## Computer Science S-111 Intensive Introduction to Computer Science

Harvard Summer School 2021 David G. Sullivan, Ph.D.

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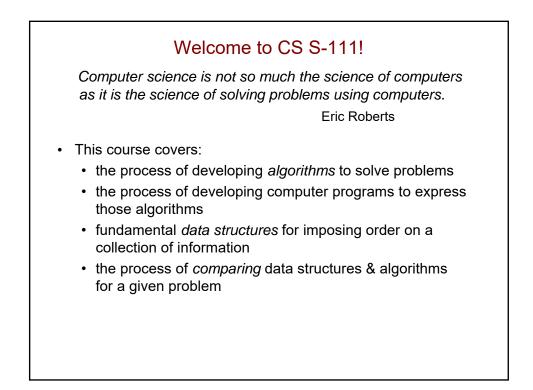
Unit 1, Part I

Intensive Introduction to Computer Science

Course Overview Programming in Scratch

Computer Science S-111 Harvard University

David G. Sullivan, Ph.D.



## **Computer Science and Programming**

- There are many different fields within CS, including:
  - software systems
  - computer architecture
  - networking
  - programming languages, compilers, etc.
  - theory
  - Al
- Experts in many of these fields don't do much programming!
- However, learning to program will help you to develop ways of thinking and solving problems used in all fields of CS.

A Rigorous Introduction     Intended for:	
<ul> <li>future concentrators who plan to take more advanced courses</li> <li>others who want a rigorous introduction</li> <li>no programming background required, but can also benefit people with prior background</li> </ul>	
<ul> <li>Allow for 20-30 hours of work per week</li> <li>start work early!</li> <li>come for help!</li> <li>don't fall behind!</li> </ul>	

## CS 111 Requirements

- · Lectures and sections
  - attendance at both is required
- Ten problem sets (40%)
  - part I = "written" problems
  - part II = "programming" problems
  - grad-credit students will have extra work on most assts.
- Four unit tests (25%)
  - given at the end of lecture (see the schedule)
- Final exam (35%)
  - Friday, August 6

Textbooks
<ul> <li>Required: The CSCI S-111 Coursepack</li> <li>contains all of the lecture notes</li> <li>print it and mark it up during lecture</li> </ul>
<ul> <li>Optional resource for the first half: Building Java Programs by Stuart Reges and Marty Stepp (Addison Wesley).</li> </ul>
<ul> <li>Optional resource for the second half: Data Structures &amp; Algorithms in Java, 2nd edition by Robert Lafore (SAMS Publishing).</li> </ul>

## **Course Staff**

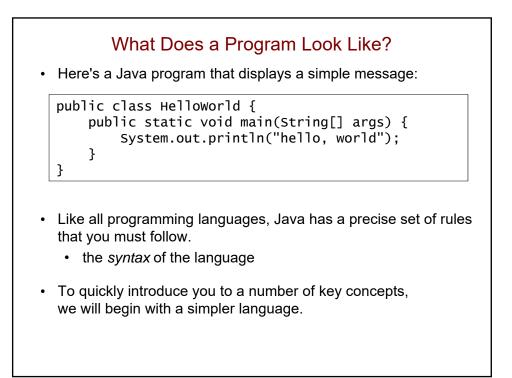
- Instructor: Dave Sullivan
- Teaching Assistant (TA): Ashby Hobart
- · See the course website for contact info. and office hours
- Piazza is your best bet for questions.
- For purely administrative questions: libs111@fas.harvard.edu
  - · will forward your email to the full course staff

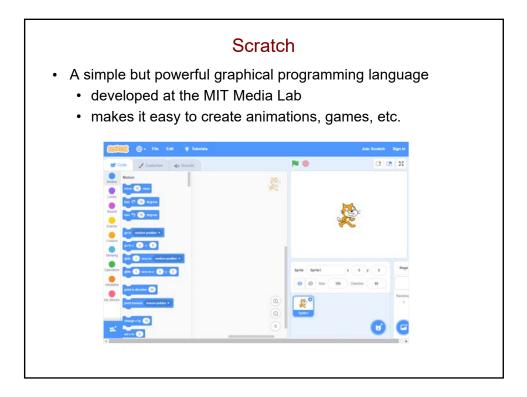
# Other Details of the Syllabus Schedule: note the due dates and test dates no lectures or sections on most Wednesdays exceptions: July 7 (July 5 is off), July 14 (July 16 is off), August 4 (August 5 is off) Policies: 10% penalty for submissions that are one day late please don't request an extension unless it's an emergency! grading Please read the syllabus carefully and make sure that you understand the policies and follow them carefully. Let us know if you have any questions.

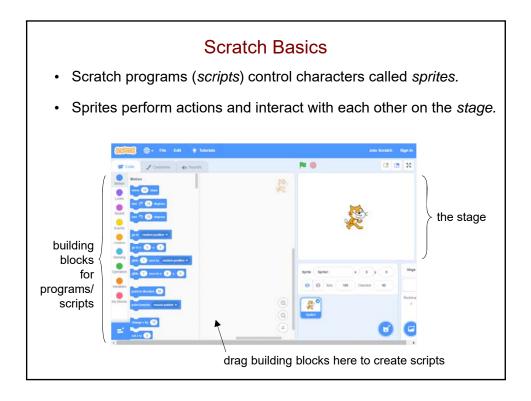
## Algorithms

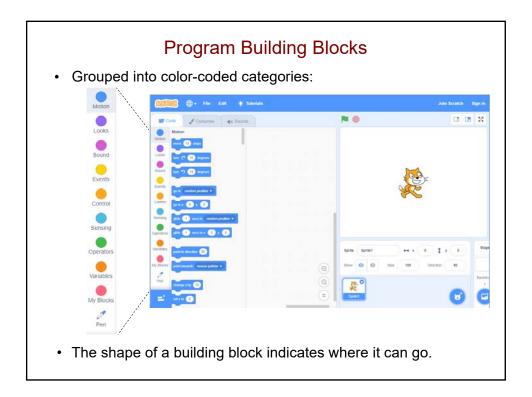
- In order to solve a problem using a computer, you need to come up with one or more *algorithms*.
- An algorithm is a step-by-step description of how to accomplish a task.
- An algorithm must be:
  - precise: specified in a clear and unambiguous way
  - effective: capable of being carried out

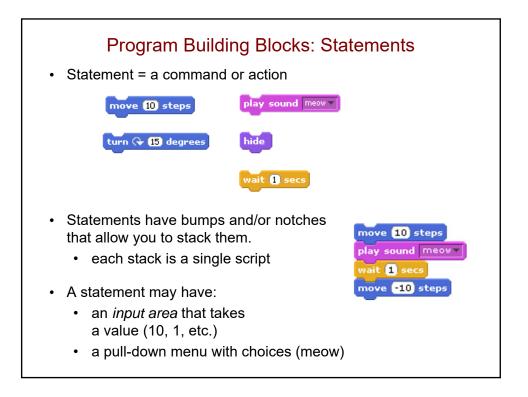
## Programming involves expressing an algorithm in a form that a computer can interpret. We will primarily be using the Java programming language. one of many possible languages The key concepts of the course transcend this language.

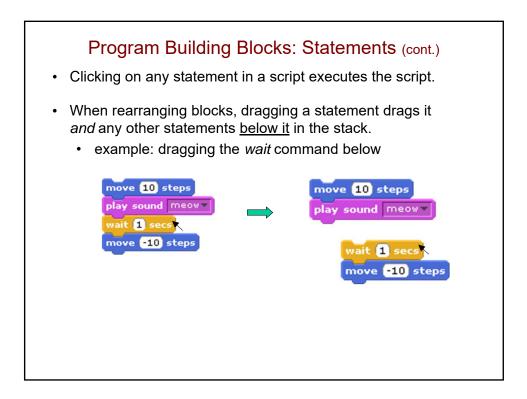


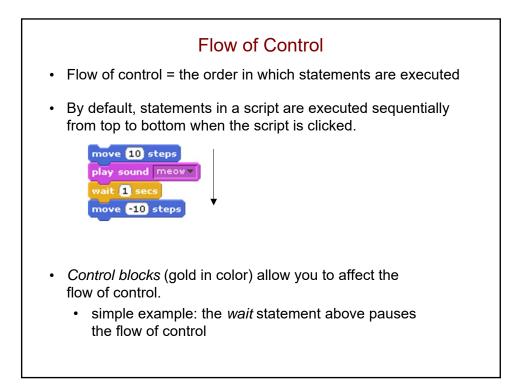


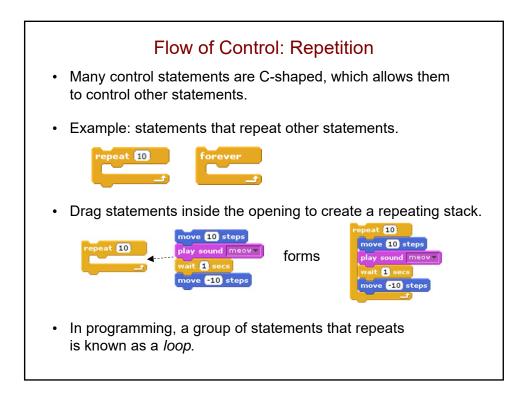


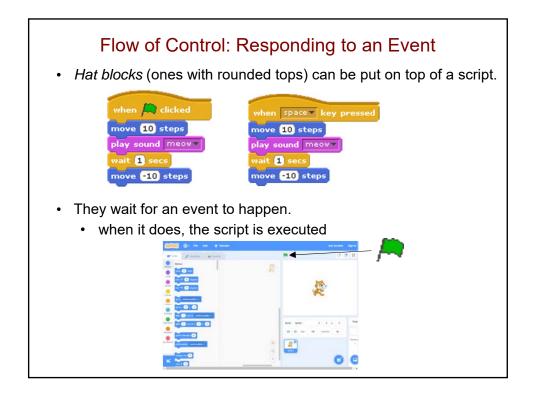


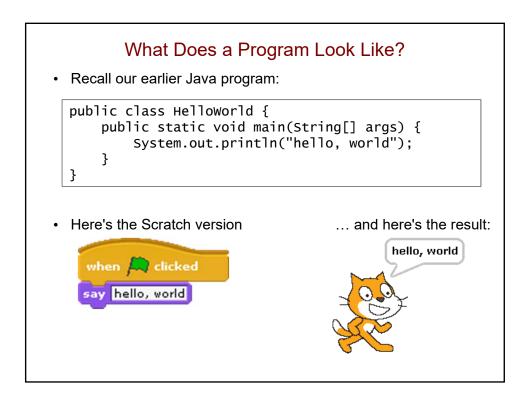


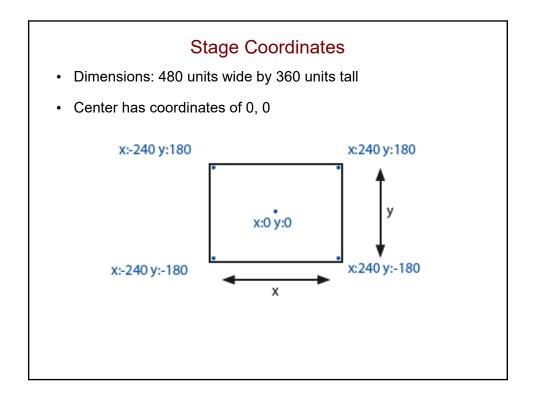


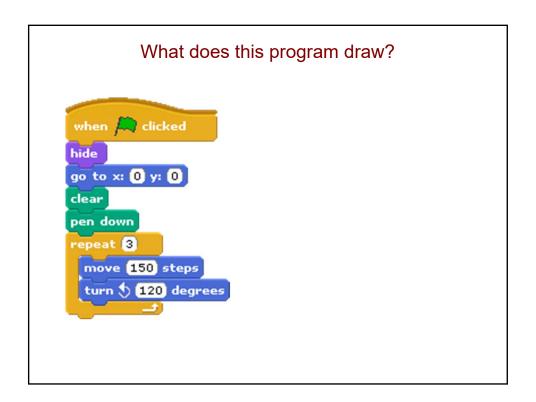


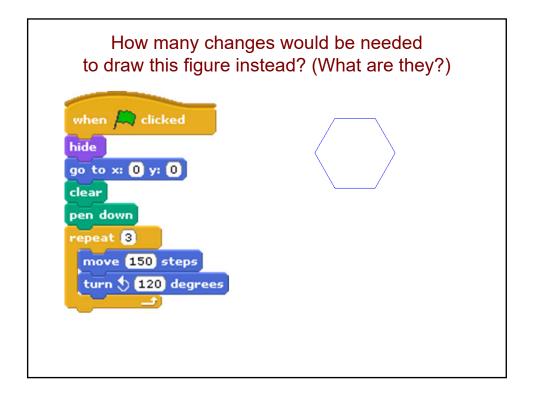


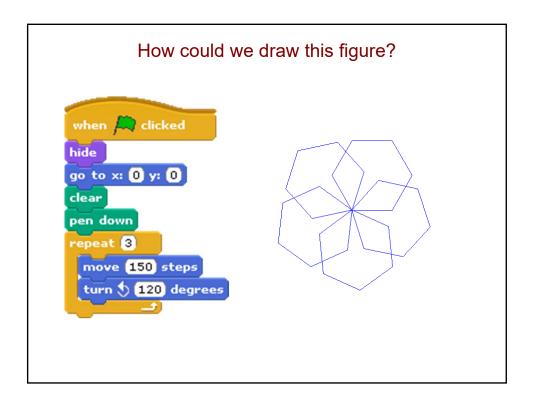


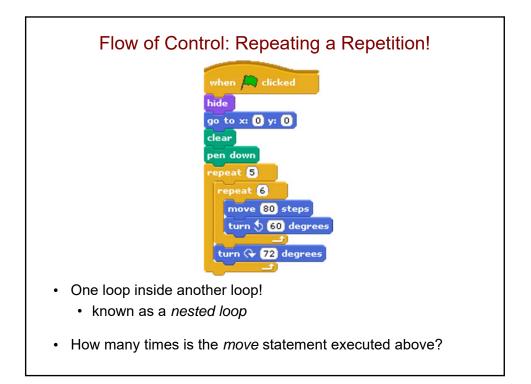


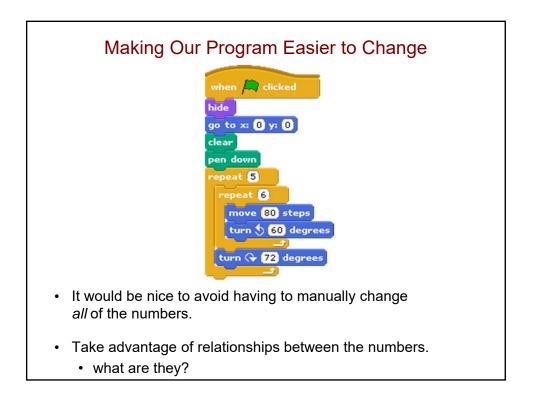


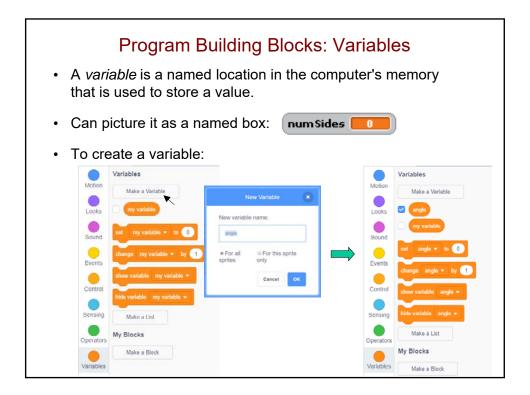


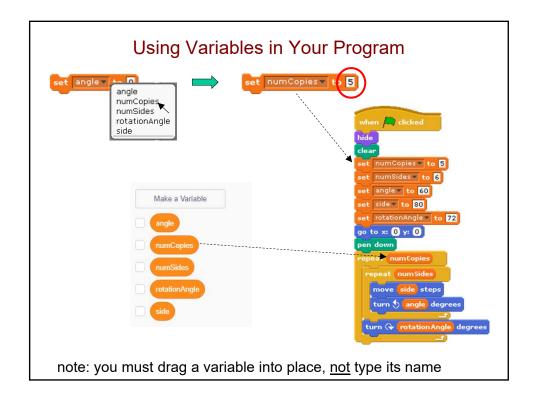


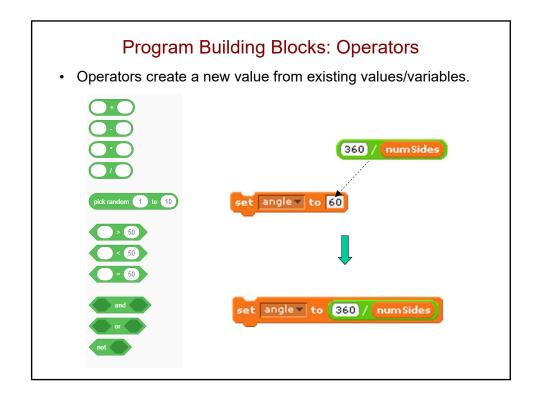


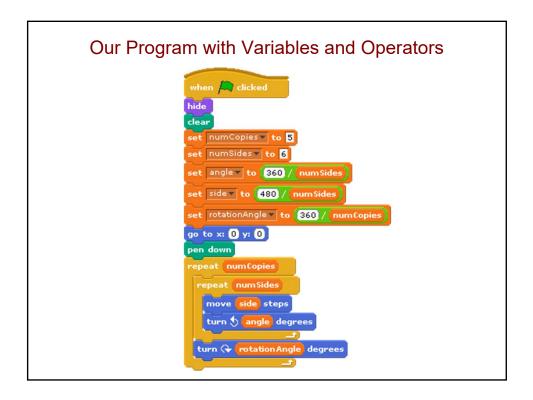


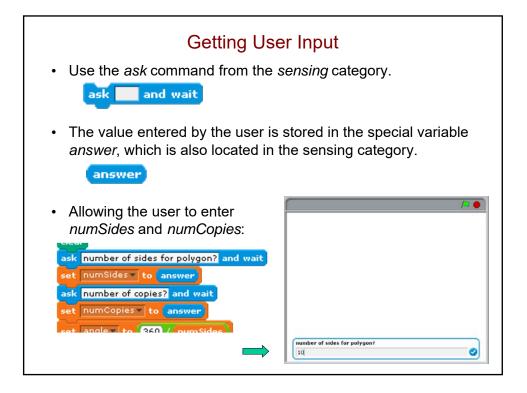


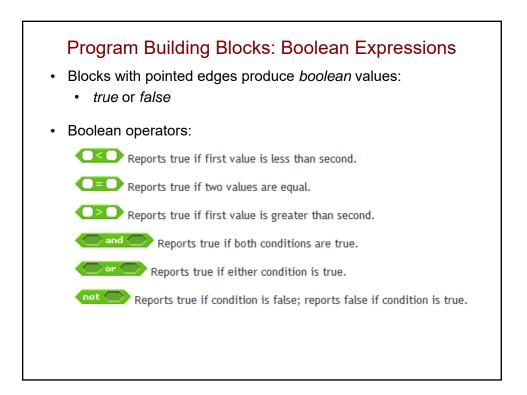


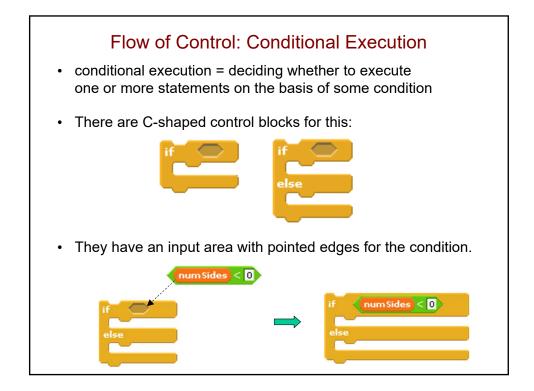


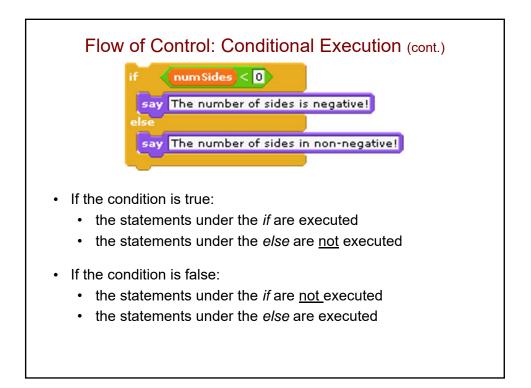


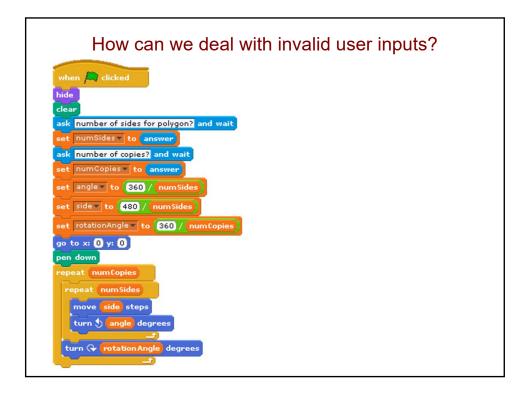


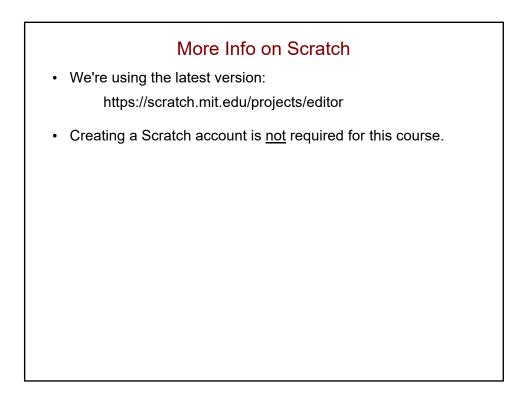




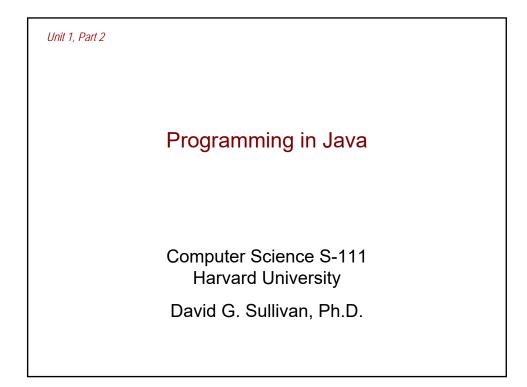


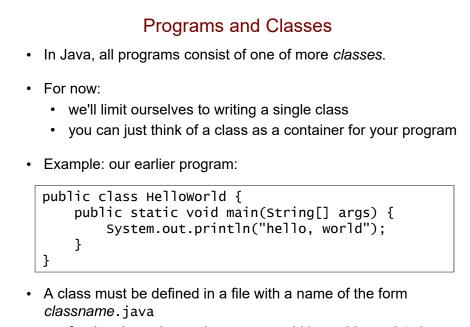






### **Final version** ides for polygon? and • We use two if-else statements to check for invalid inputs: • one checks for numSides < 3 ust have at least 3 sides • one checks for numCopies < 1 1 • If an invalid input is found, we: must be at least 1 copy · show the sprite • have the sprite say le 🔻 to [ 360 ] ide 🔻 to [ 480 / an error message ile 🔻 to [ 360 ) • end the program « O y: O Otherwise, we continue with the rest ٠ of the program.





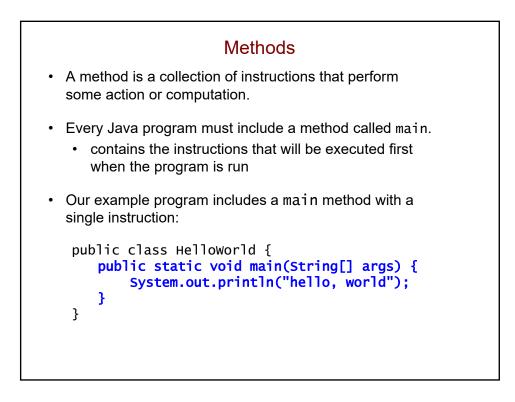
• for the class above, the name would be Helloworld.java

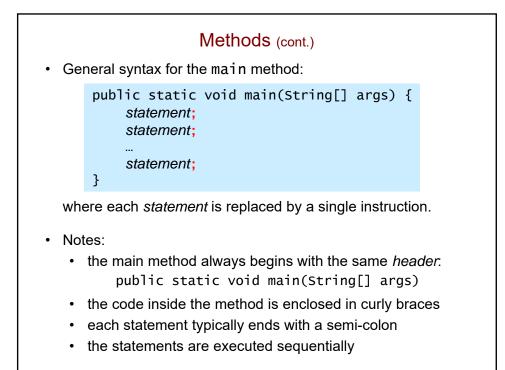
## Using an IDE

- An *integrated development environment (IDE)* is an application that helps you develop programs.
- We'll use the Dr. Java IDE.
  - PS 0 told you how to obtain and install it.
- With an IDE, you do the following:
  - use its built-in text editor to write your code
  - instruct the IDE to compile the code
    - · turns it into lower-level instructions that can be run
    - · checks for violations of the syntax of the language
  - instruct the IDE to run the program
  - · debug as needed, using the IDE's debugging tools

C:\Users\dgs\Desktop\cs111	examples\intro\He	lloWorld.java				
Eile         Edit         Tools         Project         De           Image: New         Image: New			🔵 Undo 🏾 🥲 Redo	K Find Compile	Reset Run Test	Javadoc
}	public Sys }	tem.out.prir	{ main(String[] tln("hello, w	orld");		
∫Interactions ∫ Console ∫ C Compiler ready: J Files\Java\jdk1.6	ompiler Output   DK 6.0_3 f .0_03\lib\	rom C:\Progr tools.jar.	am		Compiler JDK 6.0_3	source
	e111\ovamplas\in	tro\HelloWorld.java				3:6

	Format of a Java Class
• Gene	eral syntax:
ţ	<pre>public class name {</pre>
	code goes here
]	}
where	e <i>name</i> is replaced by the name of the class.
Notes	s:
• tł	ne class begins with a <i>header</i> . public class <i>name</i>
	ne code inside the class is enclosed in curly braces { and })

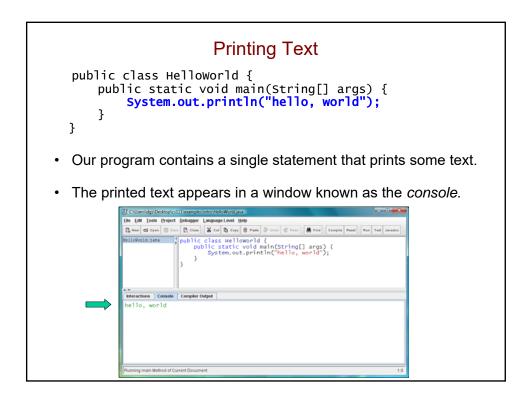




Identifiers
<ul> <li>Used to name the components of a Java program like classes and methods.</li> </ul>
<ul> <li>Rules:</li> <li>must begin with a letter (a-z, A-Z), \$, or _</li> <li>can be followed by any number of letters, numbers, \$, or _</li> <li>spaces are not allowed</li> <li>cannot be the same as a <i>keyword</i> – a word like class that is part of the language itself (see the Resources page)</li> </ul>
<ul> <li>Which of these are <i>not</i> valid identifiers?</li> <li>n1 num_values 2n</li> <li>avgSalary course name</li> </ul>
<ul> <li>Java is <i>case-sensitive</i> (for both identifiers and keywords).</li> <li>example: Helloworld is not the same as helloworld</li> </ul>

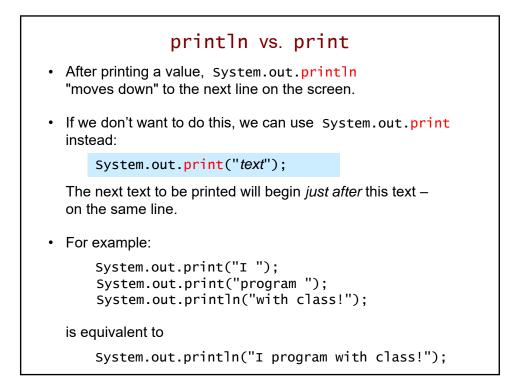
## **Conventions for Identifiers**

- · Capitalize class names.
  - example: Helloworld
- Do not capitalize method names.
  - example: main
- · Capitalize internal words within the name.
  - example: неllo<u>w</u>orld

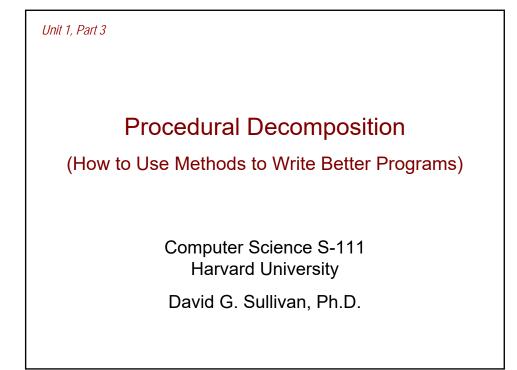


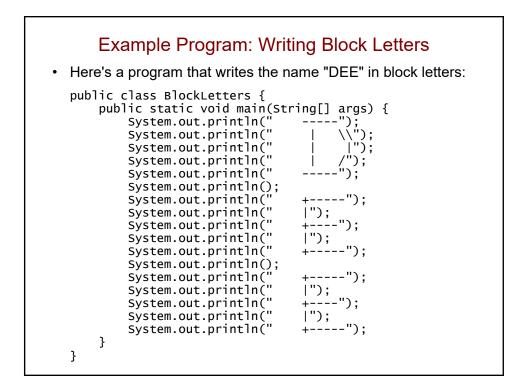
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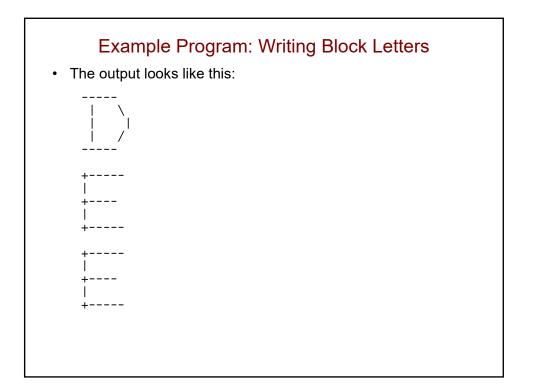
Printing Text (cont.)
<ul> <li>A string literal cannot span multiple lines.</li> </ul>
<ul> <li>example: this is not allowed:</li> </ul>
System.out.println("I want to print a string on two lines.");
<ul> <li>Instead, we can use two different statements: System.out.println("I want to print a string");</li> </ul>
System.out.println("on two lines.");

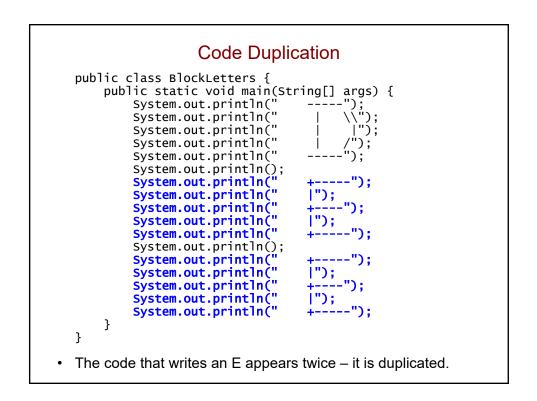


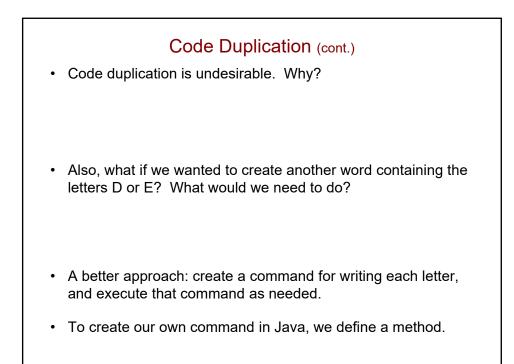
Escape Sequences
<ul> <li>Problem: what if we want to print a string that includes double quotes?</li> </ul>
<ul> <li>example: System.out.println("Jim said, "hi!"");</li> <li>this won't compile. why?</li> </ul>
<ul> <li>Solution: precede the double quote character by a \         System.out.println("Jim said, \"hi!\"");</li> </ul>
<ul> <li>∖" is an example of an escape sequence.</li> </ul>
<ul> <li>The \ tells the compiler to interpret the following character differently than it ordinarily would.</li> </ul>
Other examples:
• $n$ a newline character (goes to the next line)
• \t a tab
• ∖∖ a backslash

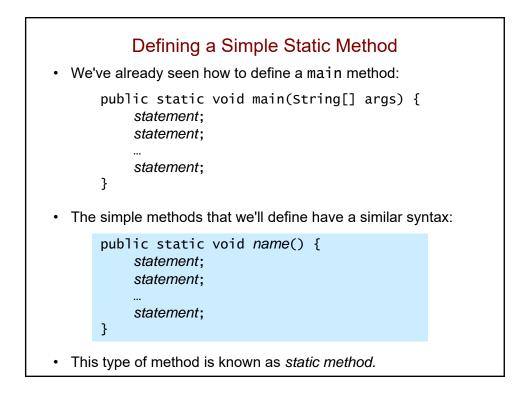


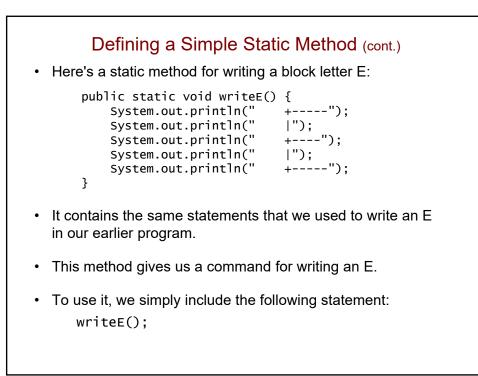


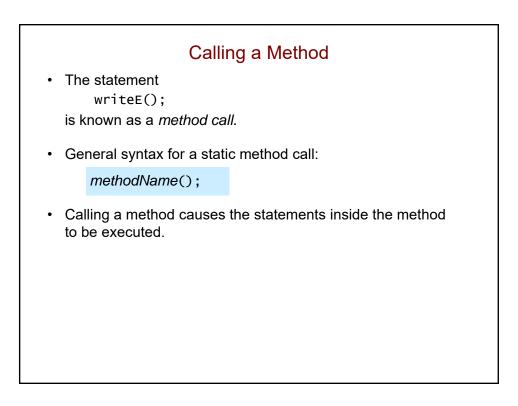


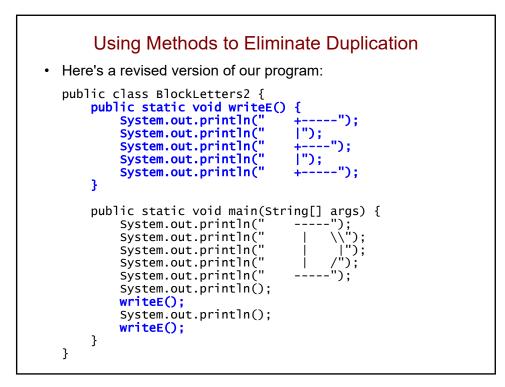


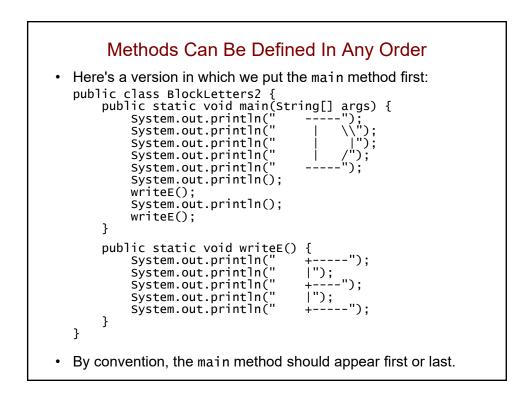


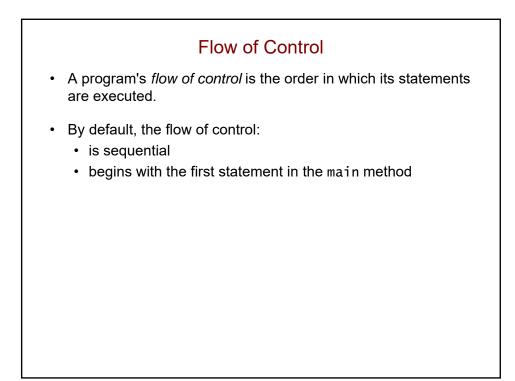


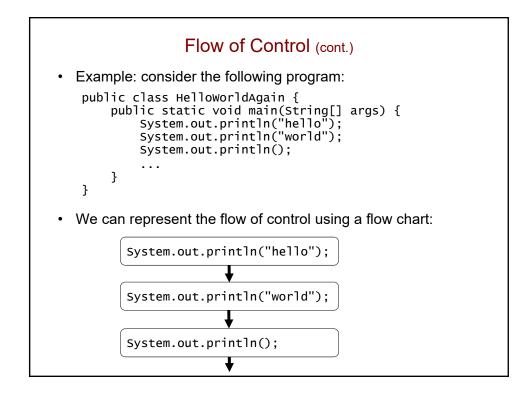


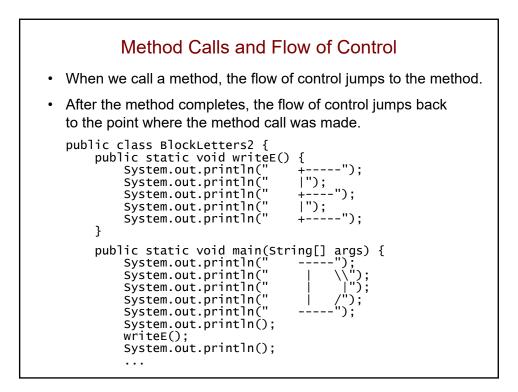


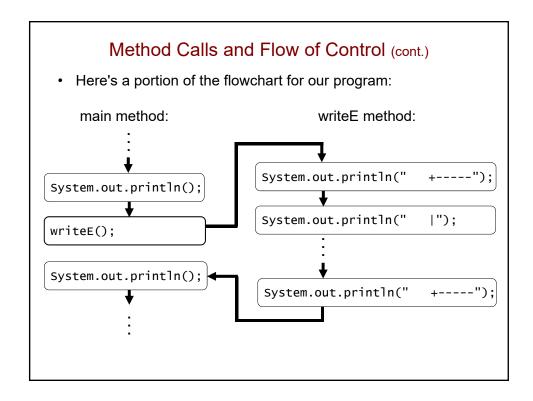


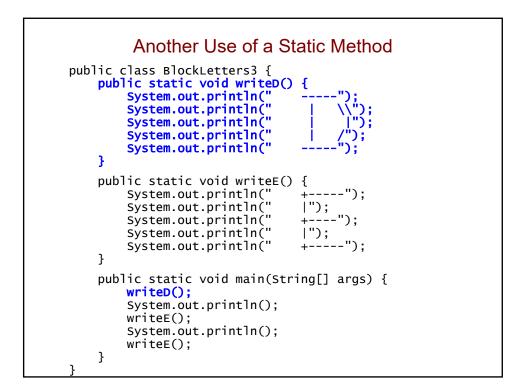


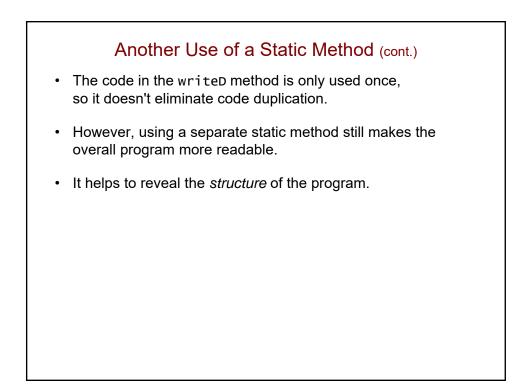


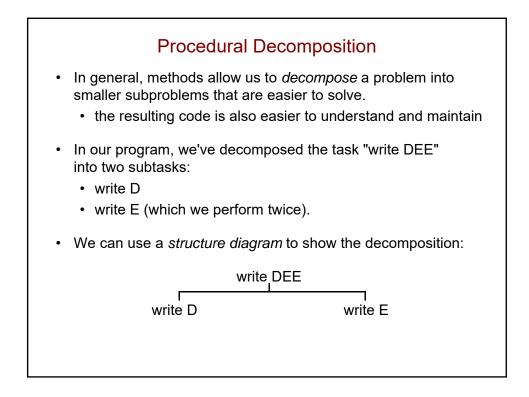


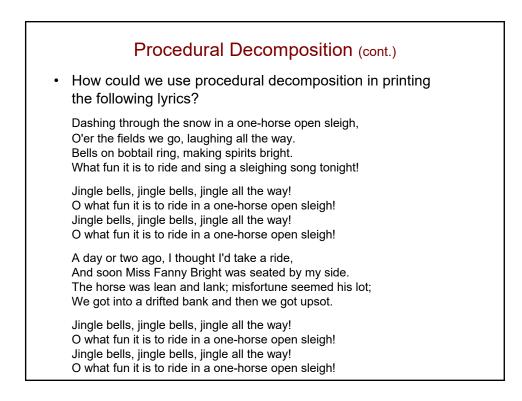


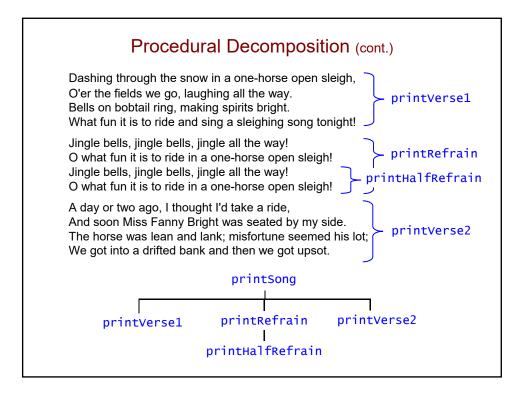


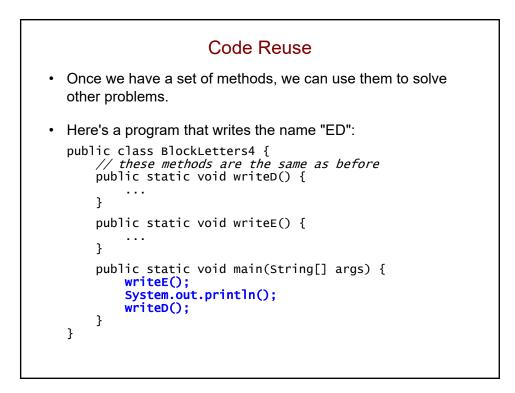




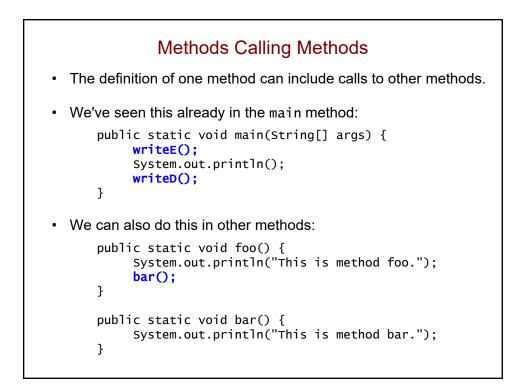


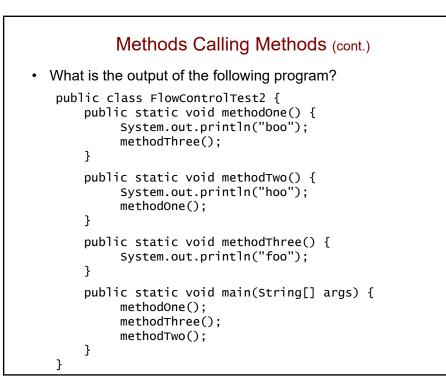


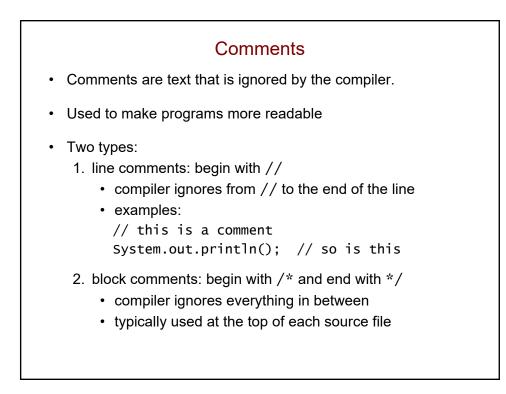


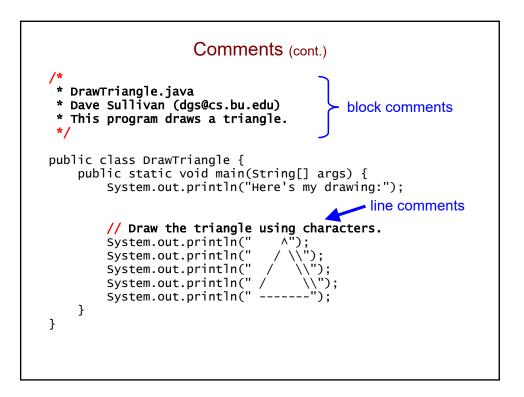


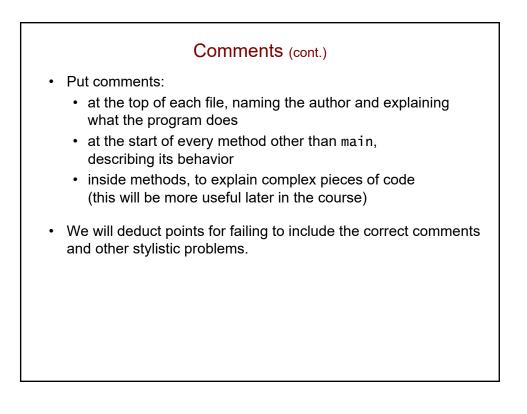
```
Tracing the Flow of Control
What is the output of the following program?
 public class FlowControlTest {
     public static void methodA() {
          System.out.println("starting method A");
     }
     public static void methodB() {
          System.out.println("starting method B");
     }
     public static void methodC() {
          System.out.println("starting method C");
     }
     public static void main(String[] args) {
          methodC();
          methodA();
     }
 }
```

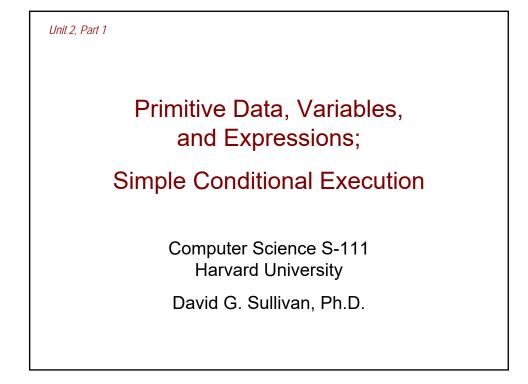


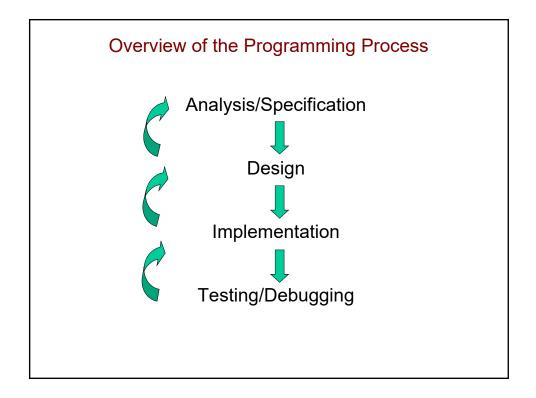


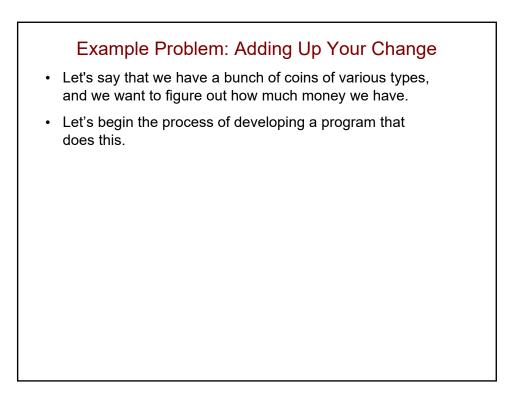


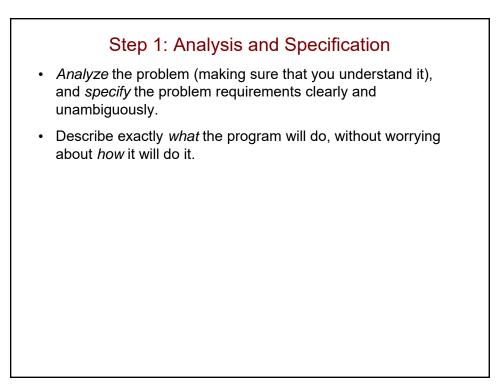


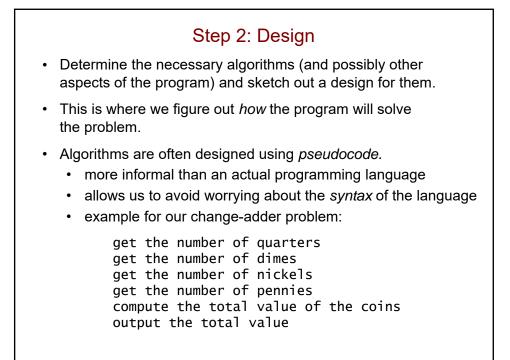


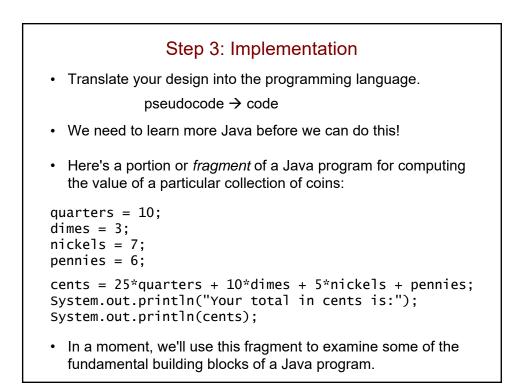


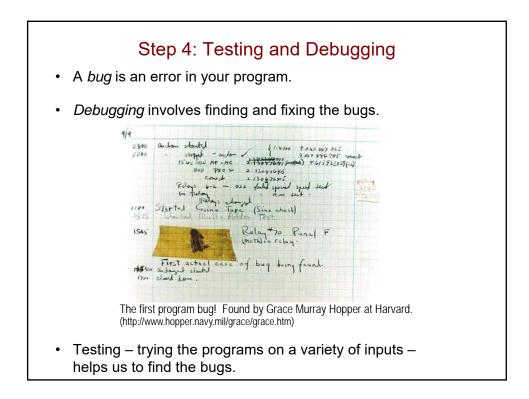


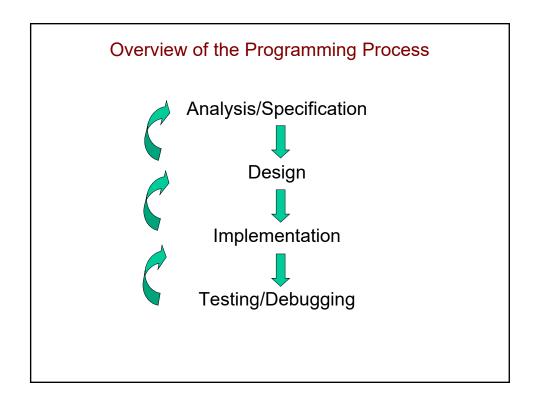








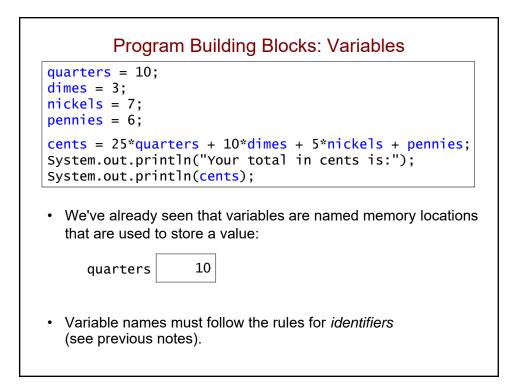




## **Program Building Blocks: Literals**

```
quarters = 10;
dimes = 3;
nickels = 7;
pennies = 6;
cents = 25*quarters + 10*dimes + 5*nickels + pennies;
System.out.println("Your total in cents is:");
System.out.println(cents);
```

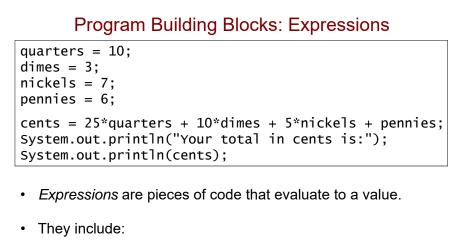
- Literals specify a particular value.
- They include:
  - string literals: "Your total in cents is:"
    - are surrounded by double quotes
  - numeric literals: 25 3.1416
    - commas are not allowed!



