

Why Solve This? In Python?

- https://en.wikipedia.org/wiki/Collatz_conjecture
- We want to illustrate an indefinite loop
 - One of many mathematical sequences, but ...
- There's an XKCD comic about it!
 - Not everyone enjoys XKCD, but ...
- Mathematics is foundational in computer science, but
 - Not everyone enjoys logic/math puzzles, but ...

Developing and Reasoning about While Loops

- Don't know: *how many times* loop executes
 - *a priori* knowledge, we'll know afterward
- Do know: condition that should be true after loop
 - Its negation is the expression for `BOOL_CONDITION` (loop guard)

```
while BOOL_CONDITION:  
    LOOP_BODY  
    # modify variables, affect expression
```

History: From while to for loops

while loop (sum list)

```
lst = [4,1,8,9]  
s = 0  
i = 0  
while i < len(lst):  
    s += lst[i]  
    i += 1  
print(s)
```

for loop (sum list)

```
lst = [4,1,8,9]  
s = 0  
for n in lst:  
    s += n  
print(s)
```

Concrete Example: Collatz/Hailstone

- Don't know: *how many times* loop executes
 - some numbers: long sequences, others short
- Do know: condition that should be true after loop
 - Its negation is the expression for loop guard!
 - What is true after loop below finishes?

```
while value != 1:  
    loop body  
    # modify value somehow
```

Collatz Code

```
6 def hailstone(start, printing=False):
7     """..."""
14    steps = 0
15    current = start
16    while current != 1:
17        if printing:
18            print("{:3d}\t{:6d}".format(steps,current))
19        if current % 2 == 0:
20            current //= 2
21        else:
22            current = current * 3 + 1
23            steps += 1
24
25    if printing:
26        print("{:3d}\t{:6d}".format(steps,current))
27    return steps
```

What is new in this code? What does that new stuff do?

What is this code doing? What gets updated? Is the loop guaranteed to stop?

Collatz code

```
6 def hailstone(start, printing=False):
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Compsci 101 Pancakes, While loops, Parallel Lists Part 2 of 3

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February 25, 2021

```
while BOOL_CONDITION:
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    # modify variables, affect expression
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Collatz Code

```
6 def hailstone(start, printing=False):
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Collatz: New stuff

```
6 def hailstone(start, printing=False):
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```

Default value, if no argument

Syntax for nicer formatting

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Collatz: Guaranteed to stop?

```
6 def hailstone(start, printing=False):
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```

current influences the stopping condition

Since current is always changed, this should eventually stop

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Collatz Data – Average no. of steps

- How do we gather data for numbers $\leq 10,000$?
 - In general for numbers in range(low,high) ?
 - Call function, store result, store 10,000 results?
- We'd like counts[k] to be length of sequence for k
 - How do we allocate 10,000 list elements?
 - Like there is "hello" * 3
 - There is [0] * 10000

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Think: Analysis in Collatz.py

```
29 def analyze(limit):
30     counts = []
31     # max index into count is limit, but start at 1
32     for _ in range(limit+1):
33         counts.append(0)
34
35     for n in range(1, limit+1):
36         counts[n] = hailstone(n)
37
38     avg = sum(counts)/len(counts)-1 # ignore index 0
39     mx = max(counts)
40     dex = counts.index(mx)
41     print("average", avg)
42     print("max is %d at %d" % (mx, dex))
```

Why do both range calls have +1?

Why no printing when this is called?

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Analysis in Collatz.py

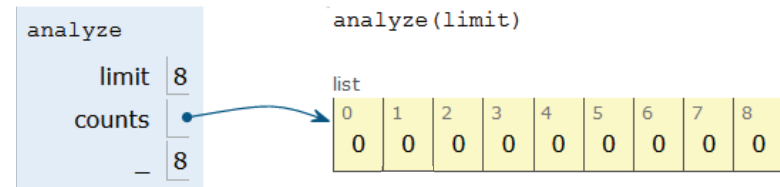
```

29 def analyze(limit):
30     counts = []
31     # max index into count is limit, but start at 1
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33         counts.append(0)
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35     for n in range(1, limit+1):
36         counts[n] = hailstone(n)
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38     avg = sum(counts)/len(counts)-1 # ignore index 0
39     mx = max(counts)
40     dex = counts.index(mx)
41     print("average", avg)
42     print("max is %d at %d" % (mx, dex))

