Convergent–Divergent Inlet	353
	6.10.2.1 Overspeeding	355
	6.10.2.2 Kantrowitz–Donaldson Inlet	356
	6.10.2.3 Variable-Throat Isentropic C–D Inlet	358
6.11	Normal Shock Inlets	359
6.12	External Compression Inlets	362
	6.12.1 Optimum Ramp Angles	365
	6.12.2 Design and Off-Design Operation	366
6.13	Variable Geometry—External Compression Inlets	368
	6.13.1 Variable Ramps	368
6.14	Mixed-Compression Inlets	368
6.15	Supersonic Inlet Types and Their Performance—A Review	370
6.16	Standards for Supersonic Inlet Recovery	371
6.17	Exhaust Nozzle	373
6.18	Gross Thrust	373
6.19	Nozzle Adiabatic Efficiency	373
6.20	Nozzle Total Pressure Ratio	374
6.21	Nozzle Pressure Ratio (NPR) and Critical Nozzle Pressure Ratio	
	(NPR _{crit.})	374
6.22	Relation Between Nozzle Figures of Merit, η_n and π_n	376
6.23	A Convergent Nozzle or a De Laval?	376
6.24	The Effect of Boundary Layer Formation on Nozzle Internal Performance	379
6.25	Nozzle Exit Flow Velocity Coefficient	379
6.26	Effect of Flow Angularity on Gross Thrust	381
6.27	Nozzle Gross Thrust Coefficient C _{fg}	385
6.28	Overexpanded Nozzle Flow—Shock Losses	386
6.29	Nozzle Area Scheduling, A_8 and A_9/A_8	389
6.30	Nozzle Exit Area Scheduling, A_9/A_8	391
6.31	Nozzle Cooling	394
6.32	Thrust Reverser and Thrust Vectoring	396
6.33	Hypersonic Nozzle	401
6.34	Exhaust Mixer and Gross Thrust Gain in a Mixed-Flow Turbofan Engine	404
6.35	Noise	406
	6.35.1 Jet Noise	407
	6.35.2 Chevron Nozzle	408
6.36	Nozzle-Turbine (Structural) Integration	409
6.37	Summary of Exhaust Systems	410
Refer		411
Proble	ems	413

Con	nbustion Chambers and Afterburners	429
7.1	Introduction	429
7.2	Laws Governing Mixture of Gases	431
7.3	Chemical Reaction and Flame Temperature	434
7.4	Chemical Equilibrium and Chemical Composition	445
	7.4.1 The Law of Mass Action	446
	7.4.2 Equilibrium Constant K_P	448
7.5	Chemical Kinetics	459
	7.5.1 Ignition and Relight Envelope	460
	7.5.2 Reaction Timescale	461
	7.5.3 Flammability Limits	461
	7.5.4 Flame Speed	464
	7.5.5 Flame Stability	466
	7.5.6 Spontaneous Ignition Delay Time	470
	7.5.7 Combustion-Generated Pollutants	472
7.6	Combustion Chamber	473
	7.6.1 Combustion Chamber Total Pressure Loss	474
	7.6.2 Combustor Flow Pattern and Temperature Profile	483
	7.6.3 Combustor Liner and Its Cooling Methods	485
	7.6.4 Combustion Efficiency	488
	7.6.5 Some Combustor Sizing and Scaling Laws	489
	7.6.6 Afterburner	493
7.7	Combustion-Generated Pollutants	498
	7.7.1 Greenhouse Gases, CO_2 and H_2O	498
	7.7.2 Carbon Monoxide, CO, and Unburned Hydrocarbons, UHC	499
	7.7.3 Oxides of Nitrogen, NO and NO_2	500
	7.7.4 Smoke	501
	7.7.5 Engine Emission Standards	502
	7.7.6 Low-Emission Combustors	503
	7.7.7 Impact of NO on the Ozone Layer	507
7.8	Aviation Fuels	509
7.9	Alternative "Drop-In" Jet Fuels (AJFs)	513
7.10	Combustion Instability: Screech and Rumble	515
	7.10.1 Screech Damper	515
7.11	Summary	516
Refer		516
Proble	ems	518

Axial Compressor Aerodynamics		
8.1	Introduction	525
8.2	The Geometry	525
8.3	Rotor and Stator Frames of Reference	526
8.4	The Euler Turbine Equation	529

8.5	Axial-Flow Versus Radial-Flow Machines	530
8.6	Axial-Flow Compressors and Fans	532
	8.6.1 Definition of Flow Angles	534
	8.6.2 Stage Parameters	536
	8.6.3 Cascade Aerodynamics	549
	8.6.4 Aerodynamic Forces on Compressor Blades	563
	8.6.5 Three-Dimensional Flow	571
	8.6.5.1 Blade Vortex Design	573
	8.6.5.2 Three-Dimensional Losses	585
	8.6.5.3 Reynolds Number Effect	590
8.7	Compressor Performance Map	593
8.8	Compressor Instability – Stall and Surge	595
8.9	Multistage Compressors and Their Operating Line	599
8.10	Multistage Compressor Stalling Pressure Rise and Stall Margin	604
8.11	Multistage Compressor Starting Problem	612
8.12	The Effect of Inlet Flow Condition on Compressor Performance	615
8.13	Isometric and Cutaway Views of Axial-Flow Compressor Hardware	620
8.14	Compressor Design Parameters and Principles	620
	8.14.1 Blade Design – Blade Selection	626
	8.14.2 Compressor Annulus Design	627
	8.14.3 Compressor Stall Margin	628
8.15	Summary	636
Refer	ences	638
Probl	ems	640

