



ACCELERATED MATHEMATICS

CHAPTER 1

NUMBER SENSE & ALGEBRAIC REASONING



TOPICS COVERED:

- Rational Numbers
- Operations with Decimals
- Squares and Square Roots
- Exponents
- Order of operations
- Algebraic Expressions and Equations
- Variables
- Properties of numbers



Frosted Fudge Cakes:



Swiss Cake Rolls:



Oatmeal Creme Pies:



Devil Squares: _



Cosmic Brownies:





Nutty Bars:__



Zebra Cakes:





Star Crunch:



Honey Buns:_____

The First Day of School

I want my students to know the following...

- 1. I want to be here.
- 2. I want you to be here.
- 3. I am excited about getting started.
- 4. I am enthusiastic and optimistic about the opportunities you will have.

5. You are important.

6. I am here to help you and learn with you – all of you.

1	This is the grade I entered Southlake schools:	
2	In my house the following adults live	
3	In my house the following kids live (list names and ages)	
4	In my house the following pets live (name and animal)	
5	Something special and unique about me is	
6	My greatest talent is	
7	My favorite subject(s) are	
8	The thing I most want to improve is	
9	Careers that might interest me are	
10	In my free time my hobbies include	
11	My favorite sports are	
12	The one song, TV show, or book I will always remember from this summer is	
13	My favorite movie of all-time is	
14	My favorite book or book series is	
15	The three people I admire the most are	
16	If I were an animal I would be a	
17	A responsibility I handle well is	
18	If I were principal of this school the one thing I would change is	
19	If I was going to eat only one food item for the entire next week it would be	
20	Major favorite restaurant is	
21	My favorite dessert is	
22	Other than people and pets the two possessions I most value in my house are	
23	My most memorable event is	

24	Places I have traveled include	
25	If I could visit any country or city outside the US it would be	
26	One thing that really gets on my nerves is	
27	The happiest day of my life was	
28	I was really sad when I learned that	
29	The best opportunity I ever had was	
30	If you were allowed to stop going to school, would you?	
31	The wildest and craziest thing I have ever done is	
32	If I were given \$1,000 to help other people I would spent it	
33	My fifth grade teachers would describe me as	
34	My parents would describe me as	
35	My best friend would describe me as	
36	What I am most proud of having accomplished in the past year is	
37	The luckiest thing that ever happened to me was	
38	If I could invite five famous people, dead or alive, to come eat dinner with me I would choose	
39	If I could grow up to be famous and successful, I would like to be known for	
40	In 5 th grade the place in school where I felt most important wasbecause	
41	<i>Think carefully about this one.</i> What I wish my teachers knew about me is	

(Taken from Cooperative Group Problem Solving – Frank Schaffer Publications, Inc.)

You are a crew member of the spaceship *DukeRules*! Your mission has been to search for life forms in space and return safely to Earth. The mission has been jeopardized because of problems with the cooling systems in your spaceship. You have been forced to land 175 miles from your space station, which is on the lighted surface of Mangham Moon. Mangham Moon has a circumference of 350 miles. Because of a difficult landing, your crew has been forced to evacuate quickly. Moments after the evacuation, an explosion destroyed most of the contents of your spaceship. All that remains are the 15 items listed below.

Your crew's survival depends on reaching the space station. You must choose the most important items from surviving gear, those which will have the most value in reaching the space station.

Place a number 1 alongside the most important item, number 2 by the second most important, and so on through number 15, the least important.

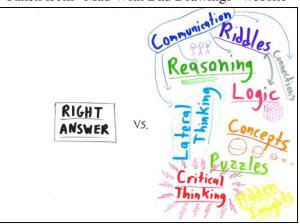
	You	Team	Expert	You/Expert	Team/Expert
A cigarette lighter					
Concentrated food					
60 feet of nylon rope					
Signal flares					
A magnetic compass					
Six 50-pound tanks of oxygen					
A case of dehydrated milk					
Parachute silk					
A solar-powered heating unit					
A 357 magnum pistol					
A map of this moon					
A self-inflating life raft					
5 gallons of water					
First-aid kit					
Solar-powered FM two-way radio					
			TOTAL		

Taken from "Mad With Bad Drawings" website

What is important in math?

The most common answer I get from students is "the right answer".

Sometimes that is true, but not all the time. There needs to be a balance between getting the answers and the process used to get the answers.



In this class there are times when you will be graded on the **process** and times when you will be graded on the **answer**.

Times when the process is more important

• Homework and classwork covering new material

Here I will usually emphasize the process. Showing your work shows me the process you used. Your grade could be up to 100% based on the work (process) you show to solve your questions.

Times when the process and the answers are balanced

• Quizzes, mini-projects over material we have covered for a few days

Often on these types of assignments both answers and process will count as part of your grade.

Times when answers are more important

• Tests, projects at the end of an entire unit to show mastery

Tests and final projects will emphasize the correct answers because you have now had numerous opportunities to practice the process. By this point in time you should know the process well enough to be able to get correct answers.

Showing your work is important so that both you can understand and I can understand your thought process. I don't ask you to show your work to make you spend more time on homework and classwork. The work you show could count anywhere from 0% to 100% of your grade.

What all students need for their future is as much about how they think as about what they know.

28	1,000,000	82%
3.14159	6.7	300%
$\frac{7}{8}$	0	$\frac{7}{2}$
1.8	0.123	-10
$\sqrt{17}$	$-\sqrt{25}$	20%
8	-6.2	157
$-5\frac{2}{3}$	$7\frac{1}{8}$	$\frac{27}{3}$
5.0	$-\frac{3}{2}$	

Place the following numbers in the correct place on the diagram on Activity 1-4.

REAL NUMBERS

All rational and irrational numbers.

RATIONAL NUMBERS

All numbers that are not irrational. Any number that can be written as a fraction.

IRRATIONAL NUMBERS

All non-repeating, non-terminating decimals.
 All square roots of non-square numbers.

