

# Channel Modeling and Characteristics

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Dr. Farid Farahmand

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# Line-of-Sight Transmission (LOS)

## Impairments

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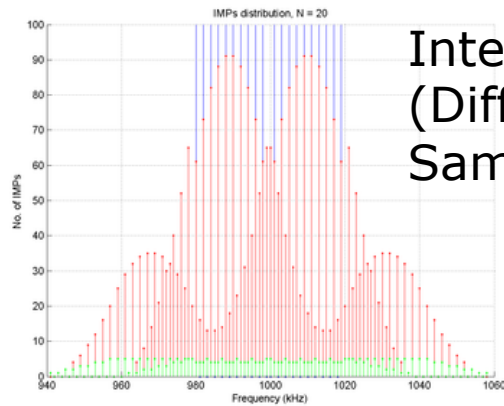
- The received signal is different from the transmitted signal due to transmission impairments
  - Most significant impairments
    - Thermal noise
    - Free space loss
      - Attenuation and attenuation distortion
    - Atmospheric absorption
      - water vapor and oxygen contribute to attenuation
    - Noise
    - Shadowing
      - due to reflection and diffraction
    - Multipath and fading
      - due to reflection, scattering, and diffraction
    - Refraction
-

# Review - Categories of Noise

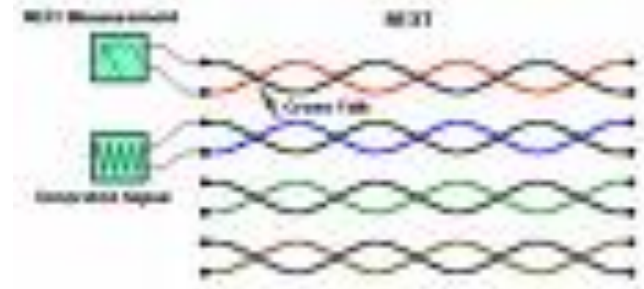
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- Thermal Noise
  - Intermodulation noise
  - Crosstalk
  - Impulse Noise
-

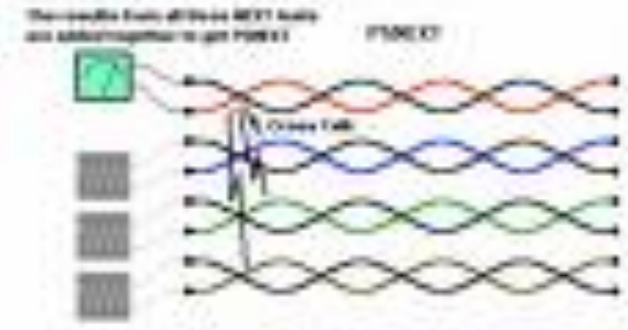
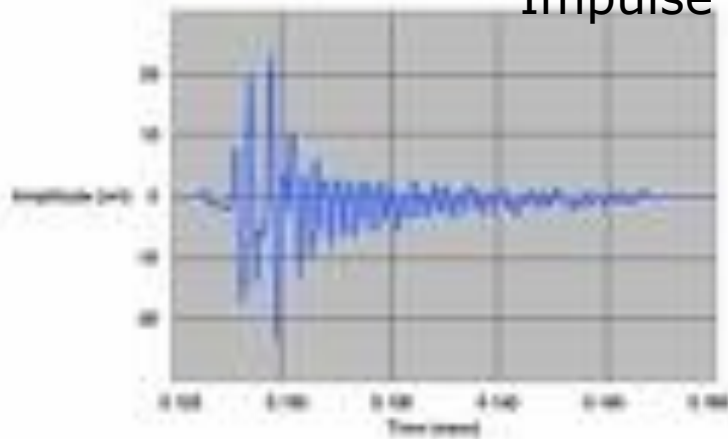
# Other Types of Noise - Example



Intermodulation noise  
(Diff. signals sharing the  
Same medium)



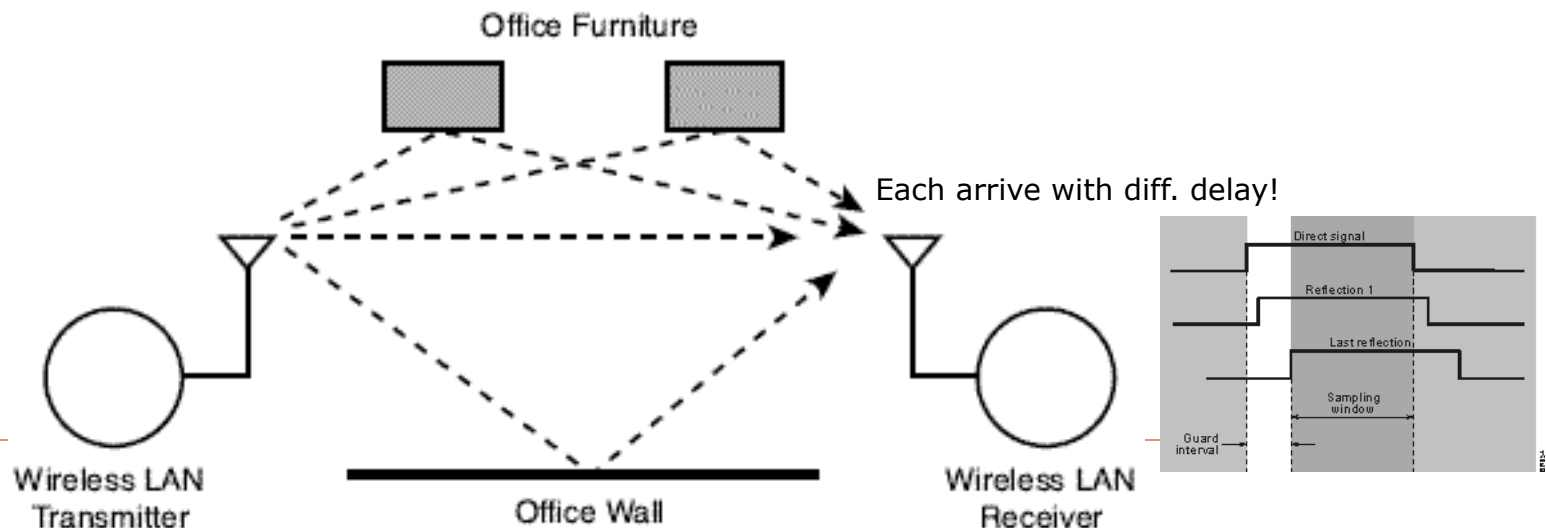
Impulse noise



Crosstalk  
(coupling)

# The Effects of Multipath Propagation

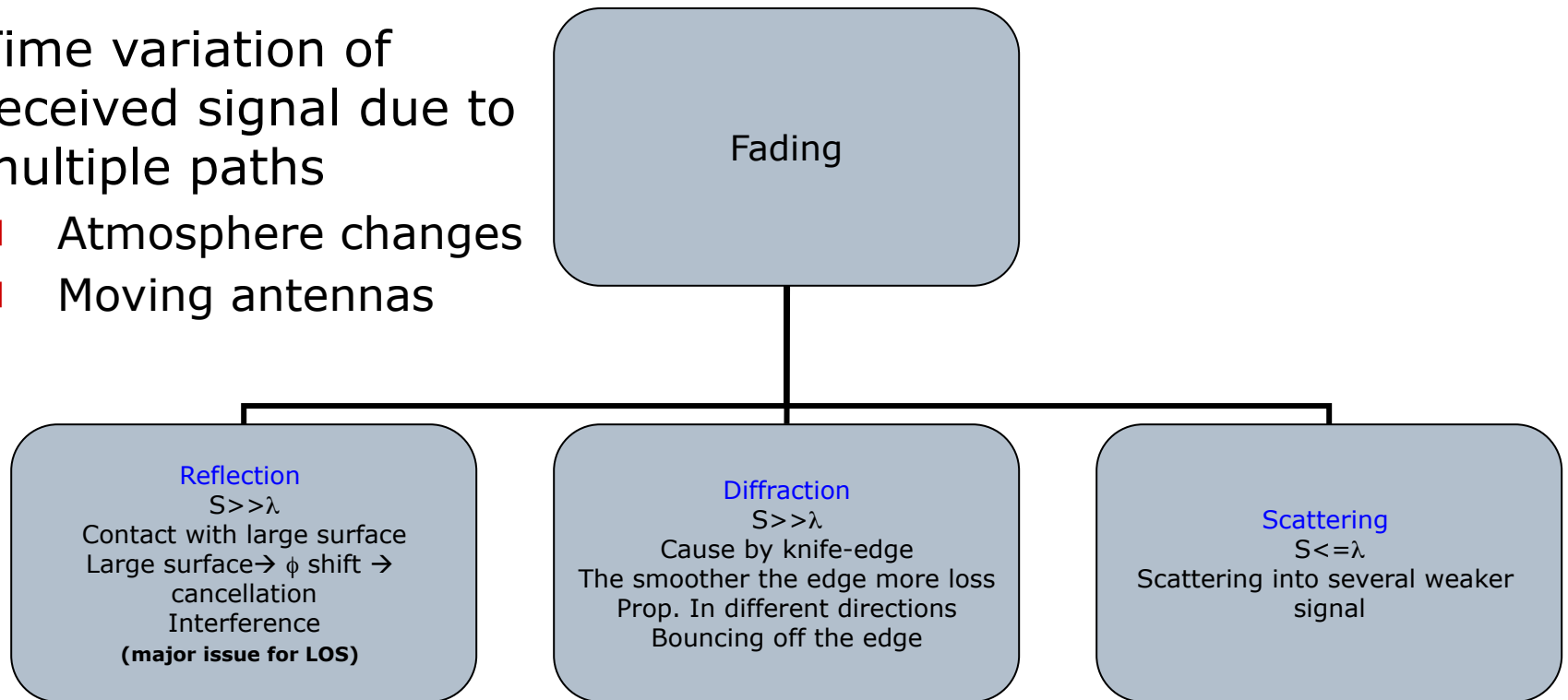
- ❑ Multiple copies of a signal may arrive at different phases
  - obstacles reflect signals so that multiple copies with varying delays are received
  - If phases add destructively, the signal level relative to noise declines, making detection more difficult
- ❑ Intersymbol interference (ISI)
  - Direct result of multipath → One or more delayed copies of a pulse may arrive at the same time as the primary pulse for a subsequent bit



