Circumference, Area, and Volume



ESSENTIAL QUESTION

How can you apply geometry concepts to solve real-world problems?



LESSON 9.1 Circumference

LESSON 9.2 Area of Circles

LESSON 9.3

Area of Composite Figures

LESSON 9.4

Solving Surface Area Problems

LESSON 9.5 Solving Volume Problems

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A 16-inch pizza has a diameter of 16 inches. You can use the diameter to find circumference and area of the pizza. You can also determine how much pizza in one slice of different sizes of pizzas.

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Reading Start-Up

Visualize Vocabulary

Use the 🗸 words to complete the graphic. You will put one word in each oval. Then write examples of formulas in each rectangle.



Understand Vocabulary

Match the term on the left to the correct expression on the right.

1	circumference	Α.	A line segment that passes through the center of a circle and has endpoints on the length of that segment.
2	diameter	В.	A line segment with one endpoint at the center of the circle and the other on the circle, or the length of that segment.
3.	radius	С.	The distance around a circle.

Active Reading

Four-Corner Fold Before beginning the module, create a four-corner fold to help you organize what you learn. As you study this module, note important ideas, such as vocabulary, properties, and formulas, on the flaps. Use one flap each for circumference, area, surface area, and volume. You can use your FoldNote later to study for tests and complete assignments.

Vocabulary

Review Words

- ✓ area (área) parallelogram (paralelogramo)
- perimeter (perímetro) prism (prisma) rectangle (rectángulo) square (cuadrado) trapezoid (trapecio) triangle (triángulo)
- ✓ volume (volumen)

Preview Words

circumference (circunferencia) composite figure (figura compuesta) diameter (diámetro) radius (radio)

Are YOU Ready?

Complete these exercises to review skills you will need for this module.



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Personal

Multiply with Fractions and Decimals

EXAMPLE	7.3 <u>× 2.4</u> 2 9 2	Multiply as you would with whole numbers. Count the total number of decimal places in the two factors.
	<u>+ 1 4 6</u> 1 7.5 2	Place the decimal point in the product so that there are the same number of digits after the decimal point.

Multiply.



Area of Squares, Rectangles, and Triangles



Find the area of each figure.

- 5. triangle with base 14 in. and height 10 in.
- 6. square with sides of 3.5 ft
- 7. rectangle with length $8\frac{1}{2}$ in. and width 6 in.
- 8. triangle with base 12.5 m and height 2.4 m

Are Ready? (cont'd)

Complete these exercises to review skills you will need for this module.

Multiply with Fractions and Decimals

9. Jon's car gets 35.5 miles per gallon in town. He used 0.3 gallon to drive to a meeting in town. How many miles did Jon drive?

10. Abby earns \$9.95 per hour doing landscape work. She worked 8.5 hours last week. How much did she earn? Explain.

Area of Squares, Rectangles, and Triangles

11. In a corner of his yard, Morgan has a garden shaped like a right triangle. The garden has the dimensions shown. What is the area of Morgan's garden? Show your work.



12. A rectangular sandbox is $10\frac{1}{2}$ feet long and 4 feet wide. What is the area of the sandbox? Show your work.

9.1 Circumference

Students will find and use the circumference of a circle.

7.4.9.1

ESSENTIAL QUESTION

How do you find and use the circumference of a circle?

EXPLORE ACTIVITY

Exploring Circumference

A circle is a set of points in a plane that are a fixed distance from the center.

A **radius** is a line segment with one endpoint at the center of the circle and the other endpoint on the circle. The length of a radius is called the radius of the circle.

A **diameter** of a circle is a line segment that passes through the center of the circle and whose endpoints lie on the circle. The length of the diameter is twice the length of the radius. The length of a diameter is called the diameter of the circle.

The **circumference** of a circle is the distance around the circle.

A Use a measuring tape to find the circumference of five circular objects. Then measure the distance across each item to find its diameter. Record the measurements of each object in the table below.

