Calibration

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Synopsis

- Why do we have to calibrate?
- Idealistic formalism → Realistic practice
- Fundamental Calibration Principles
 - Practical Calibration Considerations
 - Baseline-based vs. Antenna-based Calibration
 - Solving
- Scalar Calibration Example
- Generalizations
 - Full Polarization
 - A Dictionary of Calibration Effects
 - Calibration Heuristics and 'Bootstrapping'
- New Calibration Challenges
- Summary







References

- Synthesis Imaging in Radio Astronomy II (Editors: Taylor, Carilli, & Perley)
- Interferometry and Synthesis in Radio Astronomy (2nd ed.Thompson, Moran, & Swenson)
- Tools of Radio Astronomy (6th ed., Wilson, Rohlfs, & Huettemeister)







Why Calibration?

- Synthesis radio telescopes, though well-designed, are not perfect (e.g., surface accuracy, receiver noise, polarization purity, gain stability, geometric model errors, etc.)
- Need to accommodate deliberate engineering (e.g., frequency downconversion, analog/digital electronics, filter bandpass, etc.)
- Hardware or control software occasionally fails or behaves unpredictably
- Scheduling/observation errors sometimes occur (e.g., wrong source positions)
- Atmospheric conditions not ideal
- Radio Frequency Interference (RFI)

Determining instrumental and environmental properties (calibration) is a prerequisite to determining radio source properties







From Idealistic to Realistic

 Formally, we wish to use our interferometer to obtain the visibility function:

$$V(u,v) = \int_{skv} I(l,m)e^{-i2\pi(ul+vm)}dldm$$

•a Fourier transform which we intend to invert to obtain an image of the sky:

$$I(l,m) = \int_{uv} V(u,v)e^{i2\pi(ul+vm)}dudv$$

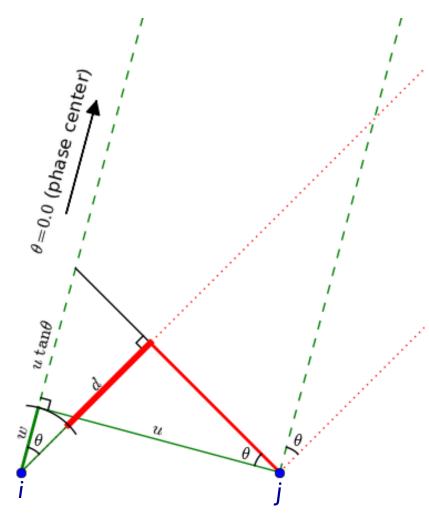
- V(u,v) describes the amplitude and phase of 2D sinusoids that add up to an image of the sky
 - Amplitude: "~how concentrated?"
 - Phase: "~where?"
 - c.f. Young's Double-Slit Interference Experiment (1804)
- How do we measure *V(u,v)?*







How do we measure V(u,v)?



 Consider direction-dependent arrival geometry for E-field disturbance reception at two points, i and j, relative to the phase center direction

$$d = (w_{\lambda} + u_{\lambda} \tan \theta) \cos \theta - w_{\lambda}$$

$$= u_{\lambda} \sin \theta + w_{\lambda} (\cos \theta - 1)$$

$$d(l) = u_{\lambda} l + w_{\lambda} (\sqrt{1 - l^{2}} - 1) \quad (1D)$$

$$(\sin \theta = l; \cos \theta = \sqrt{1 - l^{2}})$$

$$d(l,m) = u_{\lambda}l + v_{\lambda}m + w_{\lambda}\left(\sqrt{1 - l^2 - m^2} - 1\right)$$
 (2D)

$$\approx u_{\lambda}l + v_{\lambda}m \qquad (l,m << 1)$$









How do we measure V(u,v)?

- Correlate the E-field disturbances, $x_i \& x_j$ arriving at spatially separate sensors
 - delay-aligned for the phase-center
 - s_i & s_j are the direction-dependent Efield disturbances
- Direction integral and product can be reversed, because the E-field disturbances from different directions don't correlate
- s_i and s_j (for a specific direction) differ only by a phase factor given by the arrival geometry
- $<|s_i|^2>$ is proportional to the brightness distribution, I(l,m)

$$V_{ij}^{obs} = \left\langle x_i \cdot x_j^* \right\rangle_{\Delta t}$$

$$= \left\langle \int_{sky} s_i \, dl_i \, dm_i \cdot \int_{sky} s_j^* \, dl_j \, dm_j \right\rangle_{\Delta t}$$

$$= \left\langle \int_{sky} s_i s_j^* \, dl \, dm \right\rangle_{\Delta t}$$

$$= \int_{sky} \left\langle \left| s_i \right|^2 \right\rangle e^{-i2\pi d(l,m)} \, dl \, dm$$

$$= \int_{sky} I(l,m) e^{-i2\pi d(l,m)} \, dl \, dm$$

$$= \int_{sky} I(l,m) e^{-i2\pi (ul+vm)} \, dl \, dm$$

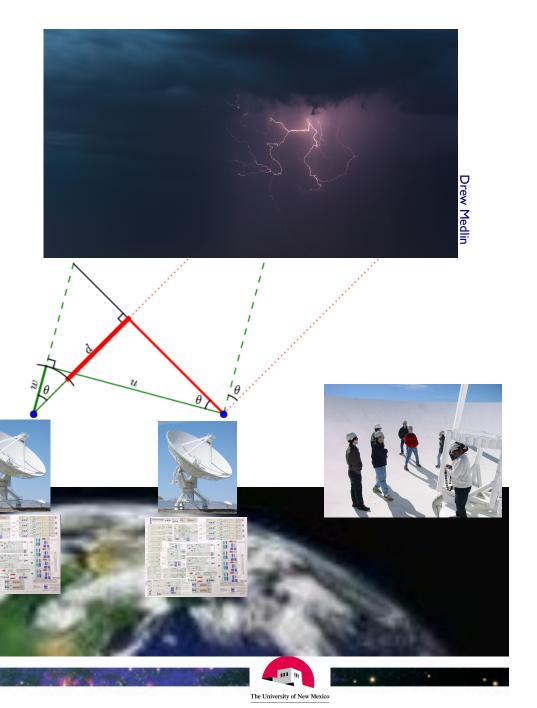






But in reality...

- Weather
- Realistic Antennas
- Electronics...
- Digital correlation
- ...and the whole is moving!



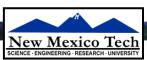
Realistic Visibility

So, in practice, we obtain an imperfect visibility measurement:

$$V_{ij}^{obs}(u,v) = \left\langle x_i(t) \cdot x_j^*(t) \right\rangle_{\Delta t}$$
$$= J_{ij} V_{ij}^{true}(u,v)$$

- $-x_i & x_i$ are mutually delay-compensated for the phase center
- Averaging duration is set by the expected timescales for variation of the correlation result (~seconds)
- J_{ij} is a generalized operator characterizing the net effect of the observing process for antennas i and j on baseline ij, which we must calibrate
 - Includes any required scaling to physical units
- Sometimes J_{ij} corrupts the measurement irrevocably, resulting in data that must be edited or "flagged"







Realistic Visibility: Noise

- Normalized visibility: $\sigma_{ij} = \frac{1}{\sqrt{2\Delta v \Delta t}}$
 - Extra 2 (cf single-dish) comes from formation from separate telescopes
- Absolute visibility: $\sigma_{ij} = \frac{\sqrt{T_i T_j}}{\sqrt{2 \Lambda v \Lambda t}}$
 - T_i , T_j are the system temperatures (total sampled powers), in whatever units the corresponding data are in
 - (The numerator, as measured by the correlator, is the factor by which visibilities are typically normalized, e.g. ALMA)
- Formal Visibility Weights:

$$w_{ij} = \frac{1}{\sigma_{ij}^2}$$







Practical Calibration Considerations

- A priori "calibrations" (provided by the observatory)
 - Antenna positions, earth orientation and rate, clock(s), frequency reference
 - Antenna pointing/focus, voltage pattern, gain curve
 - Calibrator coordinates, flux densities, polarization properties
- Absolute engineering calibration (dBm, K, volts)?
 - Amplitude: episodic (ALMA) or continuous (EVLA/VLBA) T_{sys} or switched-power monitoring to enable calibration to nominal K (or Jy, with antenna efficiency information)
 - Phase: WVR (ALMA), otherwise practically impossible (relative antenna phase)
 - Traditionally, we concentrate instead on ensuring instrumental stability on adequate timescales
- Cross-calibration a better choice
 - Observe strong astronomical sources near science target against which calibration (J_{ii}) can be solved, and transfer solutions to target observations
 - Choose appropriate calibrators; usually **point sources** because we can easily predict their visibilities (Amp ~ constant, phase ~ 0)
 - Choose appropriate timescales for calibration





"Absolute" Astronomical Calibrations

- Flux Density Calibration
 - Radio astronomy flux density scale set according to several "constant" radio sources, and planets/moons
 - Use resolved models where appropriate
- Astrometry
 - Most calibrators come from astrometric catalogs; sky coordinate accuracy of target images tied to that of the calibrators
 - Beware of resolved and evolving structures, and phase transfer biases due to troposphere (especially for VLBI)
- Polarization
 - Usual flux density calibrators also have significant stable linear polarization position angle for registration
 - Calibrator circular polarization usually assumed zero (?)
- Relative calibration solutions (and dynamic range) insensitive to errors
 in these "scaling" parameters





Baseline-based Cross-Calibration

$$V_{ij}^{obs} = J_{ij} V_{ij}^{mod}$$

- Simplest, most-obvious calibration approach: measure complex response
 of each baseline on a standard source, and scale science target visibilities
 accordingly
 - "Baseline-based" Calibration:

- $J_{ij} = \left\langle V_{ij}^{obs} / V_{ij}^{mod} \right\rangle_{\Delta t}$
- Only option for single baseline "arrays"
- Calibration precision same as calibrator visibility sensitivity (on timescale of calibration solution). Improves only with calibrator strength.
- Calibration accuracy sensitive to departures of calibrator from assumed structure
 - Un-modeled calibrator structure transferred (in inverse) to science target!



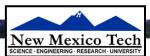




Antenna-based Cross Calibration

• Measured visibilities are formed from a product of antenna-based signals. Can we take advantage of this fact?







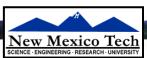
Antenna-based Cross Calibration

• The net time-dependent E-field signal sampled by antenna i, $x_i(t)$, is a combination of the desired signal, $s_i(t,l,m)$, corrupted by a factor $J_i(t,l,m)$ and integrated over the sky (l,m), and diluted by noise, $n_i(t)$:

$$x_{i}(t) = \int_{sky} J_{i}(t, l, m) s_{i}(t, l, m) dl dm + n_{i}(t)$$
$$= s'_{i}(t) + n_{i}(t)$$

- $x_i(t)$ is sampled (complex) voltage provided to the correlator input
- $J_i(t,l,m)$ is the product of a series of effects encountered by the incoming signal
- $J_i(t,l,m)$ is an antenna-based complex number
- Usually, $|n_i|^2 >> |s_i'|^2$ (i.e., noise dominates)







Correlation of Realistic Signals - I

- The correlation of two realistic (aligned for a from different antennas:
- Noise correlations have zero mean—even if $|n_i|^2 >> |s_i|^2$, the correlation process isolates desired signals:
- Same analysis as before, except we carry \int_{i} , \int_{i} terms

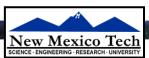
realistic (aligned for a specific direction) signals
$$\langle x_i \cdot x_j^* \rangle_{\Delta t} = \langle (s_i' + n_i) \cdot (s_j' + n_j)^* \rangle_{\Delta t}$$
 from different antennas:
$$= \langle s_i' \cdot s_j'^* \rangle_{\Delta t} + \langle s_i' \cdot n_j^* \rangle_{\Delta t} + \langle n_i \cdot s_j'^* \rangle_{\Delta t} + \langle n_i \cdot n_j^* \rangle_{\Delta t}$$
 zero mean—even if
$$= \langle s_i' \cdot s_j'^* \rangle_{\Delta t}$$
 $= \langle s_i' \cdot s_j'^* \rangle_{\Delta t}$

$$= \left\langle \int_{sky} J_{i} s_{i} dl_{i} dm_{i} \cdot \int_{sky} J_{j}^{*} s_{j}^{*} dl_{j} dm_{j} \right\rangle_{\Delta t}$$

$$= \left\langle \int_{sky} J_{i} J_{j}^{*} s_{i} s_{j}^{*} dl dm \right\rangle_{\Delta t}$$

$$= \int_{sky} J_{i} J_{j}^{*} I(l, m) e^{-i2\pi(ul+vm)} dl dm$$







The Scalar Measurement Equation

$$V_{ij}^{obs} = \int_{sky} J_i J_j^* I(l,m) e^{-i2\pi \left(u_{ij}l + v_{ij}m\right)} dl dm$$