Y		
Cer	651	
9.1	Introduction	651
9.2	Centrifugal Compressors	652
9.3	Radial Diffuser	666
9.4	Inducer	670
9.5	Inlet Guide Vanes (IGVs) and Inducer-Less Impellers	673
9.6	Impeller Exit Flow and Blockage Effects	673
9.7	Efficiency and Performance	674
9.8	Summary	677
Refe	rences	678
Prob	678	

10Aerothermo-dynamics of Gas Turbines68510.1Introduction685

10.1	Introduction	685
10.2	Axial-Flow Turbines	
	10.2.1 Optimal Nozzle Exit Swirl Mach Number $M_{\theta 2}$	698
	10.2.2 Turbine Blade Losses	702
	10.2.2.1 Blade Profile Loss	703

		10.2.2.2 Secondary Flor	w Losses	703
		10.2.2.3 Annulus Losse	S	705
	10.2.3	Optimum Solidity		714
	10.2.4	Turbine Cooling		718
		10.2.4.1 Convective Co	oling	723
		10.2.4.2 Impingement C	Cooling	728
		10.2.4.3 Film Cooling		729
		10.2.4.4 Transpiration G	Cooling	732
10.3	Turbin	e Performance Map		733
10.4	The E	fect of Cooling on Tu	urbine Efficiency	734
10.5	Turbine Blade Profile Design		735	
	10.5.1	Angles		736
	10.5.2	Other Blade Geometric	cal Parameters	737
	10.5.3	Throat Sizing		737
	10.5.4	Throat Reynolds Num	ber Re _o	738
	10.5.5	Turbine Blade Profile	Design	738
	10.5.6	Blade Vibration and C	ampbell Diagram	739
	10.5.7	Turbine Blade and Dis	k Material Selection and Design Criteria	740
10.6	Stress	s in Turbine Blades a	nd Disks and Useful Life Estimation	743
10.7	Axial-	Flow Turbine Design	and Practices	746
10.8	Gas Tu	rbine Design Summa	ıry	754
10.9	Summ	ry		755
Refer	ences			757
Proble	ems			759

11 Aircraft Engine Component Matching and Off-Design Analysis

11.1	Introduction	767
11.2	Engine (Steady-State) Component Matching	768
	11.2.1 Engine Corrected Parameters	769
	11.2.2 Inlet-Compressor Matching	769
	11.2.3 Compressor–Combustor Matching	771
	11.2.4 Combustor–Turbine Matching	773
	11.2.5 Compressor–Turbine Matching and Gas Generator	
	Pumping Characteristics	774
	11.2.5.1 Gas Generator Pumping Characteristics	777
	11.2.6 Turbine–Afterburner–(Variable-Geometry) Nozzle Matching	783
	11.2.6.1 Fixed-Geometry Convergent Nozzle Matching	784
11.3	Engine Off-Design Analysis	785
	11.3.1 Off-Design Analysis of a Turbojet Engine	786
	11.3.2 Off-Design Analysis of an Afterburning Turbojet Engine	789
	11.3.3 Off-Design Analysis of a Separate-Flow Turbofan (Two-Spool) Engine	793
11.4	Unchoked Nozzles and Other Off-Design Iteration Strategies	798
	11.4.1 Unchoked Exhaust Nozzle	799
	11.4.2 Unchoked Turbine Nozzle	800

	11.4.3	Turbine	Efficiency at Off-Design	801
	11.4.4	Variable	Gas Properties	801
11.5	Principles of Engine Performance Testing		802	
	11.5.1	Force of	Inlet Bellmouth on Engine Thrust Stand	804
		11.5.1.1	Bellmouth Instrumentation	804
		11.5.1.2	The Effect of Fluid Viscosity	805
		11.5.1.3	The Force of Inlet Bellmouth on Engine Thrust Stand	806
11.6	5 Summary		810	
References			812	
Problems			813	