Object	Circumference C	Diameter d	C d

B Divide the circumference of each object by its diameter. Record your answer, rounded to the nearest hundredth, in the table above.

Reflect

1. Make a Conjecture Describe what you notice about the ratio $\frac{C}{d}$ in your table.





Finding Circumference

The ratio of the circumference to the diameter $\frac{C}{d}$ is the same for all circles. This ratio is called π or *pi*, and you can approximate it as 3.14 or as $\frac{22}{7}$. You can use π to find a formula for circumference.

For any circle, $\frac{C}{d} = \pi$. Solve the equation for C to give an equation for the circumference of a circle in terms of the diameter.

$\frac{C}{d} = \pi$	The ratio of the circumference to the diameter is $\pi.$
$\frac{C}{d} \times d = \pi \times d$	Multiply both sides by d.
$C = \pi d$	Simplify.

The diameter of a circle is twice the radius. You can use the equation $C = \pi d$ to find a formula for the circumference C in terms of the radius r.

$$C = \pi d = \pi(2r) = 2\pi r$$

The two equivalent formulas for circumference are $C = \pi d$ and $C = 2\pi r$.

Real **EXAMPLE 1** lorl

An irrigation sprinkler waters a circular region with a radius of 14 feet. Find the circumference of the region watered by the sprinkler. Use $\frac{22}{7}$ for π .

Use the formula.

$$C = 2\pi r$$

 $C = 2\pi (14)$
The radius is 14 feet.
 $C = 2\pi (14)$
Substitute 14 for

$$C \approx 2\left(\frac{22}{7}\right)$$
(14) Substitute $\frac{22}{7}$ for π .

Substitute 14 for r.

 $C \approx 88$ Multiply.

The circumference of the region watered by the sprinkler is about 88 feet.

Reflect

2. Analyze Relationships When is it logical to use $\frac{22}{7}$ instead of 3.14 for π ?



YOUR TURN

3. Find the circumference of the circle to the nearest hundredth.



Using Circumference

Given the circumference of a circle, you can use the appropriate circumference formula to find the radius or the diameter of the circle. You can use that information to solve problems.

EXAMPLE 2

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A circular pond has a circumference of 628 feet. A model boat is moving directly across the pond, along a radius, at a rate of 5 feet per second. How long does it take the boat to get from the edge of the pond to the center?



Lesson 9.1 **267**

Online Assessment and Intervention

Guided Practice



Class

Personal **9.1** Independent Practice **Math Trainer** Online Assessment and my.hrw.com Intervention 18. Multistep Randy's circular garden has a For 11–13, find the circumference of each circle. Use 3.14 or $\frac{22}{7}$ for π . Round to the radius of 1.5 feet. He wants to enclose the nearest hundredth, if necessary. garden with edging that costs \$0.75 per foot. About how much will the edging 11. cost? Explain. 5.9 ft 19. Represent Real-World Problems The 12. Ferris wheel shown makes 12 revolutions 56 cm per ride. How far would someone travel during one ride? 13. diameter 63 fee 35 in. 14. In Exercises 11–13, for which problems did you use $\frac{22}{7}$ for π ? Explain your choice. **20.** The diameter of a bicycle wheel is 2 feet. About how many revolutions does the wheel make to travel 2 kilometers? Explain. Hint: 1 km \approx 3,280 ft **15.** A circular fountain has a radius of 9.4 feet. Find its diameter and circumference to the nearest tenth. **21.** Multistep A map of a public park shows a circular pond. There is a bridge along a **16.** Find the radius and circumference of a CD diameter of the pond that is 0.25 mi long. with a diameter of 4.75 inches. You walk across the bridge, while your friend walks halfway around the pond to meet you at the other side of the bridge. **17.** A dartboard has a diameter of 18 inches. How much farther does your friend walk?

What are its radius and circumference?

22. Architecture The Capitol Rotunda connects the House and the Senate sides of the U.S. Capitol. Complete the table. Round your answers to the nearest foot.

