ASSIGNMENT ON SETS

LEVEL 1 (CBSE/NCERT/STATE BOARDS)

1	What is the difference between a collection and a set? Give reasons to support your answer?							
2	If A = $\{0,1,2,3,4,5,6,7,8,9,10\}$, then insert the appropriate symbol \in or $\not\in$ in each of the							
	following blank spaces:							
	(i) 4A (ii) -4A (iii) 12A							
	(iv) 9A (v) 0A (vi) -2A							
3	Write the set of all integers whose cube it an even integer.							
4	Write the set of all real numbers which cannot be written as the quotient of two integers in the							
	set-builder form.							
5	Describe each of the following sets in Roster form							
	(i) $\{x : x \text{ is a positive integer and a divisor of 9} \}$ (ii) $\{x : x \in Z \text{ and } x \le 2\}$							
	(iii) {x :x is a letter of the word 'PROPORTION'} (iv) $\left\{ x : \frac{n}{n^2 + 1} \text{ and } 1 \le n \le 3, \text{ where } n \in N \right\}$							
6	[1 2 3 4 5 6 7 8 9]							
	Write the set $\left\{ \frac{1}{2}, \frac{2}{3}, \frac{3}{4}, \frac{4}{5}, \frac{5}{6}, \frac{6}{7}, \frac{7}{8}, \frac{8}{9}, \frac{9}{10} \right\}$ in the set-builder form.							
7								
	Write the set X = $\left\{1, \frac{1}{4}, \frac{1}{9}, \frac{1}{16}, \frac{1}{25}, \dots \right\}$ in the set -builder form.							
	(4) 10 23							
8	Let A and B be two sets having 3 and 6 elements respectively. Write the minimum number of							
	elements that $A \cup B$ can have.							
9	Let $A = \{x : x \in N, x \text{ is a multiple of 3}\}$ and $B = \{x : x \in N \text{ and } x \text{ is a multiple of 5}\}$. Write $A \cap B$.							
	201. (A. A. 2.11) Als a manaple of 5) write A. A. 2. (A. A. 2. It and A. 15 a manaple of 5).							
10	1							
10	If A = $\{(x, y) : y = \frac{1}{y}, 0 \neq x \in R\}$ and B = $\{(x, y) : y = -x, x \in R\}$, then write A \cap B.							
11	If $A = \{(y, y), y = 0^X, y \in P\}$ and $B = \{(y, y), y = 0^X, y \in P\}$ then write $A \in P$							
11	If A = $\{(x, y) : y = e^x, x \in R\}$ and B = $\{(x, y) : y = e^{-x}, x \in R\}$, then write A \cap B.							
12								
12	Write the following sets in Roster form: (i) $A = \{a_n : n \in \mathbb{N}, a_{n+1} = 3a_n \text{ and } a_1 = 2\}$							
	(ii) $B = \{a_n : n \in \mathbb{N}, a_{n+2} = a_{n+1} + a_n, a_1 = a_2 = 1\}$							
12	Describe the faller vice and in eat builder forms							
13	Describe the following sets in set-builder form:							