# Fading

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- Time variation of received signal due to multiple paths
  - Atmosphere changes
  - Moving antennas



# Propagation Mechanism (1)

## Reflection

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- Occurs when signal encounters a surface that is **large** relative to the wavelength of the signal
    - Generally flat surface
    - Examples: Building, walls, Earth surface
    - The surface can be dielectric or conductor
    - The reflected field is diminished
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# Propagation Mechanism (2)

## Diffraction

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- ❑ Occurs at the **edge** of an impenetrable body that is large compared to wavelength of radio wave
  - ❑ Radio path is obstructed by a surface with sharp edges
  - ❑ Secondary waves are generated
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# Propagation Mechanism (3)

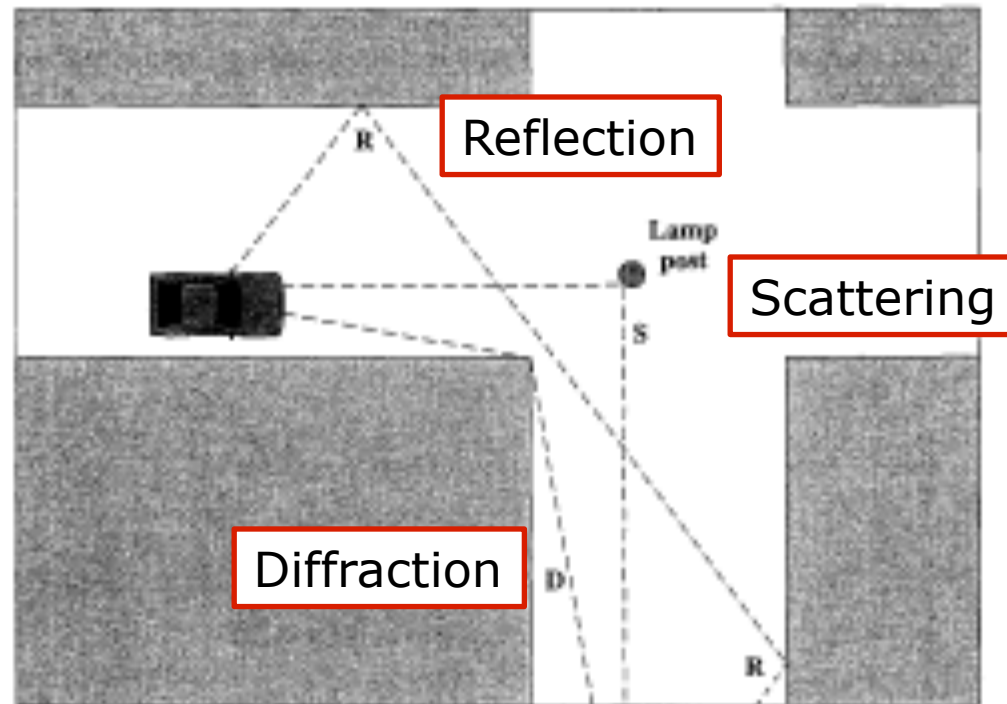
## Scattering

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- ❑ occurs when incoming signal hits an object whose size is the order of the wavelength of the signal or **less**
  - ❑ The flat surfaces can cause protuberance (projection)
  - ❑ Surface can be rough or smooth
  - ❑ Example: foliage, street signs, etc.
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# Different Propagation Mechanisms

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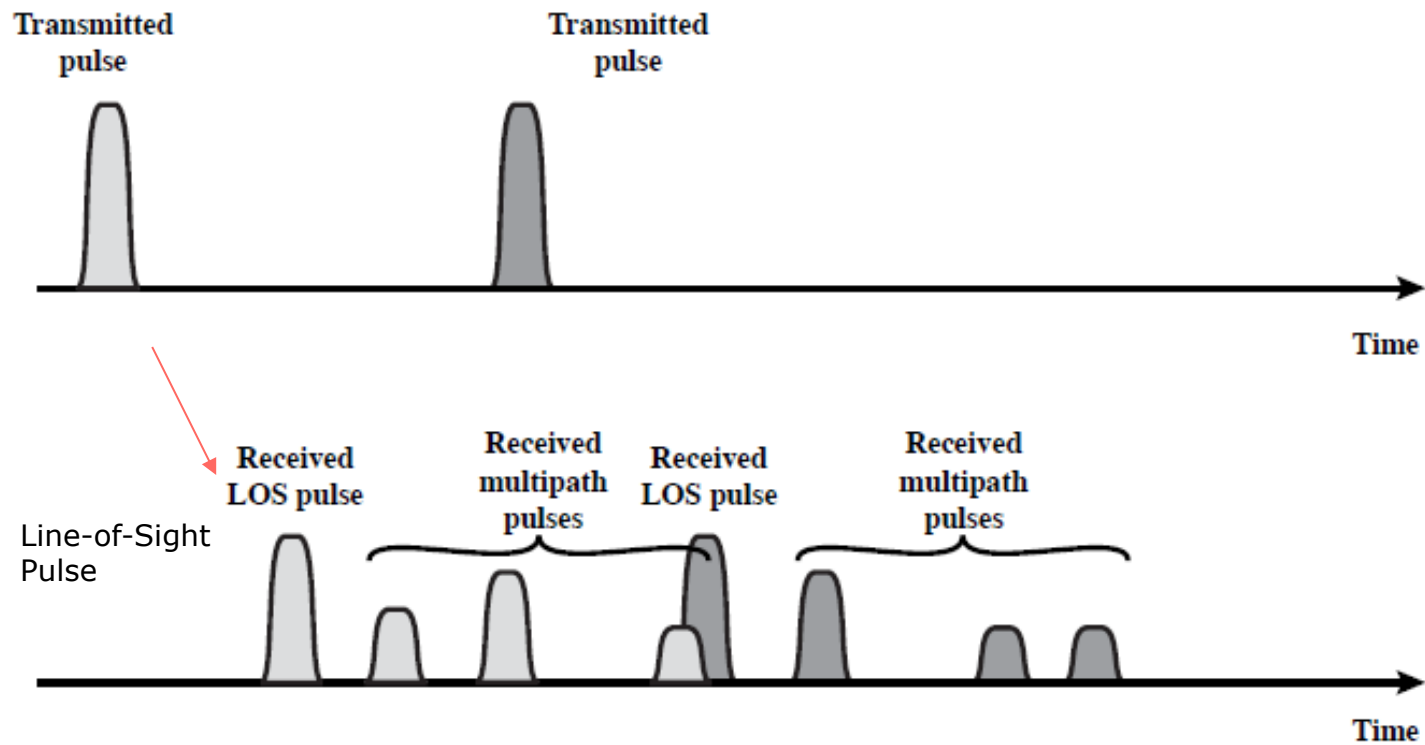


Sketch of Three Important Propagation Mechanisms:  
Reflection (R), Scattering (S), Diffraction (D) [ANDE95]

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# Impact of Fading

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# Impact of Fading

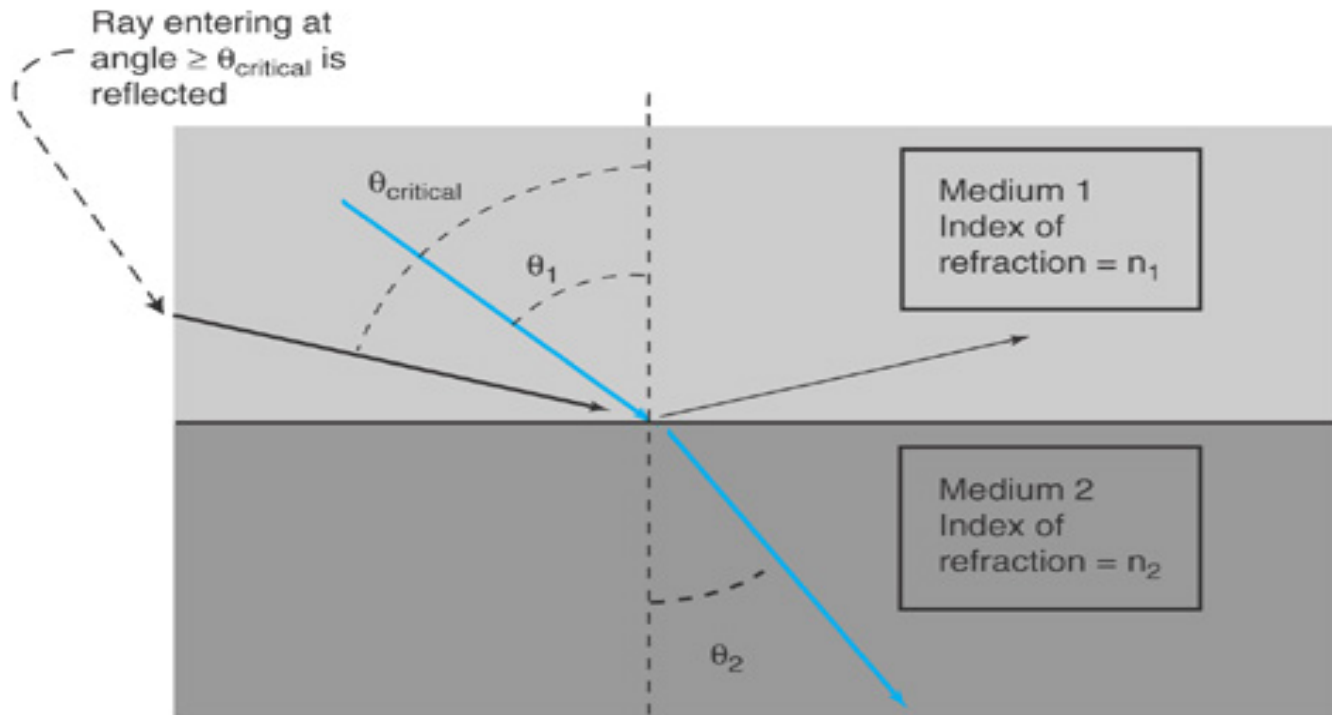
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- Beam bending
  - Ducting
  - Fast fading
  - Slow fading
  - Flat fading
  - Selective fading
  - Rayleigh fading
  - Rician fading
-