Capitol Rotunda Dimensions		
Height	180 ft	
Circumference	301.5 ft	
Radius		
Diameter		

FOCUS ON HIGHER ORDER THINKING

- **23. Multistep** A museum groundskeeper is creating a semicircular statuary garden with a diameter of 30 feet. There will be a fence around the garden. The fencing costs \$9.25 per linear foot. About how much will the fencing cost altogether?
- **24.** Critical Thinking Sam is placing rope lights around the edge of a circular patio with a diameter of 18 feet. The lights come in lengths of 54 inches. How many strands of lights does he need to surround the patio edge?
- **25. Represent Real-World Problems** A circular path 2 feet wide has an inner diameter of 150 feet. How much farther is it around the outer edge of the path than around the inner edge?
- **26.** Critique Reasoning A gear on a bicycle has the shape of a circle. One gear has a diameter of 4 inches, and a smaller one has a diameter of 2 inches. Justin says that the circumference of the larger gear is 2 inches more than the circumference of the smaller gear. Do you agree? Explain your answer.

27. Persevere in Problem Solving Consider two circular swimming pools. Pool A has a radius of 12 feet, and Pool B has a diameter of 7.5 meters. Which pool has a greater circumference? How much greater? Justify your answers. Work Area

9.2 Area of Circles

7.4.9.2 Students will find the area of a circle.

ESSENTIAL QUESTION

How do you find the area of a circle?

EXPLORE ACTIVITY 1

Exploring Area of Circles

You can use what you know about circles and π to help find the formula for the area of a circle.

STEP 1

Use a compass to draw a circle and cut it out.



STEP 3

Fold the circle three times as shown to get equal wedges.

Unfold and shade one-half of the circle.



Cut out the wedges, and fit the pieces together to form a figure that looks like a parallelogram.



The base and height of the parallelogram relate to the parts of the circle.



 $A = \pi$

a parallelogram?



Write using an exponent.



4. A circular pool has a radius of 10 feet. What is the area of the *surface* of the water in the pool? Use 3.14 for π .

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EXPLORE ACTIVITY 2

Finding the Relationship between Circumference and Area

You can use what you know about circumference and area of circles to find a relationship between them.

Find the relationship between the circumference and area of a circle.





Solve for C^2 .

The circumference of the circle squared is equal to

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EXPLORE ACTIVITY 2 (cont'd)

Reflect

5. Does this formula work for a circle with a radius of 3 inches? Show your work.

Guided Practice



9.2 Independent Practice

Name

- **12.** The most popular pizza at Pavone's Pizza is the 10-inch personal pizza with one topping. What is the area of a pizza with a diameter of 10 inches? Round your answer to the nearest hundredth.
- **13.** A hubcap has a radius of 16 centimeters. What is the area of the hubcap? Round your answer to the nearest hundredth.

l6 cm

- **14.** A stained glass window is shaped like a semicircle. The bottom edge of the window is 36 inches long. What is the area of the stained glass window? Round your answer to the nearest hundredth.
- **15.** Analyze Relationships The point (3, 0) lies on a circle with the center at the origin. What is the area of the circle to the nearest hundredth?
- **16. Multistep** A radio station broadcasts a signal over an area with a radius of 50 miles. The station can relay the signal and broadcast over an area with a radius of 75 miles. How much greater is the area of the broadcast region when the signal is relayed? Round your answer to the nearest square mile.
- **19.** Analyze Relationships A bakery offers a small circular cake with a diameter of 8 inches. It also offers a large circular cake with a diameter of 24 inches. Does the top of the large cake have three times the area of that of the small cake? If not, how much greater is its area? Explain.







- 17. Multistep The sides of a square field are 12 meters. A sprinkler in the center of the field sprays a circular area with a diameter that corresponds to a side of the field. How much of the field is **not** reached by the sprinkler? Round your answer to the nearest hundredth.
- **18.** Justify Reasoning A small silver dollar pancake served at a restaurant has a circumference of 2π inches. A regular pancake has a circumference of 4π inches. Is the area of the regular pancake twice the area of the silver dollar pancake? Explain.