	(i) A = {1, 2,3,4,5, 6}; (ii) B = {1,1/2, 1/3, 1/4, 1/5,};							
	(iii) C = {0,3, 6, 9,12,}; (iv) D = {10,11,12,13,14,15};							
	(, 0 (e)s, s, s,==,),							
14	te which of the following sets are finite and which are infinite:							
	(i) $A = \{x : x \in Z \text{ and } x^2 - 5x + 6 = 0\}$ (ii) $B = \{x : x \in Z \text{ and } x^2 \text{ is even}\}$							
	(iii) $C = \{x : x \in Z \text{ and } x^2 = 36\}$ (iv) $D = \{x : x \in Z \text{ and } x > -10\}$							
15	onsider the following sets: ϕ , A = {1, 2), B = {1,4,8}, C = {1,2,4,6, 8} usert the correct symbol \subset or $\not\subset$ between each of the following pair of sets:							
	(i) φB (ii) AB (iii) A C (iv) B C							
10								
16	In each of the following, determine whether the statement is true or false. If it is true, prove it.							
	If it is false, give an example.							
	(i) If $x \in A$ and $A \in B$, then $x \in B$ (ii) If $A \subset B$ and $B \subset C$, then $A \subset C$							
	(iii) If $A \subset B$ and $B \subset C$, then $A \subset C$ (iv) If $A \not\subset B$ and $B \not\subset C$, then $A \not\subset C$							
	(v) If $x \in A$ and $A \not\subset B$, then $x \in B$ (vi) If $A \subset B$ and $x \in B$, then $x \in A$							
17	Write the following subsets of R as intervals:							
1	(i) $\{x : x \in R, -4 < x \le 6\}$ (ii) $\{x : x \in R, -12 < x < -10\}$							
	(ii) $\{x : x \in R, 0 \le x < 7\}$ (iv) $\{x : x \in R, 3 \le x \le 4\}$.							
	(III) (X . X C II, 0 3 X 7) (IV) (X . X C II, 3 3 X 3 7).							
18	Which of the following statements are correct? Write a correct form of each of the incorrect							
	statements.							
	(i) $a \subset \{a, b, c\}$ (ii) $\{a\} \in \{a, b, c\}$ (iii) $a \in \{\{a\}, b\}$							
	(iv) $\{a\} \subset \{\{a\},b\}$ (v) $\{b,c\} \subset \{a,\{b,c\}\}$ (vi) $\{a,b\} \subset \{a,\{b,c\}\}$							
	(vii) $\phi \in \{a, b\}$ (viii) $\phi \subset \{a, b, c\}$ (ix) $\{x : x + 3 = 3\} = \phi$							
19	Let A = {a, b, {c, d},e}. Which of the following statements are false and why?							
	(i) $\{c \cdot d\} \subset A$ (ii) $\{c, d\} \in A$ (iii) $\{\{c, d\}\} \subset A$ (iv) $a \in A$							
	(v) $a \subset A$ (vi) $\{a, b, e\} \subset A$ (vii) $\{a, b, e\} \in A$ (viii) $\{a, b, c\} \subset A$							
	$(ix) \phi \in A \qquad (x) \{\phi\} \subset A$							
20	Let A = $\{\phi, \{\phi\}, 1, \{1, 0\}, 2\}$, Which of the following are true?							
20	(i) $\phi \in A$ (ii) $\{\phi\} \in A$ (iii) $\{1\} \in A$							
	$(i) \ \psi \in A \qquad (ii) \ \{\psi\} \in A \qquad (vi) \ \{1\} \notin A$ $(iv) \ \{2, \phi\} \subset A \qquad (v) \ 2 \subset A \qquad (vi) \ \{2, \{1\}\} \not\subset A$							
	(vii) $\{\{2\}, \{1\}\} \subset A$ (viii) $\{\phi, \{\phi\}, \{1, \phi\}\} \subset A$ (ix) $\{\{\phi\}\} \subset A$.							

21	If A = {1, 3, 5, 7,11,13, 15, 17}, B = {2, 4, 6,, 18} and N is the universal set, then find								
	$A' \cup ((A \cup B) \cap B').$								
22	Suppose A ₁ , A ₂ , A ₃₀ are thirty sets each with five elements and B ₁ , B ₂ ,, B _n are n sets each								
	with three elements. Let $\bigcup_{i=1}^{30} A_i = \bigcup_{j=1}^n B_j = S$. Assume that each element of S belongs to								
	exactly ten of the A _i 's and exactly 9 f B _j 's. Find n.								
23	Find sets A, B and C such that $A \cap B$, $A \cap C$ and $B \cap C$ are non-empty sets and $A \cap B \cap C = \phi$.								
24	For any two sets A and B, show that the following statements are equivalent:								
	(i) $A \subset B$ (ii) $A - B = 0$ (iii) $A \cup B = B$ (iv) $A \cap B = A$.								
25	For three sets A, B and C, show that								
	(i) $A \cap B = A \cap C$ need not imply $B = C$ (ii) $A \subset B \Rightarrow C - B \subset C - A$								
26	In a group of 50 people, 35 speak Hindi, 25 speak both English and Hindi and all the people speak at least one of the two languages. How many people speak only English and not Hindi 1 How many people speak English?								
27	There are 200 individuals with a skin disorder, 120 has been exposed to chemical C ₁ , 50								
	to chemical C_2 and 30 to both the chemicals C_1 and C_2 . Find the number of								
	individuals exposed to (i) chemical C_1 or chemical C_2 (ii) chemical C_1 but not								
	chemical C_2 (iii) chemical C_2 but not chemical C_1 .								
28	A market research group conducted a survey of 2000 consumers and reported that 1720								
	consumers liked product P ₁ and 1450 consumers liked product P ₂ . What is the								
	least number that must have liked both the products?								
29	In a survey of 700 students in a college, 180 were listed as drinking Limca, 275 as drinking Miranda and 95 were listed as both drinking Limca as well as Miranda. Find how many students were drinking neither Limca nor Miranda.								
30	In a class of 35 students, 17 have taken mathematics, 10 have taken mathematics but not								
	economics. Find the number of students who have taken both mathematics and								
	economics and the number of students who have taken economics but not								
	mathematics, if it is given that each student has taken either mathematics or economics								
	or both.								