INTEGERS

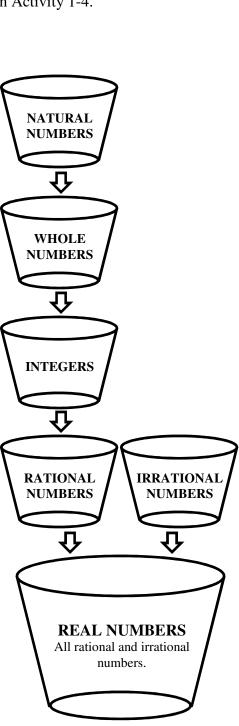
{...-3, -2, -1, 0, 1, 2, 3, ...}

WHOLE NUMBERS

 $\{0, 1, 2, 3, 4, \ldots\}$

NATURAL NUMBERS (Counting Numbers)

 $\{1, 2, 3, 4, \ldots\}$



REAL NUMBE	RS	IMAGINARY NUMBERS
INTEGERS WHOLE NUMBERS NATURAL NUMBERS	IRRATIONAL	Yes, there are such things as imaginary numbers! They all consist of the square root of -1. In fact they are not really imaginary, but they are planar. It is like rotating a point "anti- clockwise". If you are counting stones, fractions are meaningless. If you are measuring the mass of an object, negative numbers are meaningless. For many things imaginary numbers are meaningless, but some things they are very important: electromagnetism, cartography, vibration analysis, quantum mechanics, signal processing Sounds interesting, huh? You will learn more about imaginary numbers in Algebra II.
RATIONAL NUMBERS	NUMBERS	

Which of the following statements about integers, whole numbers, natural numbers and rational numbers is true?

- A Sets of whole numbers include negative and positive whole numbers.
- B Sets of integers and whole numbers include natural numbers.
- C Sets of whole numbers and natural numbers include decimals.
- D Sets of rational numbers do not include integers.

Natural Numbers start at 1 and are counting numbers 1, 2, 3, etc.

Whole Numbers start at 0 and are counting numbers 0, 1, 2, 3, etc.

Integers include all whole numbers and their opposites $\dots -3, -2, -1, 0, 1, 2, 3 \dots$

Rational Numbers include mixed numbers, decimals, integers, and whole numbers. They also include any repeating decimals.

Irrational Numbers cannot be written as a fraction. This includes non-repeating, non-terminating decimals (ex. 53.66563146....). All square roots of non-square numbers are also irrational (ex. $\sqrt{8}$ and $\sqrt{33}$).

Real Numbers are all rational and irrational numbers.

Check all the sets of numbers to which each number belongs.

	ck all the sets of r	Natural Numbers	Whole Numbers	Integers	Rational Numbers	Irrational Numbers	Real Numbers
1.	0						
2.	-0.15						
3.	-5						
4.	$\sqrt{7}$						
5.	$\frac{28}{4}$						
6.	$21\frac{1}{2}$						
7.	0.13						
8.	$-1\frac{1}{3}$						
9.	-625.0						
10.	0.14159						
11.	$-\frac{2}{3}$						
12.	$\frac{\sqrt{64}}{5}$						
13.	$\frac{5}{\frac{3}{5}}$						
14.	-1.7						
15.	6.27819234						
16.	$-\frac{6}{2}$						

Show all work on a separate sheet of paper.

1.	2.135 + 1.5		2.	14.688 + 0.384		3.	2.4 + 1.47	
4.	32.4 + 10.82		5.	3.45 + 4.18 + 5.21		6.	43.6 + 5.327	
7.	2.135 – 1.5		8.	14.688 - 0.384		9.	2.4 - 1.47	
10.	32.4 - 10.82		11.	12 - 5.003		12.	43.6 - 5.327	

Solve the following decimal addition and subtraction problems.

Solve the following decimal multiplication problems.

13.	6•0.35	14.	27 • 0.21	
15.	1.21•3.2	16.	26•1.5	
17.	4.25•5.4	18.	3.4•4.2	

 $\frac{5}{5} \xrightarrow{5} 5 \overline{68.5}$ 5.)6 don't need

Example: $\frac{30.5}{0.005} \rightarrow \frac{\bullet 1000}{\bullet 1000} = \frac{30500}{5} = 6100$

Solve the following decimal division problems. Record all answers as decimals.

19.	$\frac{1.2}{6}$	20.	$\frac{3.00}{12}$	21.	$\frac{2.46}{12}$	
22.	$\frac{0.0079}{2}$	23.	$\frac{5.04}{14}$	24.	$\frac{0.99}{6}$	
25.	1.35÷0.9	26.	$0.935 \div 0.5$	27.	19.95÷1.9	
28.	$\frac{0.105}{0.00005}$	29.	$\frac{141.62}{0.73}$	30.	2.279÷5.3	

31.	You took a car trip that was exactly 496.8 miles. The trip took 9 hours. What was your average speed (miles per hour)?
32.	Mr. Mangham's bank account had a starting balance of \$125.36. He spent one-fourth of his money to buy a gift for his sister. He then writes a check in the amount of \$26.50 to pay for his home electricity. What is the balance in Mr. Mangham's bank account?
33.	Your car gets about 19.8 miles to the gallon. If you buy 12 gallons of gas, how many miles can you expect to drive?
34.	The temperature outside is 78.3 degrees. How far away from 100 degrees is it?

Solve the following decimal word problems.

1.	If apples cost \$0.89 a pound and Mr. Wyrick buys 2.4 pounds, how much will they cost (do not round)?						
2.	If bananas cost \$0.59 a pound and Mrs. Leidner buys 6.2 pounds of bananas, how much will they cost (do not round)?						
3.	If Mrs. Scogin runs 3.1 miles for 125 straight days, how far did she run?						
4.	Mrs. Fauatea ran the 400 meter dash in 51.18 seconds. If she ran this same speed on 13 consecutive runs, what would her total time be?						
5.	The cost of 12 gallons of gas is \$14.28. How much would you pay per gallon?						
6.	Your car travels an average of 19.7 miles per gallon in the city and 23.8 miles per gallon on the highway. On an 11-gallon tank of gas how much farther can you travel on the highway than in the city?						
7.	Mr. Silvia bought a dozen donuts for \$3.38 and they gave him an additional donut free. What is Mr. Silvia's cost per donut?						
8.	Write and solve an expression to determine how many 0.3 meter pieces of duct tape can be cut from an 8.4 meter roll.						
9.	Mr. Mangham combined 6.8 pounds of chocolate with 7.6 pounds of peanut butter. He put the mixture into jars holding 0.3 pounds each. How many jars did he use?						
Bon	us On 2/2/00, the date had all even digits. Which day before this date was the last to have all even digits?						