# Refraction

bending of radio waves as they propagate through the atmosphere

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Snell's law gives  
refraction angles:

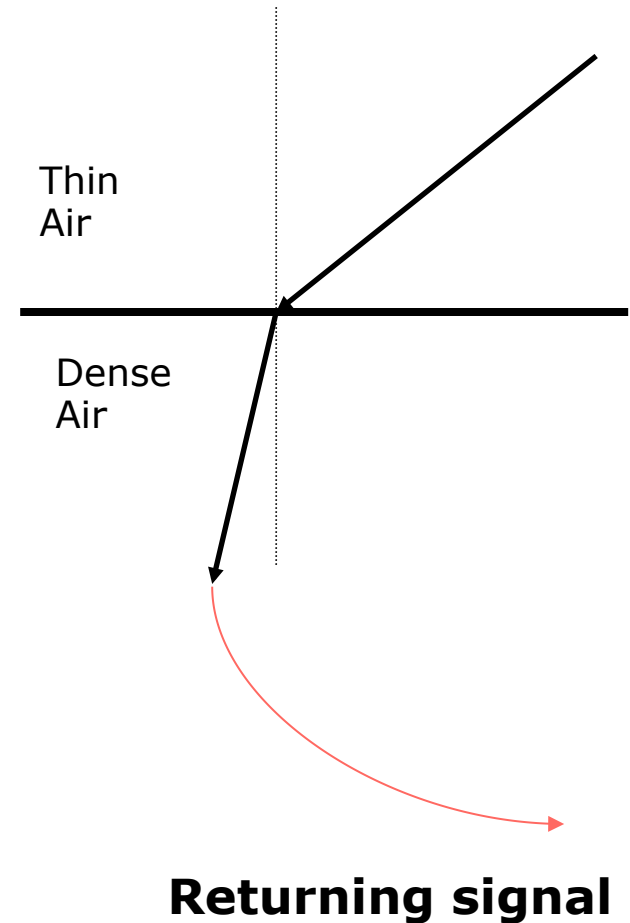
$$n_1 \sin \theta_1 = n_2 \sin \theta_2$$

$$\theta_{critical} = \sin^{-1} (n_2/n_1)$$

# Refraction

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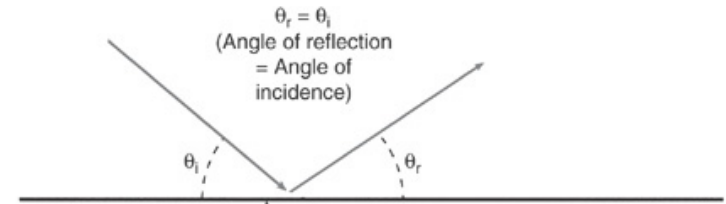
- Refraction – bending of microwaves by the atmosphere
  - Velocity of electromagnetic wave is a function of the density of the medium
  - When wave changes medium, speed changes
  - Wave bends at the boundary between mediums



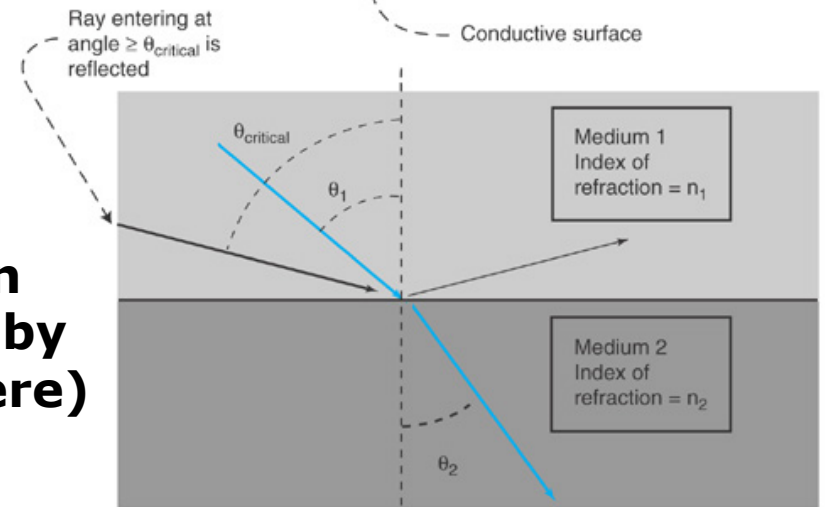
# Remember:

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## Reflection

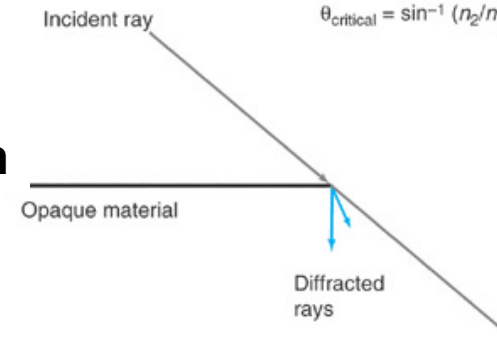


## Refraction (bending by atmosphere)



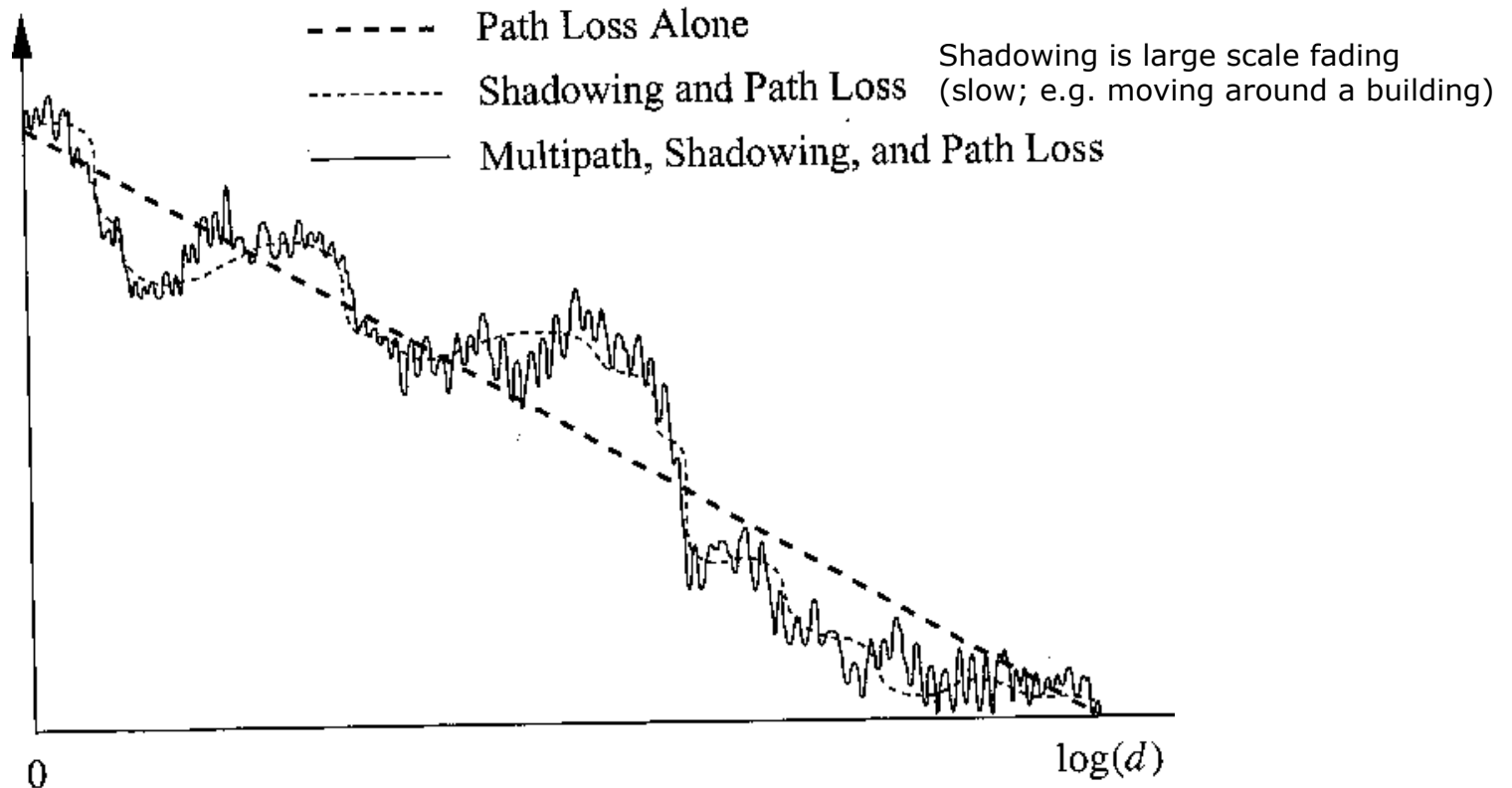
Snell's law gives refraction angles:  
 $n_1 \sin \theta_1 = n_2 \sin \theta_2$   
 $\theta_{\text{critical}} = \sin^{-1} (n_2/n_1)$