Class_

___ Date

20. Communicate Mathematical Ideas You can use the formula $A = \frac{C^2}{4\pi}$ to find the area of a circle given the circumference. Describe another way to find the area of a circle when given the circumference.

21. Draw Conclusions Mark wants to order a is the better deal? Explain.	Draw Conclusions Mark wants to order a pizza. Which	Donnie's Pizza Palace			
	is the better deal? Explain.	Diameter (in.)	12	18	
		Cost (\$)	10	20	
22.	 Multistep A bear was seen near a campground. Searcher dispatched to the region to find the bear. a. Assume the bear can walk in any direction at a rate of hour. Suppose the bear was last seen 4 hours ago. How must the searchers cover? Use 3.14 for a Pound your 	s were 2 miles per w large an area			
	nearest square mile.				
	b. What If? How much additional area would the searchers have to				
	cover if the bear were last seen 5 hours ago?				
H. 23.	FOCUS ON HIGHER ORDER THINKING Analyze Relationships Two circles have the same radius. combined area of the two circles the same as the area of a twice the radius? Explain.	ls the circle with		Work Area	
24.	Look for a Pattern How does the area of a circle change multiplied by a factor of <i>n</i> , where <i>n</i> is a whole number?	if the radius is			
25.	Represent Real World Problems The bull's-eye on a targ diameter of 3 inches. The whole target has a diameter of 1 part of the whole target is the bull's-eye? Explain.	et has a 5 inches. What			

1 ES	 Area of Composite Figures 	7.4.9.3 Students will find the area of composite figures.
ES	SENTIAL QUESTION How do you find the area of composite fig	ures?
EXP	LORE ACTIVITY Real	
Exp Aaron v irregula represe	Noring Areas of Composite Figures was plotting the shape of his garden on grid paper. While it was an ar shape, it was perfect for his yard. Each square on the grid ents 1 square meter.	
A	Describe one way you can find the area of this garden.	
B C	The area of the garden is square meters. Compare your results with other students. What other methods were used to find the area?	
D	How does the area you found compare with the area found using different methods?	
Refle 1.	ct Use dotted lines to show two different ways Aaron's garden could be divided up into simple geometric figures.	



Finding the Area of a Composite Figure

A composite figure is made up of simple geometric shapes. To find the area of a composite figure or other irregular-shaped figure, divide it into simple, nonoverlapping figures. Find the area of each simpler figure, and then add the areas together to find the total area of the composite figure.

Use the chart below to review some common area formulas.

Shape	Area Formula
triangle	$A = \frac{1}{2}bh$
square	$A = s^2$
rectangle	$A = \ell w$
parallelogram	A = bh
trapezoid	$A = \frac{1}{2}h(b_1 + b_2)$

EXAMPLE 1 (Red)

Find the area of the figure.





Using Area to Solve Problems

EXAMPLE 2

A banquet room is being carpeted. A floor plan of the room is shown at right. Each unit represents 1 yard. The carpet costs \$23.50 per square yard. How much will it cost to carpet the room?





Math Talk

Mathematical Processes Describe how you can estimate the cost to

carpet the room.

Separate the composite figure into simpler shapes as shown by the dashed lines: a parallelogram, a rectangle, and a triangle.

Find the area of the simpler figures. Count units to find the dimensions.

Parallelogram	Rectangle	Triangle
A = bh	$A = \ell w$	$A = \frac{1}{2}bh$
$A = 4 \cdot 2$	$A = 6 \cdot 4$	$A = \frac{1}{2}(1)(2)$
$A = 8 \text{ yd}^2$	$A = 24 \text{ yd}^2$	$A = 1 \text{ yd}^2$
Find the area of the c	composite figure.	