Below are the length and width of rectangles. Determine the perimeter and area of each rectangle.

10.	Length = 6.2 in	Width = 4.8 in	11.	Length $= 9.1$ in	Width = 5.22 in
12.	Width = 9.8 in	Length = 4.51 in	13.	Width = 7.6 in	Length = 7.6 in

14.	When you	• by	A number > 1	your answer gets	
15.	When you	\div by A number > 1		your answer gets	
16.	When you • by		A number between 0 and 1	your answer gets	
17.	17. When you ÷ by		A number between 0 and 1	your answer gets	

A Day at The Ballpark in Arlington

1.	Mr. Mangham wanted to know if the Red Sox had any pitchers that were good. He found the following pitcher's ERA's (how many runs a pitcher gives up): 2.76, 2.307, 2.706 What is the difference between the lowest and highest ERA's?							
	e middle of the fifth inning with the Rangers leading 4-3, Mr. Mangham decided to go to the snack The following items were for sale:							
	COTTON CANDY\$4.05SNOW CONE\$2.19CRACKER JACKS\$5.82FRITO PIE\$7.25FUNNEL CAKE\$6.60DR. PEPPER\$4.50PEANUTS\$3.47LEMONADE\$3.95							
2.	How much is it for 2 Frito pie's and 2 Dr. Pepper's?							
3.	How much more is it for 4 Cracker Jacks than for 3 peanuts?							
4.	If Mr. Mangham order a Frito pie and a lemonade and pays with \$20, how much change will he receive?							
5.	If you get 80 peanuts in a bag, how much does each peanut cost (to the nearest hundredth)?							
6.	If your Dr. Pepper contains 24 ounces, how much does it cost per ounce (exactly)?							
7.	If the lemonade contains 0.25 liters, how much does it cost per liter?							
	lly Mr. Mangham makes it back to the game and looks to see how well the Rangers' batters have e this season. He finds the following 8 batting averages (how often a batter gets a hit):							
	0.312 0.267 0.330 0.291 0.321 0.282 0.259 0.304							
8.	If you were one of the best batters of all-time, you might have a batting average of 0.4. How far away is the batter who is hitting 0.267?							
9.	What is the sum of the three highest batting averages?							
10.	Texas hits a homerun that traveled 0.078 miles (which over 400 ft.). If it traveled at 0.03 miles per second, how long did it take to get out of the park?							
11.	How long would it take if the ball traveled 0.015 miles per second?							

Below are two measurements of rectangles. Determine the perimeter and length or width of each rectangle.

12.	$A = 32.5 in^2$	Length = 6.5 in	13.	$A = 38.5 in^2$	Length = 5.5 in
14.	$A = 42.75 in^2$	Width = 9.5 in	15.	$A = 72.25 in^2$	Width = 8.5 in

Google is a play on the word googol. It refers to the number represented by the numeral 1 followed by 100 zeros. Google's use of the term reflects the company's mission to organize the immense, seemingly infinite amount of information available on the web. You couldn't count to a googol in a million lifetimes!

So a googol is:

So what about a googolplex? A googolplex is 1 with a googol of zeros. Can you imagine how big that is? If you wrote 1 zero every inch there would not be enough room to write this number if you went to the farthest star in the universe.

So what are some other large numbers?

Thousand, Million, Billion, Trillion, Quadrillion, Quintillion, Sextillion, Septillion, Octillion, Nontillion, Decillion, Undecillion, and a Duodecillion would be 1 with 39 zeros

Continuing

Tredecillion (42 zeros), Quattuordecillion (45 zeros), Quidecillion (48 zeros), Sexdecillion (51 zeros), Septendecillion (54 zeros), Octadecillion (57 zeros), Novemdecillion (60 zeros), Vigintillion (63 zeros), Unvigintillion (66 zeros), Duovigintillion (69 zeros), Trevigintillion (72 zeros), Quattuorvigintillion (75 zeros)

Q: On what day will you celebrate having been alive for one billion seconds? How old will you be?

Really big numbers are hard to comprehend. They get so big it is hard to tell them apart! Is \$1 trillion dollars that much more than \$1 billion or \$1 million? Think about this:

One trillion miles will get you to Pluto – 350 times!

A million seconds ago was 12 days ago. A billion seconds ago was 50 years ago. A trillion seconds ago Neanderthal man was walking the Earth because it was 31,688 years ago!!!

If you made 1 million dollars every day starting today, you would have 1 trillion dollars in 2737 years.

Starting Amount (\$)	Duration of Shopping Spree	Starting Amount (\$)	Duration of Shopping Spree	
1	1 second	1,000,000	13 hr, 48 min	
100	5 seconds	10,000,000	5 days, 19 hr	
1,000	50 seconds	100,000,000	57 days, 21 hr	
10,000	8 min, 20 sec	1,000,000,000	1 yr, 214 days	
100,000	1 hr, 23 min	1,000,000,000,000	1585 years	

How about a spending spree with where you spend \$20 per second?