## Diffraction



# Shadowing and Multipath Impairments

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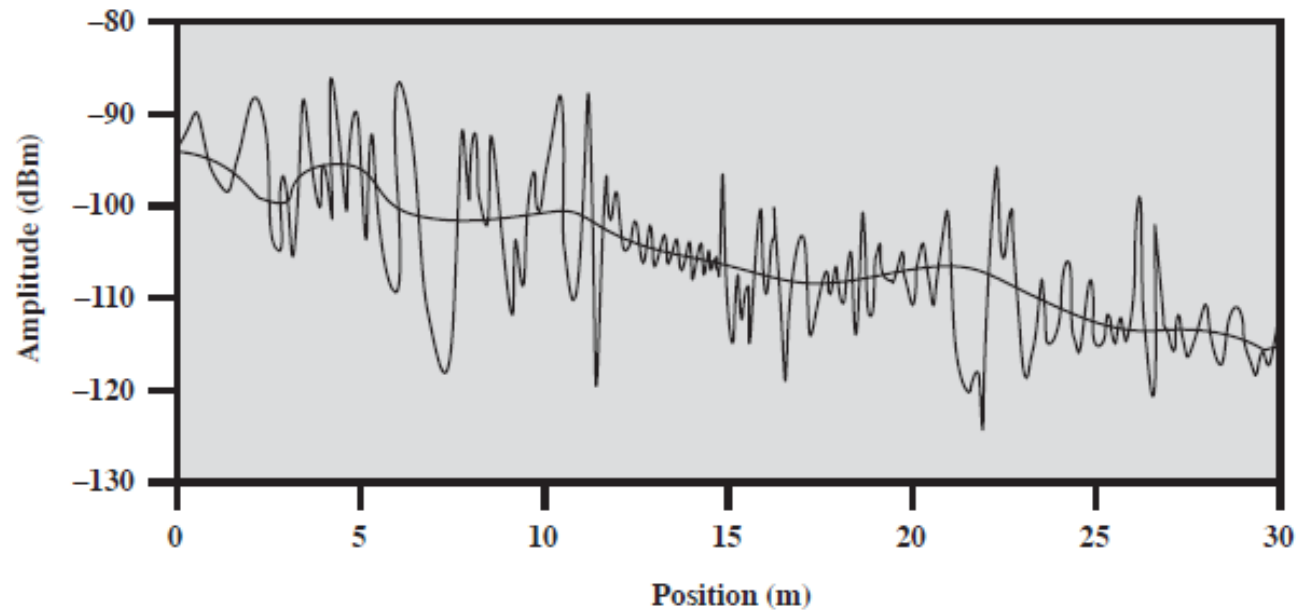




# Fast and Slow Fading

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Fast (small scale) and slow (large scale) fading  
Large scale fading is also called shadowing



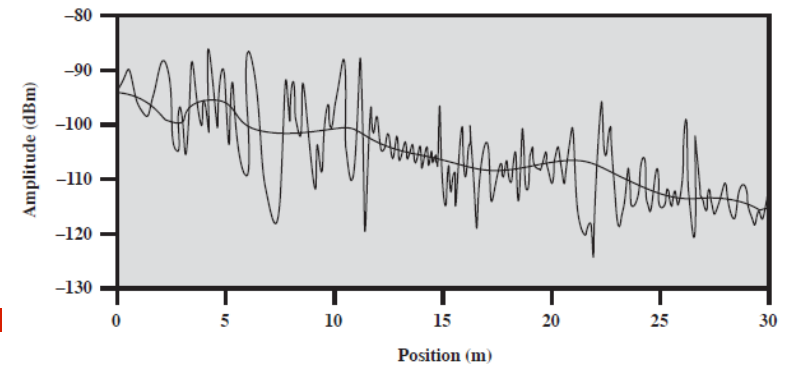
# Path Loss Channel Models

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- Free space models are limited
    - Good for satellite communications
    - Assumes line-of-sight
    - $P_{\text{received}}$  is proportional to  $1/d^2$
  - Other more realistic models
    - The receiver is not moving
    - The receiver is moving
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# Path Loss Channel Models -

Assume Stationary Receiver



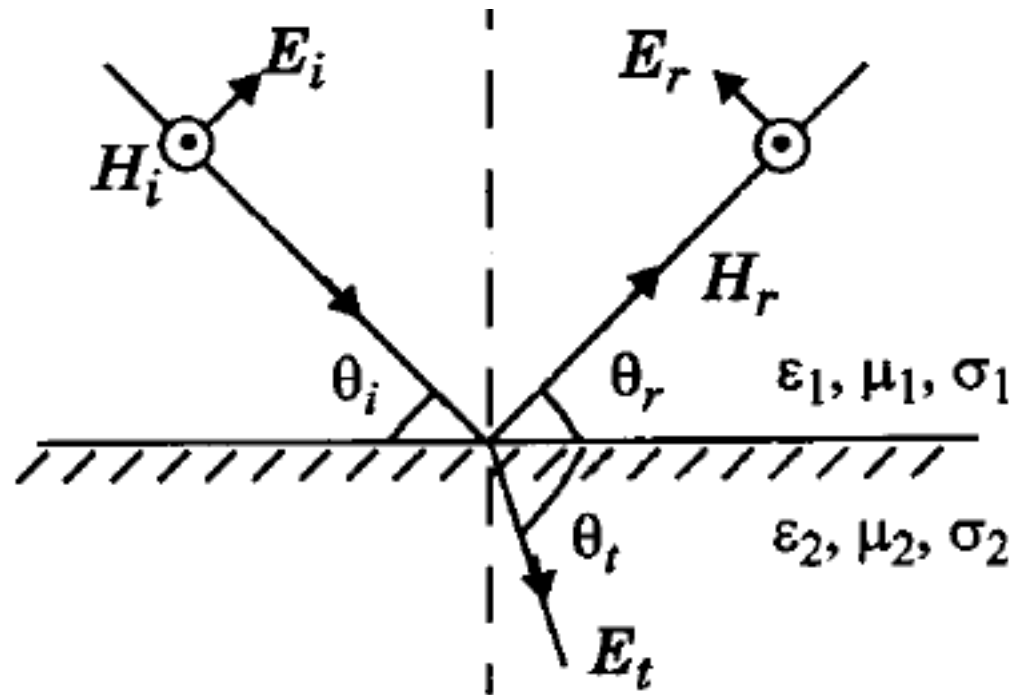
- Macroscopic Fading or large scale shadowing (fading)
  - The received power changes over as the distance varies
  - Models include:
    - 2-Ray; Statistical; Empirical
- Microscopic fading or small scale fading
  - The received power changes quickly
  - Models include:
    - 2-Ray, statistical

# 2-Ray Model (Earth Reflection)

## Assumptions

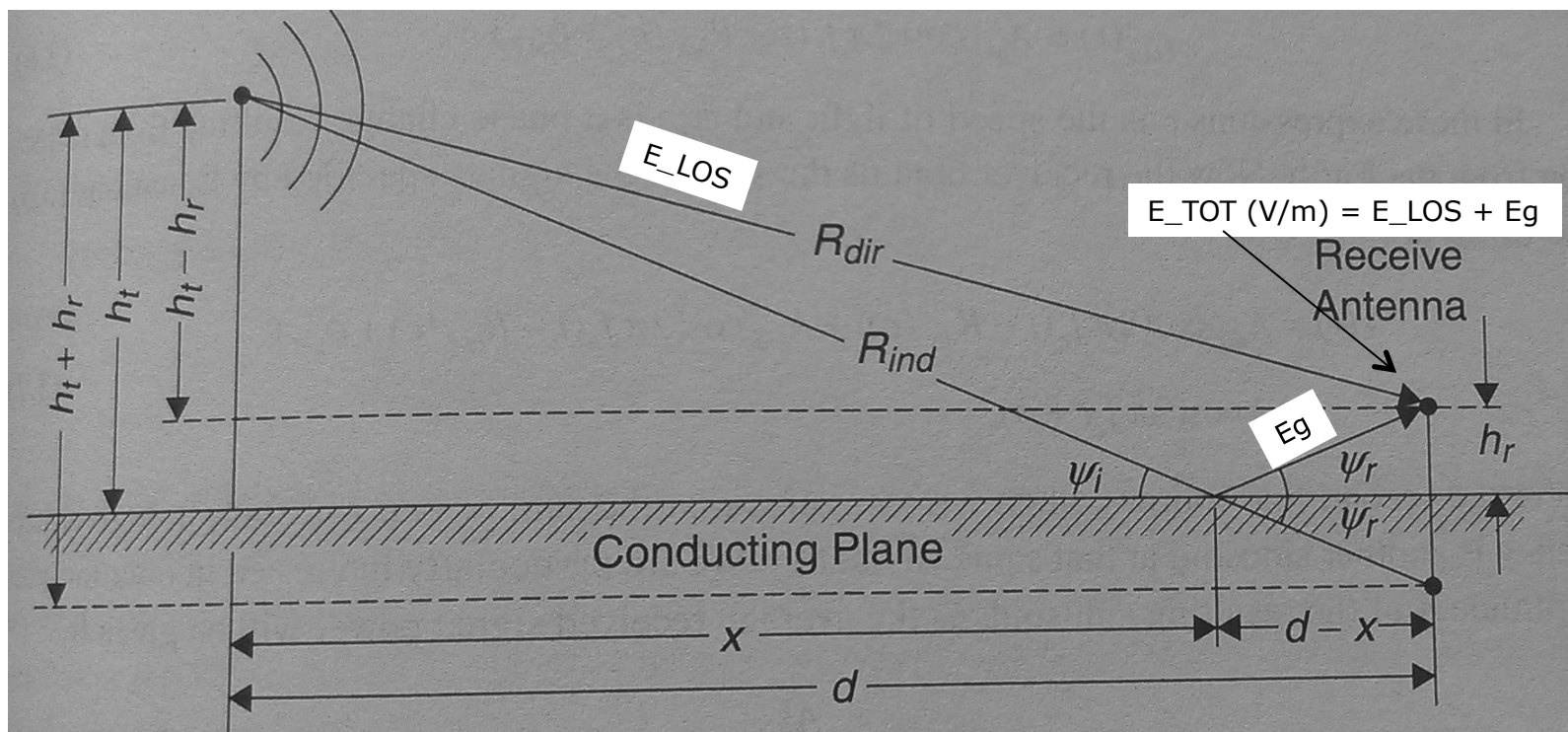
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$$\Gamma_{\parallel} = \frac{E_r}{E_i} = \frac{\eta_2 \sin \theta_t - \eta_1 \sin \theta_i}{\eta_2 \sin \theta_t + \eta_1 \sin \theta_i} \quad (\text{E-field in plane of incidence})$$