12 Chemical Rocket and Hypersonic Propulsion 821

Introduction	821
From Takeoff to Earth Orbit	823
Chemical Rockets	824
Chemical Rocket Applications	826
12.4.1 Launch Engines	826
12.4.2 Boost Engines	826
12.4.3 Space Maneuver Engines	827
12.4.4 Attitude Control Rockets	827
New Parameters in Rocket Propulsion	827
Thrust Coefficient, $C_{\rm F}$	830
Characteristic Velocity, c^*	833
Flight Performance	835
Multistage Rockets	845
Propulsive and Overall Efficiencies	847
Chemical Rocket Combustion Chamber	849
12.11.1 Liquid Propellant Combustion Chambers	849
12.11.1.1 Some Design Guidelines for Injector Plate	854
12.11.1.2 Combustion Instabilities	855
12.11.2 Solid Propellant Combustion Chambers	855
Thrust Chamber Cooling	862
12.12.1 Liquid Propellant Thrust Chambers	862
12.12.2 Cooling of Solid Propellant Thrust Chambers	868
Combustor Volume and Shape	869
Rocket Nozzles	870
12.14.1 Multiphase Flow in Rocket Nozzles	874
-	883
12.14.3 Thrust Vectoring Nozzles	884
High-Speed Airbreathing Engines	884
12.15.1 Supersonic Combustion Ramjet	891
12.15.1.1 Inlet Analysis	892
12.15.1.2 Scramjet Combustor	892
12.15.1.3 Scramjet Nozzle	895
	From Takeoff to Earth Orbit Chemical Rockets Chemical Rocket Applications 12.4.1 Launch Engines 12.4.2 Boost Engines 12.4.3 Space Maneuver Engines 12.4.3 Space Maneuver Engines 12.4.4 Attitude Control Rockets New Parameters in Rocket Propulsion Thrust Coefficient, <i>C</i> _F Characteristic Velocity, <i>c*</i> Flight Performance Multistage Rockets Propulsive and Overall Efficiencies Chemical Rocket Combustion Chamber 12.11.1 Liquid Propellant Combustion Chambers 12.11.1 Some Design Guidelines for Injector Plate 12.11.2 Combustion Instabilities 12.11.2 Solid Propellant Combustion Chambers Thrust Chamber Cooling 12.12.1 Liquid Propellant Thrust Chambers 12.12.2 Cooling of Solid Propellant Thrust Chambers 12.12.2 Cooling of Solid Propellant Thrust Chambers 12.14.1 Multiphase Flow in Rocket Nozzles 12.14.2 Flow Expansion in Rocket Nozzles 12.14.3 Thrust Vectoring Nozzles High-Speed Airbreathing Engines 12.15.1.1 Inlet Analysis 12.15.1.2 Scramjet Combustor

12.1	16 Rocket-Based Airbreathing Propulsion	895
12.1	17 Summary	897
Ref	erences	898
Pro	blems	899
А.	U.S. Standard Atmosphere	903
В.	Isentropic Table	907
C.	Normal Shock Table	924
D.	Rayleigh Flow	937
E.	Fanno Flow	946
F.	Prandtl–Meyer Function and Mach Angle	955
G.	Oblique Shock Charts	958
H.	Conical Shock Charts	963
I.	Cascade Data	966
J.	Websites	972
Κ.	10-Minute Quiz	973
L.	Some "Rules of Thumb" and Trends in Aircraft Propulsion	991
Inde	ex	999

Preface to the Second Edition

Since the first edition of this book appeared in 2008, the Uninhabited Aerial Vehicle (UAV) has gained wider interest and market share in aircraft industry. As a result, the second edition has a new chapter dedicated to *General Aviation and UAV Propulsion Systems*. The remaining changes to the second edition stem from technological advances in propulsion in recent years. For example in the commercial transport sector, we have witnessed the development of *Ultra-High Bypass (UHB)* turbofan engines with bypass ratio above 12. An enabling technology to UHB is the *Geared Turbofan*, which has also received an introductory coverage in the second edition. Other technological advances include *Chevron Nozzle, Alternative "drop-in" Jet Fuels* (AJF) and *advanced heat exchanger in airbreathing rocket engine* for single-stage-to-orbit application, which are introduced in the new edition.

Some of the reviewers and readers suggested an introductory presentation on *propeller theory* could well be integrated with the presentation of the turboprop engines. In response, I have added a section on propeller theory prior to the turboprop cycle analysis section. The instructors often wrote and asked for *more problems* at the end of chapters and as a result the new edition has about 50% more end-of-chapter problems than the first edition (i.e., 446 in 2E vs. 305 in 1E). There is an increased interest in Aerospace Engineering (AE) programs to offer propulsion system design as one of the capstone design options in AE curriculum. Towards that goal, additional *design guidelines* are added to each component chapter in 2E. A new section on aircraft engines *performance testing and basic instrumentation* in ground facilities is added to Chapter 11: Aircraft Engine Component Matching and Off-Design Analysis.

Two new appendices are created in the second edition. The first one is an assembly of 45 *Ten-Minute Quizzes* that I had given to my propulsion students at KU in the past three decades. These 10-minute closed books/notes quizzes were given to students at the beginning of my class and concentrated on recent materials. The goal is to show the importance of fundamental concepts, governing laws, important definitions to students and hopefully develop an engineering sense for "ballpark" numbers in propulsion system engineering. The quizzes may be used as an assessment tool by the instructors or the learners themselves. To help the students with the "*Rules of Thumb" and Trends* in

aircraft propulsion, a second new appendix is created. Students of propulsion and practicing system engineers should find the new appendix on "Rules of Thumb" and Trends particularly useful.

Acknowledgments

I express my sincere appreciation to my friend and colleague at KU-Aerospace, Professor Ray Taghavi, who wrote the invited chapter on General Aviation and UAV Propulsion in the second edition. I received extensive support from Pratt & Whitney on engine data, many engine cutaways, including their new geared turbofan engine, PW1000G, and others. For these, I express my sincere appreciation to Dr. Alan Epstein, Vice President of Engineering Technology and Environment at P&W and Mr. Steve O'Flarity who helped immensely with data and approvals' gathering at P&W. The copyright permissions from GE Aviation, Boeing and other industry help enrich the presentation and content of this book and are greatly appreciated.

To many colleagues who had adopted my book and sent corrections and helpful suggestions, I express my heartfelt appreciation. I have tried to adopt their suggestions and numerous corrections in the second edition. Since the last edition, I have been assisted by my new doctoral students, Seung-Jae Hwang (2011), Leslie Smith, Amool Raina and Dhaval Mysore who continue to improve my understanding of the advanced concepts in aircraft propulsion and (green) power generation. I am also indebted to many graduate students in the MS level who have helped me in research and provided solutions to the end-of-chapter problems that appear in the solution manual, as an instructor resource.