## Program Building Blocks: Statements

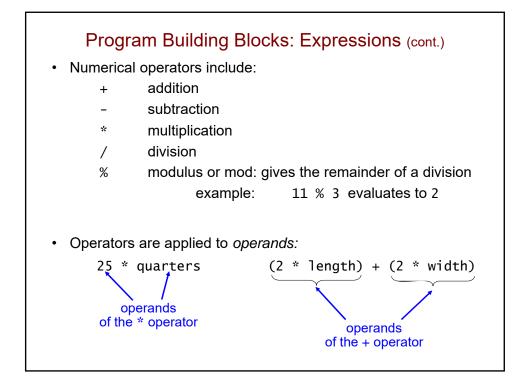
```
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dimes = 3;
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```

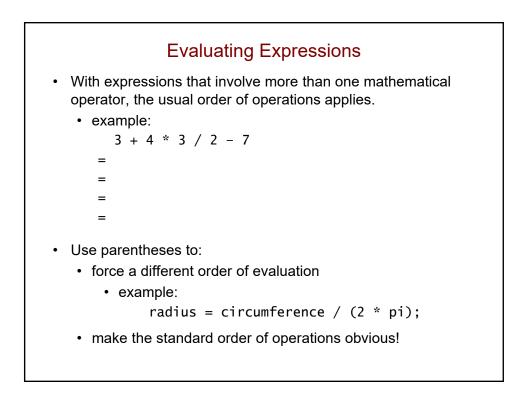
- In Java, a single-line statement typically ends with a semi-colon.
- Later, we will see examples of control statements that contain other statements, just as we did in Scratch.

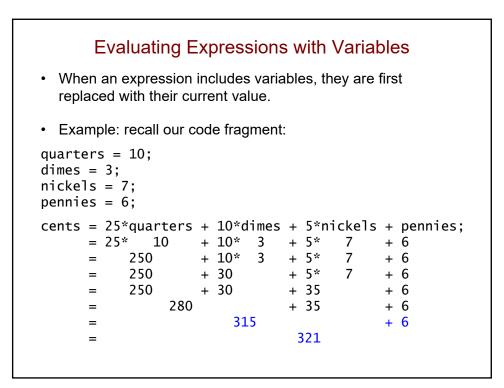


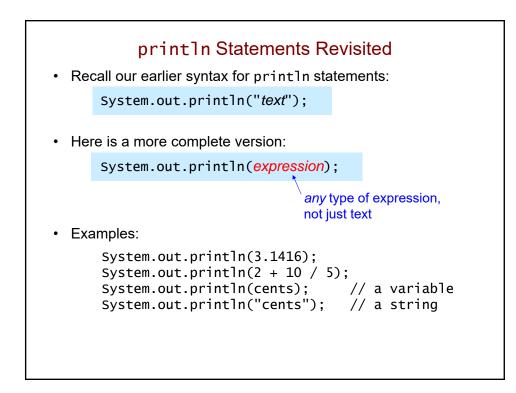
- · literals, which evaluate to themselves
- · variables, which evaluate to the value that they represent
- combinations of literals, variables, and operators:

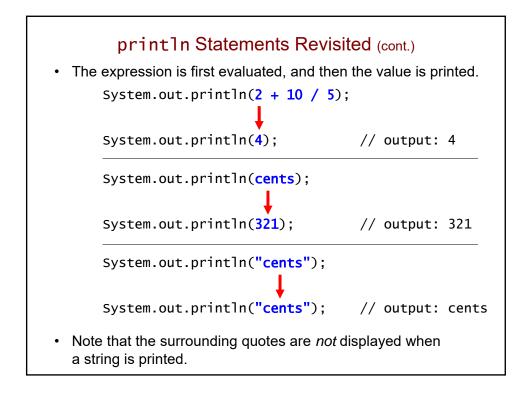
25\*quarters + 10\*dimes + 5\*nickels + pennies

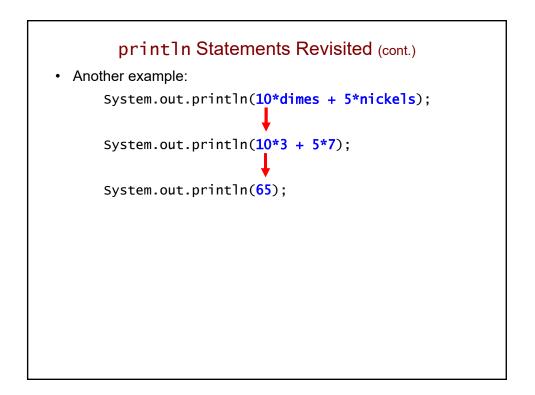


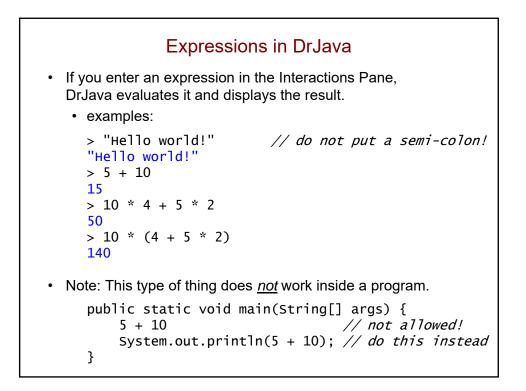


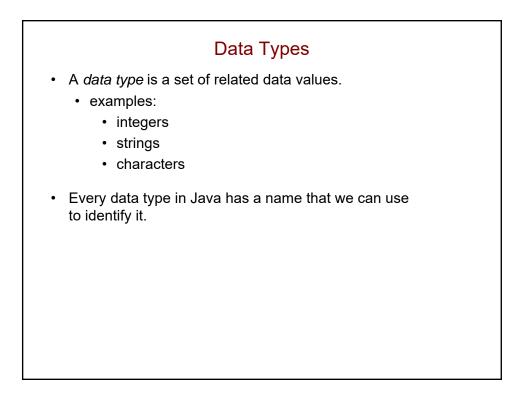


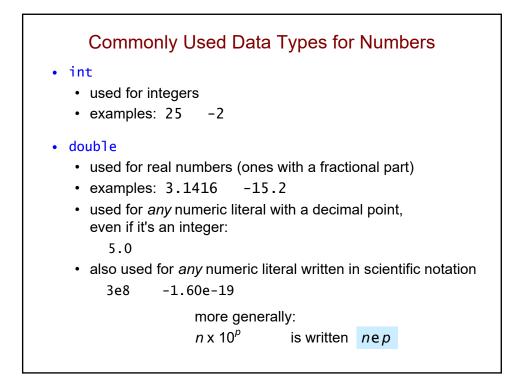


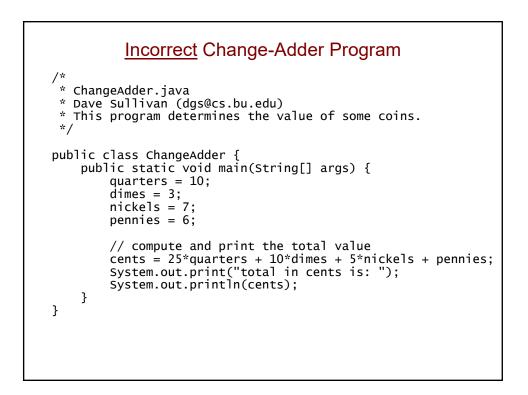


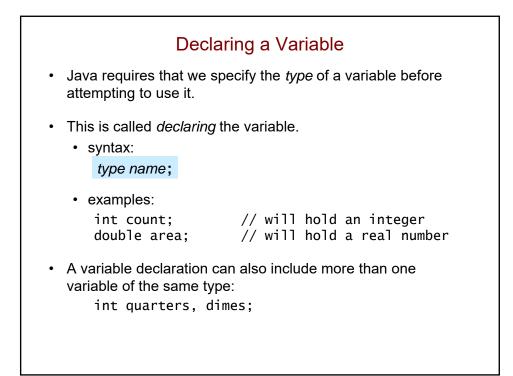


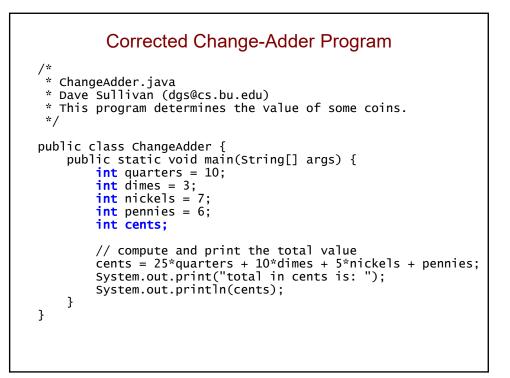


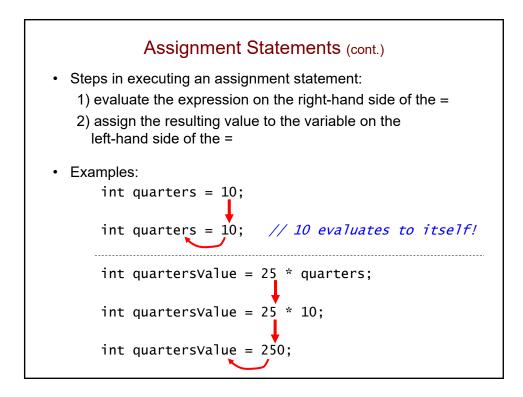


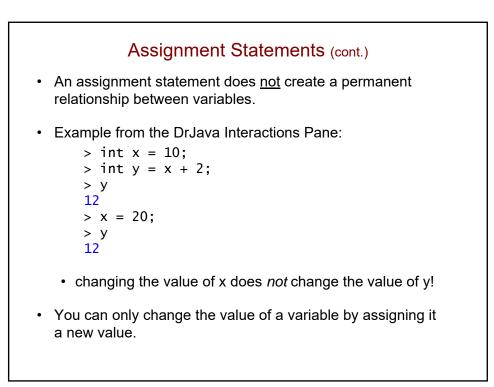


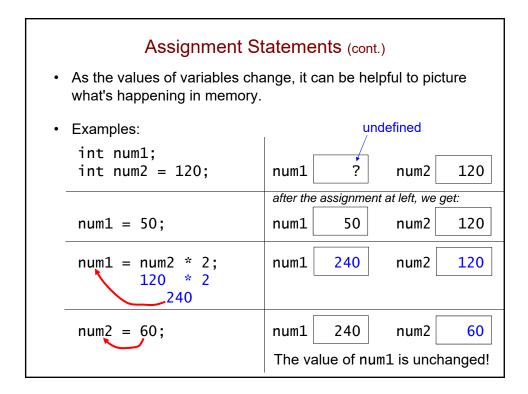


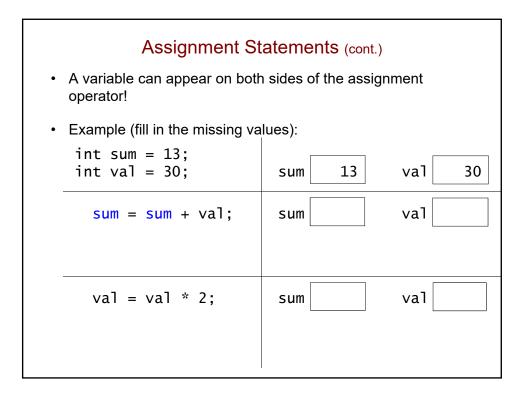


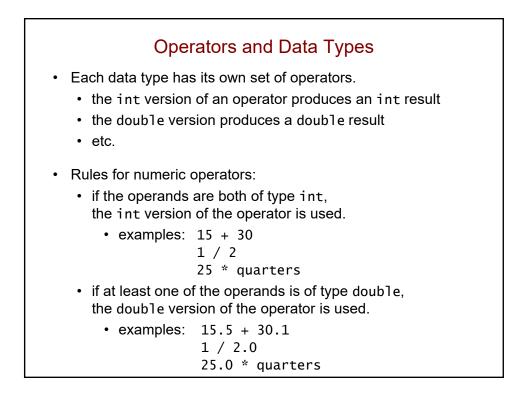


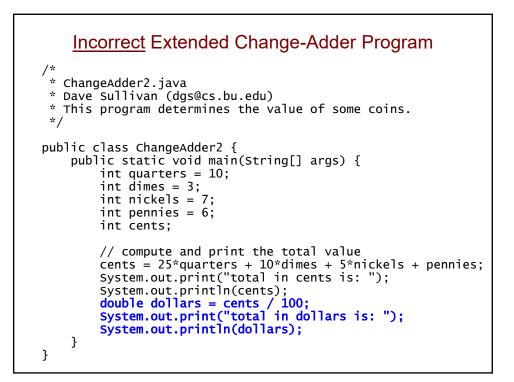


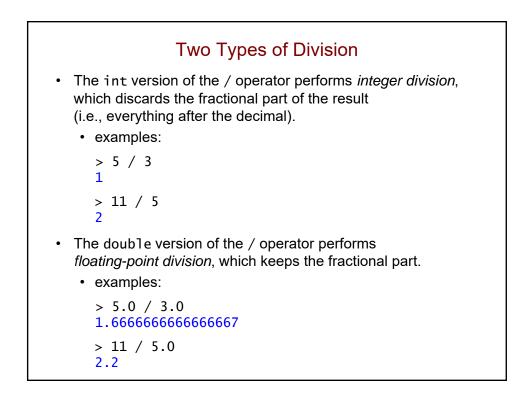


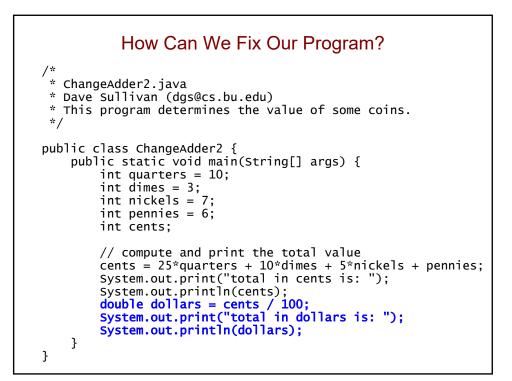


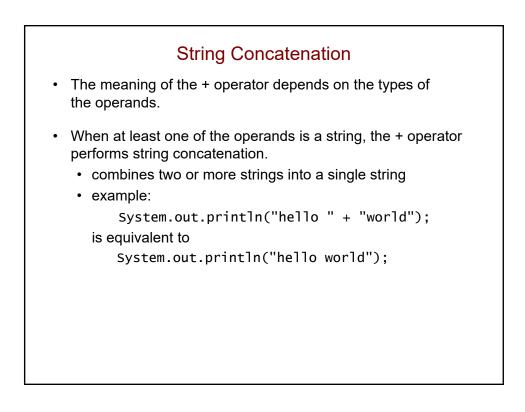


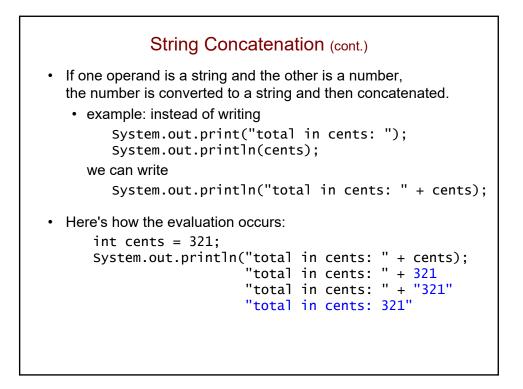


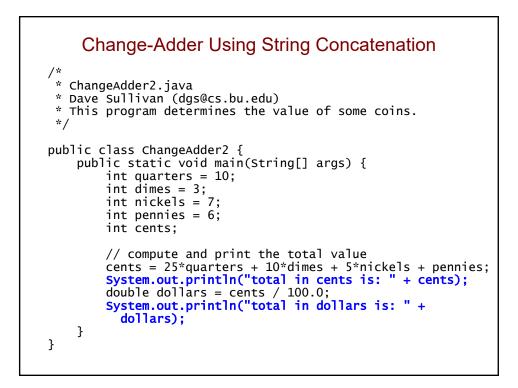


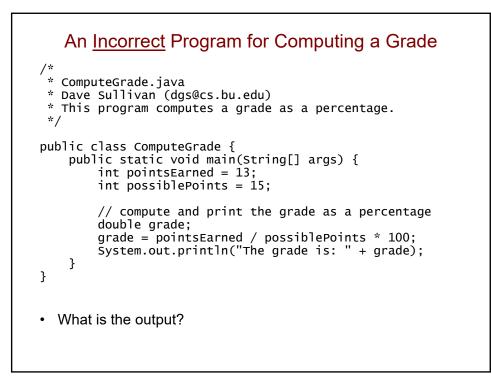


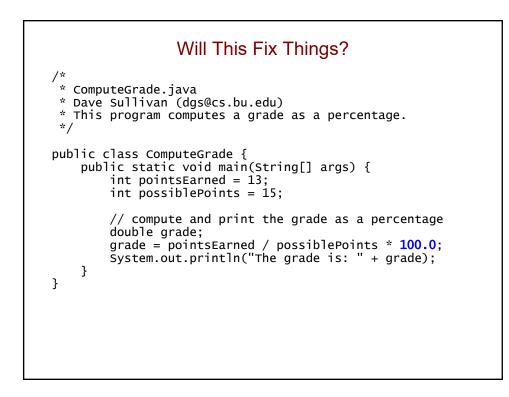


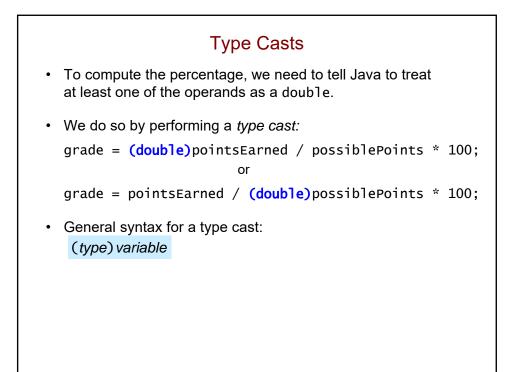


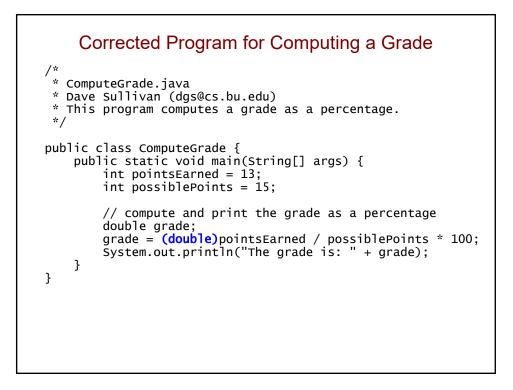


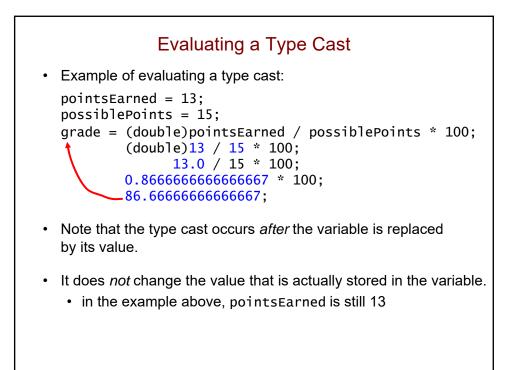


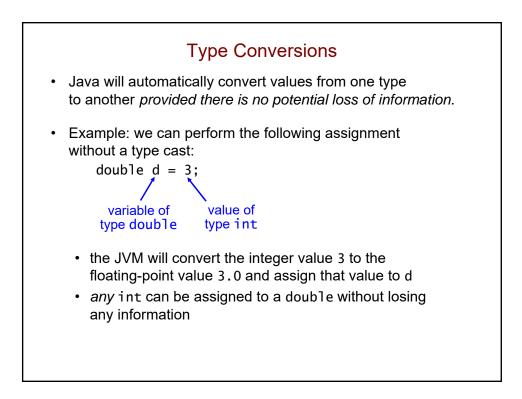


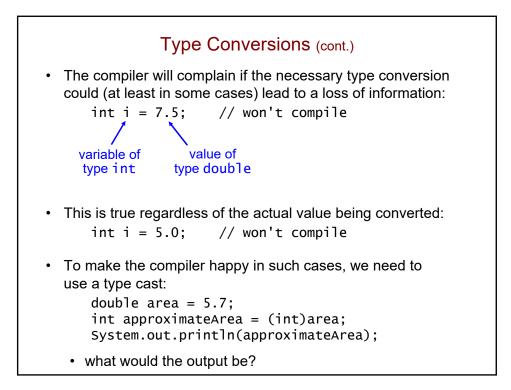


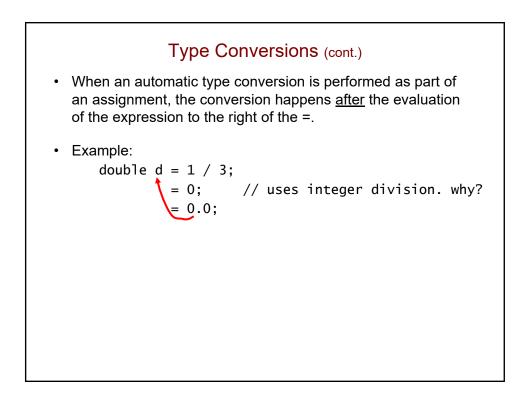


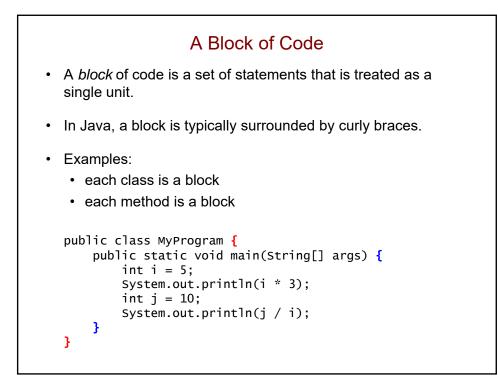


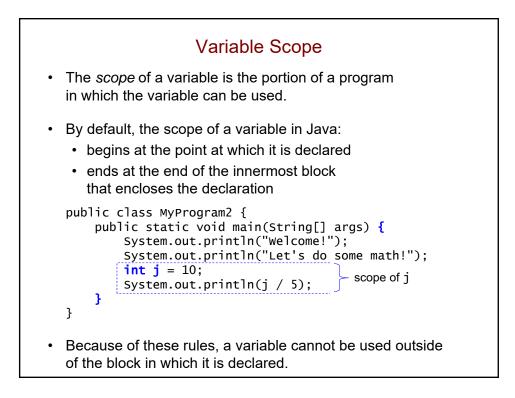


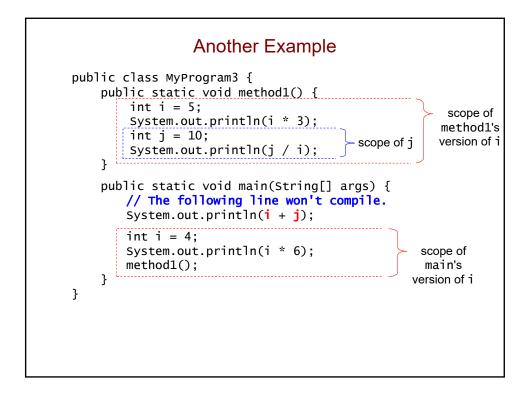


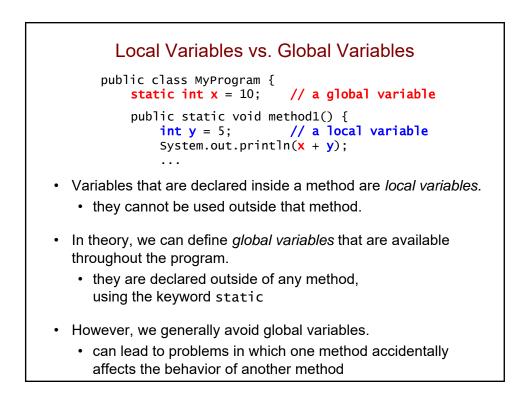


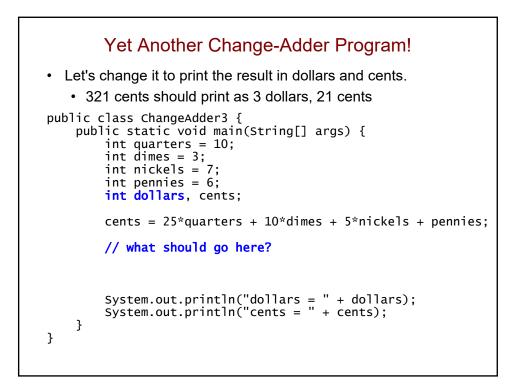


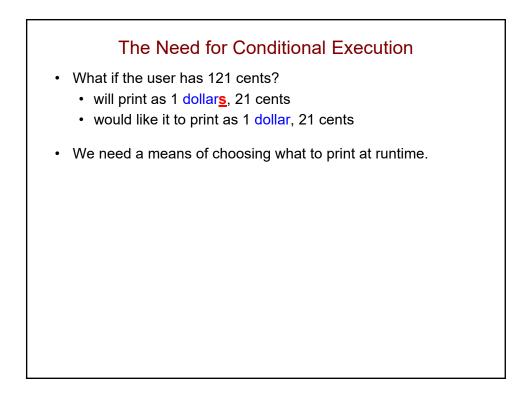


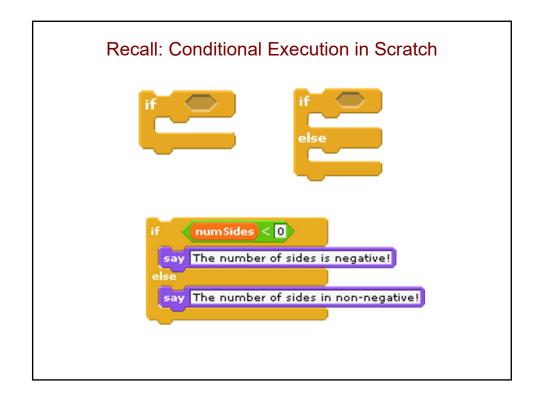


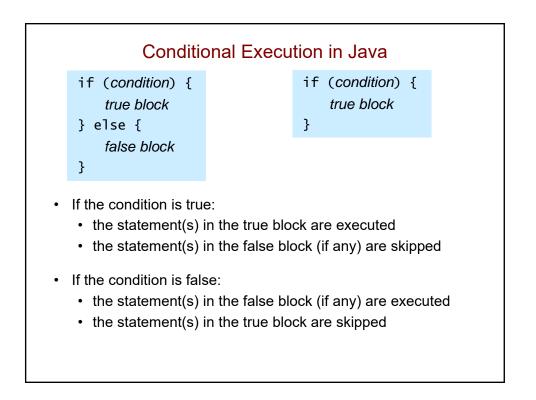




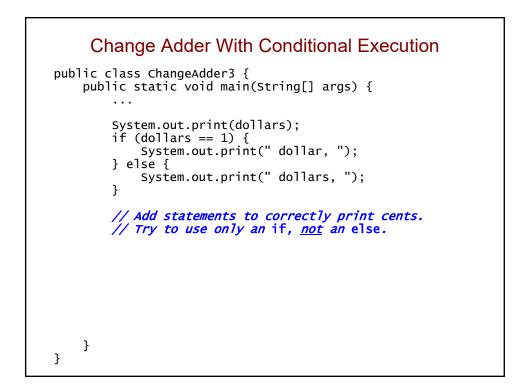


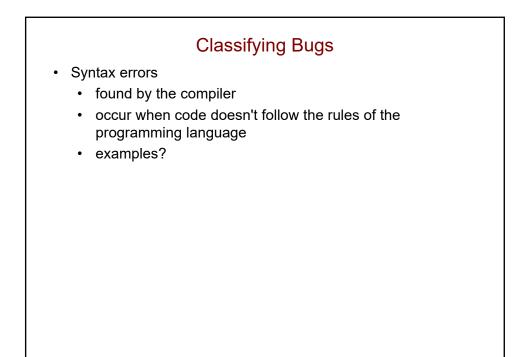




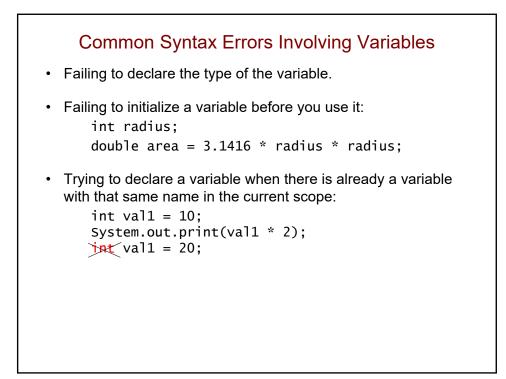


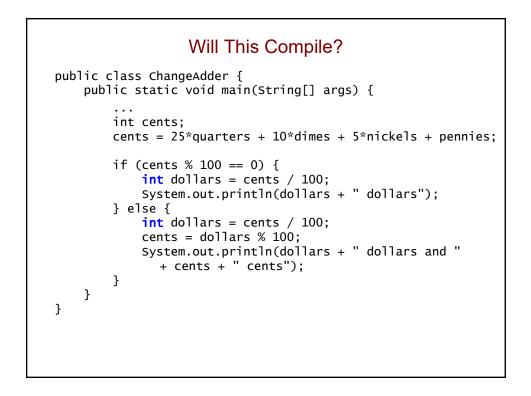
	Expressing Simple Conditions				
•	<ul> <li>Java provides a set of operators called <i>relational operators</i> for expressing simple conditions:</li> </ul>				
<u>operator</u> <	<u>name</u> less than	<u>examples</u> 5 < 10 num < 0			
>	greater than	40 > 60 (which is false!) count > 10			
<=	less than or equal to	average <= 85.8			
>=	greater than or equal to	temp >= 32			
== (don't cont	equal to iuse with = )	sum == 10 firstChar == 'P'			
!=	not equal to	age != myAge			

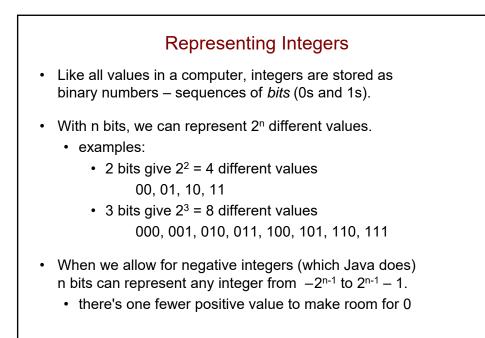




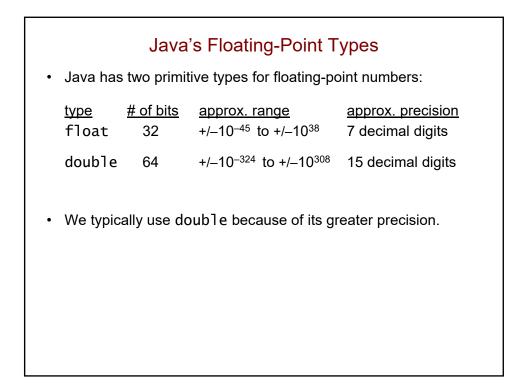
	Classifying Bugs
•	
•	gic errors the code compiles, but it doesn't do what you intended it to do may or may not cause the program to crash • called <i>runtime errors</i> if the program crashes often harder to find!

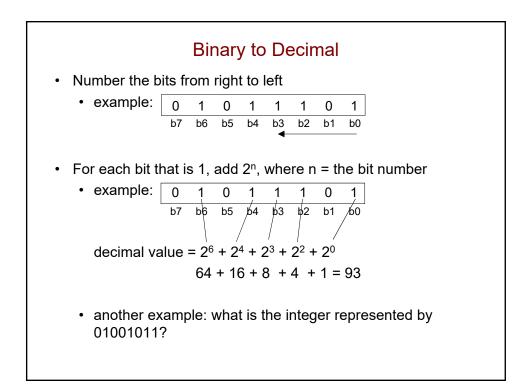


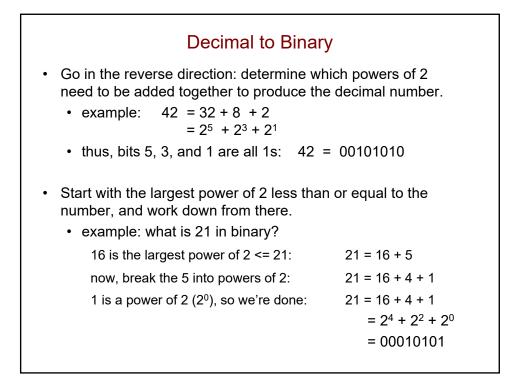


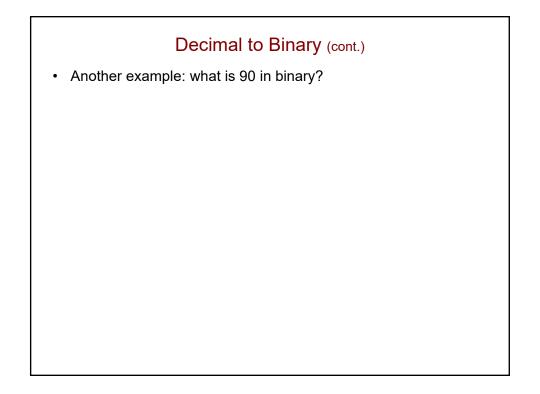


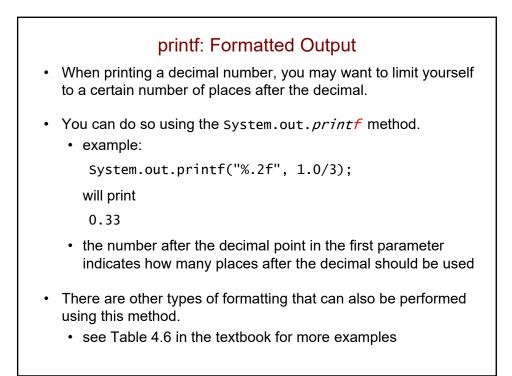
<ul> <li>Java's Integer Types</li> <li>Java's actually has four primitive types for integers, all of which represent signed integers</li> </ul>				
represent signed integers.				
<u>type</u> byte	<u># of bits</u> 8	<u>range of values</u> $-2^7$ to $2^7 - 1$ (-128 to 127)		
short	16	-2 <sup>15</sup> to 2 <sup>15</sup> - 1 (-32768 to 32767)		
int	32	–2 <sup>31</sup> to 2 <sup>31</sup> – 1 (approx. +/–2 billion)		
long	64	$-2^{63}$ to $2^{63}-1$		
• We typically use int, unless there's a good reason not to.				



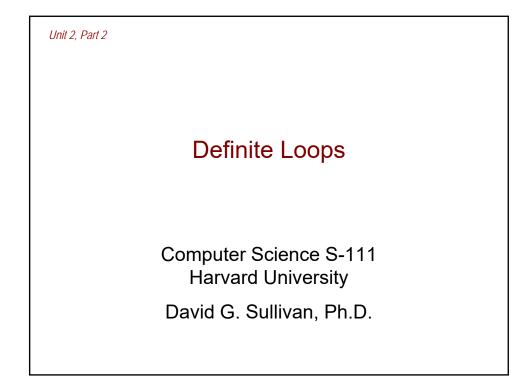


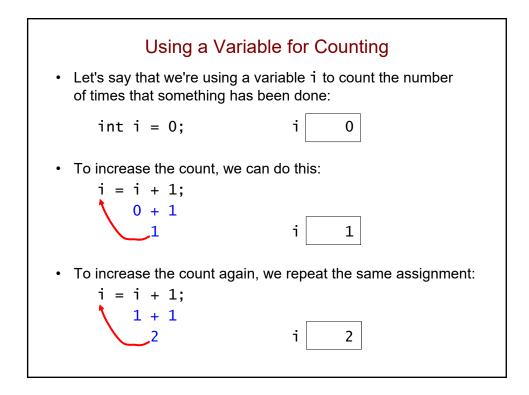


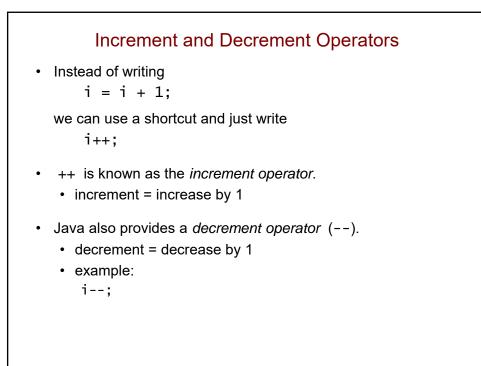


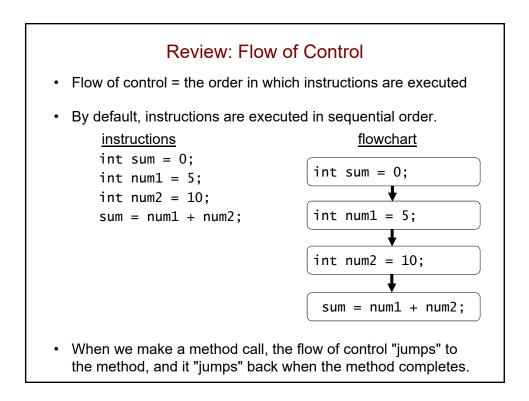


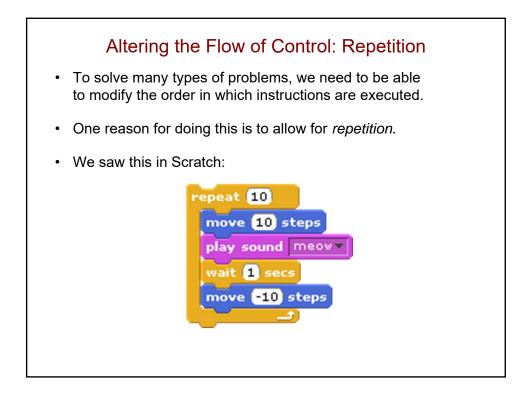
Consider the following code fragments 1) 1000 2) 10 * 5 3) System.out.println("Hello"); 4) hello 5) num1 = 5; 6) 2*width + 2*length 7) main
<ol> <li>2) 10 * 5</li> <li>3) System.out.println("Hello");</li> <li>4) hello</li> <li>5) num1 = 5;</li> <li>6) 2*width + 2*length</li> </ol>
<ul> <li>3) System.out.println("Hello");</li> <li>4) hello</li> <li>5) num1 = 5;</li> <li>6) 2*width + 2*length</li> </ul>
<ul> <li>4) hello</li> <li>5) num1 = 5;</li> <li>6) 2*width + 2*length</li> </ul>
5) num1 = 5; 6) 2*width + 2*length
6) 2*width + 2*length
, _
7) main
r) marn
Which of them are examples of:
literals?     expressions?
identifiers?         statements?

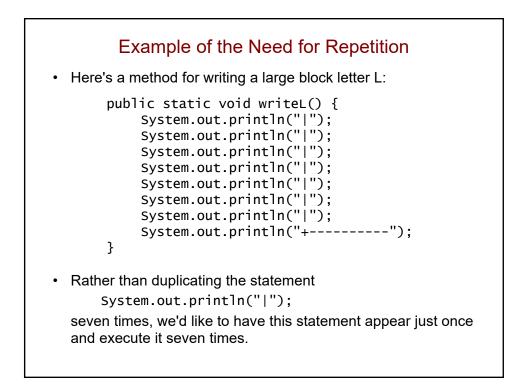




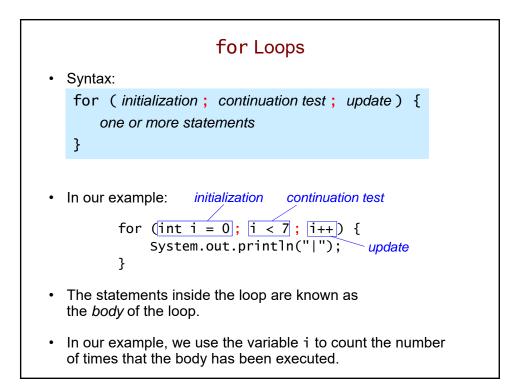


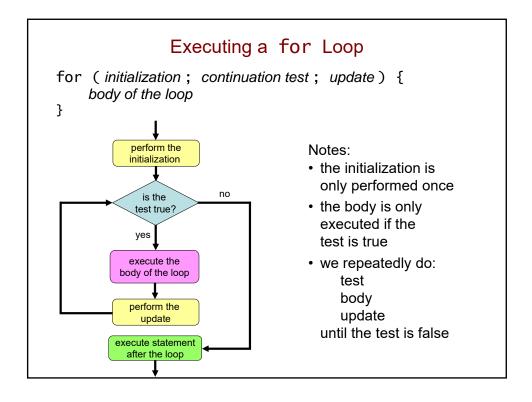


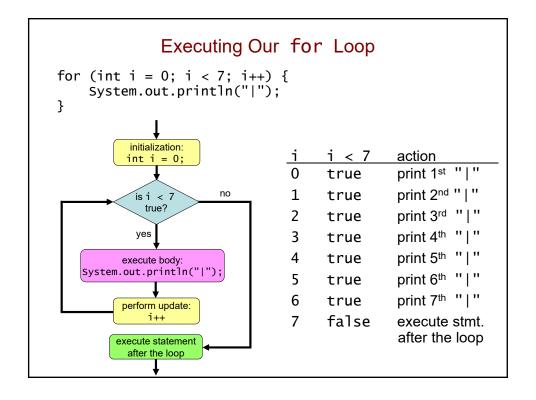


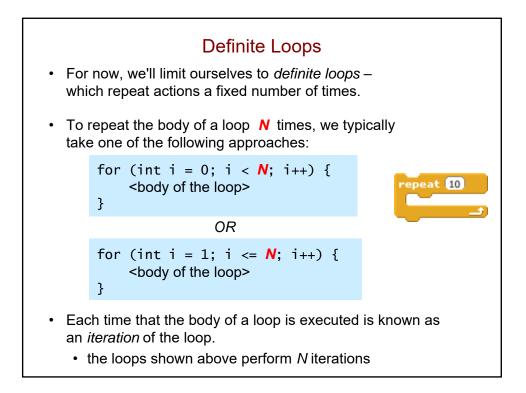


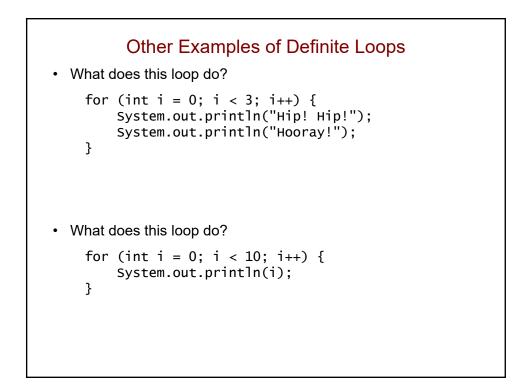
## for Loops • To repeat one or more statements multiple times, we can use a construct known as a for loop. • Here's a revised version of our writeL method that uses one: public static void writeL() { for (int i = 0; i < 7; i++) { System.out.println("|"); } System.out.println("+-----"); } </pre>

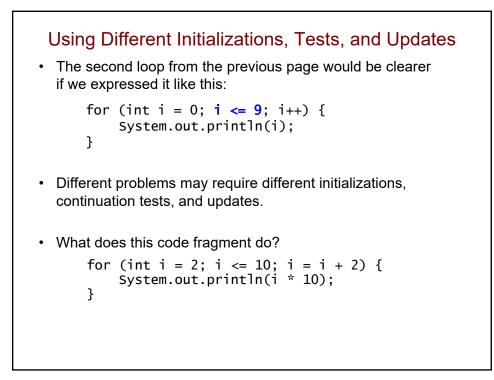


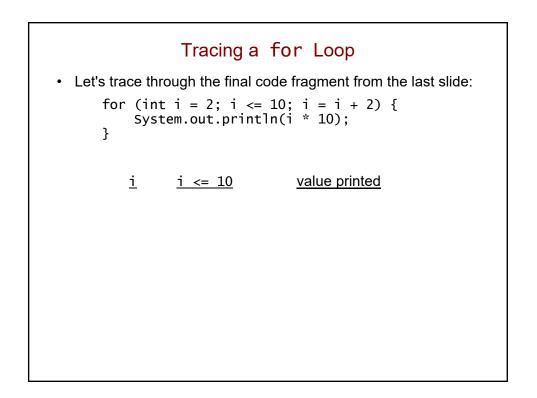










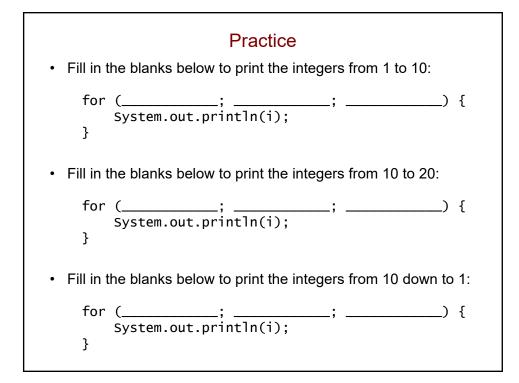


## **Common Mistake**

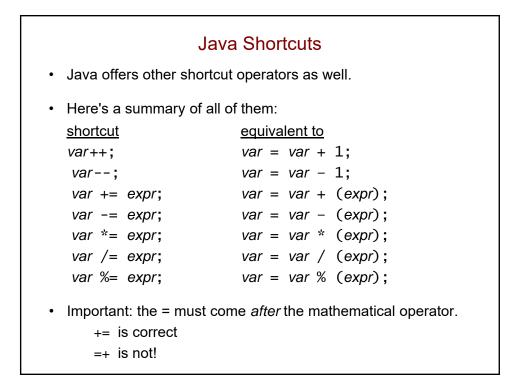
• You should <u>not</u> put a semi-colon after the for-loop header:

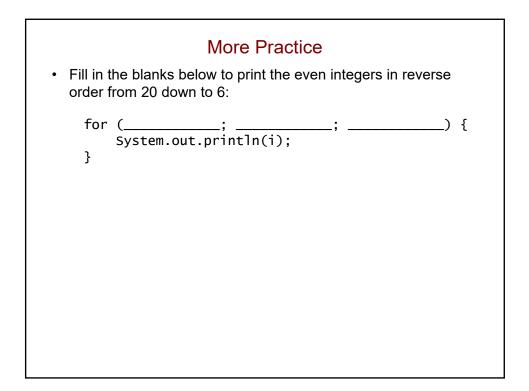
```
for (int i = 0; i < 7; i++); {
    System.out.println("|");
}</pre>
```

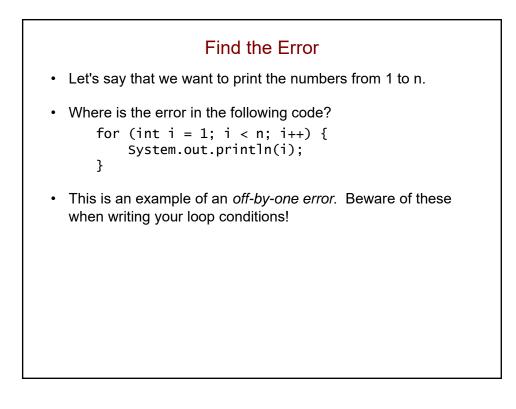
- The semi-colon ends the for statement.
  - thus, it doesn't repeat anything!
- The println is independent of the for statement, and only executes once.

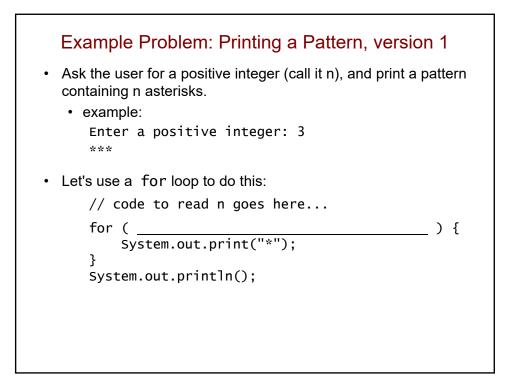


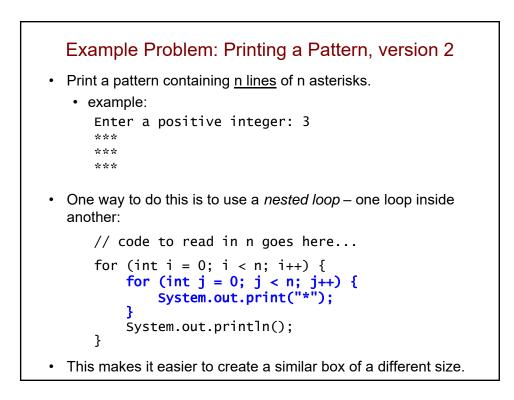
Other Java Shortcuts
• Recall this code fragment:
 for (int i = 2; i <= 10; i = i + 2) {
 System.out.println(i \* 10);
 }
• Instead of writing
 i = i + 2;
we can use a shortcut and just write
 i += 2;
• In general
 variable += expression;
is equivalent to
 variable = variable + (expression);</pre>

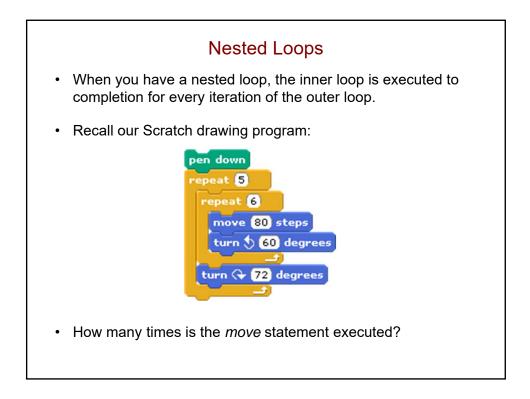


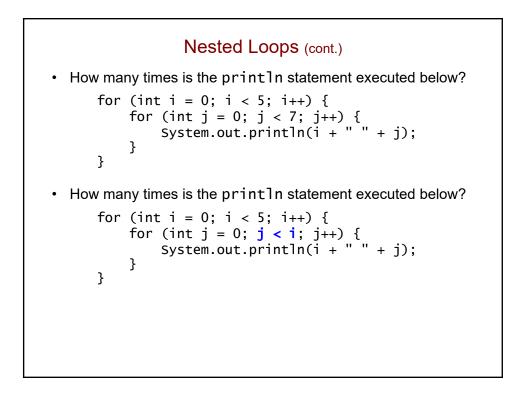






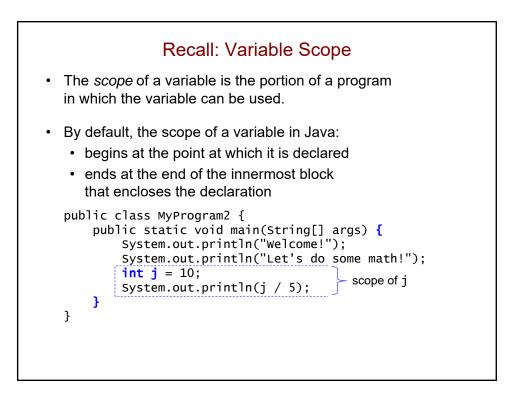


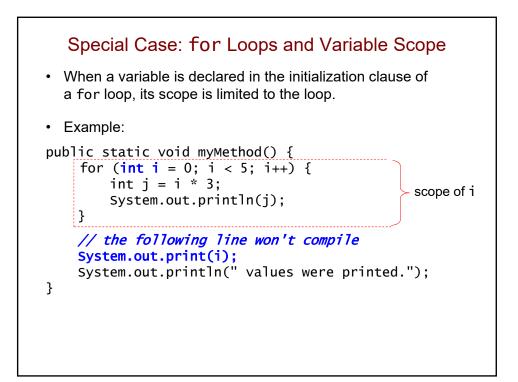


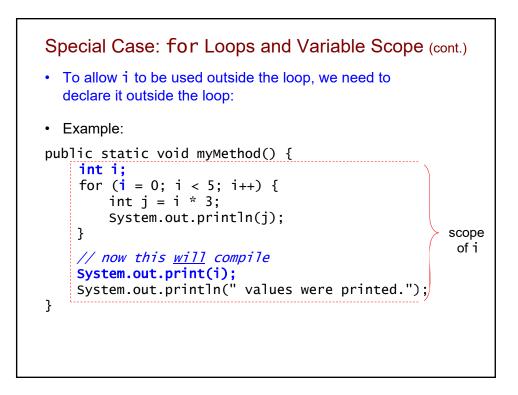


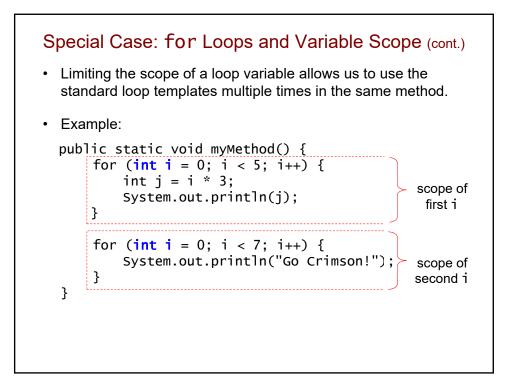
```
Tracing a Nested for Loop
for (int i = 0; i < 5; i++) {
    for (int j = 0; j < i; j++) {
        System.out.println(i + " " + j);
    }
}
i < 5 i j < i value printed</pre>
```

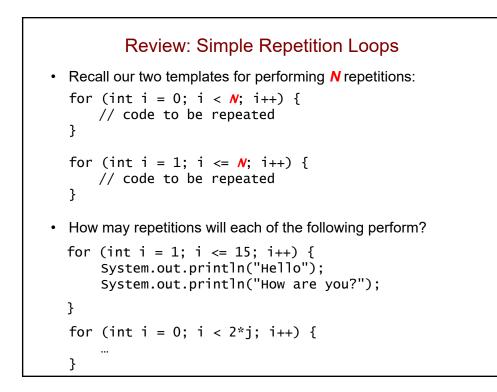
i









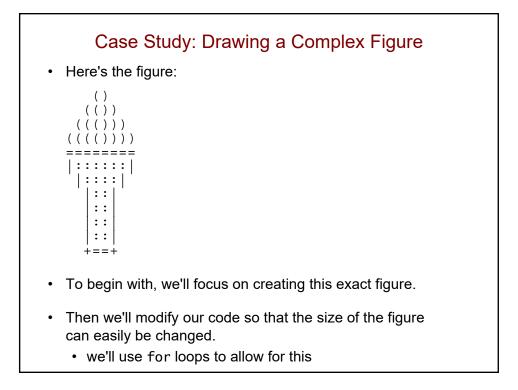


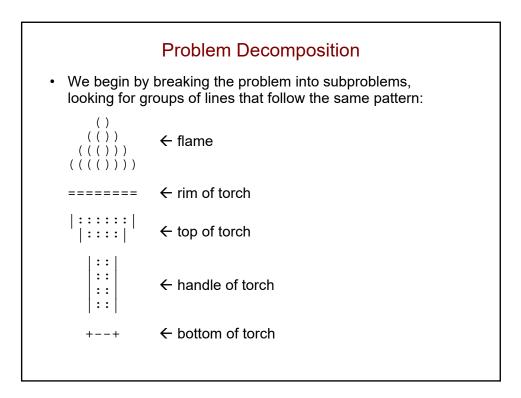
## More Practice: Tracing a Nested for Loop

<u>output</u>

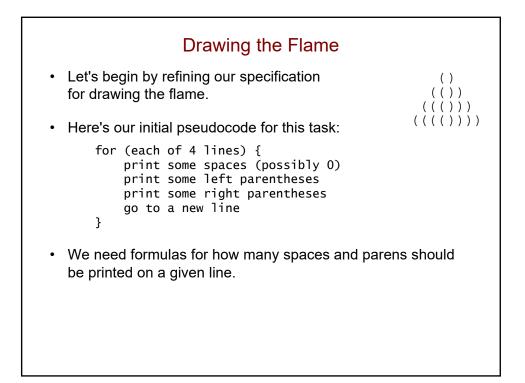
```
for (int i = 1; i <= 3; i++) {
    for (int j = 0; j < 2*i + 1; j++) {
        System.out.print("*");
    }
    System.out.println();
}</pre>
```

 $\underline{i} \leq 3$   $\underline{j} \leq 2 \times i + 1$ 

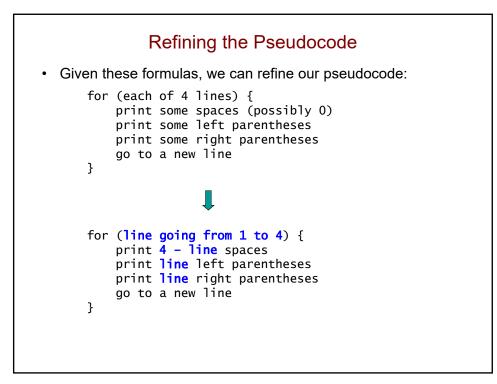


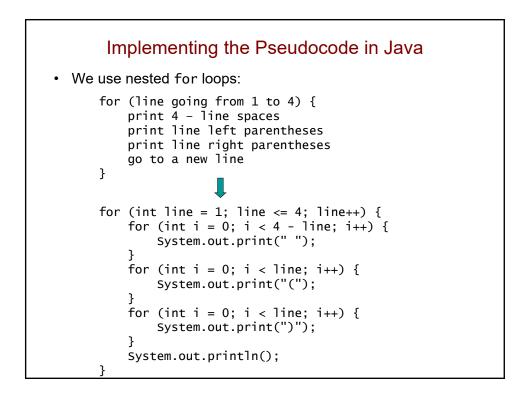


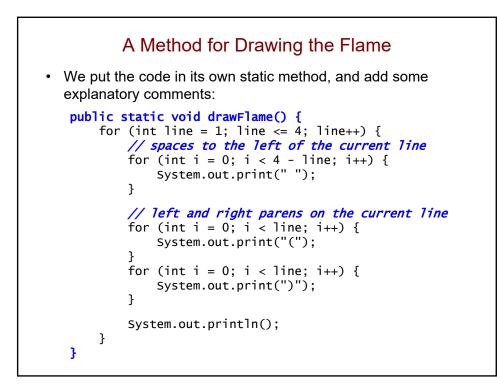
	<ul> <li>blem Decomposition (cont.)</li> <li>e following initial pseudocode: draw the flame draw the rim of the torch draw the top of the torch draw the handle of the torch draw the bottom of the torch</li> <li>This is a high-level description of what needs to be done.</li> <li>We'll gradually expand the pseudocode into more and more detailed instructions – until we're able to implement them in Java.</li> </ul>
++	until we're able to implement them in Java.

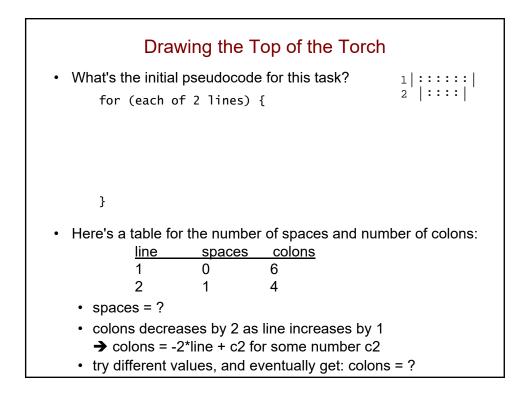


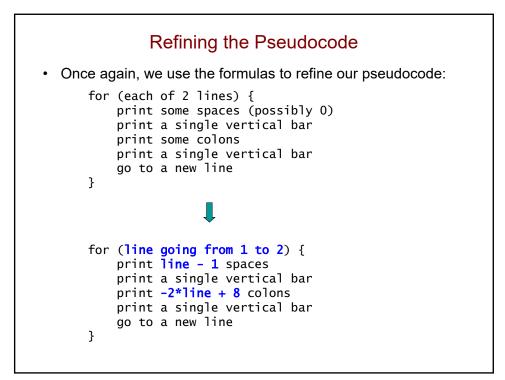
Finding the Formulas					
<ul> <li>To begin with, we: <ul> <li>number the lines in the flame</li> <li>form a table of the number of spaces and parentheses on each line:</li> </ul> </li> </ul>					
	2 2 3 1	<u>parens (eac</u> 1 2 3 4	<u>ch type)</u>		
<ul> <li>Then we find the formulas.</li> <li>assume the formulas are <i>linear functions</i> of the line number: c1*line + c2 where c1 and c2 are constants</li> <li>parens = ?</li> <li>spaces = ?</li> </ul>					

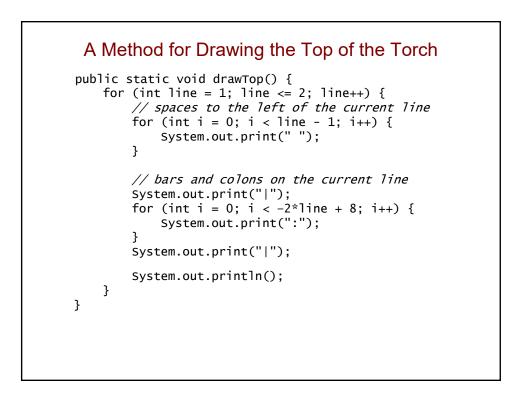


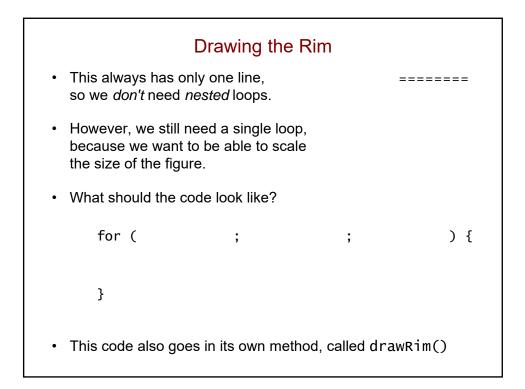


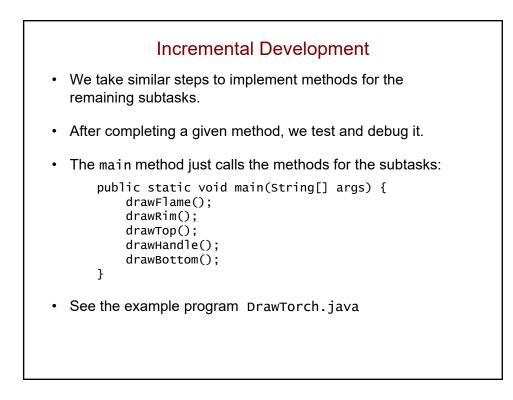


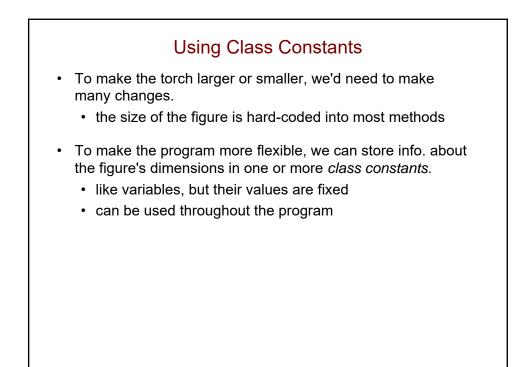


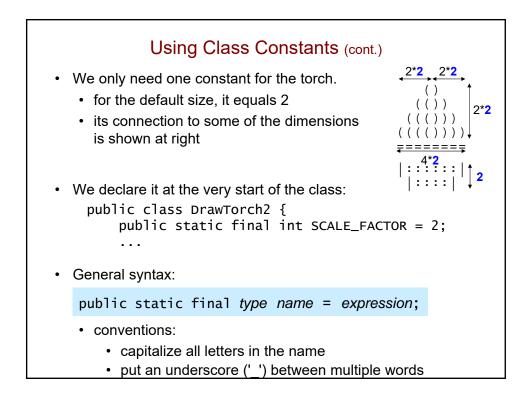


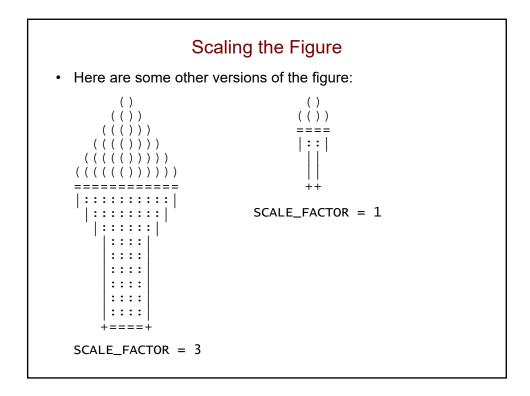


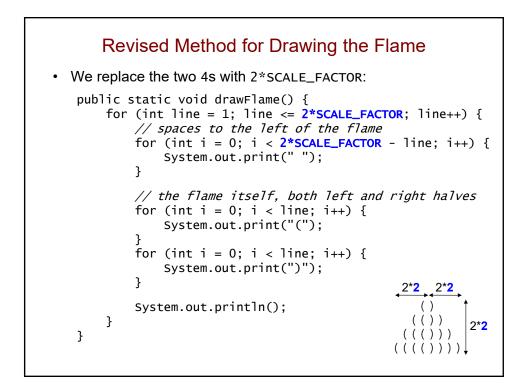


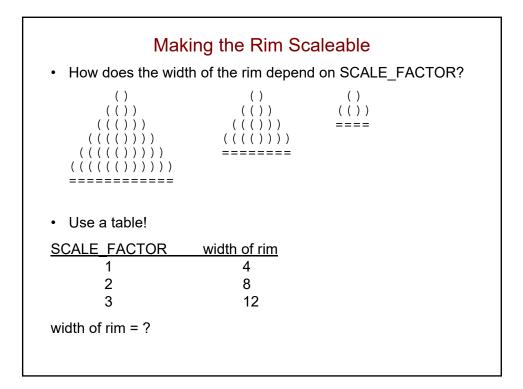


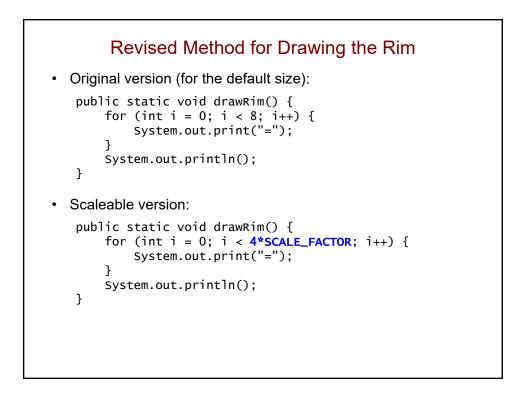


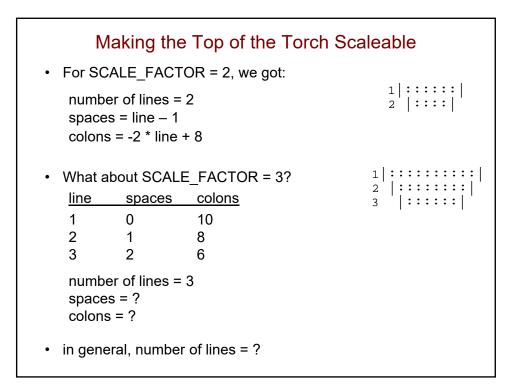


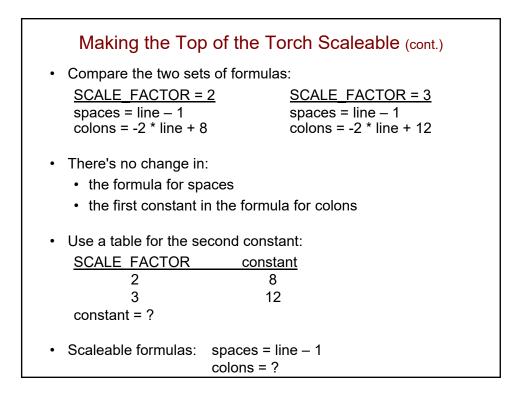


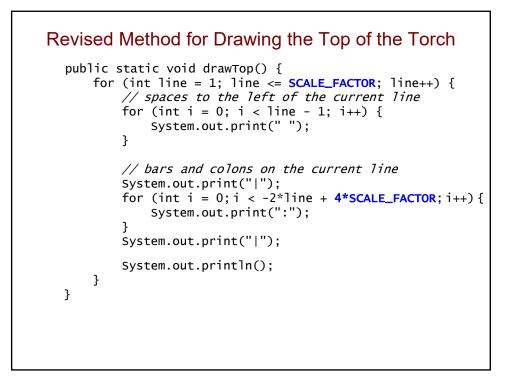


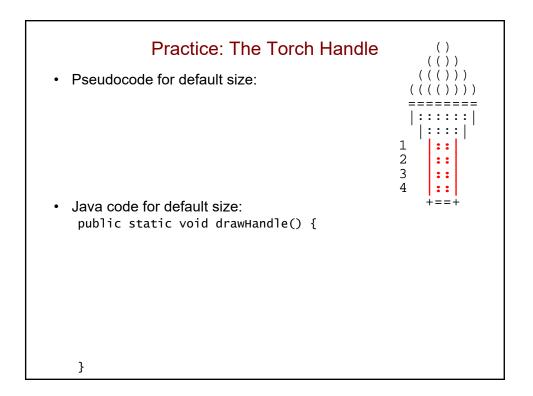


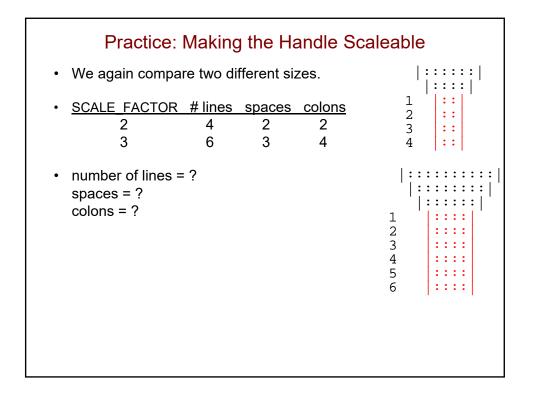


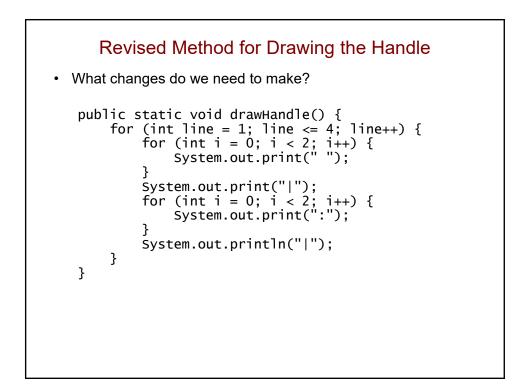


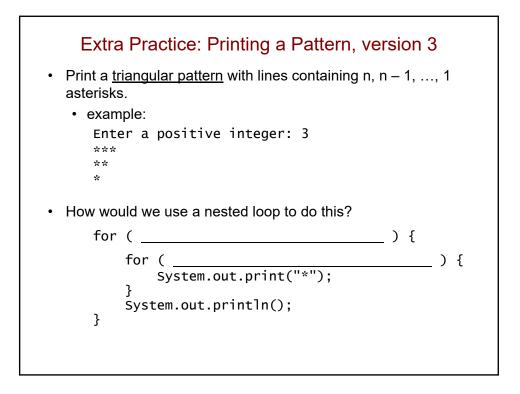


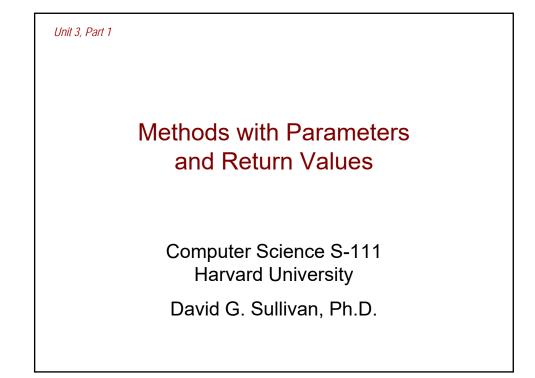


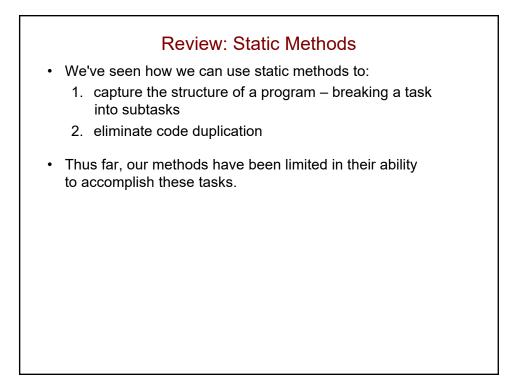












## A Limitation of Simple Static Methods

• For example, in our DrawTorch program, there are several for loops that each print a series of spaces, such as:

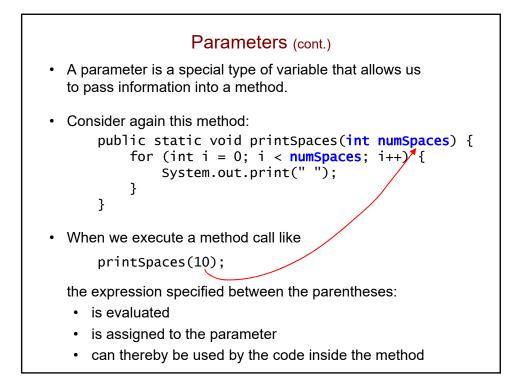
```
for (int i = 0; i < 4 - line; i++) {
    System.out.print(" ");
}
for (int i = 0; i < line - 1; i++) {
    System.out.print(" ");
}</pre>
```

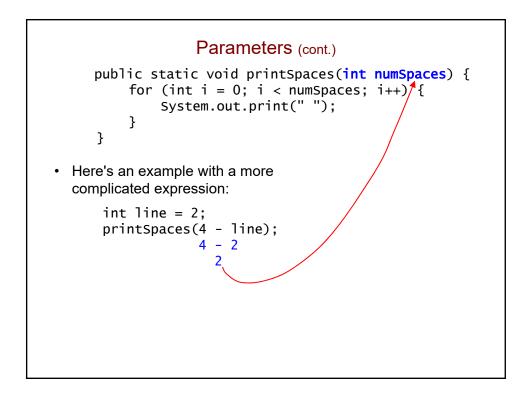
• However, despite the fact that all of these loops print spaces, we can't replace them with a method that looks like this:

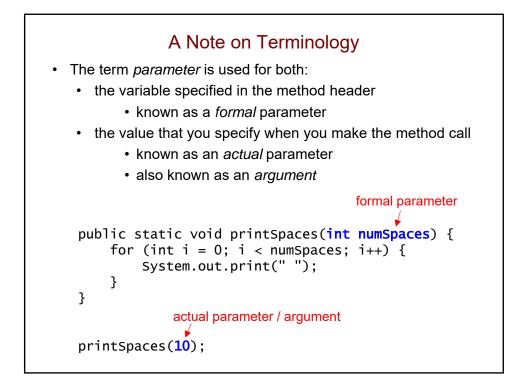
```
public static void printSpaces() {
```

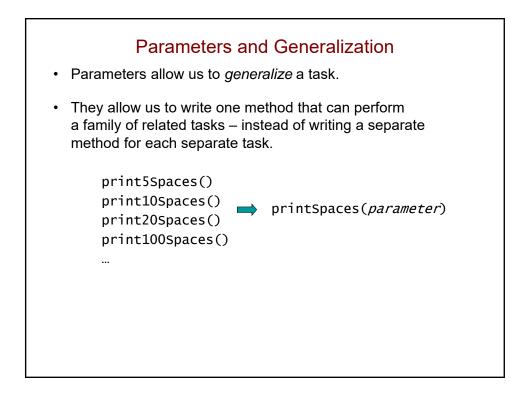
Why not?

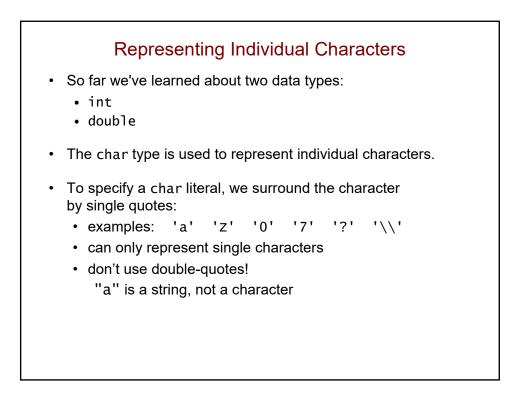
```
Parameters
• h order for a method that prints spaces to be useful,
we need one that can print an arbitrary number of spaces.
• Such a method would allow us to write commands like these:
    printSpaces(5);
    printSpaces(4 - line);
    where the number of spaces to be printed is specified
    between the parentheses.
• To do so, we write a method that has a parameter:
    public static void printSpaces(int numSpaces) {
        for (int i = 0; i < numSpaces; i++) {
            System.out.print(" ");
        }
    }
</pre>
```

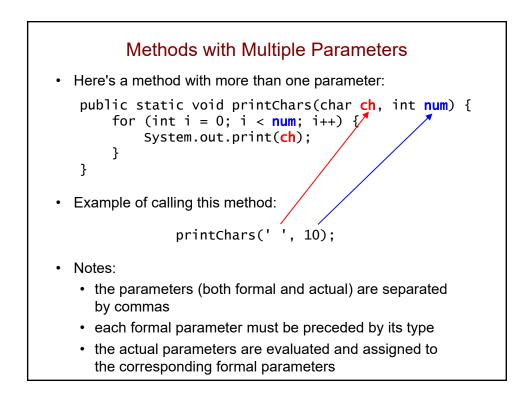


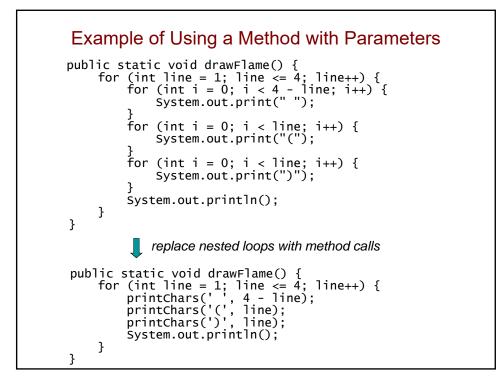


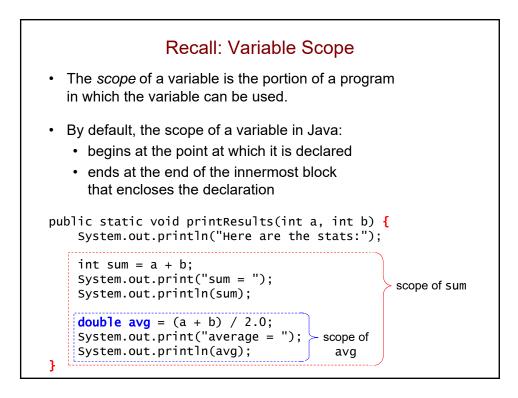


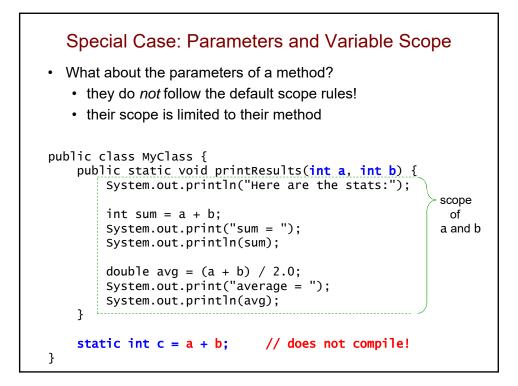








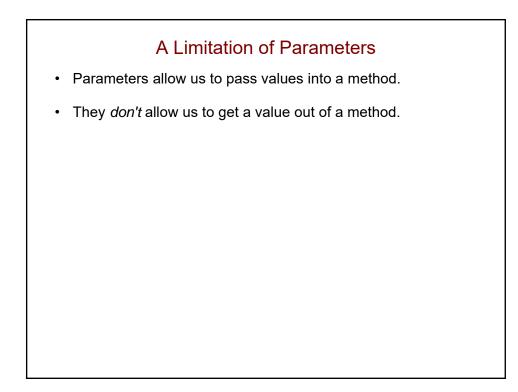


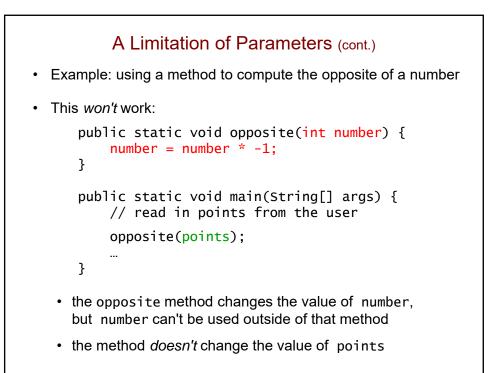


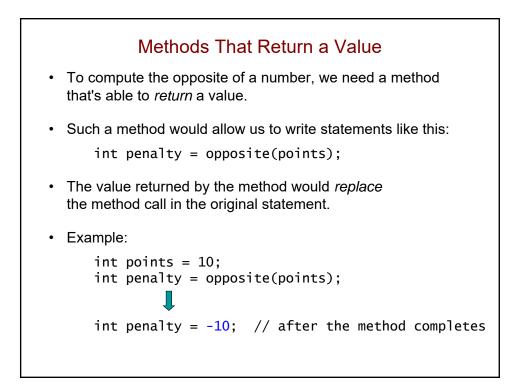
Practice with Scope				
public static void drawRectangle(int height) { for (int i = 0; i < height; i++) {				
// which variables could be used here?				
<pre>int width = height * 2; for (int j = 0; j &lt; width; j++) {     System.out.print("*");</pre>				
// what about here?				
}				
// what about here?				
System.out.println();				
} // what about here? }				
public static void repeatMessage(int numTimes) {				
// what about here?				
<pre>for (int i = 0; i &lt; numTimes; i++) {     System.out.println("what is your scope?"); }</pre>				
}				

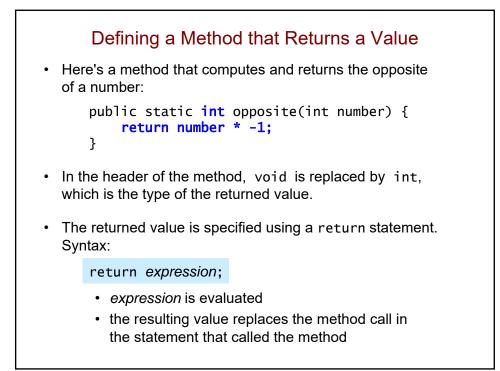
## **Practice with Parameters**

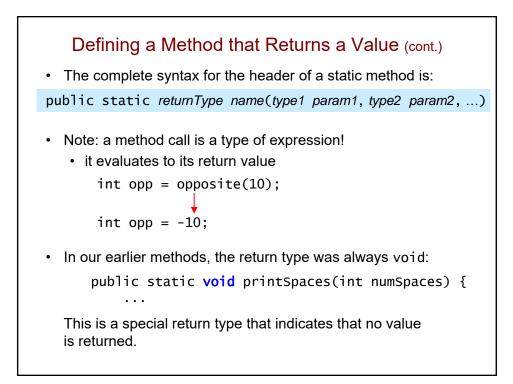
```
public static void printValues(int a, int b) {
    System.out.println(a + " " + b);
    b = 2 * a;
    System.out.println("b" + b);
}
public static void main(String[] args) {
    int a = 2;
    int b = 3;
    printValues(b, a);
    printValues(7, b * 3);
    System.out.println(a + " " + b);
}
• What's the output?
```

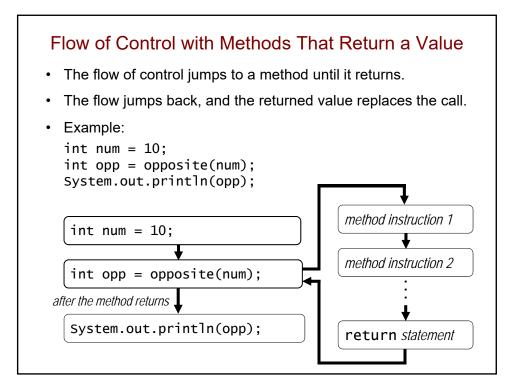


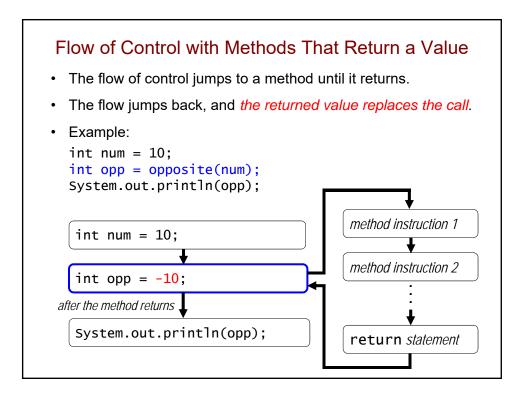


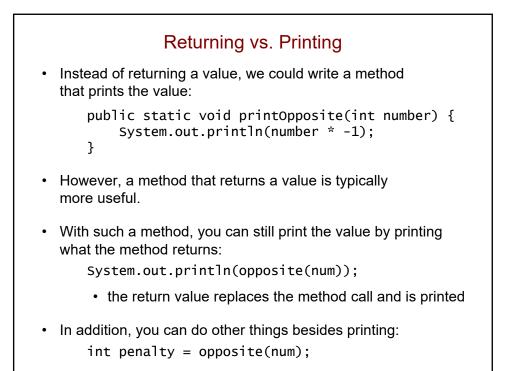


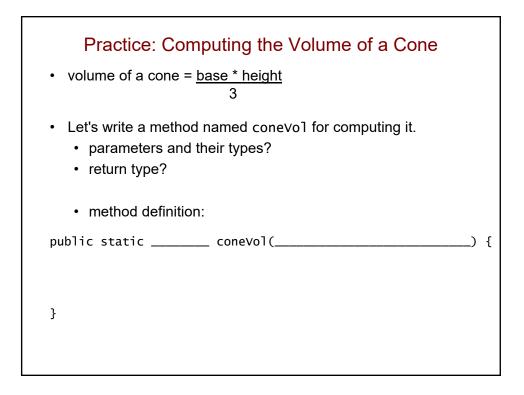


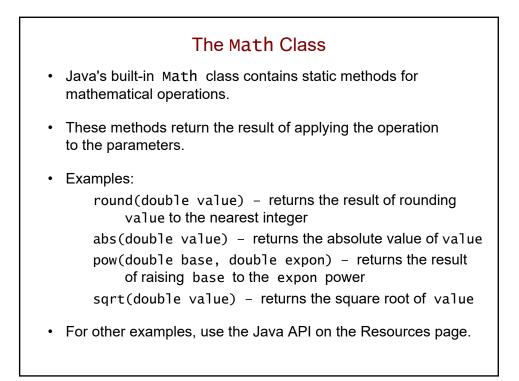


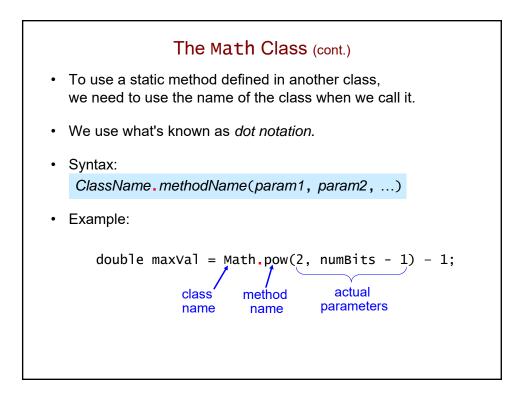


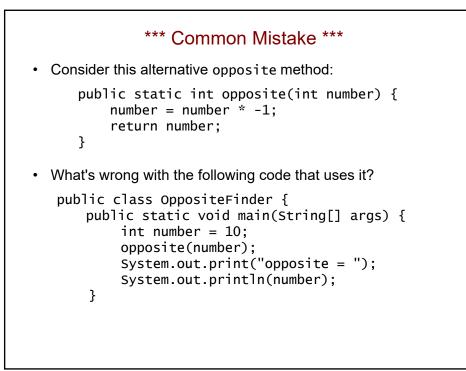


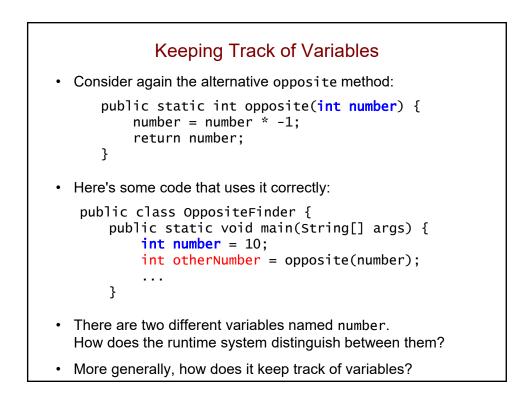




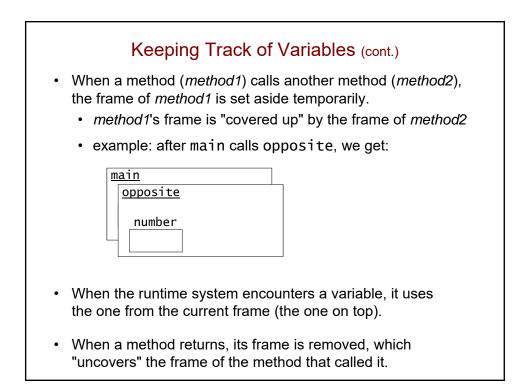


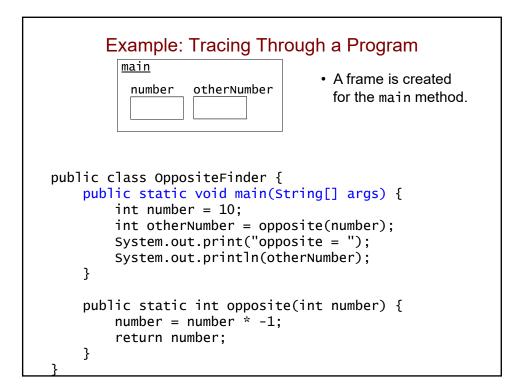


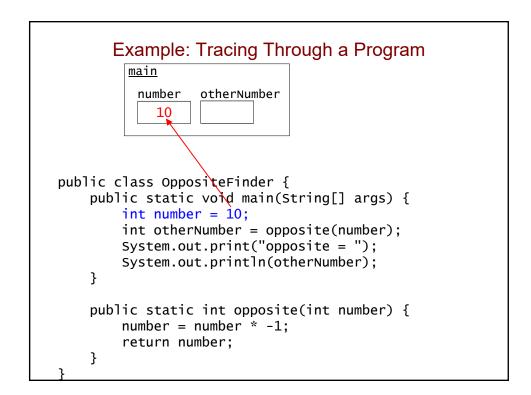


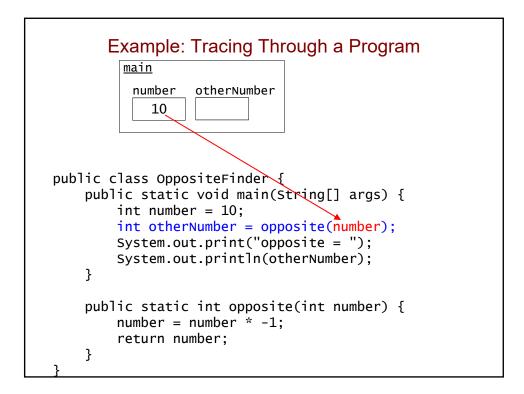


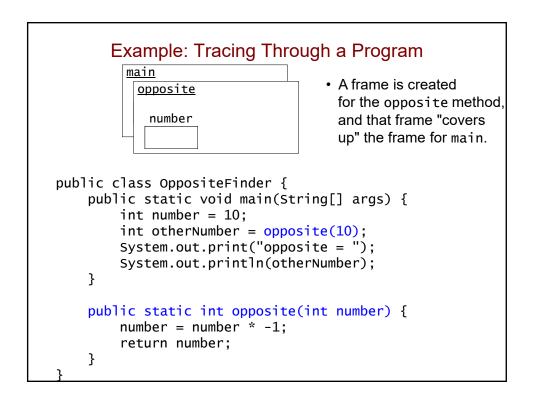
Keeping Track	of Variables (cont.)		
<ul> <li>When you make a method call, the Java runtime sets aside a block of memory known as the <i>frame</i> of that method call.</li> </ul>			
main			
number otherNumber	note: we're ignoring main's parameter for now		
<ul> <li>The frame is used to store:</li> <li>the formal parameters of</li> <li>any local variables – vari</li> </ul>	the method ables declared within the method		
<ul> <li>A given frame can only be a part of the corresponding me</li> </ul>	ccessed by statements that are ethod call.		

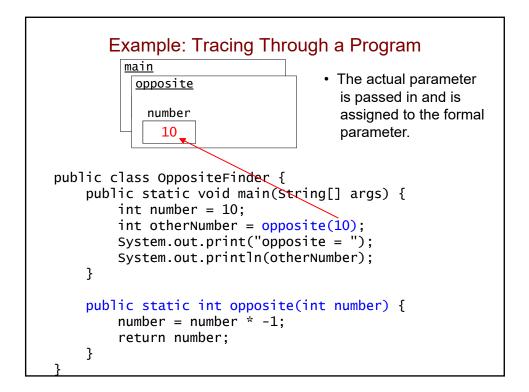


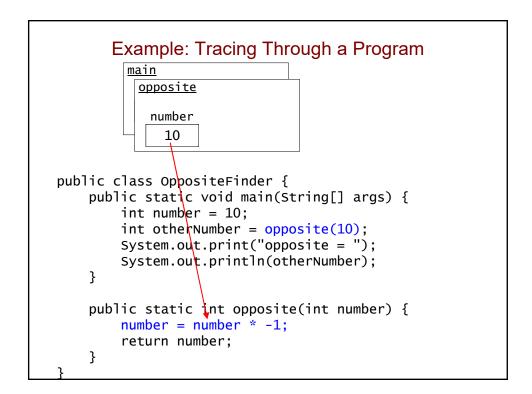


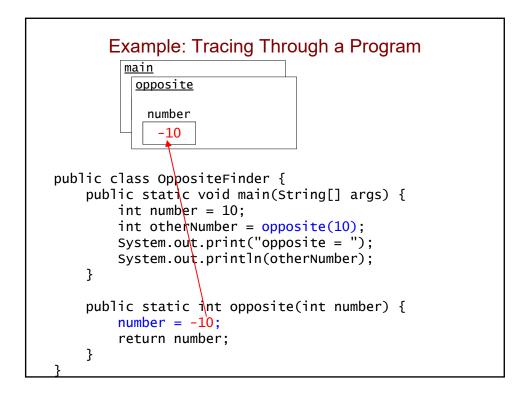


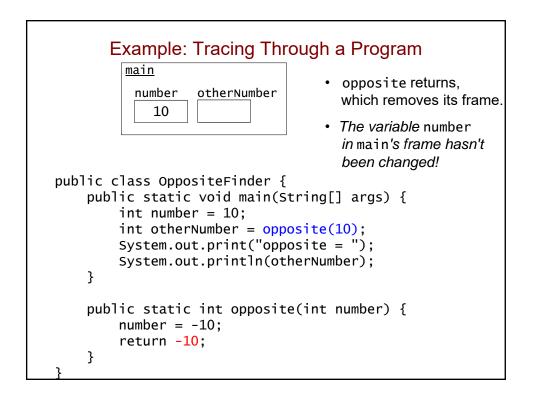


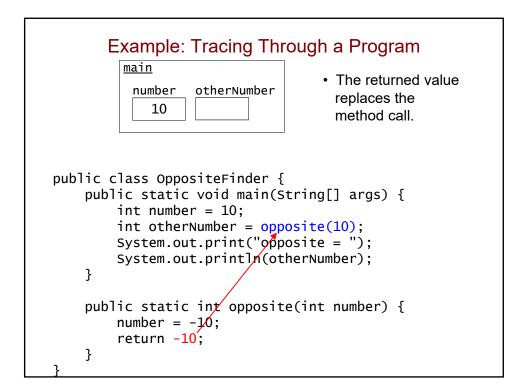


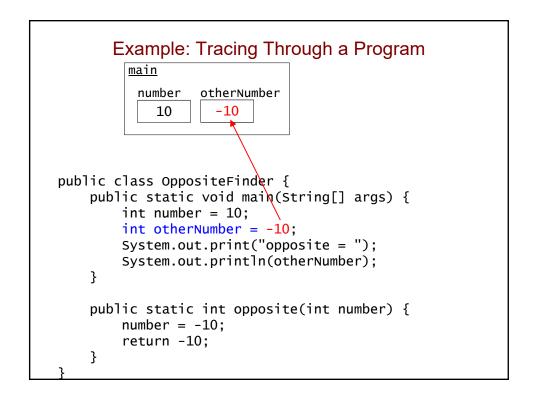


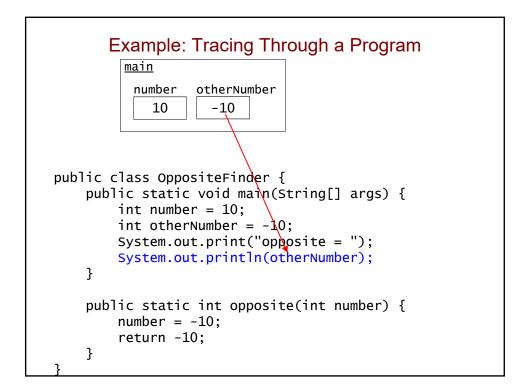


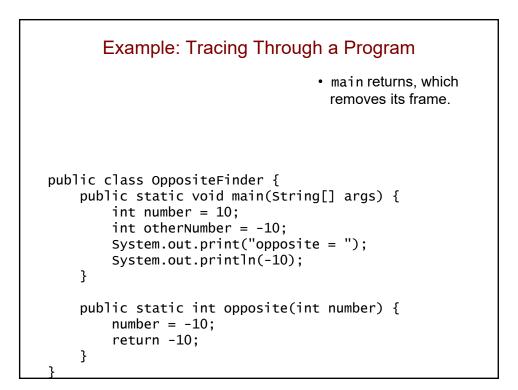






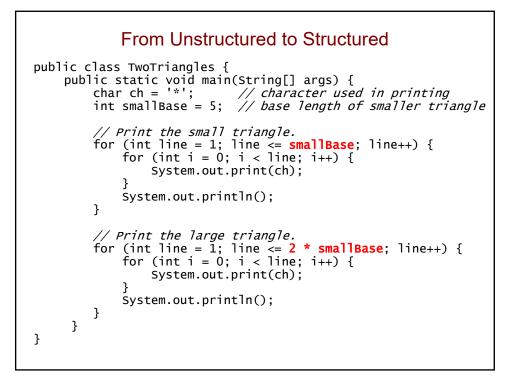


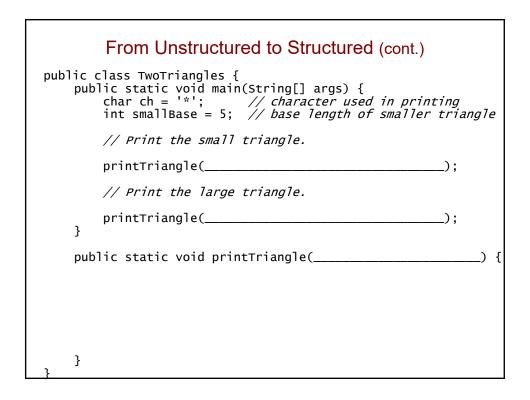


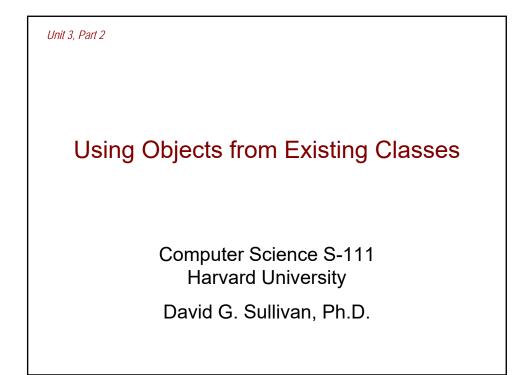


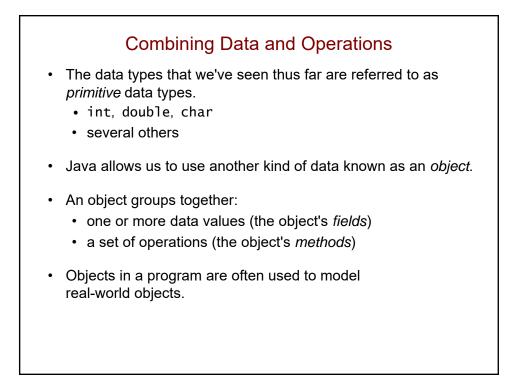
```
Practice
• What is the output of the following program?
public class MethodPractice {
    public static int triple(int x) {
        x = x * 3;
        return x;
    }
    public static void main(string[] args) {
        int y = 2;
        y = triple(y);
        System.out.println(y);
        triple(y);
        System.out.println(y);
    }
}
```

More Practic	$\frac{foo}{x \mid y}$
<pre>public class Mystery {     public static int foo(int x, int         v = v + 1;</pre>	: y) {
y = y + 1, x = x + y; System.out.println(x + " " + return x; }	- y);
<pre>public static void main(String[]     int x = 2;     int y = 0;</pre>	args) { <u>main</u> <u>x   y</u>
y = foo(y, x); System.out.println(x + " " +	- y);
foo(x, x); System.out.println(x + " " -	- y);
System.out.println(foo(x, y) System.out.println(x + " " + }	); - y);
}	

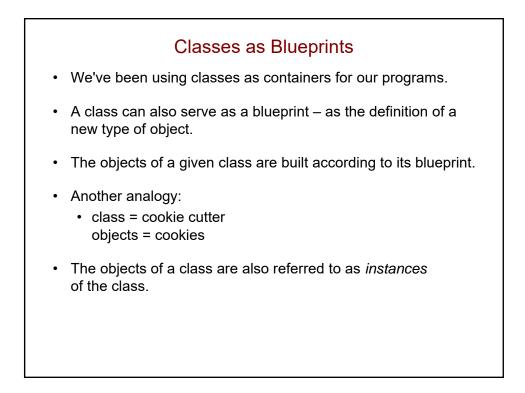


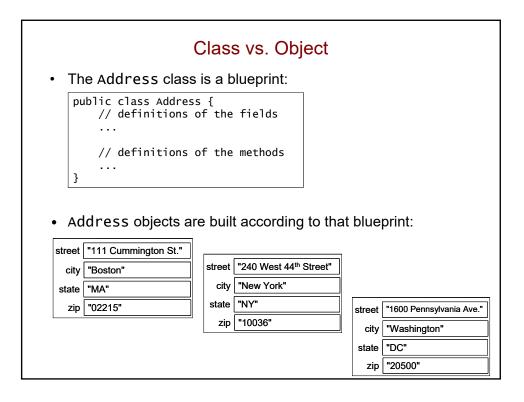


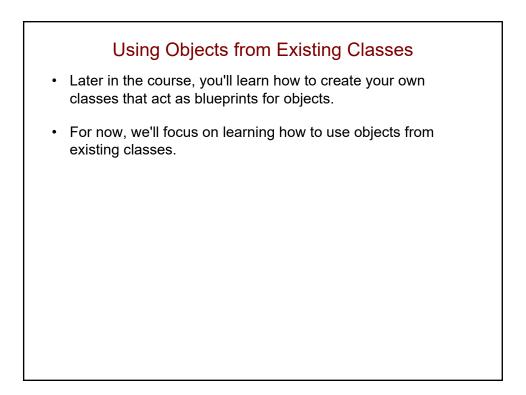


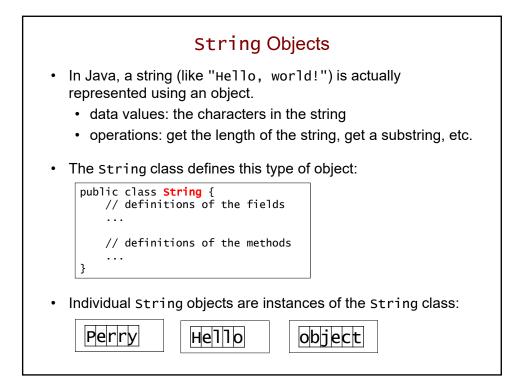


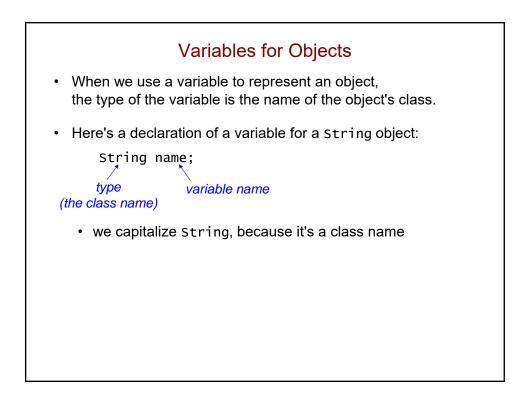
	ample: an Address ol possible fields: <i>stree</i>		e, zip		
<ul> <li>possible operations: get the city, change the city, check if two addresses are equal</li> </ul>					
• Her	e are two ways to vis				
street	-	])		, 	
city	"Boston"	fields	street	"111 Cummington St."	
state	"MA"		city	"Boston"	
zip	"02215"		state	"MA"	
		)	zip	"02215"	
getCi				L	

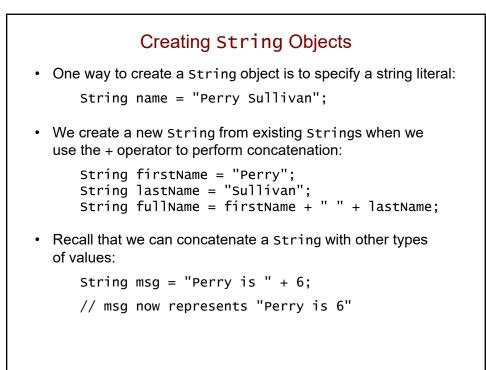


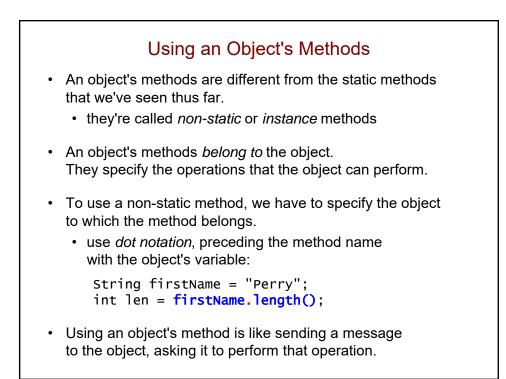


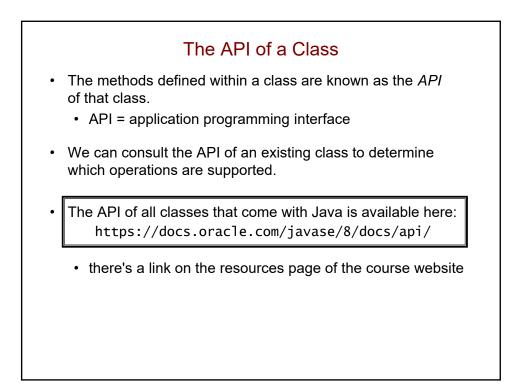


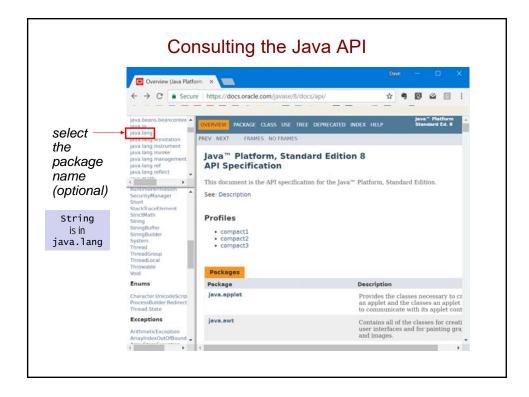




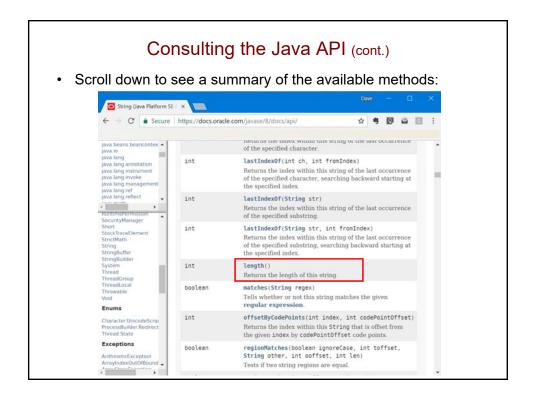




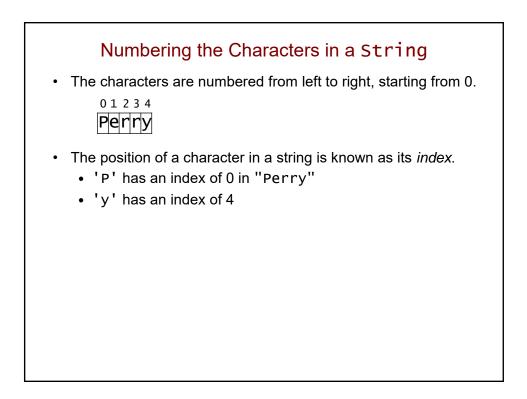


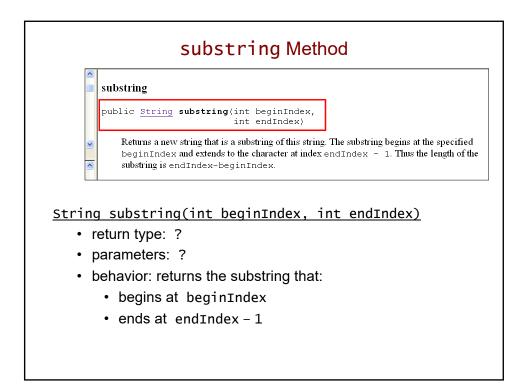


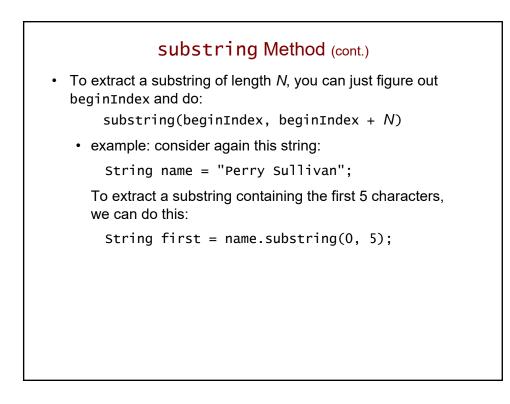




<ul> <li>Consulting the Java API (cont.)</li> <li>Clicking on a method name gives you more information:</li> </ul>				
	length			
	public int length() method header			
behavior	Returns the length of this string. The length is equal to the number of Unicode code units in the string.			
	Specified by: length in interface CharSequence			
	Returns:			
	the length of the sequence of characters represented by this object.			
<ul> <li>From the header, we can determine:</li> <li>the return type: int</li> </ul>				
	the parameters we need to supply: the empty () indicates that length has no parameters			





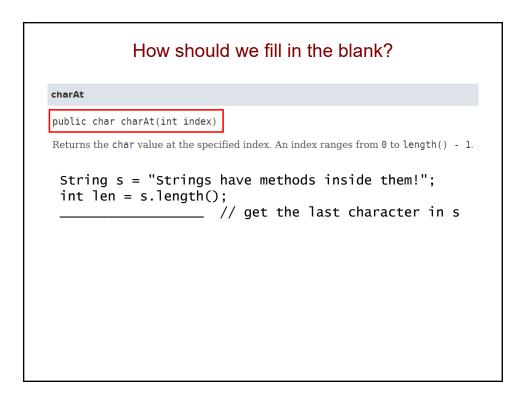


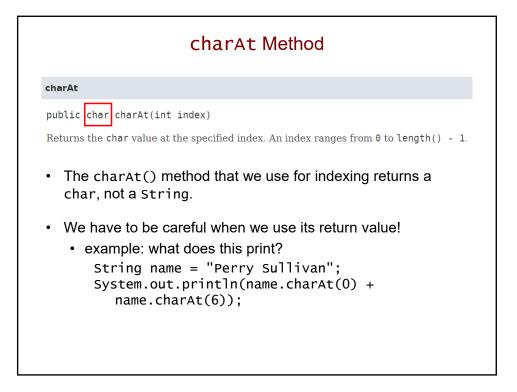
## Review: Calling a Method

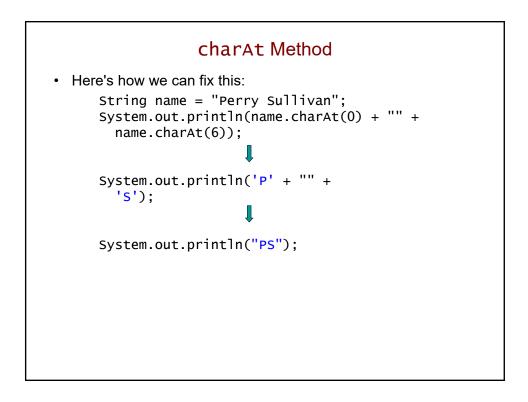
Consider this code fragment:

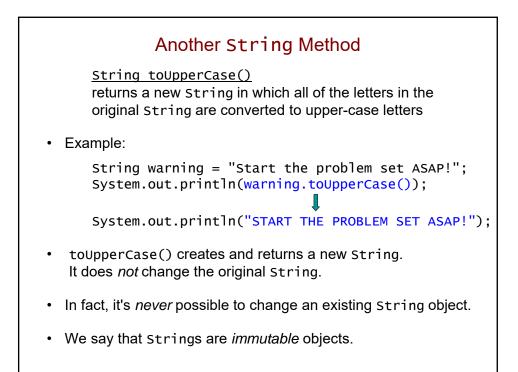
```
String name = "Perry Sullivan";
int start = 6;
String last = name.substring(start, start + 8);
```

- Steps for executing the method call:
  - 1. the actual parameters are evaluated to give: String last = name.substring(6, 14);
  - 2. a frame is created for the method, and the actual parameters are assigned to the formal parameters