My Pick	Star Wars Character	Height	Brains	Dark Side	Jedi Powers	Battle Skills	Force Factor
		h	b	d	j	S	f
	Luke Skywalker	1.72m	15	4	90	43	4
	Princess Leia	1.5m	17	1	50	38	4
	Chewbacca	2.28m	12	5	10	55	4
	СЗРО	1.67m	19	0	0	8	6
	R2D2	0.96m	14	0	0	14	6
	Lando Calrissian	1.78m	15	8	6	48	2
	Obi-Wan Kenobi	1.75m	18	1	80	26	6
	Yoda	0.66m	20	0	100	10	5
	Wedge Antilles	1.7m	11	3	10	37	3
	Imperial Stormtrooper	1.83m	9	19	1	49	3
	Jabba the Hutt	3.9m	13	20	0	10	3
	Darth Vader	2.02m	16	22	82	55	4
	Emperor Palpatine	1.73m	14	25	95	25	5
	Boba Fett	1.83m	11	20	17	49	4
	Han Solo	1.8m	13	6	4	50	3
	Anakin Skywalker	1.93m	16	10	82	55	4
	Qui-Gon Jinn	1.95m	19	2	65	41	1
	Queen Amidala	1.65m	17	2	30	40	3
	Jar Jar Binks	1.96m	2	5	20	30	3
	Darth Maul	1.75m	9	24	80	48	1

Pick your top 5 characters (rank 1 to 5)

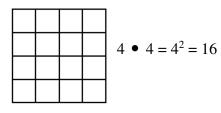
What is your Star Wars name?

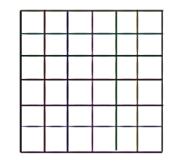
L			

Your first name:First three letters of your last name + First two letters of your first nameYour last name:First two letters of your mom's maiden name + First three letters of the city
where you were born

$1^{2} = 1$ $2^{2} = 4$ $3^{2} = 9$ $4^{2} = 16$	$5^{2} = 25$ $6^{2} = 36$ $7^{2} = 49$ $8^{2} = 64$	$10^2 = 100$ $11^2 = 121$	$\sqrt{1} = 1$ $\sqrt{4} = 2$	$\sqrt{25} = 5$	$\sqrt{64} = 8$ $\sqrt{81} = 9$ $\sqrt{100} = 10$		
Read 5^2 as "five squared." The 2 is called an exponent. Read $\sqrt{16}$ as "the square root of 16." The symbol, $$ called a radical sign . Both the squared sign and the square root sign are exponents.							

You are finding the **square** of a number when you multiply a number by itself.





$$6 \bullet 6 = 6^2 = 36$$

On a separate sheet of paper make a **drawing** to demonstrate each problem.

1.	3 ²	2. 7^2	3.	$\sqrt{25}$
4.	A side length of $\sqrt{9}$	5. A square with an area of 36 sq. units	6.	9 ²
7.	Arrange 16 marbles to demonstrate 4^2	8. $\sqrt{1}$		8 ²
10.	How many square inches are Draw a picture to prove your			

Find each square.

11.	17 ²	1	12.	30 ²	13.	24 ²	
14.	15 ²	1	15.	40^{2}	16.	22^{2}	
17.	100 ²	1	18.	45 ²	19.	31 ²	

Find each square root.

1.	$\sqrt{225}$	2.	$\sqrt{576}$	3.	$\sqrt{1225}$	
4.	$\sqrt{3600}$	5.	$\sqrt{0.09}$	6.	$\sqrt{0.0016}$	
7.	$\sqrt{900}$	8.	$\sqrt{0.25}$	9.	$\sqrt{729}$	

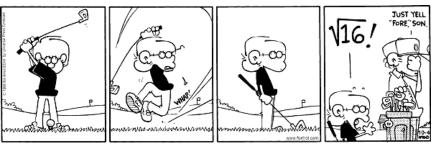
Find two consecutive whole numbers between which the square roots lie.

10. $\sqrt{76}$ 11. $\sqrt{130}$ 12. $\sqrt{200}$ 13. $\sqrt{500}$	
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Solve. Round your answer to the nearest tenth, if necessary. Draw a number line on a separate sheet of paper, label the whole numbers, and plot your answers.

14.	$\sqrt{60}$	15.	$\sqrt{10}$	16.	$\sqrt{120}$	
17.	$\sqrt{200}$	18.	$\sqrt{5}$	19.	$\sqrt{150}$	
20.	$\sqrt{2}$	21.	$\left(\sqrt{1225}\right)^2$	22.	$\sqrt{300}$	

23.	Which of the following could represent $\sqrt{225}$?A. 5 rows of 45 squaresB. 15 rows of 15 squaresD. 3 rows of 75 squares				
24.	I am larger than 15^2 and smaller than 16^2 . I am odd and divisible by 3. The product of my digits is 24. Who am I?				
25.	When, if ever, can $x^2 = 2x$?				
26.	The first five square numbers are 1, 4, 9, 16, and 25. Determine how many factors each one has. Do you notice any similarity in your numbers?				
27.	A lot is a square with each side being 72 feet long. What is the area of the lot?				
28.	The area of a square room is 150 square feet. To the nearest integer, how long is each side?				



Created by Lance Mangham, 6th grade math, Carroll ISD

Edge Length	Volume (multiply)	Volume (exponents)	Volume of cube	Edge Length	Volume (multiply)	Volume (exponents)	Volume of cube
2	$2 \times 2 \times 2$	2^{3}	8	7			
4				8			
5				9			
6				10			

1. Complete the table to show the volume of each cube in exponential form and in cubic feet.

Did You Know: If you know the volume of a cube you can find the edge length by finding the cube root. The symbol for the cube root is $\sqrt[3]{}$. For example, a cube with a volume of 27 would have an edge length of $\sqrt[3]{27} = 3$.

Compute.

2.	7^{3}	3		54	
4.	6 ³	5	5.	10^{5}	
6.	$(0.4)^3$	7	'.	9 ³	
8.	20 ³	9).	$(0.01)^3$	
10.	1.4 ³	11	1.	2 ⁵	
12.	3 ⁴	13	3.	10^{6}	
14.	The volume of a cube is 343 ft^3 . What is the length of each side?	15	5.	∛125	
16.	If $a+b=12$ and $a^2+b^2=80$, find				

Write each expression using exponents.

17.	4•4	1	18.	5•5•5•5•5•5
19.	2•2•2•2•2•2•2•2•2	2	20.	2•2•3•2•5
21.	2•3•2•3•2	2	22.	2•3•2•5•2•3•2
23.	$3 \bullet 3 \bullet 5 \bullet 7 \bullet x \bullet x$	2	24.	$5 \bullet 7 \bullet 7 \bullet r \bullet r \bullet t \bullet t \bullet t$
25.	8 to the fourth power	2	26.	<i>m</i> to the third power

G	Grouping symbols (), [], { } also the fraction bar $\frac{a}{b}$ groups <i>a</i> together, then <i>b</i> together, then <i>y</i> ou divide last.
Е	Exponents ex. x^2 or \sqrt{x}
MD	Multiplication and Division from left to right
AS	Addition and Subtraction from left to right

Circle the operation that should be performed first in each expression.