First, isolate non-direction-dependent effects, and factor them from the integral:

$$= \left(J_i^{vis} J_j^{vis*}\right) \int_{sky} \left(J_i^{sky} J_j^{sky*}\right) I(l,m) e^{-i2\pi \left(u_{ij}l + v_{ij}m\right)} dl dm$$

• Next, we recognize that over small fields of view, it is possible to assume $\int_{0.5}^{1.5} J^{sky} = 1.0$, and we have a relationship between ideal and observed Visibilities:

$$= J_i J_j^* \int_{sky} I(l,m) e^{-i2\pi \left(u_{ij}l + v_{ij}m\right)} dl dm$$

$$V_{ij}^{obs} = J_i J_j^* V_{ij}^{true}$$

- Standard calibration of most existing arrays reduces to solving this last equation for the J_{ij} assuming a visibility model V_{ii}^{mod} for a calibrator
- NB: visibilities corrupted by difference of antenna-based phases, and product of
 antenna-based amplitudes





Aside: Auto-correlations and Single Dishes

• The auto-correlation of a signal from a single antenna:

$$\langle x_i \cdot x_i^* \rangle_{\Delta t} = \langle (s_i' + n_i) \cdot (s_i' + n_i)^* \rangle_{\Delta t}$$

$$= \langle s_i' \cdot s_i'^* \rangle + \langle n_i \cdot n_i^* \rangle$$

$$= \langle \int_{sky} |J_i|^2 |s_i|^2 dl dm \rangle_{\Delta t} + \langle |n_i|^2 \rangle$$

$$= \int_{sky} |J_i|^2 I(l, m) dl dm + \langle |n_i|^2 \rangle$$

- This is an integrated (sky) power measurement plus non-zero-mean noise, i.e., the $T_{\rm sys}$
- Desired signal not simply isolated from noise
- Noise usually dominates
- Single dish radio astronomy calibration strategies rely on switching
 (differencing) schemes to isolate desired signal from the noise





Solving for the J_i

• We can write: $V_{ij}^{obs} - J_i J_j^* V_{ij}^{mod} = 0$

• ...and define chi-squared:
$$\chi^2 = \sum_{\substack{i,j\\i\neq j}} \left| V_{ij}^{obs} - J_i J_j^* V_{ij}^{mod} \right|^2 w_{ij} \qquad \left(w_{ij} = \frac{1}{\sigma_{ij}^2} \right)$$

• ...and minimize chi-squared w.r.t. each \int_i^* , yielding (iteration):

$$J_{i} = \sum_{\substack{j \\ i \neq j}} \left(V_{ij}^{obs} J_{j} V_{ij}^{mod*} w_{ij} \right) / \sum_{\substack{j \\ i \neq j}} \left(\left| J_{j} \right|^{2} \left| V_{ij}^{mod} \right|^{2} w_{ij} \right) \qquad \left(\frac{\partial \chi^{2}}{\partial J_{i}^{*}} = 0 \right)$$

• (...which we may be gratified to recognize as a peculiarly weighted average of the *implicit* J_i contribution to V^{obs} :)







Solving for J_i (cont)

Formal errors:

$$\sigma_{J_{i}} = \sqrt{\frac{1}{\sum_{j \neq i} \left|V_{ij}^{mod}\right|^{2} \left|J_{j}\right|^{2} / \sigma_{ij,\Delta t}^{2}}}$$

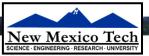
• For a ~uniform array (~same sensitivity on all baselines, ~same calibration magnitude on all antennas) and point-like calibrator:

$$\sigma_{J_i} \approx \frac{\sigma_{ij,\Delta t}}{\left|V^{mod}\right| \sqrt{\left\langle \left|J_j\right|^2 \right\rangle \left(N_{ant} - 1\right)}}$$

- Calibration error decreases with increasing calibrator strength and square-root of N_{ant} (c.f. baseline-based calibration).
- Other properties of the antenna-based solution:
 - Minimal degrees of freedom (N_{ant} factors, $N_{ant}(N_{ant}-I)/2$ measurements)
 - Net calibration for a baseline involves a phase difference, so absolute directional information is lost



- Closure...



Antenna-based Calibration and Closure

- Success of synthesis telescopes relies on antenna-based calibration
 - Fundamentally, any information that can be factored into antenna-based terms,
 could be antenna-based effects, and not source visibility
 - For $N_{ant} > 3$, source visibility information cannot be *entirely* obliterated by any antenna-based calibration
- Observables independent of antenna-based calibration:
 - Closure phase (3 baselines):

$$\phi_{ij}^{obs} + \phi_{jk}^{obs} + \phi_{ki}^{obs} = (\phi_{ij}^{true} + \theta_i - \theta_j) + (\phi_{jk}^{true} + \theta_j - \theta_k) + (\phi_{ki}^{true} + \theta_k - \theta_i)$$

$$= \phi_{ij}^{true} + \phi_{jk}^{true} + \phi_{ki}^{true}$$

Closure amplitude (4 baselines):

$$\left| \frac{V_{ij}^{obs} V_{kl}^{obs}}{V_{ik}^{obs} V_{jl}^{obs}} \right| = \left| \frac{J_i J_j V_{ij}^{true} J_k J_l V_{kl}^{true}}{J_i J_k V_{ik}^{true} J_j J_l V_{jl}^{true}} \right| = \left| \frac{V_{ij}^{true} V_{kl}^{true}}{V_{ik}^{true} V_{jl}^{true}} \right|$$

Baseline-based calibration formally violates closure!





Reference Antenna

- Since the "antenna-based" phase solution is derived from antenna phase differences, we do not measure phase absolutely
 - relative astrometry
- Phase solutions typically referred to a specific antenna, the refant, which is assumed to have constant phase (zero, in both polarizations)
 - refant typically near array center
 - The refant's phase variation distributed to all other antennas' solutions
 - For adequate time sampling, ensures reliable interpolation of phase, without ambiguity (c.f. arbitrary phase offsets between solutions)
 - Asserts stable cross-hand phase frame (which must be calibrated)
- Problems:
 - A single good refant not always available over whole observation, due to flagging, etc.
 - Cross-hand phase at refant may not, in fact, be stable...







Corrected Visibility

Visibility...

$$V_{ij}^{obs} = J_i J_j^* V_{ij}^{true} \quad \Rightarrow \quad V_{ij}^{cor} = J_i^{-1} J_j^{*-1} V_{ij}^{obs}$$

• ...and weights!

$$w_{ij}^{cor} = w_{ij}^{obs} \left| J_i \right|^2 \left| J_j \right|^2 = \frac{\left| J_i \right|^2 \left| J_j \right|^2}{\sigma_{ij}^2}$$

- (calibrate the sigmas)



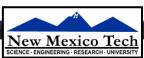




What Is Delivered by a Synthesis Array?

- An enormous list of complex visibilities! (Enormous!)
 - At each timestamp ($\sim 1-10$ s intervals): N(N-1)/2 baselines
 - EVLA: 35 I baselines
 - VLBA: 45 baselines
 - ALMA: 1225-2016 baselines
 - For each baseline: up to 64 Spectral Windows ("spws", "subbands" or "IFs")
 - For each spectral window: tens to thousands of channels
 - For each channel: I, 2, or 4 complex correlations (polarizations)
 - EVLA or VLBA: RR or LL or (RR,LL), or (RR,RL,LR,LL)
 - ALMA: XX or YY or (XX,YY) or (XX,XY,YX,YY)
 - With each correlation, a weight value and a flag (T/F)
 - Meta-info: Coordinates, antenna, field, frequency label info
- $N_{total} = N_t \times N_{bl} \times N_{spw} \times N_{chan} \times N_{corr}$ visibilities
 - − ~few 10^6 x N_{spw} x N_{chan} x N_{corr} vis/hour \rightarrow 10s to 100s of GB per observation







A Typical Dataset (Polarimetry)

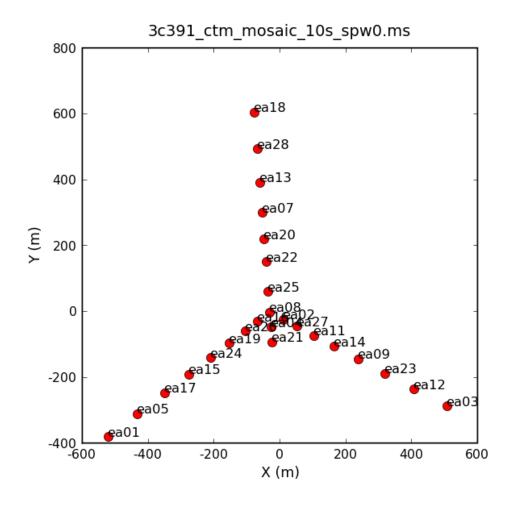
- Array:
 - EVLA D-configuration (Apr 2010)
- Sources:
 - Science Target: 3C391 (7 mosaic pointings)
 - Near-target calibrator: J1822-0938 (~11 deg from target)
 - Flux Density calibrator: 3C286
 - Instrumental Polarization Calibrator: 3c84
- Signals:
 - RR,RL,LR,LL correlations
 - One spectral window centered at 4600 MHz, I28 MHz bandwidth, 64 channels



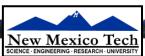




The Array

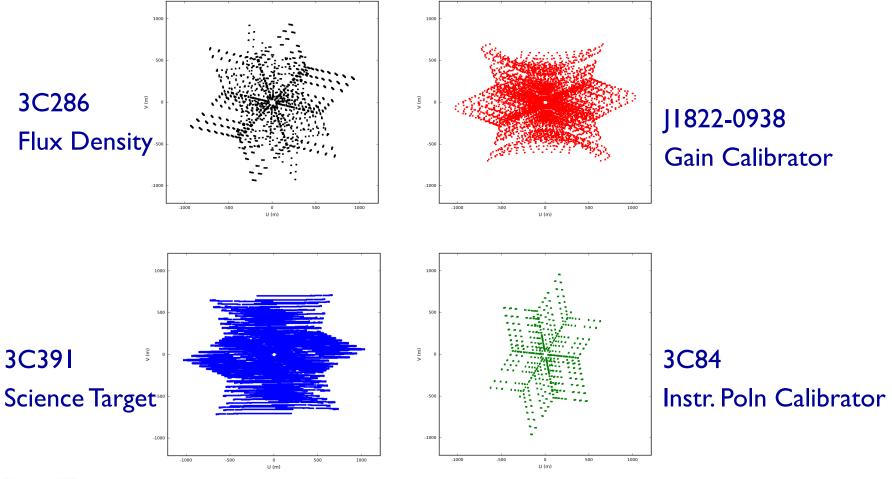








UV-coverages

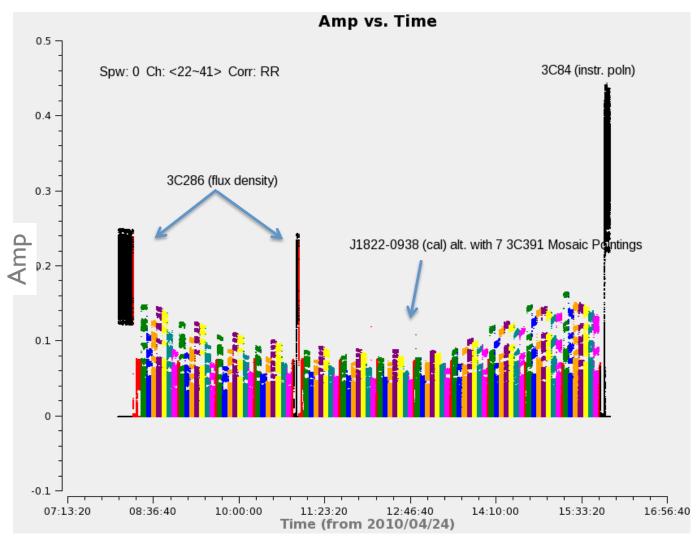








The Visibility Data (source colors)

