## Practice 12-1

1a. about 0.66 1b. about 81 persons $\mathbf{1 c}$ c. about 0.05
1d. about 0.15
2a.
1e. about 0.37
Rolling Two Number Cubes

| Sum | 5 or less | Greater than 5 |
| :--- | :---: | :---: |
| Frequency | 10 | 26 |
| Probability | $\frac{10}{36}$ | $\frac{26}{36}$ |

2b.

| Rolling Two Number Cubes |  |  |
| :--- | :---: | :---: |
| Sum Prime Composite <br> Frequency 15 21 <br> Probability $\frac{15}{36}$ $\frac{21}{36}$ |  |  |

2c.

| Rolling Two Number Cubes |  |  |  |
| :--- | :---: | :---: | :---: |
| Numbers <br> showing | Only 1 <br> Cube <br> shows 2 | Both cubes <br> show same <br> number | Cubes show <br> different <br> numbers, <br> neither is 2 |
| Frequency | 10 | 6 | 20 |
| Probability | $\frac{10}{36}$ | $\frac{6}{36}$ | $\frac{20}{36}$ |

3a. Student Pizza Preferences

| Sausage | 56 |
| :--- | :--- |
| Cheese | 43 |
| Pepperoni | 39 |
| Supreme | 28 |
| Other pizza | 31 |
| No pizza | 19 |

3b. sausage: $25.9 \%$, cheese: 19.9\%, pepperoni: 18.1\%, supreme: $13.0 \%$, other pizza: $14.4 \%$, no pizza: $8.8 \% ; 100.1 \%$;
There is a rounding error of $0.1 \%$.
3 c .


3d.


3e. The sum of the probabilities of pizza categories in part $\mathbf{d}$ equals the probability of pizza in part $\mathbf{c}$. The overall total in both is $100.1 \%$ ( $0.1 \%$ rounding error).
4a. Check student's work. 4b. Check student's work.

## Practice 12-2

1a. 8.9\%
1b. $24.6 \%$
1c. $0.2 \%$
1d. 1.1\% 1e. 6.3\%
1f. 4.0\%
2a. 11.7\%
2b. 36.8\%
2c. 21.0\%
2d. $47.2 \%$
2e. 14.4\%
2f. 16.0\%
2g. $48.9 \%$
2h. 51.1\%
3. about $58.2 \%$ 4. $D=$ drizzle, $F=$ fog without drizzle, $C=$ cancelled game, $P=$ played game


4a. $45 \% \quad$ 4b. $6 \%$
5. $M=$ male, $F=$ female, $C=$ attend concert, $N=$ not attend concert


5a. about $47 \%$ 5b. about $25 \%$

## Practice 12-3

$\begin{array}{llllll}\text { 1. } 23 & \text { 2. } & 78 & 3.3 & \text { 4. } 110 & \text { 5. about } 93.3 ; 97 ; 97\end{array}$ 6. about 47.6; 48; 41, 49 7. about 2.6; 2.45; 2.4 8. about 15.7; 15.6; no mode
9. about 418.8; 423; no mode 10. about 1021.9; 1023; 1023
11. about $0.019 ; 0.019 ; 0.018,0.019$ 12. about $26.4 ; 27 ; 29$
13. about $44.8 ; 45 ; 42,45,49$ 14. about 48.1; 50.5; no mode
15. $18 ; 16.5 ; 15$ 16. about $1.5 ; 1.5 ; 1.3,1.5$ 17. about $9.2 ; 9$;
no mode 18. about 116.2;116; 114 19. about $4.29 ; 4.26 ; 4.25$
20. about 32.4 ; 34 ; no mode
21.

22.

23.

24.

25.174;188 26.346;368 27.94;98 28. $22 ; 86$

29a. about 47.4 29b. 47.9 29c. 50.8 29d. 44.1, 47.9, 50.8;


## Practice 12-4

1. $295.7 ; 47.4$ 2. $30.3 ; 3.2$ 3. 2.4; $0.1 \quad$ 4. 74.3;3.9
2. $66.8 ; 33.1$ 6. $8 ; 9.5 ; 4$ 7.189; about 109.6; 114.5
3. 15 ; about $531.4 ; 6.5 \quad$ 9. 1.7;2.3;1.05 10. $4 ; 46.7 ; 2$
4. $8 ; 100.5 ; 2.5 \quad 12.5 \quad 13.3 \quad 14 \mathrm{a}$. about 3.49