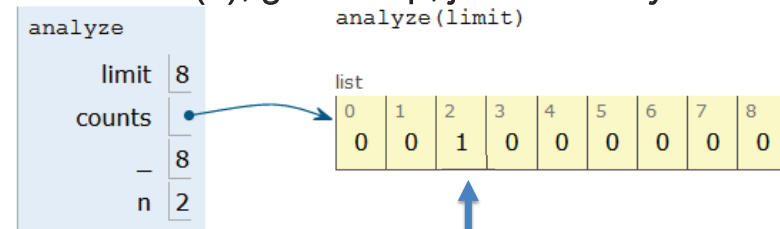
```

counts list when limit is 8?

- Counts is of size 8+1, we ignore slot 0

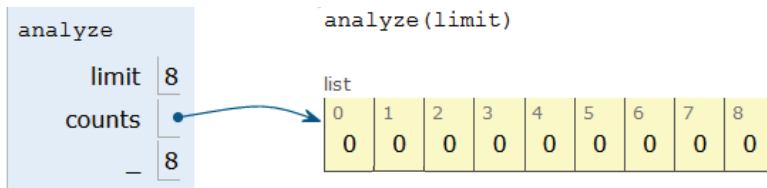


- hailstone(1), get 0
- hailstone(2), get 1 step, just divide by 2

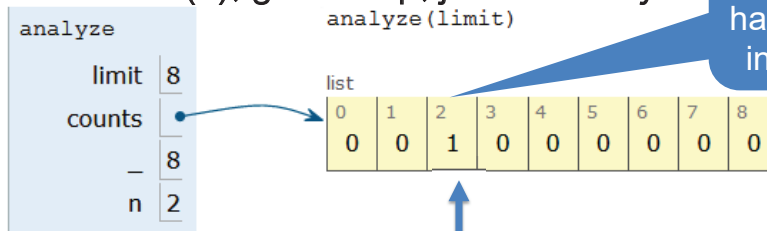


counts list when limit is 8?

- Counts is of size 8+1, we ignore slot 0



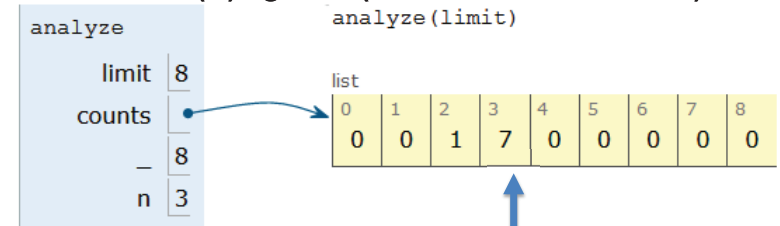
- hailstone(1), get 0
- hailstone(2), get 1 step, just divide by 2



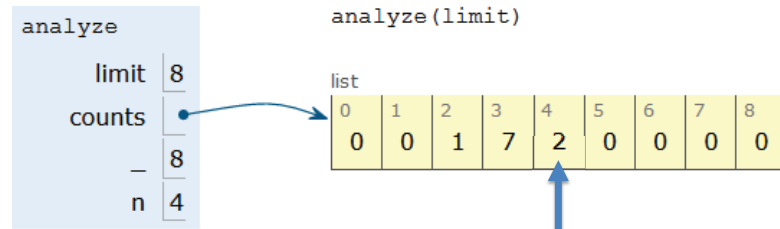
Store answer for hailstone(2) in index 2

counts list when limit is 8?

- hailstone(3), get 7 (10, 5, 16, 8, 4, 2, 1)



- hailstone(4), get 2



counts list when limit is 8?

- hailstone(3), get 7

analyze	
limit	8
counts	•
-	8
n	3

analyze(limit)	
list	0 1 2 3 4 5 6 7 8
	0 0 1 7 0 0 0 0 0

Store answer for hailstone(3) in index 3

- hailstone(4), get 2

analyze	
limit	8
counts	•
-	8
n	4

analyze(limit)	
list	0 1 2 3 4 5 6 7 8
	0 0 1 7 2 0 0 0 0

Store answer for hailstone(4) in index 4

counts list when limit is 8?

- hailstone(5), get 5 (16, 8, 4, 2, 1)

analyze	
limit	8
counts	•
-	8
n	5

analyze(limit)	
list	0 1 2 3 4 5 6 7 8
	0 0 1 7 2 5 0 0 0

Store answer for hailstone(5) in index 5

- And so on.....

- Hailstone(6) is 8, hailstone(7) is 16, hailstone(8) is 3

analyze	
limit	8
counts	•
-	8
n	8

analyze(limit)	
list	0 1 2 3 4 5 6 7 8
	0 0 1 7 2 5 8 16 3

Compsci 101 Pancakes, While loops, Parallel Lists Part 3 of 3

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```
while BOOL_CONDITION:
    LOOP_BODY
    # modify variables, affect expression
```

Parallel Lists

- Case Study: FileFrequency.py
- We'd like to analyze word occurrences
 - Google N-Gram, it's easy to do, but ...
 - What about occurrences of "cgat" in genome?
 - What about Rotten Tomatoes?
- This code is built using the tools that we have
 - In the future, learn of more efficient structures
- We'll use an API for opening files

High Level View

- We will use parallel lists to track data
 - Each word is stored in a list named **words**
 - Word's count is stored in a list named **counts**
 - # occurrences of **words[k]** is in **counts[k]**

```
["apple", "fox", "vacuum", "lime"]  
[5, 2, 25, 15]
```

- What happens when we read a word?