  - 3. flow of control jumps to the method, which creates and returns the substring "Sullivan"
  - flow of control jumps back, and the returned value replaces the method call: String last = "Sullivan";

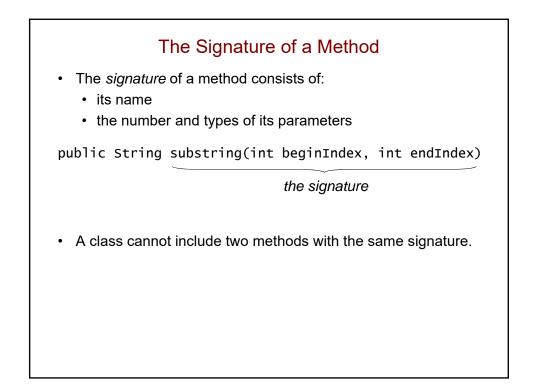


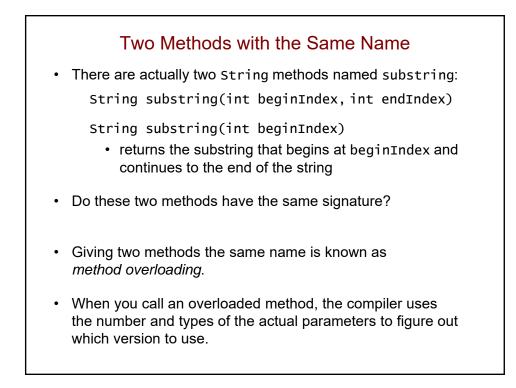


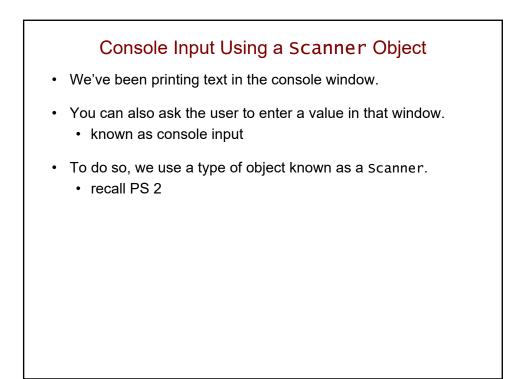


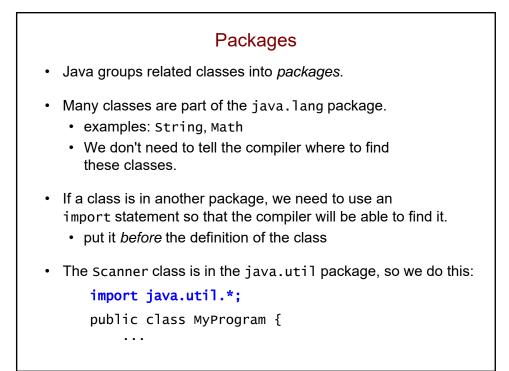


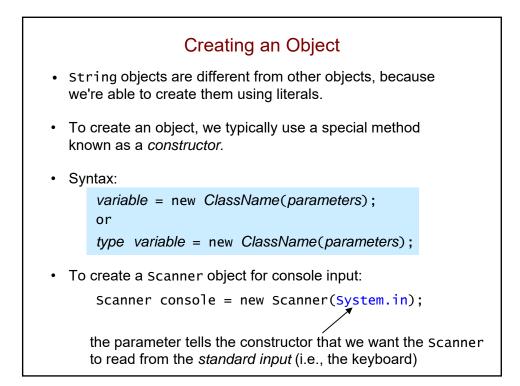
index0f Method
<pre>indexOf Method int indexOf(char ch)</pre>

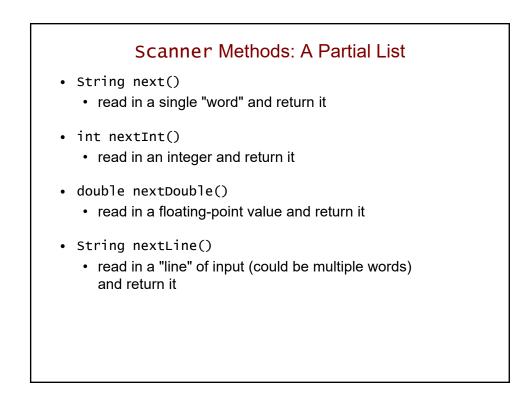










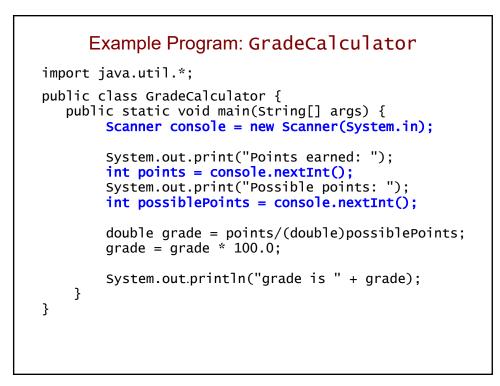


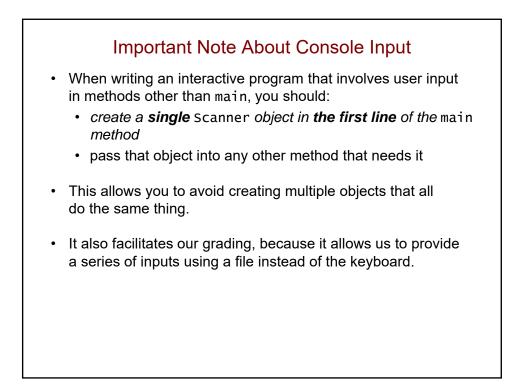
## Example of Using a Scanner Object

• To read an integer from the user:

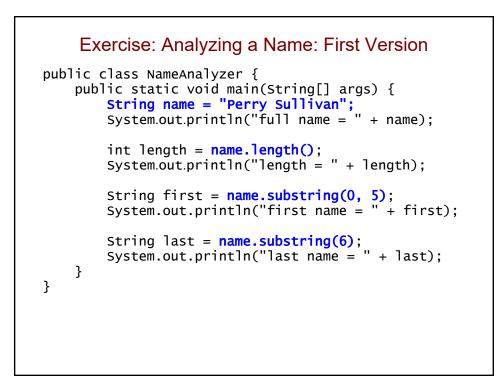
```
Scanner console = new Scanner(System.in);
int numGrades = console.nextInt();
```

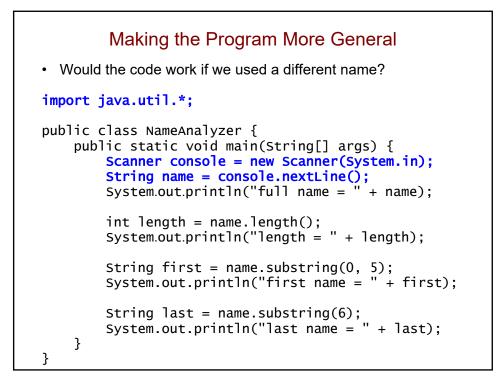
- The second line causes the program to pause until the user types in an integer followed by the [ENTER] key.
- If the user only hits [ENTER], it will continue to pause.
- If the user enters an integer, it is returned and assigned to numGrades.
- If the user enters a non-integer, an exception is thrown and the program crashes.

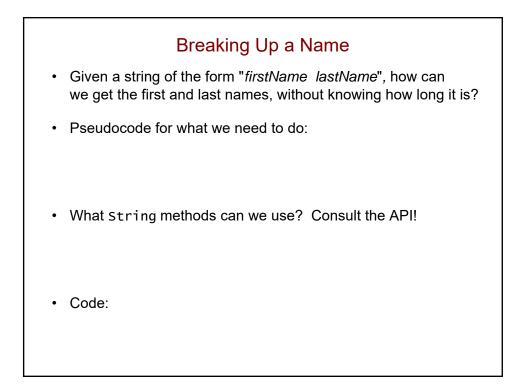


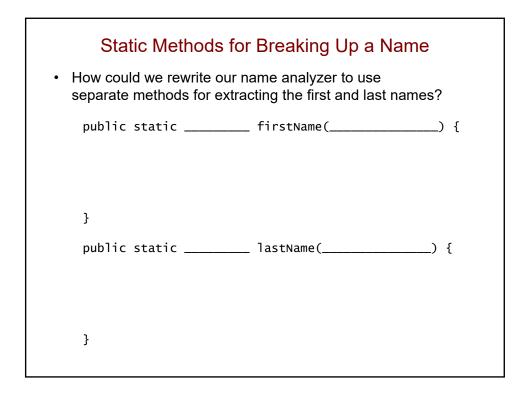


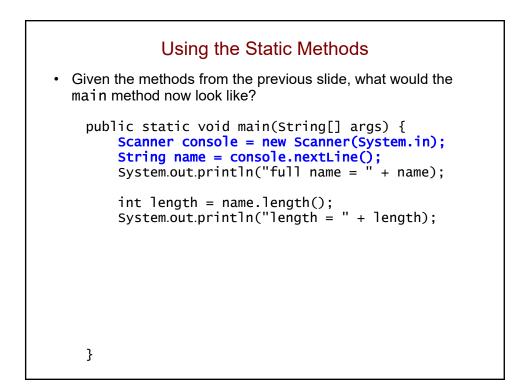
Important Note About Console Input (cont.)				
• Example:				
<pre>public class MyProgram {     public static void main(String[] args) {         Scanner console = new Scanner(System.in);         String str1 = getString(console);         String str2 = getString(console);         System.out.println(str1 + " " + str2);     } </pre>				
<pre>public static String getString(Scanner console) {     System.out.print("Enter a string: ");     String str = console.next();     return str; }</pre>				
}				

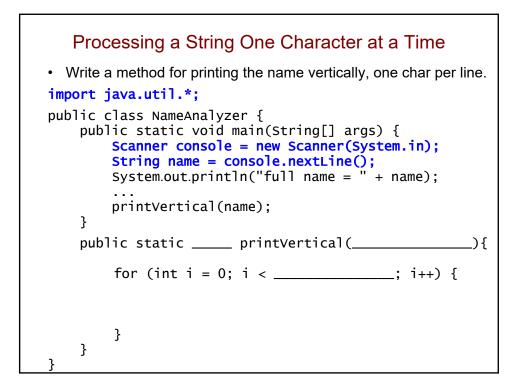


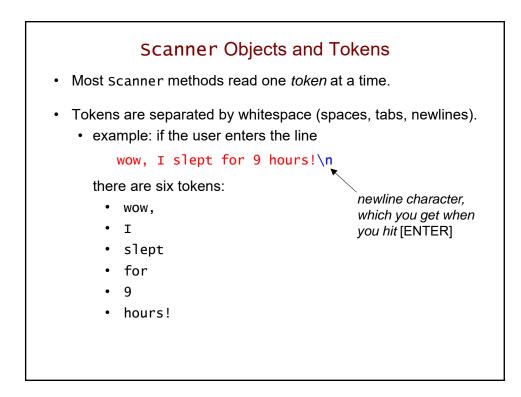


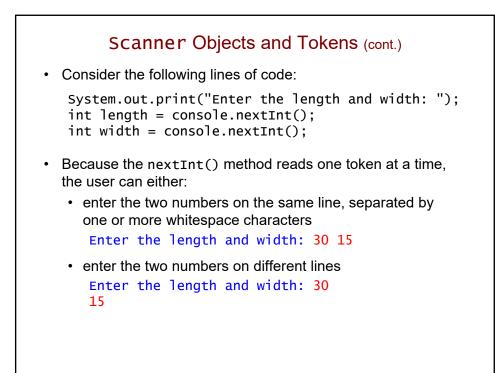


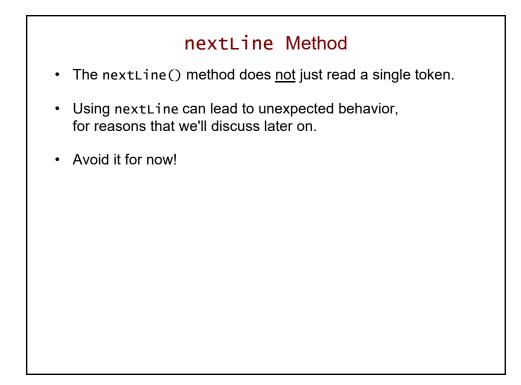






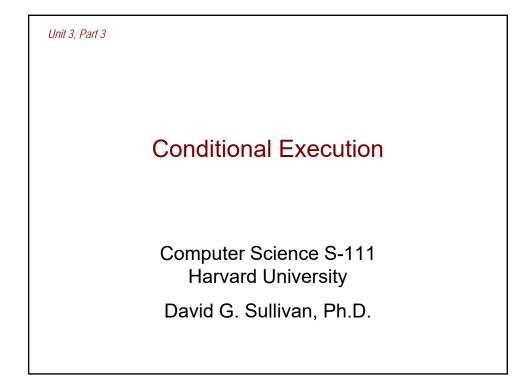


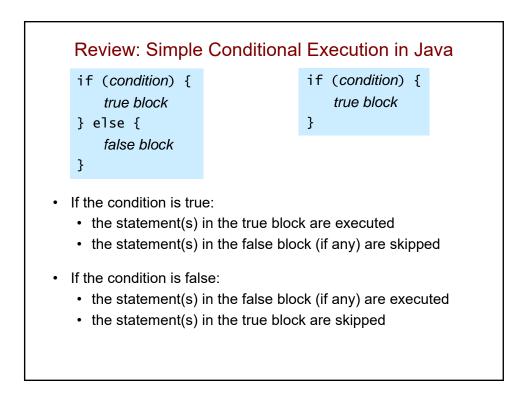




## Additional Terminology

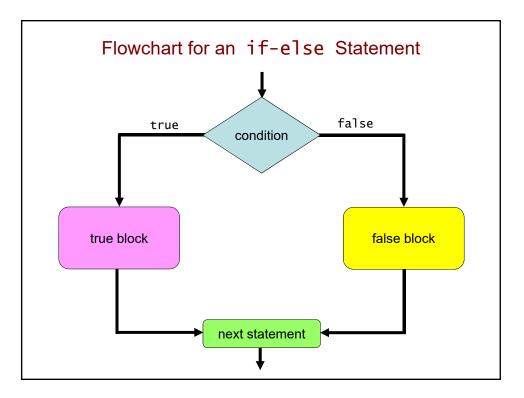
- To avoid having too many new terms at once, I've limited the terminology introduced in these notes.
- Here are some additional terms related to classes, objects, and methods:
  - *invoking* a method = calling a method
  - method *invocation* = method call
  - the *called object* = the object used to make a method call
  - *instantiate* an object = create an object
  - *members* of a class = the fields and methods of a class

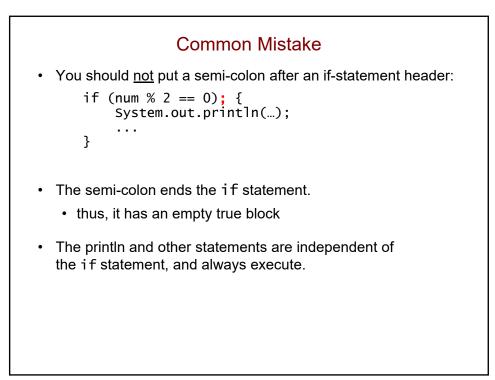


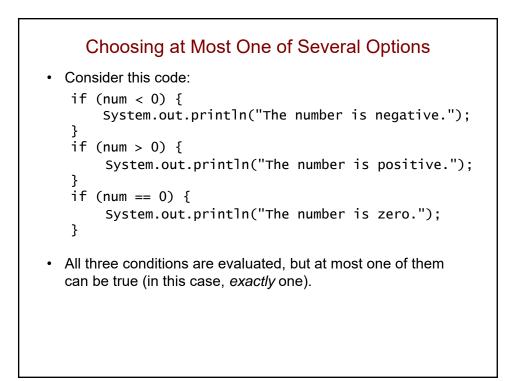


## Example: Analyzing a Number

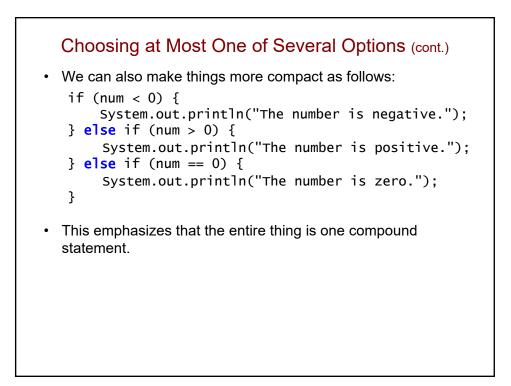
```
Scanner console = new Scanner(System.in);
System.out.print("Enter an integer: ");
int num = console.nextInt();
if (num % 2 == 0) {
   System.out.println(num + " is even.");
} else {
   System.out.println(num + " is odd.");
}
```

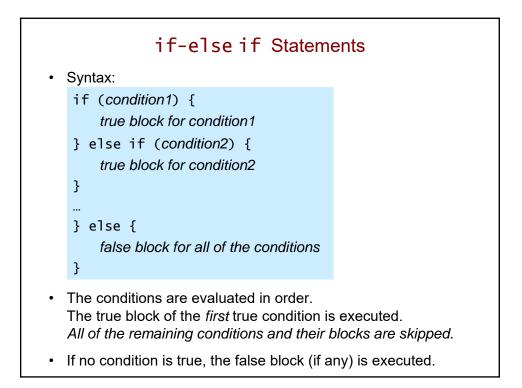


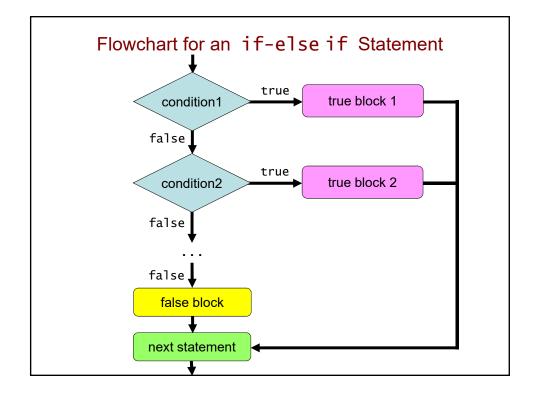




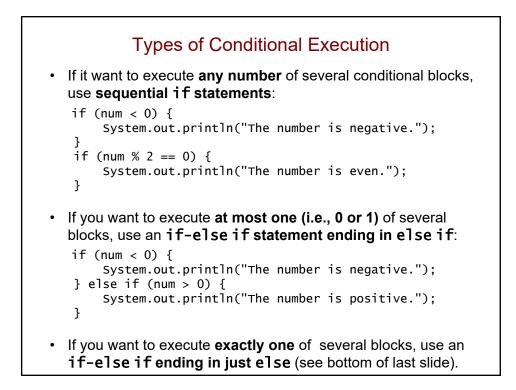
```
Choosing at Most One of Several Options (cont.)
• We can do this instead:
    if (num < 0) {
        System.out.println("The number is negative.");
    }
    else if (num > 0) {
        System.out.println("The number is positive.");
    }
    else if (num == 0) {
        System.out.println("The number is zero.");
    }
• If the first condition is true, it will skip the second and third.
• If the first condition is false, it will evaluate the second, and if the second condition is true, it will skip the third.
• If the second condition is false, it will evaluate the third, etc.
```



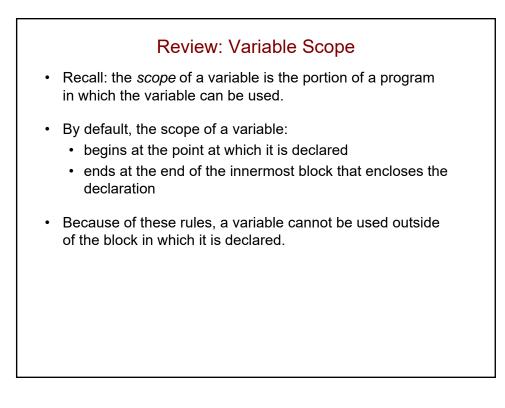


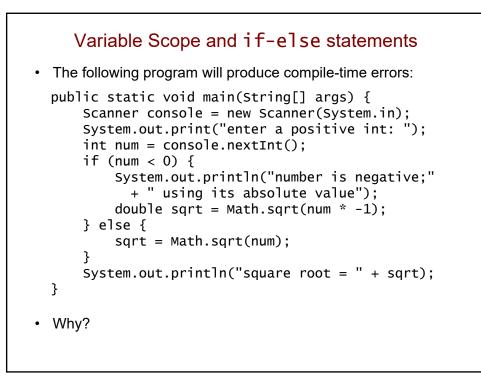


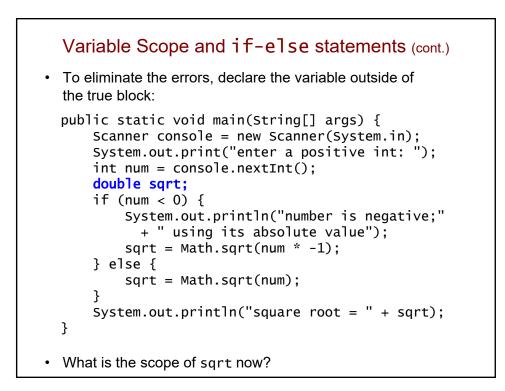
**Choosing Exactly One Option** Consider again this code fragment: if (num < 0) { System.out.println("The number is negative."); } else if (num > 0) { System.out.println("The number is positive."); } else if (num == 0) { System.out.println("The number is zero."); } One of the conditions must be true, so we can omit the last one: if (num < 0) { System.out.println("The number is negative."); } else if (num > 0) { System.out.println("The number is positive."); } else { System.out.println("The number is zero."); }

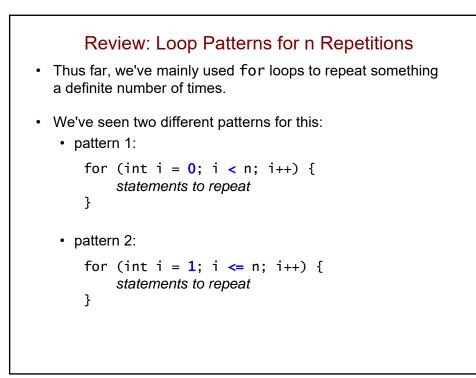


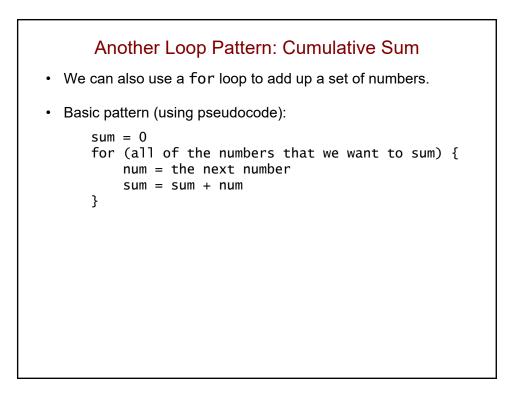
# Find the Logic Error Scanner console = new Scanner(System.in); System.out.print("Enter the student's score: "); int score = console.nextInt(); String grade; if (score >= 90) { grade = "A"; } if (score >= 80) { grade = "B"; } if (score >= 70) { grade = "C"; } if (score >= 60) { grade = "D"; }

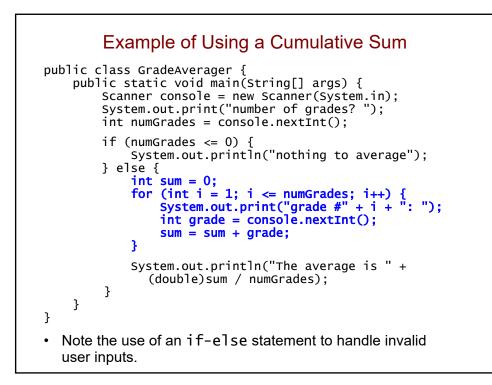


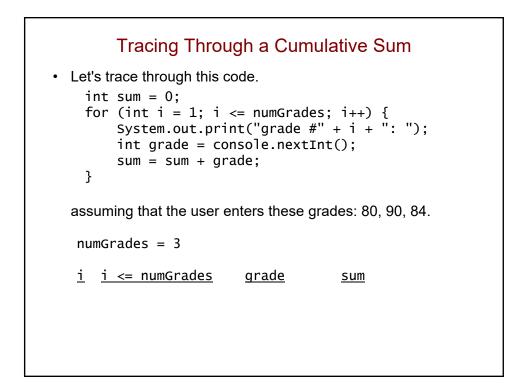


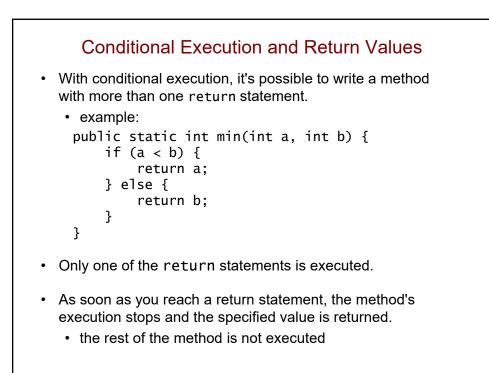


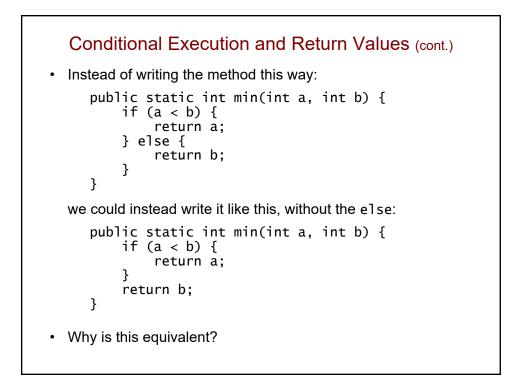


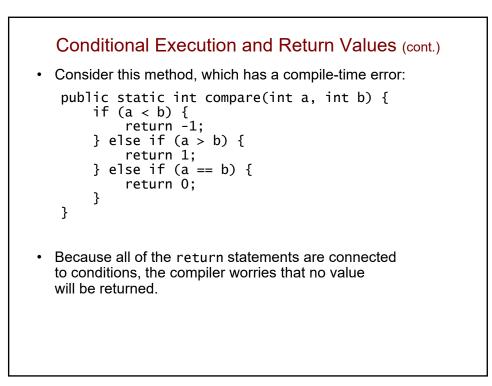


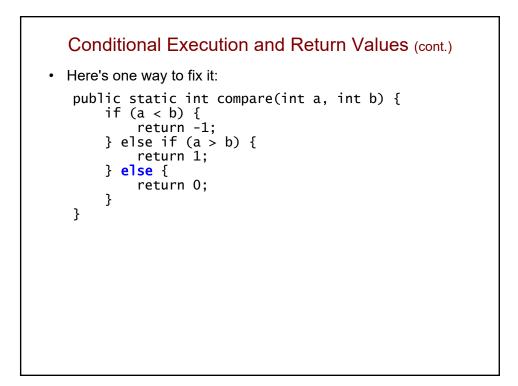


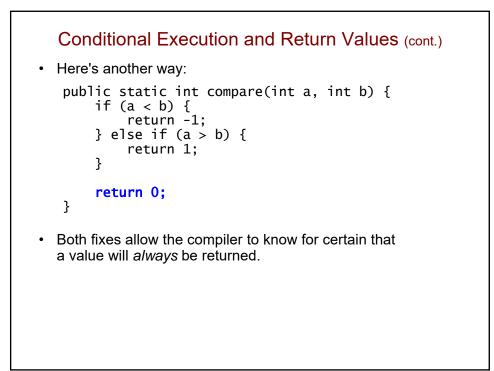


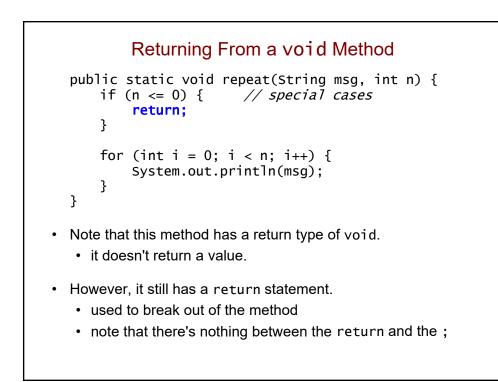


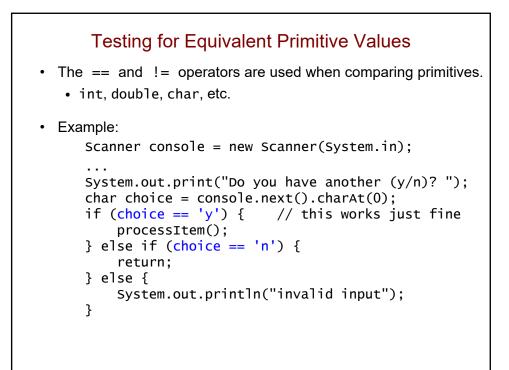


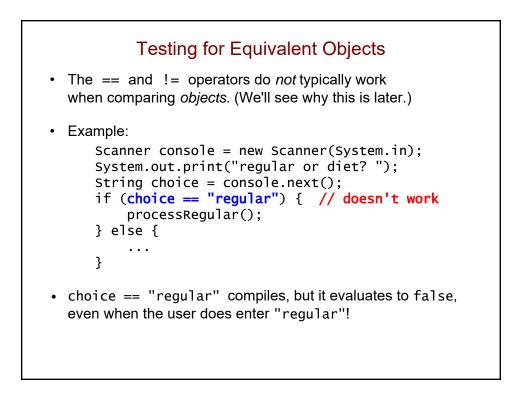


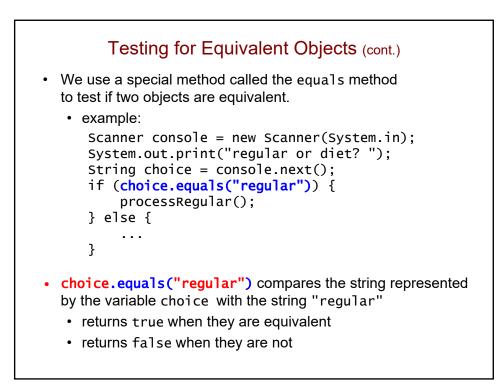


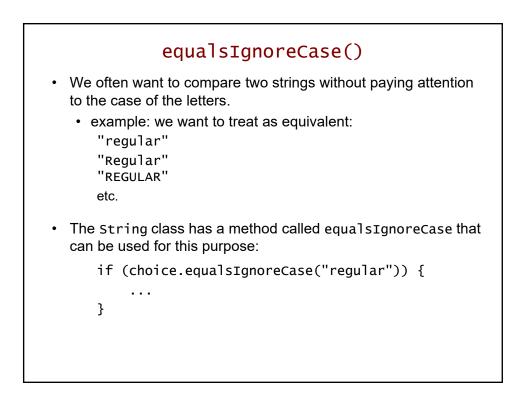












## Example Problem: Ticket Sales Different prices for balcony seats and orchestra seats Here are the rules: • persons younger than 25 receive discounted prices: • \$20 for balcony seats

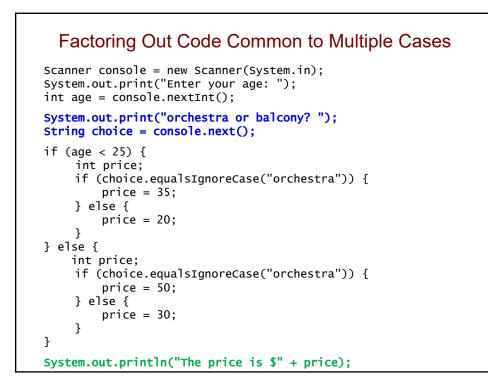
- \$35 for orchestra seats
- everyone else pays the regular prices:
  - \$30 for balcony seats
  - \$50 for orchestra seats
- · Assume only valid inputs.

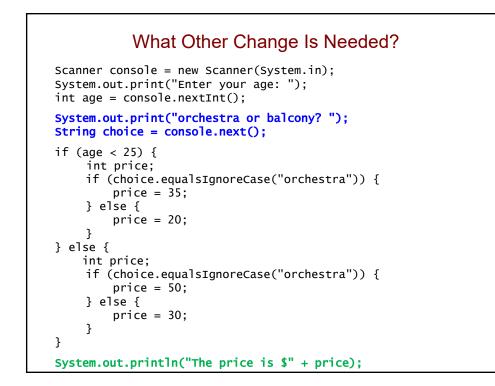
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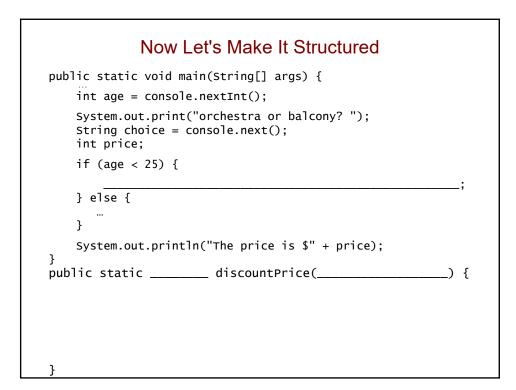
### Ticket Sales Program: main method Scanner console = new Scanner(System.in); System.out.print("Enter your age: "); int age = console.nextInt(); if (age < 25) { // handle people younger than 25 System.out.print("orchestra or balcony? "); String choice = console.next(); int price; if (choice.equalsIgnoreCase("orchestra")) { price = 35;} else { price = 20;} System.out.println("The price is \$" + price); } else { // handle people 25 and older . . . }

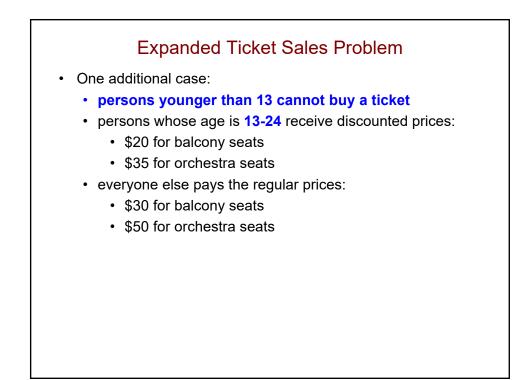
## Ticket Sales Program: main method (cont.) ... } else { // handle people 25 and older System.out.print("orchestra or balcony? "); String choice = console.next(); int price; if (choice.equalsIgnoreCase("orchestra")) { price = 50; } else { price = 30; } System.out.println("The price is \$" + price); }

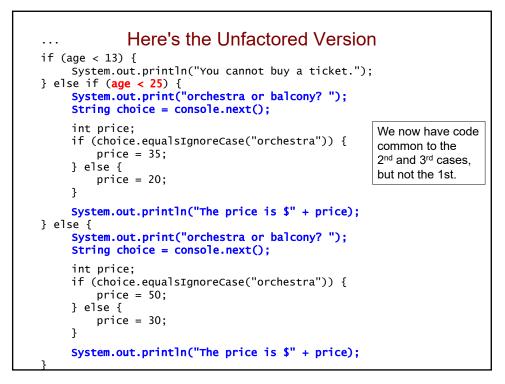
	Where Is the Code Duplication?
if (a	age < 25) { System.out.print("orchestra or balcony? "); String choice = console.next();
	<pre>int price; if (choice.equalsIgnoreCase("orchestra")) { price = 35; } else { price = 20; }</pre>
} els	System.out.println("The price is \$" + price); se { System.out.print("orchestra or balcony? "); String choice = console.next();
	<pre>int price; if (choice.equalsIgnoreCase("orchestra")) { price = 50; } else { price = 30; }</pre>
}	System.out.println("The price is \$" + price);

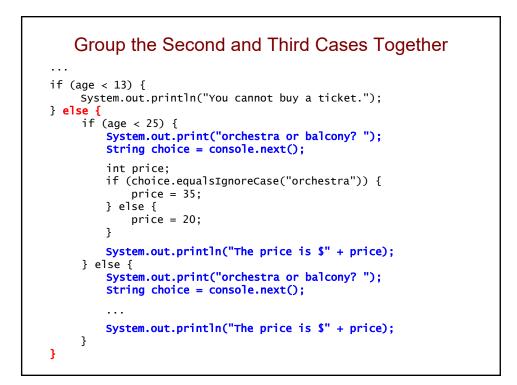


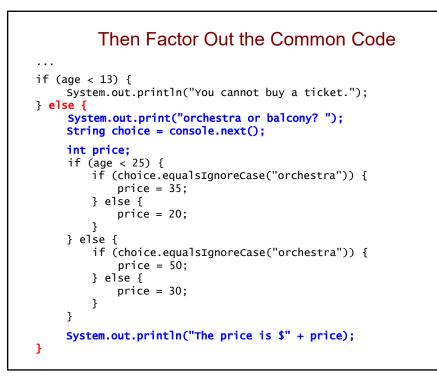


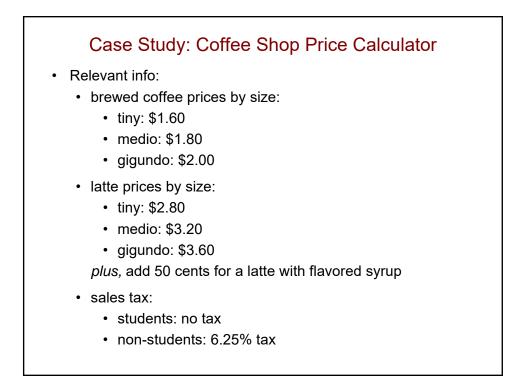








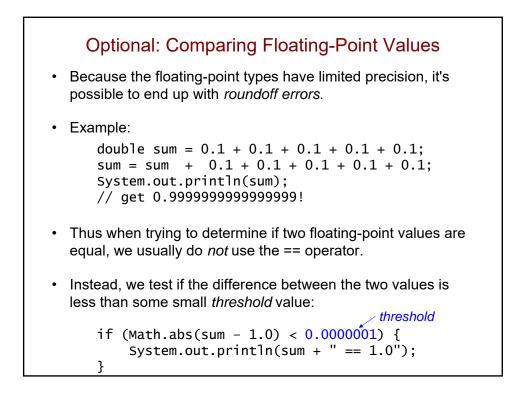


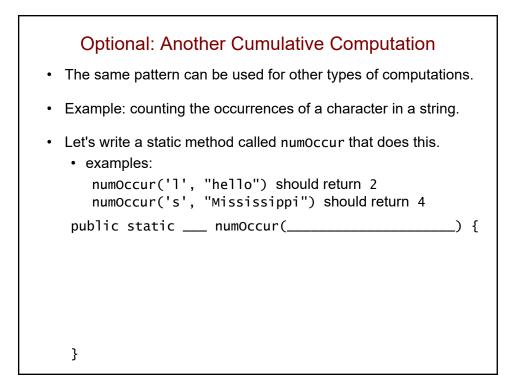


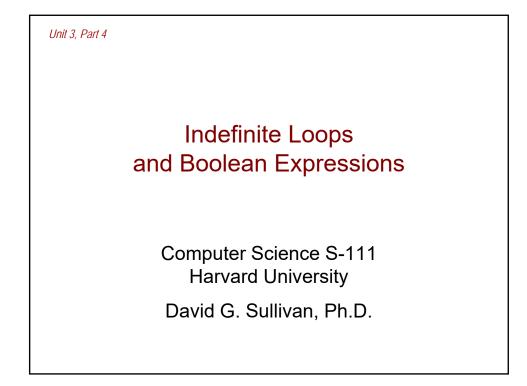


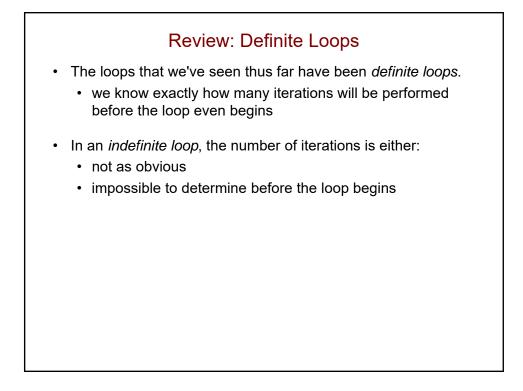
- Developing a solution:
  - 1. Begin with an *unstructured* solution.
    - everything in the main method
    - use if-else-if statement(s) to handle the various cases
  - 2. Next, factor out code that is common to multiple cases.
    - put it either before or after the appropriate if-else-if statement
  - 3. Finally, create a fully *structured* solution.
    - use procedural decomposition to capture logical pieces of the solution

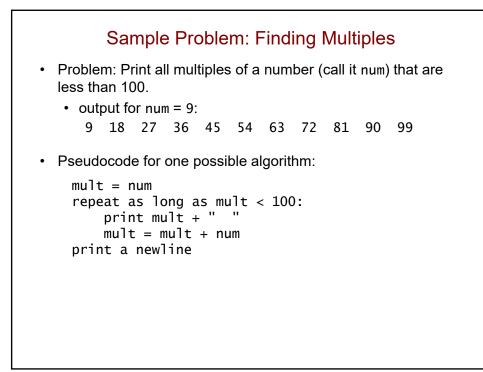
Case Study: Coffee Shop Price Calculator (cont.)

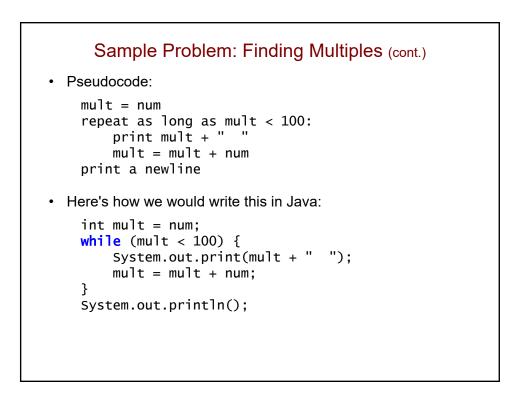


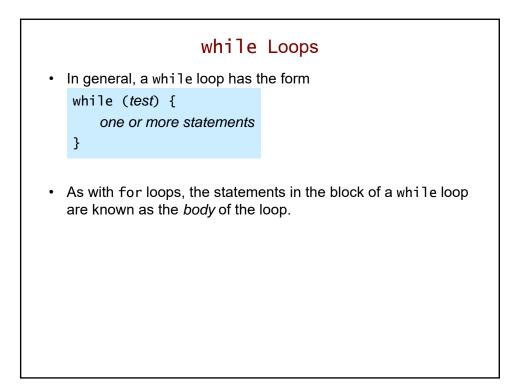


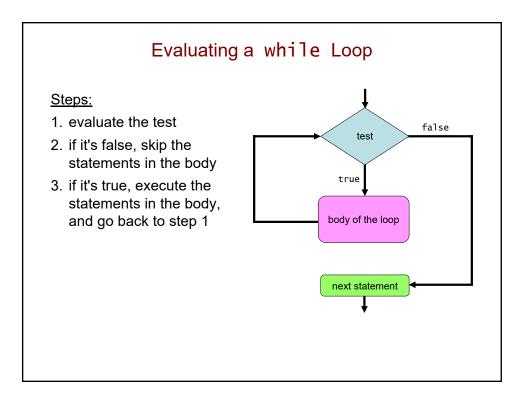




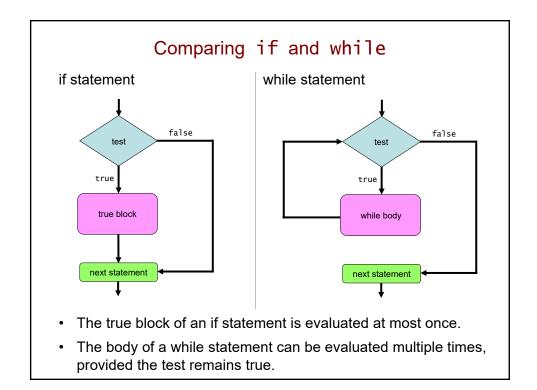


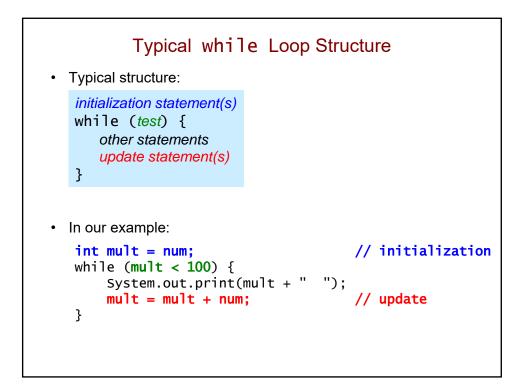


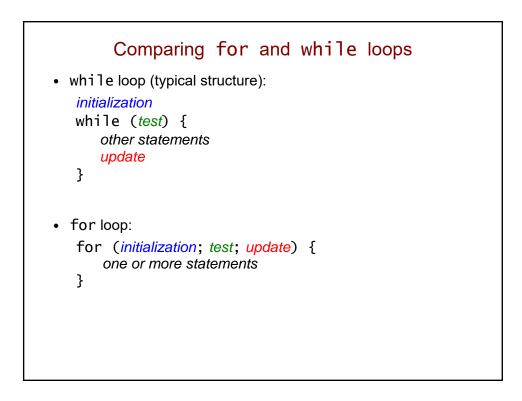


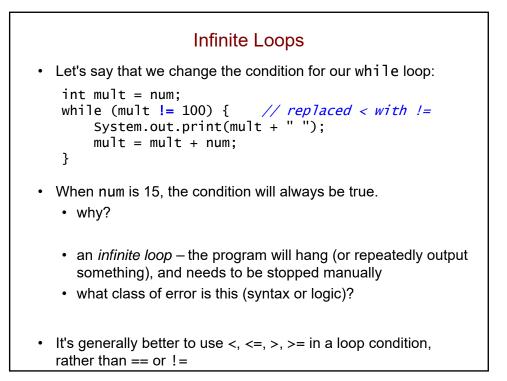


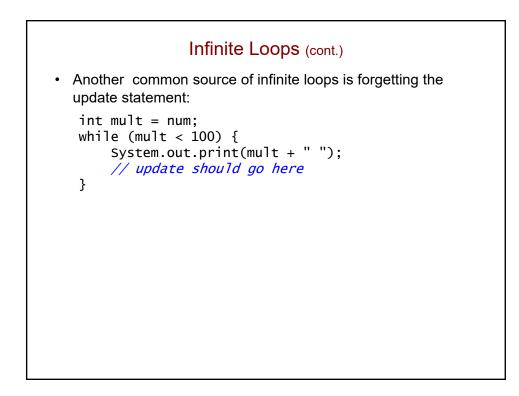
Tracing a while Loop			
<ul> <li>Let's trace through our code when num has the value 15:</li> </ul>			
<pre>int mult = num; while (mult &lt; 100) { System.out.print(mult + " "); mult = mult + num; }</pre>			
	output thus far	<u>mult</u>	
before entering the loop		15	
after the first iteration	15	30	
after the second iteration	15 30	45	
after the third iteration	15 30 45	60	
after the fourth iteration	15 30 45 60	75	
after the fifth iteration	15 30 45 60 75	90	
after the sixth iteration	15 30 45 60 75 90	105	
and now (mult < 100) is false, so we exit the loop			









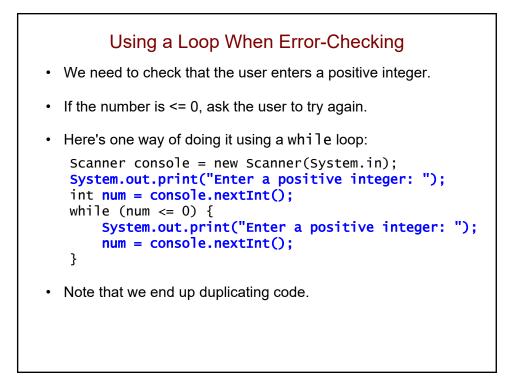


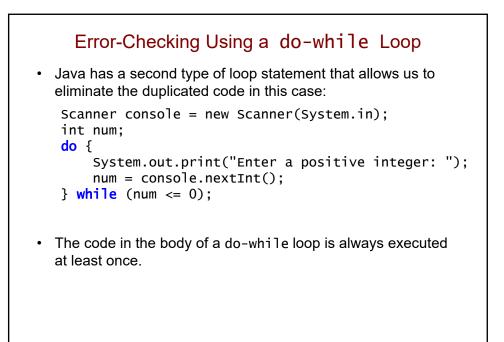
## A Need for Error-Checking

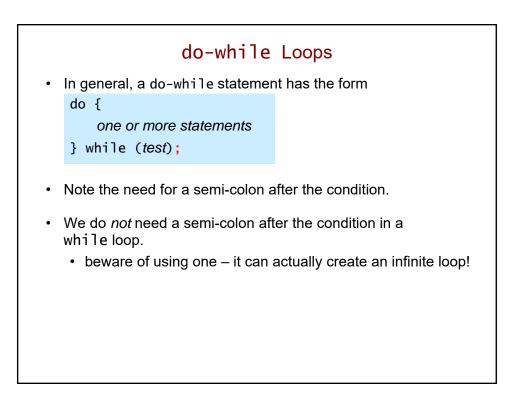
• Let's return to our original version:

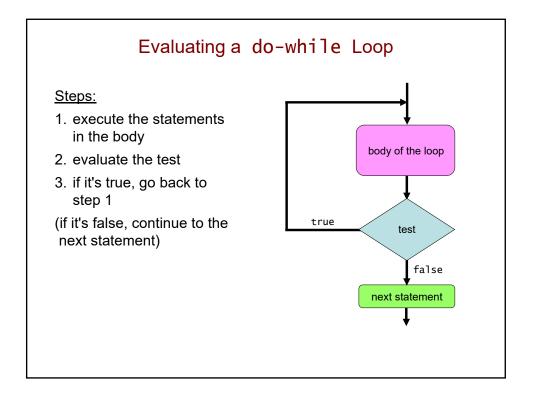
```
int mult = num;
while (mult < 100) {
    System.out.print(mult + " ");
    mult = mult + num;
}
```

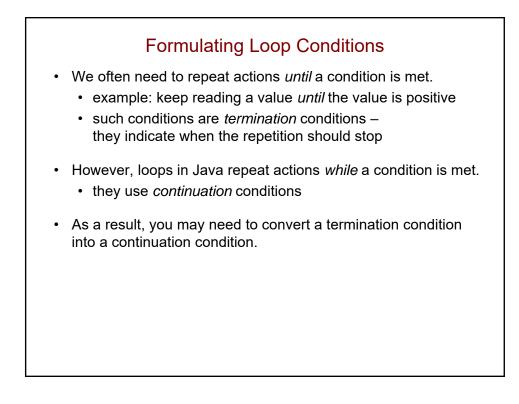
• This could still end up in an infinite loop! How?

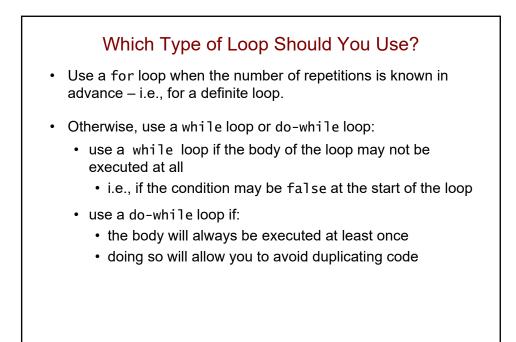




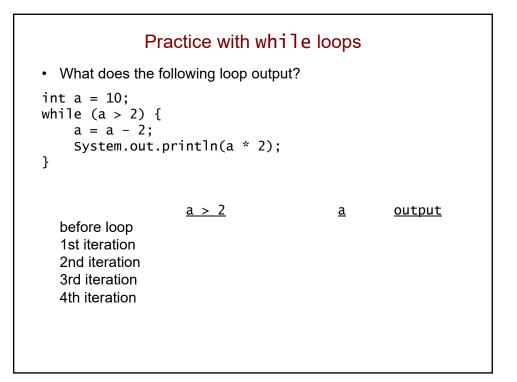


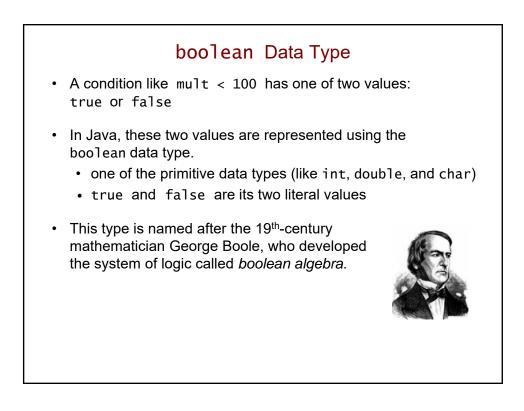


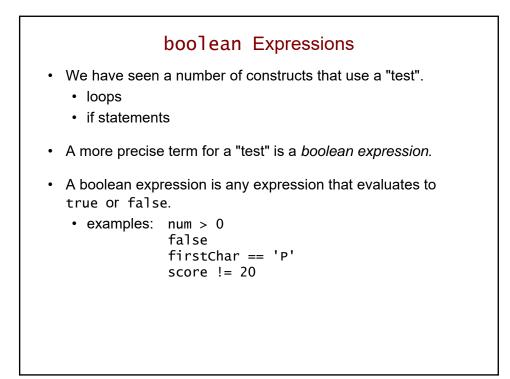


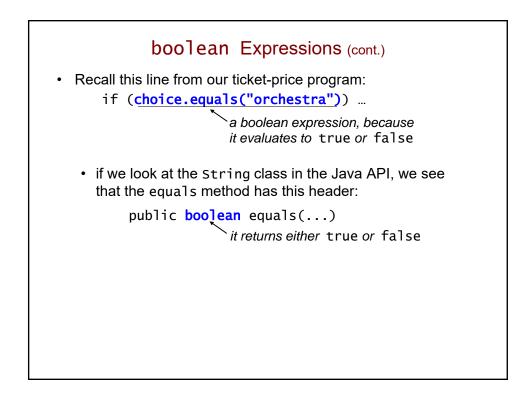


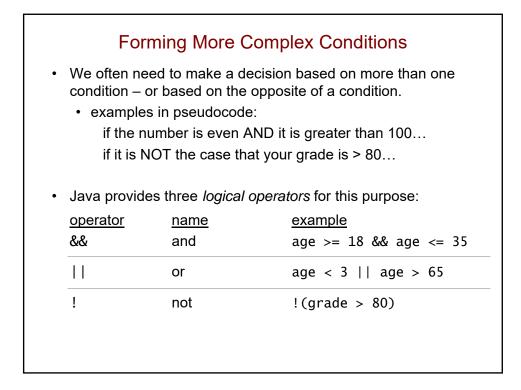
Where is the syntax error below?
Scanner console = new Scanner(System.in);
<pre>do {    System.out.print("Enter a positive integer: ")    int num = console.nextInt(); } while (num &lt;= 0);</pre>
System.out.println("\nThe multiples of " + num + " less than 100 are:");
<pre>int mult = num; while (mult &lt; 100) { System.out.print(mult + " "); mult = mult + num; }</pre>
<pre>System.out.println();</pre>



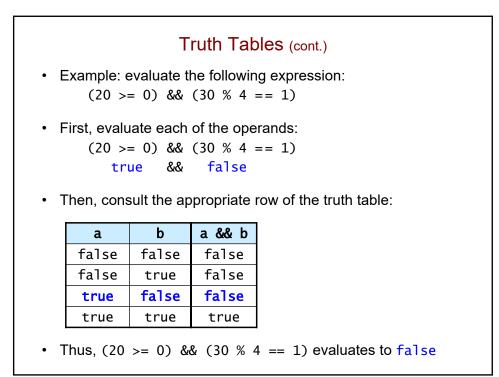


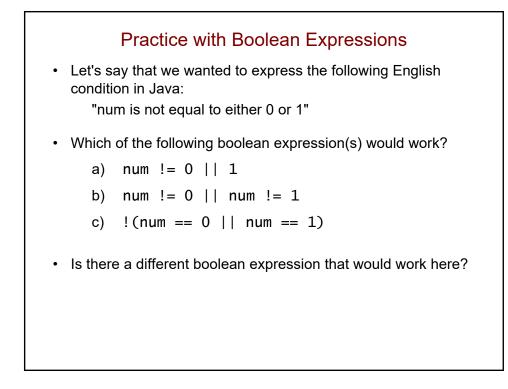


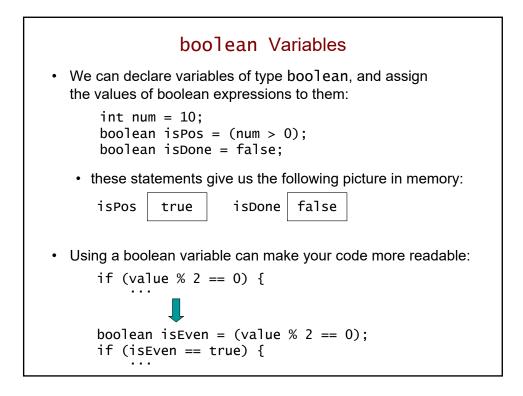




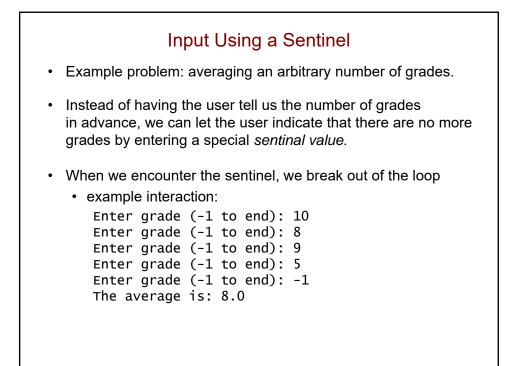
Truth Tables									
<ul> <li>The logical operators operate on boolean expressions.</li> <li>let a and b represent two such expressions</li> </ul>									
• We can define the logical operators using <i>truth tables</i> .									
	truth table	e for && (a	nd)		truth t	table	for    (oi	r)	
	a	b	a && b		a	L	b	a    b	
	false	false	false		fal	se	false	false	
	false	true	false		fal	se	true	true	
	true	false	false		trı	ue	false	true	
	true	true	true		trı	ue	true	true	
truth table for ! (not)									
			a	!	a				
			false	tr	ue				
	true		fa	lse					



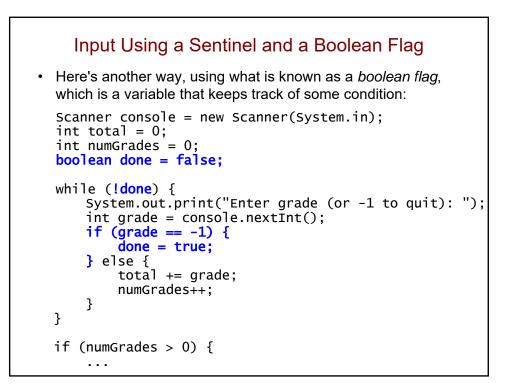


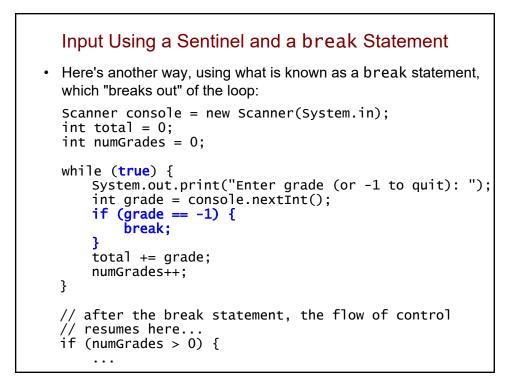


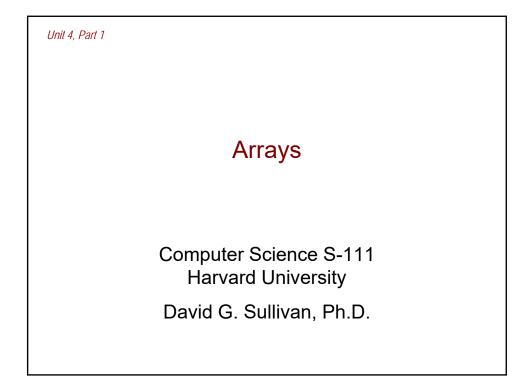
boolean Variables (cont.)
Instead of doing this:
<pre>boolean isEven = (num % 2 == 0); if (isEven == true) {    </pre>
you could just do this:
<pre>boolean isEven = (num % 2 == 0); if (isEven) {    </pre>
The extra comparison isn't necessary!
Similarly, instead of writing:
if (isEven == false) { 
you could just write this:
if (!isEven) {

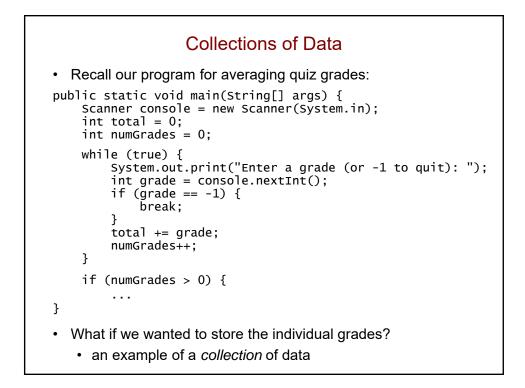


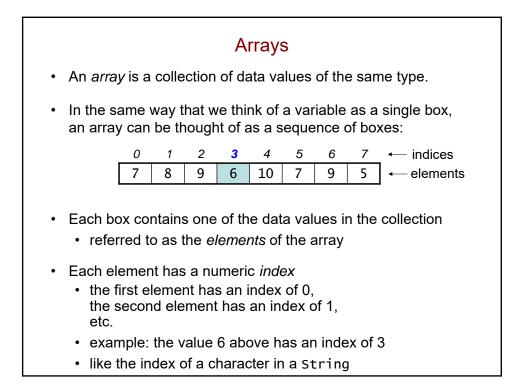
Input Using a Sentinel (cont.)
Here's one way to do this:
Scanner console = new Scanner(System.in); int total = 0; int numGrades = 0;
<pre>System.out.print("Enter grade (or -1 to quit): "); int grade = console.nextInt(); while (grade != -1) { total += grade; numGrades++; System.out.print("Enter grade (or -1 to quit): "); grade = console.nextInt(); }</pre>
<pre>if (numGrades &gt; 0) {     System.out.print("The average is ");     System.out.println((double)total/numGrades); }</pre>

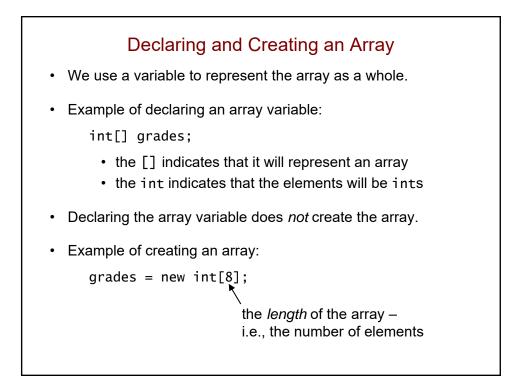


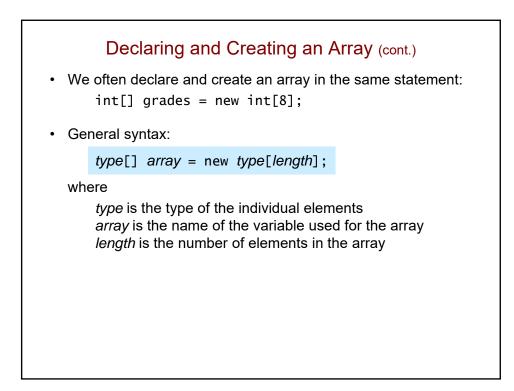


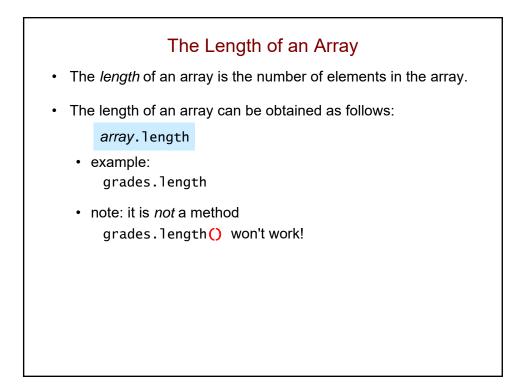




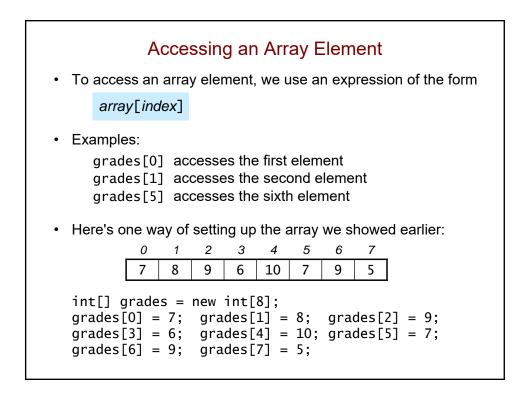


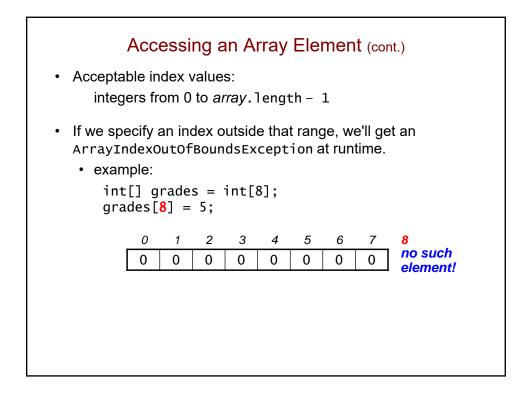


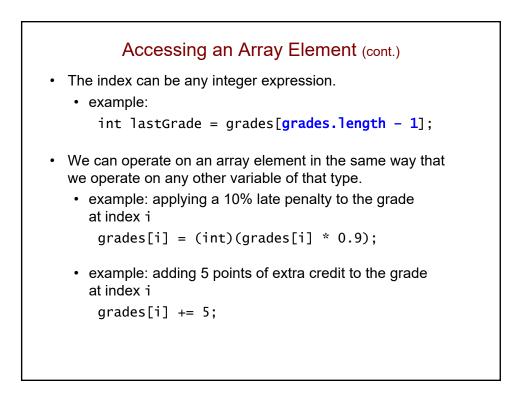


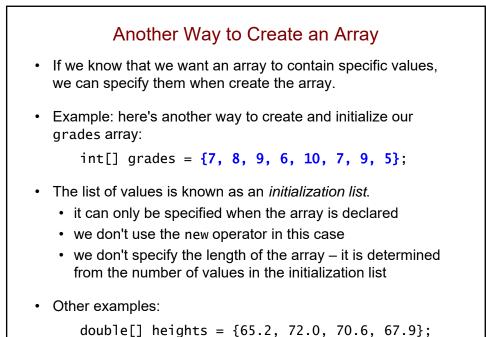


Auto-Initialization							
<ul> <li>When you create an array in this way:</li> </ul>							
<pre>int[] grades = new int[8];</pre>							
the runtime system gives the elements default values:							
0 1 2 3 4 5 6 7							
0 0 0 0 0 0 0 0							
The value used depends on the type of the elements:							
int 0 double 0.0 char '\0' boolean false objects null							

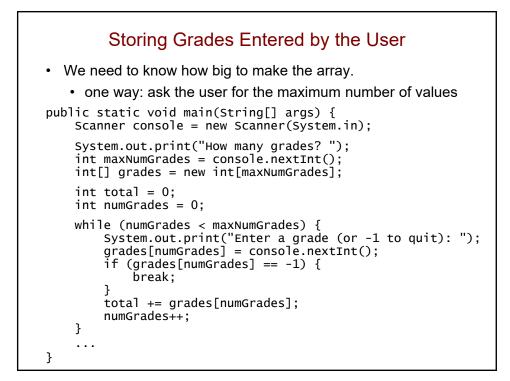


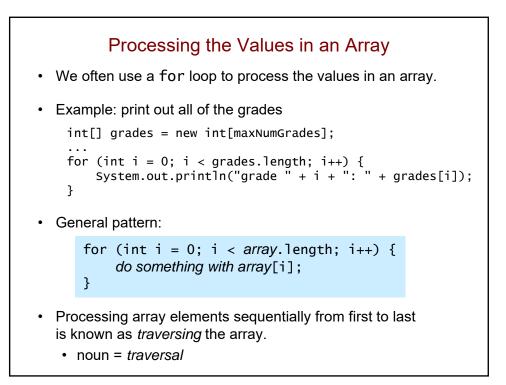


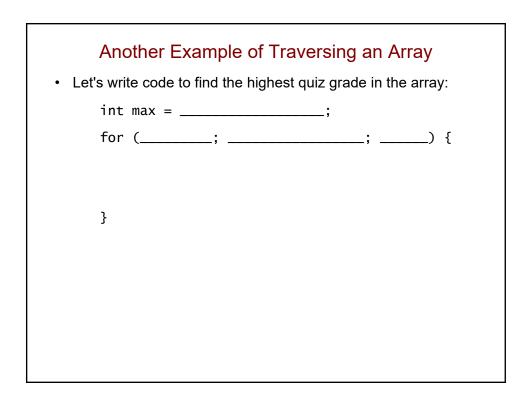


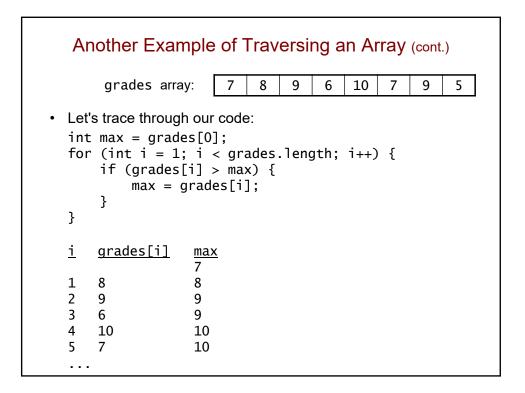


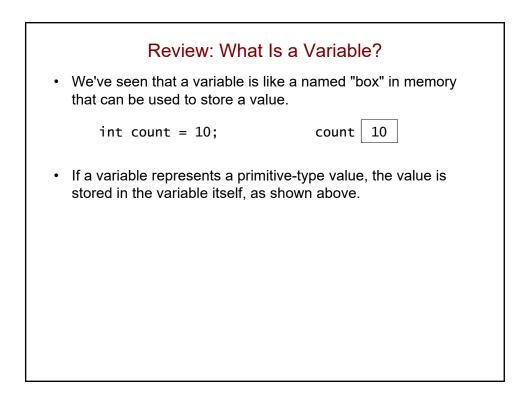
```
boolean[] isPassing = {true, true, false, true};
```

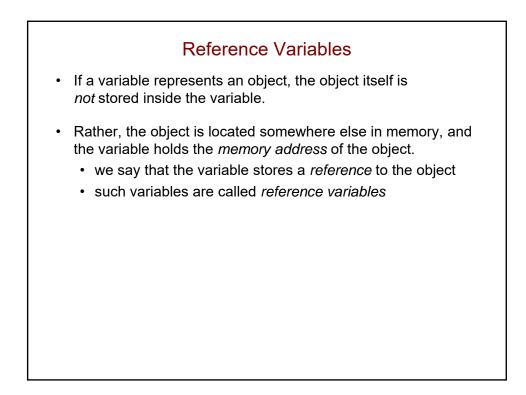


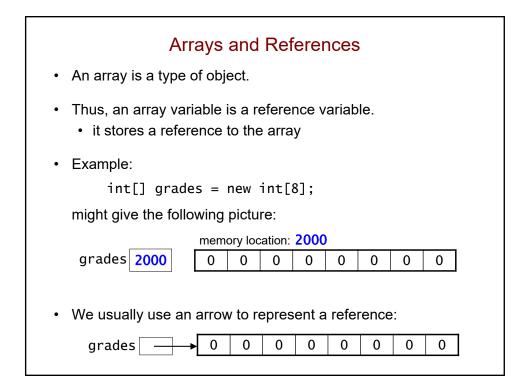


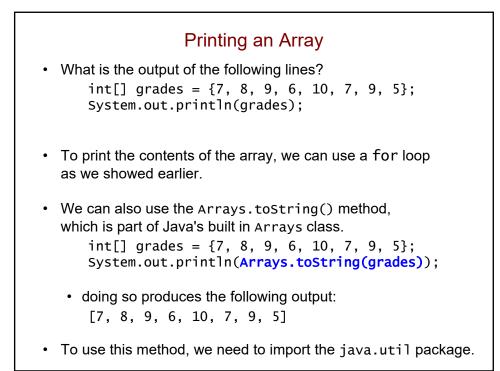


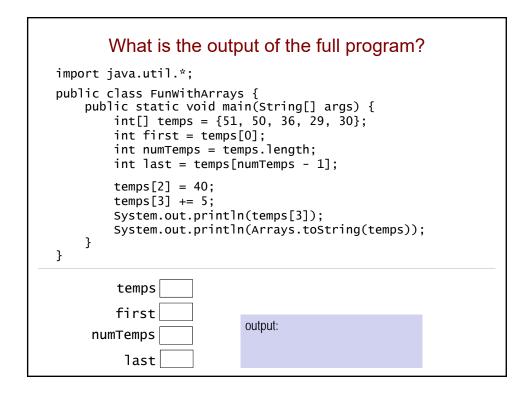


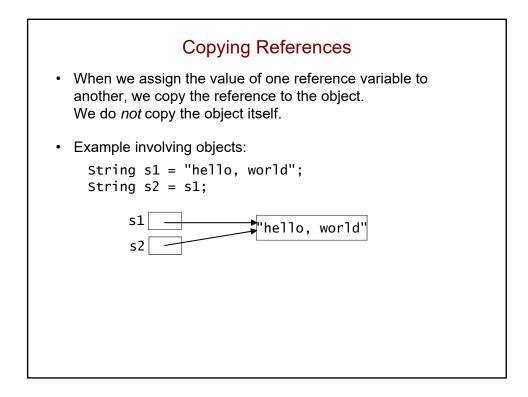


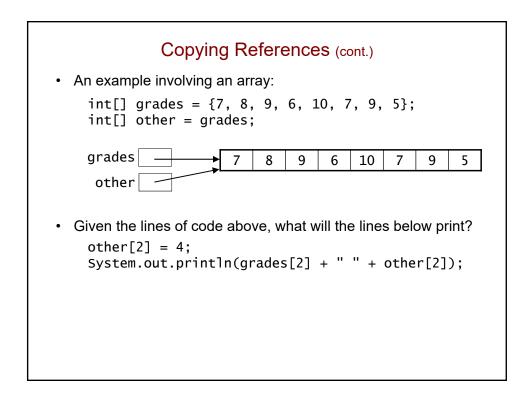


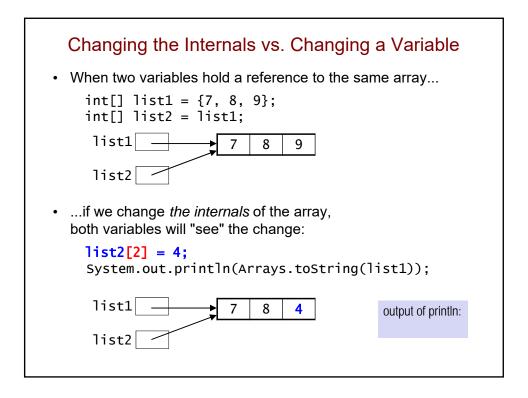


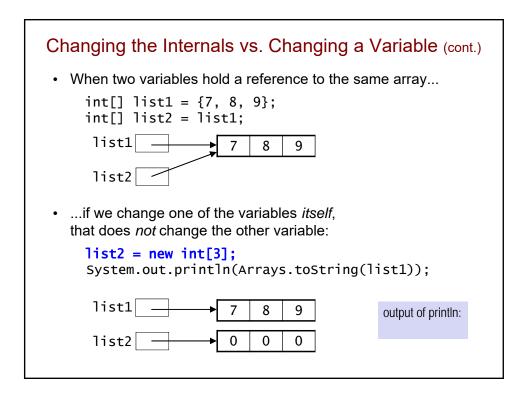


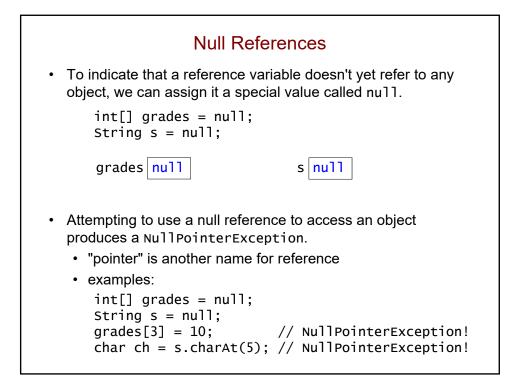


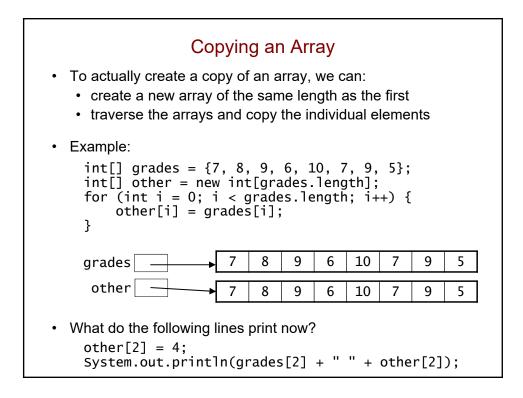




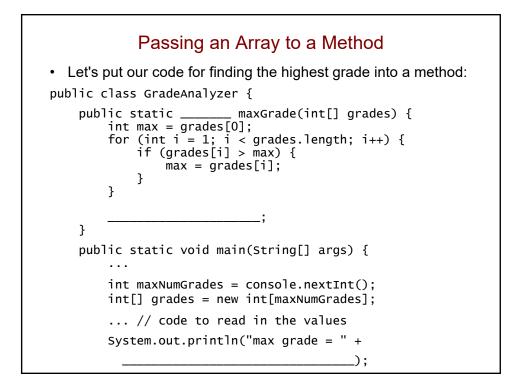


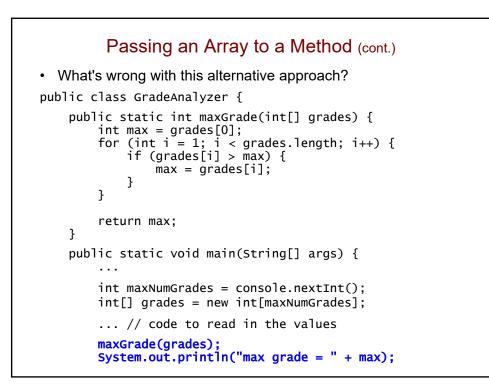


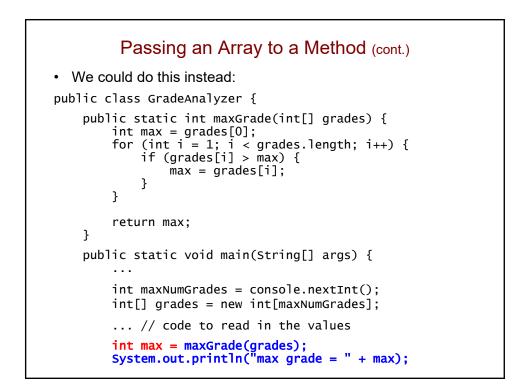




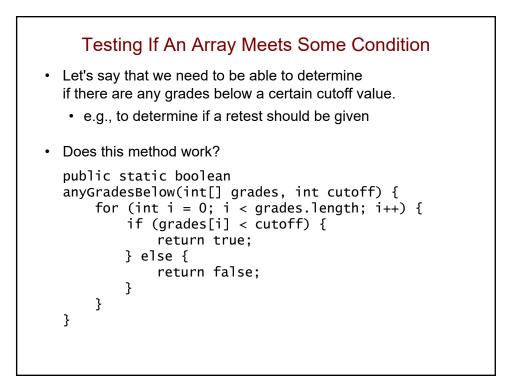
```
Programming Style Point
• Here's how we copied the array:
    int[] grades = {7, 8, 9, 6, 10, 7, 9, 5};
    int[] other = new int[grades.length];
    for (int i = 0; i < grades.length; i++) {
        other[i] = grades[i];
    }
• This would also work:
    int[] grades = {7, 8, 9, 6, 10, 7, 9, 5};
    int[] other = new int[8];
    for (int i = 0; i < 8; i++) {
        other[i] = grades[i];
    }
• Why is the first way better?</pre>
```

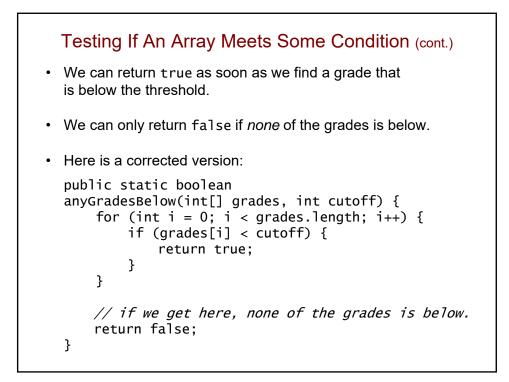


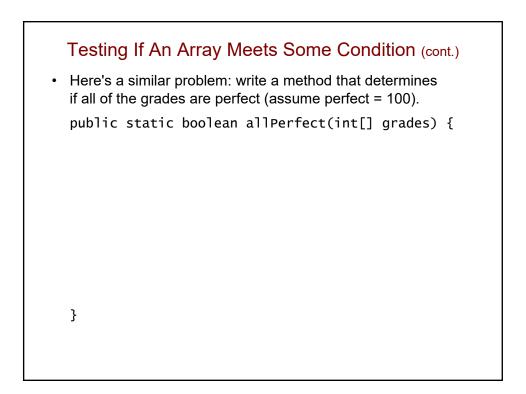


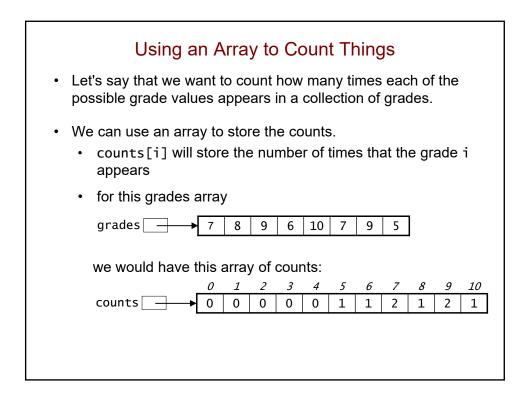


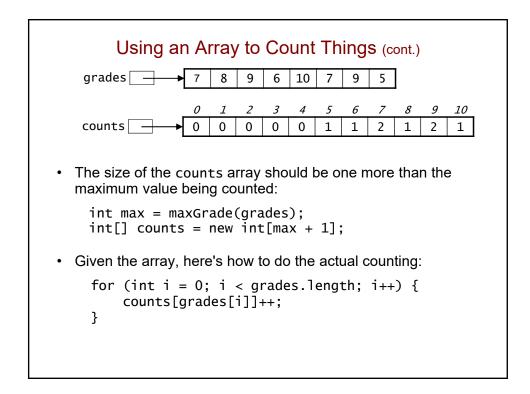
```
Finding the Average Value in an Array
• Here's a method that computes the average grade:
public static double averageGrade(int[] grades) {
    int total = 0;
    for (int i = 0; i < grades.length; i++) {
        total += grades[i];
    }
    return (double)total / grades.length;
}</pre>
```

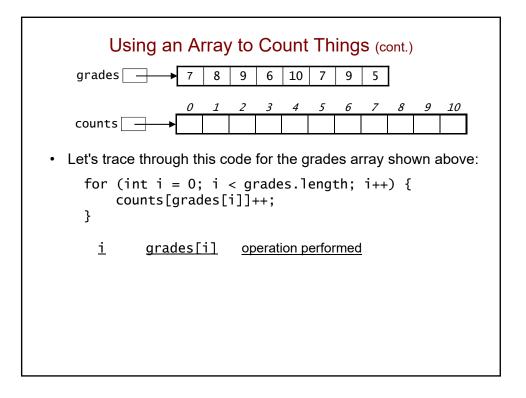


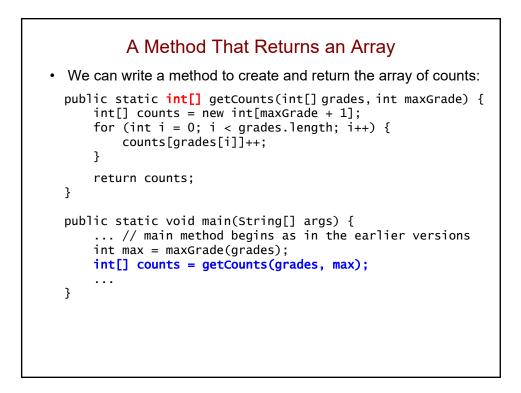


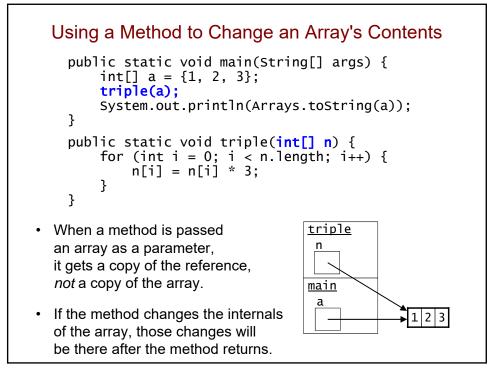


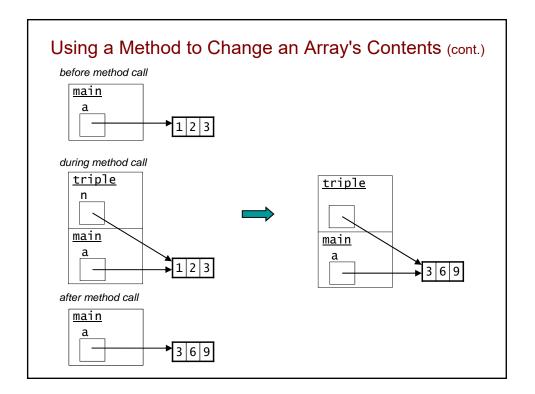


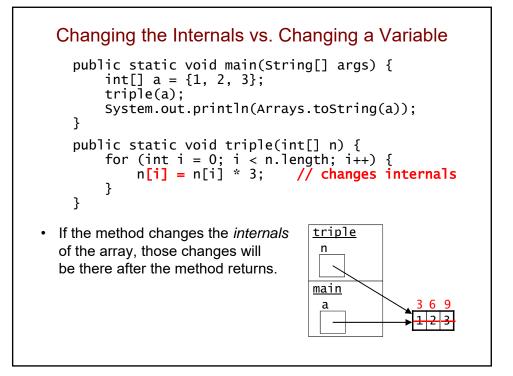


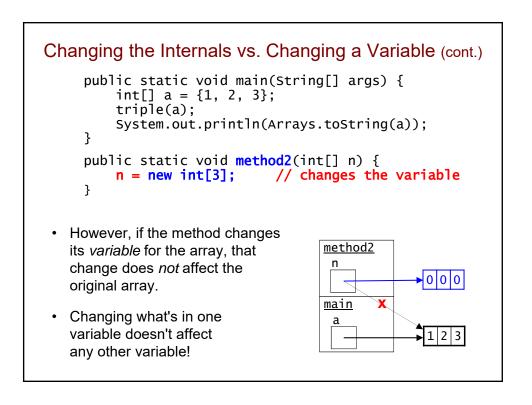


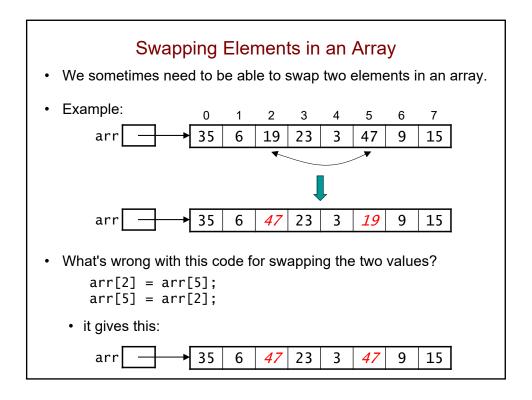


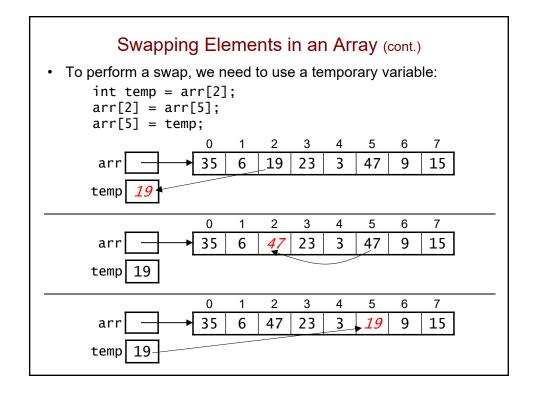


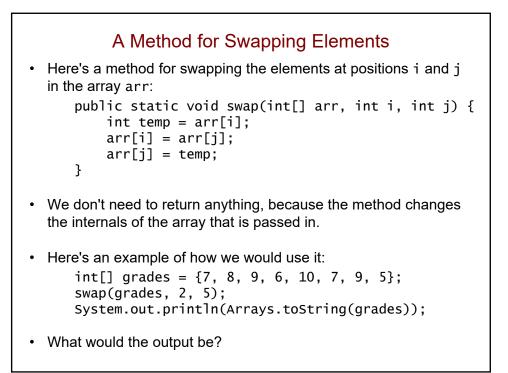


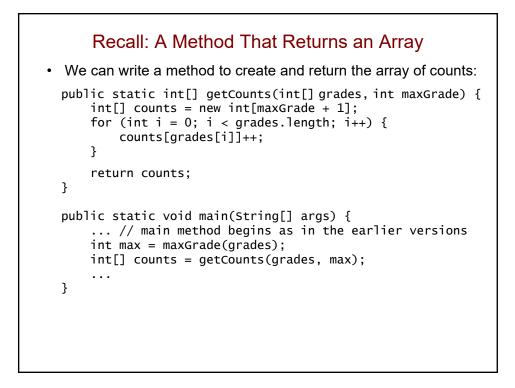


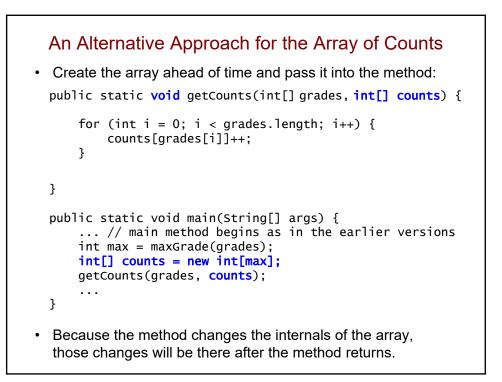




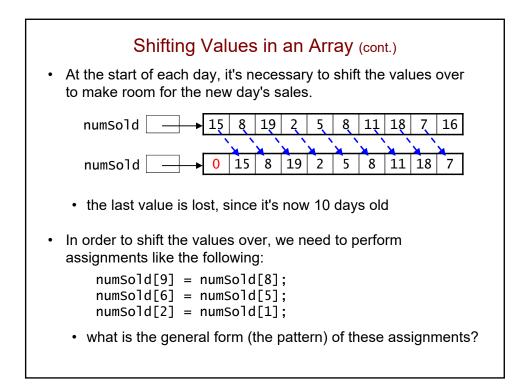


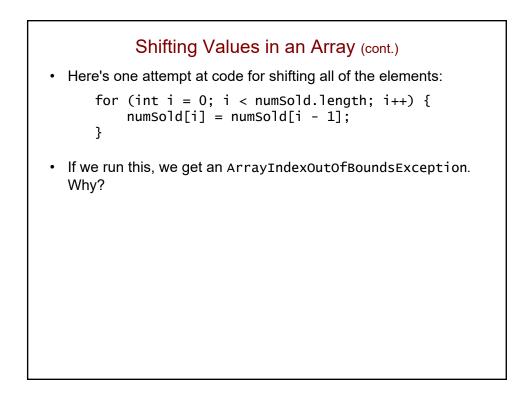


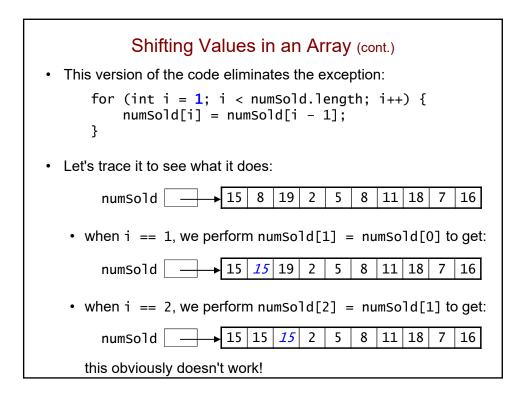


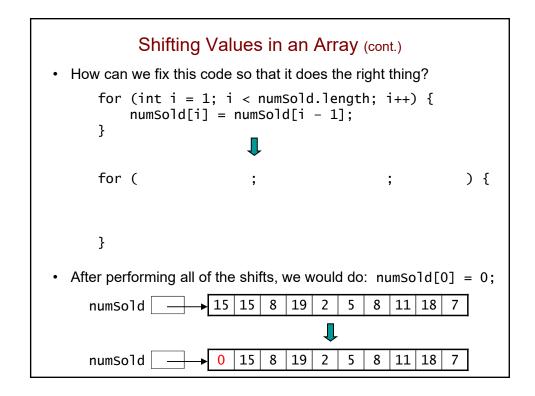


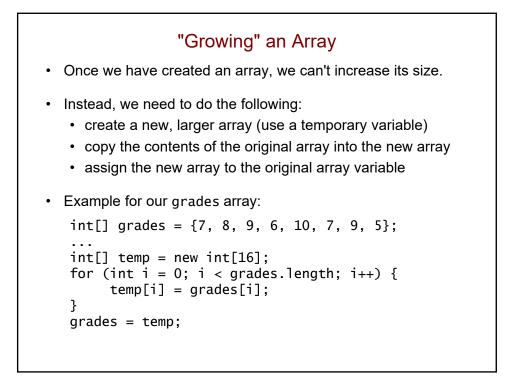
Shifting Values in an Array
<ul> <li>Let's say a small business is using an array to store the number of items sold over a 10-day period.</li> </ul>
numSold 15 8 19 2 5 8 11 18 7 16
<pre>numSold[0] gives the number of items sold today numSold[1] gives the number of items sold 1 day ago numSold[2] gives the number of items sold 2 days ago  numSold[9] gives the number of items sold 9 days ago</pre>

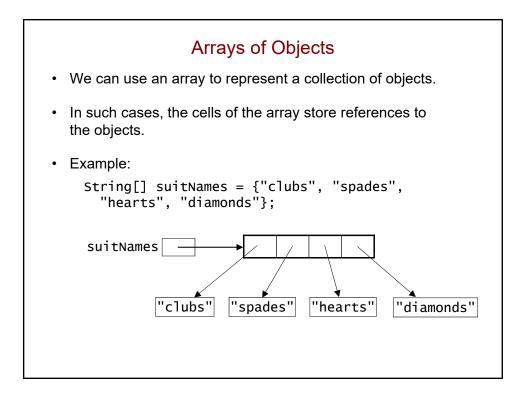


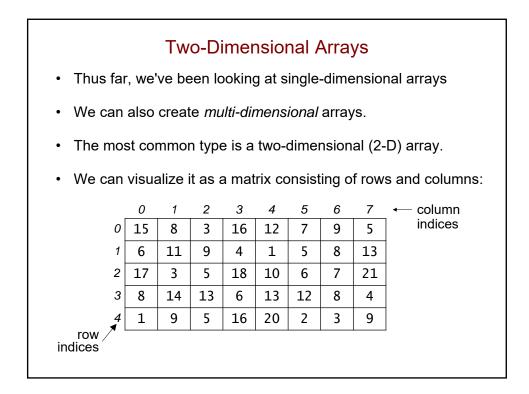


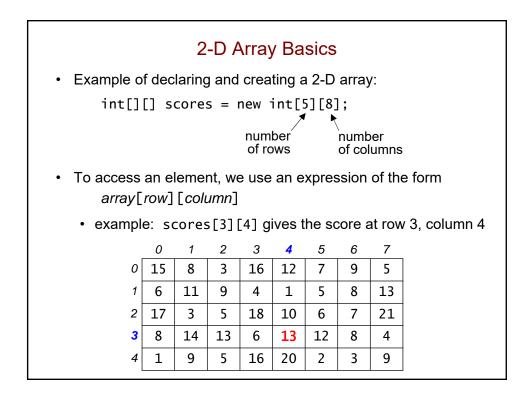


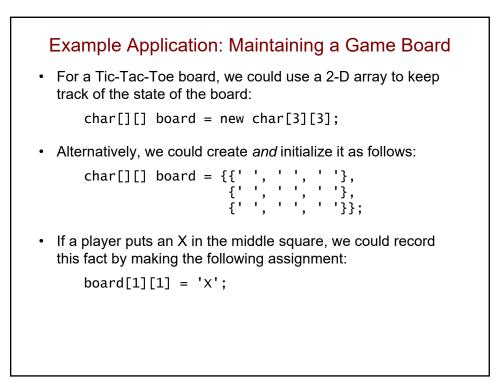


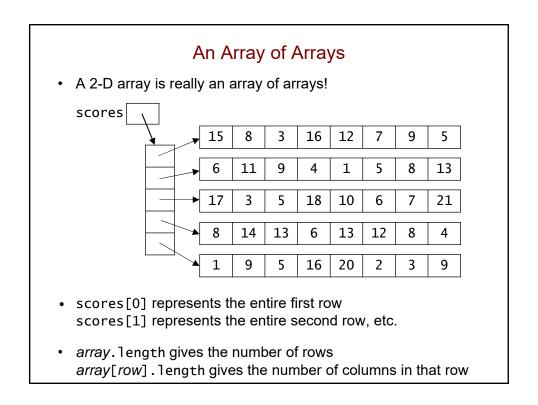


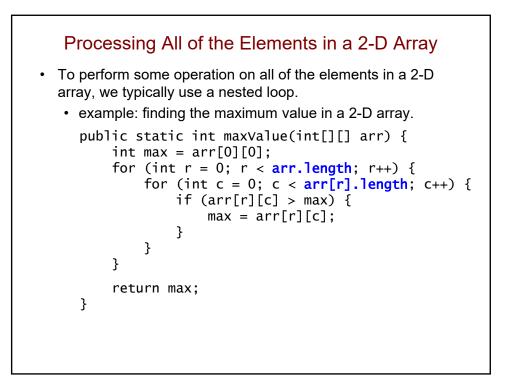


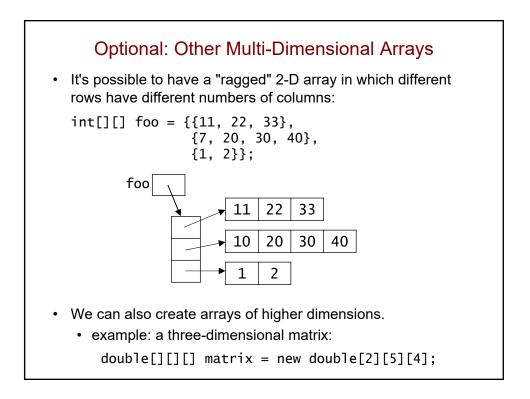


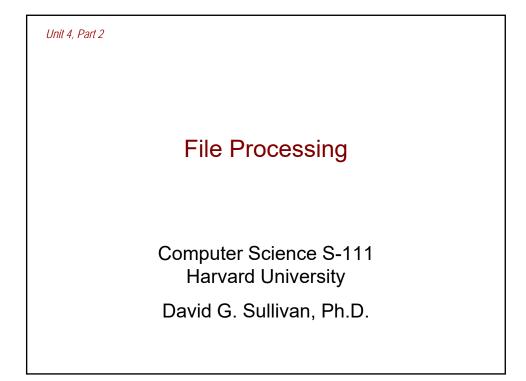


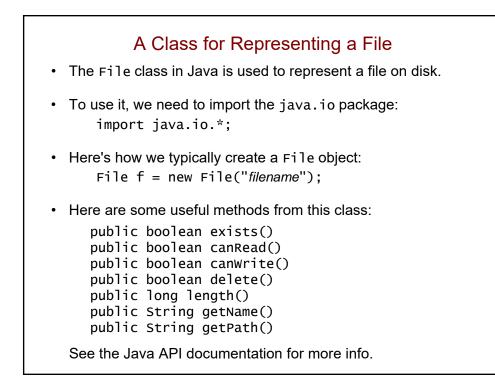


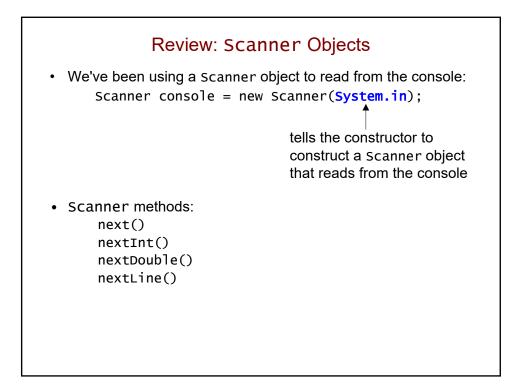


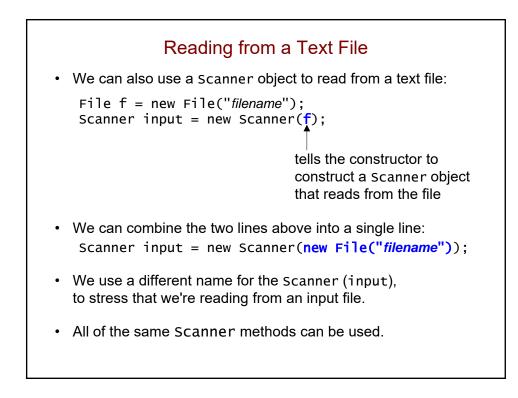


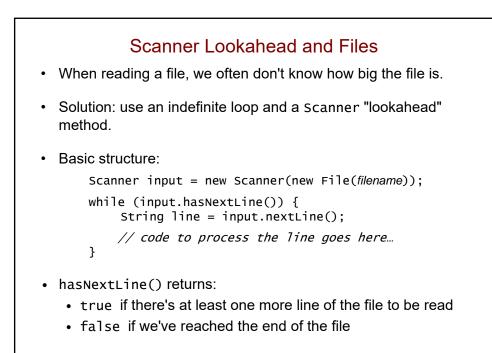


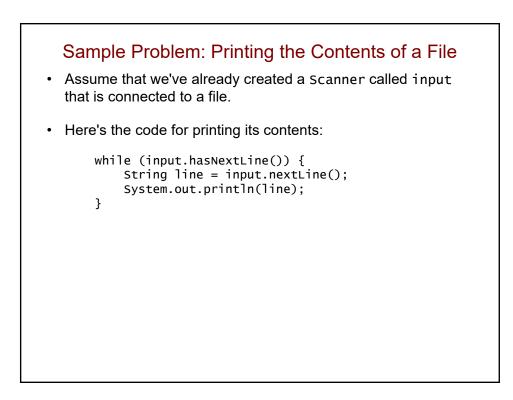


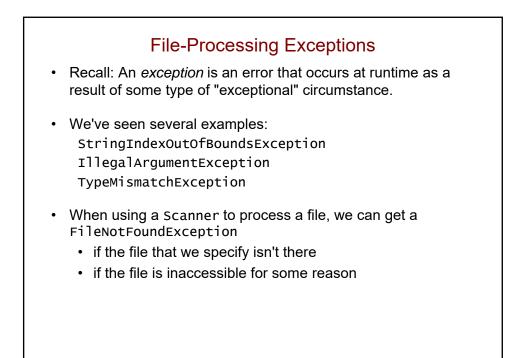


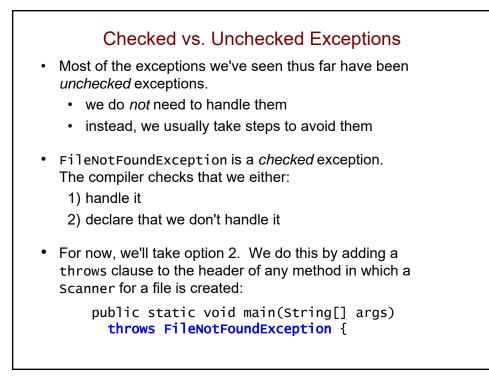






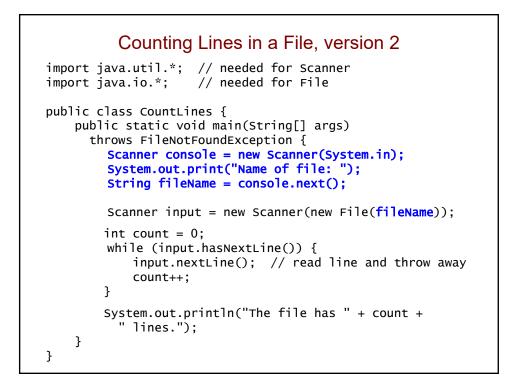


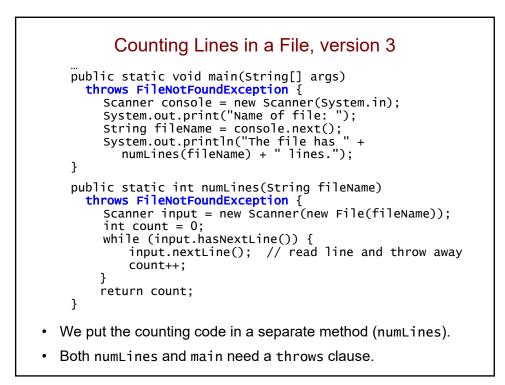


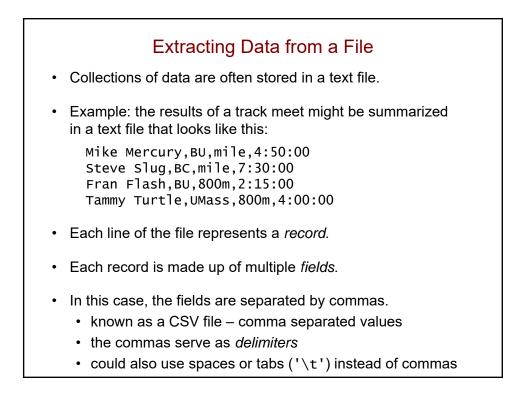