STEP 3

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STEP 1

STEP 2

A = 8 + 24 + 1 = 33 square yards

STEP 4 Calculate the cost to carpet the room.

Area \cdot Cost per yard = Total cost

$$33 \cdot $23.50 = $775.50$$

The cost to carpet the banquet room is \$775.50.





4. A window is being replaced with tinted glass. The plan at the right shows the design of the window. Each unit length represents 1 foot. The glass costs \$28 per square foot. How much will it cost to replace the glass? Use 3.14 for π .



Guided Practice



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9.3 Independent Practice

- **5.** A banner is made of a square and a semicircle. The square has side lengths of 26 inches. One side of the square is also the diameter of the semicircle. What is the total area of the banner? Use 3.14 for π .
- **6. Multistep** Erin wants to carpet the floor of her closet. A floor plan of the closet is shown.



- a. How much carpet does Erin need?
- **b.** The carpet Erin has chosen costs \$2.50 per square foot. How much will it cost her to carpet the floor?
- 7. Multiple Representations Hexagon ABCDEF has vertices A(-2, 4), B(0, 4), C(2, 1), D(5, 1), E(5, -2), and F(-2, -2). Sketch the figure on a coordinate plane. What is the area of the hexagon?





Date.

8. A field is shaped like the figure shown.What is the area of the field? Use 3.14 for π.



- **9.** A bookmark is shaped like a rectangle with a semicircle attached at both ends. The rectangle is 12 cm long and 4 cm wide. The diameter of each semicircle is the width of the rectangle. What is the area of the bookmark? Use 3.14 for π .
- **10. Multistep** Alex is making 12 pennants for the school fair. The pattern he is using to make the pennants is shown in the figure. The fabric for the pennants costs \$1.25 per square foot. How much will it cost Alex to make 12 pennants?



11. Reasoning A composite figure is formed by combining a square and a triangle. Its total area is 32.5 ft². The area of the triangle is 7.5 ft². What is the length of each side of the square? Explain.

Class_



12. Represent Real-World Problems Christina plotted the shape of her garden on graph paper. She estimates that she will get about 15 carrots from each square unit. She plans to use the entire garden for carrots. About how many carrots can she expect to grow? Explain.

HOT



13. Analyze Relationships The figure shown is made up of a triangle and a square. The perimeter of the figure is 56 inches. What is the area of the figure? Explain.



14. Critical Thinking The pattern for a scarf is shown at right. What is the area of the scarf? Use 3.14 for π .



15. Persevere in Problem Solving The design for the palladium window shown includes a semicircular shape at the top. The bottom is formed by squares of equal size. A shade for the window will extend 4 inches beyond the perimeter of the window, shown by the dashed line around the window. Each square in the window has an area of 100 in².



- **a.** What is the area of the window? Use 3.14 for π .
- **b.** What is the area of the shade? Round your answer to the nearest whole number.

Solving Surface Area 9.4 Problems

Students will find the surface area of a figure made up of cubes and prisms.

7.4.9.4

ESSENTIAL QUESTION

How can you find the surface area of a figure made up of cubes and prisms?

EXPLORE ACTIVITY

Modeling Surface Area of a Prism

The surface area of a three-dimensional figure is the sum of the areas of all its surfaces. You know how to use the net of a figure to find its surface area. Now you will discover a formula that you can use.



A The lateral area *L* of a prism is the area of all faces except the bases.

 $L = 2(___) + 2(___) = __$

B The area *B* of each base is _____.

C The surface area S of the prism is the sum of the lateral area L and the

total area of the bases, or _____.

Reflect

- 1. Analyze Relationships Use the net above to answer this question: How does the product of the perimeter *P* of the base of the prism and the height *h* of the prism compare to the lateral area *L*?
- **2.** Critical Thinking How can you express the surface area *S* of the prism in terms of *P*, *h*, and *B*? Use your answer to Question 1.



Finding the Surface Area of a Prism

Given a prism's dimensions, you can use a formula to find the surface area.