14b. about $0.55 \quad$ 14c. $1.7 \quad$ 14d. $2 ; 1 \quad$ 15a. 33 15b. 18.5
15c. about 88.2 15d. about 10.5 15e. 3 15f. 2 16. +0.375
17. +2.75

## Practice 12-5

1. It is most likely that Sample $C$ was largest since it has the smallest standard deviation, implying less variation than Samples A and B. 2. This sample is likely to contain a disproportionate number of readers. Selecting students in random classrooms would be more accurate. 3. The pizza restaurant sells to many different groups of people. The class might not like the same kinds of pizza as the population as a whole. The poll should be of class members. 4. The people eating in the restaurant probably are not indicative of the
population as a whole, either geographically or economically. The poll should be a random sample of the residents, possibly a random sample from each phone exchange to include people from all the different areas of the county. 5. This excludes the people who are working during the day. Contacting randomly selected people, either from the phone book or voter registration lists, would be more accurate. 6. This is fairly accurate usually. 7. about 44 8. about 2500 9. about 12,346 10. about 27,778 11. $53 \% ; \pm 16 \% ; 37 \%$ to $69 \%$
2. $72 \% ; \pm 4 \% ; 68 \%$ to $76 \% \quad 13.62 \% ; \pm 8 \% ; 54 \%$ to $70 \%$
3. $30 \% ; \pm 6 \% ; 24 \%$ to $36 \%$
4. $42 \% ; \pm 3 \% ; 39 \%$ to $45 \%$

## Practice 12-6

1. 


$\begin{array}{llll}\text { 1a. } 87.5 \% & \text { 1b. } 50 \% & \text { 1c. } 37.5 \% & \text { 2. the weather outcome on }\end{array}$ a given day, acceptable weather; Check students' work.
3. asking a person chosen at random; favoring an early curfew; Check students' work. 4. selecting a part; part is defective;
Check students' work. 5. about 1\% 6. about 0.002\% 7. about $25 \%$ 8. about $38 \%$


## Chapter 12 Answers (continued)

11. 


12.


13a. $68 \%$ 13b. $99 \%$ 13c. $97 \%$ 13d. $84 \%$ 14a. 18\%
14b. 6\% 14c. $56 \%$

## Practice 12-7

1. 53.3
2. 69.9
3. 36.7 4. 28.4
4. 


6.

7.

8.

9.

10.

11. about $34 \%$ 12. about $13.5 \%$ 13. about $2.5 \%$
$\begin{array}{ll}\text { 14. about } 68 \% & \text { 15. about } 16 \% \\ \text { 16. about } 50 \%\end{array}$
17a. about 6 students 17b. about 37 students
17c. about 156 students 18a. about 3 nails
18b. about 82 nails 18c. about 19 nails 19a. about $10 \%$
19b. about 5 bags 19c. about 40 bags

## Reteaching 12-1

1. | Amount of Rain | No. of years |
| :--- | :---: |$; \frac{3}{13}$
2. | Status | No. of Professors |
| :--- | :---: |$; \frac{1}{3}$

## Reteaching 12-2

1. $\frac{7}{18}$
2. $\frac{11}{18}$
3. $\frac{5}{9}$
4. $\frac{4}{9} \quad$ 5. $\frac{2}{9}$
5. $\frac{5}{18}$
6. $\frac{2}{5}$
7. $\frac{5}{8}$ 9. $\frac{5}{11}$

## Reteaching 12-3

1. about $883.8 ; 888 ; 888$ 2. about $0.9 ; 0.8 ; 0.5$
2. about $2116.9 ; 2068$; no mode 4. about $266.8 ; 289$; no mode
3. $27 ; 26.5 ; 26 \quad 6.15 ; 14 ; 21 \quad 7.3 .4 ; 3.3 ; 4.7 \quad$ 8. 6375; 6374; 6371
4. 546; 502; no mode 10. 84; 84; 81

## Reteaching 12-4

$\begin{array}{llll}\text { 1. about } 0.86 & \text { 2. about } 0.18 & \text { 3. about } 3.93 & \text { 4. about } 2.42\end{array}$
5. $\$ 72.98 \quad$ 6. $\$ 11.78 \quad 7.2 \quad 8.3 \quad 9.253 \mathrm{mi} ; 69.5 \mathrm{mi} \quad 10.5 ; 8$

## Reteaching 12-5

1. $\pm 2.8 \% ; 69.2 \%$ to $74.8 \%$
2. $\pm 4.2 \% ; 81.8 \%$ to $90.2 \%$
3. $\pm 5.6 \% ; 6.4 \%$ to $17.6 \%$
4. $\pm 2.6 \% ; 51.4 \%$ to $56.6 \%$
5. $\pm 1.9 \% ; 76.1 \%$ to $79.9 \%$

## Reteaching 12-6

1.7.6\% 2. $0.1 \%$
3. 2.1\%
4. 1.0\% 5. about 73.5\%
6. about 23.2\% 7. about 8.2\%

## Reteaching 12-7

1. 