Read word "apple"?

High Level View

- We will use parallel lists to track data
 - Each word is stored in a list named **words**
 - Word's count is stored in a list named **counts**
 - # occurrences of **words[k]** is in **counts[k]**

```
["apple", "fox", "vacuum", "lime"]  
[6, 2, 25, 15]
```



- What happens when we read a word?

Read word "apple"?

High Level View

- We will use parallel lists to track data
 - Each word is stored in a list named **words**
 - Word's count is stored in a list named **counts**
 - # occurrences of **words[k]** is in **counts[k]**

```
["apple", "fox", "vacuum", "lime"]  
[6, 2, 25, 15]
```

- What happens when we read a word?

Read word "banana"?

High Level View

- We will use parallel lists to track data
 - Each word is stored in a list named **words**
 - Word's count is stored in a list named **counts**
 - # occurrences of **words[k]** is in **counts[k]**

```
["apple", "fox", "vacuum", "lime",  
"banana"]  
[6, 2, 25, 15]
```

Add into words

- What happens when we read a word?

Read word "banana"?

High Level View

- We will use parallel lists to track data
 - Each word is stored in a list named **words**
 - Word's count is stored in a list named **counts**
 - # occurrences of **words[k]** is in **counts[k]**

```
["apple", "fox", "vacuum", "lime",  
"banana"]  
[6, 2, 25, 15, 0]
```

Expand counts

- What happens when we read a word?

Read word "banana"?

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High Level View

- We will use parallel lists to track data
 - Each word is stored in a list named **words**
 - Word's count is stored in a list named **counts**
 - # occurrences of **words[k]** is in **counts[k]**

```
["apple", "fox", "vacuum", "lime",  
"banana"]  
[6, 2, 25, 15, 1]
```

Add one

- What happens when we read a word?

Read word "banana"?

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Pseudo-code for getFileData

- Let user choose a file to open
- Read each line of the file
 - Process each word on the line
 - If word never seen before? Add to words and counts
 - Update # occurrences using .index and location
- Think: What would we do for each color when doing step 5 (translate to code) of the 7 steps?

Step 3 of 7 steps:
Generalize

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Pseudo-code for getFileData

- Let user choose a file to open
- Read each line of the file
 - FOR LOOP
 - Process each word on the line
 - SPLIT, FOR LOOP
 - If word never seen before? Add to words and counts
 - IF STATEMENT, UPDATE LIST
 - Update # occurrences using .index and location
 - UPDATE LIST, USE INDEX FUNCTION

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Pseudo-code for getFileData

- Let user choose a file to open
 - SOME KIND OF CODE CHOOSES A FILE
- Read each line of the file
 - FOR LOOP
- Process each word on the line
 - SPLIT, FOR LOOP
- If word never seen before? Add to words and counts
 - IF STATEMENT, UPDATE LIST
- Update # occurrences using .index and location
 - UPDATE LIST, USE INDEX FUNCTION

From Pseudo to Code

```
30 for line in f:
31     data = line.strip().split()
32
33     for word in data:
34         word = word.lower()
35         if word not in words:
36             words.append(word)
37             counts.append(0)
38             location = words.index(word)
39             counts[location] += 1
```

Process line in file

Process word in line

Add if not seen before

Update count

What is guaranteed about words and counts?

Comparing Two Approaches

- Why do we have a loop in a loop?
 - Code mirrors structure:
 - file has lines, lines have words
- Notice:
 - .strip
 - .split
 - .lower
 - not in
 - .append
 - .index
 - +=

```
for line in f:
    data = line.strip().split()
    for word in data:
        word = word.lower()
        if word not in words:
            words.append(word)
            counts.append(0)
            location = words.index(word)
            counts[location] += 1
```

Outer loop

Inner loop

Comparing Two Approaches

- Why do we have only one loop?
 - Code mirrors structure, which is better?
 - File is a sequence of characters!!

```
for word in f.read().lower().split():
    if word not in words:
        words.append(word)
        counts.append(0)
    location = words.index(word)
    counts[location] += 1
```

Comparing Two Approaches

- Why do we have only one loop?
 - Code mirrors structure, which is better?
 - File is a sequence of characters!!

Same in
both

```
for word in f.read().lower().split():  
    if word not in words:  
        words.append(word)  
        counts.append(0)  
    location = words.index(word)  
    counts[location] += 1
```