# 2-Ray Propagation Model – Earth Reflection Model

Using geometric optics; We assume  $d \gg h_t + h_r$



See notes

# 2-Ray Propagation Model – Earth Reflection Model

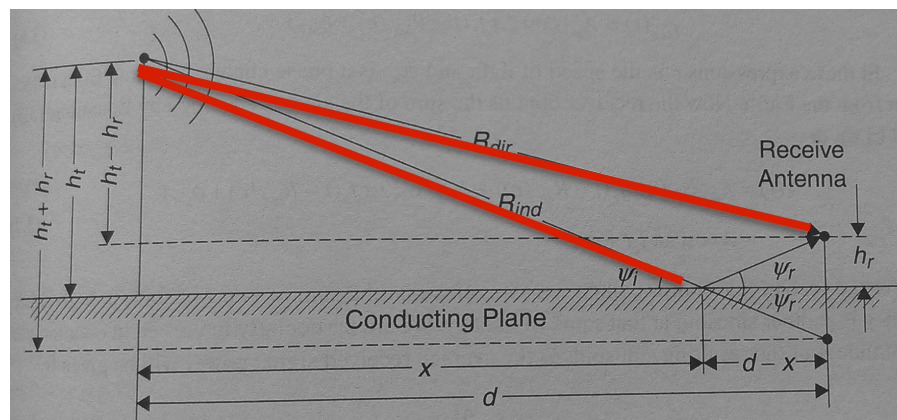
$$R_{dir} = \sqrt{(ht - hr)^2 + d^2} \approx d \left[ 1 + \frac{(ht - hr)^2}{2d^2} \right]$$

$$R_{indir} = \sqrt{(ht + hr)^2 + d^2} \approx d \left[ 1 + \frac{(ht + hr)^2}{2d^2} \right]$$

$$r_{dir}(t) = A_{dir} \cos(2\pi f_c(t - R_{dir}/c))$$

$$r_{indir}(t) = A_{indir} \cos(2\pi f_c(t - R_{indir}/c) + \phi_{ind})$$

$$r(t) = r_{dir}(t) + r_{indir}(t) = A \cos(2\pi f_c t + \phi)$$



What is A?

Key assumptions:

$A_{ind}$  and  $A_{dir}$  are almost the same

The angle of incident is about 180 deg.

$d \gg ht, hr$

$$A = 2A_{dir} \left| \sin \frac{(2\pi hr \cdot ht)}{d\lambda} \right| \approx 2A_{dir} \left| \frac{(2\pi hr \cdot ht)}{d\lambda} \right|$$

$$A_{dir} = A_0 / d$$

$$Pr_0 = A_0^2 / 2 = \frac{P_t G_t G_r \lambda^2}{(4\pi)^2 L_{sys}} \rightarrow A_0^2 = \frac{2P_t G_t G_r \lambda^2}{(4\pi)^2 L_{sys}}$$

$$Pr = A^2 / 2 = 2A_{dir}^2 \left| \frac{(2\pi hr \cdot ht)}{d\lambda} \right|^2 = 2 \frac{(2\pi hr \cdot ht)^2}{(d\lambda)^2} \times \frac{1}{d^2} \times \frac{2P_t G_t G_r \lambda^2}{(4\pi)^2 L_{sys}}$$

$$Path\_Loss = \frac{d^4}{G_t G_r h_r^2 \cdot h_t^2}$$

$$Pr = \frac{P_t G_t G_r h_r^2 \cdot h_t^2}{L_{sys}} \cdot \frac{1}{d^4}$$

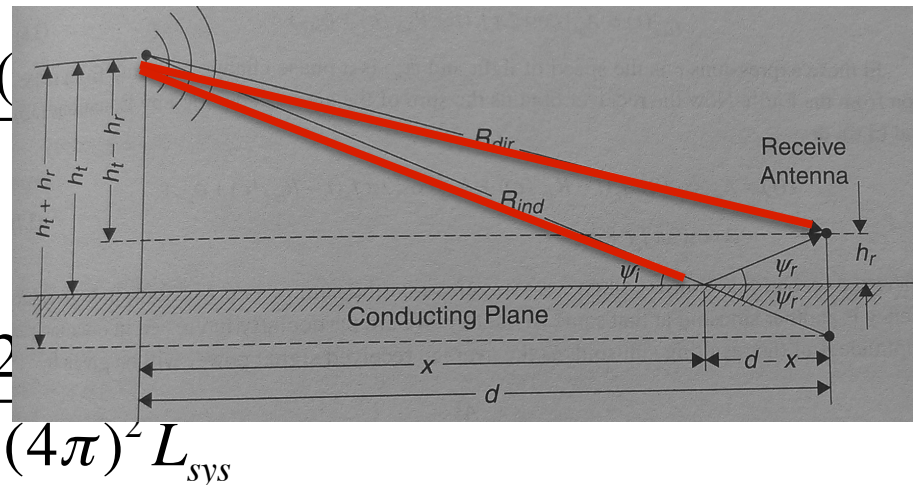
Power at the receiver

# 2-Ray Propagation Model – Earth Reflection Model

$$A = 2A_{dir} \left| \sin \frac{(2\pi hr \cdot ht)}{d\lambda} \right| \approx 2A_{dir} \left| \frac{(2\pi hr \cdot ht)}{d\lambda} \right|$$

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$$Pr = A^2 / 2 = 2A_{dir}^2 \left| \frac{(2\pi hr \cdot ht)}{d\lambda} \right|^2 = 2 \frac{(2\pi hr \cdot ht)^2}{(d\lambda)^2} \times \frac{1}{d^2} \times \frac{2 P_t G_t G_r \lambda^2}{(4\pi)^2 L_{sys}} \quad \text{Approximate to be } \rightarrow$$

$$Pr = \frac{P_t G_t G_r hr^2 \cdot ht^2}{L_{sys}} \cdot \frac{1}{d^4}$$

$$Path\_Loss = \frac{d^4}{G_t G_r hr^2 \cdot ht^2}$$

Approximated Power at the receiver

# 2-Ray Model (Earth Reflection)

## Example – A

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$H_t = 30$  m

$H_r = 2$  m

$G_r = 2$  dB

$G_t = 6$  dB

$F = 850$  MHz

Conductive Earth

$L_{\text{sys}} = 2$  dB

Using the 2-ray fading model find the RX power



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See notes



# Propagation Modes

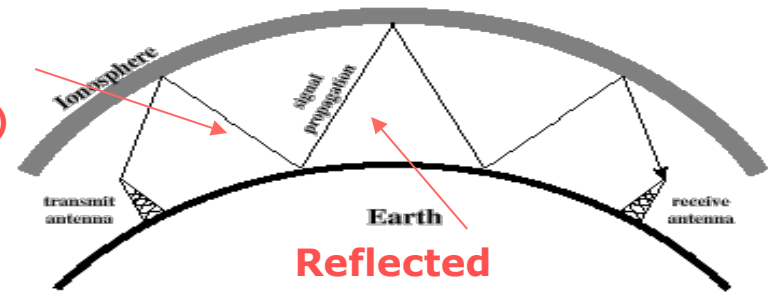
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- Radio wave reaches the receiver by one of the three signal paths:
    - Sky-wave propagation
    - Direct-wave or Line-of-sight propagation
    - Ground-wave propagation
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# Sky Wave Propagation

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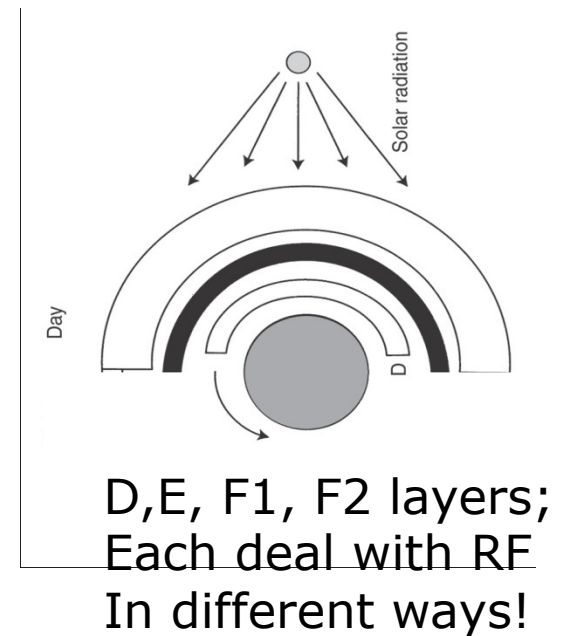
Refracted  
(reflects due to bending)