Finally, my wife Mariam and our growing family continue to be the real inspiration behind this work and I owe my peace of mind and productivity to their love and support.

> Saeed Farokhi Lawrence, Kansas November 12, 2013

Preface

Intended Audience

This book is intended to provide a foundation for the analysis and design of aircraft engines. The target audience for this book is upper classmen, undergraduates, and firstyear graduate students in aerospace and mechanical engineering. The practicing engineers in the gas turbine and aircraft industry will also benefit from the integration and system discussions in the book. Background in thermodynamics and fluid mechanics at a fundamental level is assumed.

Motivation

In teaching under graduate and graduate propulsion courses for the past 23 years, I accumulated supplemental notes on topics that were not covered in most of our adopted textbooks. The supplemental materials ranged from issues related to the propulsion system integration into aircraft to the technological advances that were spawned by research centers around the world. I could have continued handing out supplemental materials to the textbooks to my classes, except that I learned that the presentation style to undergraduate students had to be (peda-gogically) different than for the graduate students. For example, leaving out many steps in derivations of engineering principles can lead to confusion for most undergraduate students. Although it is more important to grasp the underlying principles than the mechanics of some derivations, but if we lose the students in the derivation phase, they may lose sight of the underlying principles as well. Another motivation for attention to details in analysis is my conviction that going back to basics and showing how the end results are obtained demystifies the subject and promotes students' confidence in their own abilities.

Mathematical Level

The mathematics in the present book is intentionally kept at the calculus and basic differential equations level, which makes the book readily accessible to undergraduate engineering students. Physical interpretations of mathematical relations are always offered in the text to help students grasp the physics that is hidden and inherent in the formulas.

This approach will take the mystery out of formulas and let engineering students go beyond symbols and into understanding concepts.

Chapter Organization and Topical Coverage

The first chapter is an introduction to airbreathing aircraft engines and is divided in two parts. The first part reviews the history of gas turbine engine development, and the second part highlights modern concepts in aircraft engine and vehicle design. Young engineering students are excited to learn about the new opportunities and directions in aircraft engine design that are afforded by advances in materials, manufacturing, cooling technology, computational methods, sensors, actuators, and controls. Renewed interest in hypersonicair breathing engines in general and supersonic combustion ramjets in particular as well as a sprawling interest in Uninhabited Aerial Vehicles (UAVs) has revitalized the ever-popular X-planes. The goal of Chapter 1 is first to inform students about the history, but more importantly to excite them about the future of aerospace engineering.

Chapter 2 is a review of compressible flow with heat and friction. The conservation principles are reviewed and then applied to normal and oblique shocks, conical shocks, and expansion waves, quasi-one-dimensional flows in ducts as well as Rayleigh and Fanno flows. At the closing of Chapter 2, the impulse concept and its application to gas turbine engine components are introduced.

Chapter 3 is on engine thrust and performance parameters. Here, we introduce internal and external performance of aircraft engines and their installation effect.

Chapter 4 describes aircraft gas turbine engine cycles. The real and ideal behaviors of engine components are described simultaneously in this chapter. Efficiencies, losses, and figures of merit are defined both physically and mathematically for each engine component in Chapter 4. Once we define the real behavior of all components in a cycle, we then proceed to calculate engine performance parameters, such as specific thrust, specific fuel consumption and thermal and propulsive efficiencies. The ideal cycle thus becomes a special case of a real cycle when all of its component efficiencies are equal to one.

The next five chapters treat aircraft engine components. Chapter 5 deals with aircraft inlets and nozzles. Although the emphasis throughout the book is on internal performance of engine components, the impact of external or installation effects is always presented for a balanced view on aircraft propulsion. As a building block of aircraft inlet aerodynamics, we have thoroughly reviewed two-dimensional and conical diffuser performance. Some design guidelines, both internal and external to inlet cowl, are presented. Transition duct aero-dynamics also plays an important role in design and understanding of aircraft inlets and is thus included in the treatment. Supersonic and hypersonic inlets with their attendant shock losses, boundary layer management, and instabilities such as buzz and starting problem are included in the inlet section of Chapter 5. The study of aircraft exhaust systems comprises the latter part of Chapter 5. Besides figures of merit, the performance of a convergent nozzle is compared with the de Laval or a convergent-divergent nozzle. The requirements of reverse-and vector thrust are studied in the context of thrust reversers and modern thrust vectoring nozzles. In the hypersonic limit, the exhaust nozzle is fully integrated with the vehicle and introductory design concepts and off-design issues are presented. Nozzle cooling is introduced for high-performance military aircraft engine exhaust systems and the attendant performance penalties and limitations are considered.

Plug nozzle and its on-and off-design performances are introduced. Since mixers are an integral part of long-duct turbo fan engines, their effect on gross thrust enhancement is formulated and presented in the nozzle section in Chapter 5.

Chemical reaction is studied on a fundamental basis in Chapter 6. The principles of chemical equilibrium and kinetics are used to calculate the composition of the products of combustion in a chemical reaction. These principles allow the calculation of flame temperature and pollutant formations that drive the design of modern aircraft gas turbine combustors. Further details of flame speed, stability, and flame holding are presented in the context of combustion chamber and afterburner design. Pollutant formation and its harmful impact on ozone layer as well as the greenhouse gases in the exhaust are presented to give students an appreciation for the design issues in modern combustors. Aviation fuels and their properties and a brief discussion of combustion instability known as screech are included in Chapter 6.