```
import java.util.*; // needed for Scanner
                     // needed for File
import java.io.*;
public class CountLines {
    public static void main(String[] args)
      throws FileNotFoundException {
        Scanner input = new Scanner(new File("romeo.txt"));
        int count = 0;
        while (input.hasNextLine()) {
            input.nextLine(); // read line and throw away
            count++;
        }
        System.out.println("The file has " + count +
          " lines.");
    }
}
```





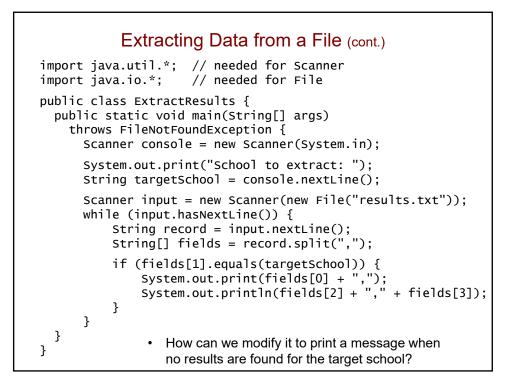


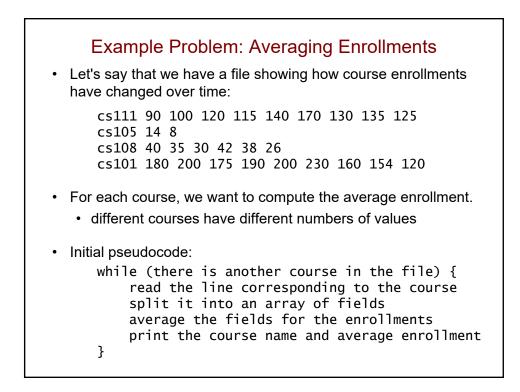
## Extracting Data from a File (cont.)

Mike Mercury, BU, mile, 4:50:00 Steve Slug, BC, mile, 7:30:00 Fran Flash, BU, 800m, 2:15:00 Tammy Turtle, UMass, 800m, 4:00:00

- We want a program that:
  - · reads in a results file like the one above
  - · extracts and prints only the results for a particular school
    - with the name of the school omitted
- · Basic approach:
  - ask the user for the school of interest (the target school)
  - · read one line at a time from the file
  - split the line into fields
  - if the field corresponding to the school name matches the target school, print out the other fields in that record

Splitting a String	
<ul> <li>The String class includes a method named split().</li> <li>breaks a string into component strings</li> <li>takes a parameter indicating what delimiter should be used when performing the split</li> <li>returns a String array containing the components</li> </ul>	
<pre>• Example: &gt; String sentence = "How now brown cow?"; &gt; String[] words = sentence.split(" "); &gt; words[0] "How" &gt; words[1] "now" &gt; words[3] "cow?" &gt; words.length 4</pre>	





```
Example Problem: Averaging Enrollments (cont.)
      cs108 40 35 30 42 38 26
      cs111 90 100 120 115 140 170 130 135 125
      cs105 14 8
      cs101 180 200 175 190 200 230 160 154 120

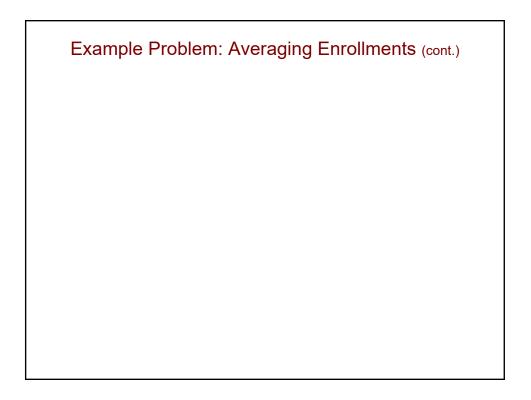
    When we split a line into fields, we get an array of strings.

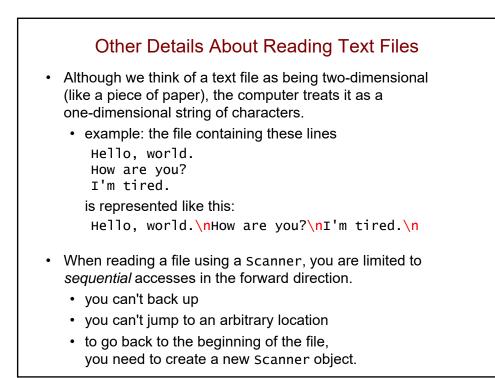
    example for the first line above:

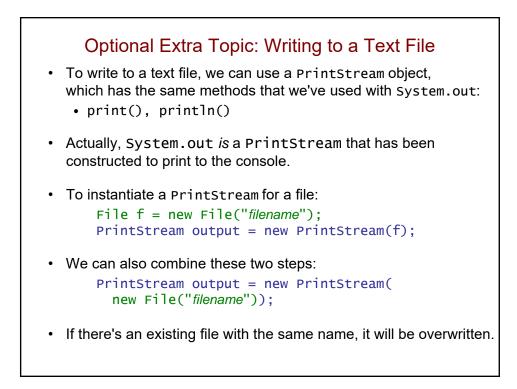
      {"cs108", "40", "35", "30", "42", "38", "26"}
· We can convert the enrollments from strings to integers using
  a method called Integer.parseInt()
   • example:
      String[] fields = record.split(" ");
      String courseName = fields[0];
      int firstEnrollment = Integer.parseInt(fields[1]);

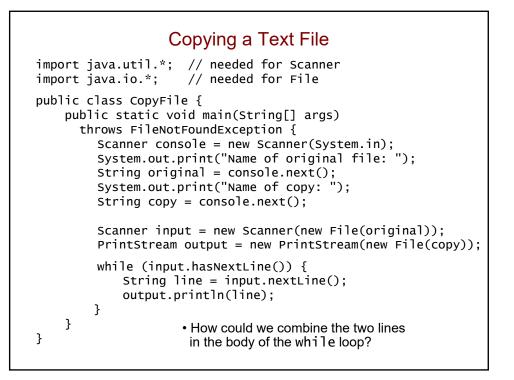
    note: parseInt() is a static method, so we call it using