1.	$(9+3) \bullet 7$	2.	98-5•7	3.	$5 \bullet (\sqrt{9} - 1)$
4.	$\left(\frac{15}{3}\right) + (4+5)$	5.	$\frac{8^2 - 2 \bullet 10}{30 - 8}$	6.	$5(5-3) \bullet 2$
7.	5+4•7	8.	13(6 + 3)	9.	$32 \div 4 \bullet 2$

Solve. Use the tornado method and show all work and answers on a separate sheet of paper.

10.	2(16 - 9) - (5 + 1)	11.	$(43 - 23) - 2 \bullet 5$	12.	$90 - 45 - 24 \div 2$
13.	81 ÷ (13 – 4)	14.	$7 \bullet 8 - 2 \bullet 8$	15.	$10^2 \bullet 3^2 + 1$
16.	$5 + 42 \div 3 - 3^2$	17.	$8 \bullet 3 + 2^2 - 1$	18.	$8 \bullet 3^2 + 7^2 - 2$
19.	$(15+9^2) \div 3-4$	20.	$(12-3) \div 3^2$	21.	$(34 + 46) \div 20 + 20$
22.	$18 \div 3 \bullet 6$	23.	$5^2 - 12 + 84 \div 3$	24.	$1 + 3 \bullet 4 + 5 - 3^2$
25.	$\frac{450 \div (3+3) \bullet 2}{3^2 + 1}$	26.	$\frac{9 \bullet 3 + 8^2}{\sqrt{64} - 1}$	27.	$\frac{125-5\bullet7}{2\sqrt{16}-2}$

Insert parentheses to make each statement true.

28.	$16 - 8 \div 4 + 10 = 12$	29.	$5 \bullet 5 + 5 - 5 = 45$
30.	$24 \div 4 \bullet 6 \div 12 = 3$	31.	$5 + 5 \bullet 5 - 28 \div 4 \bullet 7 = 1$

Compare. Use, <, >, or = to make each statement true.

32.	3 • (8 – 2)	3 • 8 - 2	33.	$(7+2) \bullet 4$	7 + 2 ● 4
34.	$4 + (20 \div 4)$	$(4 + 20) \div 4$	35.	42 – (35 + 4)	42 - 35 + 4

	Which does not represent 256 using exponents?	
1.	$2^8, 16^2, 8^3, 4^4$	

Evaluate each expression. For expressions with more than one operation use the tornado method.

2.	2 ⁵	3.	4 ³	4.	2^{3}
5.	$2^2 \bullet 3^2$	6.	$2^2 \bullet 11^3$	7.	$2 \bullet 5 \bullet 3^3$
8.	$3^3 + 2^2 \bullet 5^2$	9.	$(3^3-4^1)\bullet 2^2$	10.	$2^3 \bullet (5^2 \bullet 7^1)$
11.	$(7^2+2)\bullet 3^2$	12.	$\frac{14^2}{2^3+2^3}$	13.	$11^2 + 13^2$
14.	$\frac{6^2-2^2}{5^2}$	15.	$5^2 \bullet (7^3 + 4^2)$	16.	$2^6 - 3^3$
17.	$2^3 \bullet 3^2$	18.	$1^3 - 1^4 + 2^5$	19.	$2^2 \bullet 3^3 - 2^3 \bullet 3^2$
20.	$3+2^4+(5-2)^3$	21.	$2^5 + 5^3$	22.	$3^4 \bullet 5^2 + 2^3 \bullet 3^2$

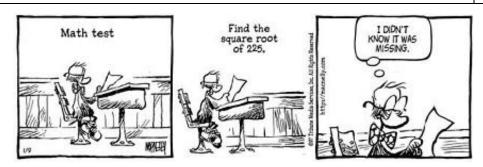
Write each power as the product of the same factor (write it out the long way).

23.	x^7	24.	$(-2)^4$	25.	61
26.	$(y+3)^2$	27.	13 ³	28.	5 ⁶
29.	18	30.	$(cd)^4$	31.	$(-g)^{5}$

Evaluate each expression if p = 1, m = 6, r = 2, y = 3, and z = 5.

32.	3ry	33.	p^2m^2	34.	$(rm)^2$
35.	$p^2(ry)$	36.	$2zy^2$	37.	$y^3r^3p^3$

38. Six farmers each have 6 barrels. In each barrel are 6 cats that each has 6 kittens. How many total legs are there?



Expressions vs. Equations

Expression: An expression is a mathematical phrase that combines numbers and/or variables using mathematical operations. It can be *simplified or evaluated*, but it cannot be solved.

There is no equal sign.

$$2+2$$
 $3x-5$ x^2-2x-8

Equation: An equation is a mathematical sentence that combines numbers and/or variables that shows the equality of two expressions. An equation is two expressions set equal to each other. It can usually be *solved*.

There must be an equal sign.

2+2=4 3x-5=7 $x^2-2x-8=0$

79-X 3t 6 W+12 13m 43-Z Expressions b-2 000,002-30 6÷3 131=100 nk=45 3X=2 13-h 00-X=9 1a= Ja 2 √= 72 W=2000

Created by Lance Mangham, 6th grade math, Carroll ISD

Kaadu lived on the planet Naboo. They were large flightless waterfowl. They were excellent runners and strong swimmers. They laid their eggs on land. Gungans like Jar Jar Binks rode on the kaadu.



First carton numbers:		Total:
Second carton numbers:		Total:
Egg carton letter:	Egg carton letter:	
Egg carton letter:	Egg carton letter:	
Egg carton letter:	Egg carton letter:	
	Egg carton letter.	