- Signal reflected from ionized layer of atmosphere (**ionosphere**) back down to earth
    - Ionosphere is a region of atmosphere that is ionized (charged)
    - This region of atmosphere has free electrons → different **index of refraction**
  - Signal can travel a number of hops, back and forth between ionosphere and earth's surface
  - **Reflection effect caused by refraction (this is because the signal bends and reflects back)**
  - Examples
    - Amateur radio
    - CB radio
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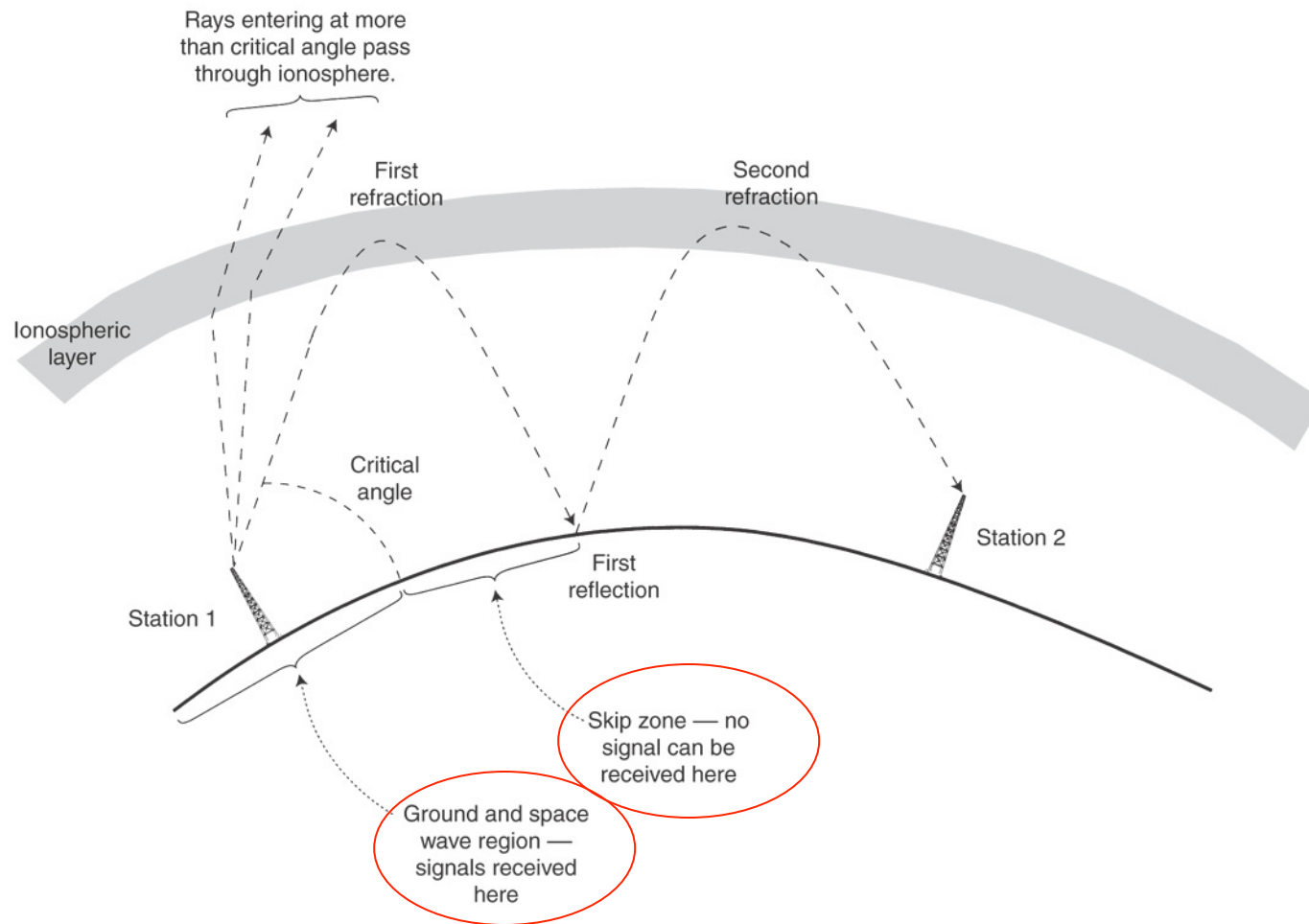
# Sky Wave Propagation

- D-layer is close to earth (45-55 miles altitude)
  - Absorbs RF ( $f > 300\text{MHz}$ ) – RF Sponge
  - For RF  $< 300\text{MHz}$  D-layer ends the signal (refraction)
  - Ionization fades at night
  - Highly ionized during day time
    - It occupies denser atmosphere (electrons are denser)
    - Absorbs most of the RF except the ones radiated with critical angle

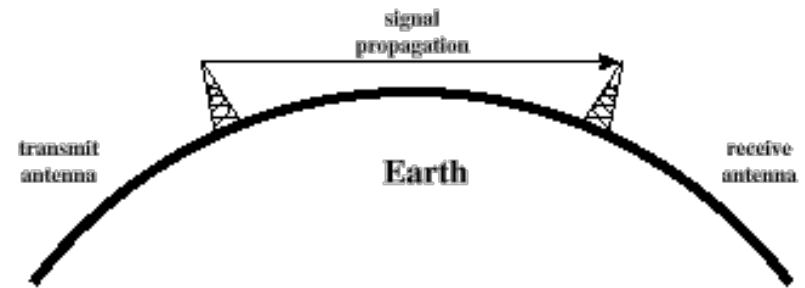


**Distant AM broadcast can be received much better at night!**

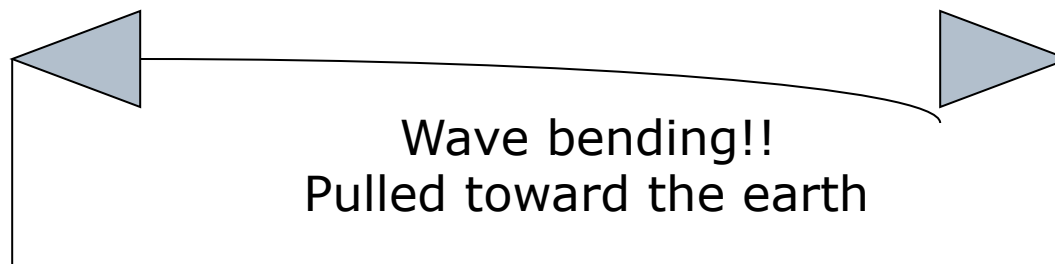
# Sky Wave (Skip) Propagation



# Line-of-Sight Propagation



- Transmitting and receiving antennas must be within line-of-sight
  - Example: Satellite communication
  - Dominant for **signals above 30 MHz**; no reflection due to ionosphere → can be transmitted via LOS
  - For ground communication – antennas must be within **effective line-of-site**
    - Note that microwaves are bent or refracted by the atmosphere





# Line-of-Sight Equations

- Optical line of sight

Max. distance between two Antennas for LOS when there is no obstacles

$$d = 3.57\sqrt{h}$$

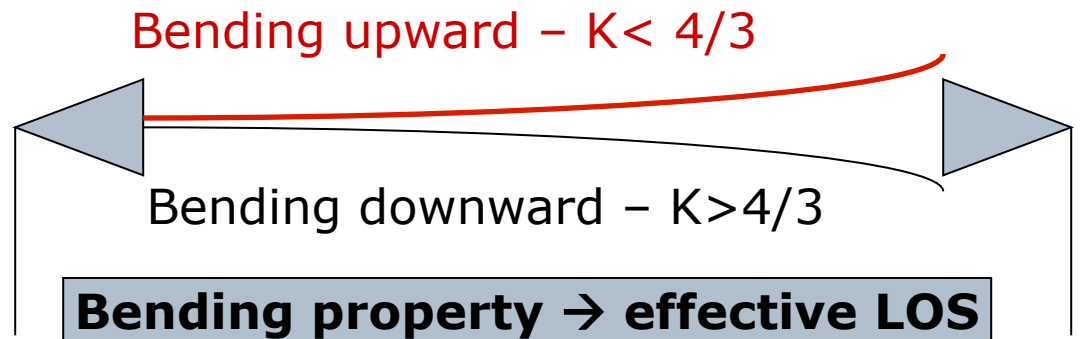
- Effective, or radio, line of sight (longer than optical)

$$d = 3.57\sqrt{Kh}$$

$d$  = distance between antenna and horizon (km)

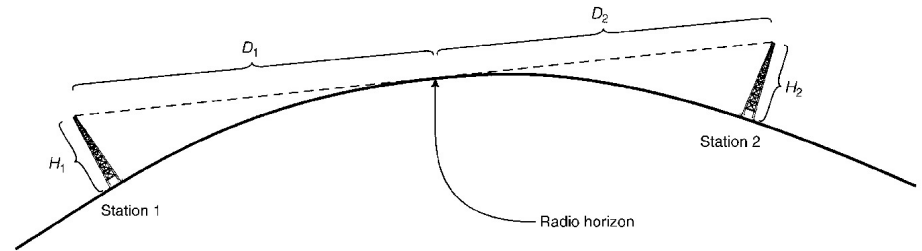
$h$  = antenna height (m)

$K$  = adjustment factor to account for refraction, rule of thumb  $K = 4/3$



# Line-of-Sight Equations

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- Maximum distance between two antennas for LOS propagation:

$$3.57 \left( \sqrt{Kh_1} + \sqrt{Kh_2} \right)$$

- $h_1$  = height of antenna one
- $h_2$  = height of antenna two

**Antennas placed in higher towers can have better reception!**

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# What is the benefit of raising the antenna?

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Case 1:

$H_2 = 0$ ;  $H_1 = 100$  m

$K = 4/3$

Find  $d$  (maximum distance between the two antennas)

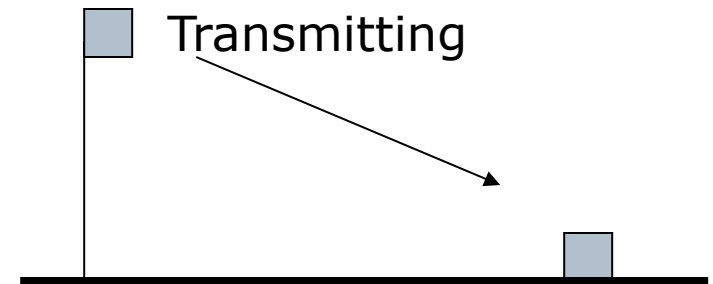
$$3.57 \left( \sqrt{Kh_1} + \sqrt{Kh_2} \right)$$

Case 2:

Let  $d = 41$  Km

$H_2 = 10$  m

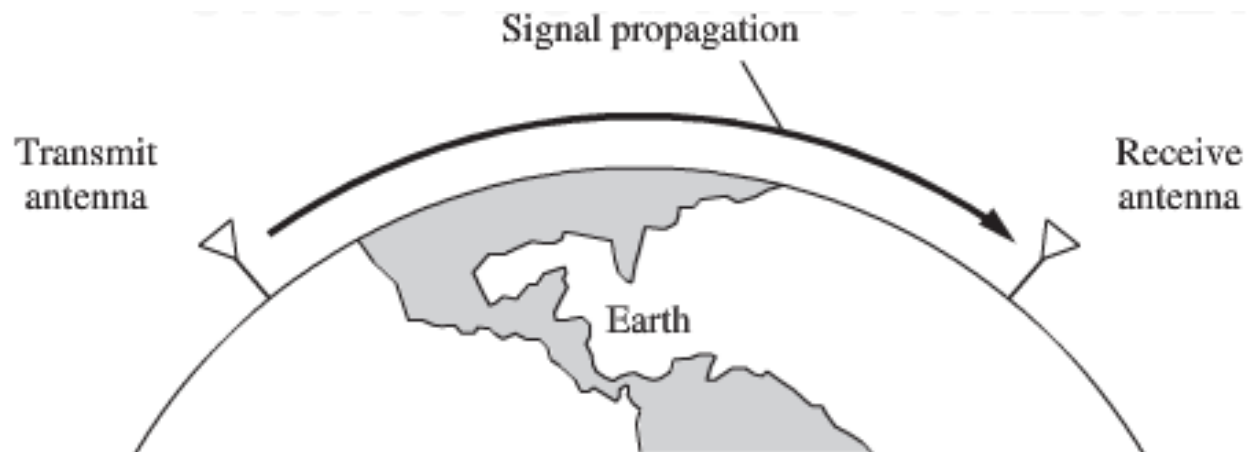
Find  $H_1$



# Ground-wave propagation

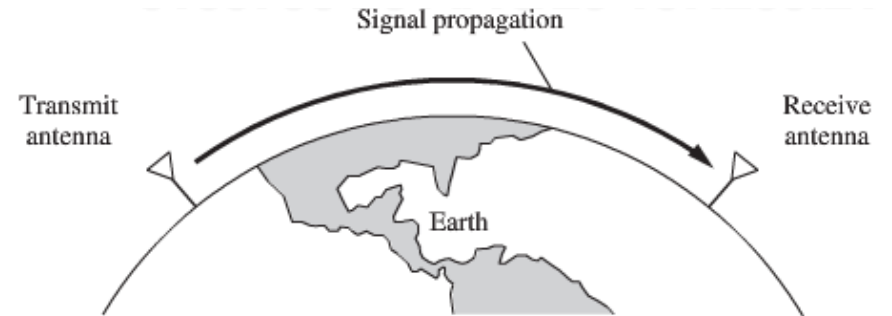
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- Follows contour of the earth
  - Thus, goes beyond the radio horizon limit
  - RF follows the curvature of the earth
- The dominant mode of propagation
  - waves are refracted (i.e., bent) gradually in an inverted U shape



# Ground-wave propagation

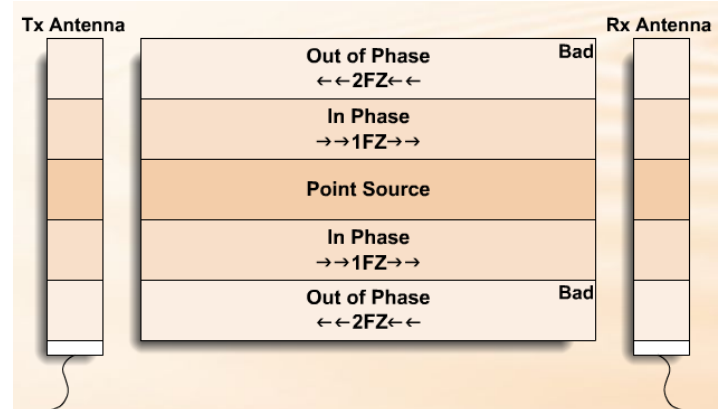
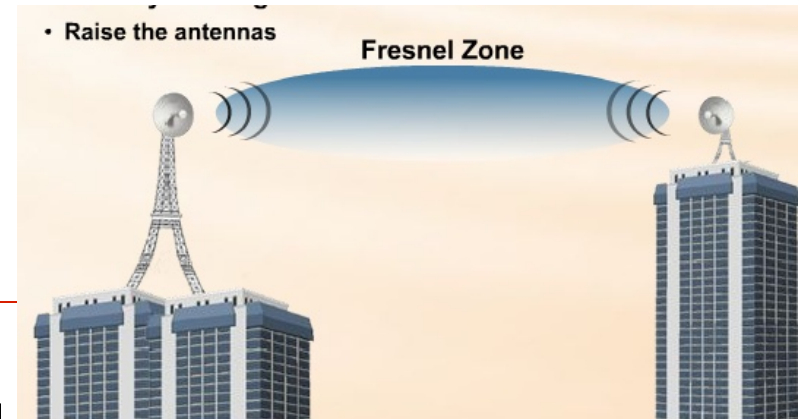
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- ❑ Can Propagate considerable distances
  - ❑ Does not penetrate the upper atmosphere
  - ❑ Frequencies up to 2 MHz
    - Example: AM radio
  - ❑ Not impacted by weather conditions s!o much
  - ❑ Highly impacted by earth conductivity
    - When traveling over Salt water (good conductive) → ground wave propagation is good
    - When the ground is dry or rocky → wave propagation is bad
-

# Diffraction: Fresnel (Freh-Nel)

- Fresnel discovered electromagnetic waves (light and RF signals) can bend (diffract) as they travel long distance and hit objects ( $S \gg WL$ )
- As a result of bending multiple signals along various paths can results
  - The paths vary  $n(WL)/2$
  - Out of phase signals  $\rightarrow$  signal cancelation!
- In order to minimize out-of-phase signals we need to make sure there is no obstacle within the first Fresnel (%60 or F1)



$$F_n = \sqrt{\frac{n \lambda d_1 d_2}{d_1 + d_2}}$$

# Fresnel Zone

$$F_n = \sqrt{\frac{n\lambda d_1 d_2}{d_1 + d_2}}$$

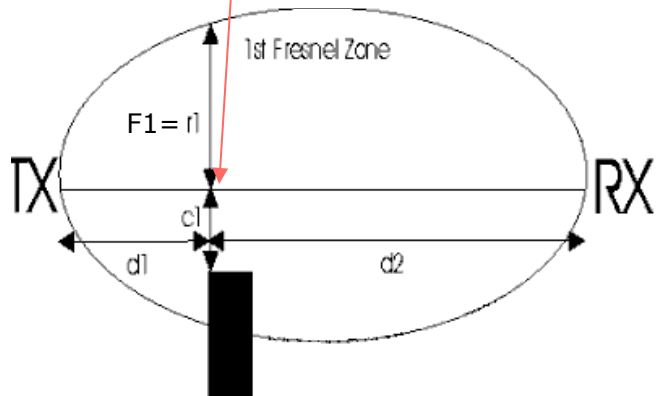
where,

$F_n$  = The **n**th Fresnel Zone radius in metres

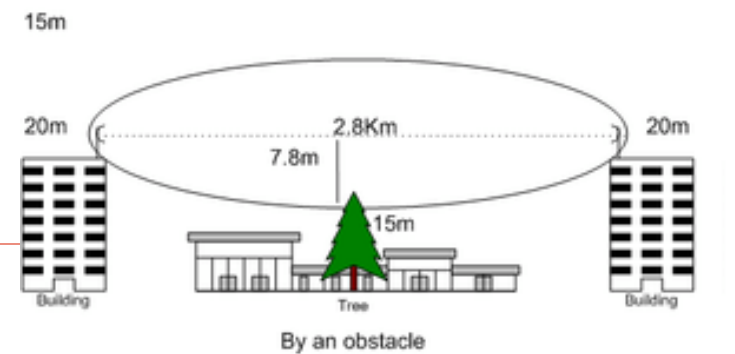
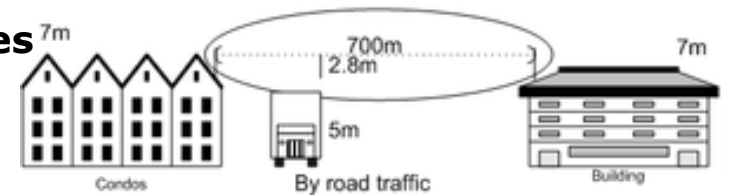
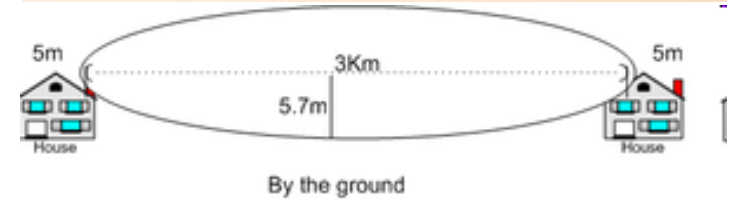
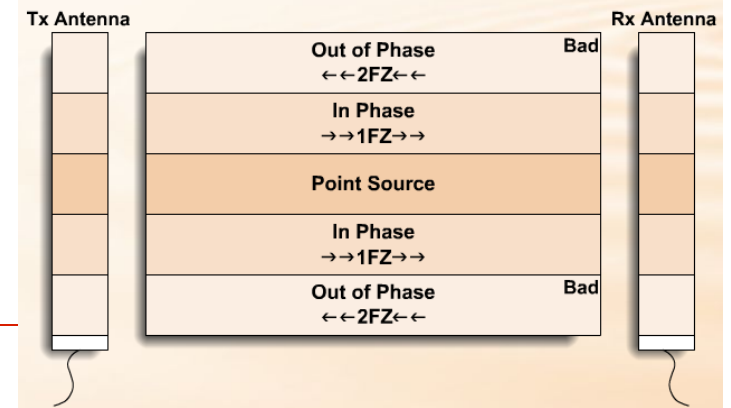
$d_1$  = The distance of P from one end in metres

$d_2$  = The distance of P from the other end in metres

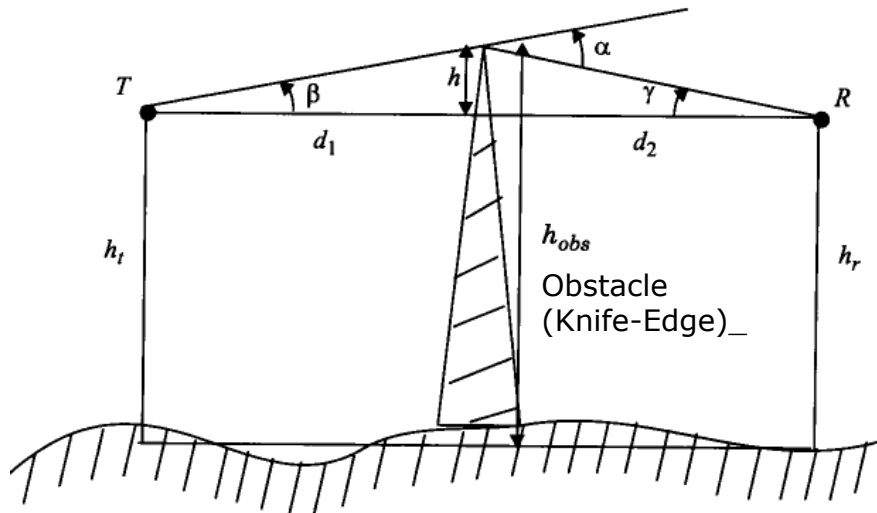
$\lambda$  = The wavelength of the transmitted signal in metres