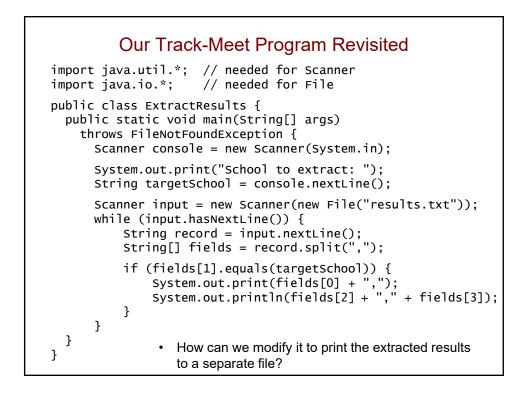
     its class name (Integer)
```



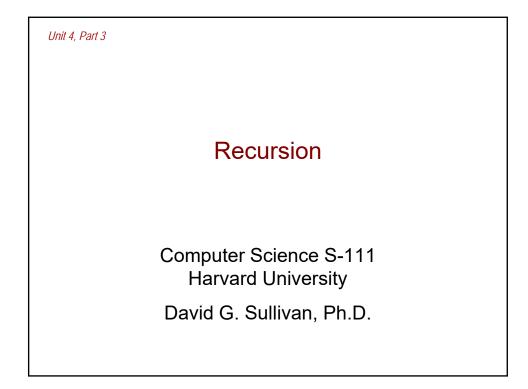


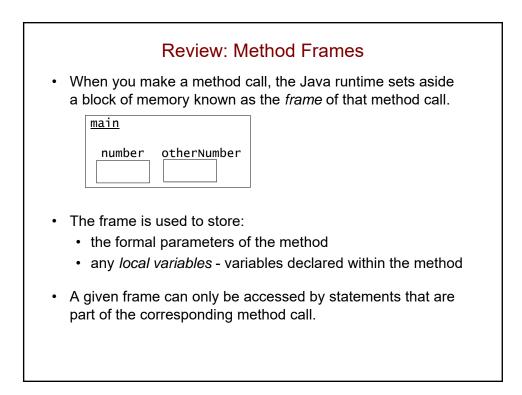


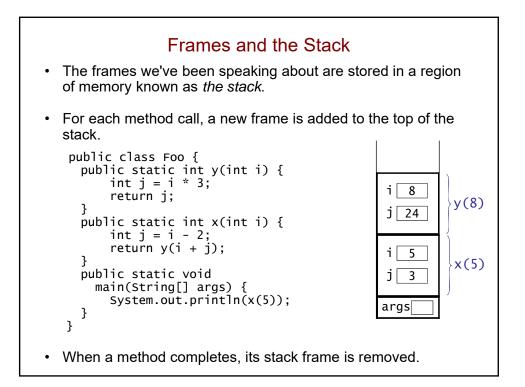


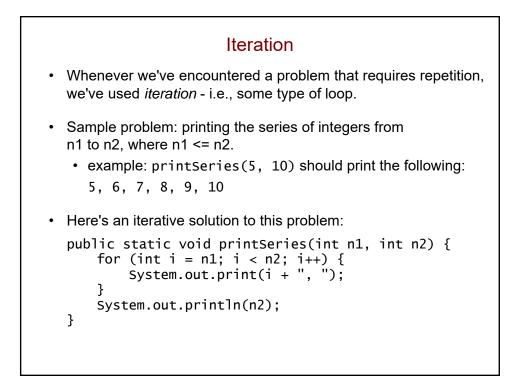


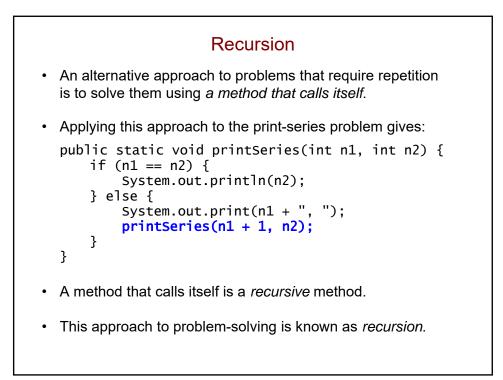
Optional Extra Topic: Binary Files
Not all files are text files.
<ul> <li>Binary files don't store the string representation of non-string values.</li> <li>instead, they store their <i>binary</i> representation – the way they are stored in memory</li> </ul>
<ul> <li>Example: 125</li> <li>the text representation of 125 stores the string "125" – i.e., the characters for the individual digits in the number</li> <li>1'1' '2' '5'</li> <li>49 50 53</li> </ul>
<ul> <li>the binary representation of 125 stores the four-byte</li> </ul>
binary representation of the integer 125

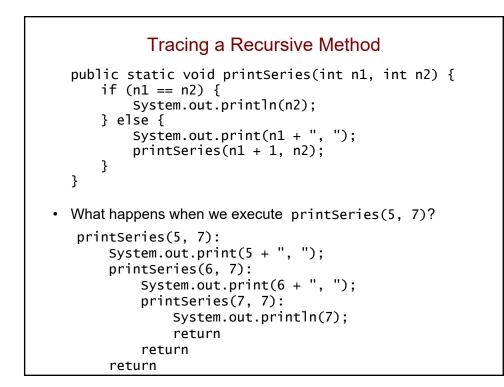


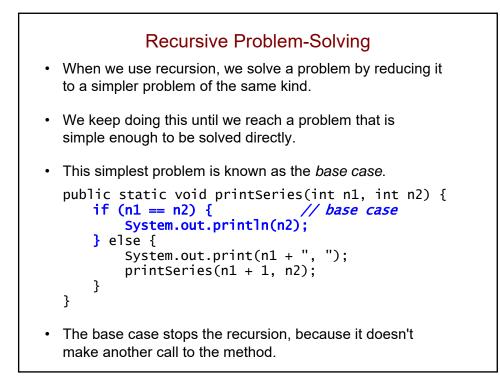


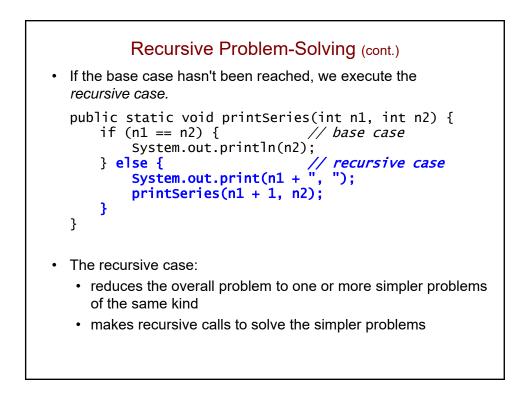


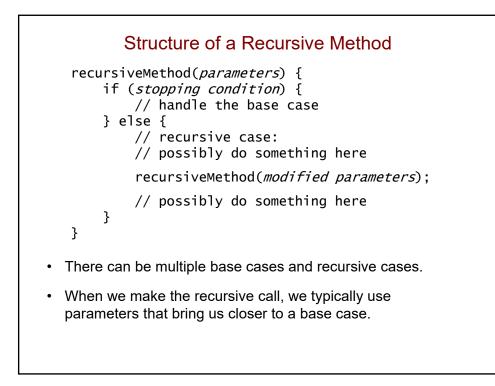


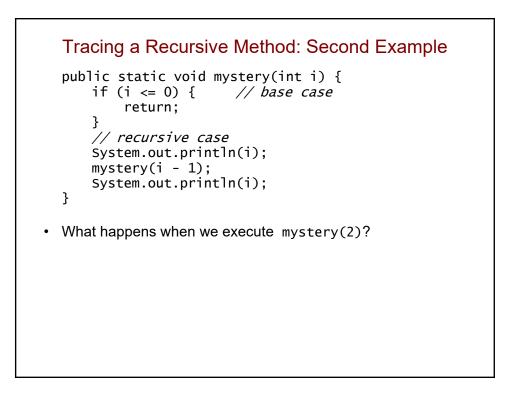


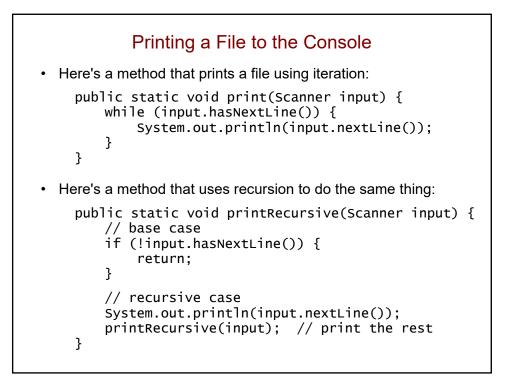


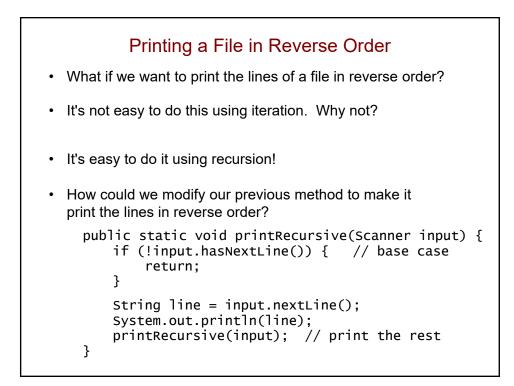


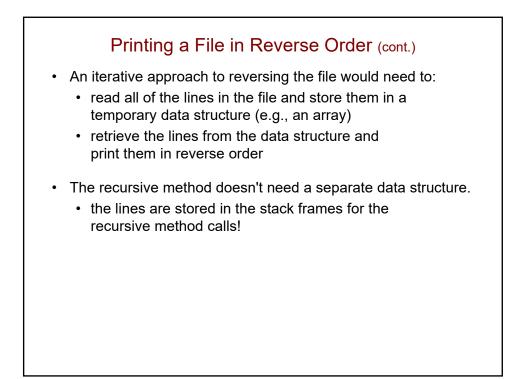


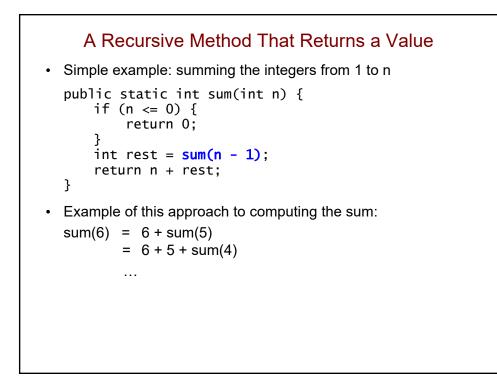






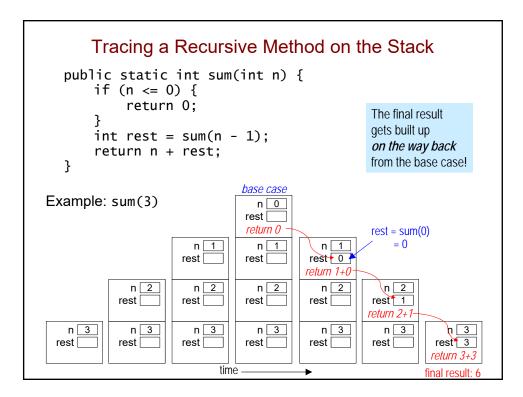






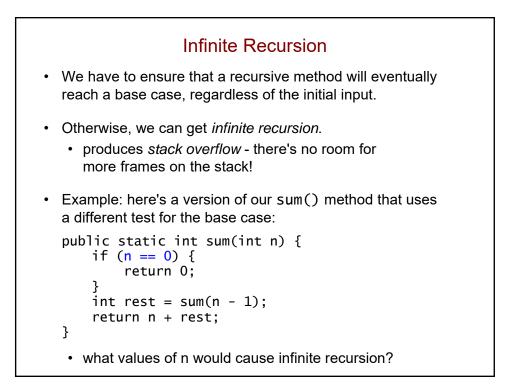
## Tracing a Recursive Method

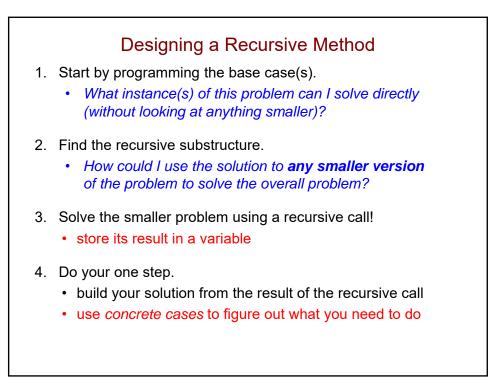
```
public static int sum(int n) {
    if (n <= 0) {
        return 0;
    }
    int rest = sum(n - 1);
    return n + rest;
}
• What happens when we execute int x = sum(3);
from inside the main() method?</pre>
```

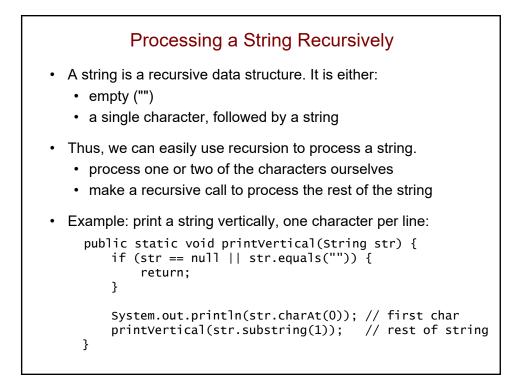


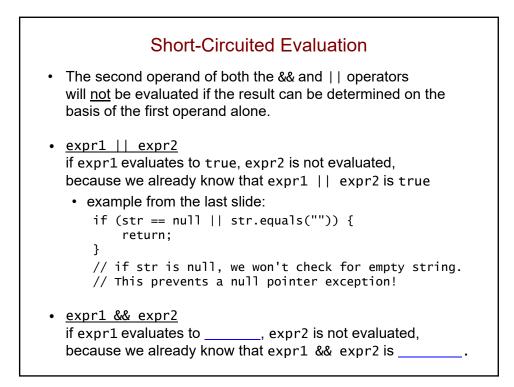
```
Another Option for Tracing a Recursive Method
```

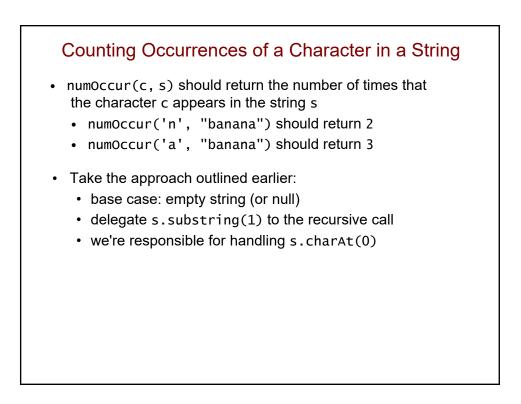
```
public static int sum(int n) {
    if (n <= 0) {
        return 0;
    }
    int rest = sum(n - 1);
    return n + rest;
}</pre>
```

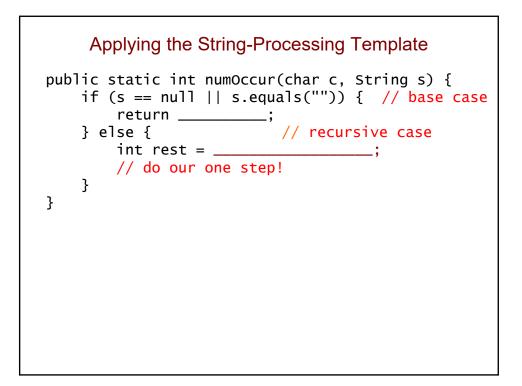




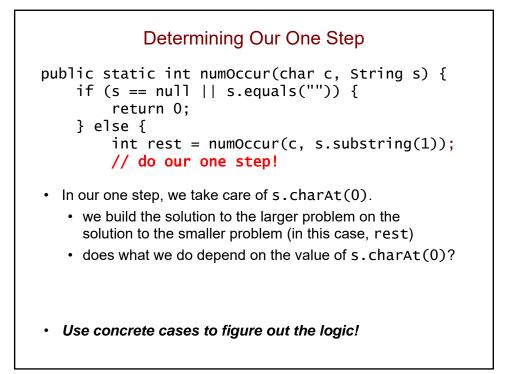




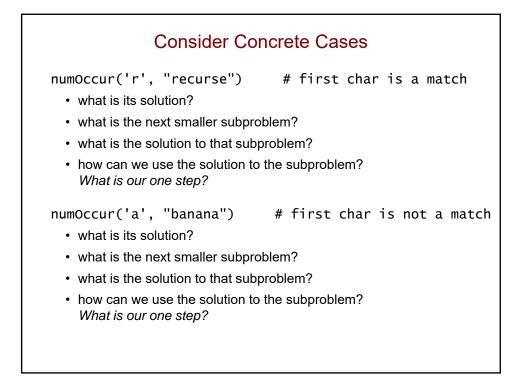


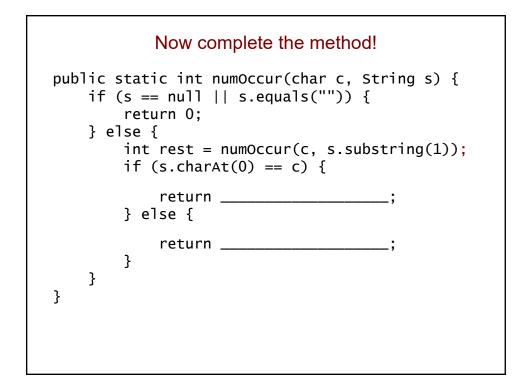


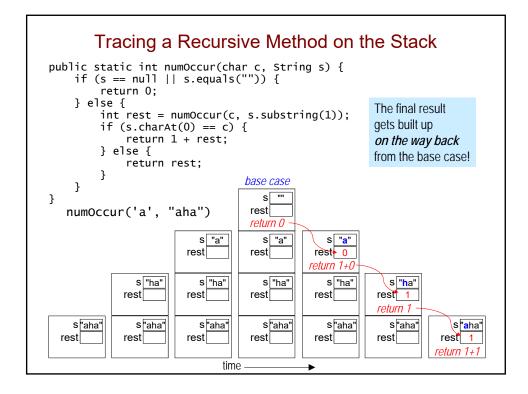




```
Consider this concrete case...
public static int numOccur(char c, String s) {
    if (s == null || s.equals("")) {
        return 0;
    } else {
        int rest = numOccur(c, s.substring(1));
        // do our one step!
        ...
numOccur('r', "recurse")
        r = 'r', s = "recurse"
```







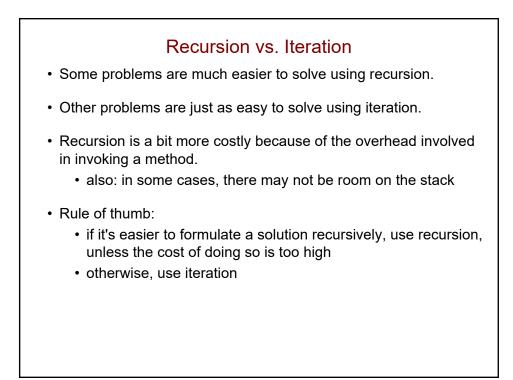
```
Common Mistake
• This version of the method does not work:
public static int numOccur(char c, String s) {
    if (s == null || s.equals("")) {
        return 0;
    }
    int count = 0;
    if (s.charAt(0) == c) {
        count++;
    }
    numOccur(c, s.substring(1));
    return count;
}
```

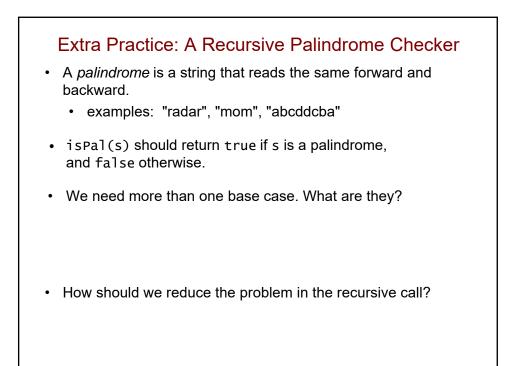
## Another Faulty Approach

• Some people make count "global" to fix the prior version:

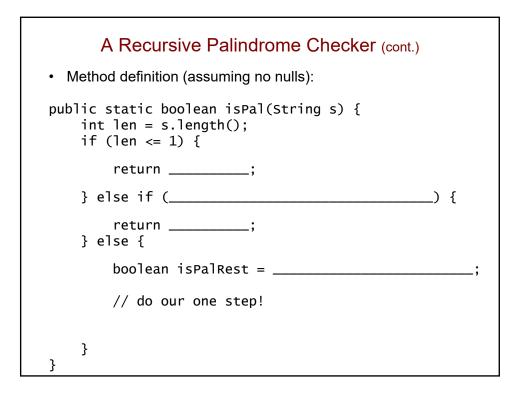
```
public static int count = 0;
public static int numOccur(char c, String s) {
    if (s == null || s.equals("")) {
        return 0;
    }
    if (s.charAt(0) == c) {
        count++;
    }
    numOccur(c, s.substring(1));
    return count;
}
• Not recommended, and not allowed on the problem sets!
```

• Problems with this approach?





Consider Concrete Cases!
isPal("radar")
<ul> <li>what is its solution?</li> </ul>
<ul><li>what is the next smaller subproblem?</li></ul>
<ul><li>what is the solution to that subproblem?</li></ul>
<ul> <li>how can we use the solution to the subproblem?</li> <li>What is our one step?</li> </ul>
isPal("modem")
<ul> <li>what is its solution?</li> </ul>
<ul><li>what is the next smaller subproblem?</li></ul>
<ul><li>what is the solution to that subproblem?</li></ul>
<ul> <li>how can we use the solution to the subproblem?</li> <li>What is our one step?</li> </ul>

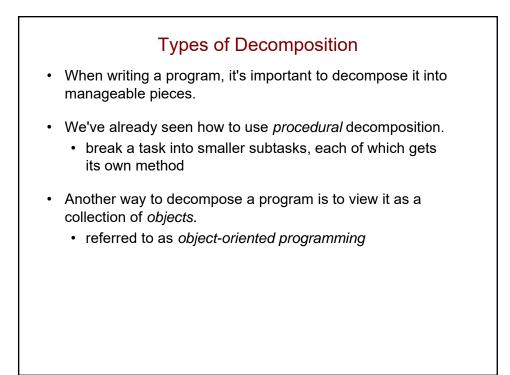


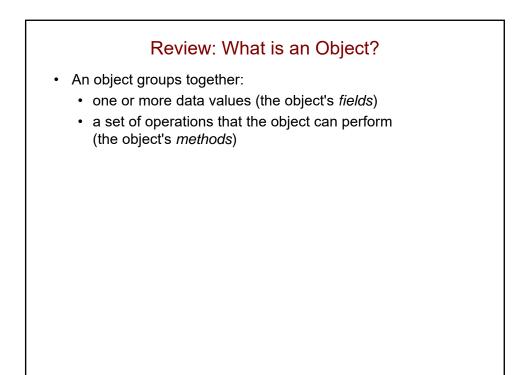


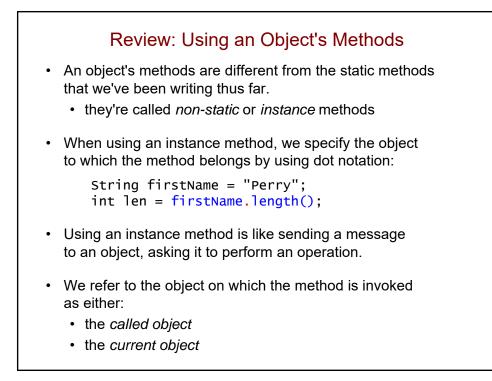
## Classes as Blueprints: How to Define New Types of Objects

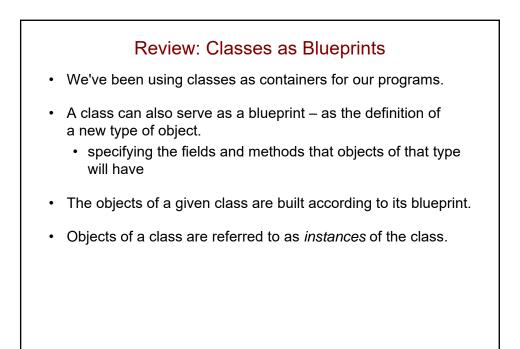
Computer Science S-111 Harvard University

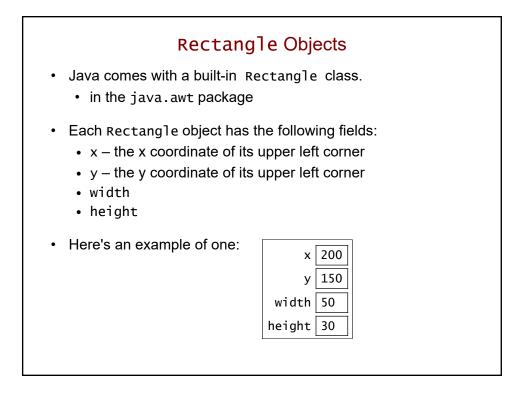
David G. Sullivan, Ph.D.

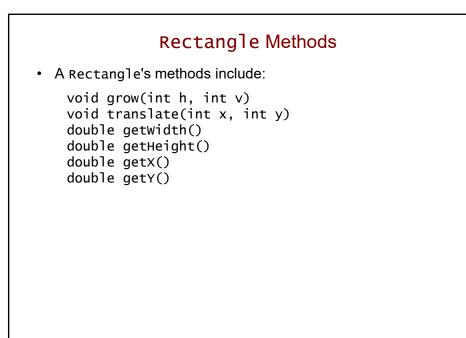


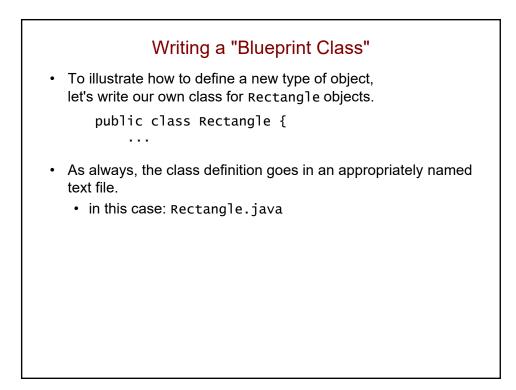


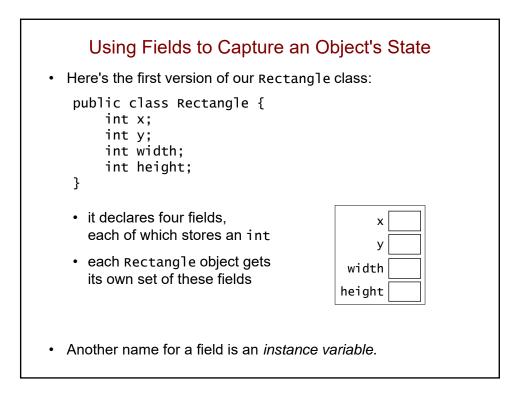


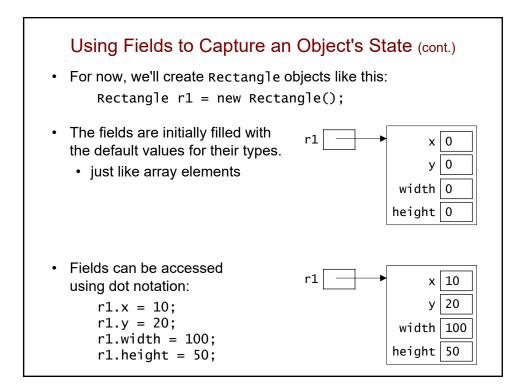


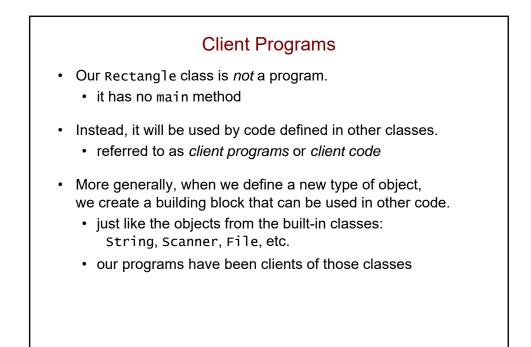




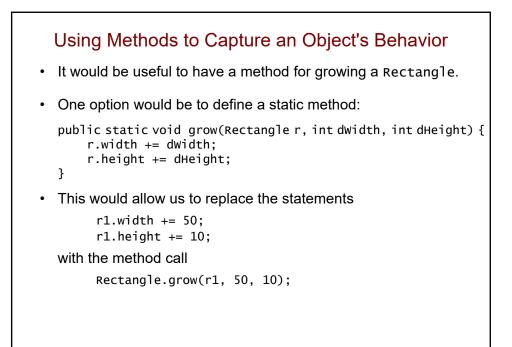


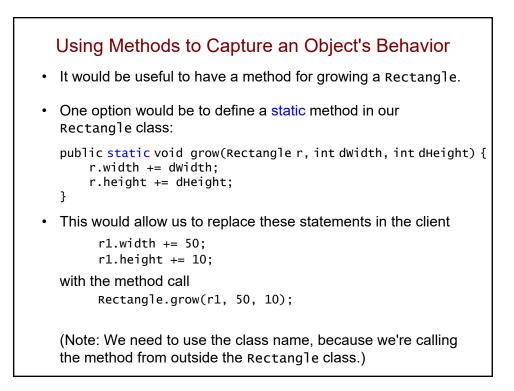


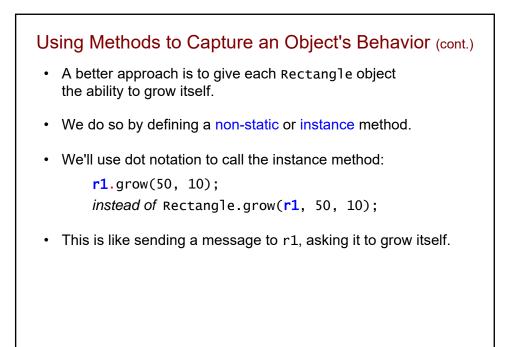


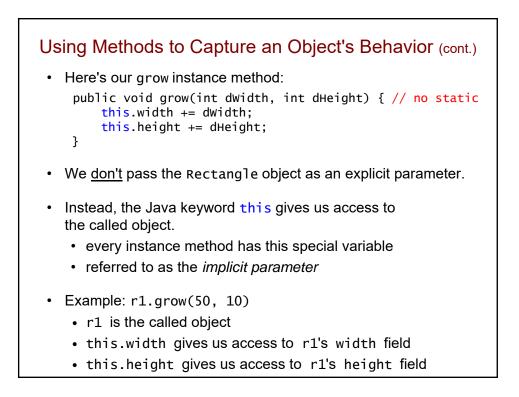


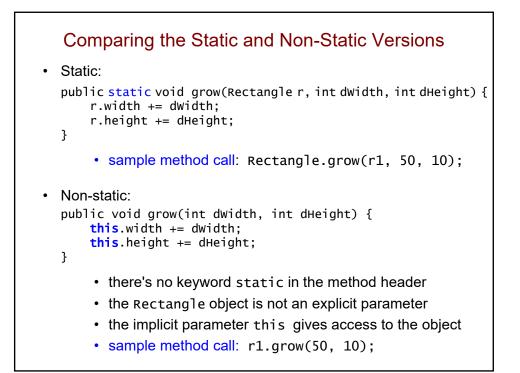
Initial Client Program
<pre>public class RectangleClient {     public static void main(String[] args) {         Rectangle r1 = new Rectangle();         r1.x = 10; r1.y = 20;         r1.width = 100; r1.height = 50;</pre>
Rectangle r2 = new Rectangle(); r2.x = 50; r2.y = 100; r2.width = 20; r2.height = 80;
System.out.println("r1: "+r1.width+"x"+r1.height); int area1 = r1.width * r1.height; System.out.println("area = " + area1);
System.out.println("r2: " + r2.width + " x " + r2.height); int area2 = r2.width * r2.height; System.out.println("area = " + area2);
// grow both rectangles r1.width += 50; r1.height += 10; r2.width += 5; r2.height += 30;
<pre>System.out.println("r1: " + r1.width + " x " + r1.height); System.out.println("r2: " + r2.width + " x " + r2.height); }</pre>

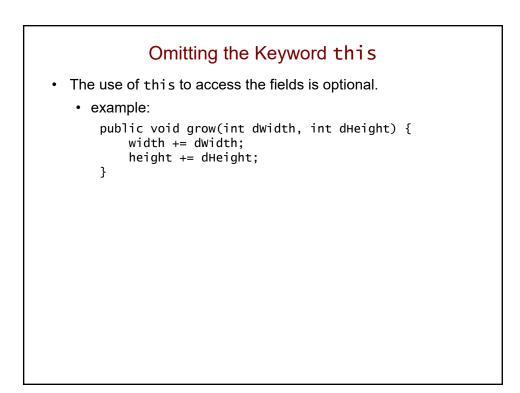


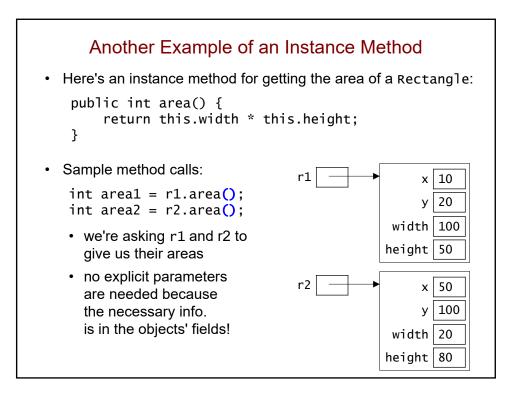


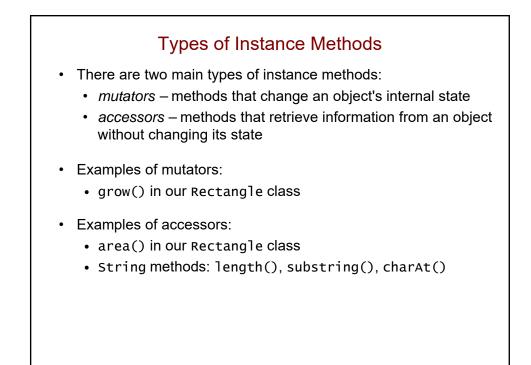






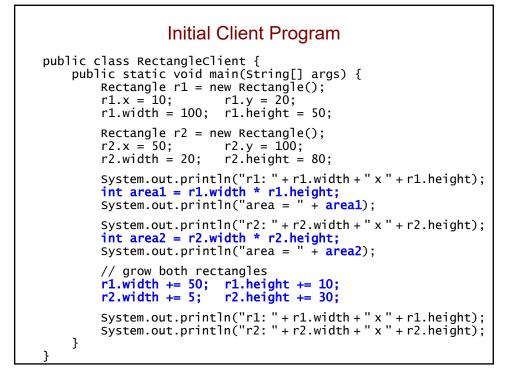


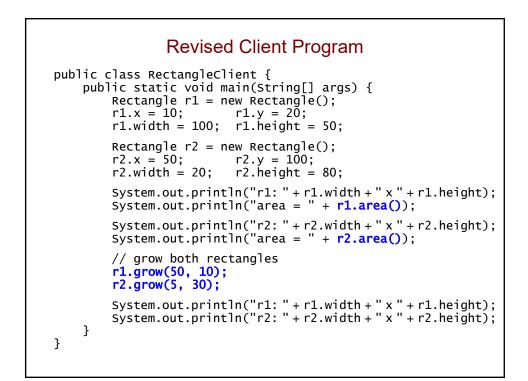


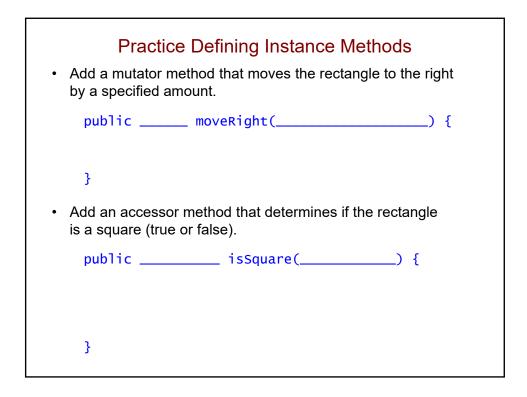


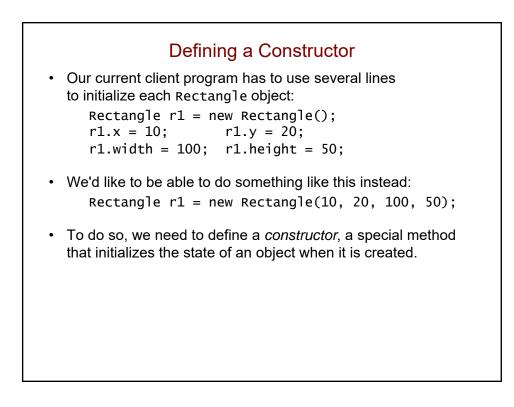
```
second Version of our Rectangle Class
public class Rectangle {
    int x;
    int y;
    int width;
    int height;
    public void grow(int dwidth, int dHeight) {
        this.width += dwidth;
        this.height += dHeight;
    }
    public int area() {
        return this.width * this.height;
    }
}
```

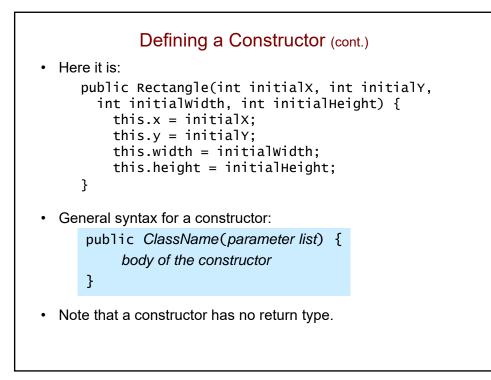
```
Which method call increases r's height by 5?
public class Rectangle {
    int x;
    int y;
int width;
    int height;
    public void grow(int dwidth, int dHeight) {
        this.width += dwidth;
        this.height += dHeight;
    }
    public int area() {
        return this.width * this.height;
    }
}
· Consider this client code:
  Rectangle r = new Rectangle();
  r.width = 10;
  r.height = 15;
      ___???____;
```

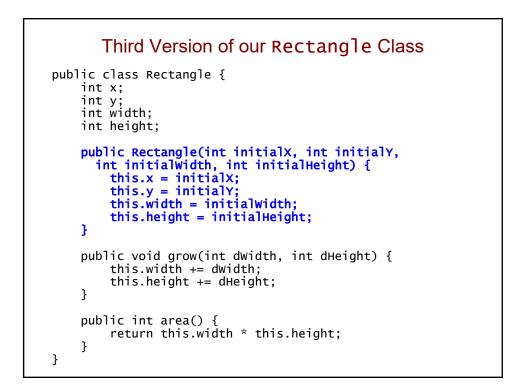


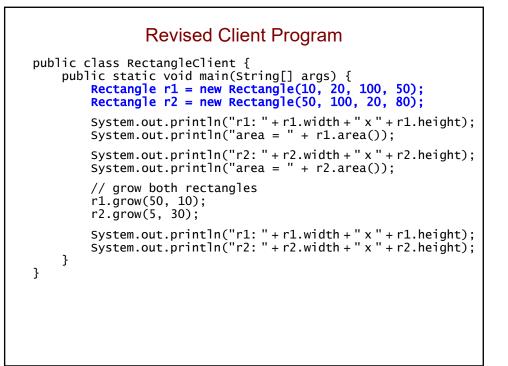


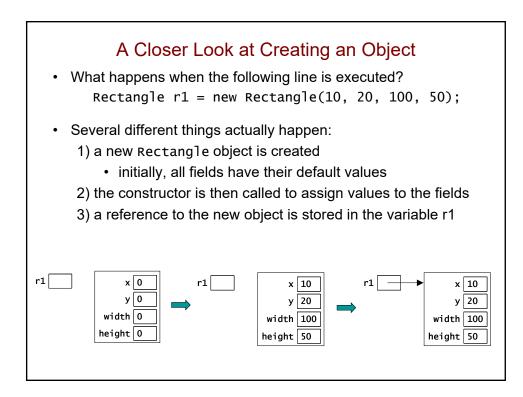


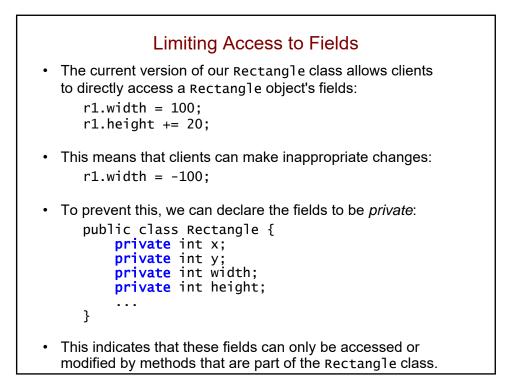


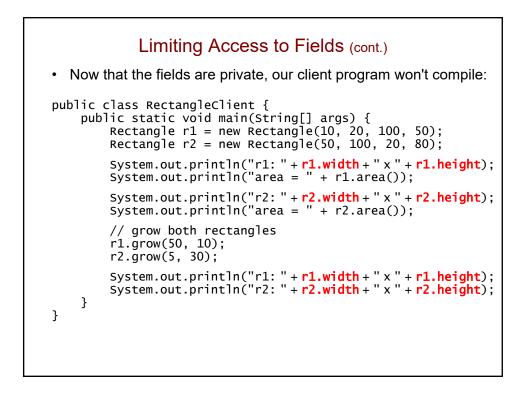


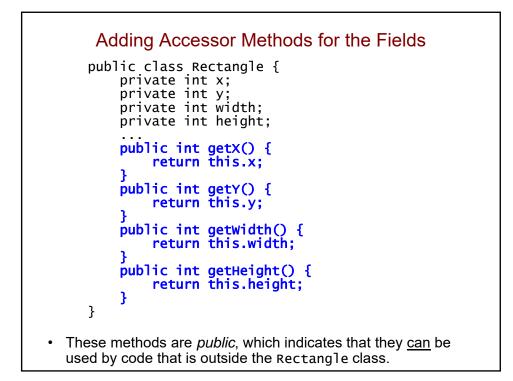


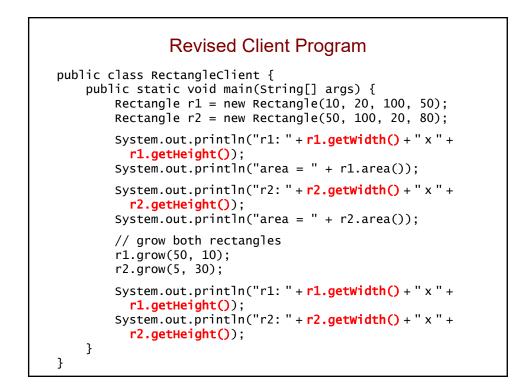






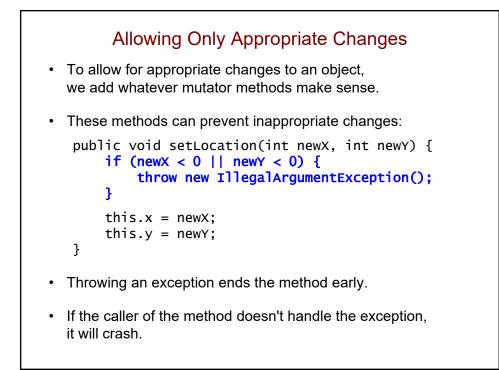






## **Access Modifiers**

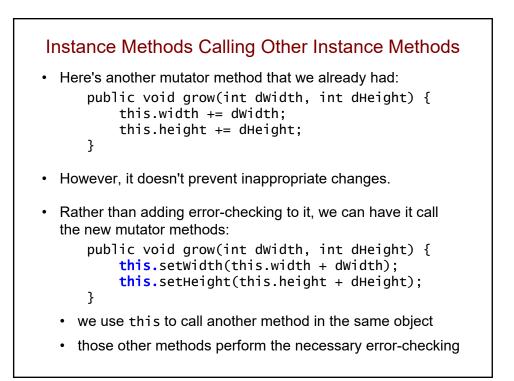
- public and private are known as access modifiers.
  - they specify where a class, field, or method can be used
- A class is usually declared to be public:
  - public class Rectangle {
  - indicates that objects of the class can be used anywhere, including in other classes
- Fields are usually declared to be private.
- Methods are usually declared to be public.
- We occasionally define private methods.
  - serve as *helper methods* for the public methods
  - · cannot be invoked by code that is outside the class

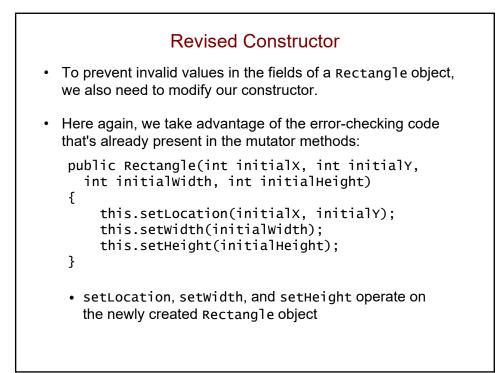


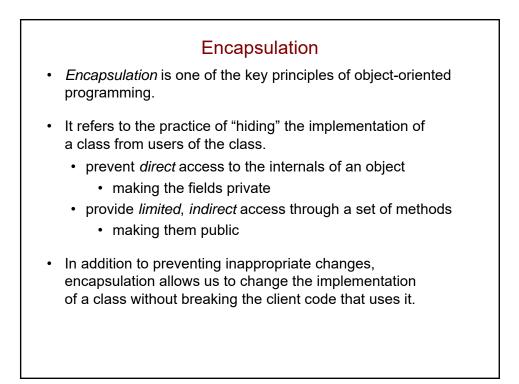
```
Allowing Only Appropriate Changes (cont.)

• Here are two other mutator methods:
    public void setWidth(int newWidth) {
        if (newWidth <= 0) {
            throw new IllegalArgumentException();
        }
        this.width = newWidth;
    }