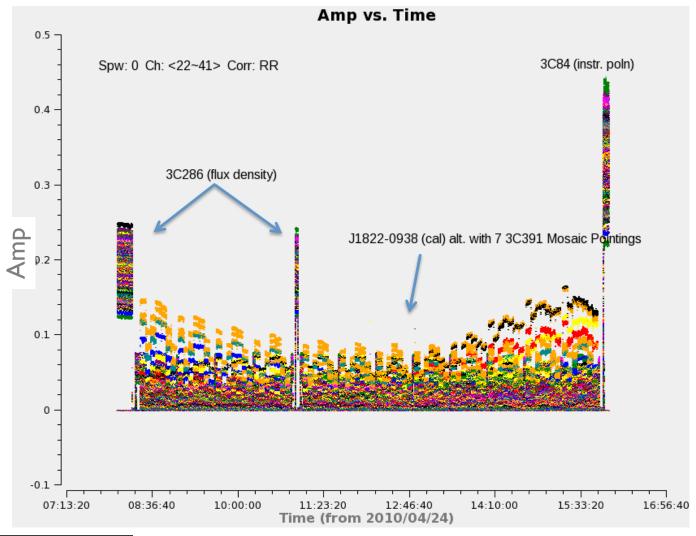




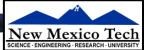




The Visibility Data (baseline colors)

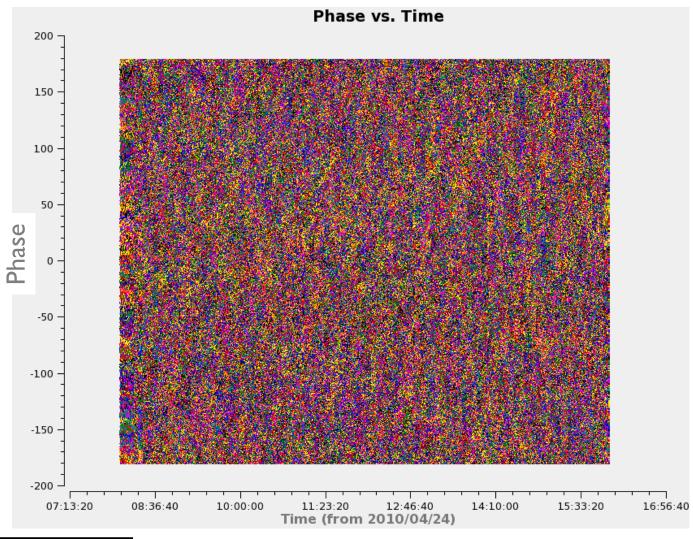




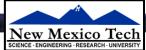




The Visibility Data (baseline colors)

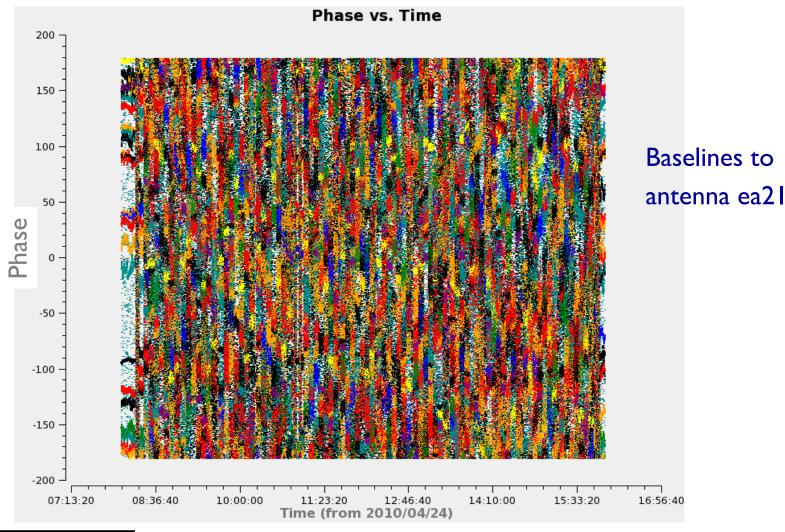








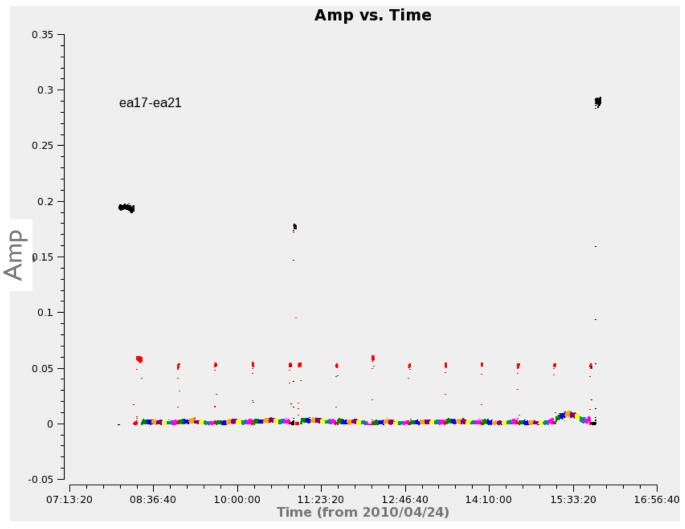
The Visibility Data (baseline colors)







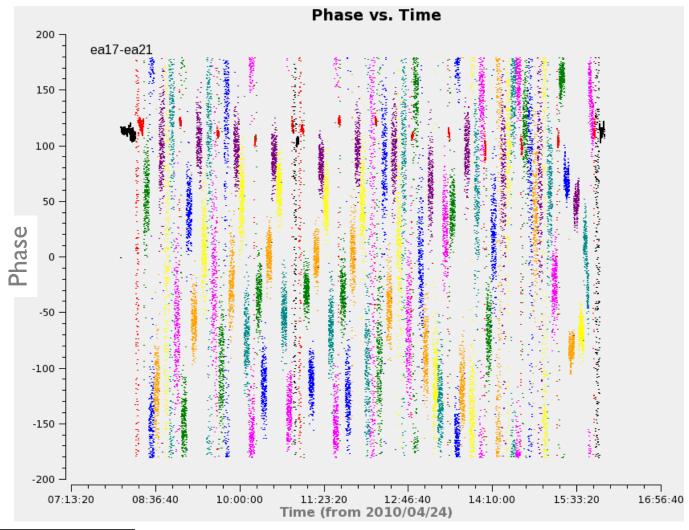
A Single Baseline – Amp (source colors)







A Single Baseline - Phase (source colors)

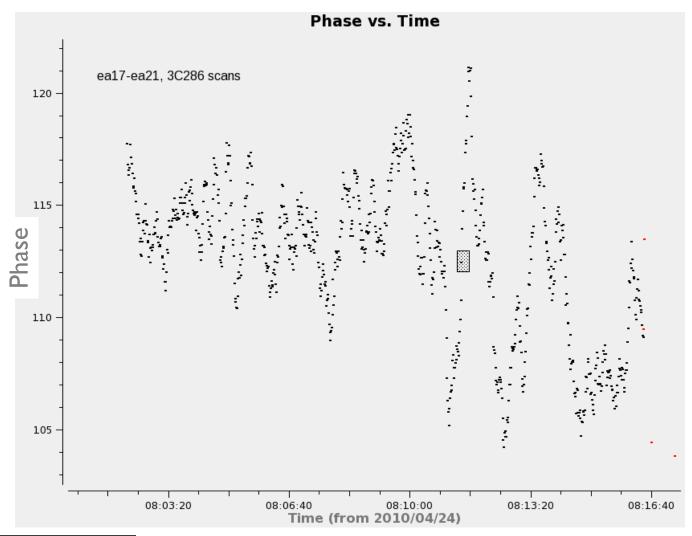








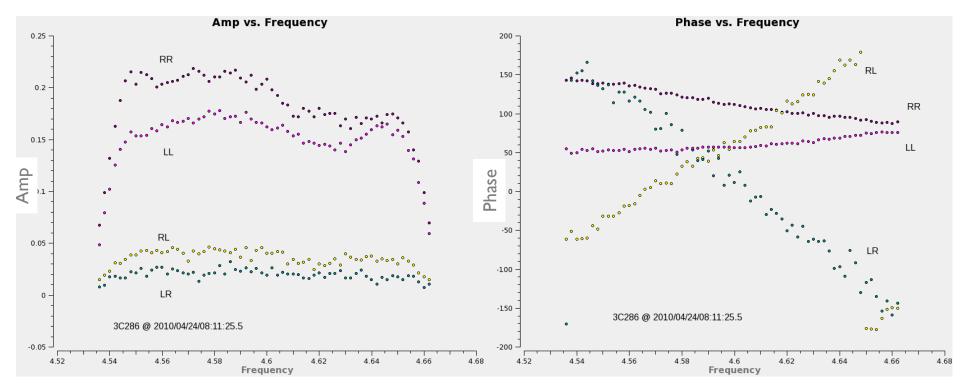
A Single Baseline – 2 scans on 3C286







Single Baseline, Single Integration Visibility Spectra (4 correlations)

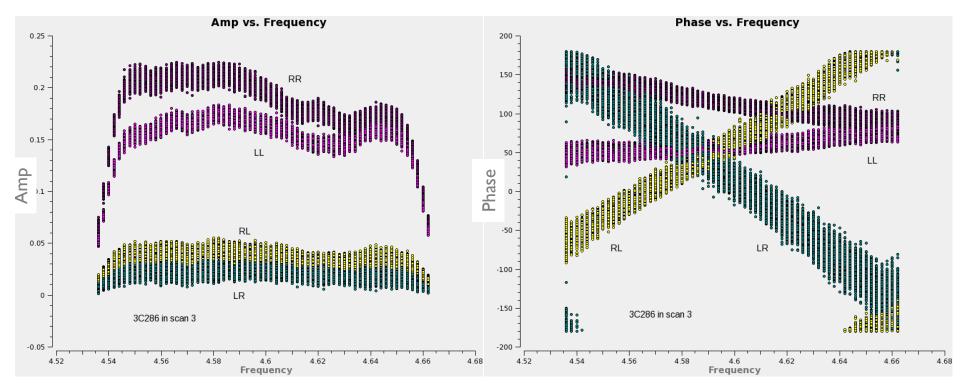


baseline ea 17-ea 21





Single Baseline, Single Scan Visibility Spectra (4 correlations)

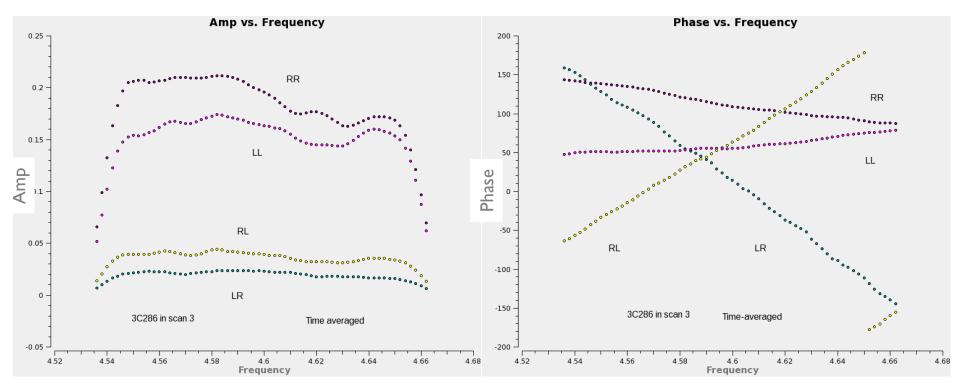


baseline eal7-ea21





Single Baseline, Single Scan (time-averaged) Visibility Spectra (4 correlations)



baseline ea 17-ea 21





Data Examination and Editing

- After observation, initial data examination and editing very important
 - Will observations meet goals for calibration and science requirements?
- What to edit (much of this is now automated):
 - Some real-time flagging occurred during observation (antennas off-source, LO out-of-lock, etc.). Any such bad data left over? (check operator's logs)
 - Any persistently 'dead' antennas (check operator's logs)
 - Periods of especially poor weather? (check operator's log)
 - Any antennas shadowing others? Edit such data.
 - Amplitude and phase should be continuously varying—edit outliers
 - Radio Frequency Interference (RFI)?