About 25 light bulbs will not last 79 h .


About 4 students would still be working after 5 min .

## 3. <br> 

About 2 frogs will hop more than 72 in.

## Enrichment 12-1

1. 31 to 5 2. $\frac{5}{36}$ or about $13.9 \% \quad 3.1$ to 3 4. $\frac{9}{36}$ or $25 \%$
2. 3 to 2 6. 2 to 3 7. $\frac{3}{23}$ or about $13.0 \%$
3. $\frac{20}{23}$ or about $87.0 \% \quad 9.3$ to $7 \quad 10.3$ to $2 \quad 11.7$ to 1
4. 1 to 7 13. 1 to 3

## Enrichment 12-2

1. $\frac{47}{50} ; \frac{3}{50}$
2. $\frac{{ }_{47} \mathrm{C}_{2}}{{ }_{50} \mathrm{C}_{2}} ; \frac{{ }_{3} \mathrm{C}_{2}}{50}$
3. $\frac{15}{16} ; \frac{1}{16}$
4a. $\frac{{ }_{75} \mathrm{C}_{3}}{{ }_{80} \mathrm{C}_{3}}$
4b. $\frac{{ }_{55} \mathrm{C}_{2} \times{ }_{5} \mathrm{C}_{1}}{{ }_{80} \mathrm{C}_{3}}$ 4c. $\frac{{ }_{75} \mathrm{C}_{1} \times{ }_{5} \mathrm{C}_{2}}{{ }_{80} \mathrm{C}_{3}}$
4d. $\frac{{ }_{5} \mathrm{C}_{3}}{{ }_{80} \mathrm{C}_{3}}$
4e. $\frac{{ }_{75} \mathrm{C}_{2} \times{ }_{5} \mathrm{C}_{1}+{ }_{5} \mathrm{C}_{3}}{{ }_{80} \mathrm{C}_{3}}$
5a. $\frac{{ }_{45} \mathrm{C}_{3}}{{ }_{85} \mathrm{C}_{3}}$
5b. $\frac{{ }_{45} \mathrm{C}_{2} \times{ }_{40} \mathrm{C}_{1}}{{ }_{85} \mathrm{C}_{3}}$
5c. $\frac{{ }_{81} \mathrm{C}_{2} \times{ }_{4} \mathrm{C}_{1}}{{ }_{85} \mathrm{C}_{3}}$ 5d. $\frac{{ }_{38} \mathrm{C}_{2} \times{ }_{2} \mathrm{C}_{1}}{{ }_{85} \mathrm{C}_{3}}$
5e. $\frac{{ }_{43} \mathrm{C}_{1} \times{ }_{2} \mathrm{C}_{1} \times{ }_{2} \mathrm{C}_{1}}{{ }_{85} \mathrm{C}_{3}}$

## Enrichment 12-3

1. $f_{i} x_{i}$ 2. $\sum_{i=1}^{n} f_{i} x_{i}$ 3. $\bar{x}=\frac{\sum_{i=1}^{n} f_{i} x_{i}}{\sum_{i=1}^{n} f_{i}}$ 4. $f_{i}\left(x_{i}-m\right)$
2. $\sum_{i=1}^{n} f_{i}\left(x_{i}-m\right)$ 6. $y=\sum_{i=1}^{n} f_{i} x_{i}-\left(\sum_{i=1}^{n} f_{i}\right) m$ 7. linear
3. Any linear function with nonzero slope meets the $x$-axis at only one point.
4. $M=\frac{\sum_{i=1}^{n} f_{i} x_{i}}{\sum_{i=1}^{n} f_{i}}$ 10. mean 11. mean; sum; zero
5. 12
6. $\sum_{i=1}^{n} f_{i}\left(x_{i}-m\right)=1(15-12)+4(14-12)$
$+7(13-12)+13(12-12)+18(11-12)=0$