public void setHeight(int newHeight) {
        if (newHeight <= 0) {
            throw new IllegalArgumentException();
        }
        this.height = newHeight;
    }
</pre>
```

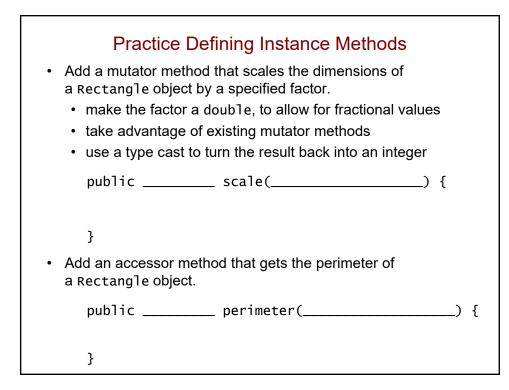


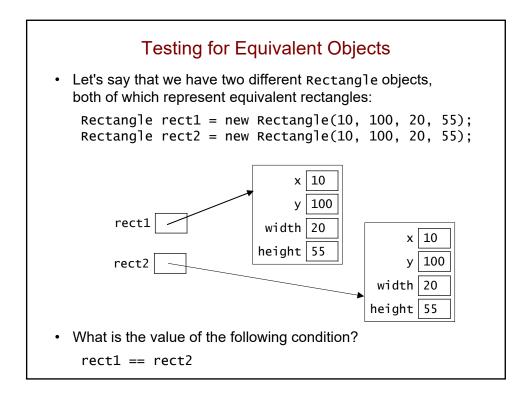


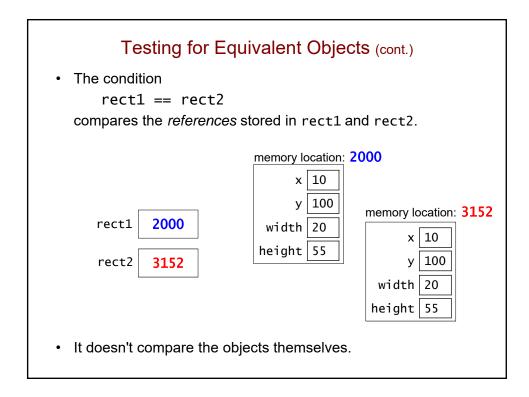


## Abstraction

- *Abstraction* involves focusing on the essential properties of something, rather than its inner or low-level details.
  - an important concept in computer science
- Encapsulation leads to abstraction.
  - example: rather than treating a Rectangle as four ints, we treat it as an object that's capable of growing itself, changing its location, etc.





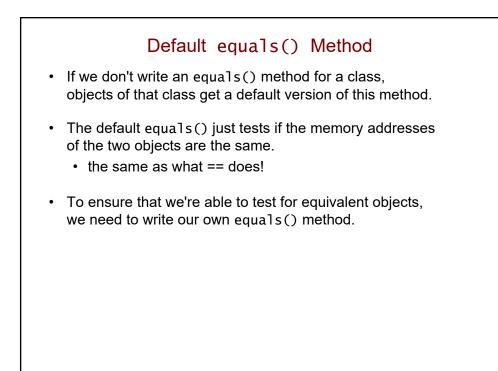


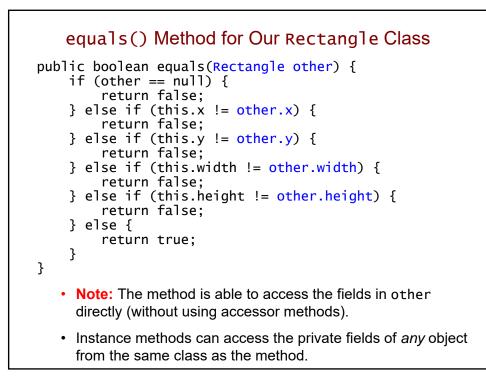
## Testing for Equivalent Objects (cont.)

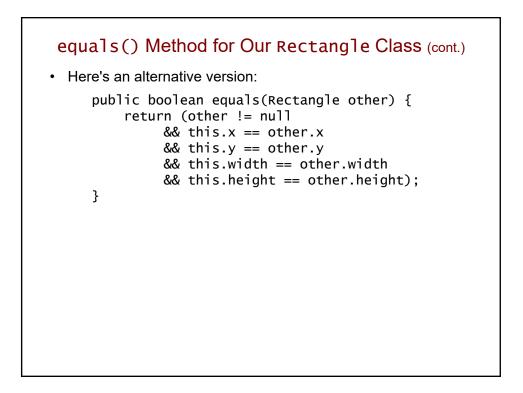
• Recall: to test for equivalent objects, we need to use the equals method:

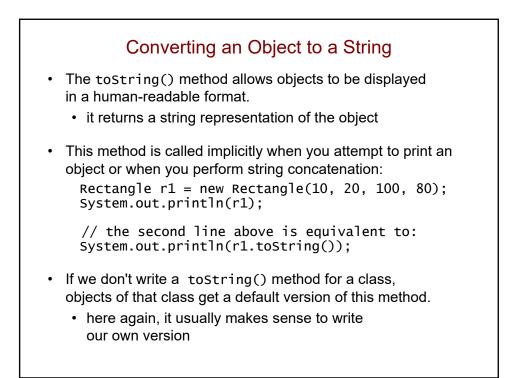
```
rect1.equals(rect2)
```

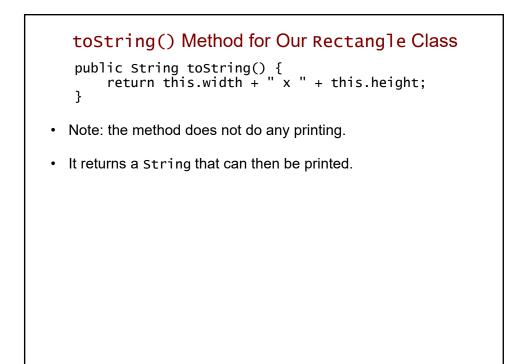
- Java's built-in classes have equals methods that:
  - return true if the two objects are equivalent to each other
  - return false otherwise





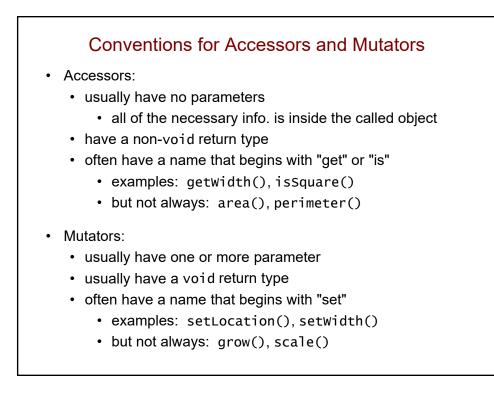


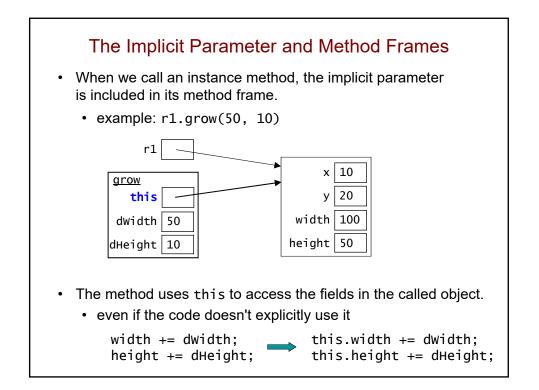


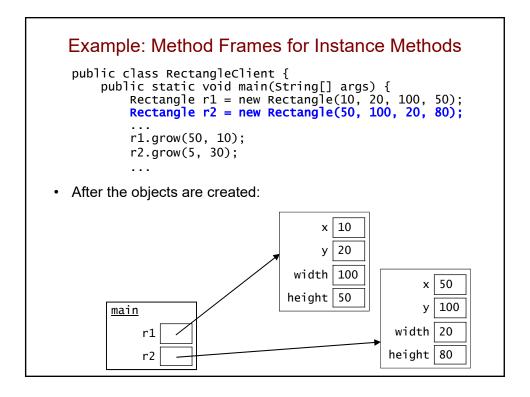


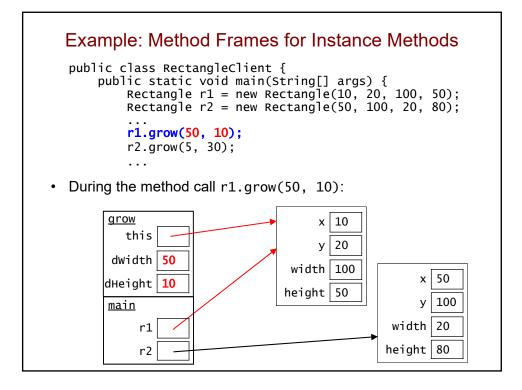
## **Revised Client Program**

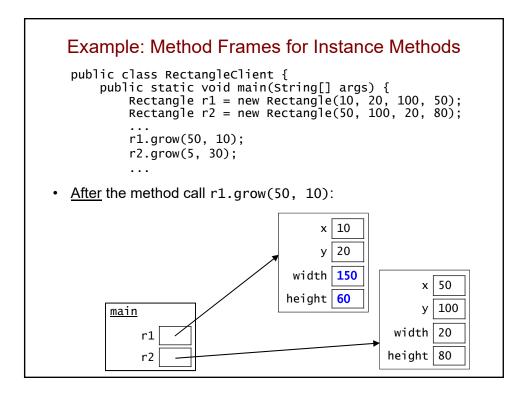
```
public class RectangleClient {
    public static void main(String[] args) {
        Rectangle r1 = new Rectangle(10, 20, 100, 50);
        Rectangle r2 = new Rectangle(50, 100, 20, 80);
        System.out.println("r1: " + r1);
        System.out.println("area = " + r1.area());
        System.out.println("r2: " + r2);
        System.out.println("area = " + r2.area());
        // grow both rectangles
        r1.grow(50, 10);
        r2.grow(5, 30);
        System.out.println("r1: " + r1);
        System.out.println("r1: " + r1);
        System.out.println("r1: " + r2);
    }
}
```

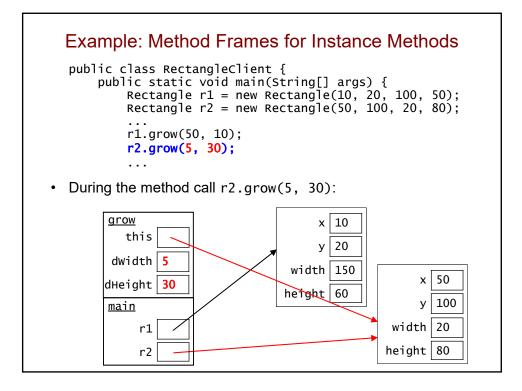


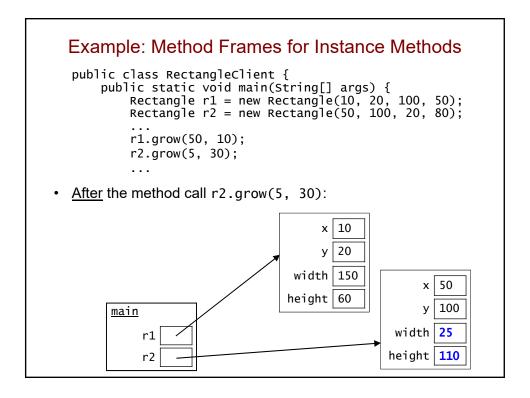


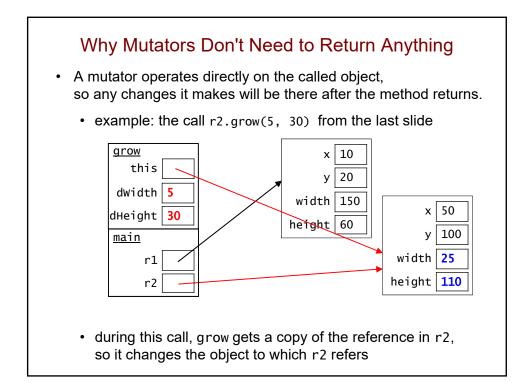




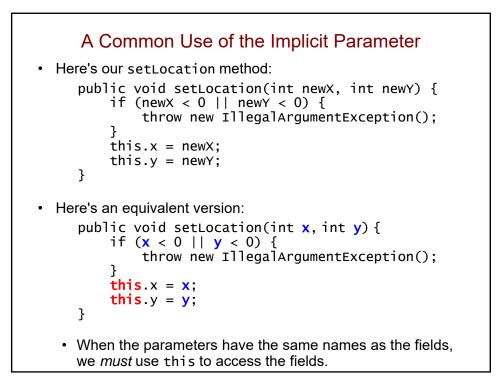


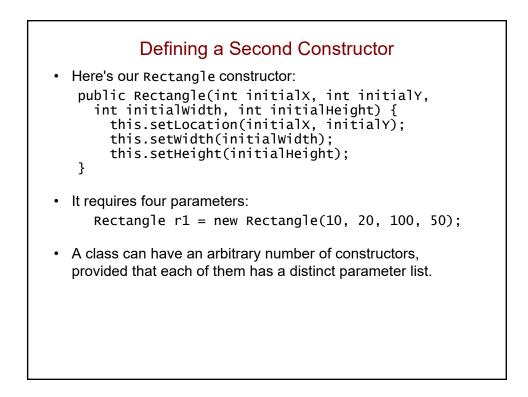


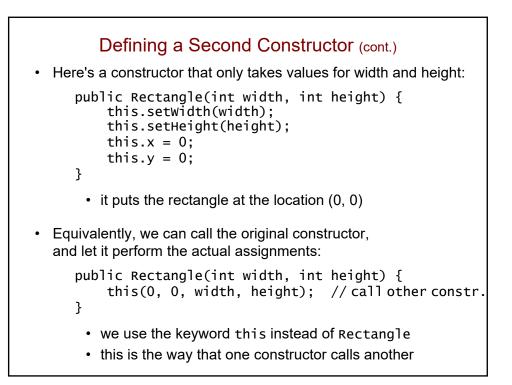


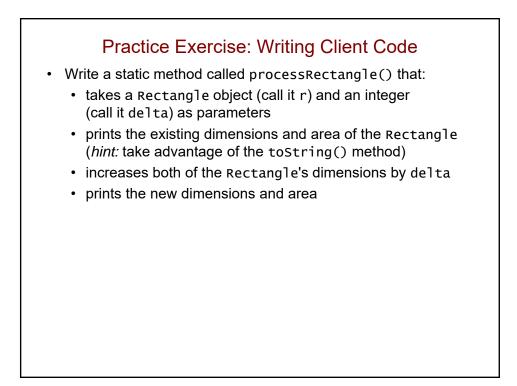


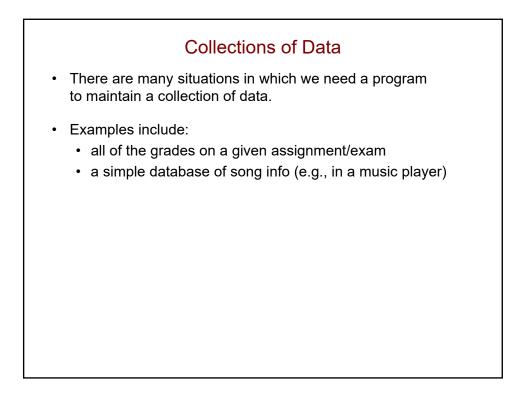
```
Variable Scope: Static vs. Non-Static Methods
public class Foo {
    private int x;
    public static int bar(int b, int c, Foo f) {
        c = c + this.x; // would not compile
        return 3*b + f.x;
                                  // would compile
    }
    public int boo(int d, Foo f) {
        d = d + this.x + f.x; // would compile
        return 2 * d;
    }
}
• Static methods (like bar above) do NOT have a called object,
  so they can't access its fields.
  Instance/non-static methods (like boo above) do have a called
  object, so they can access its fields.
  Any method of a class can access fields in an object of that class
  that is passed in as a parameter (like the parameter f above).
```

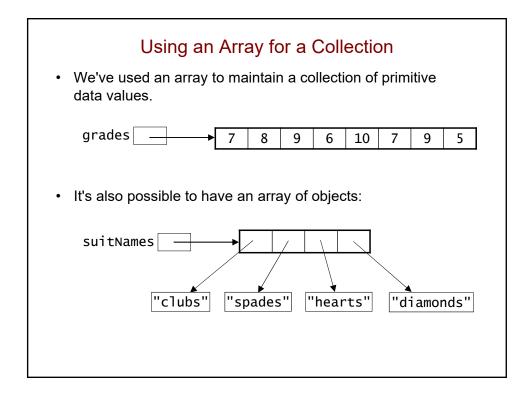


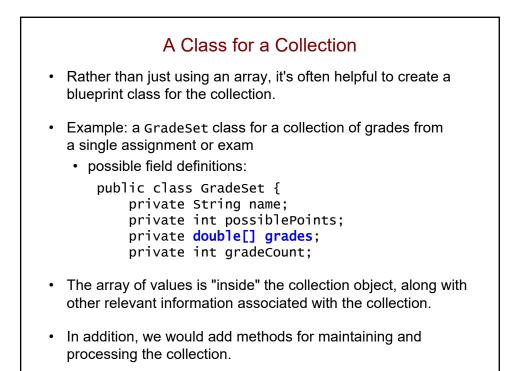


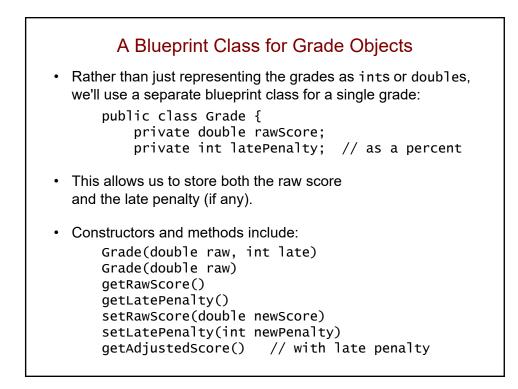


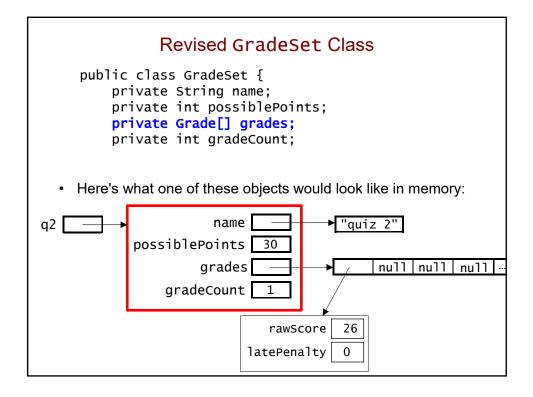


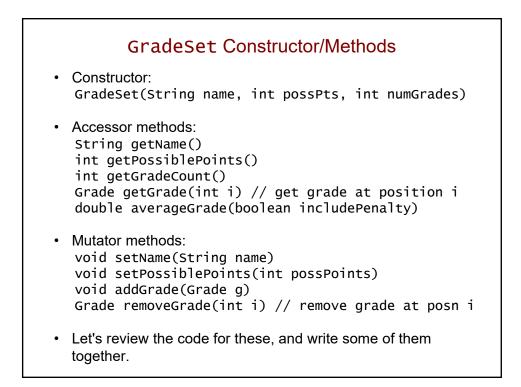


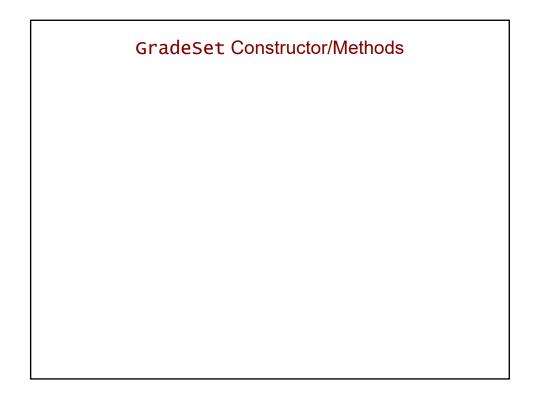


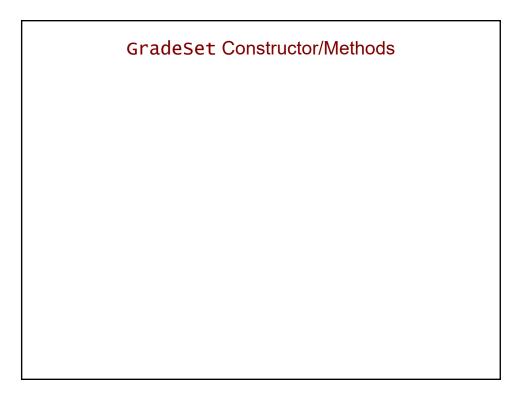


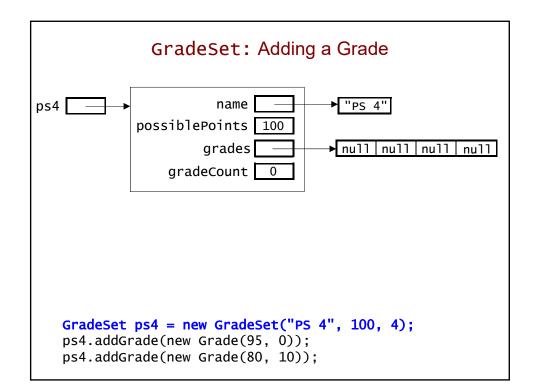


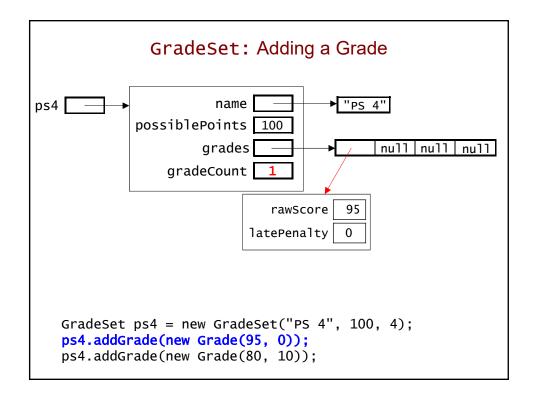


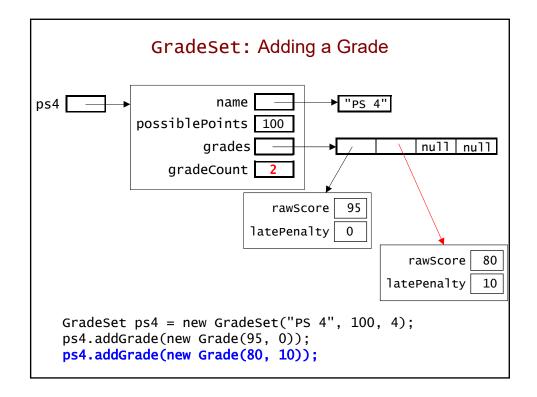


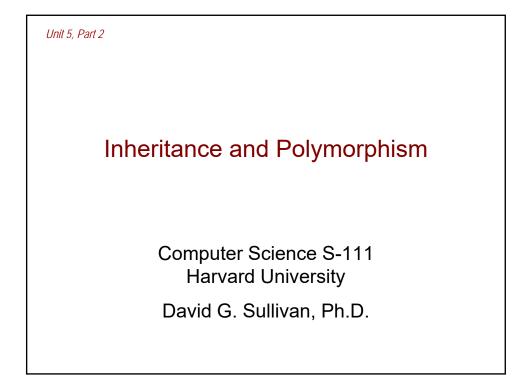


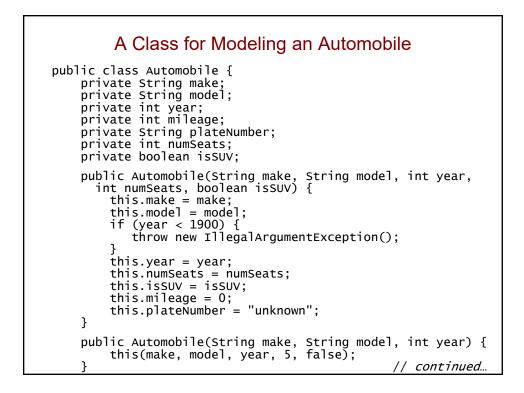


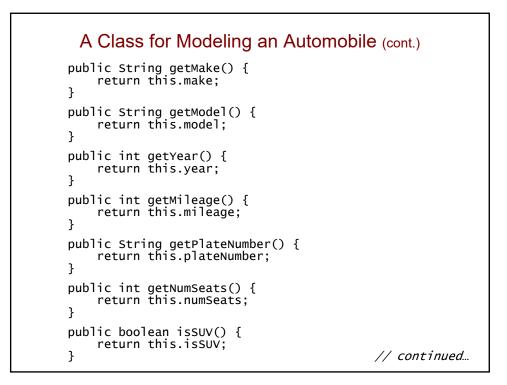




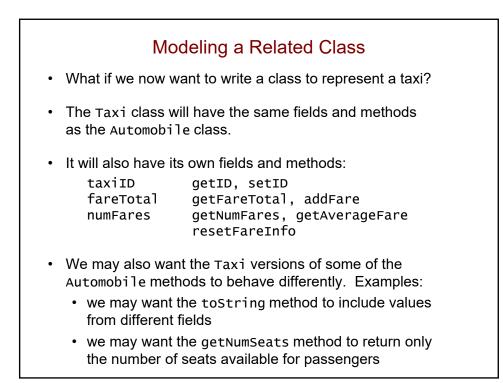


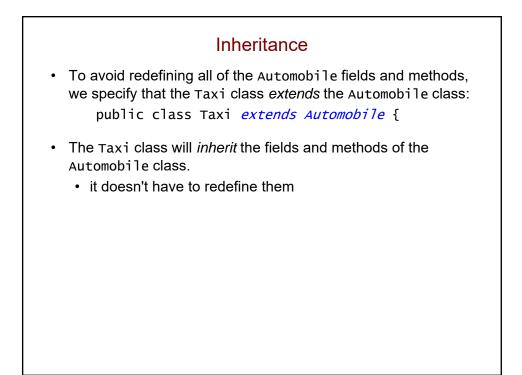


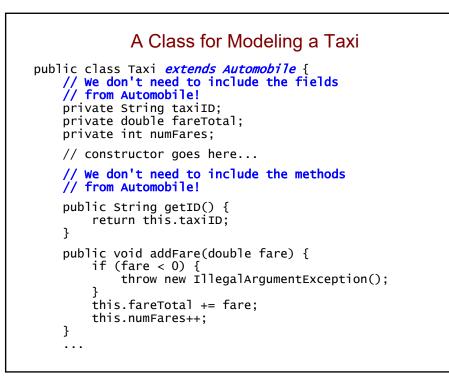


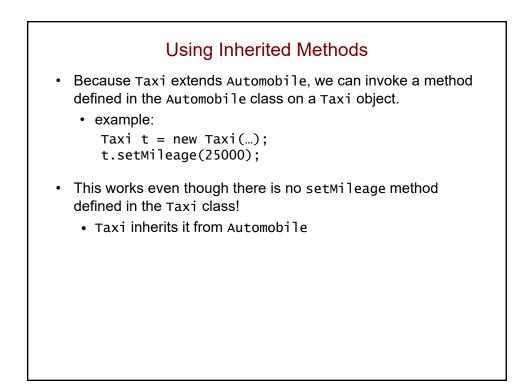


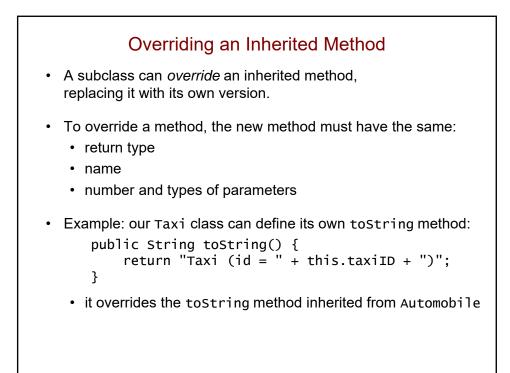
```
A Class for Modeling an Automobile (cont.)
    public void setMileage(int newMileage) {
        if (newMileage < this.mileage) {</pre>
            throw new IllegalArgumentException();
        }
        this.mileage = newMileage;
    }
    public void setPlateNumber(String plate) {
        this.plateNumber = plate;
    }
    public String toString() {
        String str = this.make + " " + this.model;
        str += "( " + this.numSeats + " seats)";
        return str;
    }
}
  There are no mutators for the other fields. Why not?
٠
```

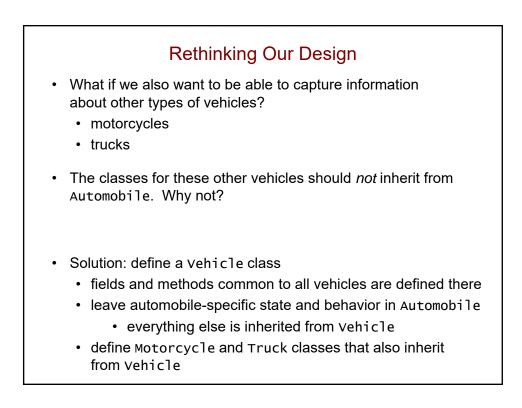


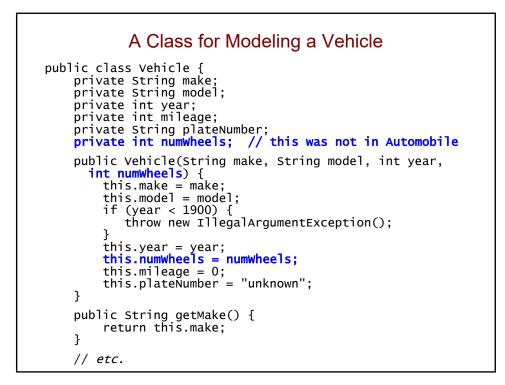


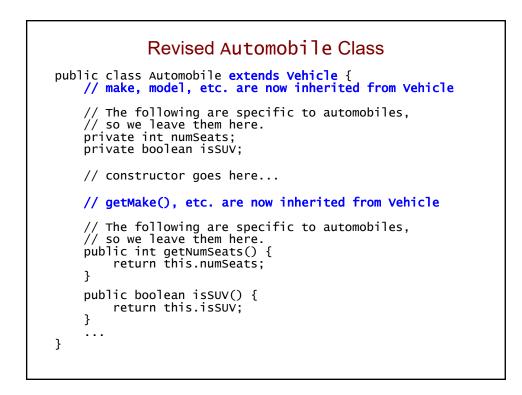


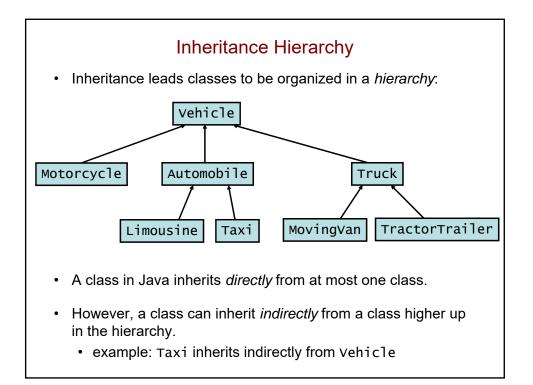


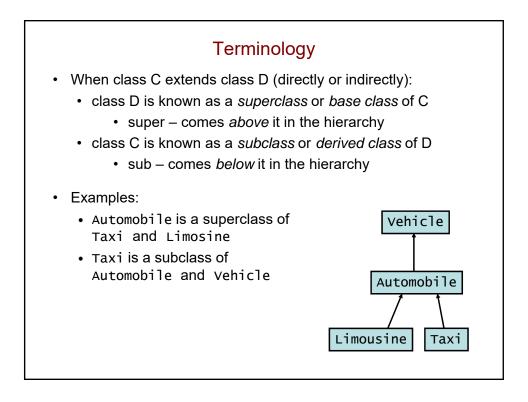


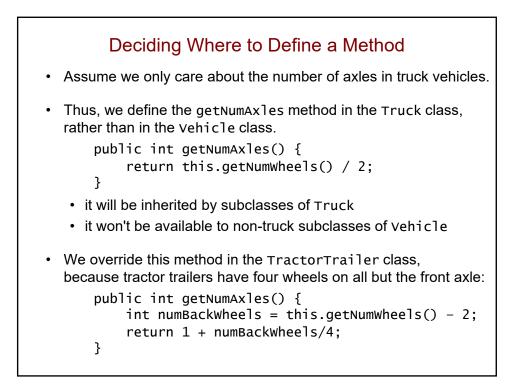


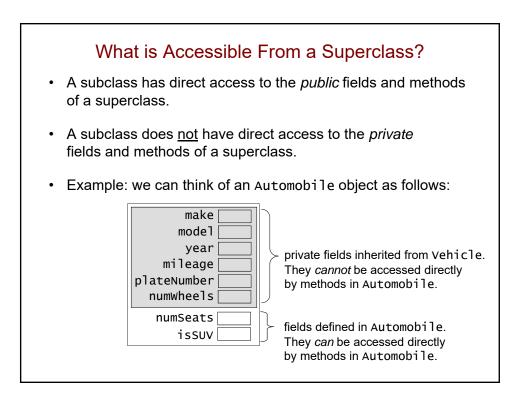


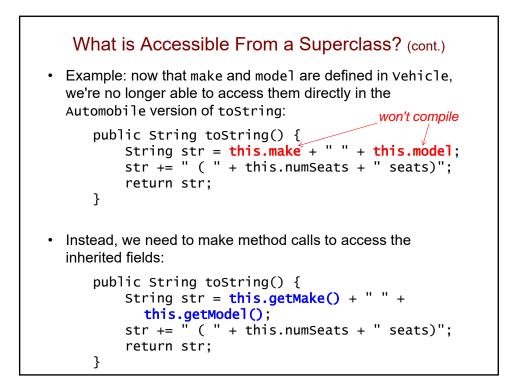


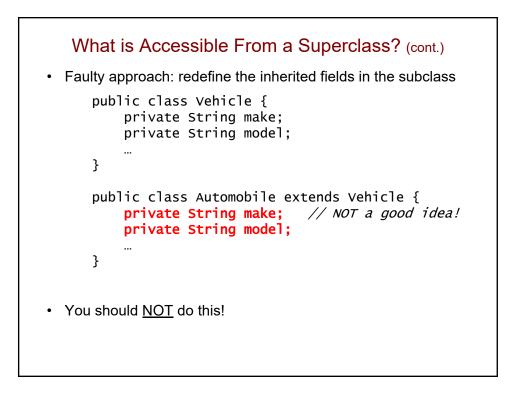


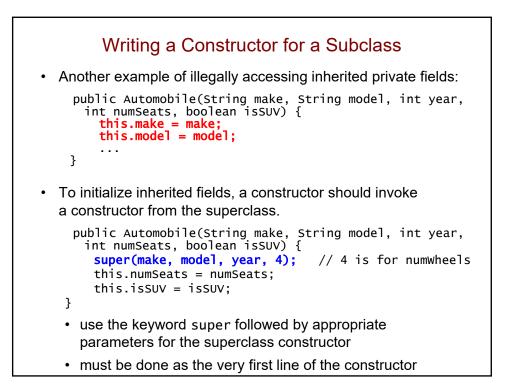


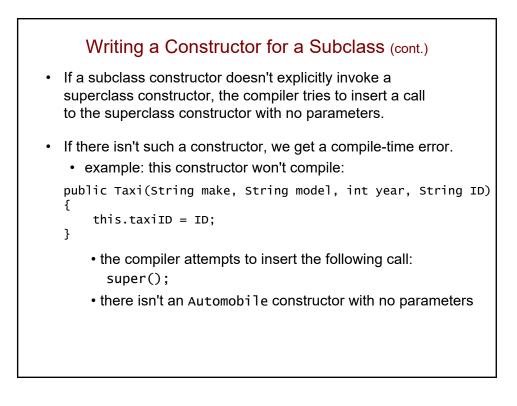


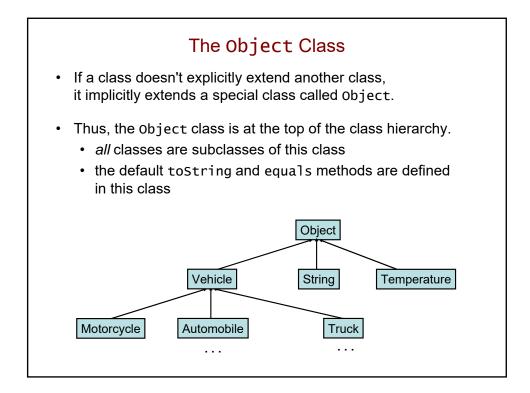


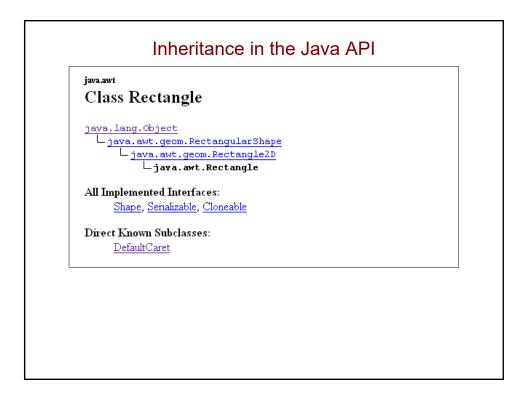


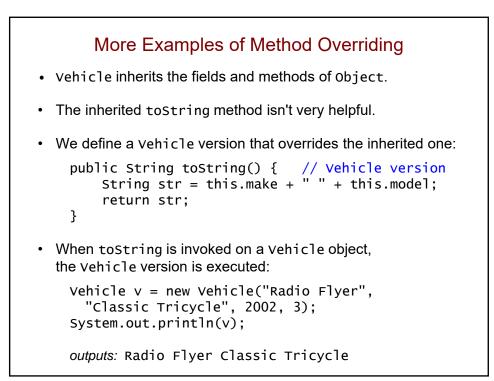


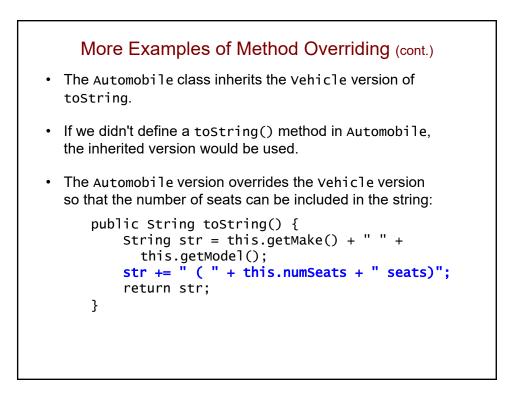


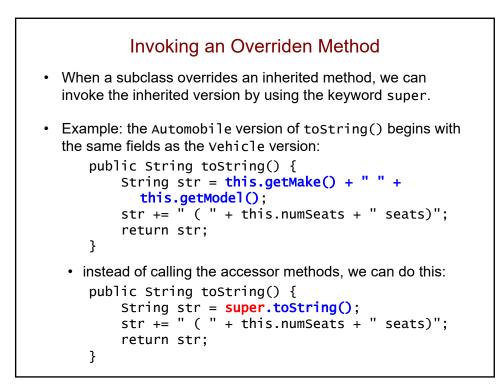


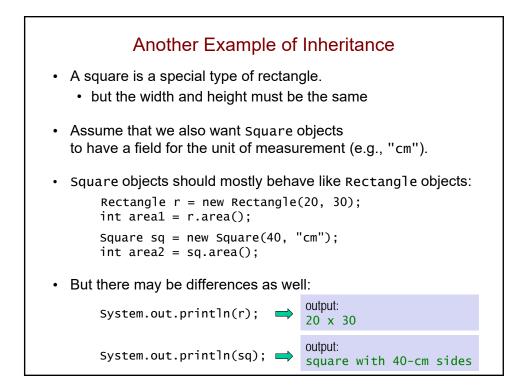


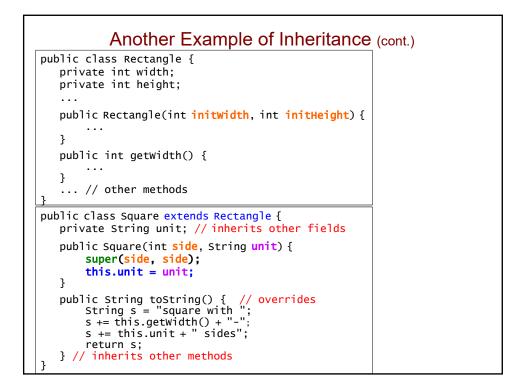


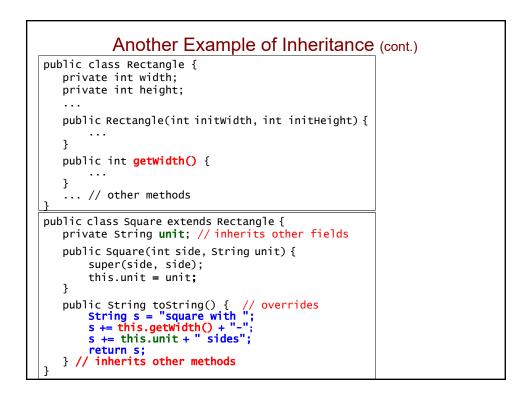


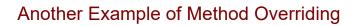








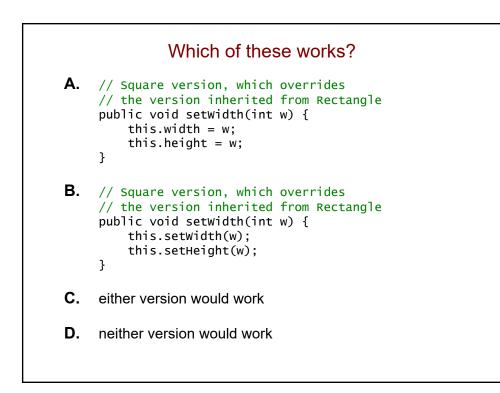


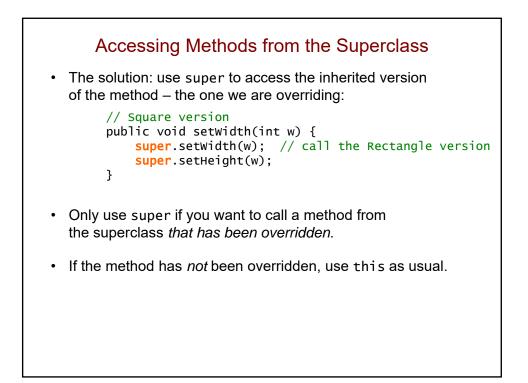


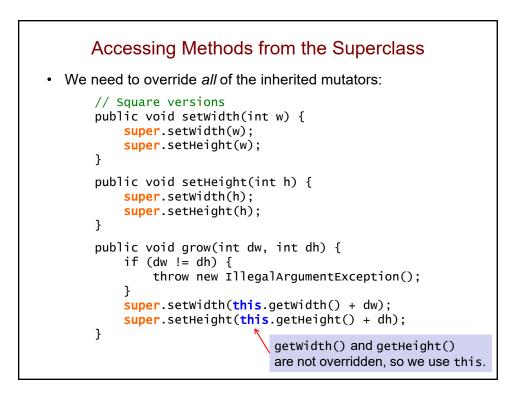
• The Rectangle class has the following mutator method:

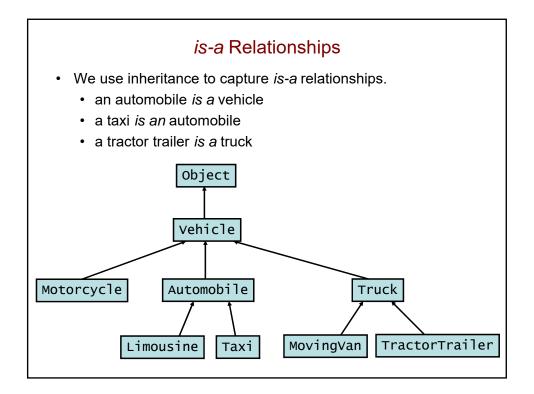
```
public void setWidth(int w) {
    if (w <= 0) {
        throw new IllegalArgumentException();
    }
    this.width = w;
}</pre>
```

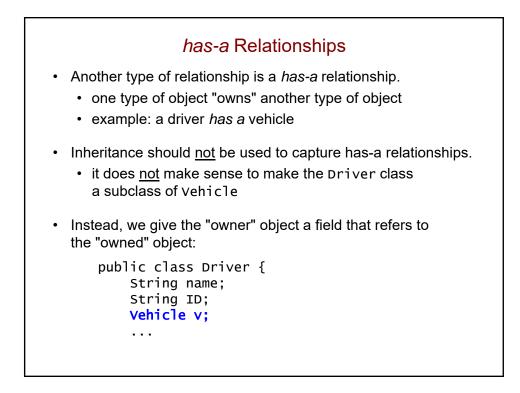
• The square class inherits it. Why should we override it?

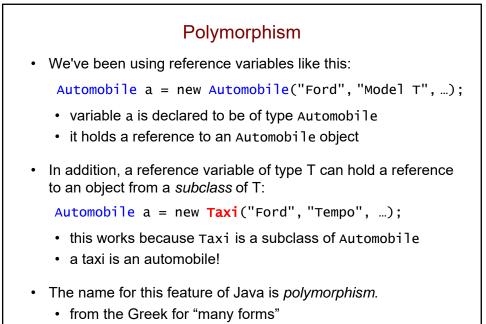




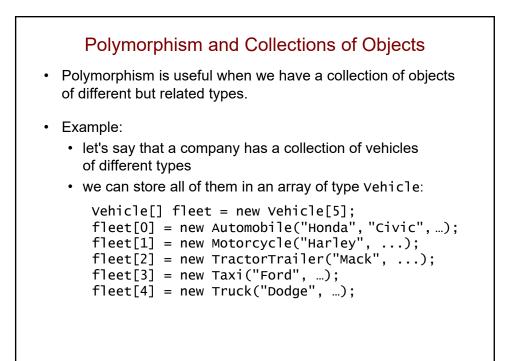


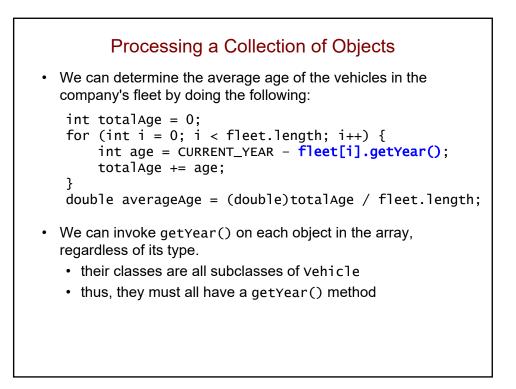


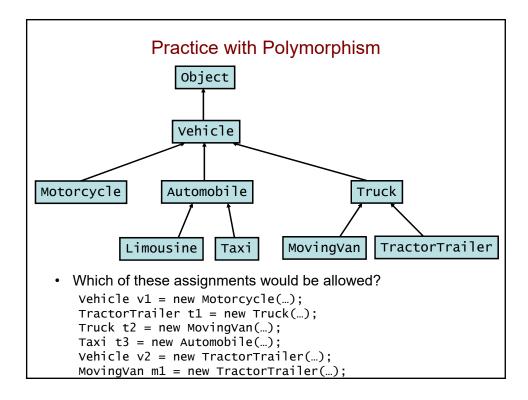


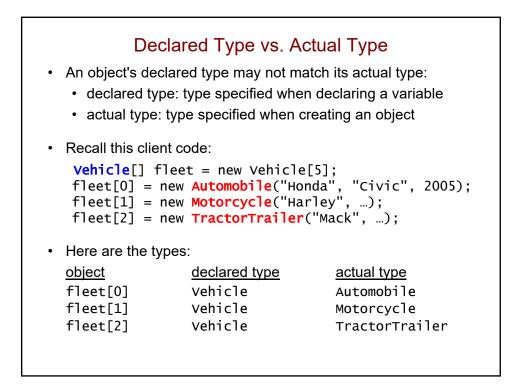


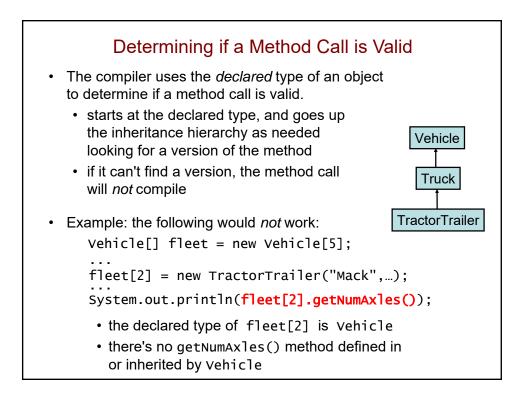
• the same code can be used with objects of different types!

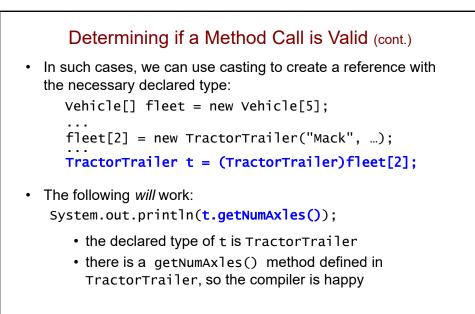


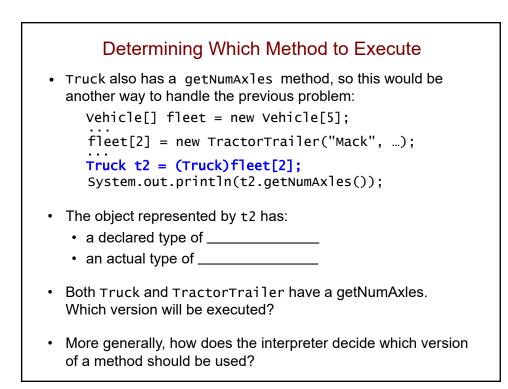


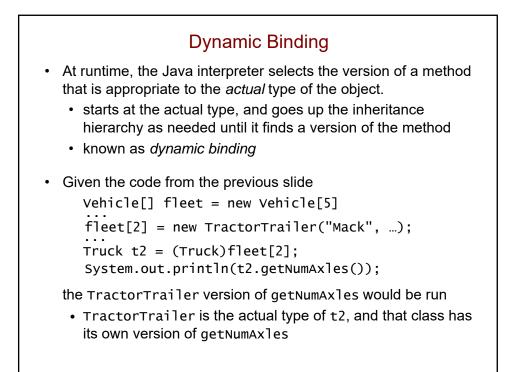


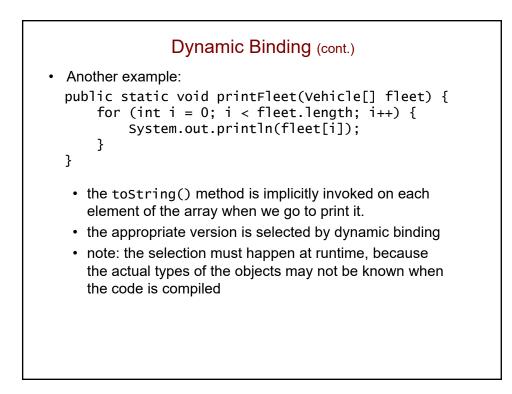






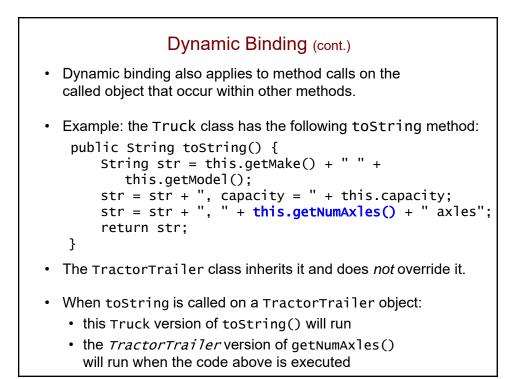


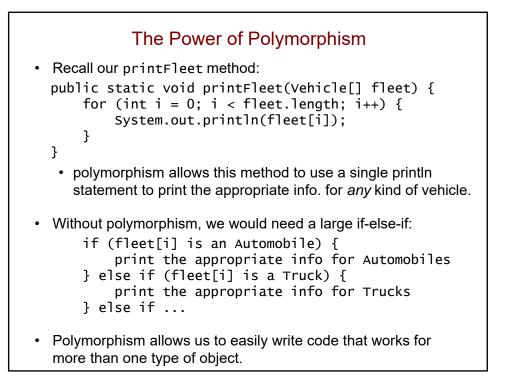


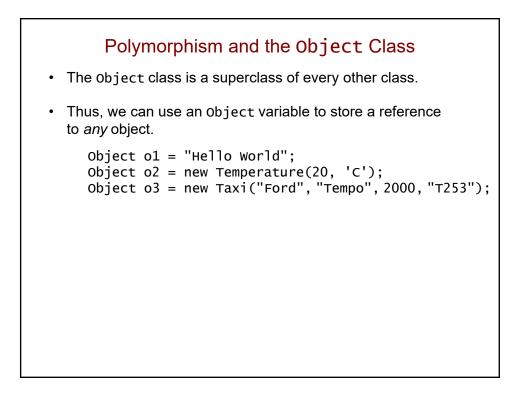


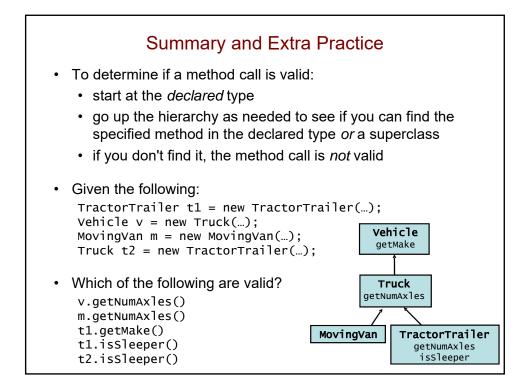
```
Dynamic Binding (cont.)
• Recall our initialization of the array:
    Vehicle[] fleet = new Vehicle[5];
    fleet[0] = new Automobile("Honda", "Civic", ...);
    fleet[1] = new Motorcycle("Harley", ...);
    fleet[2] = new TractorTrailer("Mack", ...);
    ...
• System.out.println(fleet[0]); will invoke the
    Automobile version of the toString() method.
• Motorcycle does not define its own toString() method,
    so System.out.println(fleet[1]); will invoke the vehicle
    version of toString(), which is inherited by Motorcycle.
• TractorTrailer does not define its own toString()
    but Truck does, so System.out.println(fleet[2]);
    will invoke the Truck version of toString(), which is inherited
```

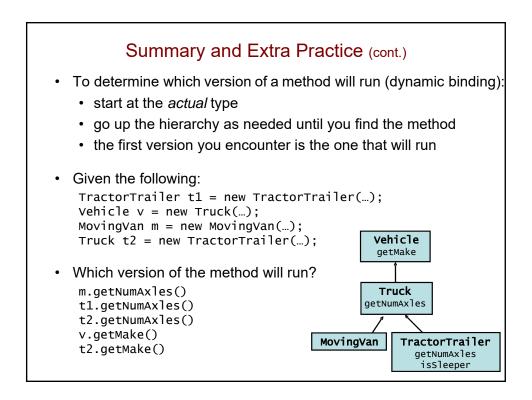
by TractorTrailer.

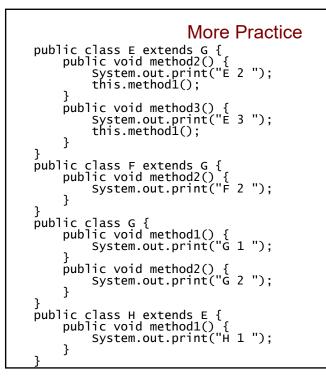


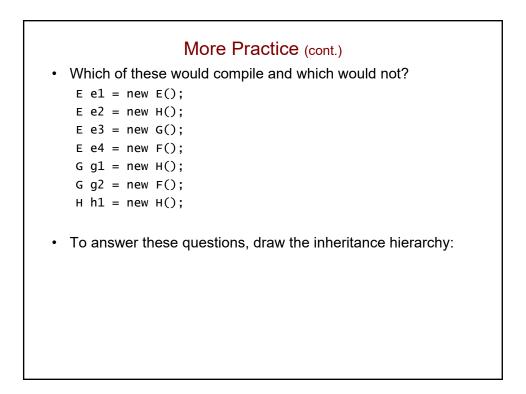


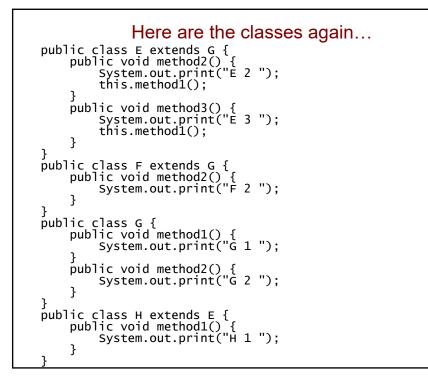


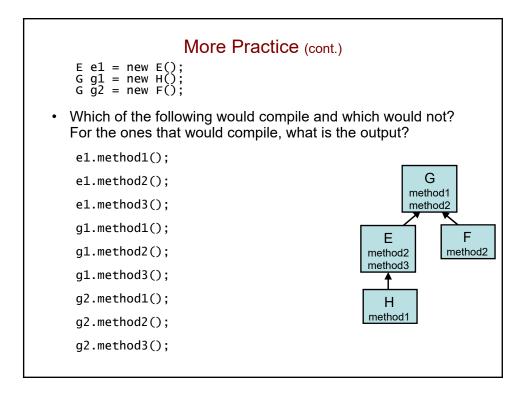


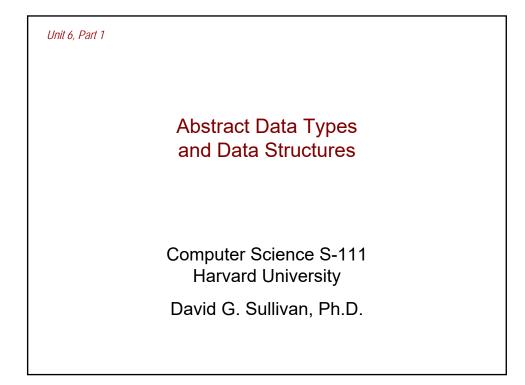


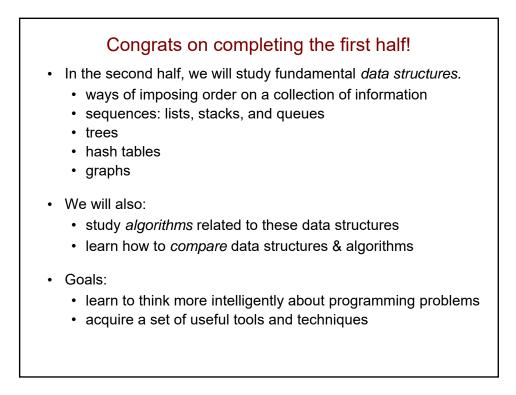


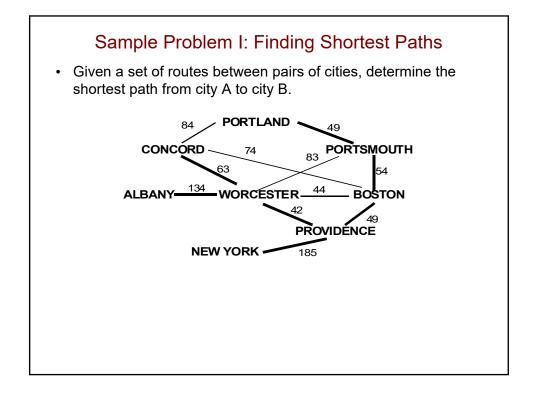


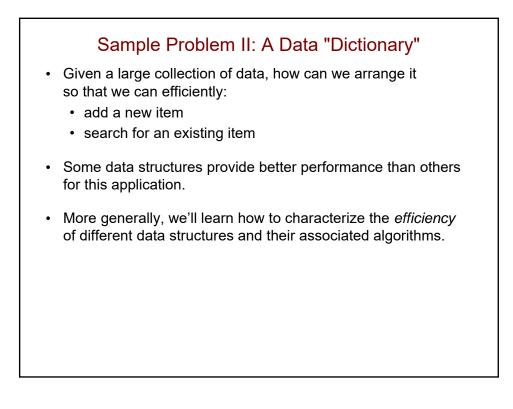






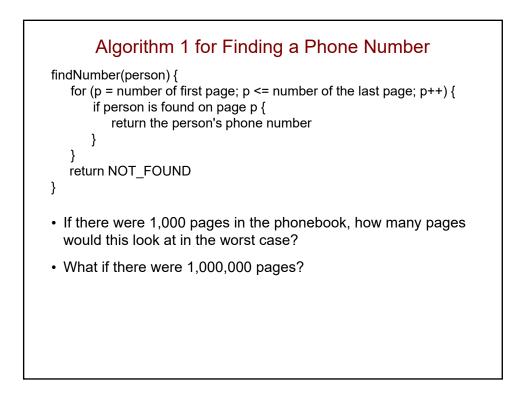


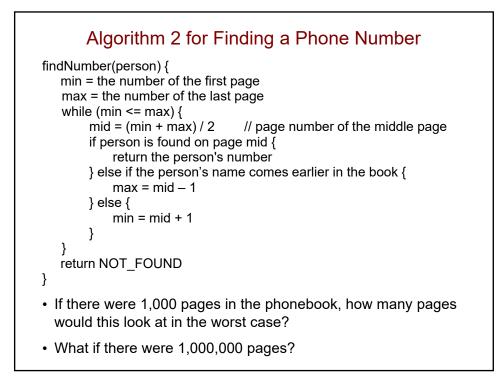


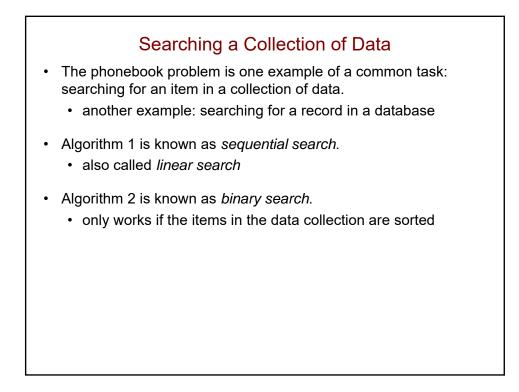


## Example of Comparing Algorithms

- Consider the problem of finding a phone number in a phonebook.
- Let's informally compare the time efficiency of two algorithms for this problem.





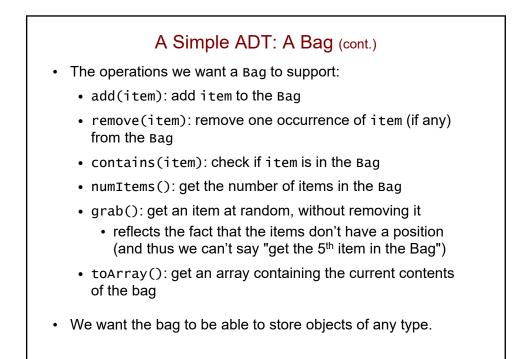


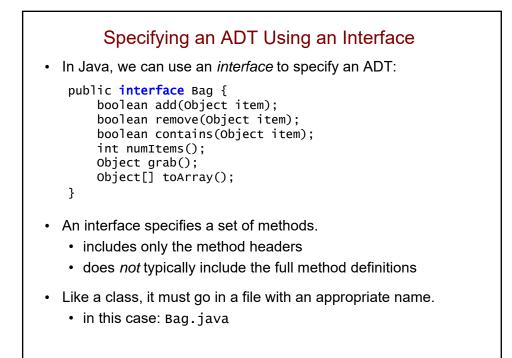
## Abstract Data Types

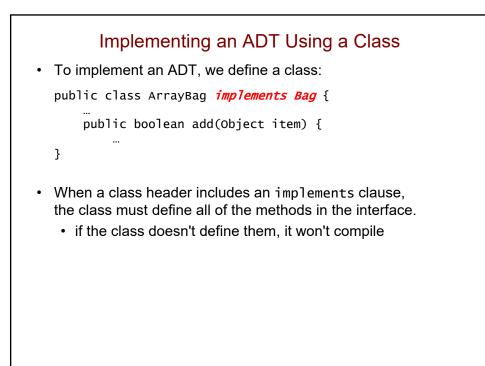
- An abstract data type (ADT) is a model of a data structure that specifies:
  - · the characteristics of the collection of data
  - · the operations that can be performed on the collection
- It's *abstract* because it doesn't specify *how* the ADT will be implemented.
  - does not commit to any low-level details
- A given ADT can have multiple implementations.

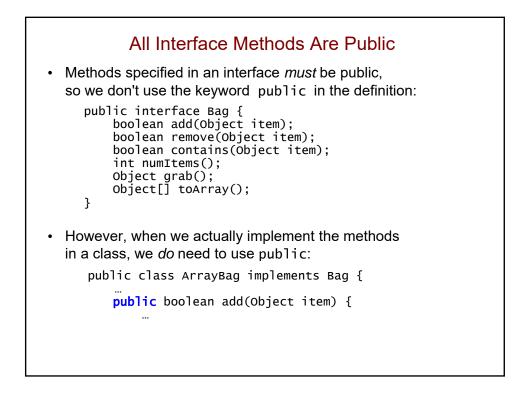
## A Simple ADT: A Bag

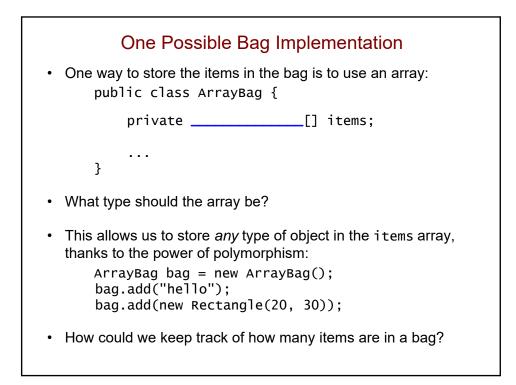
- A bag is just a container for a group of data items.
  - · analogy: a bag of candy
- The positions of the data items don't matter (unlike a list).
  - {3, 2, 10, 6} is equivalent to {2, 3, 6, 10}
- The items do *not* need to be unique (unlike a set).
  - {7, 2, 10, 7, 5} isn't a set, but it is a bag

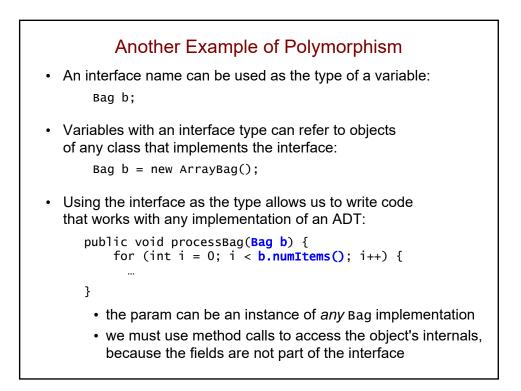


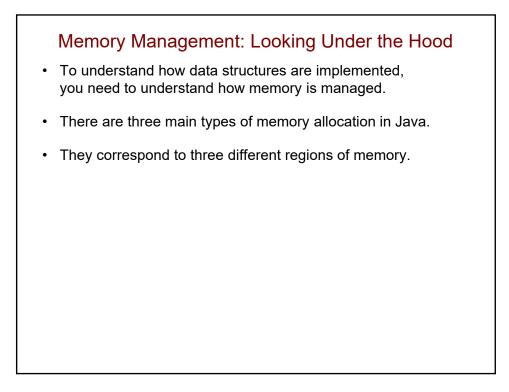


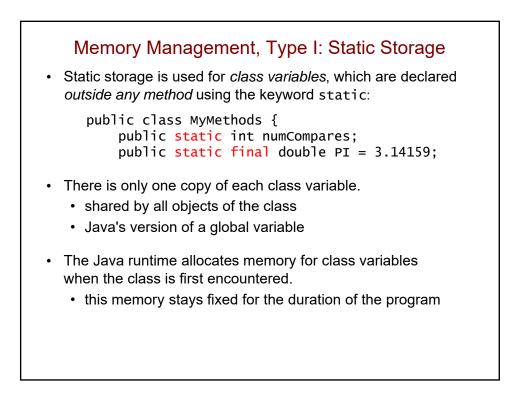


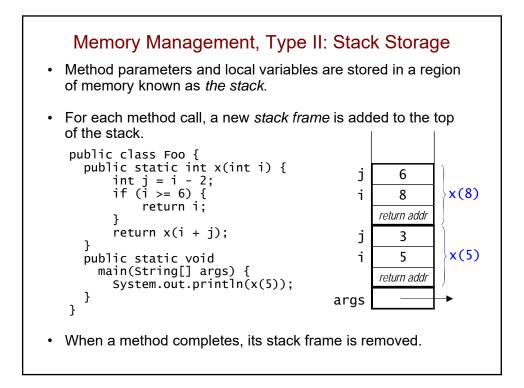


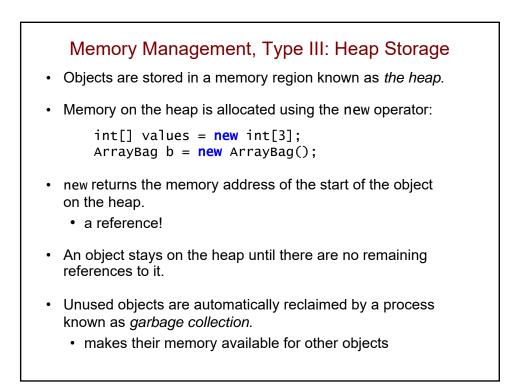


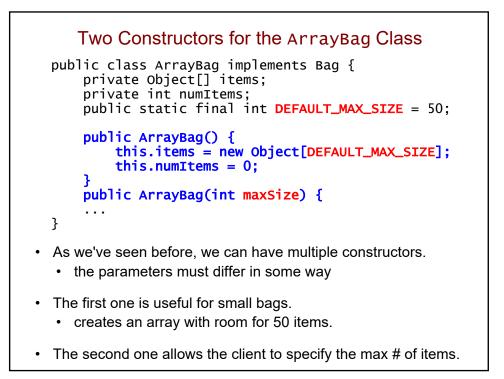


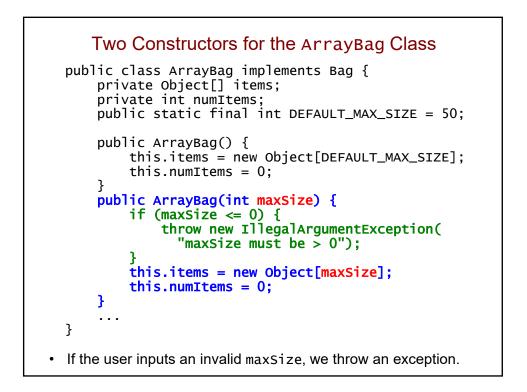


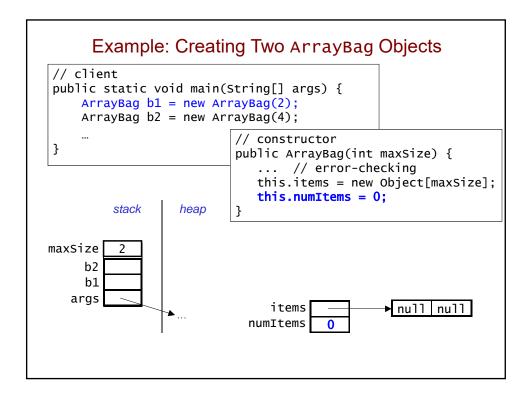


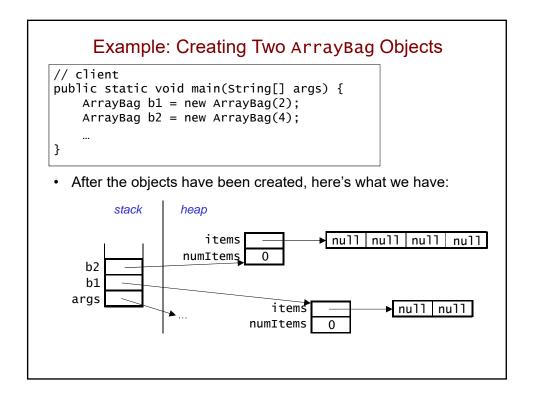


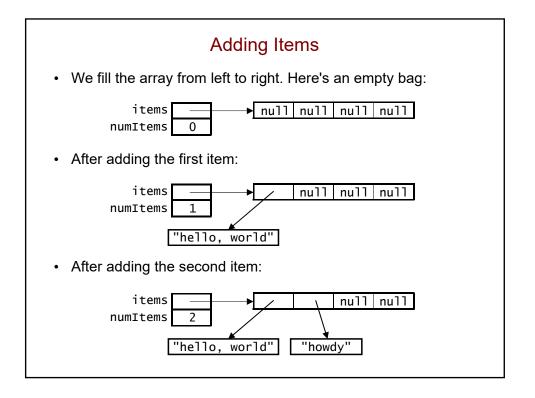


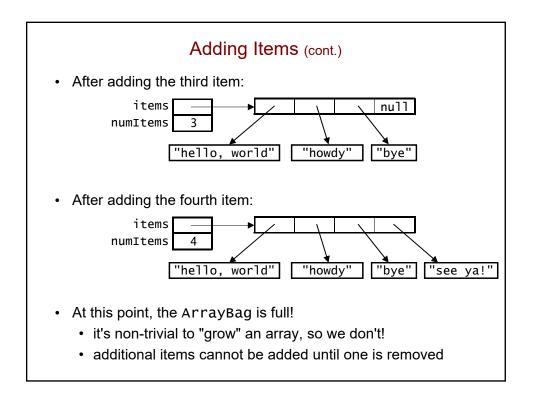


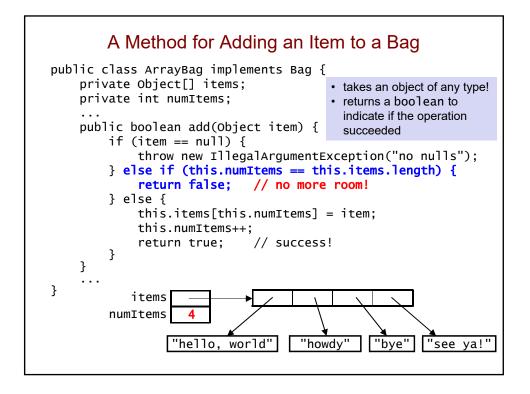


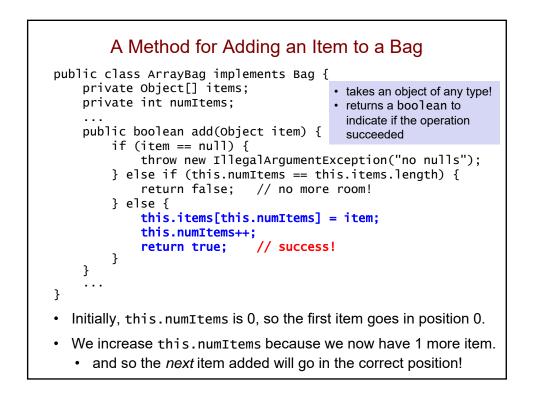


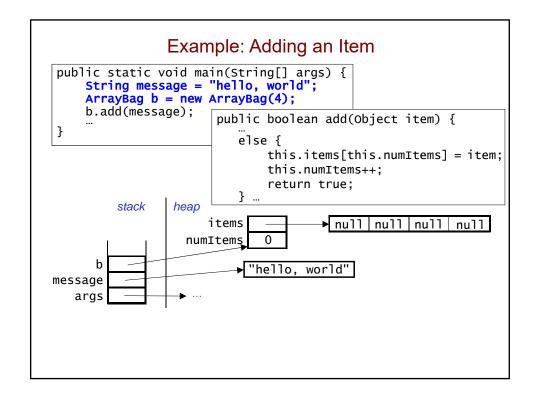


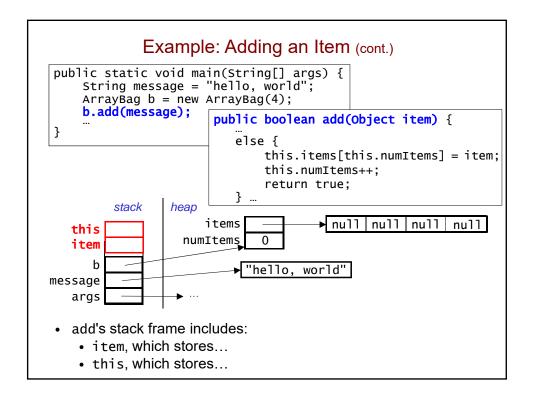


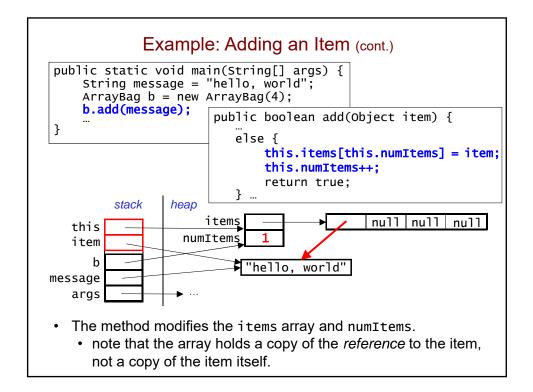


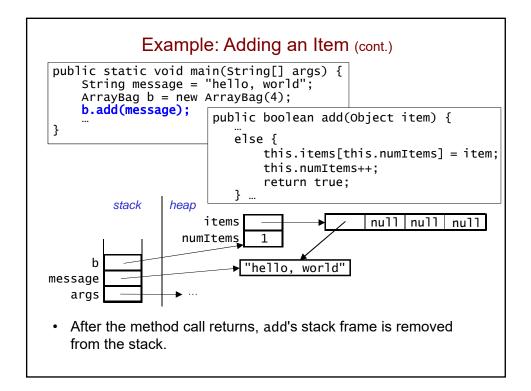


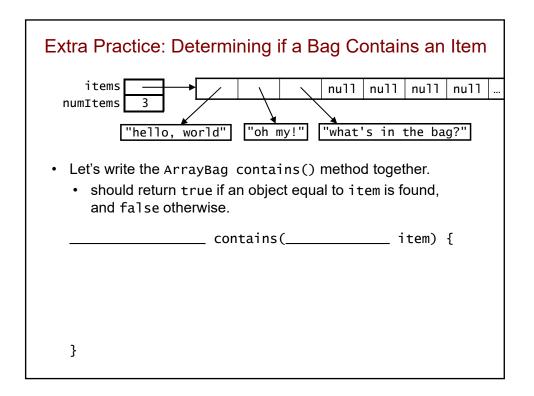




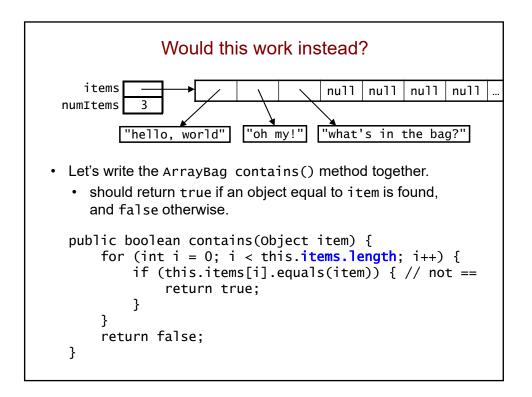


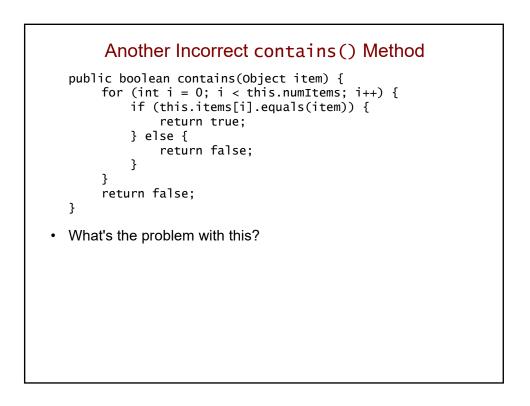




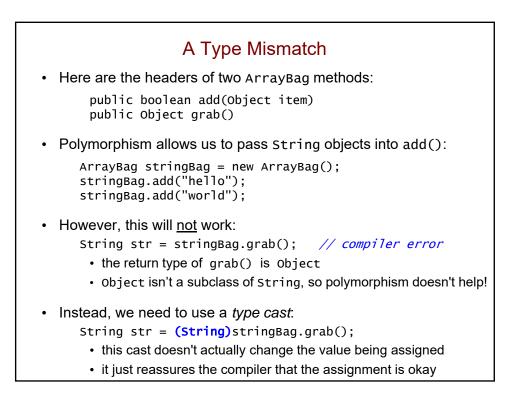


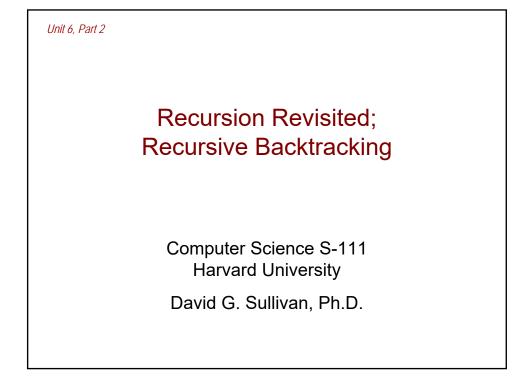


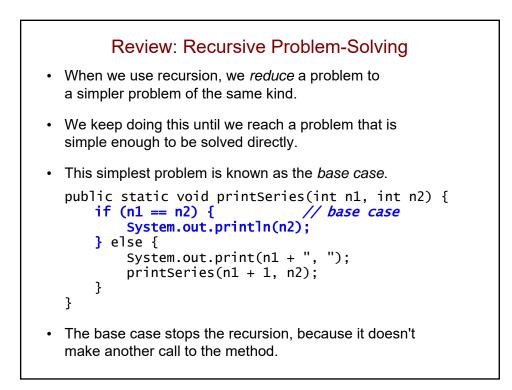


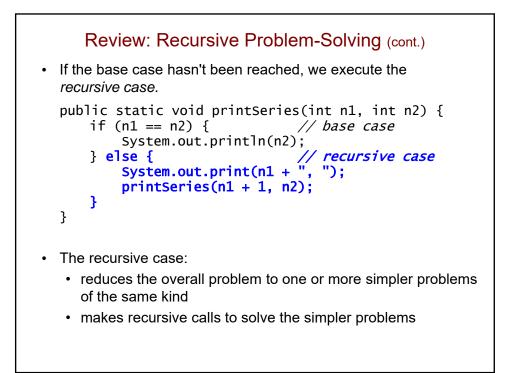


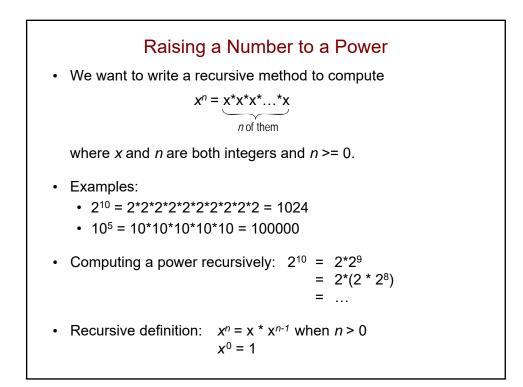
## A Method That Takes a Bag as a Parameter public boolean containsAll(Bag otherBag) { if (otherBag == null || otherBag.numItems() == 0) { return false; } Object[] otherItems = otherBag.toArray(); for (int i = 0; i < otherItems.length; i++) {</pre> if (! this.contains(otherItems[i])) { return false; } } return true; } We use Bag instead of ArrayBag as the type of the parameter. allows this method to be part of the Bag interface allows us to pass in any object that implements Bag We must use methods in the interface to manipulate otherBag. · we can't use the fields, because they're not in the interface

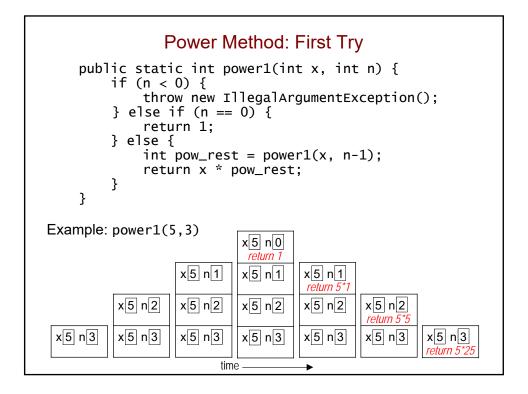


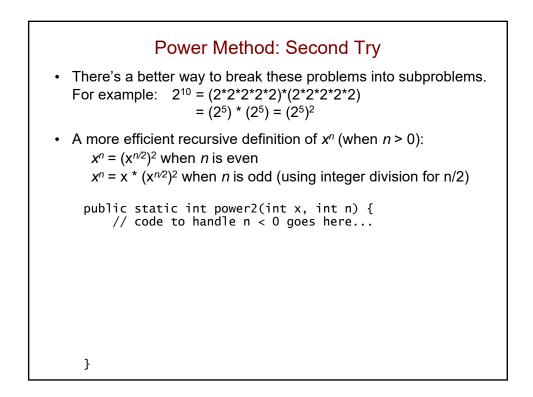


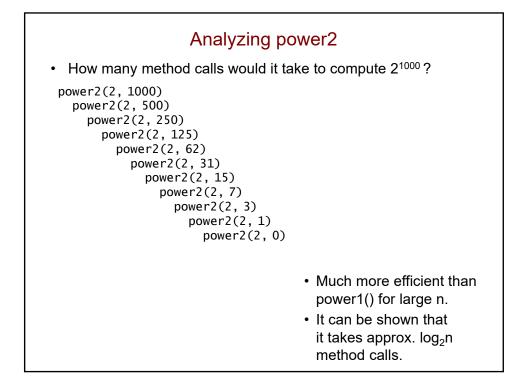


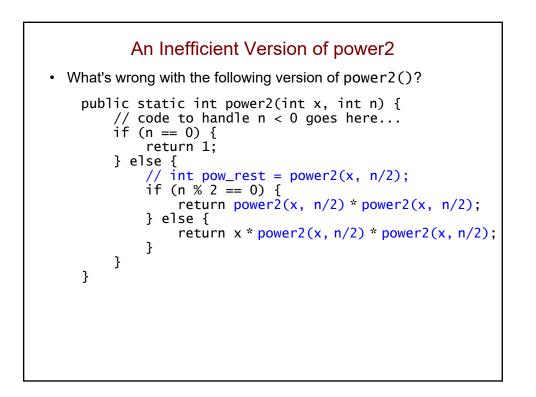


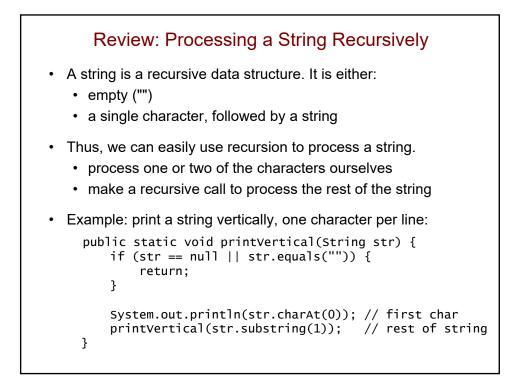


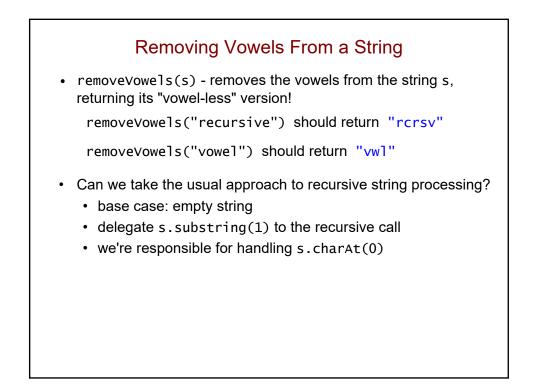


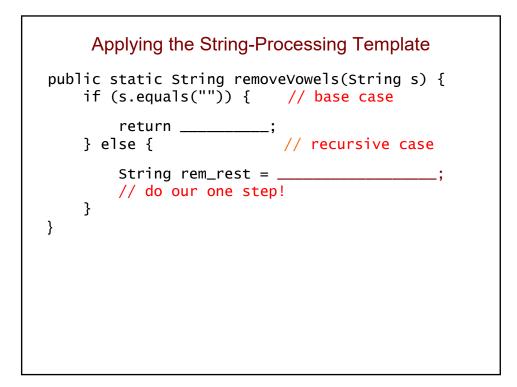


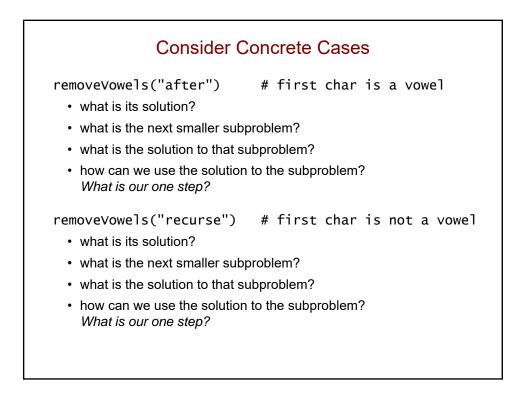


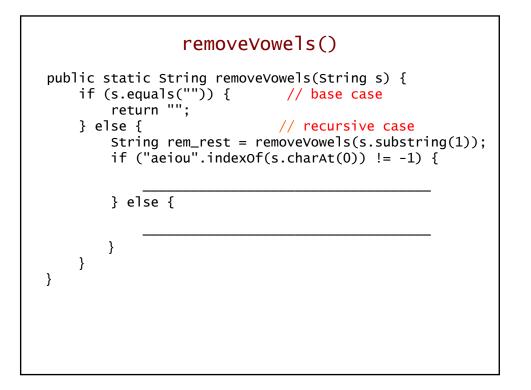


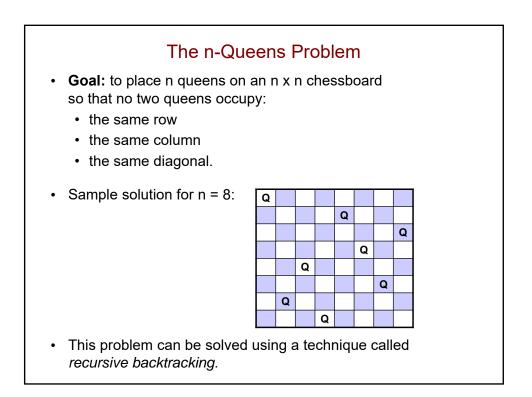


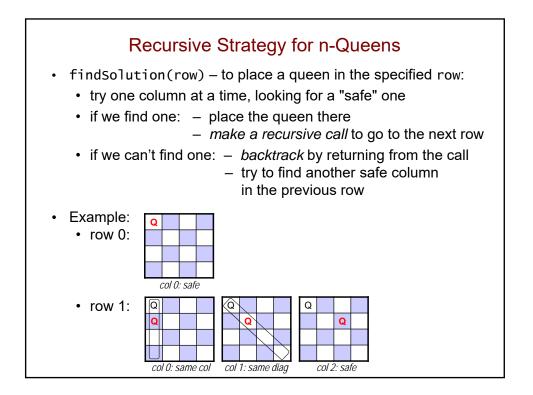


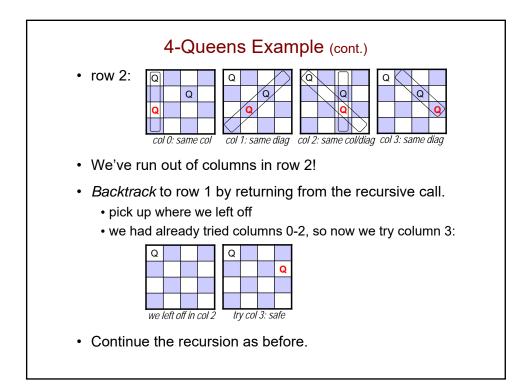


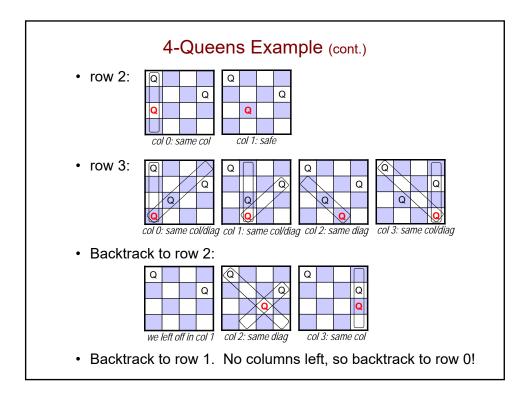


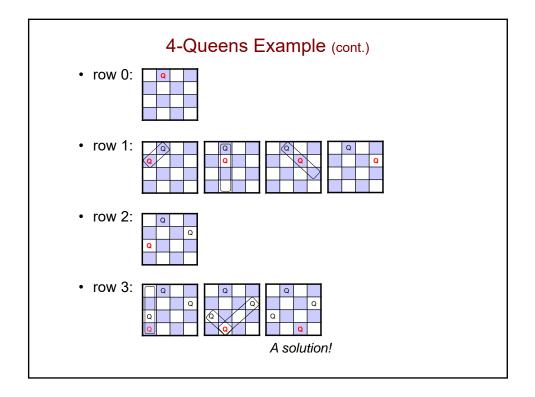


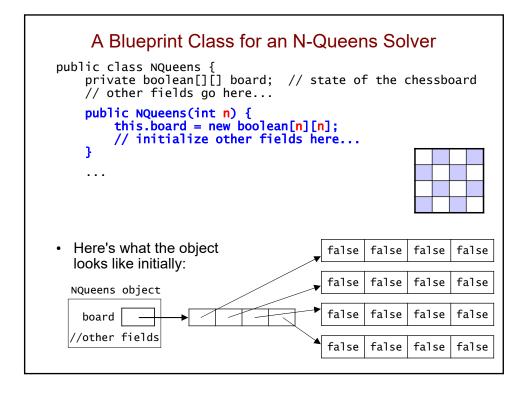


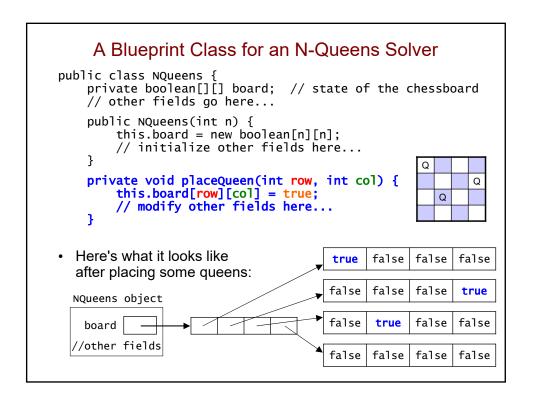


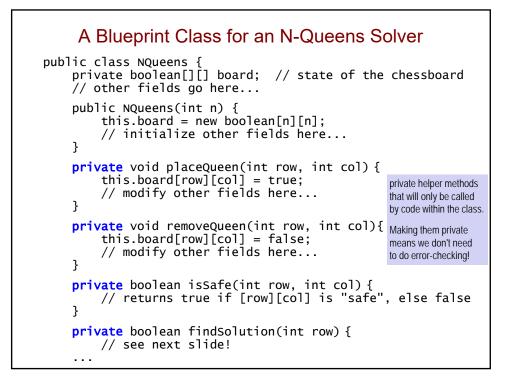


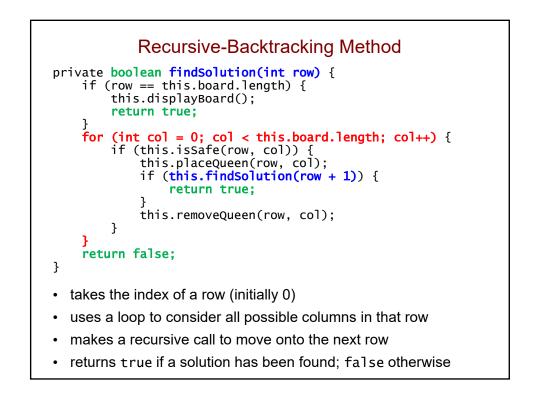


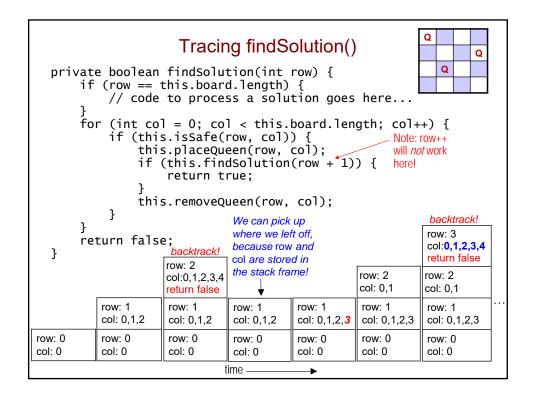


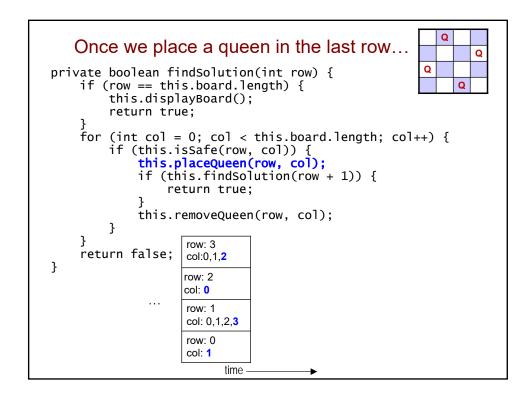


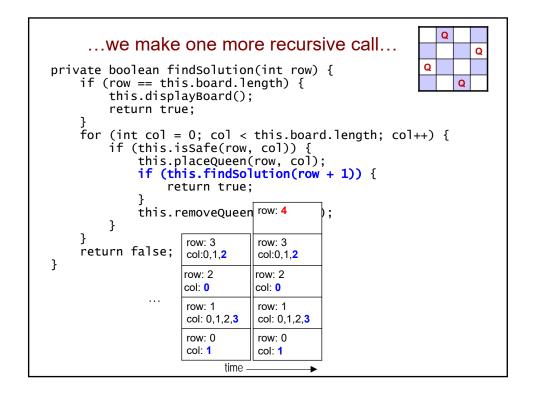


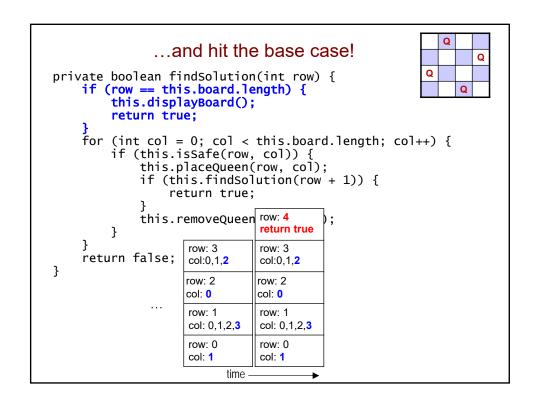


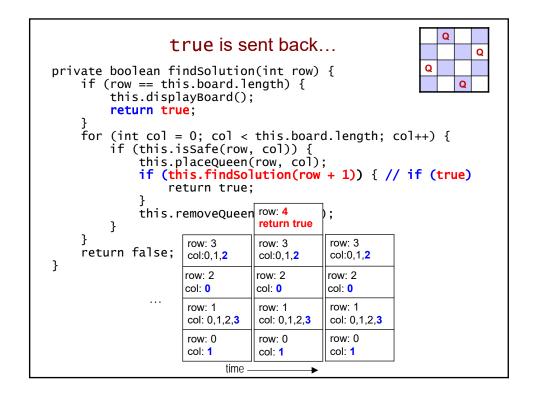


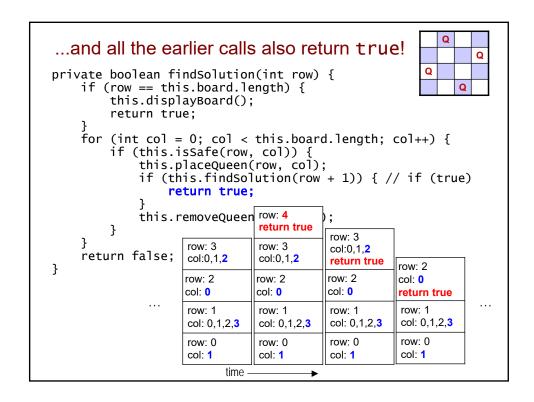


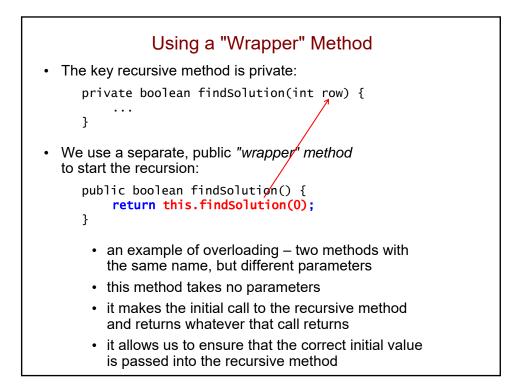


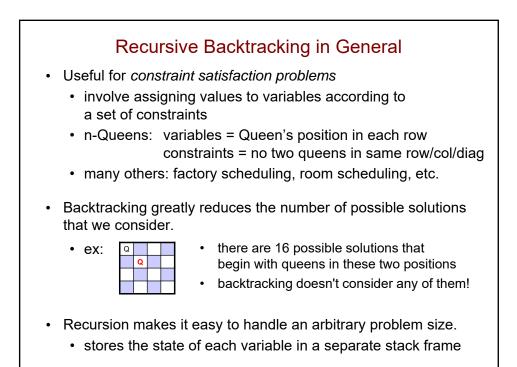


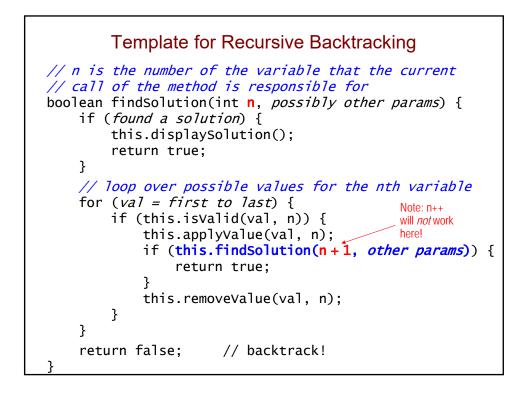


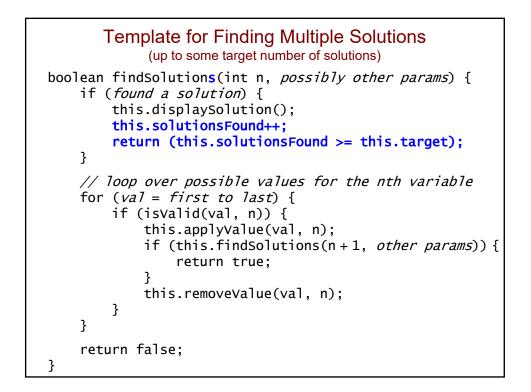


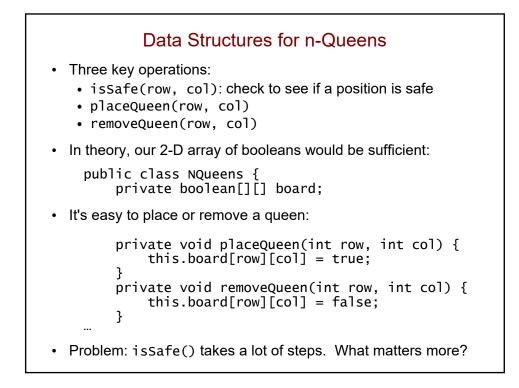


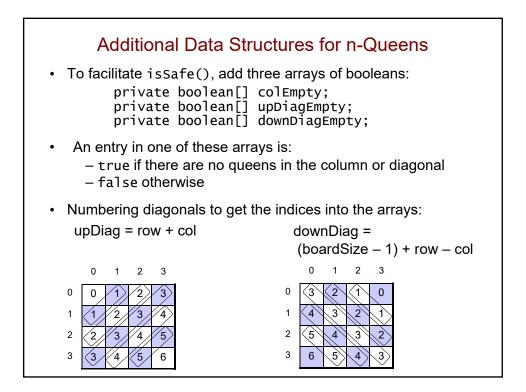


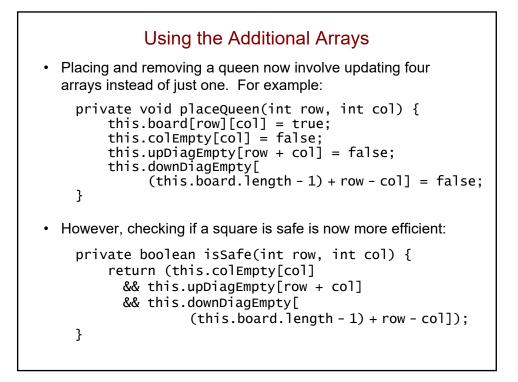


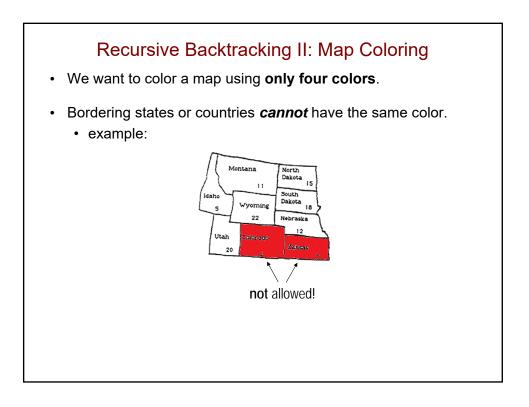


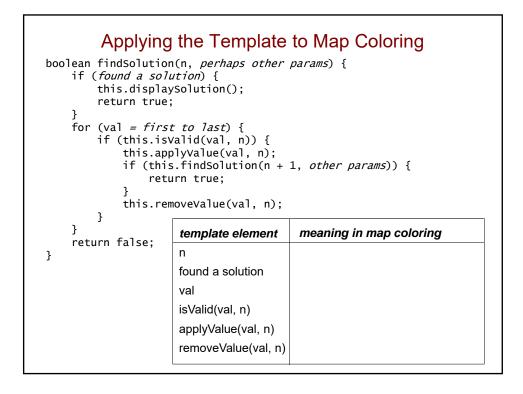


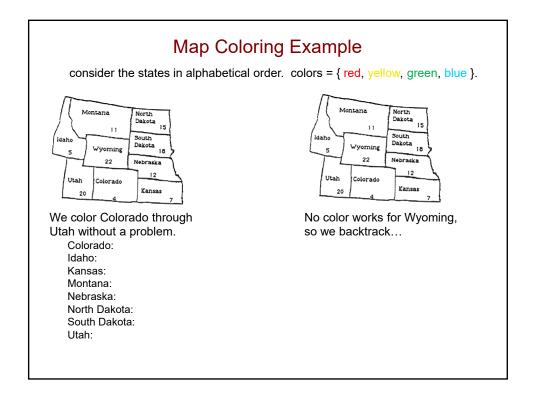


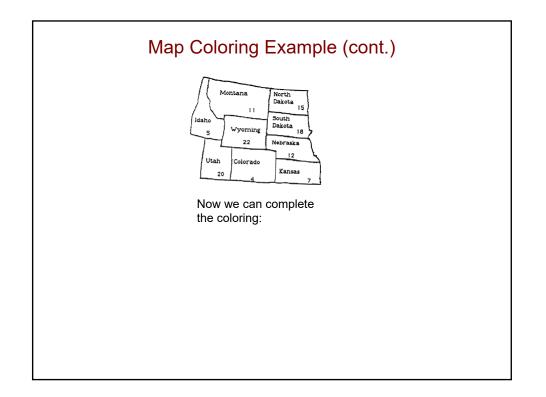


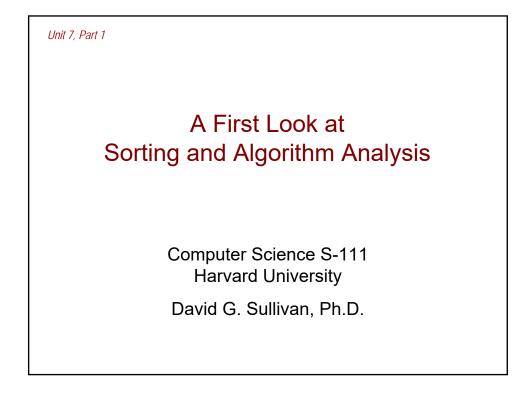


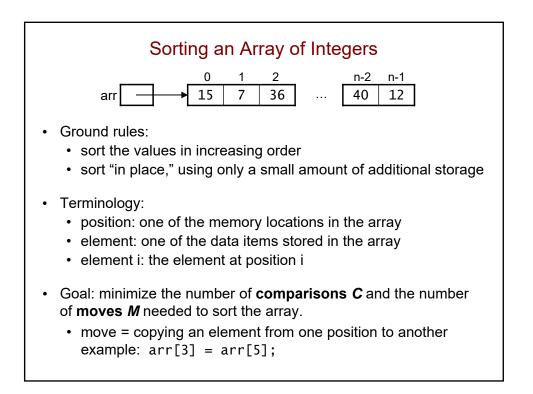








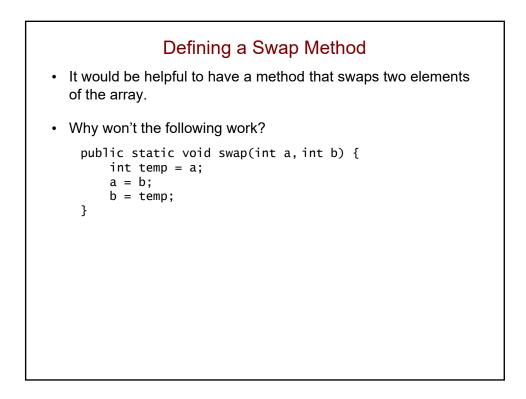