Caution:

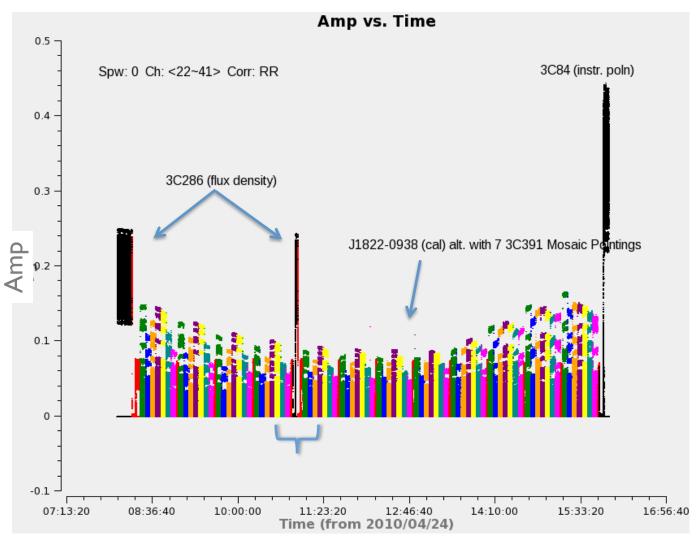
- Be careful editing noise-dominated data.
- Be conservative: those antennas/timeranges which are obviously bad on calibrators are probably (less obviously) bad on weak target sources—edit them
- Distinguish between bad (hopeless) data and poorly-calibrated data. E.g., some antennas may have significantly different amplitude response which may not be fatal—it may only need to be calibrated
- Choose (phase) reference antenna wisely (ever-present, stable response)

Increasing data volumes increasingly demand automated editing algorithms...





Editing Example

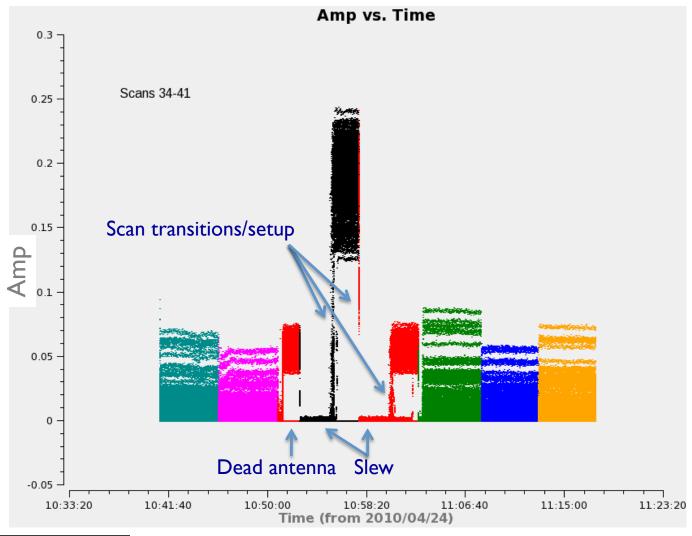




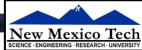




Editing Example

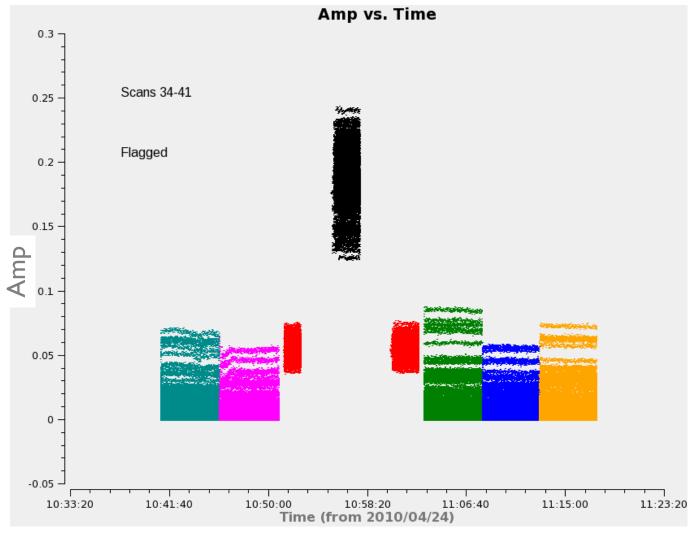








Editing Example

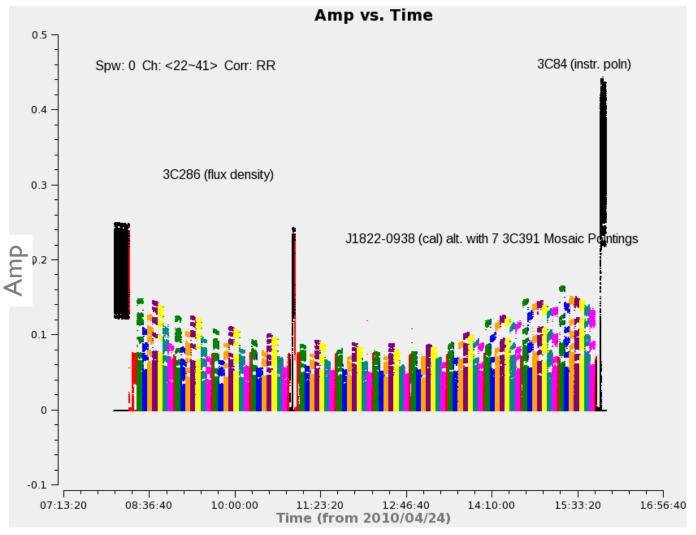








Editing Example (before)

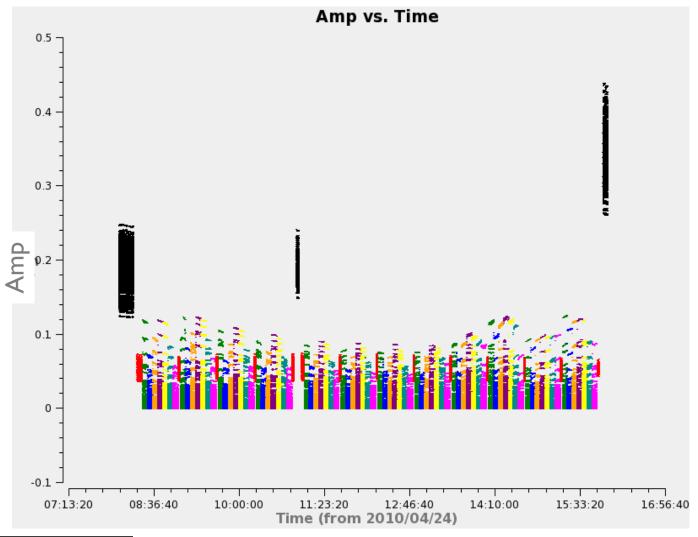




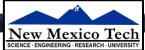




Editing Example (after)





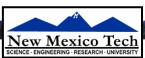




Simple Scalar Calibration Example

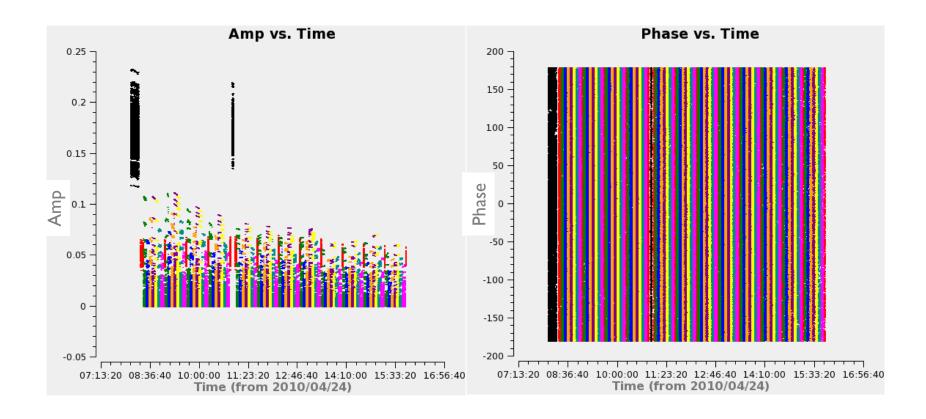
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 - EVLA D-configuration (Apr 2010)
- Sources:
 - Science Target: 3C391 (7 mosaic pointings)
 - Near-target calibrator: J1822-0938 (~II deg from target; unknown flux density, assumed I Jy)
 - Flux Density calibrator: 3C286 (7.747 Jy, essentially unresolved)
- Signals:
 - RR correlation only for this illustration (total intensity only)
 - One spectral window centered at 4600 MHz, I28 MHz bandwidth
 - 64 observed spectral channels averaged with normalized bandpass calibration applied (this illustration considers only the time-dependent 'gain' calibration)
 - (extracted from a continuum polarimetry mosaic observation)



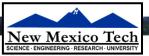




Views of the Uncalibrated Data

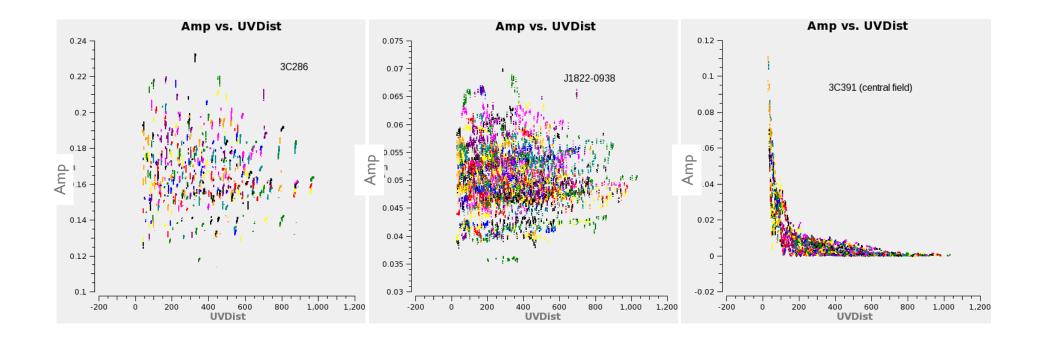




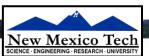




Views of the Uncalibrated Data

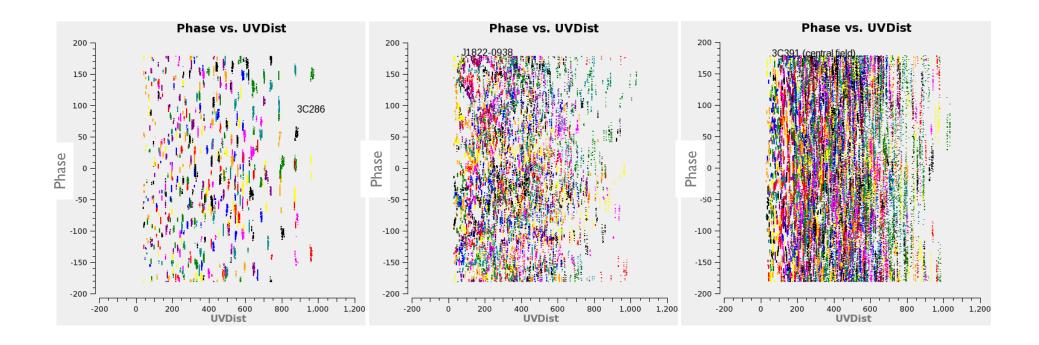








Views of the Uncalibrated Data

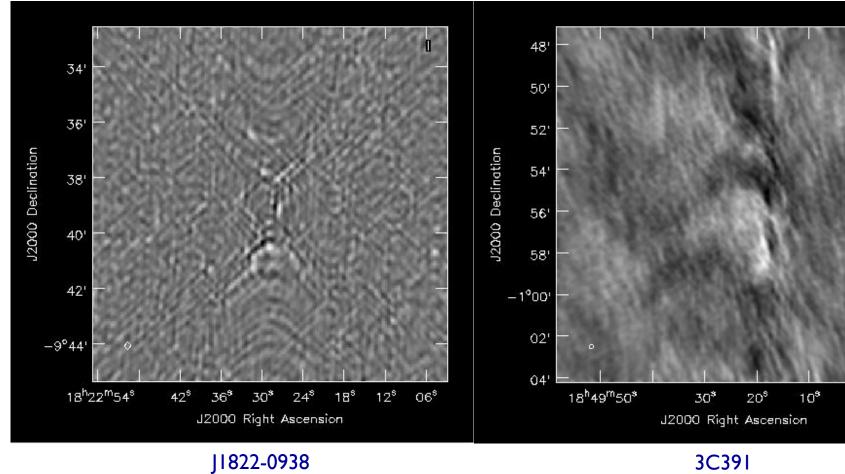








Uncalibrated Images



(calibrator)

