# CALCULUS

#### **THIRD EDITION**

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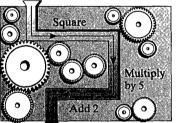
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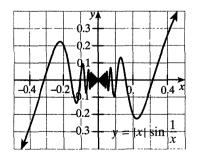




Output value  $5x^2 + 2$ 

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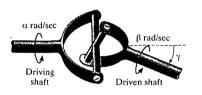
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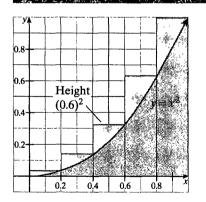
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 $r = f(\theta) / \theta = \beta$ 

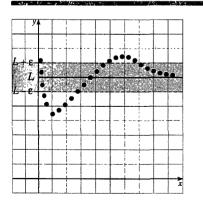
 $\theta = \theta_i$ 

 $\theta = \theta_k$ 

 $\theta = \alpha$ 

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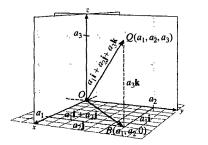
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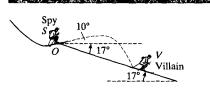
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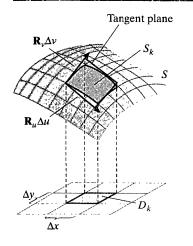
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