31	In a town of '10,000 families it was found that 40% families buy newspaper A, 20%
	families buy newspaper B and 10% families buy newspaper C. 5% families buy A
	and B, 3% buy B and C and 4% buy A and C. If 2% families buy all the three
	news papers, find the number of families which buy (i) A only (ii) B only (in)
	none of A, B and C.
32	A college awarded 38 medals in Football, 15 in Basketball and 20 to Cricket. If, these medals
	went to a total of 58 men and only three men got medals in all the three sports, how
	many received medals in exactly two of the three sports ?
33	In a survey of 25 students, it was found that 15 had taken mathematics, 12 had taken physics
	and 11 had taken chemistry, 5 had taken mathematics and chemistry, 9 had taken
	mathematics and physics, 4 had taken physics and chemistry and 3 had taken all the
	three subjects. Find the number of students that had
	(i) only chemistry. (ii) only mathematics. (iii) only physics. (iv) physics and chemistry but
	not mathematics. (v) mathematics and physics but not chemistry. (vi) only one of the
	subjects. (vii) at least one of the three subjects. (viii) none of the subjects.
34	Of the members of three athletic teams in a certain school, 21 are in the basketball team, 26 in
	hockey team and 29 in the football team. 14 play hockey and basket ball, 15 play hockey
	and football, 12 play football and basketball and 8 play all the three games. How many
	members are there in all ?
35	A survey of 500 television viewers produced the following information; 285 watch football, 195
33	
	watch hockey, 115 watch basketball, 45 watch football and basketball, 70 watch
	football and hockey, 50 watch hockey and basketball, 50 do not watch any of the three
	games. How many watch all the three games? How many watch exactly one of the three
	games ?
36	In a survey it was found that 21 persons liked product P ₁ , 26 liked product P ₂ and 29
	liked product P ₃ . If 14 persons liked products P ₁ and P ₂ ; 12 persons liked product
	P ₃ and P ₁ ; 14 persons liked products P ₂ and P ₃ and 8 liked all the three products.
	Find how many liked product P ₃ only.
	Find now many fixed product 1 3 only.

ASSIGNMENT ON SETS

LEVEL 2 (OBJECTIVE QUESTIONS FOR IIT-MAIN AND OTHER ENTRANCES)