Turbomachinery is introduced in three chapters. Chapter 7 deals with axial-flow com-pressors in two and three dimensions. The aerodynamics of axial-flow compressors and stage performance parameters are derived. The role of cascade data in two-dimensional design is presented. Emphasis throughout this chapter is in describing the physical phenomena that lead to losses in compressors. Shock losses and transonic fans are introduced. The physics of compressor instability in stall and surge is described. A simple model by Greitzer that teaches the value of characteristic timescales and their relation to compressor instability is outlined. Chapter 8 discusses the aerodynamics and performance of centrifugal compressors. Distinctive characters of centrifugal compressors are highlighted and compared with axial-flow compressors. Turbine aerodynamics and cooling are presented in Chapter 9. Component matching and engine parametric study is discussed in Chapter 10. Finally, chemical rocket and hypersonic propulsion is presented in Chapter 11.

Instructor Resources

The following resources are available to instructors who adopt this book for their course. Please visit the website at www.wiley.com/go/farokhi to request a password and access these resources.

- Solutions Manual
- Image Gallery

Acknowledgments

I express my sincere appreciation and gratitude to all those who have contributed to my understanding of fluid mechanics and propulsion. Notable among these are my professors in Illinois and MIT. Hermann Krier, Jack Kerrebrock, James McCune, William Hawthorne, and Ed Greitzer contributed the most. The fellow graduate students in the Gas Turbine Lab were also instrumental in my education. Choon Tan, Maher El-Masri, Alan Epstein, Arun Sehra, Mohammad Durali, Wai Cheng, Segun Adebayo, James Fabunmi, and Anthony Nebo discussed their dissertations with me and helped me understand my own. In the Gas Turbine Division of Brown, Boveri and Co. in Baden, Switzerland, I learned the value

of hardware engineering and testing, advanced product development, and component research. My colleagues, Meinhard Schobeiri, Konrad Voegeler, Hans Jakob Graf, Peter Boenzli, and Horst Stoff, helped me understand how industry works and how it engineers new products. At the University of Kansas, my graduate students were my partners in research and we jointly advanced our understanding of fluid mechanics and propulsion. My doctoral students, Ray Taghavi, Gary Cheng, Charley Wu, Ron Barrett, and Kyle Wetzel, taught me the most. I appreciate the contributions of 30 M.S. students whom I chaired their theses to our ongoing research. The colleagues at NASA-Lewis (now Glenn) who sponsored my research and provided insightful discussions and hospitality over the summer months in Cleveland are Ed Rice, Khairul Zaman, Ganesh Raman, Bernie Anderson, Reda Mankbadi, James Scott, and Charlie Towne who welcomed me into their laboratory (and their homes), and we enjoyed some fruitful research together. The faculty and staff in the Aerospace Engineering Department of the University of Kansas have been very supportive for the past 23 years, and I would like to express my sincere appreciation to all of them. Vince Muirhead, Jan Roskam, Eddie Lan, Dave Downing, Howard Smith, Dave Ellis, Tae Lim, John Ogg, James Locke, Mark Ewing, Rick Hale, and Trevor Sorenson taught me an appreciation for their disciplines in aerospace engineering. I joined my colleagues in GE-Aircraft Engines in teaching propulsion system design and integration short courses to engineers in industry, FAA, and NASA for many years. I learned from Don Dusa and Jim Younghans from GE and Bill Schweikhard of KSR some intricate aspects of propulsion engineering and flight-testing.

I would like to thank the following colleagues who reviewed the draft manuscript:

David Benson, Kettering University Kirby S. Chapman, Kansas State University Mohamed Gad-el-Hak, Virginia Commonwealth University Knox Millsaps, Naval Postgraduate School Alex Moutsoglou, South Dakota State University Norbert Mueller, Michigan State University Meinhard T. Schobeiri, Texas A&M University Ali R. Ahmadi, California State University and Polytechnic—Pomona Ganesh Raman, Illinois Institute of Technology

Finally, I express my special appreciation to my wife of 36 years, Mariam, and our three lovely daughters, Kamelia, Parisa, and Farima (Fallon) who were the real inspiration behind this effort. I could not have contemplated such a huge project without their love, understanding, encouragement, and support. I owe it all to them.