3C391 (science)

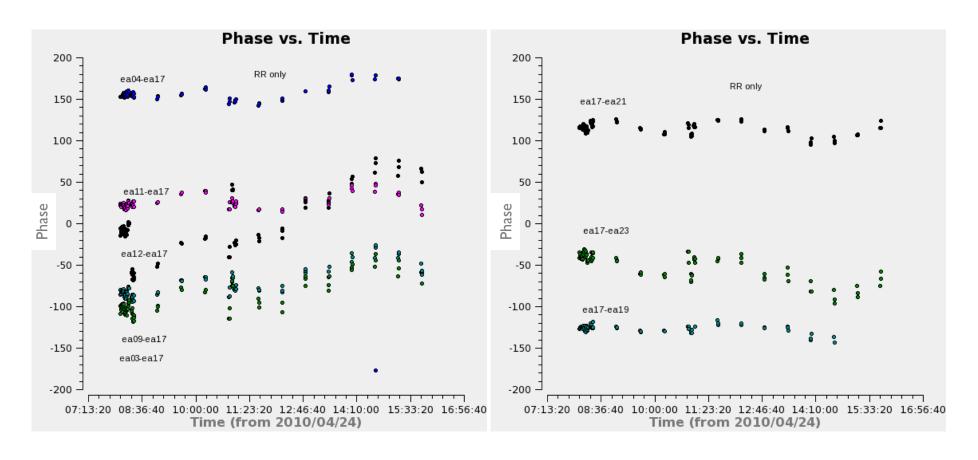
OO^s



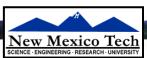




Rationale for Antenna-based Calibration









The Calibration Process

• Solve for antenna-based gain factors for each scan on all calibrators $(V^{mod}=S \text{ for f.d. calibrator}; V^{mod}=I.0 \text{ for others})$:

$$V_{ij}^{obs} = G_i G_j^* V_{ij}^{mod}$$

 Bootstrap flux density scale by enforcing gain consistency over all calibrators:

$$\langle G_i/G_i(fd\ cal)\rangle_{time,antennas} = 1.0$$

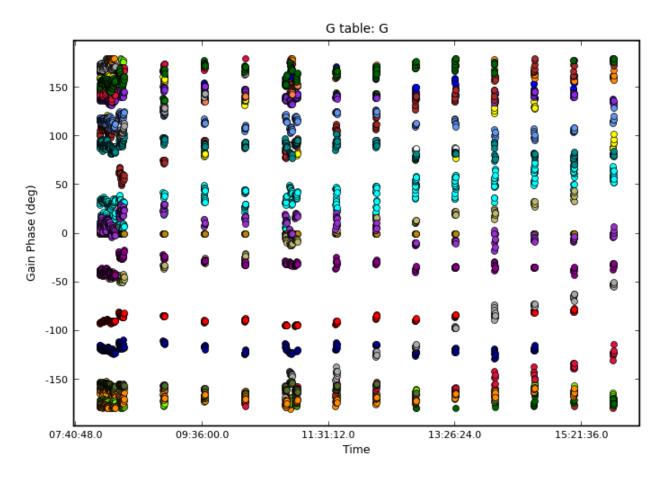
• Correct data (interpolate, as needed):

$$V_{ij}^{cor} = G_i^{-1} G_j^{*-1} V_{ij}^{obs}$$



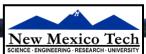


The Antenna-based Calibration Solution



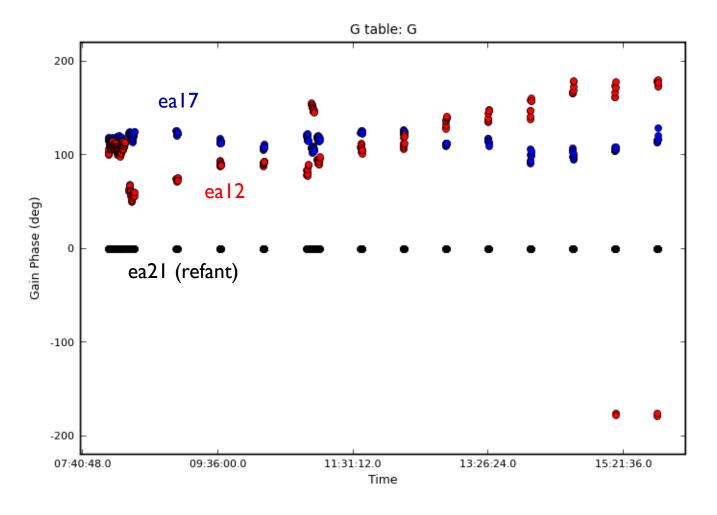
Reference antenna: ea21 (phase = 0)







The Antenna-based Calibration Solution

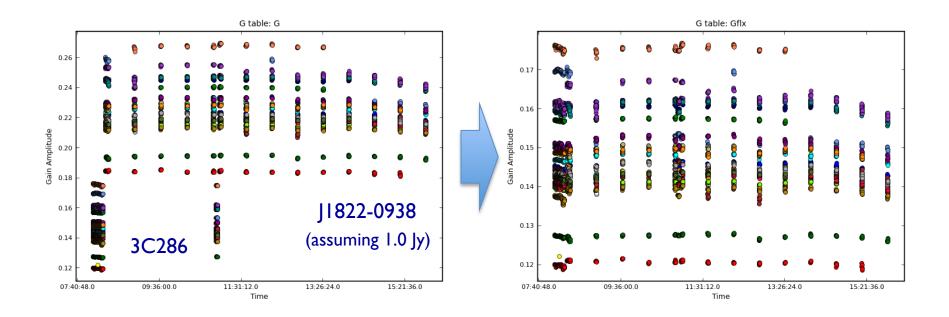








The Antenna-based Calibration Solution



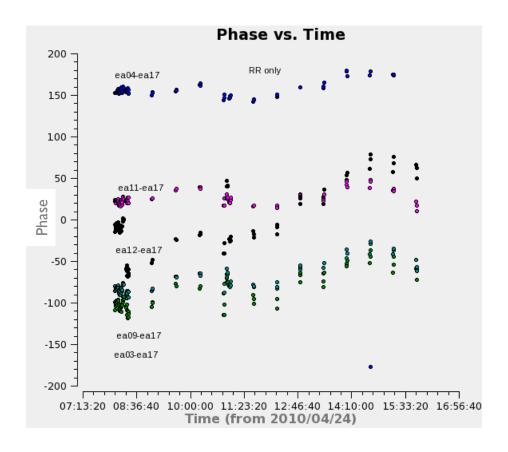
- 3C286's gains have correct scale
- Thus, J1822-0938 is 2.32 Jy (not 1.0 Jy, as assumed)



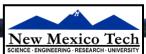




Effect of Antenna-based Calibration: Phase (before)

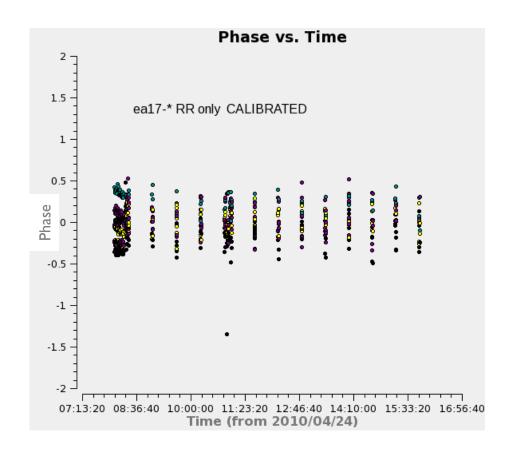




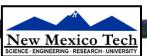




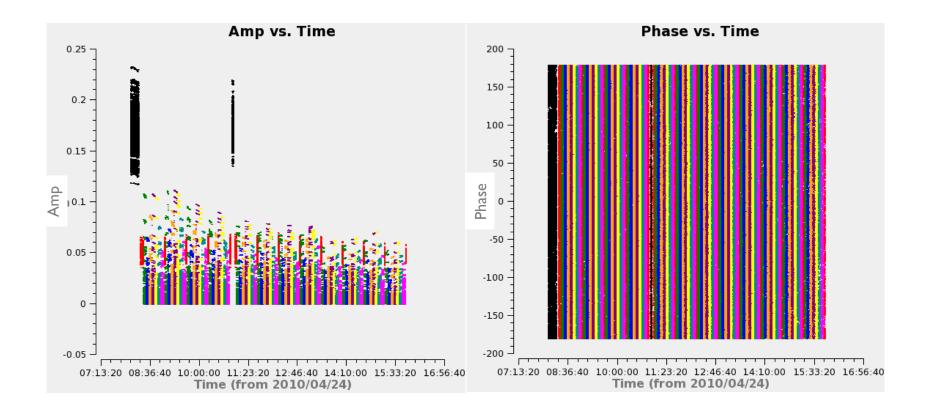
Effect of Antenna-based Calibration Phase (after)