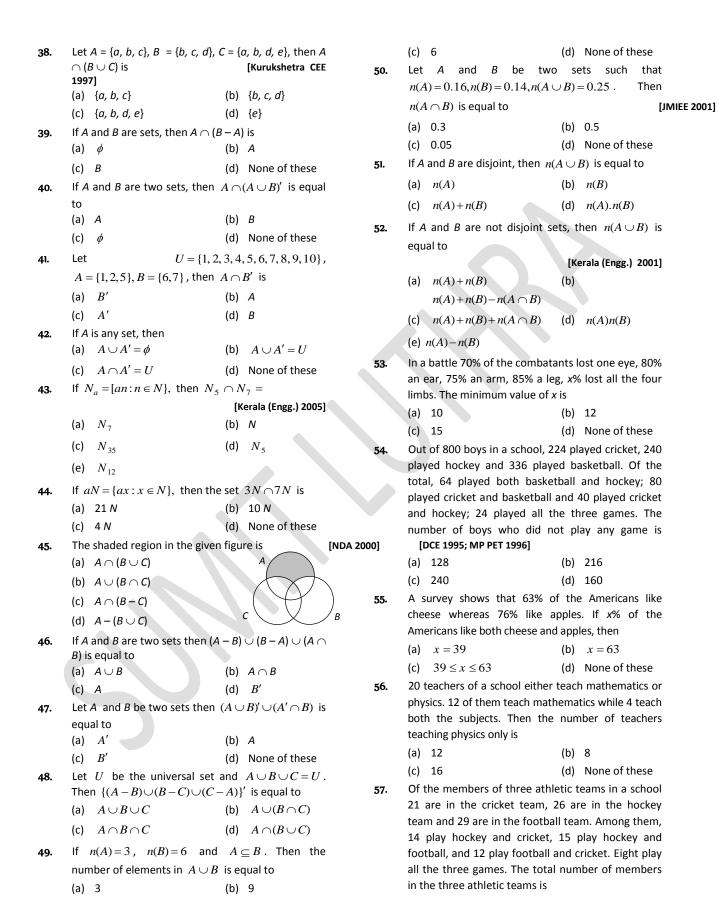
		$A = \{(x, y) : y = \frac{1}{x}, 0 \neq x \in R\}$					
1.	The set of intelligent students in a class is [AMU 1998] (a) A null set	$X = \{(x,y): y = x, 0 \neq x \in X\}$					
	(b) A singleton set	$B = \{(x, y) : y = -x, x \in R\}$, then					
	(c) A finite set	(a) $A \cap B = A$ (b) $A \cap B = B$					
	(d) Not a well defined collection	(c) $A \cap B = \phi$ (d) None of these					
2.	Which of the following is the empty set	Let $A = [x : x \in R, x < 1];$					
2.	[Karnataka CET 1990]	$B = [x : x \in R, x-1 \ge 1]$ and $A \cup B = R - D$,					
	(a) $\{x:x \text{ is a real number and } x^2-1=0\}$	then the set D is					
	(b) $\{x : x \text{ is a real number and } x^2 + 1 = 0\}$	(a) $[x:1 < x \le 2]$ (b) $[x:1 \le x < 2]$ (c) $[x:1 \le x \le 2]$ (d) None of these If the sets A and B are defined as					
	(c) $\{x : x \text{ is a real number and } x^2 - 9 = 0\}$						
	(d) $\{x : x \text{ is a real number and } x^2 = x + 2\}$	$A = \{(x,y): y = e^x, x \in R\};$					
3.	The set $A = \{x : x \in R, x^2 = 16 \text{ and } 2x = 6\}$	$B = \{(x,y) : y = x, x \in R\}, \text{ then}$ [UPSEAT 1994, 99, 2002]					
	equals	(a) $B \subseteq A$ (b) $A \subseteq B$					
	[Karnataka CET 1995]	(c) $A \cap B = \phi$ (d) $A \cup B = A$					
	(a) ϕ (b) {14, 3, 4}	If $X = \{4^n - 3n - 1 : n \in N\}$ and					
	(c) {3} (d) {4}	$Y = \{9(n-1) : n \in N\}$, then $X \cup Y$ is equal to					
4.	If a set A has n elements, then the total number of subsets of A is [Roorkee 1991; Karnataka CET 1992, 2000]	(a) X (b) Y					
	(a) n (b) n^2	(c) N (d) None of these					
	13.	Let $n(U) = 700, n(A) = 200, n(B) = 300$ and					
_	(c) 2^n (d) $2n$ The number of proper subsets of the set $\{1, 2, 3\}$ is	$n(A \cap B) = 100$, then $n(A^c \cap B^c) =$					
5.	[JMIEE 2000]	(a) 400 (b) 600					
	(a) 8 (b) 7	(c) 300 (d) 200					
	(c) 6 (d) 5	In a town of 10,000 families it was found that 40%					
6.	Given the sets $A = \{1, 2, 3\}, B = \{3, 4\}, C = \{4, 5, 6\},$	family buy newspaper <i>A</i> , 20% buy newspaper <i>B</i> and 10% families buy newspaper <i>C</i> , 5% families buy <i>A</i>					
	then $A \cup (B \cap C)$ is [MNR 1988; Kurukshetra CEE 1996]	and B, 3% buy B and C and 4% buy A and C. If 2%					
	(a) {3} (b) {1, 2, 3, 4}	families buy all the three newspapers, then number					
	(c) {1, 2, 4, 5} (d) {1, 2, 3, 4, 5, 6}	of families which buy A only is [Roorkee 1997]					
7.	If A and B are any two sets, then $A \cup (A \cap B)$ is	(a) 3100 (b) 3300					
	equal to	(c) 2900 (d) 1400					
	[Karnataka CET 1996] (a) A (b) B 15.	In a city 20 percent of the population travels by car,					
		50 percent travels by bus and 10 percent travels by both car and bus. Then persons travelling by car or bus is					
_							
8.	If A and B are two given sets, then $A \cap (A \cap B)^c$ is	[Kerala (Engg.) 2002]					
	equal to [AMU 1998; Kurukshetra CEE 1999]	(a) 80 percent (b) 40 percent					
	(a) A (b) B	(c) 60 percent (d) 70 percent					
	(c) ϕ (d) $A \cap B^c$	In a class of 55 students, the number of students					