Saeed Farokhi Lawrence, Kansas March 16, 2007

Nomenclature

Latin	Definition	Unit
a	Local speed of sound	m/s, ft/s
a	Semimajor axis of inlet elliptic lip (internal)	m, ft
a	Swirl profile parameter	
a_{t}	Speed sound based on total temperature	m/s, ft/s
Α	Area	m^2 , ft^2
A _n	Projection of area in the normal direction	m^2 , ft^2
A_9	Nozzle exit flow area	m^2 , ft^2
A _{ref}	Reference area	m^2 , ft^2
A _o	Inlet (freestream) capture area	m^2 , ft^2
A_1	Inlet capture area	m^2 , ft^2
A_8, A_{8geo}	Nozzle throat area (geometrical area)	m^2 , ft^2
A _{8eff}	Effective nozzle throat area	m^2 , ft^2
$A_{\scriptscriptstyle \rm B}$	Blocked area (due to boundary layer)	m^2 , ft^2
$A_{\rm b}$	Burning area of grain in solid rocket motors	m^2 , ft^2
$A_{\rm e}$	Effective area	m^2 , ft^2
$A_{\rm HL}$	Inlet highlight area	m^2 , ft^2
$A_{\rm m}$	Maximum nacelle area	m^2 , ft^2
$A_{ m th}$	Inlet throat area	m^2 , ft^2
A^*	Sonic throat, choked area	m^2 , ft^2
b	Semiminor axis of inlet elliptic lip (internal)	m, ft
b	Swirl profile parameter	
В	Blockage	
В	Compressor instability parameter due to Greitzer	_
\vec{C}	Absolute velocity vector in turbomachinery	m/s, ft/s
С	Absolute flow speed, i.e., $\sqrt{C_r^2 + C_\theta^2 + C_z^2}$	m/s, ft/s
с	Chord length	m, ft
С	Effective exhaust velocity in rockets	m/s, ft/s
<i>c</i> *	Characteristic velocity in rockets	m/s, ft/s
C_r, C_{θ}, C_z	Radial, tangential, axial velocity components in the absolute frame of reference	m/s, ft/s
C _D	drag coefficient, discharge coefficient	
C_{f}	Friction drag coefficient	

c_f	Local skin friction coefficient	_
Č _F	Force coefficient	—
С _F С _P	Pressure coefficient	_
$C_{\rm PR}$	Diffuser static pressure recovery coefficient	_
C _A	Nozzle flow angularity loss coefficient	_
\hat{C}_{D8}	Nozzle (throat) discharge coefficient	_
$C_{\rm fg}$	Nozzle gross thrust coefficient	_
C_V	Nozzle exit velocity coefficient	_
C_d	Sectional profile drag coefficient	_
$C_{\text{D}i}$	Induced drag coefficient	
C_l	Sectional lift coefficient	_
C_h	Enthalpy-equivalent of the static pressure rise coefficient due to Koch	
	Specific heat at constant pressure	J/kg · K
<i>c</i> _{<i>p</i>}	Specific heat at constant pressure	J/kg · K
c_v	Molar specific heat at constant pressure	J/kmol · I
\bar{c}_p	Flameholder width	m, ft
d		,
D	Diameter, drag	m, N
D	Liquid fuel droplet diameter	micron
D _{flameholder}	Flameholder drag	N, lbf
$D_{\rm add}$	Additive drag	N, lbf
D _{nacelle}	Nacelle drag	N, lbf
$D_{ m pylon}$	Pylon drag	N, lbf
D _r	Ram drag	N, lbf
D _{spillage}	Spillage drag	N, lbf
D _{aft-end}	Nozzle aft-end drag	N, lbf
D _{boattail}	Nozzle boattail drag	N, lbf
D _{plug-friction}	Friction drag on the plug nozzle	N, lbf
D	Diffusion factor in turbomachinery	—
D′	Two-dimensional or sectional profile drag	N/m
ê	Unit vector	_
е	Specific internal energy	J/kg
$e_{\rm c}, e_{\rm t}$	Polytropic efficiency of compressor or turbine	_
E	Internal energy	J
E_{a}	Activation energy	kcal/mol
f	Fuel-to-air ratio	_
fstoich	Stoichiometric fuel-to-air ratio	_
F _g	Gross thrust	N, lbf
F _{lip}	Lip suction force	N, lbf
$F_{\rm plug}$	Axial force on the nozzle plug	N, lbf
F_{n}	Net thrust	N, lbf
F	Force	N, lbf
	Tangential force, axial force	N, lbf
F_{θ}, F_{z}		18, 101
f _D	D'Arcy (pipe) friction factor	
g	Staggered spacing (s.cos β in a rotor and s.cos α in a stator)	m
g ₀	Gravitational acceleration on the surface of the earth	m/s^2 , ft/s
h	Specific enthalpy	J/kg
h _t	Specific total enthalpy	J/kg