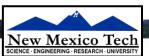




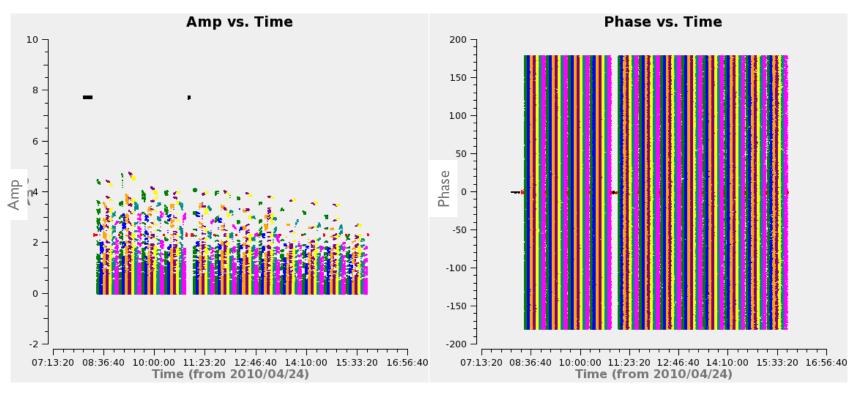










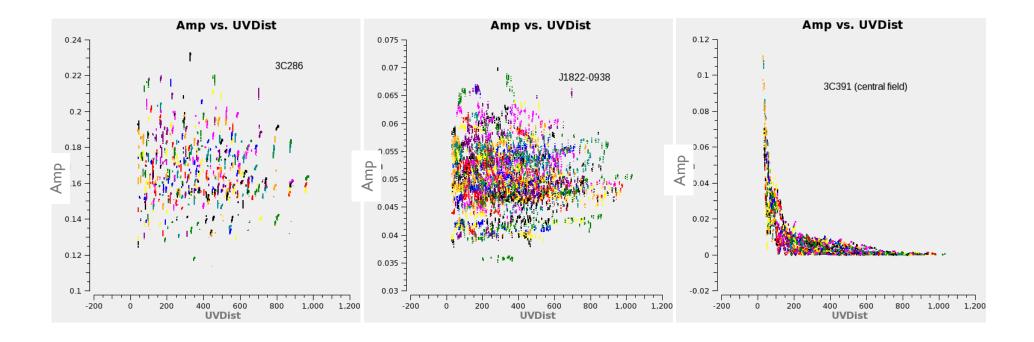


CALIBRATED





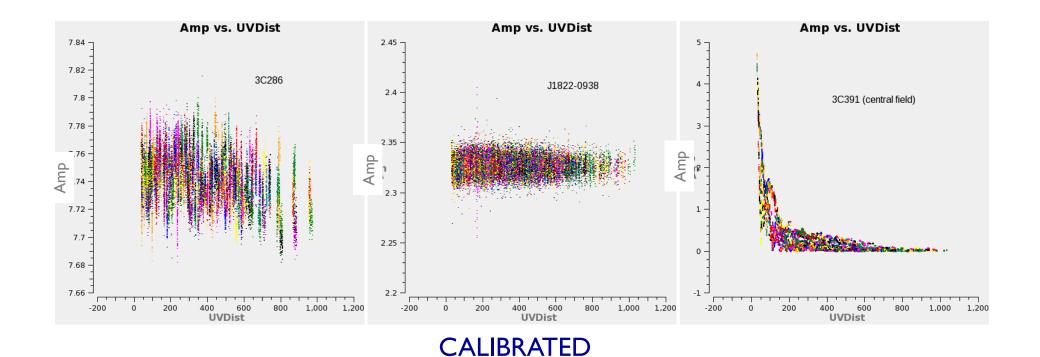




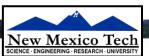




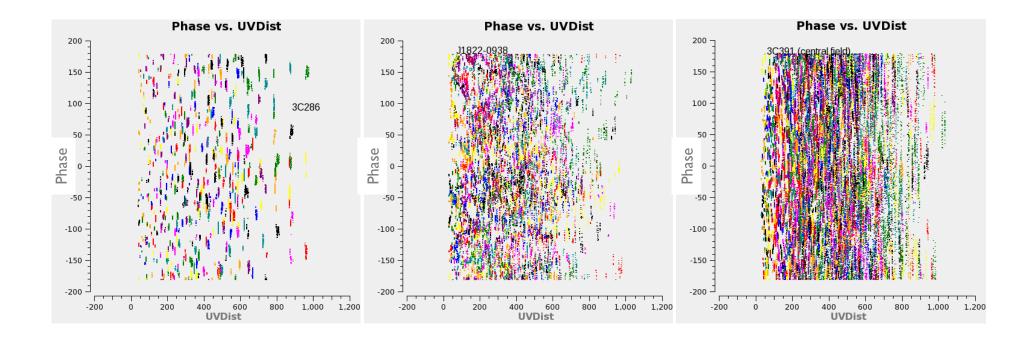




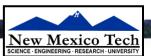




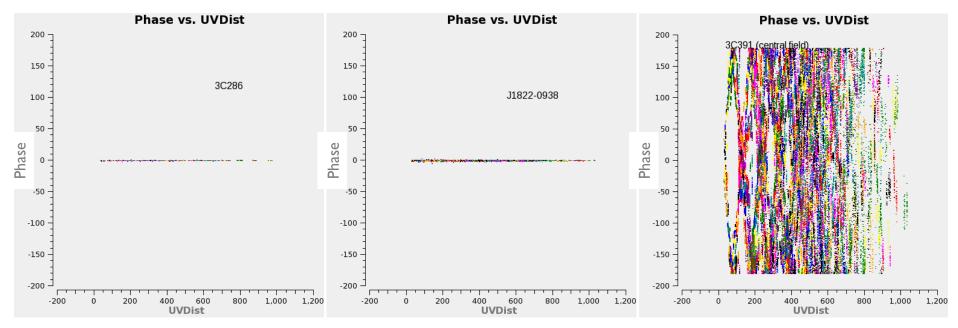










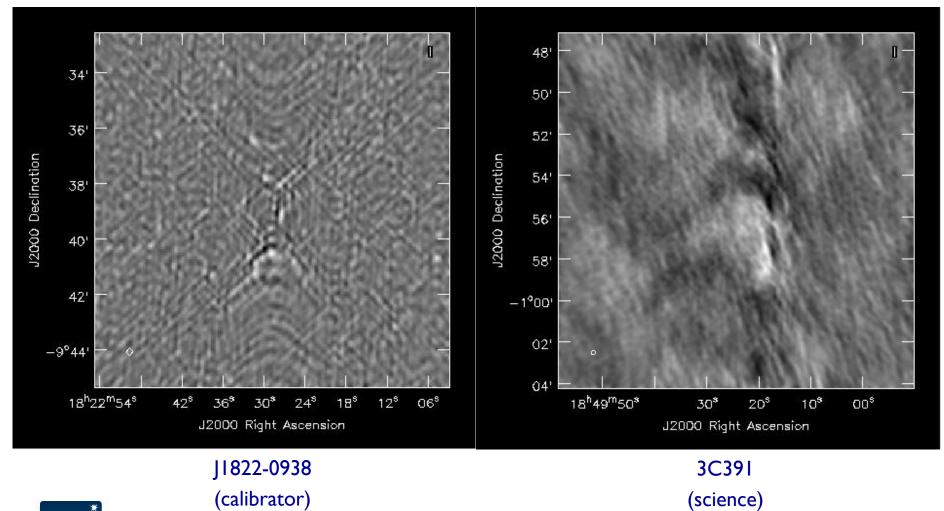




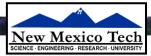




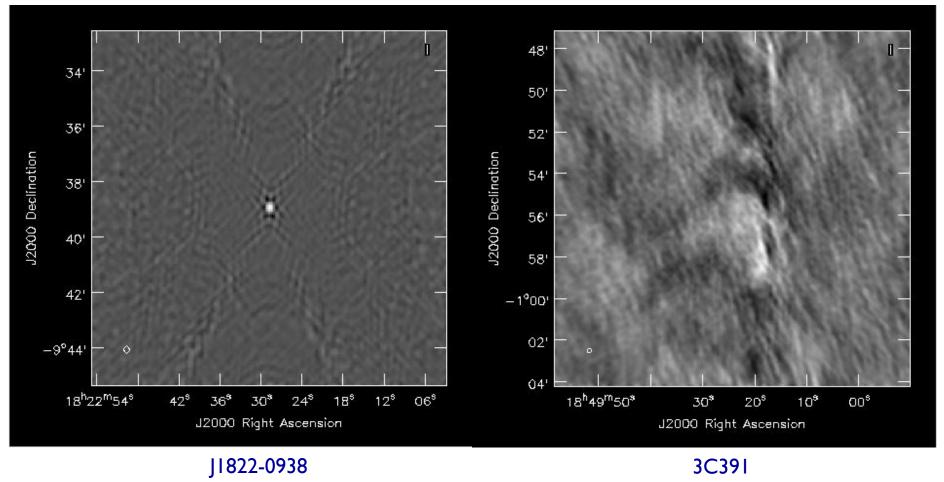












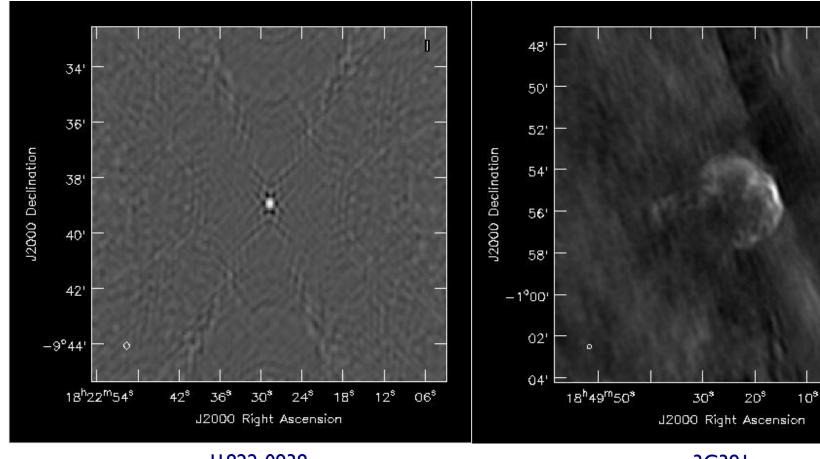
J1822-0938 (calibrator)

3C391 (science)







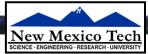


J1822-0938 (calibrator)

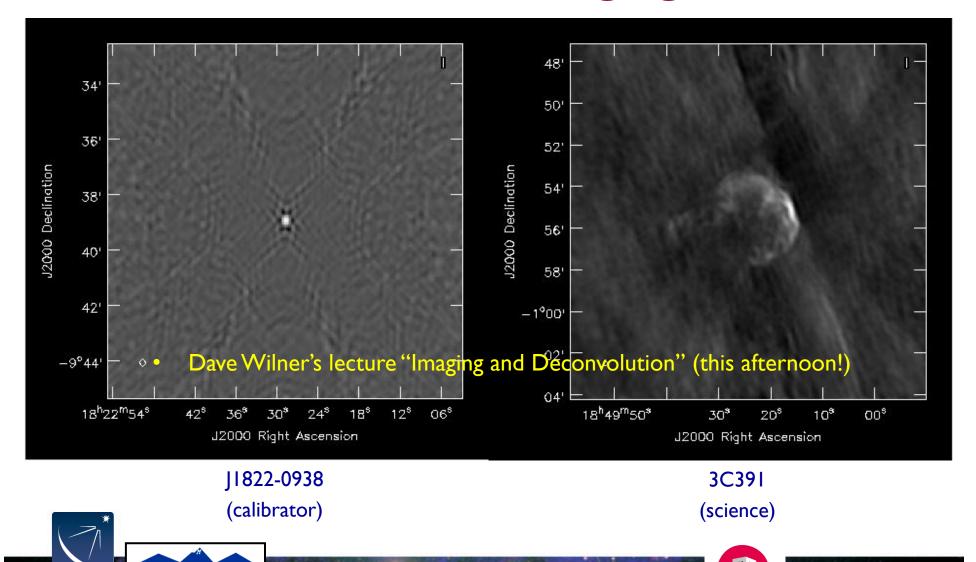
3C391 (science)

OO^s









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Evaluating Calibration Performance

- Are solutions continuous?
 - Noise-like solutions are just that—noise (beware: calibration of pure noise generates a spurious point source)
 - Discontinuities indicate instrumental glitches (interpolate with care)
 - Any additional editing required?
- Are calibrator data fully described by antenna-based effects?
 - Phase and amplitude closure errors are the baseline-based residuals
 - Are calibrators sufficiently point-like? If not, self-calibrate: model calibrator visibilities (by imaging, deconvolving and transforming) and resolve for calibration; iterate to isolate source structure from calibration components
 - Crystal Brogan's lecture: "Advanced Calibration" (Thursday)
- Any evidence of unsampled variation? Is interpolation of solutions appropriate?
 - Reduce calibration timescale, if SNR permits
 - Greg Taylor's lecture: "Error Recognition" (Monday)

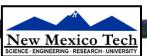




Summary of Scalar Example

- Dominant calibration effects are antenna-based
 - Minimizes degrees of freedom
 - More precise
 - Preserves closure
 - Permits higher dynamic range safely!
- Point-like calibrators effective
- Flux density bootstrapping







Generalizations

- Full-polarization Matrix Formalism
- Calibration Effects Factorization
- Calibration Heuristics and 'Bootstrapping'







Full-Polarization Formalism (Matrices!)