If the sets A and B are defined as

studying different subjects are 23 in Mathematics,

24 in Physics, 19 in Chemistry, 12 in Mathematics

and Physics, 9 in Mathematics and Chemistry, 7 in If $Q = \left\{ x : x = \frac{1}{y}, \text{ where } y \in N \right\}$, then Physics and Chemistry and 4 in all the three subjects. The number of students who have taken (b) $1 \in Q$ exactly one subject is [UPSEAT 1990] (a) 6 (b) 9 (c) $2 \in Q$ (d) All of these (c) 7 If A, B and C are any three sets, then $A \times (B \cup C)$ is 17. Which set is the subset of all given sets $\{1, \overline{2}, \overline{3}, \overline{4}, \dots \}$ (b) {1} (b) $(A \cup B) \times (A \cup A)$ (a) $(A \times B) \cup (A \times C)$ (c) {0} (d) {} C) Let $S = \{0,1,5,4,7\}$. Then the total number of 28. (c) $(A \times B) \cap (A \times C)$ (d) None of these subsets of S is 18. If A, B and C are any three sets, then $A - (B \cup C)$ is (b) 32 (a) 64 equal to (c) 40 (d) 20 (a) $(A - B) \cup (A - C)$ (b) $(A - B) \cap (A -$ The number of non-empty subsets of the set {1, 2, 3, 4} 29. C) (c) $(A-B)\cup C$ (d) $(A-B) \cap C$ [Karnataka CET 1997; AMU 1998] If A, B and C are non-empty sets, then $(A - B) \cup (B -$ 19. (b) 14 (a) 15 A) equals [AMU 1992, 1998; DCE 1998] (d) 17 (c) 16 (a) $(A \cup B) - B$ (b) $A - (A \cap B)$ (c) $(A \cup B) - (A \cap B)$ (d) $(A \cap B) \cup (A \cup A)$ (a) {2, 3, 5} (b) {3, 5, 9} (c) {1, 2, 5, 9} (d) None of these If $A = \{2, 4, 5\}$, $B = \{7, 8, 9\}$, then $n(A \times B)$ is equal 20. If $A \cap B = B$, then [JMIEE 2000] (a) $A \subset B$ (b) $B \subset A$ (a) 6 (b) 9 (d) 0 (c) $A = \phi$ (d) $B = \phi$ (c) 3 21. If the set A has p elements, B has q elements, then If A and B are two sets, then $A \cup B = A \cap B$ iff 32. the number of elements in $A \times B$ is [Karnataka CET 1999] (a) $A \subseteq B$ (b) $B \subseteq A$ (b) p+q+1(a) p+qof (c) A = B(d) None (c) pq these If $A = \{a,b\}, B = \{c,d\}, C = \{d,e\},$ then 22. Let A and B be two sets. Then 33. (b) $A \cap B \subset A \cup B$ $\{(a,c),(a,d),(a,e),(b,c),(b,d),(b,e)\}$ is equal to (a) $A \cup B \subseteq A \cap B$ [AMU 1999; Him. CET 2002] (c) $A \cap B = A \cup B$ (d) None of these (a) $A \cap (B \cup C)$ (b) $A \cup (B \cap C)$ Let $A = \{(x, y) : y = e^x, x \in R\}$, 34. (d) $A \times (B \cap C)$ (c) $A \times (B \cup C)$ $B = \{(x, y) : y = e^{-x}, x \in R\}.$ Then If P, Q and R are subsets of a set A, then $R \times (P^c \cup P^c)$ 23. (a) $A \cap B = \phi$ (b) $A \cap B \neq \phi$ $Q^{c})^{c} =$ [Karnataka CET 1993] (c) $A \cup B = R^2$ (d) None of these (a) $(R \times P) \cap (R \times Q)$ (b) If $A = \{2, 3, 4, 8, 10\}, B = \{3, 4, 5, 10, 12\},$ 35. $(R \times Q) \cap (R \times P)$ $C = \{4, 5, 6, 12, 14\}$ then $(A \cap B) \cup (A \cap C)$ is equal to (c) $(R \times P) \cup (R \times Q)$ (d) None of these (b) {2, 8, 10} (a) {3, 4, 10} In rule method the null set is represented by 24. [Karnataka CET 1998] (c) {4, 5, 6} (d) {3, 5, 14} If A and B are any two sets, then $A \cap (A \cup B)$ is 36. (a) {} (b) ϕ equal to (c) $\{x : x = x\}$ (d) $\{x: x \neq x\}$ (a) A (b) B 25. $A = \{x : x \neq x\}$ represents [Kurukshetra (d) B^c (c) A^c **CEE 1998]** If A, B, C be three sets such that $A \cup B = A \cup C$ and 37. (a) {0} (b) {} $A \cap B = A \cap C$, then [Roorkee 1991] (c) {1} (d) $\{x\}$ (a) A = B(b) B = C(c) A = C(d) A = B = C