Jedi 3 #1		Jedi 3 #2	
EQUATIONS:	ANSWERS:	EQUATIONS:	ANSWERS:
тиаца		T - J! 2 #4	
Jedi 3 #3		Jedi 3 #4	
EQUATIONS:	ANSWERS:	EQUATIONS:	ANSWERS:
Jedi 4 #1		Jedi 4 #2	
EQUATIONS:	ANSWERS:	EQUATIONS:	ANSWERS:
Jedi 4 #3		Jedi 4 #4	
EQUATIONS:	ANSWERS:	EQUATIONS:	ANSWERS:

A *variable* is a symbol used to represent one or more numbers. Some of the following problems use a variable to represent an unknown amount.

For each story below, determine or write the correct mathematical expression or equation.

1. Darth Vader makes \$7.50 per party to attend birthday parties. He attends 8 parties in June and 6 parties in July. Which equation can be used to find the total amount Darth Vader made during those two months? A $t = $7.50(8 \cdot 8 + 6)$ B $t = $7.50(8 \cdot 8 + 57.50 \cdot 6)$ C $t = $7.50(6 \cdot 8 + 8)$ D $t = $7.50(8 \cdot 6)$	2. Luke Skywalker decides he wants to sell lemonade to all of his galactic friends. He buys 2 bags of cups and 6 packets of lemonade for a total of \$6.03. Each bag of cups costs \$1.29. Which equation can be used to find the total cost of one packet of lemonade? A $t = (\$1.29 \cdot 2) + 6.03$ B $t = \$6.03 - (6 \cdot \$1.29)$ C $t = (\$6.03 - 2 \cdot \$1.29) \div 6$
3. Princess Leia is a very good math student. Her average math grade was a 95 on her 15 tests. If Darth Mangham decides to drop her lowest grade, write an expression that could be used to determine her new test average. You do not need to solve.	D $t = (\$6.03 - \$1.29) \div 6$ 4. Jabba the Hut needs to drink a lot of water. His water tank contains 2,500 gallons. A faucet attached to the tank releases water at 5 gallons per minute. Write an expression to express the amount of water left after the faucet has been left open for 2 hours. You do not need to solve.
5. The Force Inc. employs 450 workers. It plans to increase its workforce by 8 employees per month until it has doubled in size. Which equation could be used to determine <i>m</i> , the number of months it will take to double in size? A $8m+450m=900$ B $2m+450=900$ C $2(8m+450)=900$ D $8m+450=900$	 6. Which situation is best represented by the equation 4 • h = 68? A Chewbacca had 68 pieces of candy to give to 4 friends. How many pieces of candy will each friend get? B If one gallon of water costs \$4, how many gallons of water will Han Solo need to drink to walk 68 miles? C Luke is 68 inches tall. How tall will he be if he grows 4 more inches? D Yoda read 4 pages of a book that is 68 pages long. How many pages does Yoda have left to read?
 7. Obi-Wan owns a Jedi training business. Each week, he buys 45 pints of "the force" for \$3.49 per pint. If he teaches an 18 week long class, which expression could be used to determine the total amount he spends on "the force"? A 3.49•18 B 3.49•45•18 C 45•18 D 45÷3.49•18 	8. C3PO and R2D2 are both building droids to help Luke. They work 8 hours a day. In one day, C3PO can make 9 droids and R2D2 can make 12 droids. Which equation shows how many total droids C3PO and R2D2 can build in 72 hours? A $(12+9) \cdot 8$ B $(12+9) \cdot 72$ C $(12+9)(72 \div 8)$ D $(12+9)(8 \div 72)$

Vocabulary:

A *variable* is a symbol used to represent one or more numbers.

A *variable expression* is a mathematical phrase that uses numbers, variables, and operation symbols.

Variable expressions are made up of one or more terms.

A *term* is a number, a variable, or the product or quotient of a number and a variable.

These variables represent information about a particular math class.

s = number of students in the class	g = number of girls in the class
r = number of students in the class with red hair	b = number of students in the class with black hair
t = number of textbooks given to each student	h = number of hours of classes each day

Tell what each of the following expressions represents.

1.	s-g	4.	s-b	
2.	5 <i>h</i>	5.	st	
3.	b+r	6.	$\frac{g}{s} \bullet 100$	

Write an expression for each of the following.

7.	the number of students who do not have red hair
8.	the number of textbooks handed out to girls
9.	the number of minutes of classes each day
10.	the number of textbooks handed out to all the students
11.	the percentage of students who have black hair

Write an equation for each of the following.

12.	2. there are 16 more students with black hair than students with red hair		
13.	there are twice as many students as girls		
14.	40% of the students have black hair		

Translate each equation into words. Then make a table showing four pairs of sample values that fit the equation.

15.	s = b + 21	
16.	b = 4r	
17.	s = 2g + 5	

Write an equation that says that y is equal to 1.25 times x. Then make a table of values that fit the equation. For x, pick whole numbers ranging from 1 to 10. Write y as a decimal. Show all work on a separate sheet of paper.

Phrases	Expression	Phrases	Expression
9 more than a number		4 subtracted from a number	
the sum of 9 and a number		a number minus 4	
a number plus 9	<i>x</i> +9	4 less than a number	h-4
a number increased by 9		a number decreased by 4	
the total of x and 9		the difference of h and 4	
Phrases	Expression	Phrases	Expression
6 multiplied by g		a number divided by 5	+
6 times a number	6 <i>g</i>	the quotient of t and 5	$\frac{i}{\overline{z}}$
the product of g and 6		divide a number by 5	5

Phrases	Equation
Sixty less than three times a number is \$59.	
Three times the amount less 60 is equal to 59.	
59 is equal to 60 subtracted from three times a	3n - 60 = 59
number.	
A number times three minus 60 equals 59.	

On a separate sheet of paper, write each phrase as an algebraic expression or equation.