• Need dual-polarization basis (p,q) to fully sample the incoming EM wave front, where p,q = R,L (circular basis) or p,q = X,Y (linear basis):

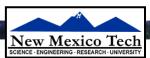
$$\vec{I}_{circ} = \vec{S}_{circ} \vec{I}_{Stokes}$$

$$\vec{I}_{lin} = \vec{S}_{lin} \vec{I}_{Stokes}$$

$$\vec{I}_{lin} = \vec{I}_{lin} \vec$$

- Devices can be built to sample these circular (R,L) or linear (X,Y) basis states in the signal domain (Stokes Vector is defined in "power" domain)
- Some components of J_i involve mixing of basis states, so dual-polarization matrix description desirable or even required for proper calibration







Full-Polarization Formalism: Signal Domain

Substitute:

$$S_i \rightarrow \vec{S}_i = \begin{pmatrix} S^p \\ S^q \end{pmatrix}_i, \quad J_i \rightarrow \vec{J}_i = \begin{pmatrix} J^{p \rightarrow p} & J^{q \rightarrow p} \\ J^{p \rightarrow q} & J^{q \rightarrow q} \end{pmatrix}_i$$

• The Jones matrix thus corrupts the vector wavefront signal as follows:

$$\vec{S}_{i}' = \vec{J}_{i}\vec{S}_{i}$$

$$\begin{pmatrix} S'^{p} \\ S'^{q} \end{pmatrix}_{i} = \begin{pmatrix} J^{p \to p} & J^{q \to p} \\ J^{p \to q} & J^{q \to q} \end{pmatrix}_{i} \begin{pmatrix} S^{p} \\ S^{q} \end{pmatrix}_{i}$$

$$= \begin{pmatrix} J^{p \to p}S^{p} + J^{q \to p}S^{q} \\ J^{p \to q}S^{p} + J^{q \to q}S^{q} \end{pmatrix}_{i}$$







Full-Polarization Formalism: Correlation - I

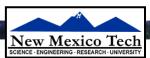
• Four correlations are possible from two polarizations. The *coherency* matrix represents correlation in the matrix formalism:

$$\vec{V}_{ij}^{true} = \left\langle \vec{S}_i \cdot \vec{S}_j^{*+} \right\rangle = \left\langle \left(\begin{array}{c} S^p \\ S^q \end{array} \right)_i \cdot \left(\begin{array}{c} S^{p*} \\ S^{p*} \end{array} \right)_j \right\rangle = \left(\begin{array}{c} \left\langle S_i^p \cdot S_j^{p*} \right\rangle & \left\langle S_i^p \cdot S_j^{q*} \right\rangle \\ \left\langle S_i^q \cdot S_j^{p*} \right\rangle & \left\langle S_i^q \cdot S_j^{q*} \right\rangle \end{array} \right)$$

Observed visibilities:

$$\vec{V}_{ij}^{obs} = \left\langle \vec{S}_i' \cdot \vec{S}_j'^* \right\rangle = \left\langle \left(\vec{J}_i \vec{S}_i \right) \cdot \left(\vec{J}_j^* \vec{S}_j^* \right)^+ \right\rangle = \vec{J}_i \left\langle \vec{S}_i \cdot \vec{S}_j^{*+} \right\rangle \vec{J}_j^{*+} = \vec{J}_i \vec{V}_{ij}^{true} \vec{J}_j^{*+}$$







Full-Polarization Formalism: Correlation - II

And finally, for fun, expand the correlation of corrupted signals:

$$\begin{split} \vec{V}_{ij}^{obs} &= \vec{J}_i \left\langle \vec{s}_i \cdot \vec{s}_j^{*+} \right\rangle \vec{J}_j^{*+} \\ &= \begin{pmatrix} J_i^{p \to p} J_j^{*p \to p} \left\langle s_i^p \cdot s_j^{*p} \right\rangle + J_i^{p \to p} J_j^{*q \to p} \left\langle s_i^p \cdot s_j^{*q} \right\rangle + & J_i^{p \to p} J_j^{*p \to q} \left\langle s_i^p \cdot s_j^{*p} \right\rangle + J_i^{p \to p} J_j^{*q \to q} \left\langle s_i^p \cdot s_j^{*q} \right\rangle + \\ J_i^{q \to p} J_j^{*p \to p} \left\langle s_i^q \cdot s_j^{*p} \right\rangle + J_i^{q \to p} J_j^{*q \to p} \left\langle s_i^q \cdot s_j^{*q} \right\rangle & J_i^{q \to p} J_j^{*p \to q} \left\langle s_i^q \cdot s_j^{*p} \right\rangle + J_i^{q \to p} J_j^{*q \to q} \left\langle s_i^p \cdot s_j^{*q} \right\rangle \\ &= \begin{pmatrix} J_i^{p \to q} J_j^{*p \to p} \left\langle s_i^p \cdot s_j^{*p} \right\rangle + J_i^{p \to q} J_j^{*q \to p} \left\langle s_i^p \cdot s_j^{*q} \right\rangle + & J_i^{p \to q} J_j^{*p \to q} \left\langle s_i^p \cdot s_j^{*p} \right\rangle + J_i^{p \to q} J_j^{*q \to q} \left\langle s_i^p \cdot s_j^{*q} \right\rangle + \\ J_i^{q \to q} J_j^{*p \to p} \left\langle s_i^q \cdot s_j^{*p} \right\rangle + J_i^{q \to q} J_j^{*q \to p} \left\langle s_i^q \cdot s_j^{*q} \right\rangle & J_i^{q \to q} J_j^{*p \to q} \left\langle s_i^q \cdot s_j^{*p} \right\rangle + J_i^{q \to q} J_j^{*q \to q} \left\langle s_i^q \cdot s_j^{*q} \right\rangle \\ &= \begin{pmatrix} J_i^{p \to q} J_j^{*p \to p} \left\langle s_i^q \cdot s_j^{*p} \right\rangle + J_i^{p \to q} J_j^{*q \to p} \left\langle s_i^q \cdot s_j^{*q} \right\rangle + & J_i^{p \to q} J_j^{*p \to q} \left\langle s_i^q \cdot s_j^{*p} \right\rangle + J_i^{p \to q} J_j^{*q \to q} \left\langle s_i^q \cdot s_j^{*q} \right\rangle \\ &= \begin{pmatrix} J_i^{p \to q} J_j^{*p \to p} \left\langle s_i^q \cdot s_j^{*p} \right\rangle + J_i^{p \to q} J_j^{*q \to p} \left\langle s_i^q \cdot s_j^{*q} \right\rangle + & J_i^{p \to q} J_j^{*p \to q} \left\langle s_i^q \cdot s_j^{*p} \right\rangle + J_i^{p \to q} J_j^{*q \to q} \left\langle s_i^q \cdot s_j^{*q} \right\rangle \\ &= \begin{pmatrix} J_i^{p \to q} J_j^{*p \to q} \left\langle s_i^q \cdot s_j^{*p} \right\rangle + J_i^{p \to q} J_j^{*q \to p} \left\langle s_i^q \cdot s_j^{*q} \right\rangle + & J_i^{p \to q} J_j^{*p \to q} \left\langle s_i^q \cdot s_j^{*p} \right\rangle + J_i^{p \to q} J_j^{*q \to q} \left\langle s_i^q \cdot s_j^{*p} \right\rangle + & J_i^{p \to q} J_j^{*p \to q} \left\langle s_i^q \cdot s_j^{*p} \right\rangle + J_i^{p \to q} J_j^{*p \to q} \left\langle s_i^q \cdot s_j^{*p} \right\rangle + & J_i^{p \to q} J_j^{*p \to q} \left\langle s_i^q \cdot s_j^{*p} \right\rangle + & J_i^{p \to q} J_j^{*p \to q} \left\langle s_i^q \cdot s_j^{*p} \right\rangle + & J_i^{p \to q} J_j^{*p \to q} \left\langle s_i^q \cdot s_j^{*p} \right\rangle + & J_i^{p \to q} J_j^{*p \to q} \left\langle s_i^q \cdot s_j^{*p} \right\rangle + & J_i^{p \to q} J_j^{*p \to q} \left\langle s_i^q \cdot s_j^{*p} \right\rangle + & J_i^{p \to q} J_j^{*p \to q} \left\langle s_i^q \cdot s_j^{*p} \right\rangle + & J_i^{p \to q} J_j^{*p \to q} \left\langle s_i^q \cdot s_j^{*p} \right\rangle + & J_i^{p \to q} J_j^{*p \to q} \left\langle s_i^q \cdot s_j^{*p} \right\rangle + & J_i^{p \to q} J_j^$$

- UGLY, but we rarely, if ever, need to worry about algebraic detail at this level---just let this occur "inside" the matrix formalism, and work (think) with the matrix short-hand notation
- Synthesis instrument design driven by minimizing off-diagonal terms in J_i





The Matrix Measurement Equation

• We can now write down the Measurement Equation in matrix notation:

$$\vec{V}_{ij}^{obs} = \int_{sky} \left(\vec{J}_i \vec{I}_c(l,m) \vec{J}_j^{*+} \right) e^{-i2\pi \left(u_{ij}l + v_{ij}m \right)} dl dm$$

- $I_c(l,m)$ is the 2x2 matrix of Stokes parameter combinations corresponding to the coherency matrix of correlations (basis-dependent)
- ...and consider how the J_i are products of many effects.

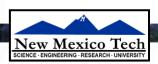






A Dictionary of Calibration Components

- \int_i contains many components, in principle:
 - *F* = ionospheric effects
 - *T* = tropospheric effects
 - *P* = parallactic angle
 - X = linear polarization position angle
 - *E* = antenna voltage pattern
 - D = polarization leakage
 - *G* = electronic gain
 - B = bandpass response
 - *K* = geometric compensation
 - M,A = baseline-based corrections
- Order of terms follows signal path (right to left)
- Each term has matrix form of J_i with terms embodying its particular algebra (on- vs. off-diagonal terms, etc.)
- Direction-dependent terms must stay inside FT integral
- 'Full' calibration is traditionally a bootstrapping process wherein relevant terms (usually a minority of above list) are considered in decreasing order of dominance, relying on approximate separability





 $\vec{J}_i = \vec{K}_i \vec{B}_i \vec{G}_i \vec{D}_i \vec{E}_i \vec{X}_i \vec{P}_i \vec{T}_i \vec{F}_i$

Ionospheric Effects, F

$$\vec{F}^{RL} = e^{i\Delta\phi} \begin{pmatrix} e^{-i\varepsilon} & 0 \\ 0 & e^{i\varepsilon} \end{pmatrix}; \ \vec{F}^{XY} = e^{i\Delta\phi} \begin{pmatrix} \cos\varepsilon & \sin\varepsilon \\ -\sin\varepsilon & \cos\varepsilon \end{pmatrix}$$

- The ionosphere introduces a dispersive path-length offset:
- $\Delta \phi \propto \frac{\int n_e \, dl}{v}$

- More important at lower frequencies (<5 GHz)
- Varies more at solar maximum and at sunrise/sunset, when ionosphere is most active and variable
- Direction-dependent within wide field-of-view
- The ionosphere is birefringent: Faraday rotation:

$$\varepsilon \propto \frac{\int B_{\parallel} \, n_e \, dl}{2}$$

- as high as 20 rad/m² during periods of high solar activity will rotate linear polarization position angle by ε = 50 degrees at 1.4 GHz
- Varies over the array, and with time as line-of-sight magnetic field and electron density vary, violating the usual assumption of stability in position angle calibration
- Book: Chapter 5, sect. 4.3,4.4,9.3; Chapter 6, sect. 6; Chapter 29, sect.3
 - Michiel Brentjens lecture: "Polarization in Interferometry" (next!)
 - Tracy Clark's lecture: "Low Frequency Interferometry" (Monday)





Tropospheric Effects, *T*

$$\vec{T} = \begin{pmatrix} t & 0 \\ 0 & t \end{pmatrix} = t \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$$

- The troposphere causes polarization-independent amplitude and phase effects due to emission/opacity and refraction, respectively
 - Up to 2.3m excess path length at zenith compared to vacuum
 - Higher noise contribution, less signal transmission: Lower SNR
 - Most important at v > 20 GHz where water vapor and oxygen absorb/emit
 - Zenith-angle-dependent (more troposphere path nearer horizon)
 - Clouds, weather = variability in phase and opacity; may vary across array
 - Water vapor radiometry (estimate phase from power measurements)
 - Phase transfer from low to high frequencies (delay calibration)
- Book: Chapter 5: sect. 4.3,4.4; Chapter 28, sect. 3
- ALMA!
 - Crystal Brogan's lecture: "Advanced Calibration Techniques" (Thursday)







Parallactic Angle, P

$$\vec{P}^{RL} = \begin{pmatrix} e^{-i\chi} & 0 \\ 0 & e^{i\chi} \end{pmatrix}; \ \vec{P}^{XY} = \begin{pmatrix} \cos \chi & \sin \chi \\ -\sin \chi & \cos \chi \end{pmatrix}$$

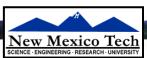
- Changing orientation of sky in telescope's field of view
 - Constant for equatorial telescopes
 - Varies for alt-az-mounted telescopes:

$$\chi(t) = \arctan\left(\frac{\cos l \sin h(t)}{\sin l \cos \delta - \cos l \sin \delta \cos h(t)}\right)$$

l = latitude, h(t) = hour angle, δ = declination

- Rotates the position angle of linearly polarized radiation
- Analytically known, and its variation provides leverage for determining polarization-dependent effects
- Book: Chapter 6, sect. 2.1
- Michiel Brentjens' lecture: "Polarization in Interferometry" (next!)