h	Heat transfer rate per unit area per unit temp. difference	W/m ² K
h h	Altitude above a planet	km, kft
$h_{ m t}$	Specific total (or stagnation) enthalpy in the absolute frame; $h + C^2/2$	J/kg
$h_{\rm t}$ $h_{\rm tr}$	Specific total (of sugmation) entitiapy in the absolute frame, $n + C/2$ Specific total enthalpy in relative frame of reference; $h + W^2/2$	J/kg
	Latent heat of vaporization	J/kg
$h_{ m lg} \ m HHV$	Higher heating value	J/kg, BTU/lbm
H H		J, ft-lbf
н Н	Enthalpy A frahumen duct beight	
	Afterburner duct height	m, ft
i	Blade section incidence angle	deg
i _{opt}	Optimum incidence angle	deg
I _s	Specific impulse	S II C
I _t	Total impulse	$N \cdot s$, $lbf \cdot s$
I	Impulse	N, lbf
K _p	Equilibrium constant based on partial pressure	$(bar)^x$
K _n	Equilibrium constant based on molar concentration	_
L	Length	m, ft
L	Lift	N, lbf
L	Flameholder length of recirculation zone	m, ft
L	Diffuser wall length	m, ft
L	Diffusion length scale in a blade row	m, ft
LHV	Lower heating value	J/kg, BTU/lbm
L/D	Aircraft lift-to-drag ratio	—
$M_{ m b}$	Blowing parameter in film cooling, $\rho_c u_c / \rho_g u_g$	—
$M_{ m T}$	Blade tangential Mach number U/a	—
M _z	Axial Mach number, C_z/a	_
$M_{ m r}$	Relative Mach number (in turbomachinery); $(M_z^2 + M_T^2)^{1/2}$	—
М	Mach number	_
M^*	Characteristic Mach number	—
M _s	Gas Mach number upstream of a shock inside a nozzle	—
m	Parameter in Carter's rule for deviation angle	—
m	Mass	kg, lbm
ṁ	Mass flow rate	kg/s, lbm/s
\dot{m}_c	Corrected mass flow rate	kg/s, lbm/s
\dot{m}_0	Air mass flow rate	kg/s, lbm/s
\dot{m}_f	Fuel mass flow rate	kg/s, lbm/s
<i>m</i> _p	Propellant (oxidizer and fuel) mass flow rate	kg/s, lbm/s
m ['] s	Mass flow rate through the side of the control volume	kg/s, lbm/s
\dot{m}_c	Coolant flow rate	kg/s, lbm/s
MW	Molecular weight	kg/kmol
п	Exponent of superellipse	
п	Polytropic exponent; parameter in general swirl distribution	_
Ν	Number of blades; shaft rotational frequency; number of stages	_
Ν	Number of bluff bodies in a flameholder	
Ν	Diffuser axial length	m, ft
N_{a}	Avagadro's number (6.023×10^{23} molecules per gmole)	
N _B	Inlet lip bluntness parameter	
$N_{\rm c}^{\rm B}$	Corrected shaft speed	rad/s, rpm
U	1	· / r

ĥ	Unit normal vector (pointing out of a surface)	_
Nu	Nusselt number	_
Pr	Prandtl number	_
р	Static pressure	bar, Pa, psia
$p_{\rm t}$	Total pressure	bar, Pa, psia
$P_{\rm s}$	Static pressure upstream of a shock (in nozzle)	bar, Pa, psia
<i>©</i>	Power	W, hp
©s	Shaft power	W, BTU/s
PF	Pattern factor	
P _f	Profile factor	_
Q	Heat exchange	J, BTU
	Dynamic pressure	bar, atm
<i>q</i>	Heat transfer rate per unit area (heat flux)	W/m^2 , BTU/s.ft ²
<i>q</i>	Heat transfer rate per unit mass flow rate	J/kg, BTU/lbm
$q = Q_{R}$	Fuel heating value	kJ/kg, BTU/lbm
Q Q	Heat transfer rate	W, BTU/s
Q R		,
	Aircraft range	nm
Re R	Reynolds number	 I/I I∕ DTII//I °D
	Gas constant	J/kg · K, BTU/lbm-°R
R _{l.e.}	Blade leading-edge radius	m, in Marcal - K
<i>R</i>	Universal gas constant	J/kmol · K
r	Mixture ratio (oxidizer to fuel) in liquid propellant rockets	
r	Burning rate in solid propellant rockets	cm/s, in/s
r	Radius	m, ft
r	Cylindrical or spherical coordinate	
$r_{\rm h}$	Hub radius	m, ft
r _t	Tip radius	m, ft
r _m	Pitchline or mean radius $(r_h+r_t)/2$	m, ft
°R	Stage degree of reaction in turbomachinery	
S	Entropy	J/K
S _L	Laminar flame speed	m/s, ft/s
S _T	Turbulent flame speed	m/s, ft/s
St	Stanton number	
SN	Smoke number	_
S	Specific entropy	J/kg · K
S	Blade spacing	m, ft
t	Blade thickness	m, ft
t	Time	s, hr
t _{max}	Maximum blade thickness	m, ft
t _{reaction}	Reaction time scale in a combustor	ms
t _i	Ignition delay time	ms
t _e	Evaporation time scale in a combustor	ms
Т	Static temperature	K, °R, °C, °F
$T_{\rm t}$	Total temperature	K, °R, °C, °F
$T_{\rm f}$	Reference temperature, 298.16 K	K, °R, °C, °F
$T_{\rm g}$	Gas temperature	K, °R, °C, °F
$T_{\rm c}$	Coolant temperature	K, °R, °C, °F