1.	the total of 5 and c	2.	23 divided into y
3.	the product of <i>k</i> and 9	4.	the difference of 6 and r
5.	nine less than t	6.	a number increased by 7 is 11
7.	the price decreased by \$4 is \$29	8.	twice as many points as Bob would be 18 points
9.	after dividing the money 5 ways, each person got \$67	10.	three more than 8 times as many trees is 75 trees
11.	seven less than a number is 15	12.	the difference of six squared and a number is nine
13.	fourteen divided by a number is 21	14.	four times the number of feet is 12 feet
15.	27 is seven fewer students than last year	16.	the number of cats decreased by 17 is 19
17.	two and one-half times the amount of interest is \$2,500	18.	one hundred increased by a number is 537
19.	81 increased by <i>n</i>	20.	the sum of b squared and h
21.	three times the difference of a number and nine equals 15	22.	five less than a six times a number is equal to 5
23.	12 times the number of muffin pans	24.	the quotient of five divided by the sum of g and k
25.	two times a number decreased by 5 is equal to 8	26.	a service charge of \$20 plus a charge of \$3 per window cleaned
27.	two times the quantity <i>x</i> decreased by 8 is 23	28.	five times a number divided by 8 is one

1.	2m-5j	2.	3m + j	3.	$42 \div k + m$	
4.	j+m-k	5.	2j+k-m	6.	jm-k	

Evaluate each expression if j = 2, k = 7, and m = 9.

Evaluate each expression if x = 5, y = 4, and z = 3.

7.	x + z	8.	y+3-z	9.	x - x + 4	
10.	<i>xy</i> – 2	11.	<i>yz</i> +10	12.	<i>xz</i> +4	

For all problems below, use the tornado method and show all work on a separate sheet of paper.

13.	$\frac{a}{b}+5$	14.	3 <i>bc</i> – 7	15.	$\frac{b}{c} + a$
16.	$\frac{2a}{4}-b$	17.	3(b+a)-c	18.	2b-3c
19.	$\frac{2b}{c}$	20.	$\frac{6(a+c)}{b}$	21.	b(b+a)-b

Evaluate each expression if a = 8, b = 4, and c = 2.

Evaluate each expression if a = 12, b = 3, and c = 4, m = 9, n = 3.

22.	$\frac{m}{n}$ + 6	23.	10 <i>mn</i>	24.	$\frac{a}{c}-b$
25.	$\frac{3n}{m} + 4$	26.	3(n+n)-m	27.	4 <i>c</i> – 3 <i>b</i>
28.	$10-\frac{2m}{n}$	29.	$\frac{3(b+c)}{(b+c)}$	30.	b(c-b)+c

Evaluate each algebraic expression for the given values of the variables.

31.	$(b^2 - c) \bullet d - 4$, for $b = 6$, $c = 4$, and $d = 12$	
32.	$(a+b^2) \bullet c \div d$, for $a = 7, b = 2, c = 6$, and $d = 3$	
33.	$s^2 - 3 \bullet t \div v$, for $s = 5, t = 7$, and $v = 3$	

Will Anakin Skywalker restore order to the force? Will you restore order to the operations?

For all problems on this page, show all work using the tornado method on a separate sheet of paper. When necessary, round answers to the nearest tenth.

Back at the beginning of this unit you chose a Star Wars character to be for this unit. For the following order of operations, use your character and the numbers given to solve the following problems.

1.	The Tall and Small Index	10h+2b-d	
2.	The Smart Heart Index	$4(2b^2-df)$	
3.	The Dark Mark Index	$\frac{50d + 2s}{f}$	
4.	The Power Hour Index	$\frac{jsf}{(f+4)}$	
5.	The Skill and Chill Index	$4(b+j) - \frac{d}{2}$	
6.	The Force is the Source Index	$100f^2 + 5j - 3d$	

Apply the same indices to one of the following characters: C3PO, Qui-Gon Jinn, or Jabba the Hut.

7.	The Tall and Small Index	10h + 2b - d	
8.	The Smart Heart Index	$4(2b^2-df)$	
9.	The Dark Mark Index	$\frac{50d + 2s}{f}$	
10.	The Power Hour Index	$\frac{jsf}{(f+4)}$	
11.	The Skill and Chill Index	$4(b+j) - \frac{d}{2}$	
12.	The Force is the Source Index	$100f^2 + 5j - 3d$	

Create a brand new index name and formula and apply it to the characters below.

New name:	New formula:

13.	Yoda	14.	Darth Maul	
15.	Chewbacca	16.	Princess Leia	

CAPIC	.551011.	
1.		3 times a number
2.		3 more than a number
3.		3 decreased by a number
4.		3 less than a number
5.		one third of a number
6.		8 more than 3 times a number
7.		8 less than 3 times a number

Translate each phrase below into an algebraic expression. Write the correct letter next to each expression.

Α	<i>x</i> +3
В	3x-8
C	x-3
D	3 <i>x</i> +8
Е	3 <i>x</i>
F	3-x
G	$\frac{x}{3}$

8.	7 less than 4 times a number		
9.	7 decreased by 4 times a number		
10.	9 less than twice a number		
11.	9 decreased by twice a number		
12.	9 less than half a number		
13.	7 times a number, increased by 4		
14.	7 times a number, increased by 4 times the number		

15.	5 times a number, increased by 8		
16.	5 times the sum of a number and 8		
17.	5 more than 8 times a number		
18.	8 times the sum of a number and 5		
19.	twice the sum of 5 times a number and 8		
20.	2 more than five-eighths of a number		
21.	8 times the sum of twice a number and 5		

22.	9 meters higher than altitude x
23.	15 meters per second slower than speed x
24.	15 degrees hotter than temperature x
25.	9 meters shorter than twice length x
26.	9 years older than twice age x
27.	\$9 cheaper than 4 times price x
28.	9 centimeters less than three-fourths of length x

Η	7 - 4x
Ι	2x - 9
J	7 <i>x</i> +4
Κ	4x - 7
L	7x + 4x
Μ	9-2x
N	$\frac{x}{2}-9$

0	8(x+5)
Р	8(2x+5)
Q	8 <i>x</i> +5
R	2(5x+8)
S	5 <i>x</i> +8
Т	5(x+8)
U	$\frac{5}{8}x+2$

V	x+15
W	<i>x</i> +9
Х	4x - 9
Y	2x - 9
Ζ	2 <i>x</i> +9
AA	x-15
BB	$\frac{3}{4}x-9$