Surface Area of a Prism

The surface area S of a prism with base perimeter *P*, height *h*, and base area *B* is S = Ph + 2B.

My Notes

Erin is making a jewelry box of wood in the shape of a rectangular prism. The jewelry box will have the dimensions shown. She plans to spray paint the exterior of the box. How many square inches will she have to paint?

solve the problem.



STEP 2

STEP 1

Identify a base, and find its area and perimeter.

Make a sketch of the box. Drawing a

diagram helps you understand and

Any pair of opposite faces can be the bases. For example, you can choose the bottom and top of the box as the bases.

$B = \ell \times w$	P = 2(12) + 2(15)
$=$ 12 \times 15	= 24 + 30
= 180 square inches	= 54 inches

STEP 3

Identify the height, and find the surface area.

The height h of the prism is 6 inches. Use the formula to find the surface area.

S = Ph + 2B

S = 54(6) + 2(180) = 684 square inches

Erin will have to spray paint 684 square inches of wood.

YOUR TURN

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Math

Mathematical Processes How can you express the

formula for the surface area S of a rectangular prism in

terms of its dimensions *l*, *w*, and *h*?

3. A brand of uncooked spaghetti comes in a box that is a rectangular prism with a length of 9 inches, a width of 2 inches, and a height of $1\frac{1}{2}$ inches.

What is the surface area of the box? _____

Finding the Surface Area of a Composite Solid

A composite solid is made up of two or more solid figures. To find the surface area of a composite solid, find the surface area of each figure. Subtract any area not on the surface.

8 cm

30 cm

EXAMPLE 2 Problem

Daniel built the birdhouse shown. What was the surface area of the birdhouse before the hole was drilled?

Analyze Information

Identify the important information.

- The top is a triangular prism with h = 24 cm. The base is a triangle with height 8 cm and base 30 cm.
- The bottom is a rectangular prism with *h* = 18 cm. The base is a 30 cm by 24 cm rectangle.
- One face of each prism is not on the surface of the figure.

Formulate a Plan

Find the surface area of each prism.

Add the surface areas. Subtract the areas of the parts not on the surface.

Solve

Find the surface area of the triangular prism.

Perimeter = 17 + 17 + 30 = 64 cm; Base area = $\frac{1}{2}$ (30)(8) = 120 cm²

Surface area = Ph + 2B

= 64(24) + 2(120) = 1,776 cm²

Find the surface area of the rectangular prism.

Perimeter = 2(30) + 2(24) = 108 cm; Base area = 30(24) = 720 cm²

Surface area = Ph + 2B

= 108(18) + 2(720) = 3,384 cm²

Add. Then subtract the areas of the parts not on the surface.

Surface area = $1,776 + 3,384 - 2(720) = 3,720 \text{ cm}^2$

The surface area before the hole was drilled was 3,720 cm².

Justify and Evaluate

You can check your work by using a net to find the surface areas.

Math Talk Mathematical Processes

How could you find the surface area by letting the front and back of the prism be the bases?

Lesson 9.4 285



17 cm

18 cm

, 24 cm







4. Dara is building a plant stand. She wants to stain the plant stand, except for the bottom of the larger prism. Find the surface area of the part of the plant

stand she will stain.



Guided Practice



Class

9.4 Independent Practice

4. Carla is wrapping a present in the box shown. How much wrapping paper does she need, not including overlap?



 Dmitri wants to cover the top and sides of the box shown with glass tiles that are 5 mm square. How many tiles does he need?



6. Shera is building a cabinet. She is making wooden braces for the corners of the cabinet. Find the surface area of each brace.



7. The doghouse shown has a floor, but no windows. Find the total surface area of the doghouse, including the door.





Eddie built the ramp shown to train his puppy to do tricks. Use the figure for 8–9.



8. Analyze Relationships Describe two ways to find the surface area of the ramp.

9. What is the surface area of the ramp?

Marco and Elaine are building a stand like the one shown to display trophies. Use the figure for 10–11.