$T_{ m af}$	Adiabatic flame temperature	K, °R, °C, °F
T_{af} T_{aw}	Adiabatic wall temperature	K, °R, °C, °F
T _{aw} Tu	Turbulence intensity, $[(u'^2 + v'^2 + w'^2)/3]^{1/2}/V_{\rm m}$	
u	Speed, velocity normal to a shock	m/s, ft/s
u	Gas speed	m/s, ft/s
u' _{rms}	Turbulent fluctuating speed (root mean square)	m/s, ft/s
\vec{U} rms	Rotational velocity vector of rotor; v-reg	m/s, ft/s
U_{T}	Blade tip rotational speed, ωr_t	m/s, ft/s
u', v', w'	Root mean square of fluctuating velocities in 3 spatial directions	m/s, ft/s
\bar{v}	Average gas speed in the mixing layer	m/s, ft/s
V	Volume	m^3 , ft ³
, V	Speed	m/s, ft/s
, V _m	Mean speed (used in stall margin or turbulence intensity)	m/s, ft/s
V'	Relative speed (used in stall margin of the bally is	m/s, ft/s
V _c	Compressor or chamber volume	m^3 , ft ³
V _p	Plenum volume	m^3 , ft ³
W P	Weight	N, lbf
W	Flame width in afterburner	m, ft
W	Width	m, ft
\vec{W}, W	Relative velocity vector, relative flow speed	m/s, ft/s
W_r, W_{θ}, W_z	Radial, tangential and axial velocity components in relative frame of reference	m/s, ft/s
W_c	Rotor specific work (rotor power per unit mass flow rate; \wp/m)	J/kg, BTU/lbm
w	Specific work	J/kg, BTU/lbm
W	Tangential speed to an oblique shock	m/s, ft/s
w _p	Propellant weight	N, lbf
W _{visc.}	Rate of work done by the viscous force	W, BTU/s
X Visc.	Solid flow fraction in a rocket nozzle	
X	Semimajor axis of an elliptic external cowl	m, ft
Y	Semiminor axis of an elliptic external cowl	m, ft
z	Axial coordinate in the cylindrical coordinate system	_
z	Airfoil camber	m, ft
Z _{max}	Maximum airfoil camber	m, ft
x, y, z	Cartesian coordinates	
Greek	Definition	Unit
α	Bypass ratio in a turbofan engine	_
α	Angle of attack	deg
α	Absolute flow angle with respect to the axial direction in turbomachinery	deg
$\Delta \alpha$	Flow turning angle across a stator blade section	deg
Δp	Pressure drop	Pa, psi
β	Plane oblique shock wave angle	deg
β	Relative flow angle with respect to the axial direction in turbomachinery	deg
$\beta_{\rm m}$	Mean flow angle corresponding to an average swirl across a blade row	deg
$\Delta \beta$	Flow turning angle across a rotor blade section	deg
δ	Boundary layer thickness	m, ft
δ^*	Boundary layer displacement thickness	m, ft
δ	Ratio of total pressure to reference (standard sea level) pressure; p/p_{ref}	

XXVIII Nomenclature

δ_{T}	Thermal boundary layer thickness	m, ft
δ^*	Deviation angle defined at the blade trailing edge, a cascade parameter	deg
$\Delta ar{h}_{ m f}^0$	(Standard) molar heat of formation	J/kmol
$\Delta h_{\rm f}^0$	(Standard) specific heat of formation	J/kg
-	Tip clearance; slip factor in turbomachinery	J /Kg
ε	A small quantity ($\ll 1$)	_
ε		
ε_{g}	Emissivity of gas	W/m V
К	Coefficient of thermal conductivity	W/m · K
κ ₁	Blade leading-edge angle in turbomachinery	deg
κ ₂	Blade trailing-edge angle in turbomachinery	deg
π	Total pressure ratio	
ω	Angular speed	rad / s, rpm
σ	Total pressure loss parameter in a cascade; $\Delta p_t/q_r$	—
ϕ	Spherical coordinate	
ϕ	Equivalence ratio	_
ϕ	Diffuser wall divergence angle	deg
ϕ	Flow coefficient; C_z/U	—
arphi	Camber angle, $\kappa_{I} - \kappa_{2}$	deg
Φ	Cooling effectiveness parameter	—
γ	Ratio of specific heats	—
Γ	Circulation (of a vortex filament), blade circulation	m^2/s , ft^2/s
γ°	Cascade stagger angle or blade setting angle	deg
ρ	Fluid density	kg/m ³ , lbm/ft ³
μ	Coefficient of viscosity	$N \cdot s/m^2$
μ	Mach angle	degree
v	Kinematic viscosity $\equiv \mu/\rho$	m^2/s , ft^2/s
v	Prandtl-Meyer angle	radians, degree
π_{c}	Compressor total pressure ratio	_
$\pi_{ m b}$	Burner total pressure ratio	_
$\pi_{ m d}$	Inlet total pressure recovery	_
π_{n}	Nozzle total pressure ratio	_
π_{K}	Temperature sensitivity of chamber pressure in solid rockets	%/K, %/F
П _М	Mach index $\equiv U_{\rm T}/a_{\rm t1}$	_
θ	Flow angle, cylindrical or spherical coordinate	deg
θ	Nozzle exit flow angle (from axial direction)	deg
θ	Ratio of total temperature to the reference (standard sea level) temperature; T/T_{ref}	_
heta	Circumferential extent of the inlet spoiled or distortion sector	deg
$ heta^*$	Momentum deficit thickness in the boundary layer	m
σ	Cascade or blade solidity; c/s, in turbomachinery	_
σ	Stefan–Boltzmann constant	W/m^2K^4
$\sigma_{ m p}$	Temperature sensitivity of burning rate in solid propellant grain	%/K, %/F
$ au^{ m p}$	Shear stress	Pa, lbf/ft ² , psi
τ	Total temperature ratio	
τ	Characteristic timescale	8
$ au_{\mathrm{r}}, au_{\mathrm{s}}$	Rotor torque, stator torque in turbomachinery	N · m, ft-lbf
$\tau_{\rm r}^{\rm r}, \tau_{\rm s}$	Turbine total temperature ratio, T_{t5}/T_{t4}	
$ au_t$	Cycle limit enthalpy ratio, $c_{pt}T_{t4}/c_{pc}T_0$	_
$ au_{\lambda} au_{\lambda AB}$	Limit enthalpy ratio, $c_{pt} r_{14} c_{pc} r_0$ Limit enthalpy ratio with afterburner, $c_{pAB} T_{t7} / c_{pc} T_0$	_
	Resident timescale	ms
$ au_{ m resident}$		111.9