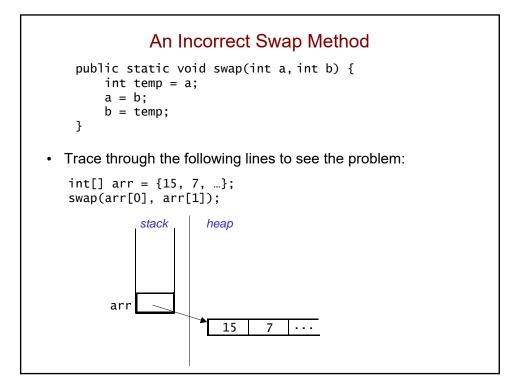


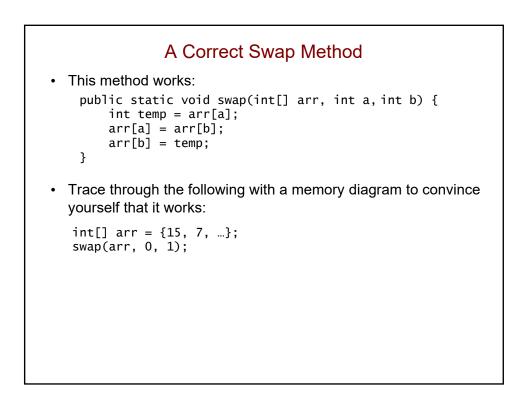
## Defining a Class for our Sort Methods

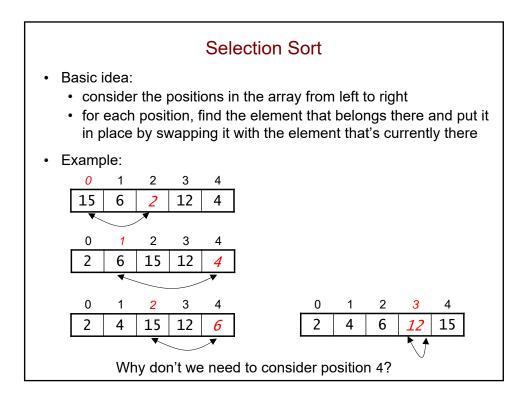
```
public class Sort {
    public static void bubbleSort(int[] arr) {
        ...
    }
    public static void insertionSort(int[] arr) {
        ...
    }
    ...
}
```

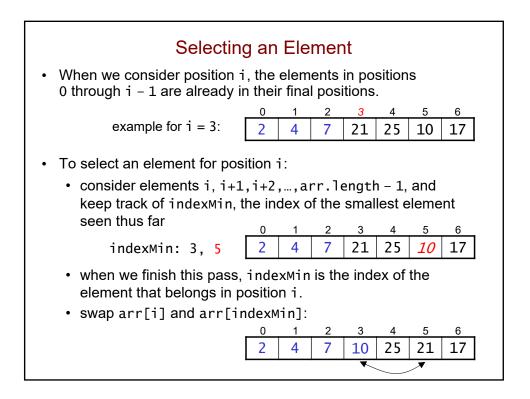
- Our Sort class is simply a collection of methods like Java's built-in Math class.
- Because we never create Sort objects, all of the methods in the class must be *static*.
  - outside the class, we invoke them using the class name:
     e.g., Sort.bubbleSort(arr)

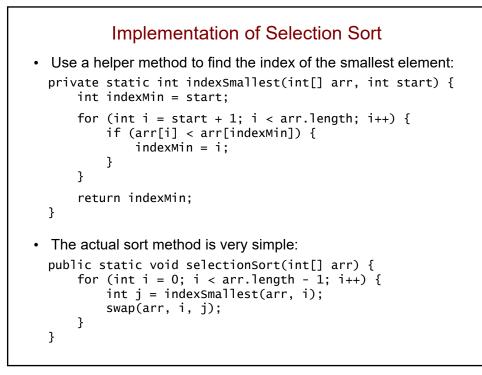


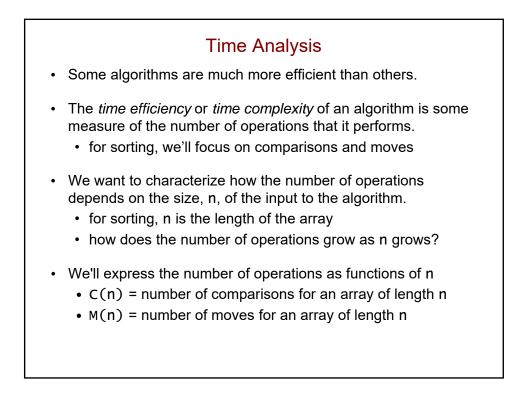


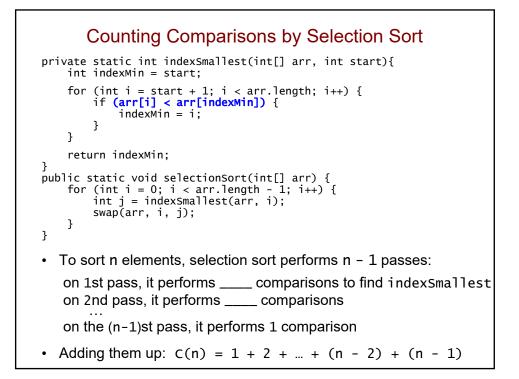


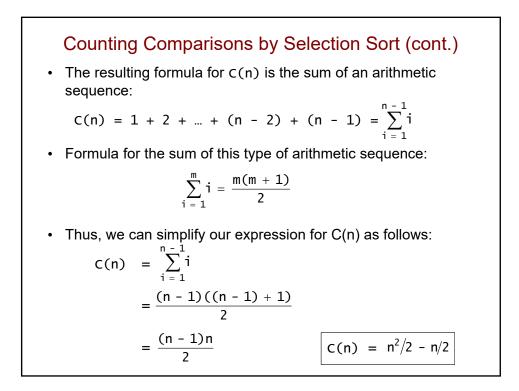






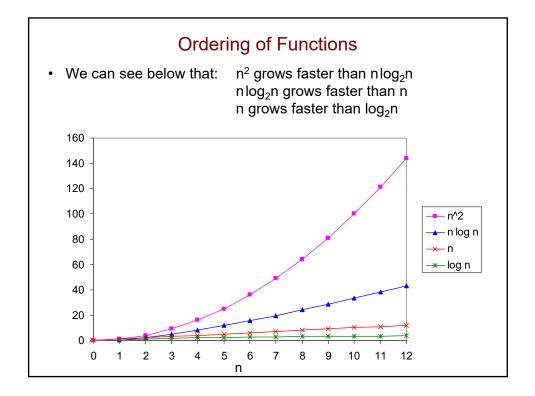


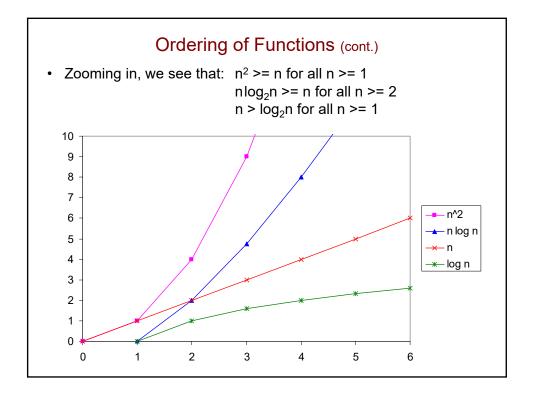


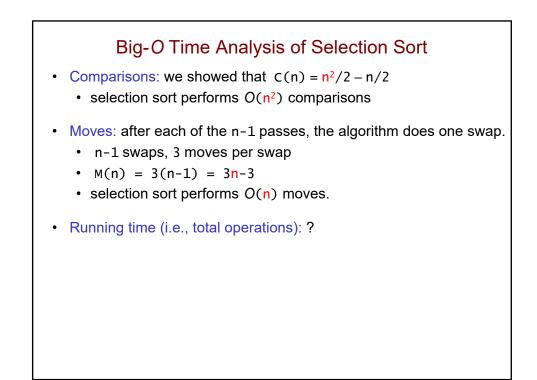


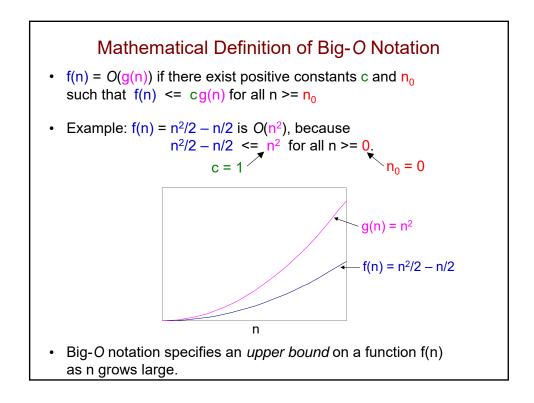
<ul> <li>Focusing on the Largest Term</li> <li>When n is large, mathematical expressions of n are dominated by their "largest" term — i.e., the term that grows fastest as a function of n.</li> </ul>				
• example: <u>n</u> 10 100 1000	n <sup>2</sup> /2 50 5000 00 50,000,000	n/2 5 50 5000	<u>n²/2 – n/2</u> 45 4950 49,995,000	
<ul> <li>In characterizing the time complexity of an algorithm, we'll focus on the largest term in its operation-count expression.</li> <li>for selection sort, C(n) = n²/2 - n/2 ≈ n²/2</li> <li>In addition, we'll typically ignore the coefficient of the largest term (e.g., n²/2 → n²).</li> </ul>				

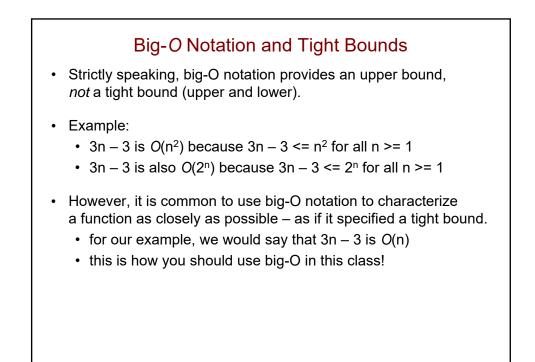
<ul> <li>Big-O Notation</li> <li>We specify the largest term using big-O notation.</li> <li>e.g., we say that C(n) = n²/2 - n/2 is O(n²)</li> </ul>				
Common classes of <u>name</u> constant time logarithmic time linear time nlogn time quadratic time exponential time	example expressions 1, 7, 10 $3\log_{10}n$ , $\log_2n + 5$ $5n$ , $10n - 2\log_2n$ $4n\log_2n$ , $n\log_2n + n$ $2n^2 + 3n$ , $n^2 - 1$ $2^n$ , $5e^n + 2n^2$	$\frac{\text{big-O notation}}{O(1)}$ $O(\log n)$ $O(n)$ $O(n\log n)$ $O(n^2)$ $O(c^n)$		
<ul> <li>For large inputs, efficiency matters more than CPU speed.</li> <li>e.g., an O(log n) algorithm on a slow machine will outperform an O(n) algorithm on a fast machine</li> </ul>				



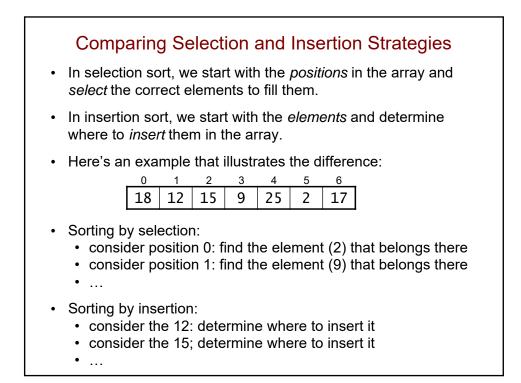


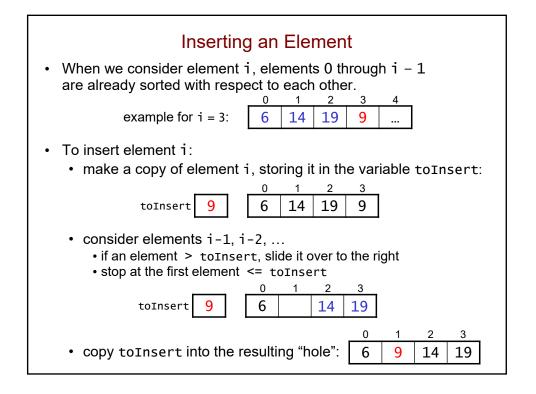




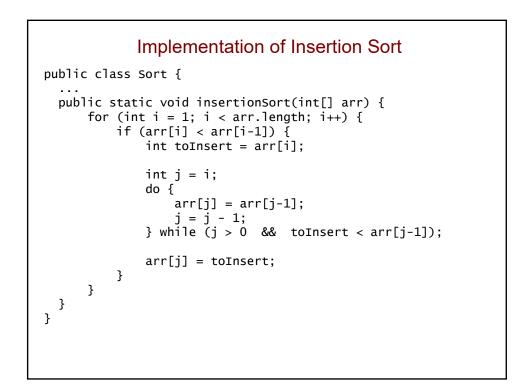


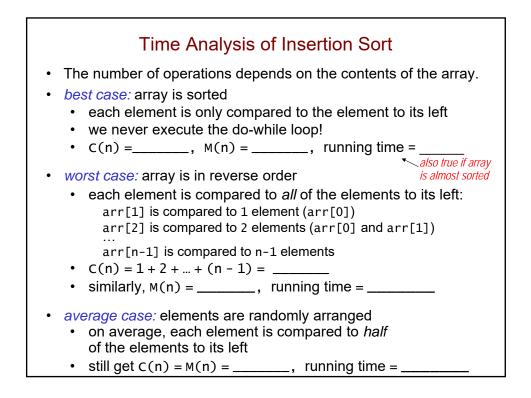
Insertion Sort							
<ul> <li>Basic idea:</li> <li>going from left to right, "insert" each element into its proper place with respect to the elements to its left</li> <li>"slide over" other elements to make room</li> </ul>							
• Example:	0 1 2 3 4						
	<b>*</b> 15 <b>4</b> 2 12 6						
	<b>4</b> 15 <b>2</b> 12 6						
	2 4 15 12 6						
	2 4 12 15 6						
	2 4 6 12 15						



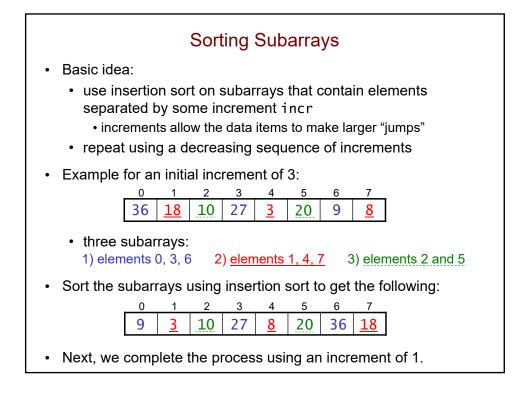


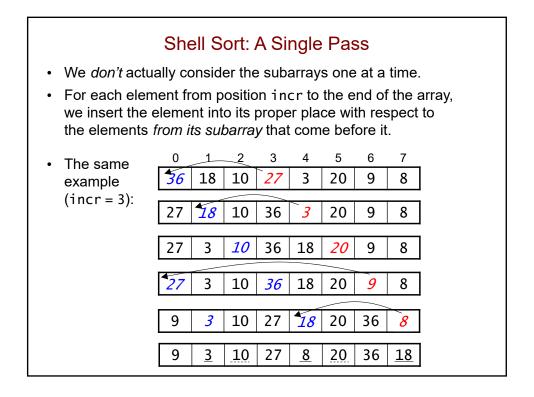
Insertion Sort Example (done together)							
description of steps	12 5 2 13 18 4						

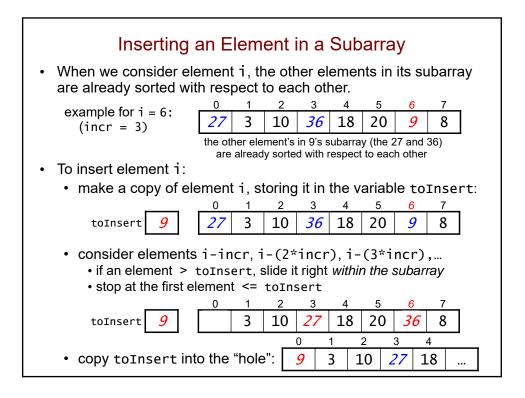


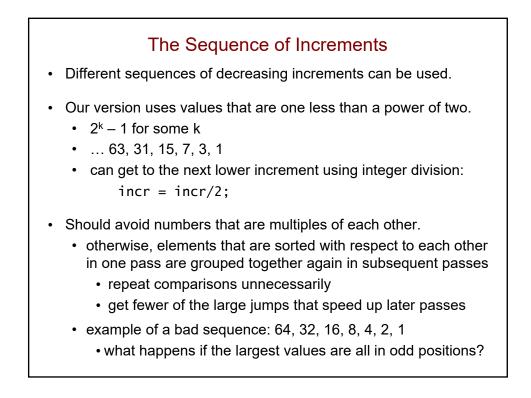


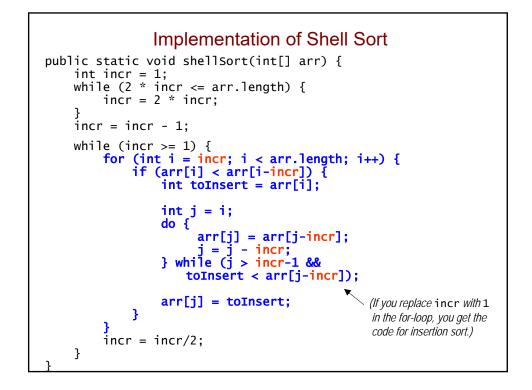
Shell Sort							
Developed by Donald Shell							
<ul> <li>Improves on insertion sort</li> <li>takes advantage of the fact that it's fast for almost-sorted arrays</li> <li>eliminates a key disadvantage: an element may need to move many times to get to where it belongs.</li> </ul>							
<ul> <li>Example: if the largest element starts out at the beginning of the array, it moves one place to the right on <i>every</i> insertion!</li> <li>0</li> <li>1</li> <li>2</li> <li>3</li> <li>4</li> <li>5</li> <li></li> <li>1000</li> </ul>							
999 42 56 30 18 23 11							
<ul> <li>Shell sort uses larger moves that allow elements to quickly get close to where they belong in the sorted array.</li> </ul>							



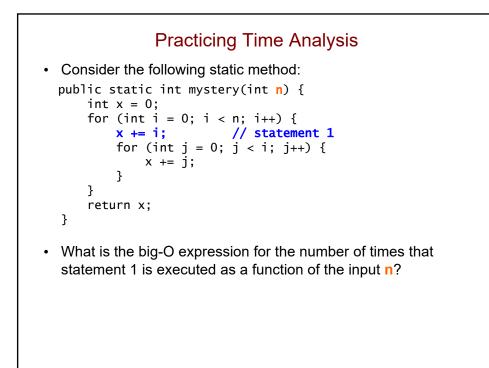




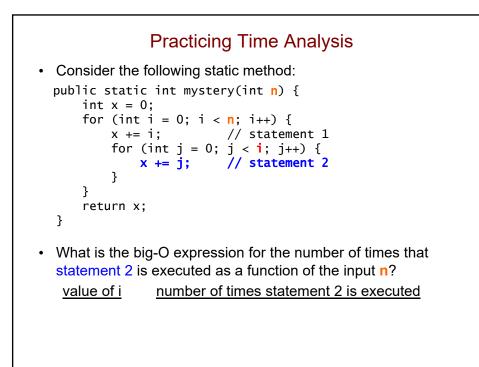




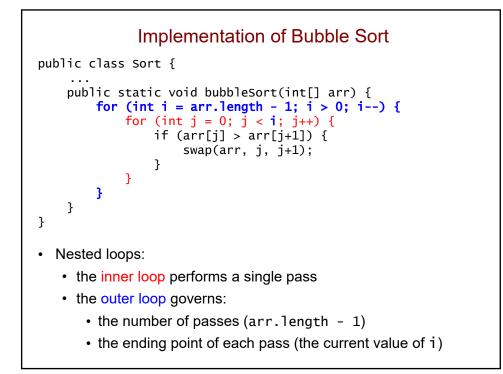
Time Analysis of Shell Sort							
Difficult to analyze precisely							
<ul> <li>typically ι</li> </ul>	use experiments to	measure its eff	ficiency				
<ul> <li>With a bad ir</li> </ul>	nterval sequence, i	it's O(n²) in the	worst case.				
<ul> <li>With a good interval sequence, it's better than O(n<sup>2</sup>).</li> <li>at least O(n<sup>1.5</sup>) in the average and worst case</li> <li>some experiments have shown average-case running times of O(n<sup>1.25</sup>) or even O(n<sup>7/6</sup>)</li> </ul>							
n	better than insertion n <sup>2</sup>	n <sup>1.5</sup>	n <sup>1.25</sup>				
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$							
<ul> <li>We've wrapped insertion sort in another loop and increased its efficiency! The key is in the larger jumps that Shell sort allows.</li> </ul>							

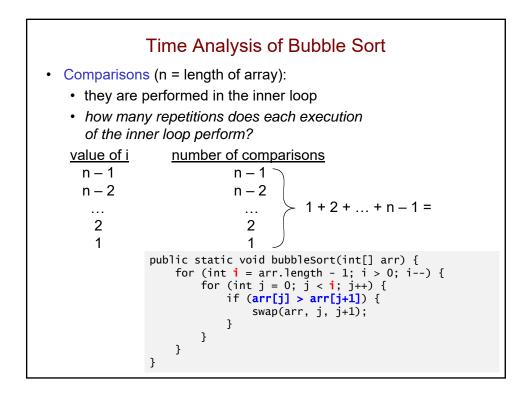


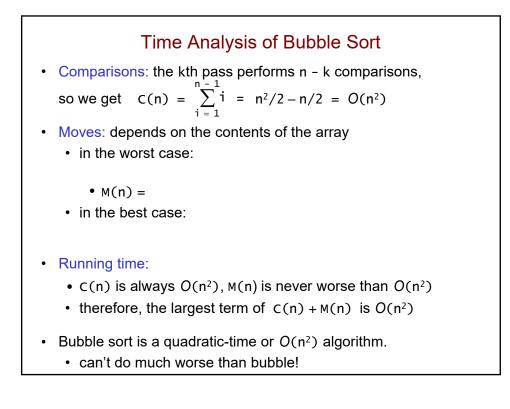
What about now?
Consider the following static method:
<pre>public static int mystery(int n) {</pre>
int $x = 0;$
<pre>for (int i = 0; i &lt; 3*n + 4; i++) {     x += i;</pre>
for (int j = 0; j < i; j++) {
x += j;
}
return x;
}
<ul> <li>What is the big-O expression for the number of times that statement 1 is executed as a function of the input n?</li> </ul>



<ul> <li>Bubble Sort</li> <li>Perform a sequence of passes from left to right</li> <li>each pass swaps adjacent elements if they are out of order</li> </ul>						rder
larger elements "bubble u	p" to tl	ne eno	d of th	e arra	У	
we don't need to consider	<ul> <li>At the end of the kth pass:</li> <li>the k rightmost elements are in their final positions</li> <li>we don't need to consider them in subsequent passes.</li> </ul>					
• Example.	• Example:     0     1     2     3     4       28     24     37     15     5					
after the first pass:	after the first pass: 24 28 15 5 <i>37</i>					
after the second:	after the second: 24 15 5 28 37					
after the third:	after the third: 15 5 24 28 37					
after the fourth:	5	15	24	28	37	





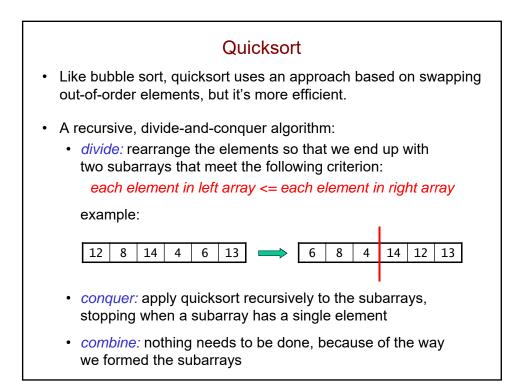


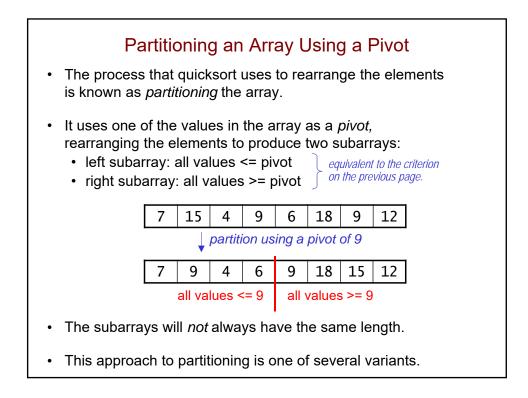


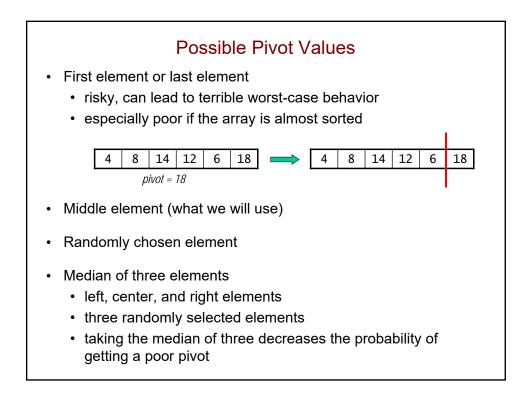
## Sorting II: Divide-and-Conquer Algorithms, Distributive Sorting

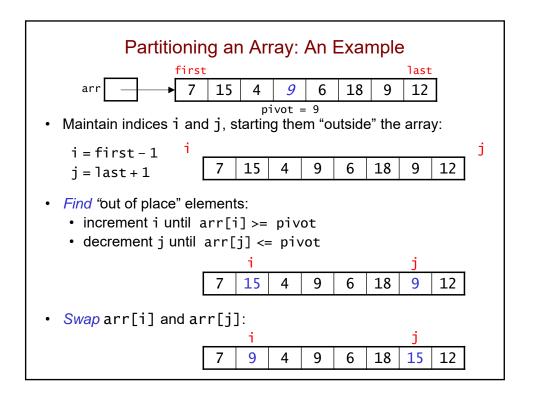
Computer Science S-111 Harvard University

David G. Sullivan, Ph.D.

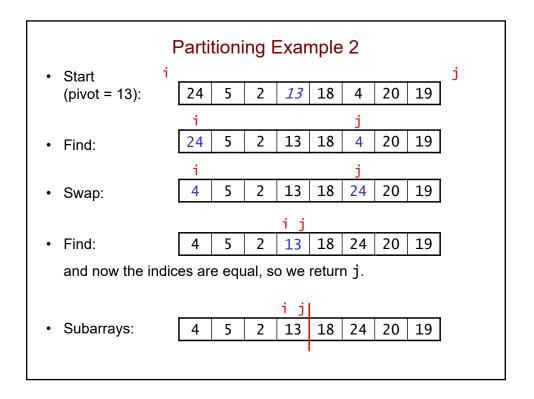


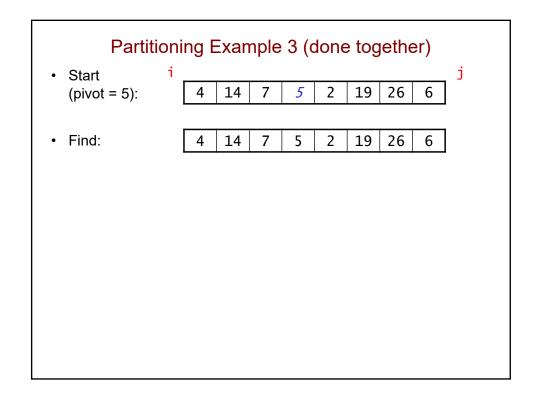


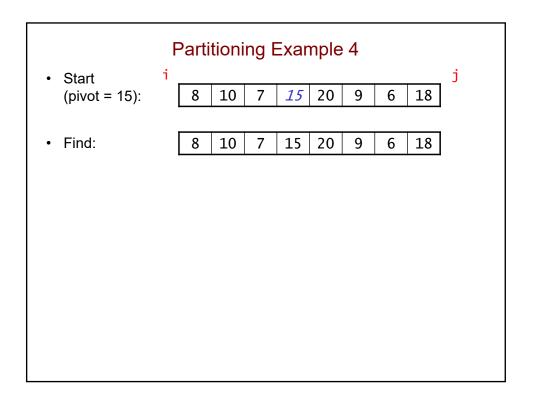


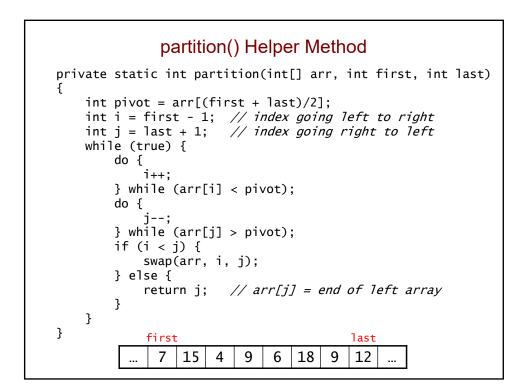


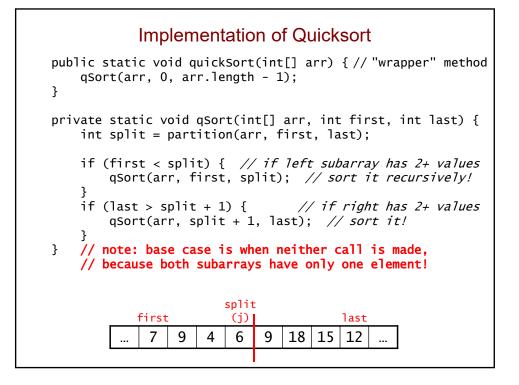
Partitioning Example (cont.)								
		i					j	
from prev. page:	7	9	4	9	6	18	15	12
				i	j			
• Find:	7	9	4	9	6	18	15	12
				i	j			
• Swap:	7	9	4	6	9	18	15	12
				j	i			
• Find:	7	9	4	6	9	18	15	12
and now the indices have crossed, so we return j.								
<ul> <li>Subarrays: left = from first to j, right = from j+1 to last</li> </ul>								
first j i last								
	7	9	4	6	9	18	15	12

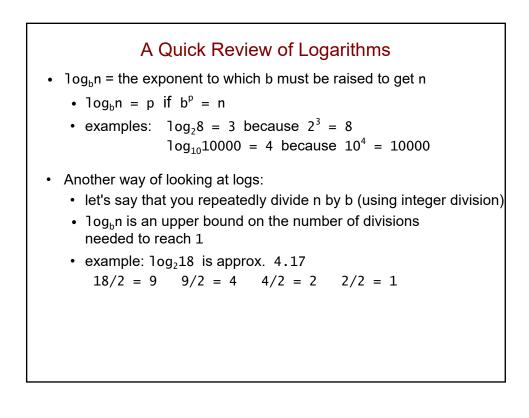




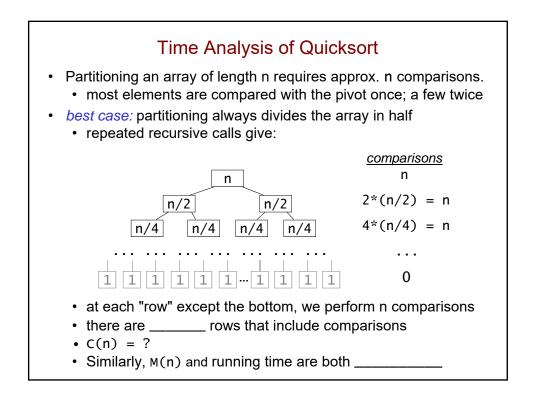


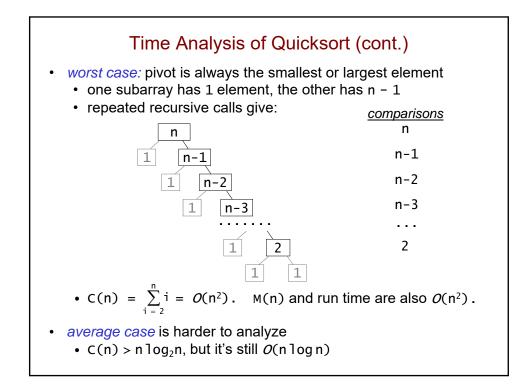


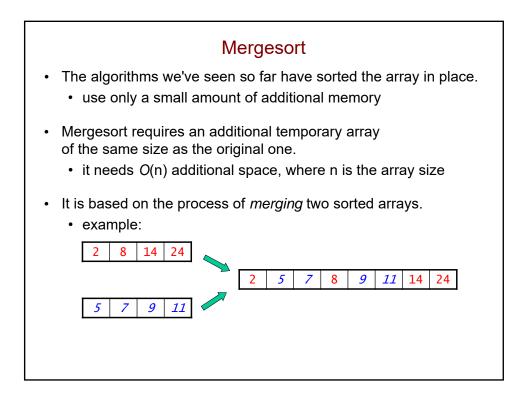


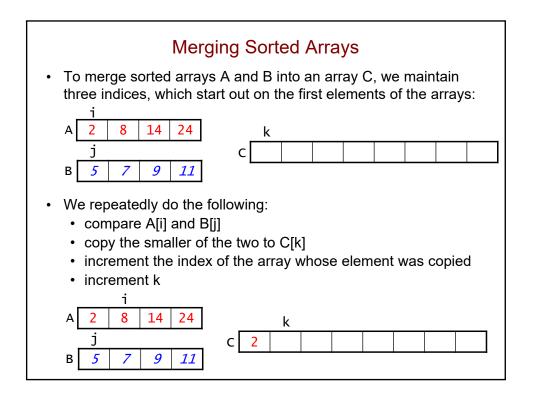


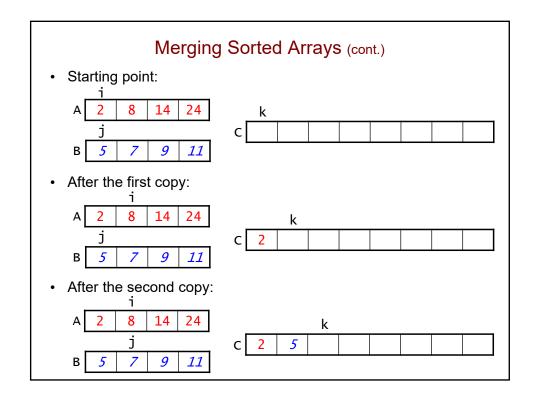
	A Quick Review of a) algorithm – one in which rtional to log <sub>b</sub> n for any bas	the number of	,				
• log <sub>b</sub> n g	prows much more slowly that	an n					
	n log <sub>2</sub> n						
	2	1					
	1024 (1K)	10					
	1024*1024 (1M)						
	1024*1024*1024 (1G)	30					
• a O(	r large values of n: log n) algorithm is much fa log n << n		-				
	n log n) algorithm is much n * log n << n * n n log n << n <sup>2</sup>	it's also faster	O(n <sup>2</sup> ) algorithm than a O(n <sup>1.5</sup> ) ike Shell sort				

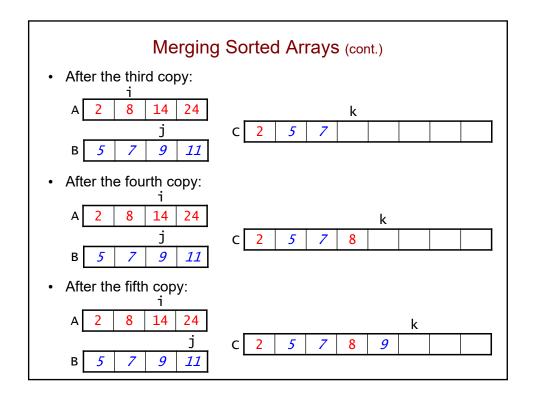


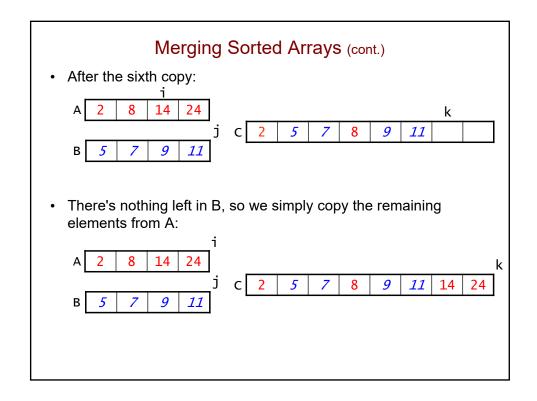




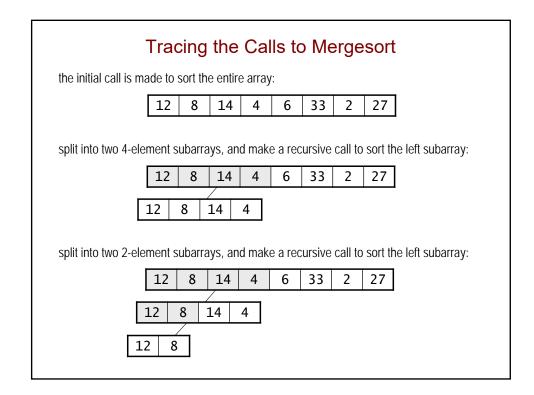


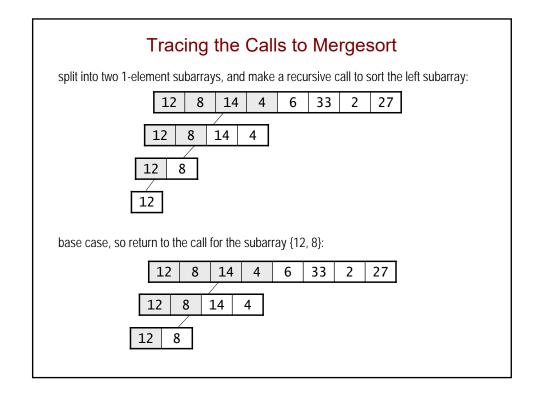


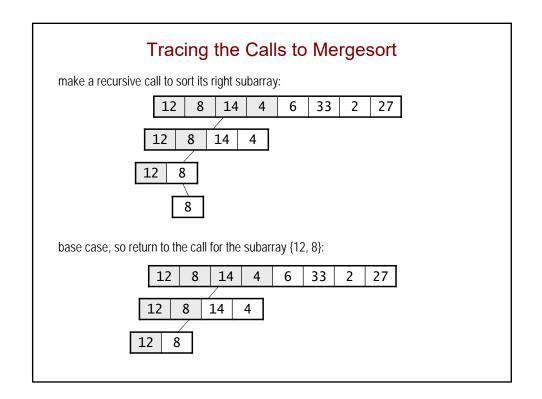


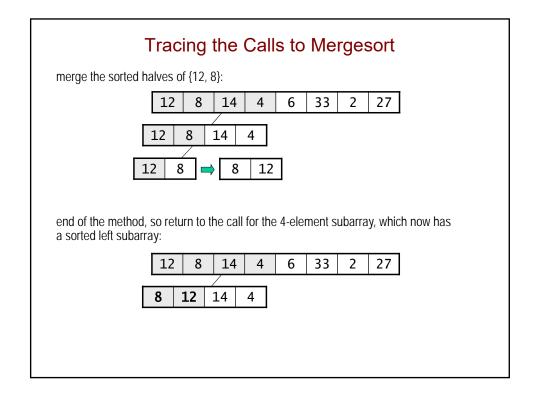


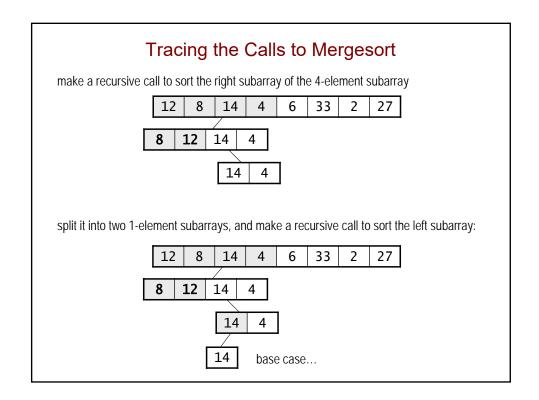
	Divide and Conquer								
-	<ul> <li>Like quicksort, mergesort is a divide-and-conquer algorithm.</li> <li><i>divide:</i> split the array in half, forming two subarrays</li> </ul>								
• comb	ine: merge the sorted subarrays								
	12 8 14 4 6 33 2 27								
split	12 8 14 4 6 33 2 27								
split	12 8 14 4 6 33 2 27								
split	12 8 14 4 6 33 2 27								
merge	merge 8 12 4 14 6 33 2 27								
merge	4 8 12 14 2 6 27 33								
merge	2 4 6 8 12 14 27 33								

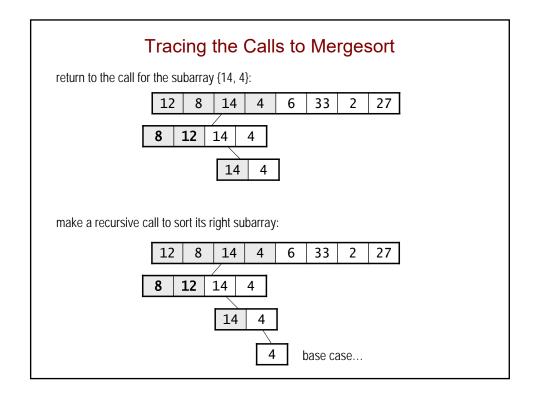


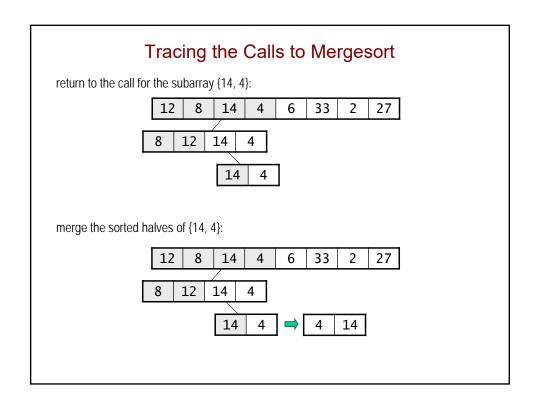


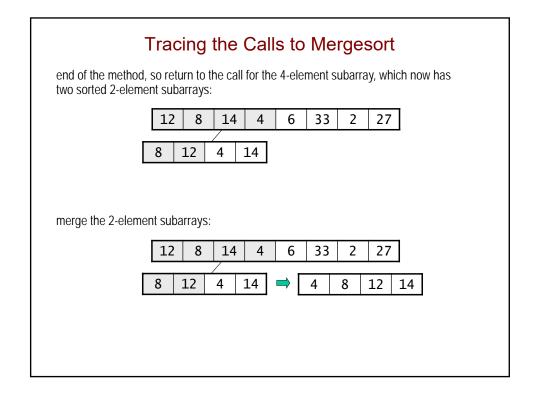


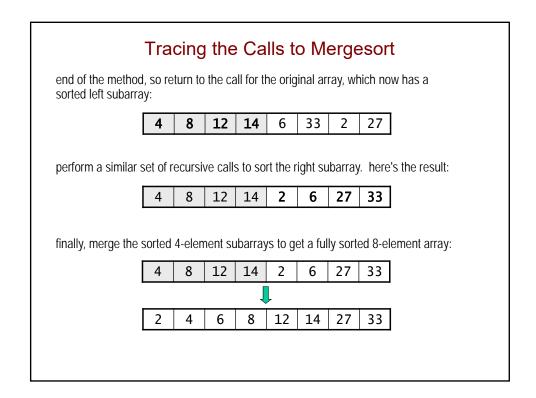


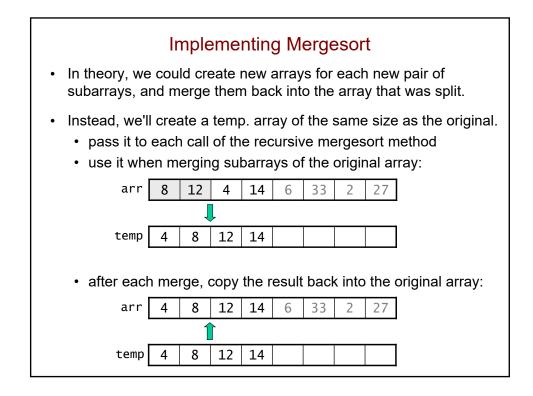




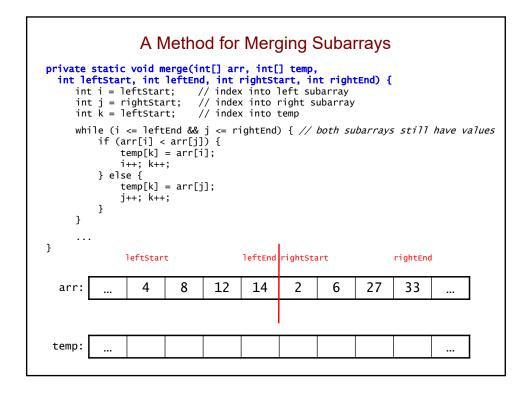




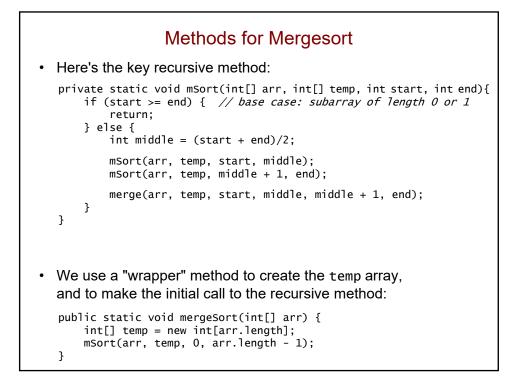


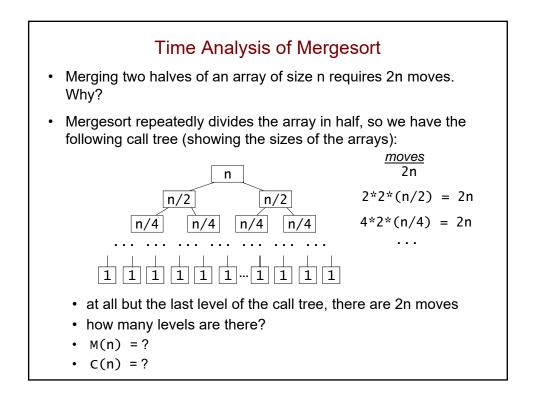


A Method for Merging Subarrays					
	<pre>ate static void merge(int[] arr, int[] temp, it leftStart, int leftEnd, int rightStart, int rightEnd) { int i = leftStart; // index into left subarray int j = rightStart; // index into right subarray int k = leftStart; // index into temp</pre>				
	<pre>while (i &lt;= leftEnd &amp;&amp; j &lt;= rightEnd) {     if (arr[i] &lt; arr[j]) {         temp[k] = arr[i];         i++; k++;     } else {         temp[k] = arr[j];         j++; k++;     } }</pre>				
	<pre>while (i &lt;= leftEnd) {     temp[k] = arr[i];     i++; k++; } while (j &lt;= rightEnd) {     temp[k] = arr[j];     j++; k++; }</pre>				
}	<pre>for (i = leftStart; i &lt;= rightEnd; i++) {     arr[i] = temp[i]; }</pre>				



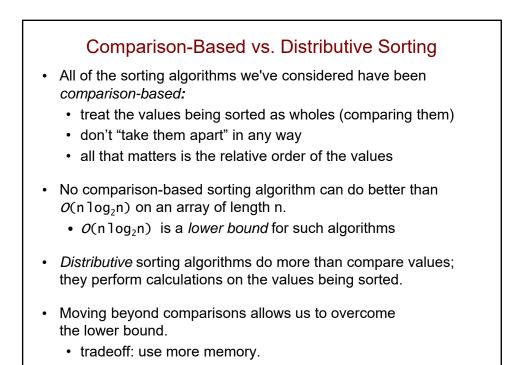
Methods for Mergesort									
Here's the key recursive method:									
<pre>private static void mSort(int[] arr, int[] temp, int start, int end){     if (start &gt;= end) { // base case: subarray of length 0 or 1         return;     } else {         int middle = (start + end)/2;     } }</pre>									
mSort(arr, temp, start, middle); mSort(arr, temp, middle + 1, end);									
<pre>merge(arr, temp, start, middle, middle + 1, end); }</pre>									
start end									
arr: <u></u> 12 8 14 4 6 33 2 27									
temp:									

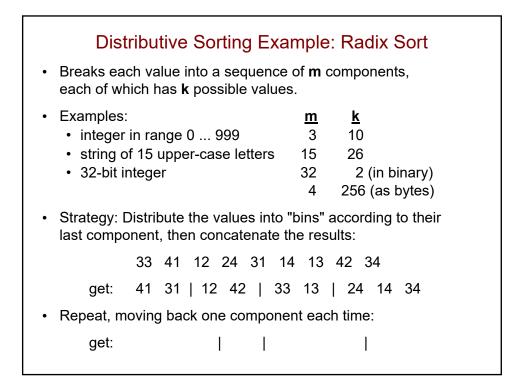




Summary: Sorting Algorithms									
algorithm best case avg case worst case extra memory									
selection sort	O(n <sup>2</sup> )	O(n <sup>2</sup> )	O(n <sup>2</sup> )	0(1)					
insertion sort	0(n)	O(n <sup>2</sup> )	O(n <sup>2</sup> )	0(1)					
Shell sort	O(n log n)	O(n <sup>1.5</sup> )	O(n <sup>1.5</sup> )	0(1)					
bubble sort	O(n <sup>2</sup> )	O(n <sup>2</sup> )	O(n <sup>2</sup> )	0(1)					
quicksort	O(n log n)	O(n log n)	O(n <sup>2</sup> )	best/avg: O(log n) worst: O(n)					
mergesort	O(n log n)	O(n log n)	O(nlogn)	O(n)					

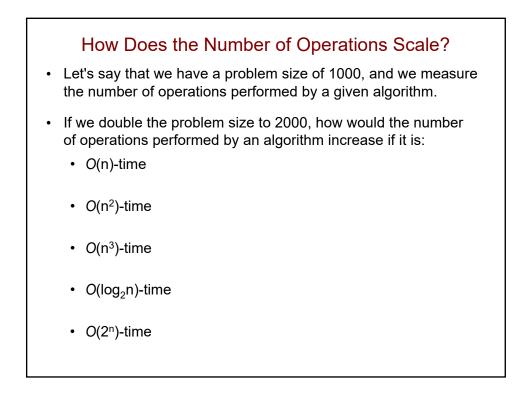
- · Insertion sort is best for nearly sorted arrays.
- Mergesort has the best worst-case complexity, but requires O(n) extra memory – and moves to and from the temp. array.
- Quicksort is comparable to mergesort in the best/average case.
  - efficiency is also O(n log n), but less memory and fewer moves
  - its extra memory is from...
  - · with a reasonable pivot choice, its worst case is seldom seen

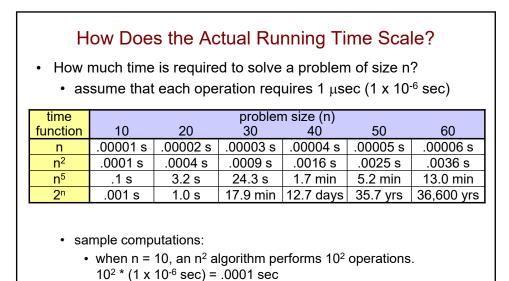




Analysis of Radix Sort
<ul> <li>m = number of components</li> <li>k = number of possible values for each component</li> <li>n = length of the array</li> </ul>
<ul> <li>Time efficiency: O(m*n)</li> <li>perform m distributions, each of which processes all n values</li> <li>O(m*n) &lt; O(nlogn) when m &lt; logn so we want m to be small</li> </ul>
<ul> <li>However, there is a tradeoff:</li> <li>as m decreases, k increases</li> <li>fewer components → more possible values per component</li> <li>as k increases, so does memory usage</li> <li>need more bins for the results of each distribution</li> <li>increased speed requires increased memory usage</li> </ul>

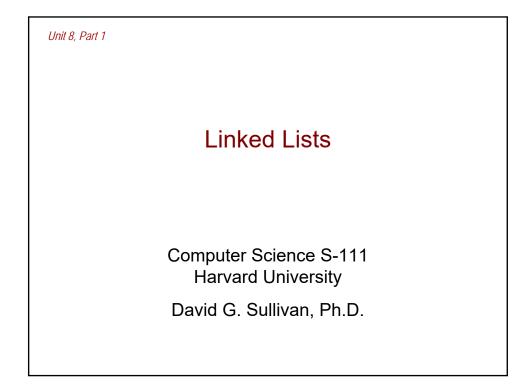
Big-	O Notation Revisite	d
	can group functions into o est-growing term in the ex s that they perform.	•
<b>3</b> • <b>3</b>	h that performs n²/2 – n/ adratic-time algorithm	2 operations is a