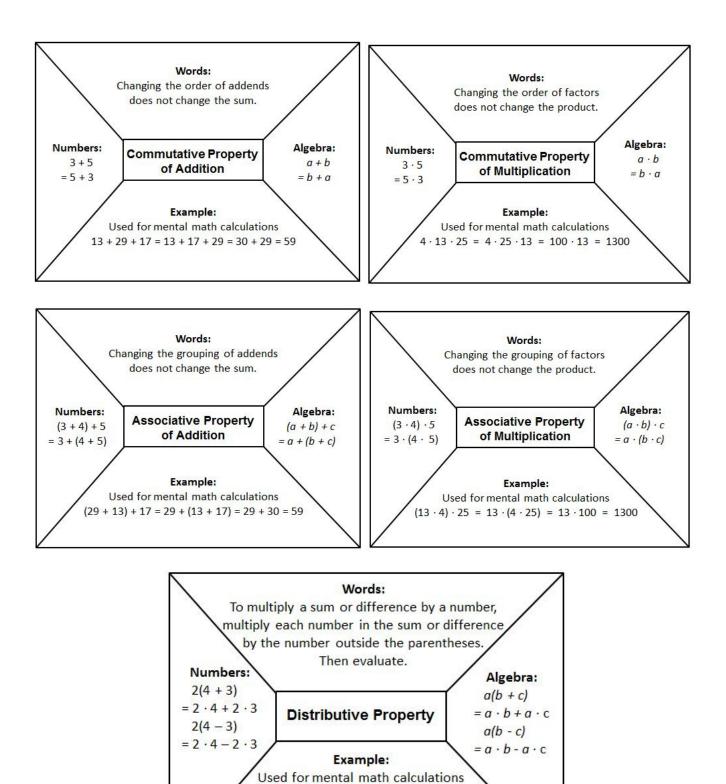
Γ

1.	Product of 7 and <i>x</i>			
2.	7 less than 3 times x			
3.	Product of 3 and the sum of 7 and <i>x</i>			
4.	7 less than the quotient of 3 and x			
5.	Sum of 7 and three times x			
6.	3 more than twice <i>x</i>			
7.	Twice the sum of 7 and x			
8.	7 subtracted from <i>x</i>			
9.	2 more than <i>x</i> tripled			
10.	7 more than <i>x</i> doubled			
11.	x less than 7			
12.	Twice <i>x</i> minus 7			
13.	2 plus the product of <i>x</i> and 7			
14.	3 less than x squared			
15.	Difference of 7 times <i>x</i> and 3			
16.	x squared subtracted from 3			
17.	The square of the sum of <i>x</i> and 3			
18.	3 more than <i>x</i> squared			
19.	3 plus the quotient of <i>x</i> and 7			
20.	Product of 3, 7 and <i>x</i>			

Translate each phrase below into an algebraic expression. Write the correct letter next to each expression.

А	2+7 <i>x</i>				
В	3x + 7				
С	7 <i>x</i> -3				
D	x-7				
Е	$3 \bullet 7 \bullet x$				
F	7 <i>x</i>				
G	$x^2 + 3$				
Н	$(x+3)^2$				
Ι	$\frac{3}{x}-7$				
J	2(7+x)				
K	$3 - x^2$				
L	7-x				
Μ	3x - 7				
Ν	2 <i>x</i> +7				
0	$3 \bullet (7+x)$				
Р	$3 + \frac{x}{7}$				
Q	2x+3				
R	$x^2 - 3$				
S	3x+2				
Т	2 <i>x</i> -7				

1



 $12 \cdot 52 = 12(50 + 2)$

= 12(50) + 12(2) = 600 + 24 = 624

А	Commutative Property of Addition	The order in which numbers are added does not change the sum.	5 + 3 = 3 + 5
В	Commutative Property of Multiplication	The order in which numbers are multiplied does not change the product.	$2 \bullet 4 = 4 \bullet 2$
С	Associative Property of Addition	The way in which addends are grouped does not change the sum.	(2+4) + 6 = 2 + (4+6)
D	Associative Property of Multiplication	The way in which factors are grouped does not change the product.	$(3\bullet 5)\bullet 7 = 3\bullet(5\bullet 7)$
Е	Identity Property of Addition	The sum of an addend and zero is the addend.	7 + 0 = 7
F	Identity Property of Multiplication	The product of a factor and one is the factor.	9•1=9
G	Multiplicative Property of Zero	The product of a factor and zero is zero.	$5 \bullet 0 = 0$
Н	Distributive Property	The sum of two addends multiplied by a number is the sum of the product of each addend and the number.	$4 \bullet (7+2) = 4 \bullet 7 + 4 \bullet 2$

Name the property shown by each statement. You may write the letter listed for your answer.

1.	4 + (9 + 6) = (4 + 9) + 6	2.		x + 12 = 12 + x	
3.	(3+y)+0=3+y	4.		(x+y)+z = x+(y+z)	
5.	(15+x) + 2 = 2 + (15+x)	6.		$x \bullet 1 = x$	
7.	14xy = 14yx	8.		(3+5) + c = 3 + (5+c)	
9.	$(2\bullet 5)\bullet 0=0$	10).	$6 \bullet (8+c) = (8+c) \bullet 6$	
11.	$6 \bullet (4 \bullet 3) = (6 \bullet 4) \bullet 3$	12	2.	$(3 \bullet 9) \bullet 1 = 3 \bullet 9$	
13.	(a+b)+c = c + (a+b)	14		$(x+y)\bullet 5 = (y+x)\bullet 5$	
15.	$(x \bullet y) \bullet z = (y \bullet x) \bullet z$	16	5.	$(7+3) \bullet 5 = (3+7) \bullet 5$	

Use the distributive property to rewrite each of the following.

17.	8(50+4)	18.	5•(20+9)	
19.	7(40-2)	20.	$4 \bullet 400 - 4 \bullet 2$	
21.	800 • 200 + 800 • 10	22.	89•10+89•2	
23.	$2 \bullet 60 + 2 \bullet 4$	24.	501•11	