- **10.** What is the surface area of the stand?
- 11. Critique Reasoning Marco and Elaine want to paint the entire stand silver. A can of paint covers 25 square feet and costs \$6.79. They set aside \$15 for paint. Is that enough? Explain.

12. Henry wants to cover the box shown with paper without any overlap. How many square centimeters will be covered with paper?



13. What If? Suppose the length and width of the box in Exercise 12 double. Does the surface area *S* double? Explain.



FOCUS ON HIGHER ORDER THINKING

14. Persevere in Problem Solving Enya is building a storage cupboard in the shape of a rectangular prism. The rectangular prism has a square base with side lengths of 2.5 feet and a height of 3.5 feet. Compare the amount of paint she would use to paint all but the bottom surface of the prism to the amount she would use to paint the entire prism.

15. Interpret the Answer The oatmeal box shown is shaped like a cylinder. Use a net to find the surface area *S* of the oatmeal box to the nearest tenth. Then find the number of square feet of cardboard needed for 1,500 oatmeal boxes. Round your answer to the nearest whole number.



16. Analyze Relationships A prism is made of centimeter cubes. How can you find the surface area of the prism in Figure 1 without using a net or a formula? How does the surface area change in Figures 2, 3, and 4? Explain.









Work Area

Solving Volume 9.5 Problems

7.4.9.5

Students will find the volume of a figure made of cubes and prisms.





Volume of a Trapezoidal Prism

Prisms are named for the polygons that form their bases. In this lesson, you will focus on prisms whose bases are either triangles or quadrilaterals other than squares and rectangles.

EXAMPLE 2

Cherise is setting up her tent. Her tent is in the shape of a trapezoidal prism. How many cubic feet of space are in her tent?



STEP 1 Find the base area *B* of the trapezoidal prism.

Math Talk Mathematical Processes

Without calculating the volumes, how can you know whether Bradley's or Cherise's tent has a greater volume? $B = \frac{1}{2}(b_1 + b_2) h$ $= \frac{1}{2}(6 + 4)4$ $= \frac{1}{2}(10)4 = 20 \text{ ft}^2$ Find the volume of the prism.

V = BhVolume of a prism with base area B and height h= (20)(9)Substitute 20 for B and 9 for h. $= 180 \text{ ft}^3$

The volume of Cherise's tent is 180 ft³.

Reflect

ò

STEP 2

- **3.** Look for a Pattern How could you double the volume of the tent by doubling just one of its dimensions?
- **4.** What If? How would doubling *all* the dimensions of the prism affect the volume of the tent?



5. Find the volume of the prism.

12 cm 10 cm -8 cm

Volume of a Composite Solid

You can use the formula for the volume of a prism to find the volume of a composite figure that is made up of prisms.

EXAMPLE 3 Real



The volume of the aquarium is 74 ft³.

Reflect

6. What If? Find the volume of one of the large aquariums on either end using another pair of opposite sides as the bases. Do you still get the same volume? Explain.



7. The figure is composed of a rectangular prism and a triangular prism. Find the volume of the figure.







My Notes

Guided Practice

1. Find the volume of the triangular prism. (Example 1)



2. Find the volume of the trapezoidal prism. (Example 2)

$$B = \frac{1}{2}(b_1 + b_2)h = \frac{1}{2}(15 + 5)(3) = 30m$$

$$V = Bh = \left(\bigcirc \times \bigcirc \right) m \bigcirc = \bigcirc m^3$$

3. Find the volume of the composite figure. (Example 3)

Volume of rectangular prism = _____

Volume of triangular prism = _____

Volume of composite figure = _____

Find the volume of each figure. (Examples 2 and 3)

4. The figure shows a barn that Mr. Fowler is building for his farm.





5 ft

5 ft

5. The figure shows a container, in the shape of a trapezoidal prism, that Pete filled with sand.



ESSENTIAL QUESTION CHECK-IN

6. How do you find the volume of a composite solid formed by two or more prisms?

12.