Linear Polarization Position Angle, X

$$\vec{X}^{RL} = \begin{pmatrix} e^{-i\Delta\chi} & 0 \\ 0 & e^{i\Delta\chi} \end{pmatrix}; \ \vec{X}^{XY} = \begin{pmatrix} \cos\Delta\chi & \sin\Delta\chi \\ -\sin\Delta\chi & \cos\Delta\chi \end{pmatrix}$$

- Configuration of optics and electronics (and refant) causes a net linear polarization position angle offset
- Can be treated as an offset to the parallactic angle, P
- Calibrated by registration with a strongly polarized source with known polarization position angle (e.g., flux density calibrators)
- For circular feeds, this is a phase difference between the R and L polarizations, which is frequency-dependent (a R-L phase bandpass)
- For linear feeds, this is the orientation of the dipoles in the frame of the telescope
- Michiel Brentjens' lecture: "Polarization in Interferometry" (next!)







Antenna Voltage Pattern, E

$$\vec{E}^{pq} = \begin{pmatrix} E^p(l,m) & 0\\ 0 & E^q(l,m) \end{pmatrix}$$

- Antennas of all designs have direction-dependent gain within field-of-view
 - Important when region of interest on sky comparable to or larger than λ/D
 - Important at lower frequencies where radio source surface density is greater and wide-field imaging techniques required
 - Beam squint: E^p and E^q offset, yielding spurious polarization
 - Sky rotates within field-of-view for alt-az antennas, so off-axis sources move through the pattern
 - Direction dependence of polarization leakage (D) may be included in E (off-diagonal terms then non-zero)
- Shape and efficiency of the voltage pattern may change with zenith angle: 'gain curve'
- Book: Chapters 19, 20
 - Steve Myers' lecture: "Wide Field Imaging I" (Thursday)
 - Brian Mason's lecture: "Wide Field Imaging II" (Monday)
 - Urvashi Rao Venkata's lecture: "Wide Bandwidth Imaging" (Monday)





Polarization Leakage, D

$$\vec{D} = \begin{pmatrix} 1 & d^p \\ d^q & 1 \end{pmatrix}$$

- Antenna & polarizer are not ideal, so orthogonal polarizations not perfectly isolated
 - Well-designed feeds have d ~ a few percent or less
 - A geometric property of the optics design, so frequency-dependent
 - For R,L systems, total-intensity imaging affected as $\sim dQ$, dU, so only important at high dynamic range $(Q,U,d \ each \ \sim few \ \%$, typically)
 - For R,L systems, linear polarization imaging affected as ~dl, so almost always important
 - For small arrays (no differential parallactic angle coverage), only relative D solution is possible from standard linearized solution, so parallel-hands cannot be corrected absolutely (closure errors)
- Best calibrator: Strong, point-like, observed over large range of parallactic angle (to separate source polarization from D)
- Book: Chapter 6

Michiel Brentjens' lecture: "Polarization in Interferometry" (next!)



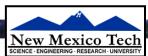


"Electronic" Gain, G

$$\vec{G}^{pq} = \begin{pmatrix} g^p & 0 \\ 0 & g^q \end{pmatrix}$$

- Catch-all for most amplitude and phase effects introduced by antenna electronics and other generic effects
 - Most commonly treated calibration component
 - Dominates other effects for most standard observations
 - Includes scaling from engineering (correlation coefficient) to radio astronomy units (Jy), by scaling solution amplitudes according to observations of a flux density calibrator
 - Includes any internal system monitoring, like EVLA switched power calibration
 - Often also includes tropospheric and (on-axis) ionospheric effects which are typically difficult to separate uniquely from the electronic response
 - Excludes frequency dependent effects (see B)
- Best calibrator: strong, point-like, near science target; observed often enough to track expected variations
 - Also observe a flux density standard
- Book: Chapter 5





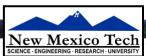


Bandpass Response, B

$$\vec{B}^{pq} = \begin{pmatrix} b^p(v) & 0 \\ 0 & b^q(v) \end{pmatrix}$$

- G-like component describing frequency-dependence of antenna electronics, etc.
 - Filters used to select frequency passband not square
 - Optical and electronic reflections introduce ripples across band
 - · Often assumed time-independent, but not necessarily so
 - Typically (but not necessarily) normalized
 - ALMA Tsys is a "bandpass"
- Best calibrator: strong, point-like; observed long enough to get sufficient per-channel SNR, and often enough to track variations
- Book: Chapter 12, sect. 2
- Mark Lacy's lecture: "Spectral Line Data Analysis" (today!)







Geometric Compensation, K

$$\vec{K}^{pq} = \begin{pmatrix} k^p & 0 \\ 0 & k^q \end{pmatrix}$$

- Must get geometry right for Synthesis Fourier Transform relation to work in real time
 - Antenna positions (geodesy)
 - Source directions (time-dependent in topocenter!) (astrometry)
 - Clocks
 - Electronic path-lengths introduce delays (polarization, spw differences)
 - Longer baselines generally have larger relative geometry errors, especially if clocks are independent (VLBI)
 - Importance scales with frequency
- K is a clock- & geometry-parameterized version of G (see chapter 5, section 2.1, equation 5-3 & chapters 22, 23)
 - All-sky observations used to isolate geometry parameters
- Book: Chapter 5, sect. 2.1; Chapters 22, 23
 - Adam Deller's lecture: "Very Long Baseline Interferometry" (Thursday)



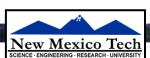




Non-closing Effects: M, A

- Baseline-based errors which do not decompose into antenna-based components
 - Digital correlators designed to limit such effects to well-understood and uniform (not dependent on baseline) scaling laws (absorbed in f.d. calibration)
 - Simple noise (additive)
 - Additional errors can result from averaging in time and frequency over variation in antenna-based effects and visibilities (practical instruments are finite!)
 - Instrumental polarization effects in parallel hands
 - Correlated "noise" (e.g., RFI)
 - Difficult to distinguish from source structure (visibility) effects
 - Geodesy and astrometry observers consider determination of radio source structure—a baseline-based effect—as a required calibration if antenna positions are to be determined accurately
 - Separate factors for each element of the coherency matrix; M multiplies, A adds







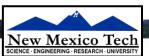
Solving the Measurement Equation

 Formally, solving for any antenna-based visibility calibration component is always the same general non-linear fitting problem:

$$\vec{V}_{ij}^{corrected \cdot obs} = \vec{J}_i \vec{V}_{ij}^{corrupted \cdot mod} \vec{J}_j^{*+}$$

- Observed and Model visibilities are corrected/corrupted by available prior calibration solutions
- Resulting solution used as prior in subsequent solves, as necessary
- Each solution is relative to priors and assumed source model
- lterate sequences, as needed → generalized self-calibration
- Viability and accuracy of the overall calibration depends on isolation of different effects using proper calibration observations, and appropriate solving strategies







Measurement Equation Heuristics

• When considering which effects are relevant to a particular observation, and how to sequence calibration determination, it is convenient to express the Measurement Equation in a "Heuristic Operator" notation:

$$V^{obs} = M B G D E X PT F V^{true} + A$$

- Rigorous notation, antenna-basedness, etc., suppressed
- Usually, only a subset of terms are considered, though highestdynamic range observations may require more
- An expression of a "Calibration Model"

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- Order is important (handled in software)
- Solve for terms in decreasing order of dominance, iterate to isolate
- NB: Non-trivial direction-dependent solutions involve convolutional treatment of the visibilities, and is coupled to the imaging and deconvolution process---see advanced imaging lectures....)



Decoupling Calibration Effects

- Multiplicative gain (G) term will soak up many different effects; known priors should be compensated for *explicitly*, especially when direction-dependent differences (e.g., between calibrator and target) will limit the accuracy of calibration transfer:
 - Zenith angle-dependent atmospheric opacity, phase (T,F)
 - Zenith angle-dependent gain curve (E)
 - Antenna position errors (K)
- Early calibration solves (e.g., G) are always subject to more subtle, uncorrected effects
 - E.g., instrumental polarization (D), which introduces gain calibration errors and causes apparent closure errors in parallel-hand correlations
 - When possible, iterate and alternate solves to decouple effects...







Calibration Heuristics – Spectral Line

Total Intensity Spectral Line (B=bandpass, G=gain):

$$V^{obs} = B G V^{true}$$

I. Preliminary Gain solve on B-calibrator:

$$V^{obs} = \underline{G}_R V^{mod}$$

2. Bandpass Solve (using G_B) on B-calibrator (then discard G_B):

$$V^{obs} = \underline{B} (G_B V^{mod})$$

3. Gain solve (using inverse of B) on all calibrators:

$$(B' V^{obs}) = \underline{G} V^{mod}$$

4. Flux Density scaling:

$$G \rightarrow G_f$$
 (enforce gain consistency)

5. Correct with inverted (primes) solutions:

$$V^{cor} = G_f B' V^{obs}$$

6. Image!







Calibration Heuristics - Polarimetry

Polarimetry (B=bandpass, G=gain, D=instr. poln, X=pos. ang., P=parallactic ang.): $V^{obs} = B G D X P V^{true}$

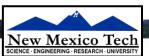
I. Preliminary Gain solve on B-calibrator:

$$V^{obs} = \underline{G}_{R} V^{mod}$$

- 2. Bandpass (B) Solve (using G_B) on B-calibrator (then discard G_B): $V^{obs} = B (G_B V^{mod})$
- 3. Gain (G) solve (using parallactic angle P, inverse of B) on calibrators: $(B' V^{obs}) = \underline{G} (PV^{mod})$
- 4. Instrumental Polarization (D) solve (using P, inverse of G,B) on instrumental polarization calibrator:

$$(G'B'V^{obs}) = D (PV^{mod})$$







Calibration Heuristics – Polarimetry

5. Polarization position angle solve (using P, inverse of D,G,B) on position angle calibrator:

$$(D'G'B'V^{obs}) = X (PV^{mod})$$

6. Flux Density scaling:

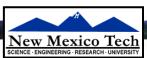
$$G \rightarrow G_f$$
 (enforce gain consistency)

7. Correct with inverted solutions:

$$V^{cor} = P'X'D'G_f'B'V^{obs}$$

- 8. Image!
- To use external priors, e.g., T (opacity), K (ant. position errors), E (gaincurve), revise step 3 above as:
 - 3. $(B'K'V^{obs}) = G(EPTV^{mod})$
 - and carry T, K, and E forward along with G to subsequent steps







New Calibration Challenges (EVLA, ALMA)

- 'Delay-aware' gain (self-) calibration
 - Troposphere and lonosphere introduce time-variable phase effects which are easily parameterized in frequency and should be (c.f. merely sampling the calibration in frequency)
- Frequency-dependent Instrumental Polarization
 - Contribution of geometric optics is wavelength-dependent (standing waves)
- Voltage pattern
 - Frequency-dependence voltage pattern
 - Wide-field accuracy (sidelobes, rotation)
 - Instrumental polarization (incl. frequency-dependence)
- WVR
- RFI mitigation
- Pipeline Heuristics
- Generalized refant algorithms

→Increased sensitivity: Can implied dynamic range be reached by calibration and imaging techniques?





Summary

- Determining calibration is as important as determining source structure—can't have one without the other
- Data examination and editing an important part of calibration
- Calibration dominated by antenna-based effects
 - permits efficient, accurate and defensible separation of calibration from astronomical information (satisfies closure)
- Full calibration formalism algebra-rich, but is modular
- Calibration an iterative process, improving various components in turn, as needed
- Point sources are the best calibrators
- Observe calibrators according requirements of calibration components