Nasty obstacle must be more than 60% from the center line of TX to RX ( $c_1 \Rightarrow r_1 \times 0.6$ )

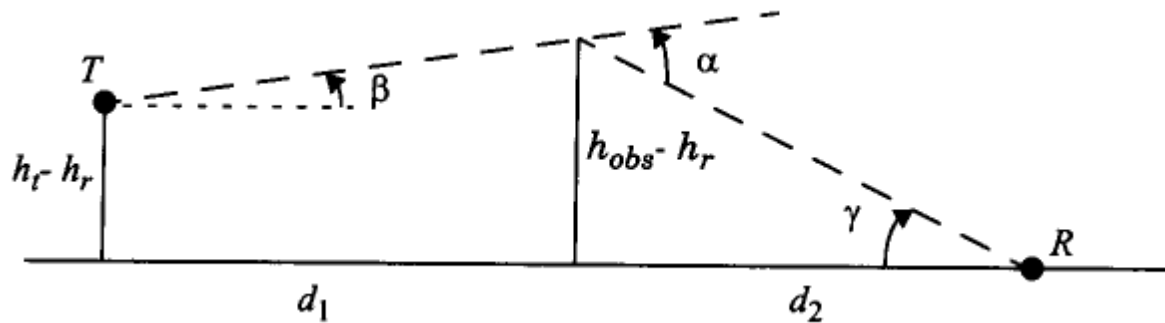


# Fresnel-Kirchoff Diffraction Parameter (V)



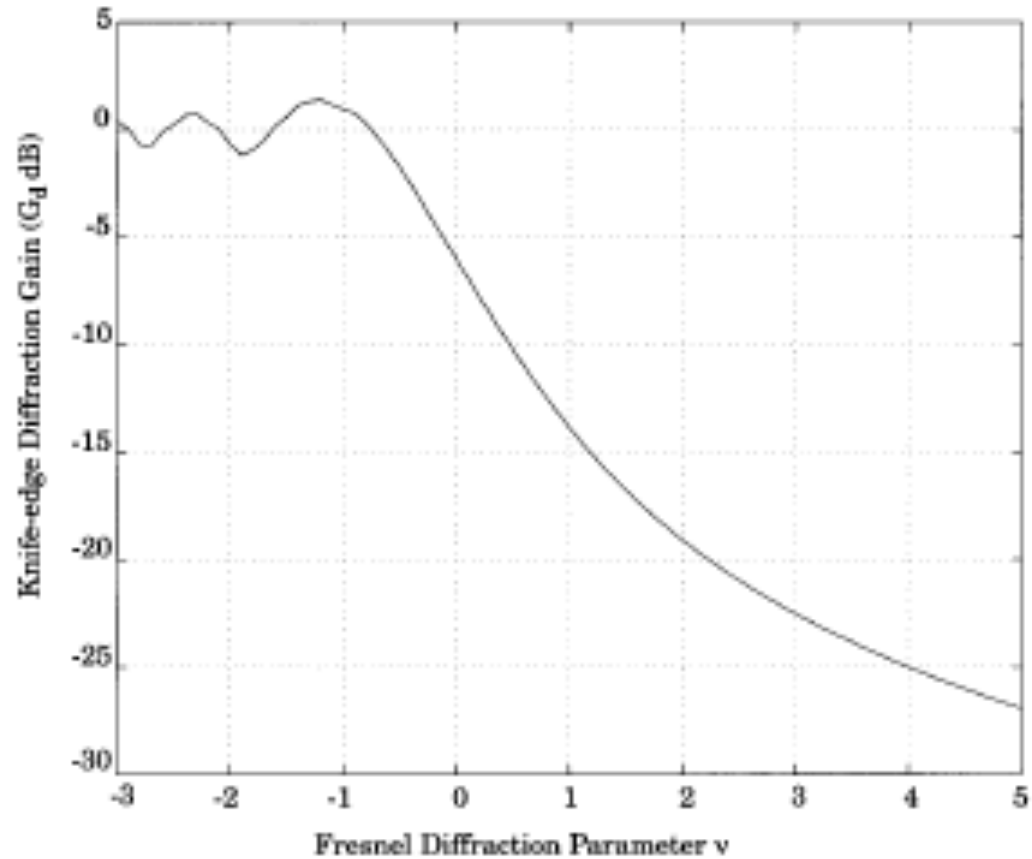
$$v = \alpha \sqrt{\frac{2d_1d_2}{(d_1 + d_2)\lambda}}$$

$$\alpha = \beta + \gamma$$



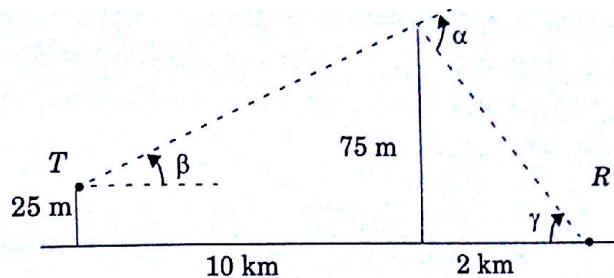
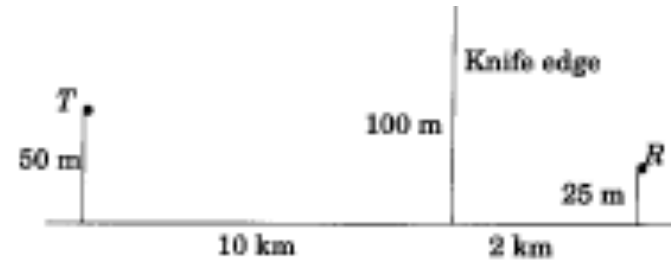
# Given the Fresnel Effect ( $v$ ) We can figure out the loss

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# EXAMPLE

Assume  $f=1900 \rightarrow WL=1/3$  m  
 Find the loss due to diffraction from the Knife edge obstacle



$$\beta = \tan^{-1}\left(\frac{75-25}{10000}\right) = 0.2865^\circ$$

$$\gamma = \tan^{-1}\left(\frac{75}{2000}\right) = 2.15^\circ$$

and

$$\alpha = \beta + \gamma = 2.434^\circ = 0.0424 \text{ rad}$$

Then using equation (3.56)

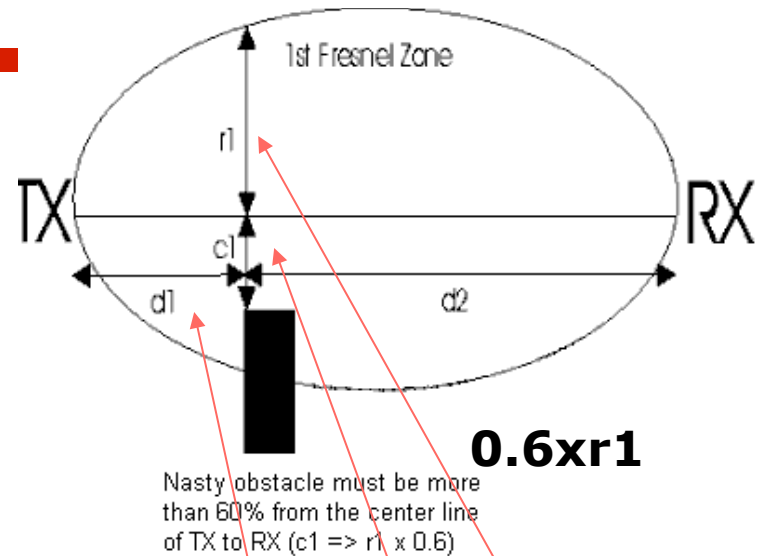
$$v = 0.0424 \sqrt{\frac{2 \times 10000 \times 2000}{(1/3) \times (10000 + 2000)}} = 4.24.$$

$$v = \alpha \sqrt{\frac{2d_1d_2}{(d_1 + d_2)\lambda}}$$

$$\alpha = \beta + \gamma$$

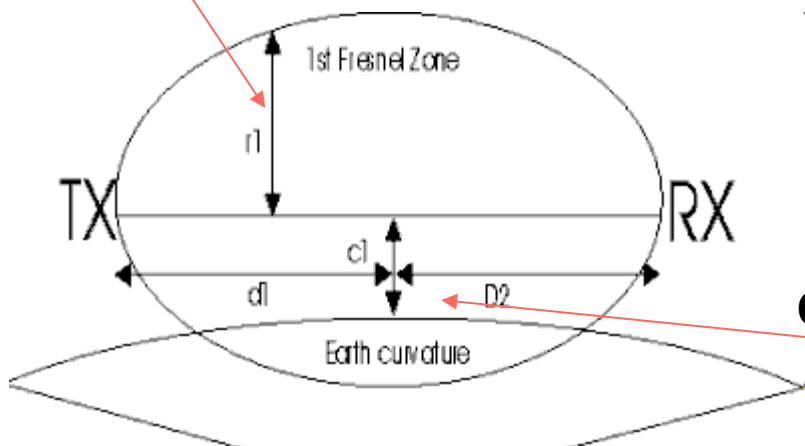


# Fresnel Effect



At mid-point (same height antenna)

$$r = 17.32 \sqrt{\frac{D}{4f}}$$



Total Link		Obstacle Distance		1st Fresnel Zone Radius	
10	Km	4	Km	17	m
OR		OR		56	ft
				at	at
				4	Km
	Miles		Miles	2.484	Miles
Frequency				60% No Obstacle Radius	
2400	MHz			10.2	m
				33	ft
Calculate				Earth Height (mid-point)	
				1.47	m
				4.821	ft

Read: <http://www.zytrax.com/tech/wireless/fresnel.htm>

# References

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  - ❑ Rappaport, Theodore S. *Wireless communications: principles and practice*. Vol. 2. New Jersey: Prentice Hall PTR, 1996, Chapter 3
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