- (c) $\phi \in \{a, b, c\}$
- (d) None of these
- 77. If $A = \{x : x \text{ is a multiple of 4}\}$ and $B = \{x : x \text{ is a multiple of 6}\}$ then $A \subset B$ consists of all multiples of [UPSEAT 2000]
 - (a) 16

(b) 12

(c) 8

- (d) 4
- 78. A class has 175 students. The following data shows the number of students obtaining one or more subjects. Mathematics 100, Physics 70, Chemistry 40; Mathematics and Physics 30, Mathematics and Chemistry 28, Physics and Chemistry 23; Mathematics, Physics and Chemistry 18. How many students have offered Mathematics alone

[Kerala (Engg.) 2003]

(a) 35

(b) 48

(c) 60

(d) 22

- (e) 30
- **79.** Consider the following relations :
 - (1) $A B = A (A \cap B)$
 - (2) $A = (A \cap B) \cup (A B)$
 - (3) $A (B \cup C) = (A B) \cup (A C)$

which of these is/are correct

- (a) 1 and 3
- (b) 2 only
- (c) 2 and 3
- (d) 1 and 2
- **80.** If two sets A and B are having 99 elements in common, then the number of elements common to each of the sets $A \times B$ and $B \times A$ are
 - (a) 2^{99}

(b) 99^2

(c) 100

(d) 18

- (e) 9
- **81.** Given n(U) = 20, n(A) = 12, n(B) = 9, $n(A \cap B) = 4$, where U is the universal set, A and B

are subsets of *U*, then $n((A \cup B)^C) =$

(a) 17

(b) 9

(c) 11

(d) 3

(e) 16

Inswers

	1	d	2	b	3	а	4	С	5	С
	6	b	7	а	8	d	9	С	10	b
	11	С	12	b	13	С	14	b	15	С
	16	d	17	a	18	b	19	С	20	b
	21	С	22	С	23	a,b	24	d	25	b
[NDA 2003	26	b	27	d	28	b	29	а	30	b
	31	b	32	С	33	b	34	b	35	а
	36	а	37	b	38	а	39	а	40	С
	41	b	42	b	43	С	44	а	45	d
	46	а	47	а	48	С	49	С	50	С
	51	С	52	b	53	а	54	d	55	С
	56	а	57	а	58	d	59	С	60	b
,	61	d	62	а	63	а	64	b	65	b
3	66	а	67	b	68	С	69	а	70	е
	71	С	72	С	73	а	74	d	75	d
	76	а	77	b	78	С	79	d	80	b
	81	d								