## Enrichment 12-4

1. $\bar{x}=\frac{\sum_{i=1}^{n} x_{i}}{n}$ 2. $\sigma^{2}=\frac{1}{n} \sum_{i=1}^{n}\left(x_{i}-\bar{x}\right)^{2}$
2. $\sigma^{2}=\frac{1}{n} \sum_{i=1}^{n}\left(x_{i}{ }^{2}-2 x_{i} \bar{x}+\bar{x}^{2}\right)$
3. $\sigma^{2}=\frac{1}{n}\left(\sum_{i=1}^{n} x_{i}{ }^{2}-2 \bar{x} \sum_{i=1}^{n} x_{i}+n \bar{x}^{2}\right)$
4. $\sigma^{2}=\frac{1}{n}\left[\sum_{i=1}^{n} x_{i}{ }^{2}-\frac{1}{n}\left(\sum_{i=1}^{n} x_{i}\right)^{2}\right]$
5. $\sigma=\sqrt{\frac{1}{n} \sum_{i=1}^{n} x_{i}{ }^{2}-\frac{1}{n^{2}}\left(\sum_{i=1}^{n} x_{i}\right)^{2}}$
6. $\sum_{i=1}^{n} f_{i} x_{i}$ 8. $\sum_{i=1}^{n} f_{i}\left(x_{i}\right)^{2} \quad$ 9. about 20.4 10. about 3.1

## Enrichment 12-5

1. $25 \% ; 25 \% \quad$ 2. $40 \% ; 40 \% \quad$ 3. Check student's work.
2. Check students' work. 5. about $32 \%$
3. Check students' work. 7. Check students' work.
4. Check students' work. 9. Check student's work.
5. about $12 \%$ 11. Check student's work.
6. Check students' work. 13. smaller intervals for the true proportion

## Enrichment 12-6

1. $\frac{5}{6} ; \frac{1}{6}$ 2. $\frac{4!}{2!2!}=6 ; N N 33, N 3 N 3, N 33 N, 33 N N, 3 N 3 N$,
$3 N N 3$ 3. $[P(N)]^{2}[P(3)]^{2} \quad$ 4. $\frac{25}{1296}$ 5. $\frac{25}{216} \quad 6.1-p$
2. $n-r$ 8. $p^{r}(1-p)^{n-r}$ 9. ${ }_{n} \mathrm{C}_{r}$ 10. ${ }_{n} \mathrm{C}_{r} p^{r}(1-p)^{n-r}$
3. about $0.0754 ;-0.4$ 12. about 0.0485 ; about $0.0108 ; 1 ; 2$
4. about 0.00003 ; about $0.0664 ; 4 ; 0$ 14. about 0.0354 ; about 5 fish

## Enrichment 12-7

1. that $\frac{3}{4}$ of data lie within 55 and 95 2.19 3. that $\frac{8}{9}$ of data lie within 45 and 105 4. 23 5. No; it says that at least 0 measurements lie within 65-85. 6. 52; 22 7. 27; between 8 and 96 8.36 9.32; between 0 and $118 \quad \mathbf{1 0 . 3 6}$

## Chapter Project

## Activity 1: Interviewing

Check students' work.
Activity 2: Analyzing
Check students' work.

## Activity 3: Creating

Check students' work.
Activity 4: Interviewing
Check students' work.

## Chapter 12 Answers (continued)

$\checkmark$ Checkpoint Quiz 1
1.

$\begin{array}{llllllll}\text { 2. } 46.4 \% & \text { 3. } \frac{2}{9} & \text { 4. } \frac{2}{3} & \text { 5. } \frac{7}{9} & \text { 6. } \frac{1}{3} & 7.7 ; 7 ; 7 & \text { 8. 10.5; } 10.5 ; \text { none }\end{array}$
9. Mean is the sum of data values in a data set divided by the number of data values. Median is the middle value or mean of the two middle values of a data set that has been arranged in increasing or decreasing order. Mode is the most frequently occurring value in a data set.

## Checkpoint Quiz 2

1. about $67.9 ; 10$; about 3.5 2. about $11.3 ; 12$; about 3.9
2. about $10.4 ; 8$; about 2.6
3. 130
5a. about 73\%
5b. about $\pm 4 \% \quad 5$ c. $69 \%$ to $77 \%$
4. about 278
5. $6.25 \%$
6. about 5.95\%
7. about 12.4\%

## Chapter Test, Form A

1 a .

1b. $\frac{18}{30}=60 \%$
2. $\frac{5}{11}$
3. $\frac{5}{22}$
4. $\frac{4}{25}$
5. $\frac{15}{22}$
6. D
7. Answers may vary. Sample: Arrange the data set into increasing or decreasing order. The median is the middle value. If there is an even number of values in the data set, the median is the mean of the two middle values.
8. $0.75 ; 0.6 ; 0.2,0.6$
9.