 $B \approx 23.4 \text{ in}^2$

9.5 Independent Practice

- **7.** A trap for insects is in the shape of a triangular prism. The area of the base is 3.5 in² and the height of the prism is 5 in. What is the volume of this trap?
- **8.** Arletta built a cardboard ramp for her little brothers' toy cars. Identify the shape of the ramp. Then find its volume.
- **9.** Alex made a sketch for a homemade soccer goal he plans to build. The goal will be in the shape of a triangular prism. The legs of the right triangles at the sides of his goal measure 4 ft and 8 ft, and the opening along the front is 24 ft. How much space is contained within this goal?
- **10.** A gift box is in the shape of a trapezoidal prism with base lengths of 7 inches and 5 inches and a height of 4 inches. The height of the gift box is 8 inches. What is the volume of the gift box?
- **11.** Explain the Error A student wrote this statement: "A triangular prism has a height of 15 inches and a base area of 20 square inches. The volume of the prism is 300 square inches." Identify and correct the error.

Find the volume of each figure. Round to the nearest hundredth if necessary.

3 in.

3 in.

3 in. 3 in.

14. Multi-Step Josie has 260 cubic centimeters of candle wax. She wants to make a hexagonal prism candle with a base area of 21 square centimeters and a height of 8 centimeters. She also wants to make a triangular prism candle with a height of 14 centimeters. Can the base area of the triangular prism candle be 7 square centimeters? Explain.











Class



Date

15. A movie theater offers popcorn in two different containers for the same price. One container is a trapezoidal prism with a base area of 36 square inches and a height of 5 inches. The other container is a triangular prism with a base area of 32 square inches and a height of 6 inches. Which container is the better deal? Explain.



2.5 cm

6 cm



18. Analyze Relationships What effect would tripling all the dimensions of a triangular prism have on the volume of the prism? Explain your reasoning.

8.6 grams. Find the volume of the metal in the doorstop. Then find the mass of

the doorstop.

19. Persevere in Problem Solving Each of two trapezoidal prisms has a volume of 120 cubic centimeters. The prisms have no dimensions in common. Give possible dimensions for each prism.

Work Area



9.1, 9.2 Circumference and Area of Circles

Find the circumference and area of each circle. Use 3.14 for $\pi.$ Round to the nearest hundredth if necessary.



MODULE 9 MIXED REVIEW Assessment Readiness



Selected Response

1. What is the circumference of the circle?



- (A) 34.54 m
- **B** 69.08 m
- **(C)** 379.94 m
- **D** 1,519.76 m
- 2. What is the area of the circle?



(B) 47.1 m²

- C 176.625 m²
 D 706.5 m²
- 3. What is the area of the figure?



(B) 36 m²

- C 64.26 m²
 D 92.52 m²
- **4.** A one-year membership to a health club costs \$480. This includes a \$150 fee for new members that is paid when joining. Which equation represents the monthly cost *x* in dollars for a new member?
 - (A) 12x + 150 = 480
 - **B** $\frac{x}{12} + 150 = 480$
 - (C) 12x + 480 = 150
 - (D) $\frac{x}{12} + 480 = 150$

5. What is the volume of the prism?



- (A) 192 ft³
 (B) 48 ft³
 (D) 96 ft³
- 6. A school snack bar sells a mix of granola and raisins. The mix includes 2 pounds of granola for every 3 pounds of raisins. How many pounds of granola are needed for a mix that includes 24 pounds of raisins?
 - (A) 16 pounds (C) 48 pounds
 - (B) 36 pounds (D) 120 pounds
- **7.** Find the percent change from \$20 to \$25.
 - (A) 25% decrease (C) 20% decrease
 - (B) 25% increase (D) 20% increase

Mini-Task

8. Each dimension of the smaller prism is half the corresponding dimension of the larger prism.



- a. What is the surface area of the figure?
- **b.** What is the volume of the figure?