$\begin{array}{lllll}\text { 10. } 1.2 & 11.0 .9 & \text { 12. } 0.43 & \text { 13. } 0.3 ; 1.2 & \text { 14. Answers may vary. }\end{array}$ Sample: $\{5,12,15,17,20,22,40\},\{5,20,31,32,33,39,40\}$
15. 4 16. about $4.4 \%$ 17. about $81.0 \%$
18. $\pm 5 \% ; 13 \%$ to $23 \% \quad$ 19. $\pm 2 \% ; 39 \%$ to $43 \%$
20. $\pm 4 \% ; 2 \%$ to $10 \% \quad$ 21. $\pm 2 \% ; 95 \%$ to $99 \%$ 22. D
23. about $16 \%$ 24a. $11 \%$ 24b. $1 \%$ 25. about 68 students
26. about 5 students 27. about 100 students
28. about 163 students 29. 45.4

Chapter Test, Form B
1a.

1b. $\frac{6}{40}=15 \% \quad$ 2.D 3.H 4.A 5.F 6.B

9. 12 10. C 11. about 17.8\% 12. about $68.3 \%$
13. $\pm 5 \% ; 13 \%$ to $23 \%$ 14. $\pm 6 \% ; 0 \%$ to $12 \%$ 15. H
16. about $1 \%$
17. A
18. G
19. 46.7

## Alternative Assessment, Form C

## TASK 1 Scoring Guide:

a.


3 Graph is accurate and neatly done. Simulation is conducted, and explanation is sufficiently detailed to indicate a clear understanding of all aspects of probability distribution.
2 Graph is mostly accurate but contains minor errors. Simulation is conducted, but more detail is needed in the explanation.

1 Graph contains major errors. Simulation is incomplete, and explanation contains major errors that indicate lack of understanding of probability distribution.
0 Student makes no attempt, or no response is given.

## TASK 2 Scoring Guide:

3 Student conducts survey and records data correctly in the table. Probabilities are calculated correctly based on the data collected. Tree diagram is neatly drawn, and the data is accurate.

2 Student conducts survey and records data correctly in the table. Probabilities are calculated with only minor errors based on the data collected. Tree diagram is neatly drawn, with only minor mistakes in the data presented.
1 Student does not record all the data in the table. Probability calculations contain significant computational errors. Tree diagram is not constructed correctly, and data is inaccurate.
0 Student makes no attempt, or no response is given.

## TASK 3 Scoring Guide:

a. about $66.4^{\prime \prime} ; 67$ "; 62 ", 67 "
b. about $3.33^{\prime \prime}$
c.

d. No, there is no central grouping of data that falls off as you move away from the mean.
3 Student's calculations are correct. Graph is neatly drawn and accurately represents data. Student correctly identifies whether data represents a normal curve with an explanation that indicates a clear understanding of data spread.
2 Student's calculations contain only minor errors. Graph is neatly drawn with only minor errors in data. Student correctly identifies whether data represents a normal curve, but explanation could have more detail.
1 Student's calculations contain major errors. Graph could be neater, and data is not represented accurately. Student's explanation of normal curve is unclear and does not indicate an understanding of data spread.
0 Student makes no attempt, or no response is given.

## TASK 4 Scoring Guide:

3 Student selects an unbiased sample to conduct the survey. Explanation is sufficient to explain the choice. Margin of error is calculated correctly. Probabilities based on the percent from the sample are calculated correctly.

2 Student selects an unbiased sample to conduct the survey. Explanation could be more detailed to explain the choice. Margin of error is calculated with only minor errors. Probabilities based on the percent from the sample are calculated with only minor errors.

1 Student selects a more biased sample to conduct the survey. Explanation does not contain sufficient detail. Margin of error is calculated with only minor errors. Probabilities based on the percent from the sample are calculated incorrectly.
0 Student makes no attempt, or no response is given.

## Cumulative Review

1.A 2.G 3.A 4.F 5.C 6.J 7.B 8. H 9.A
10. G 11. A 12. G 13a. $-\frac{1}{3}$

13b. 4 14. 81.3; $81 ; 82$
15. $\pm \sqrt{5}$ 16. $4 ; 4,2$, or $0 ; \pm \frac{1}{2}, \pm 1, \pm 2, \pm 4, \pm 8$
$17.3-\sqrt{3}$ 18. $\frac{x^{2}}{36}+\frac{y^{2}}{64}=1$
19. Answers may vary. Sample: $\left\{\begin{array}{l}y=x+1 \\ y=2 x\end{array}\right.$;(1,2)
20. Check students' work.