<ul> <li>name constant time logarithmic time linear time nlogn time quadratic time cubic time exponential time factorial time</li> </ul>	$\frac{\text{example expressions}}{1, 7, 10}$ $3\log_{10}n, \log_{2}n + 5$ $5n, 10n - 2\log_{2}n$ $4n\log_{2}n, n\log_{2}n + n$ $2n^{2} + 3n, n^{2} - 1$ $n^{2} + 3n^{3}, 5n^{3} - 5$ $2^{n}, 5e^{n} + 2n^{2}$ $3n!, 5n + n!$	$\frac{\text{big-O notation}}{O(1)}$ $O(1 \text{ og } n)$ $O(n)$ $O(n \log n)$ $O(n^2)$ $O(n^3)$ $O(c^n)$ $O(n!)$

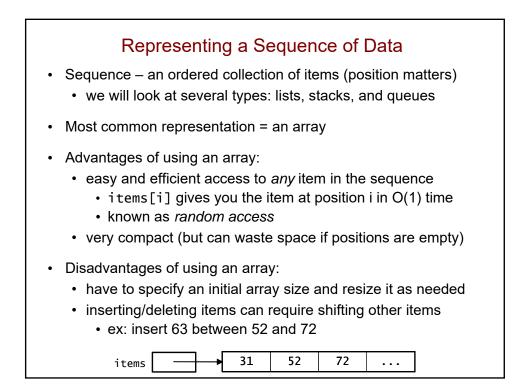


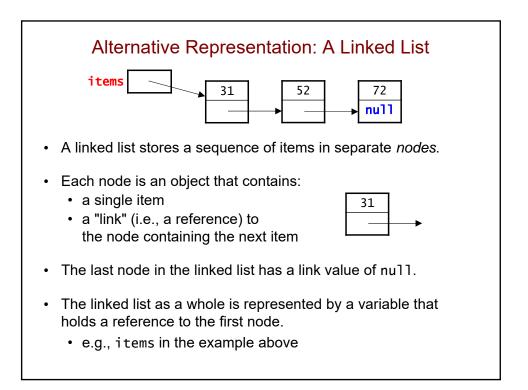


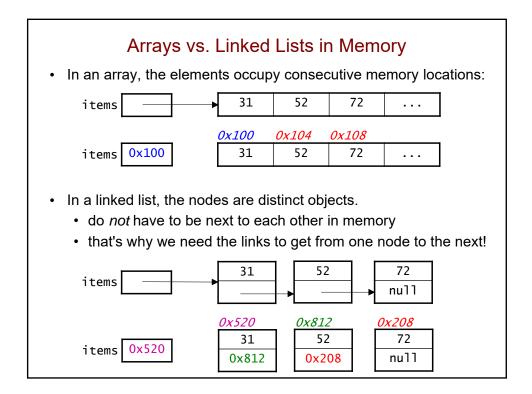
• when n = 30, a  $2^n$  algorithm performs  $2^{30}$  operations.  $2^{30} * (1 \times 10^{-6} \text{ sec}) = 1073 \text{ sec} = 17.9 \text{ min}$ 

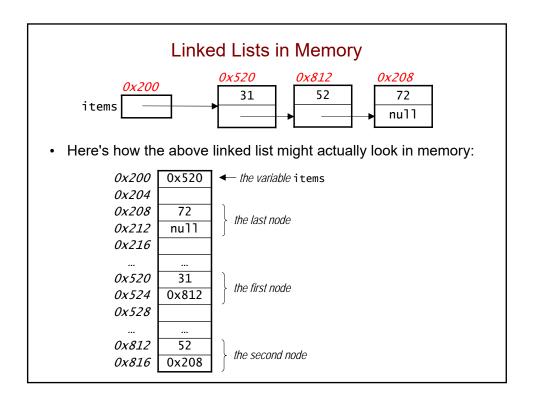
	Suicia		m eize n the	it can be solv	und in
give	n time	T? (again a			
	me		•	ilable (T)	,
	iction	1 min	1 hour	1 week	1 year
	n	60,000,000	3.6 x 10 <sup>9</sup>	6.0 x 10 <sup>11</sup>	3.1 x 10 <sup>13</sup>
	n²	7745	60,000	777,688	5,615,692
	n <sup>5</sup>	35	81	227	500
	2 <sup>n</sup>	25	31	39	44
	1 hour that's • n <sup>2</sup>	promputations: r = $3600 \text{ sec}$ enough time for algorithm: r <sup>2</sup> = $2.0 \times 100$	·		
	1 hour that's • n <sup>2</sup>	r = 3600 sec enough time fe	·		

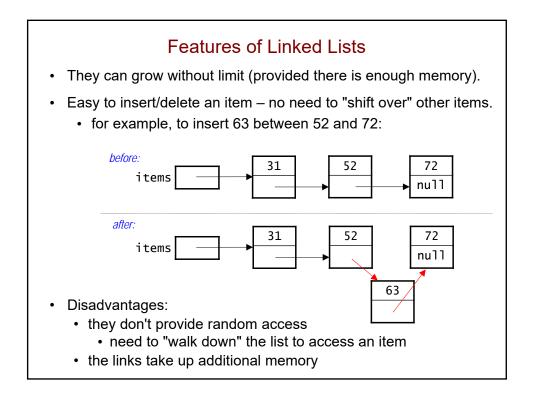


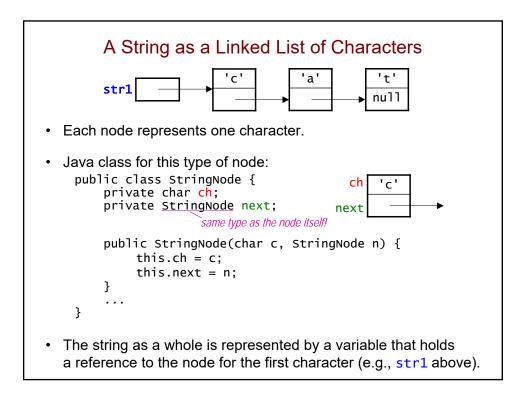


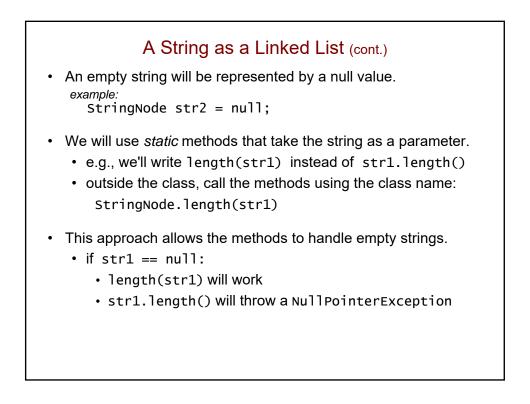


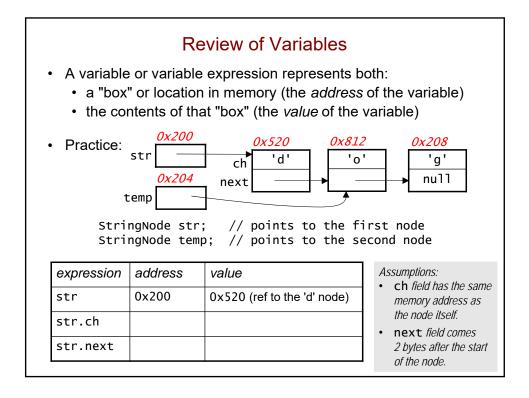


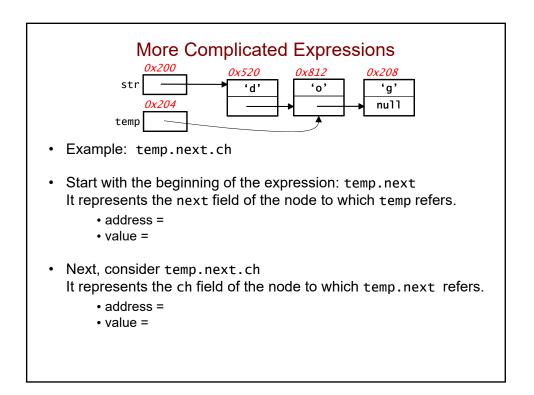


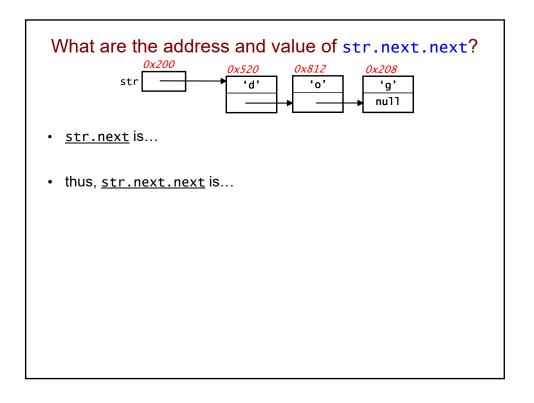


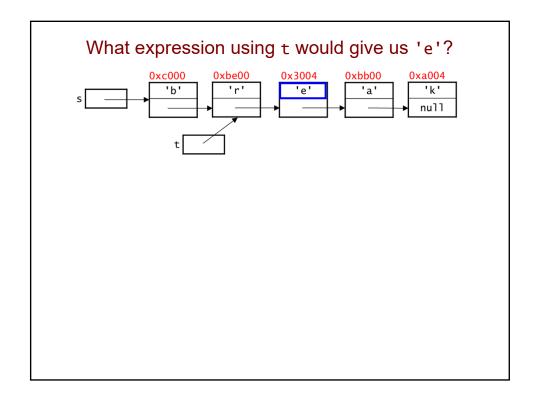


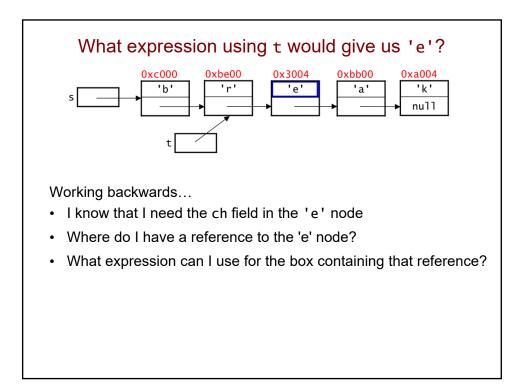


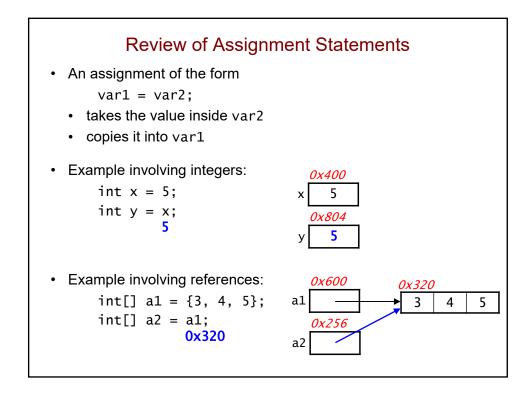


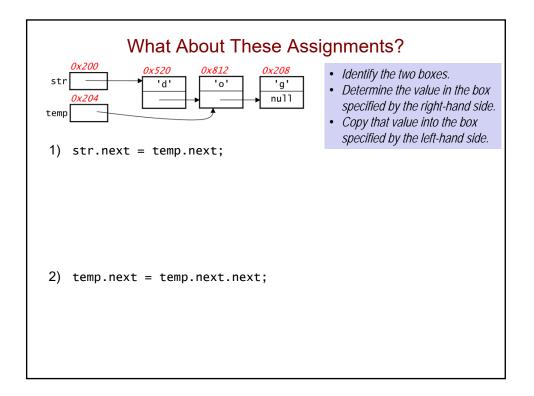


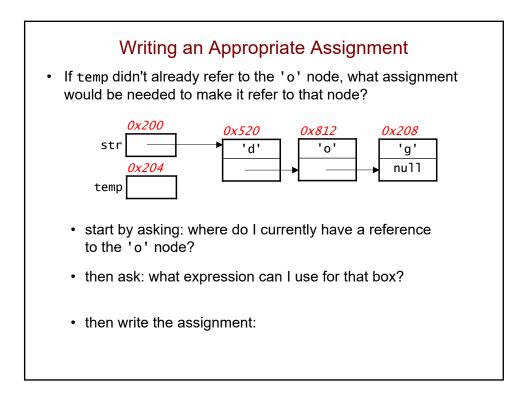


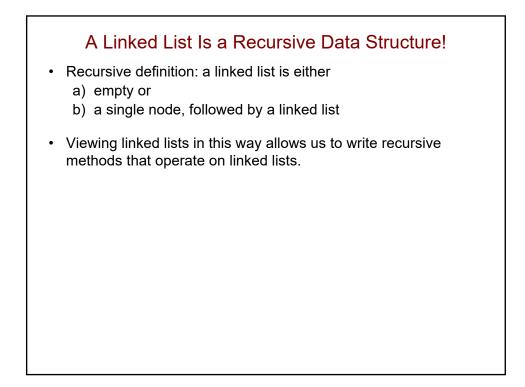


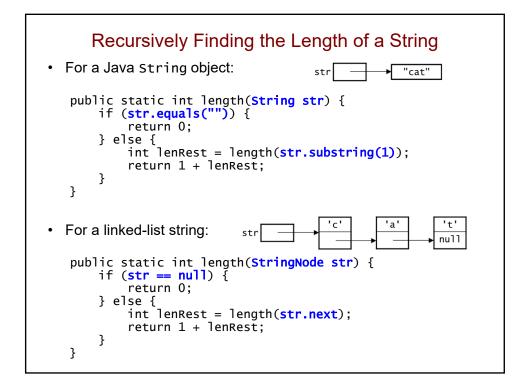


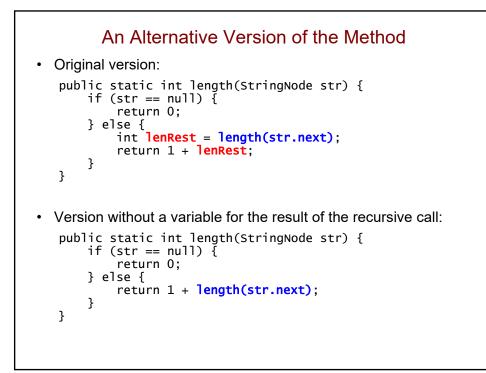


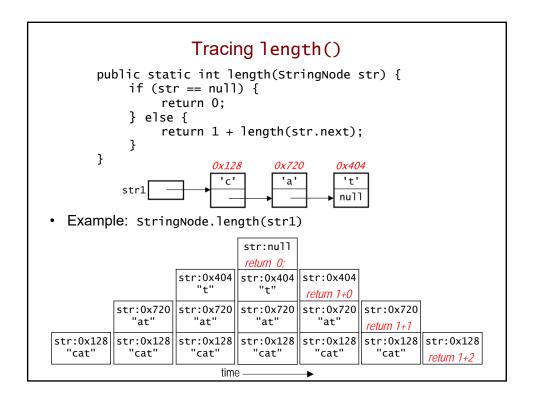


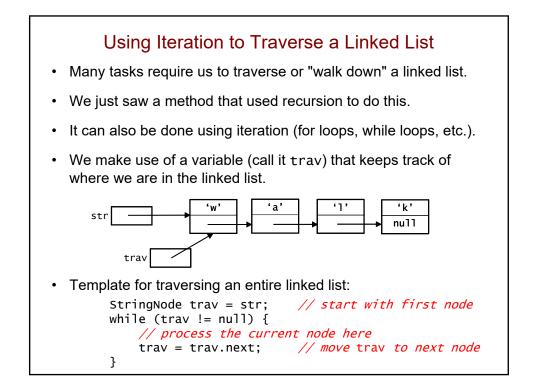


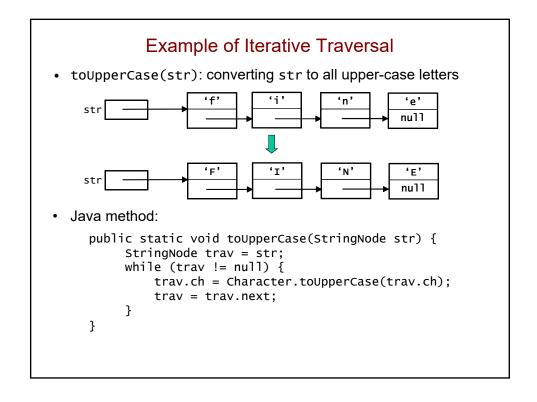


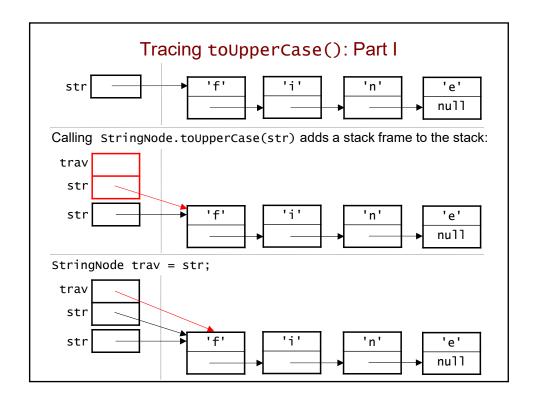


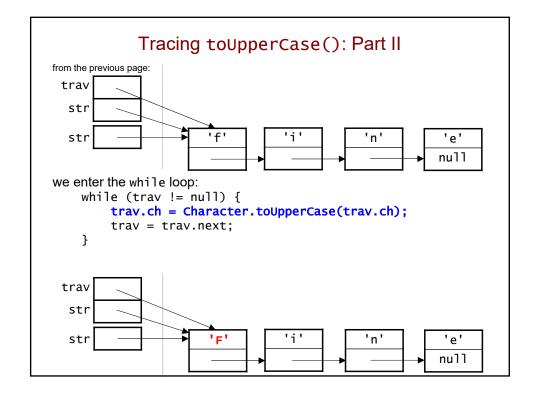


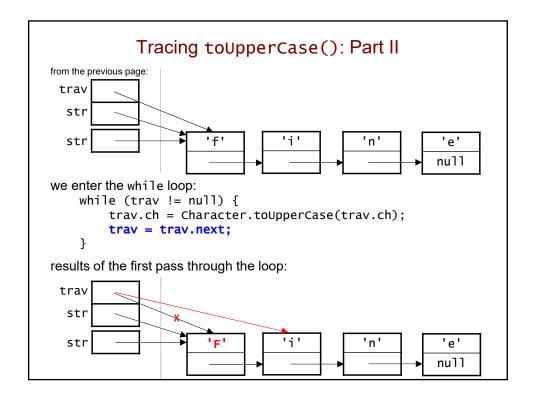


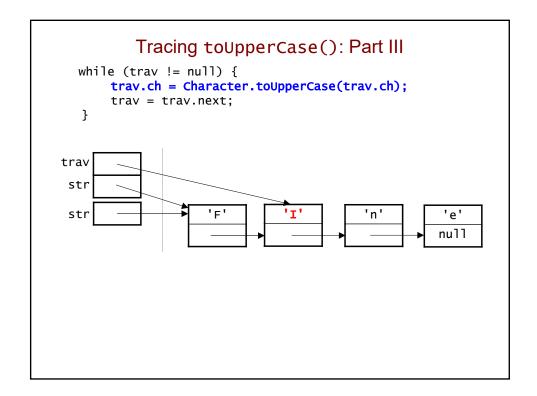


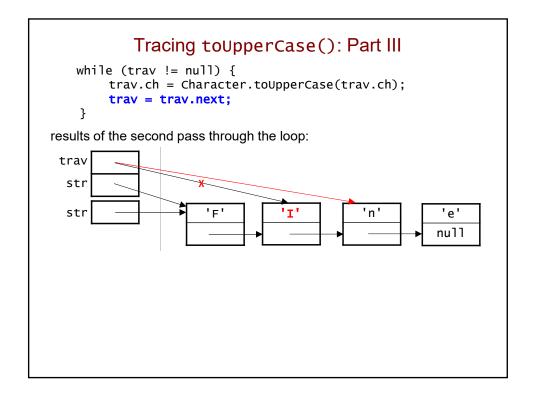


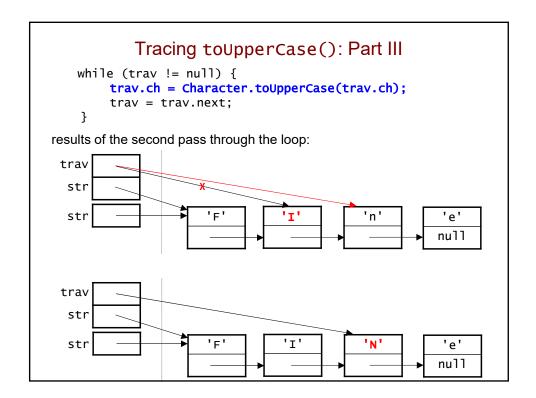


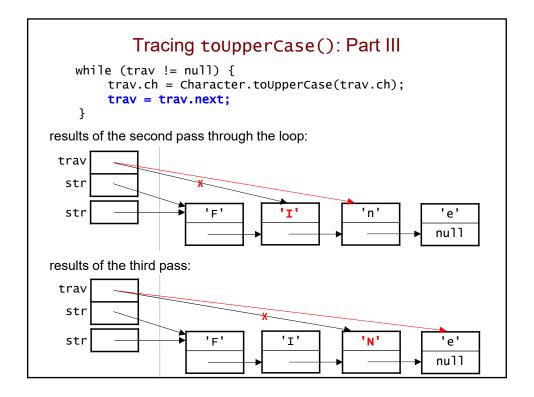


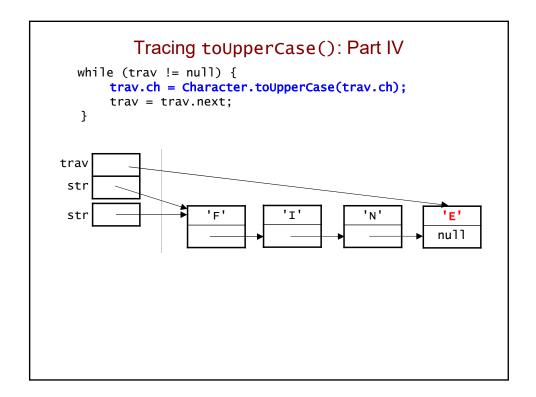


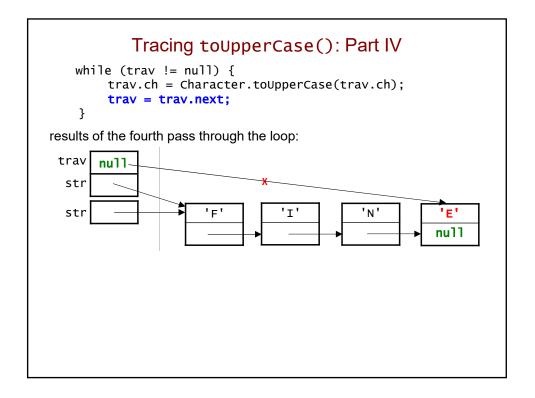


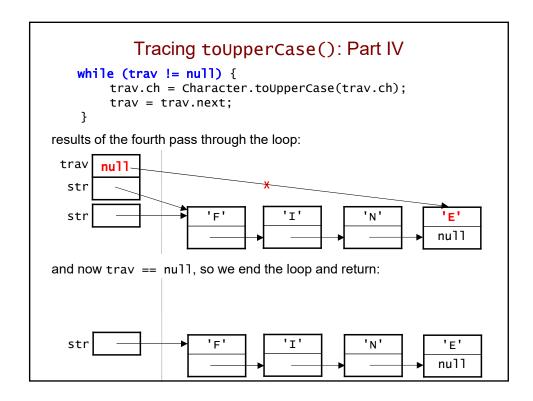


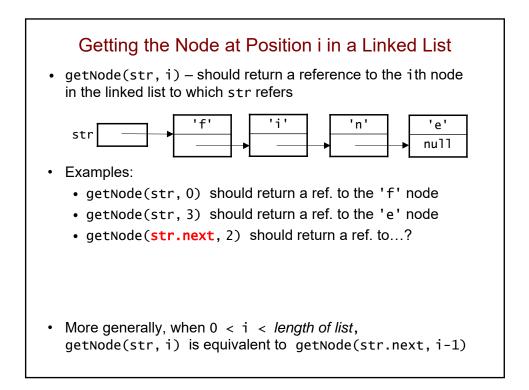


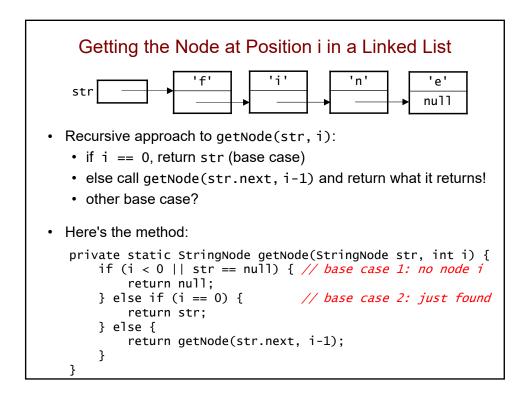


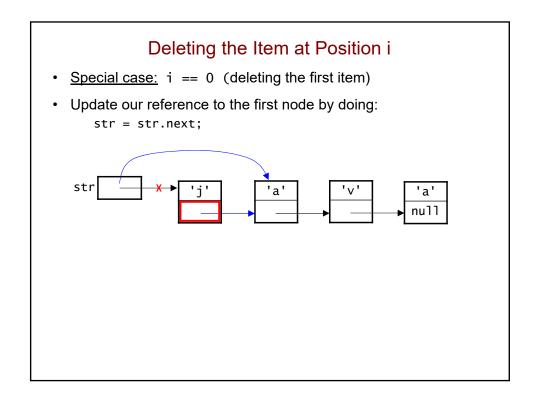


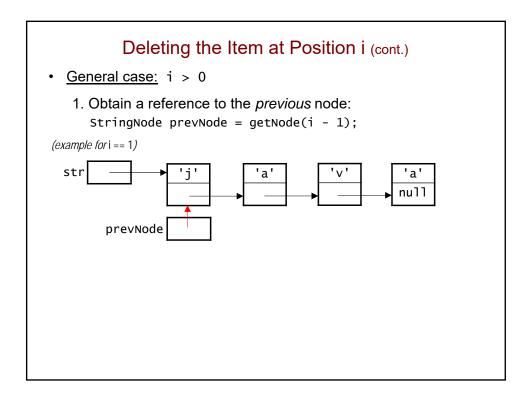


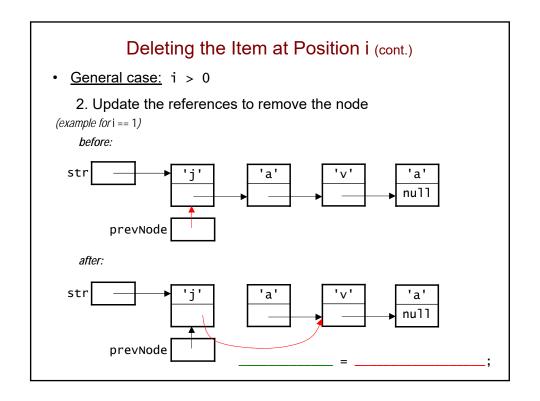


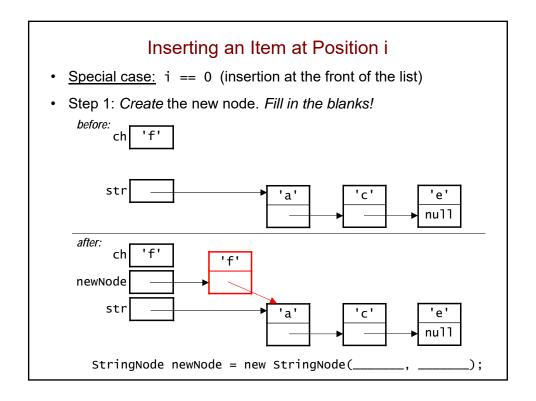


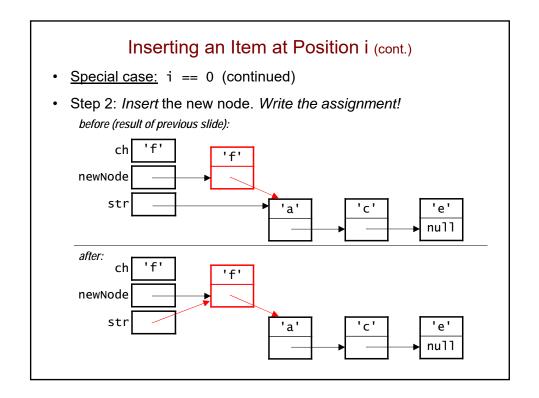


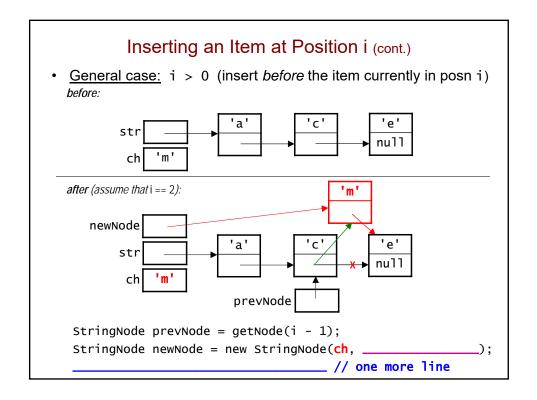


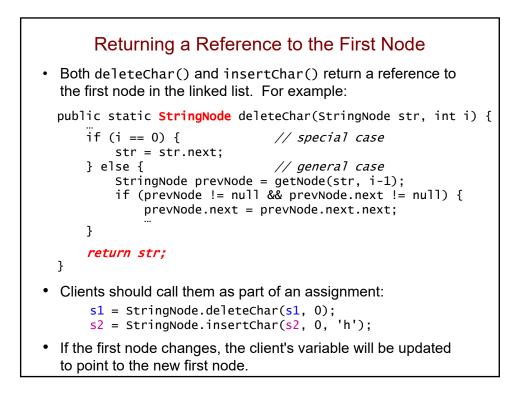


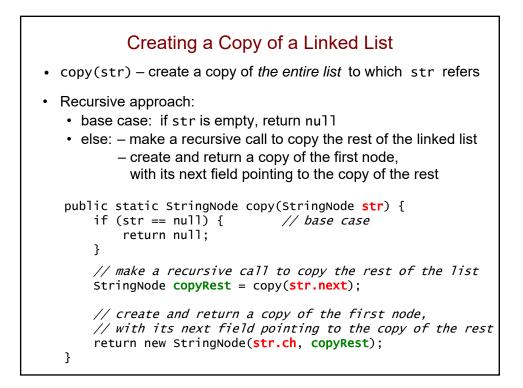


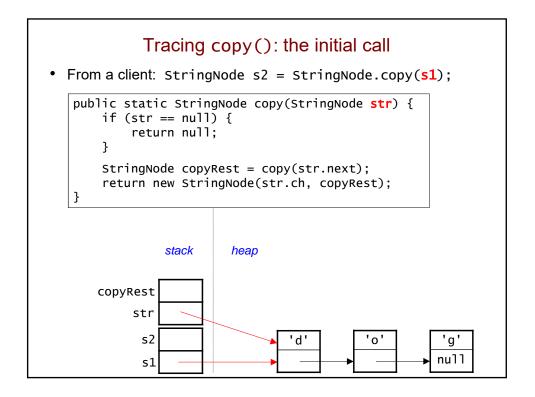


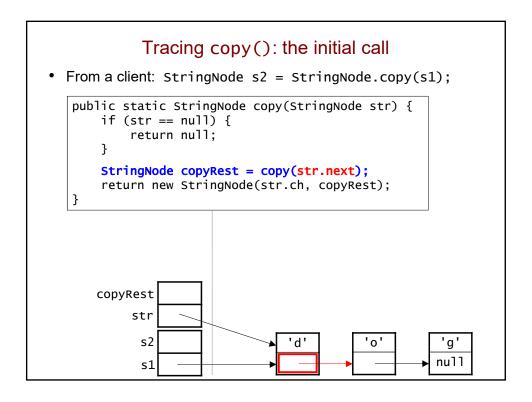


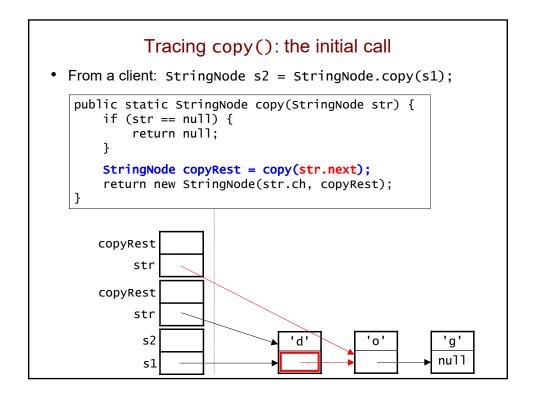


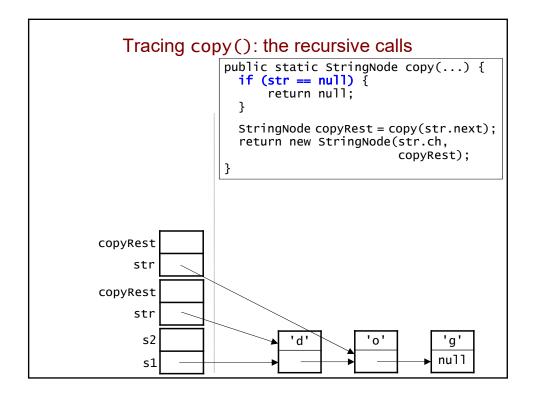


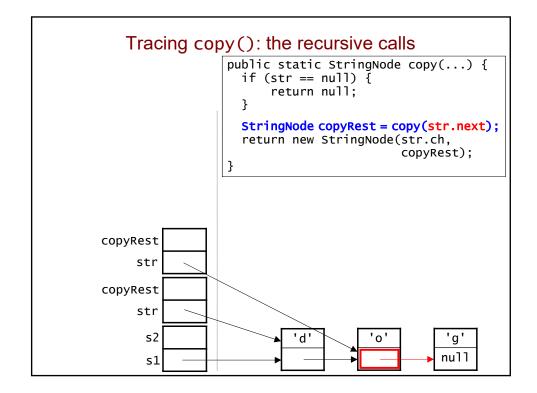


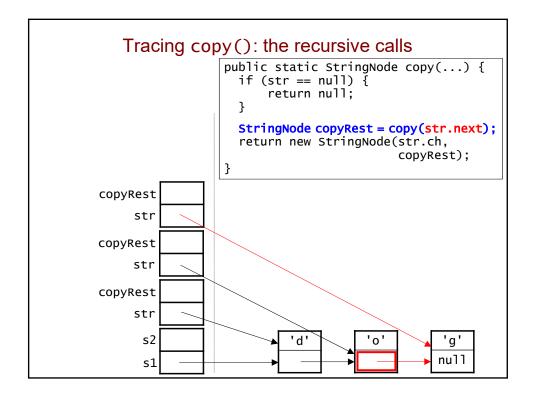


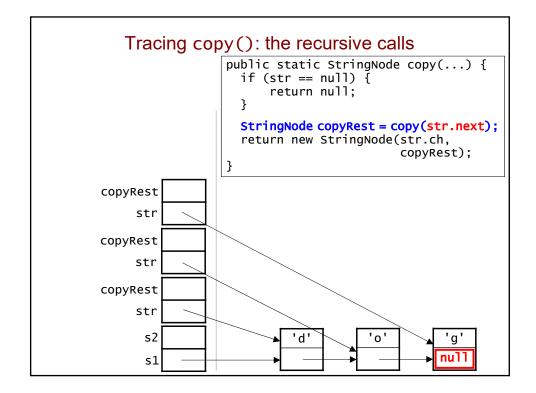


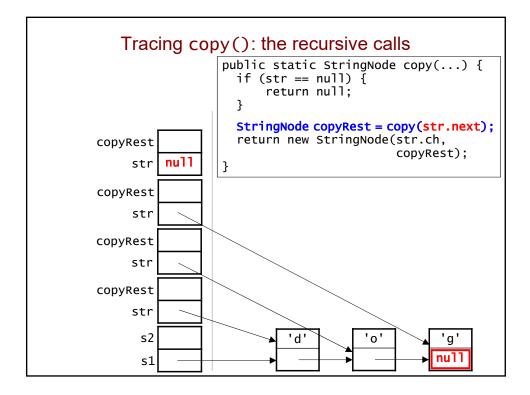


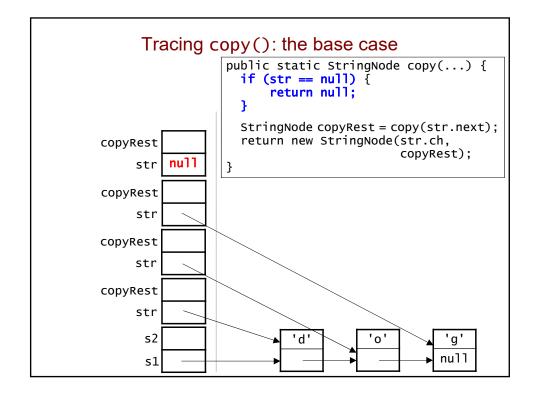


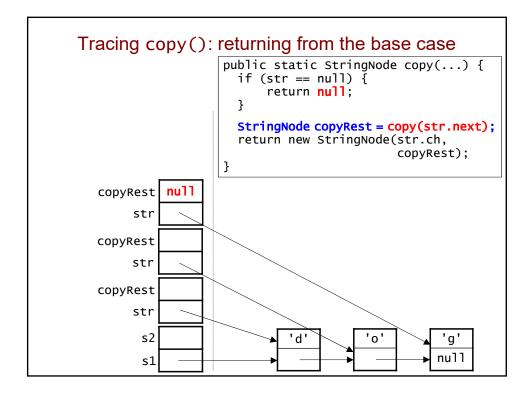


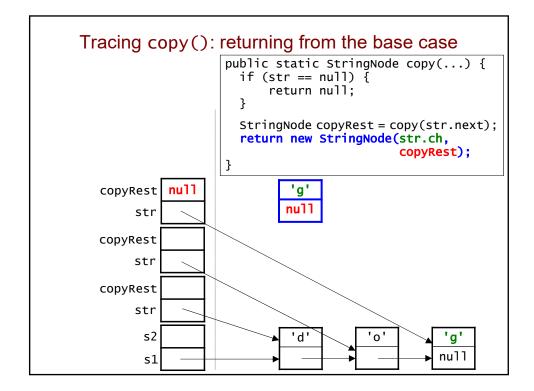


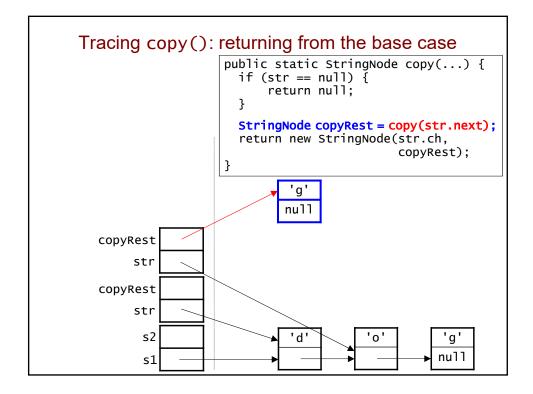


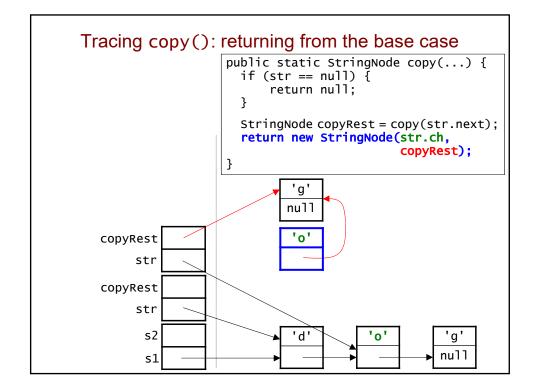


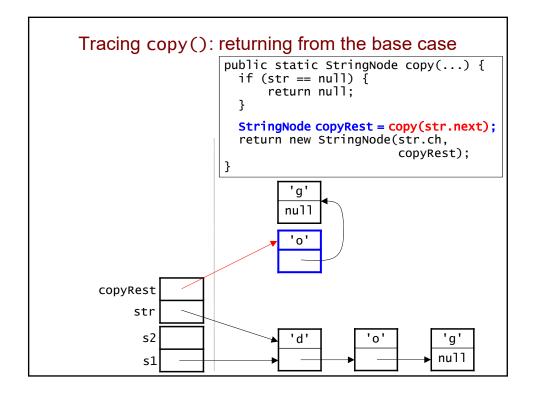


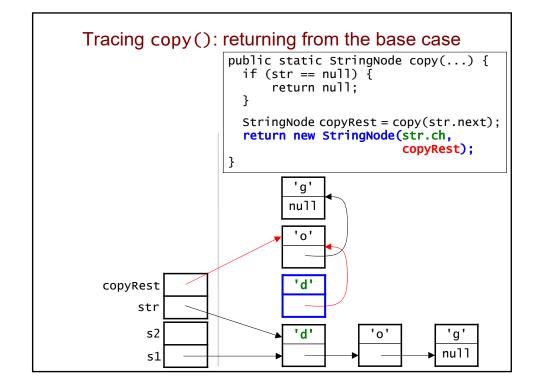


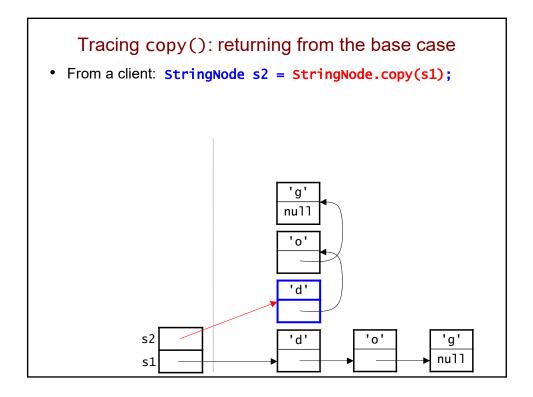


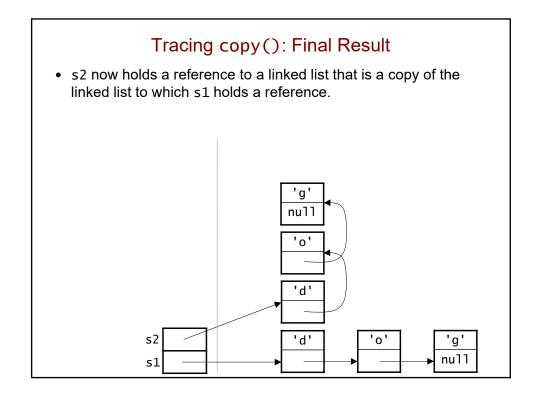


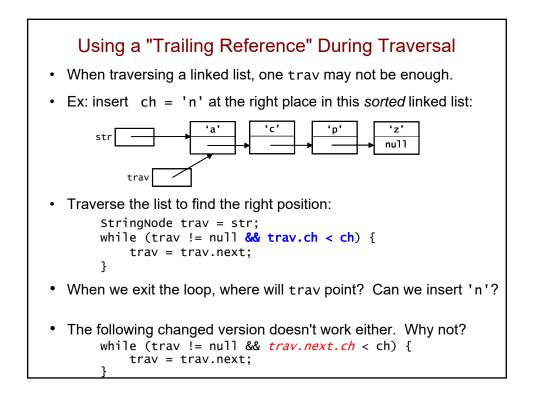


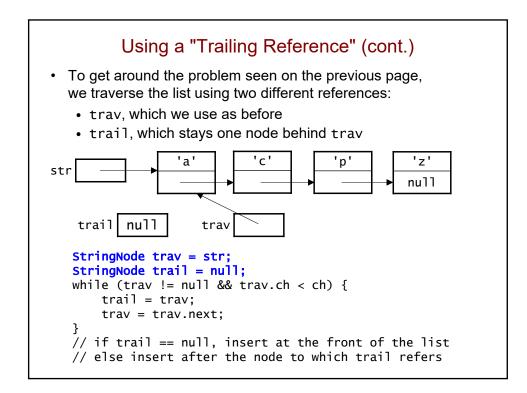


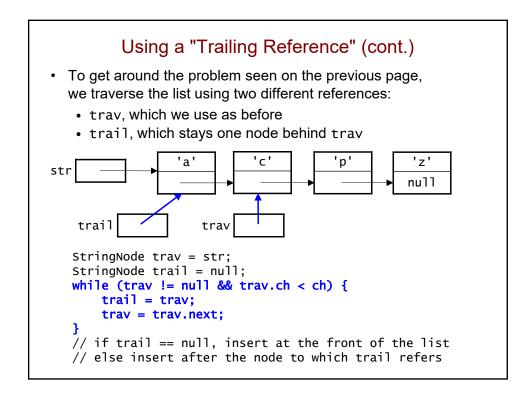


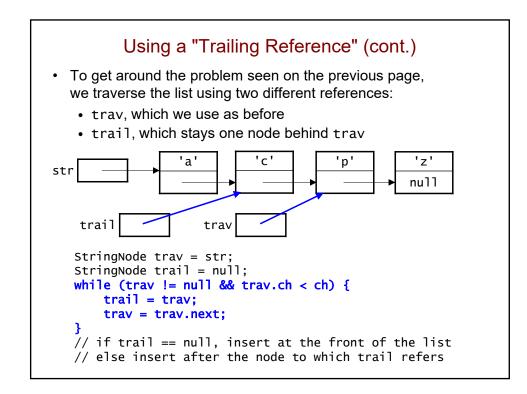


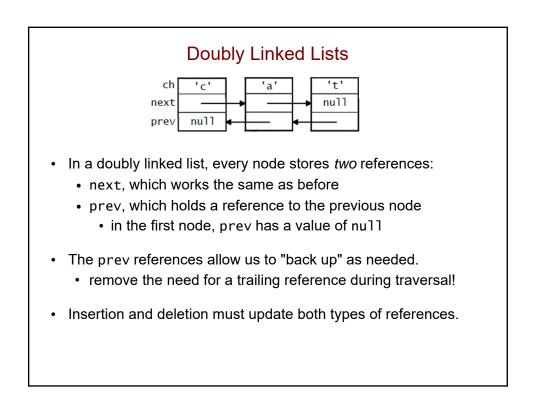


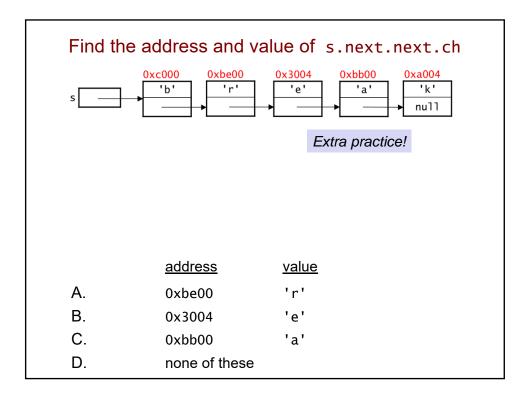


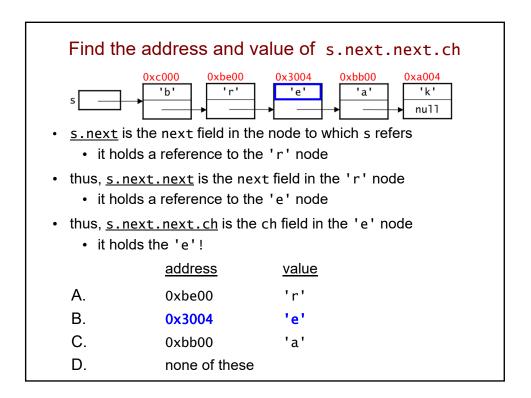


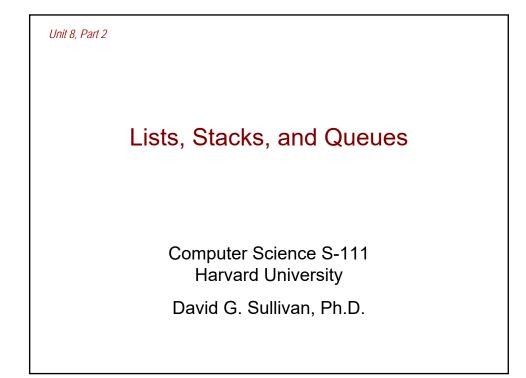










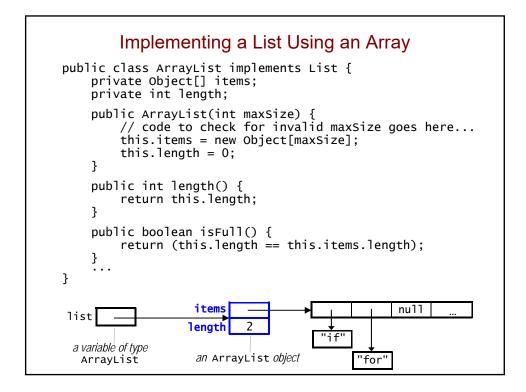


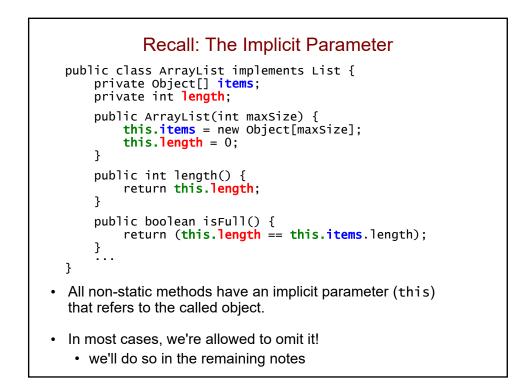
<ul> <li>Representing a Sequence: Arrays vs. Linked Lists</li> <li>Sequence – an ordered collection of items (position matters)</li> <li>we will look at several types: lists, stacks, and queues</li> <li>Can represent any sequence using an array <i>or</i> a linked list</li> </ul>		
	array	linked list
representation in memory	elements occupy consecutive memory locations	nodes can be at arbitrary locations in memory; the links connect the nodes together
advantages	<ul> <li>provide random access         <ul> <li>(access to any item in constant time)</li> <li>no extra memory needed for links</li> </ul> </li> </ul>	<ul> <li>can grow to an arbitrary length</li> <li>allocate nodes as needed</li> <li>inserting or deleting does <i>not</i> require shifting items</li> </ul>
disadvantages	<ul> <li>have to preallocate the memory needed for the maximum sequence size</li> <li>inserting or deleting can require shifting items</li> </ul>	<ul> <li>no random access (may need to traverse the list)</li> <li>need extra memory for links</li> </ul>

## The List ADT

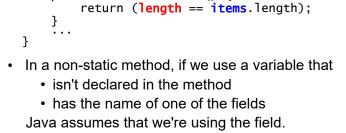
- A list is a sequence in which items can be accessed, inserted, and removed *at any position in the sequence*.
- The operations supported by our List ADT:
  - getItem(i): get the item at position i
  - addItem(item, i): add the specified item at position i
  - removeItem(i): remove the item at position i
  - length(): get the number of items in the list
  - isFull(): test if the list already has the maximum number of items
- Note that we *don't* specify *how* the list will be implemented.

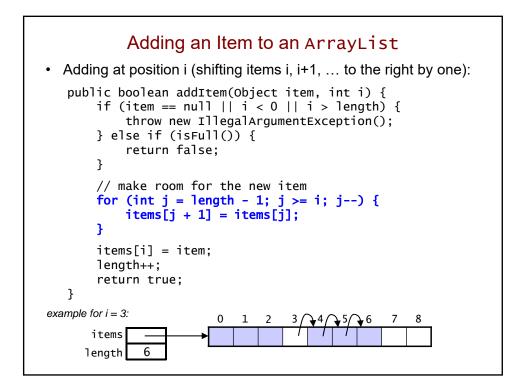
## Our List Interface public interface List { Object getItem(int i); boolean addItem(Object item, int i); Object removeItem(int i); int length(); boolean isFull(); } Recall that all methods in an interface must be public, so we don't need the keyword public in the headers. We use the Object type to allow for items of any type. addItem() returns false if the list is full, and true otherwise.

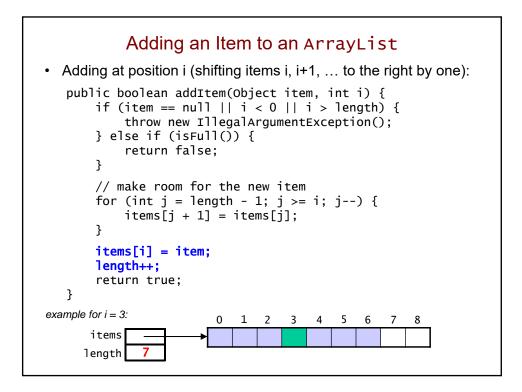


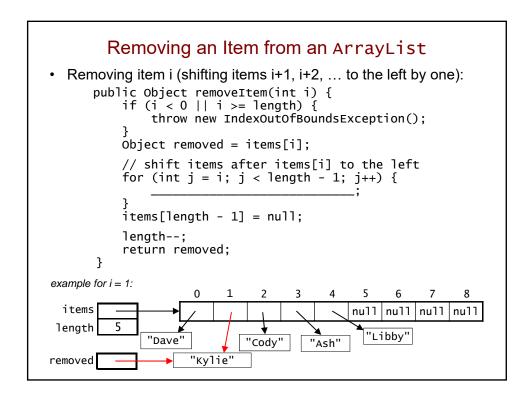


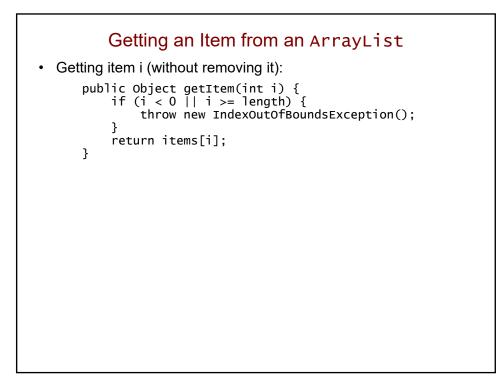
## Omitting The Implicit Parameter public class ArrayList implements List { private Object[] items; private int length; public ArrayList(int maxSize) { items = new Object[maxSize]; length = 0; } public int length() { return length; } public boolean isFull() { } }



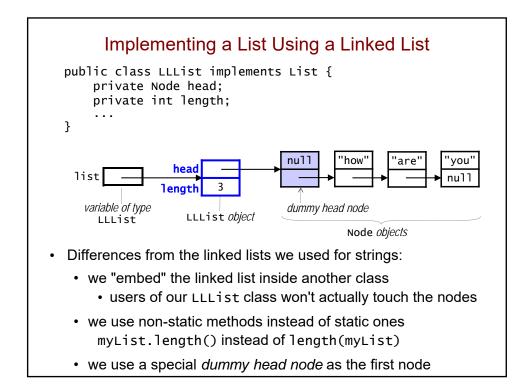


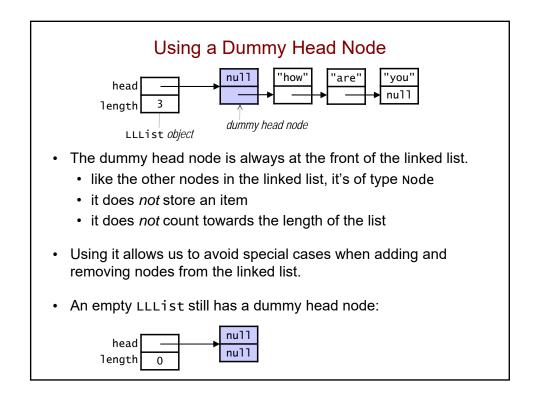


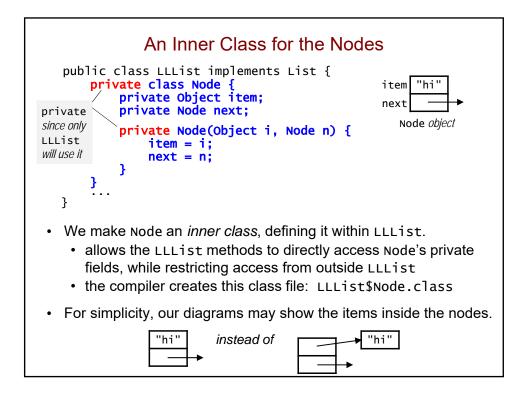




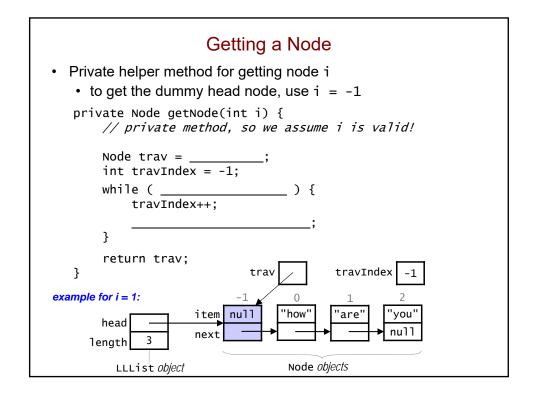
```
toString() Method for the ArrayList Class
   public String toString() {
       String str = "{";
       if (length > 0) {
            for (int i = 0; i < length - 1; i++) {
    str = str + items[i] + ", ";</pre>
            }
            str = str + items[length - 1];
       }
       str = str + "}";
        return str;
   }
  Produces a string of the following form:
٠
       {items[0], items[1], ... }
  Why is the last item added outside the loop?
٠
  Why do we need the if statement?
```

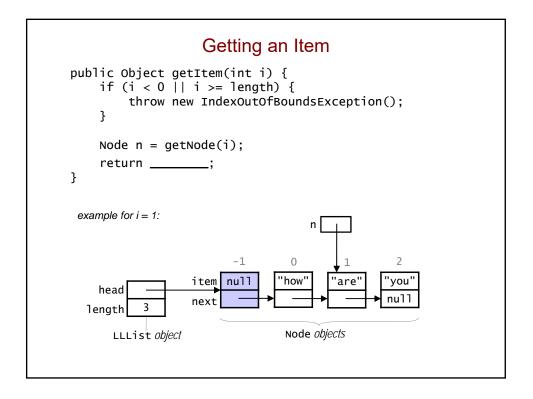


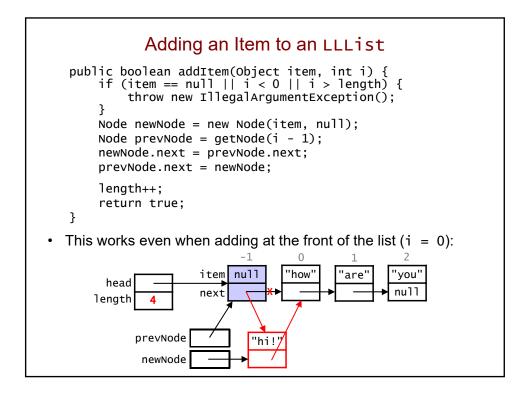


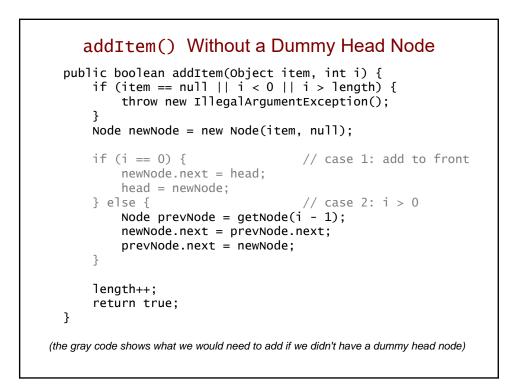


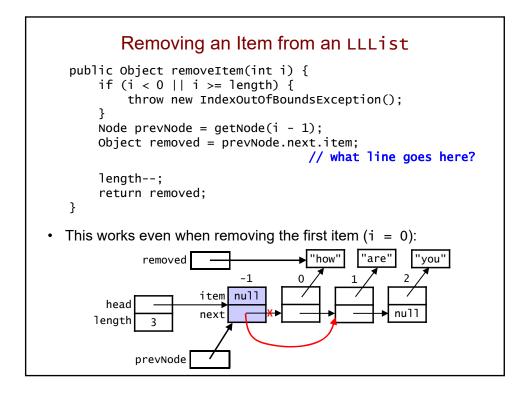
Other Details of Our LLList Class
<pre>public class LLList implements List {     private class Node {         // see previous slide     }</pre>
private Node head; private int length;
<pre>public LLList() {     head = new Node(null, null);     length = 0; }</pre>
<pre>public boolean isFull() {     return false;   }  }</pre>
<ul> <li>Unlike ArrayList, there's no need to preallocate space for the items. The constructor simply creates the dummy head node.</li> </ul>
The linked list can grow indefinitely, so the list is never full!

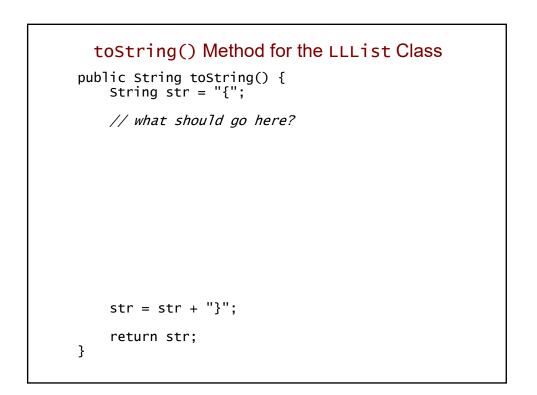












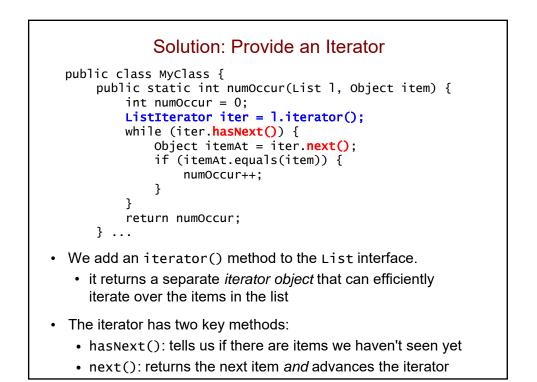
	ArrayList	items in the list	
getItem()	only one case:	best: worst: average:	
addItem()	best: worst:	best: worst:	
	average:	average:	

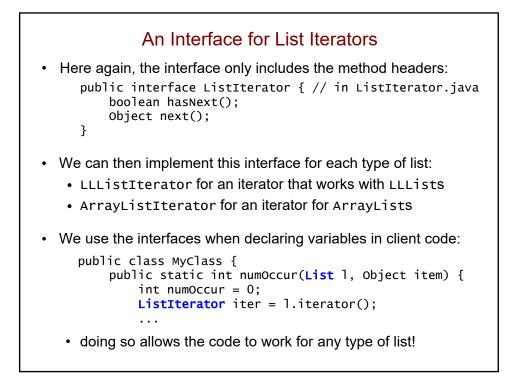
Efficiency of the List ADT Implementations (cont.) n = number of items in the list					
	n = number of items ArrayList				
<pre>removeItem()</pre>	best:	best:			
	worst:	worst:			
	average:	average:			
space efficiency					

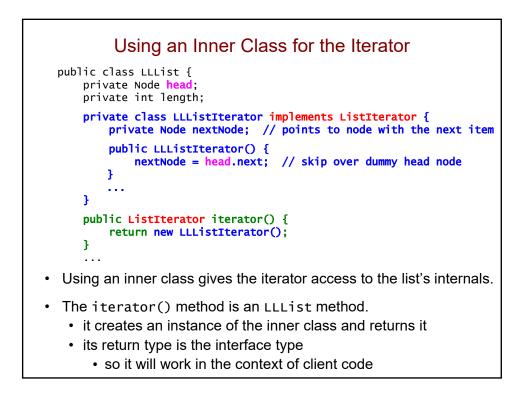
## Counting the Number of Occurrences of an Item

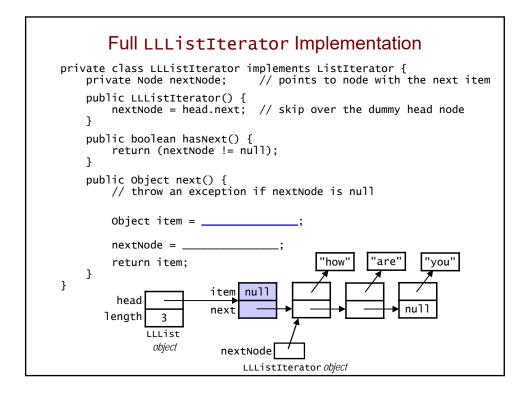
```
public class MyClass {
    public static int numOccur(List 1, Object item) {
        int numOccur = 0;
        for (int i = 0; i < 1.length(); i++) {
            Object itemAt = 1.getItem(i);
            if (itemAt.equals(item)) {
                numOccur++;
            }
            return numOccur;
        } ...
This method works fine if we pass in an ArrayList object.
        time efficiency (as a function of the length, n) = ?</pre>
```

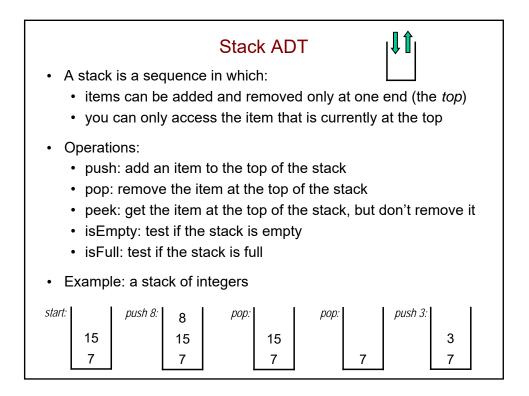
- However, it's not efficient if we pass in an LLList.
  - each call to getItem() calls getNode()
  - to access item 0, getNode() accesses 2 nodes (dummy + node 0)
  - to access item 1, getNode() accesses 3 nodes
  - to access item i, getNode() accesses i+2 nodes
  - 2 + 3 + ... + (n+1) = ?







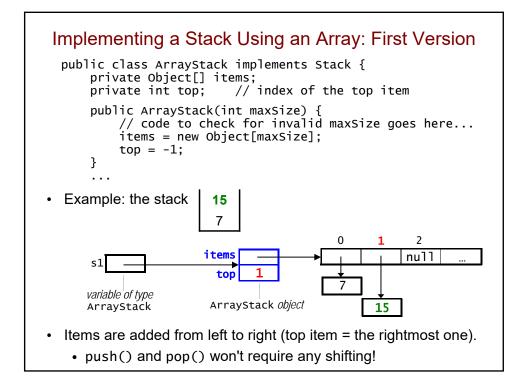


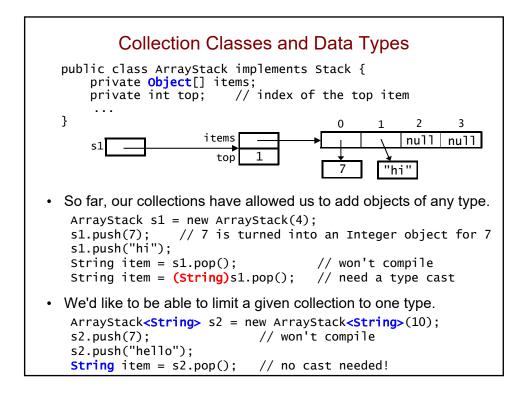


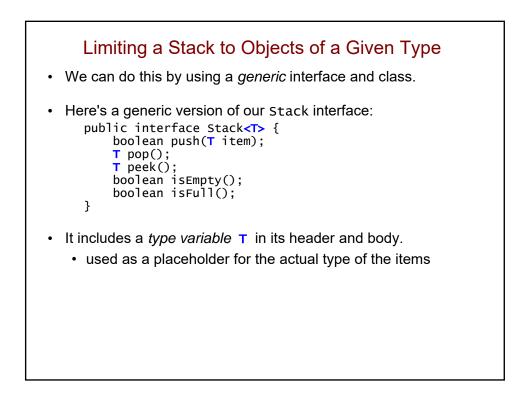
## A Stack Interface: First Version

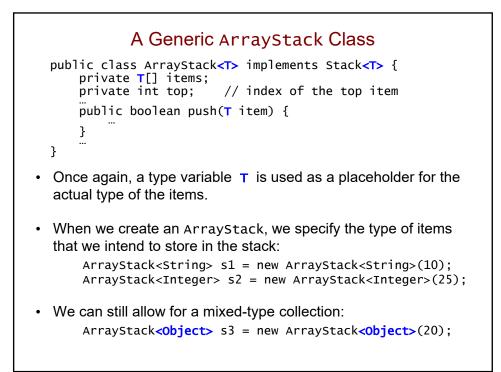
```
public interface Stack {
    boolean push(Object item);
    Object pop();
    Object peek();
    boolean isEmpty();
    boolean isFull();
}
```

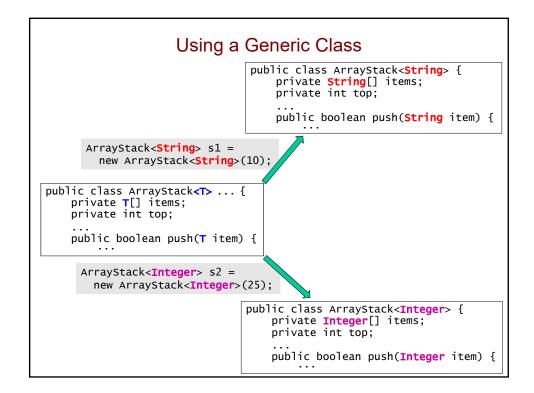
- push() returns false if the stack is full, and true otherwise.
- pop() and peek() take no arguments, because we know that we always access the item at the top of the stack.
  - return null if the stack is empty.
- The interface provides no way to access/insert/delete an item at an arbitrary position.
  - encapsulation allows us to ensure that our stacks are only manipulated in appropriate ways

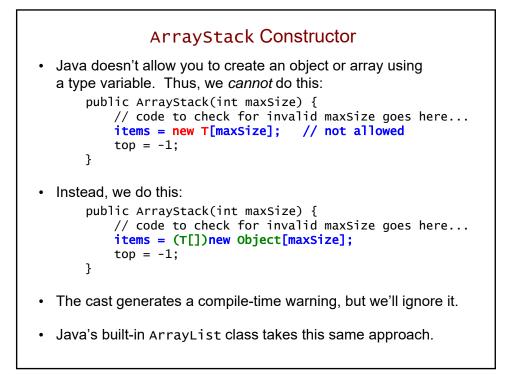


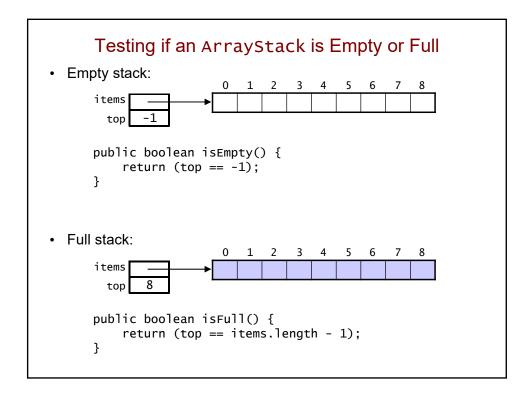


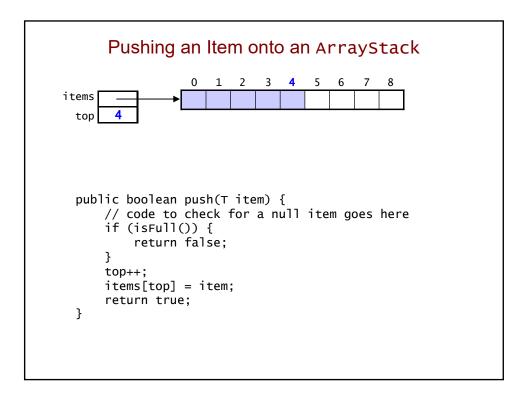


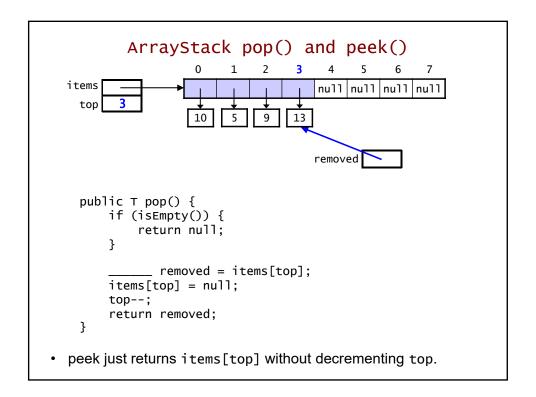


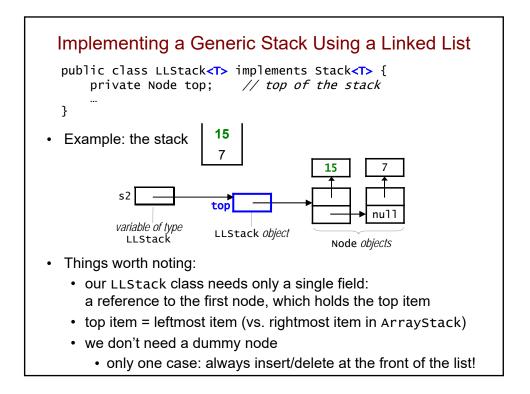


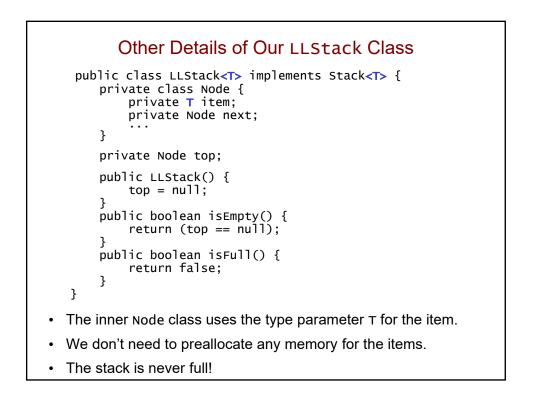


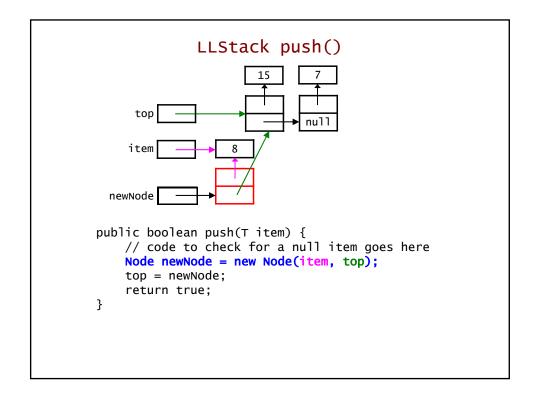


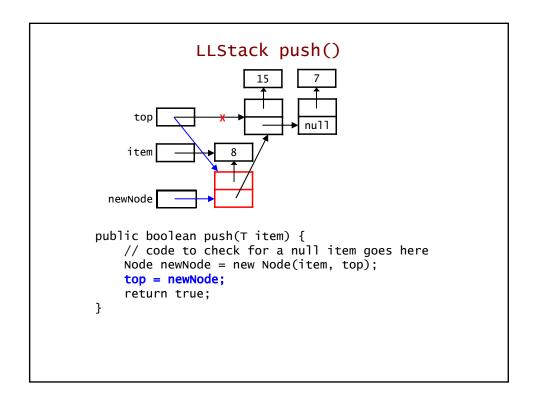


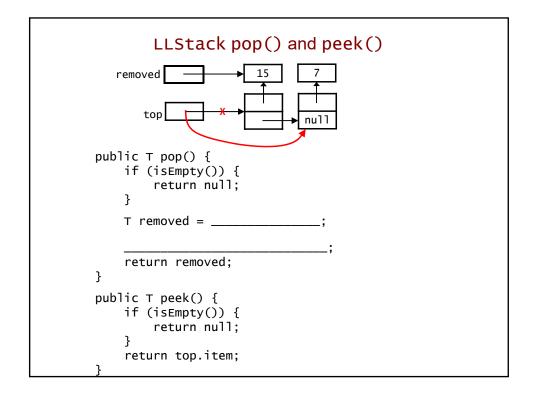




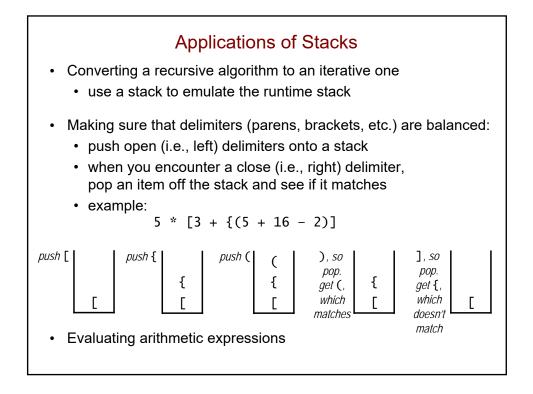


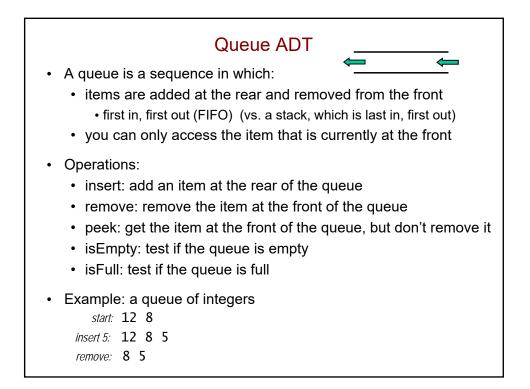


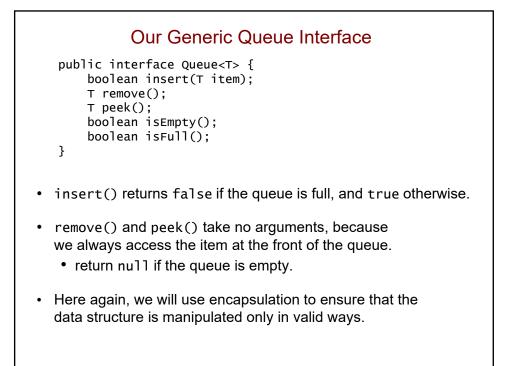


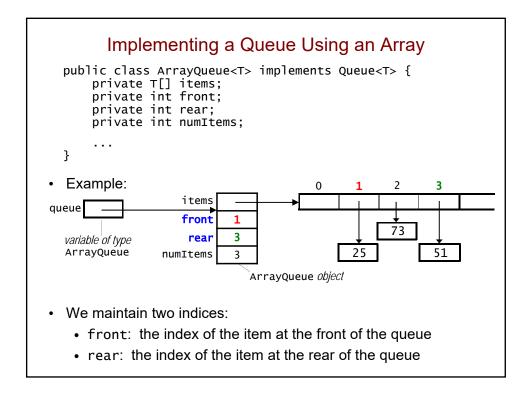


Oush()         O(1)         O(1)           oop()         O(1)         O(1)           oeek()         O(1)         O(1)           opace         O(m) where m is the         O(n) where n is the number of
Deek()O(1)O(1)SpaceO(m) where m is theO(n) where n is the number of
space O(m) where m is the O(n) where n is the number of
efficiency anticipated maximum number items currently on the stack of items

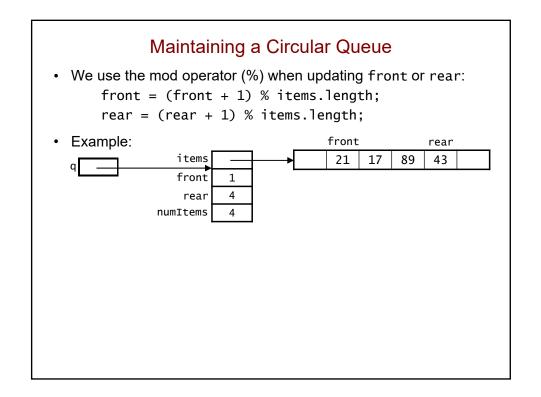


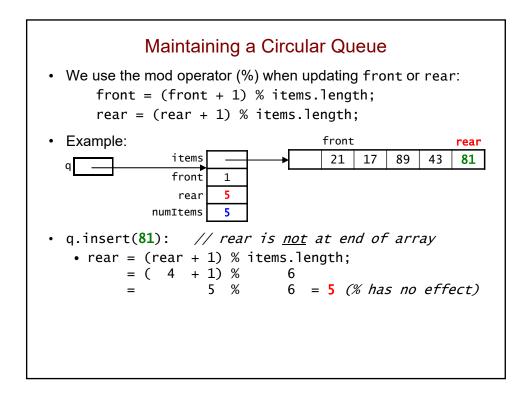


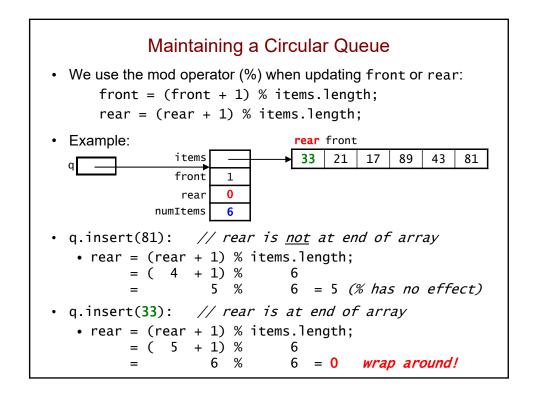


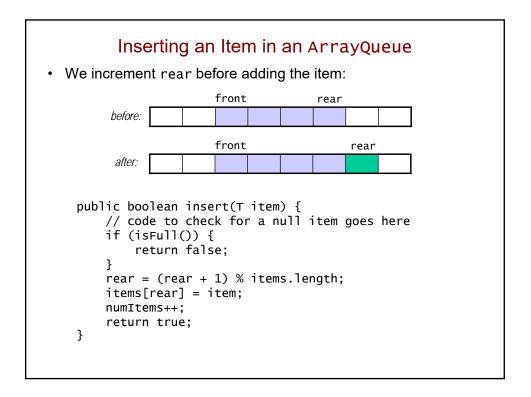


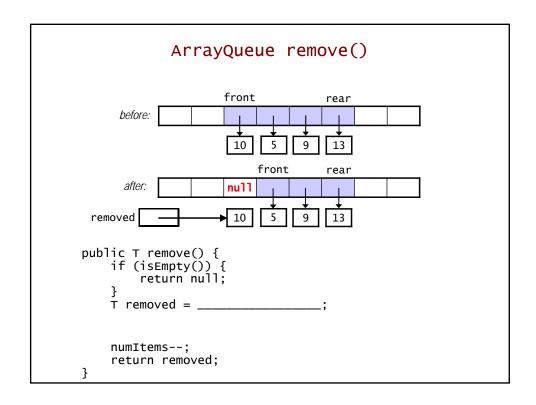
Avoiding the Need to Shift Items
<ul> <li>Problem: what do we do when we reach the end of the array?</li> </ul>
example: a queue of integers:
front rear
54 4 21 17 89 65
the same queue after removing two items and inserting two:
<ul> <li>we have room for more items, but shifting to make room is inefficient</li> <li>Solution: maintain a <i>circular queue</i>. When we reach the end of the array, we wrap around to the beginning.</li> </ul>
insert 5: wrap around!
rear front
5         21         17         89         65         43         81

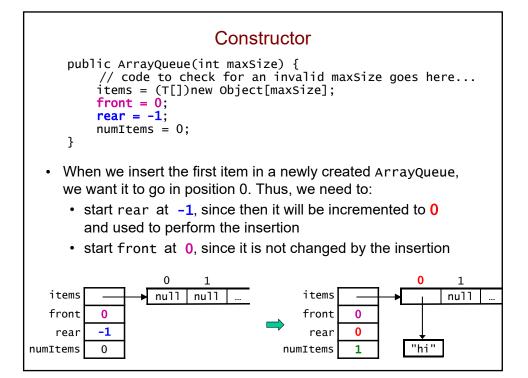


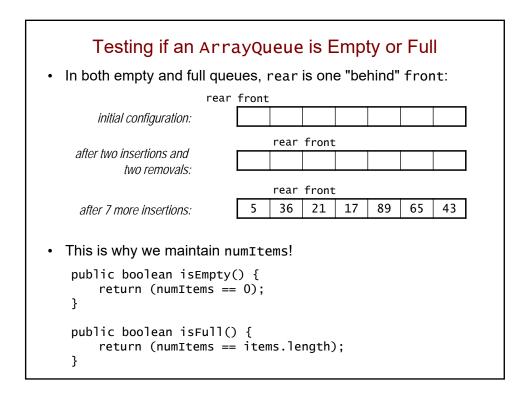


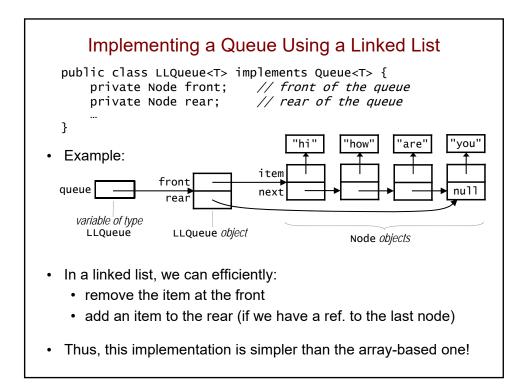


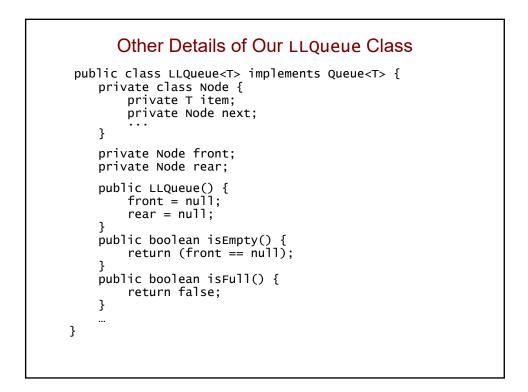


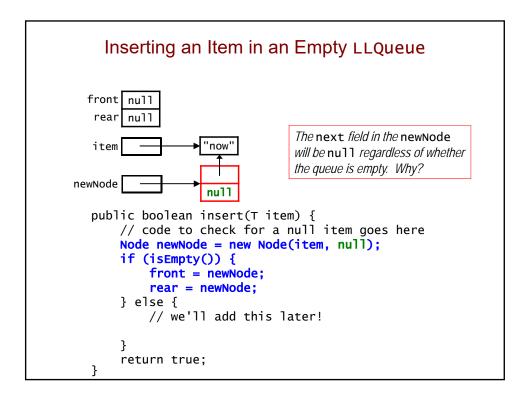


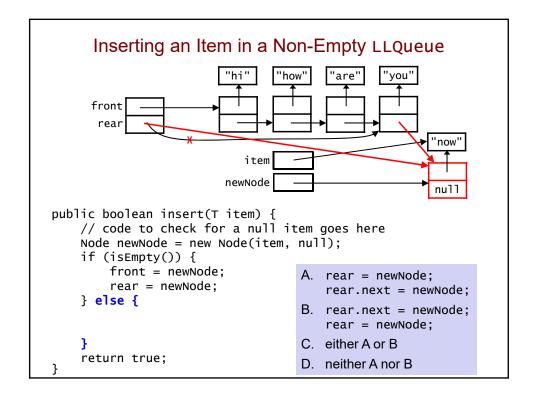


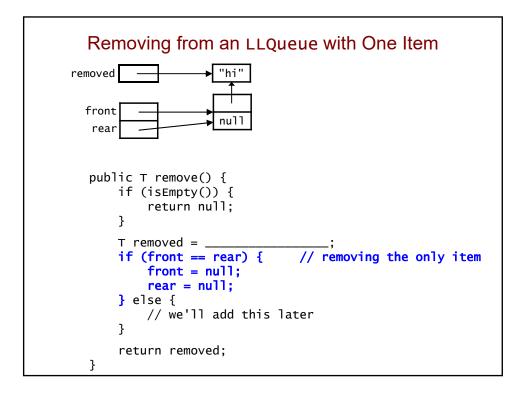


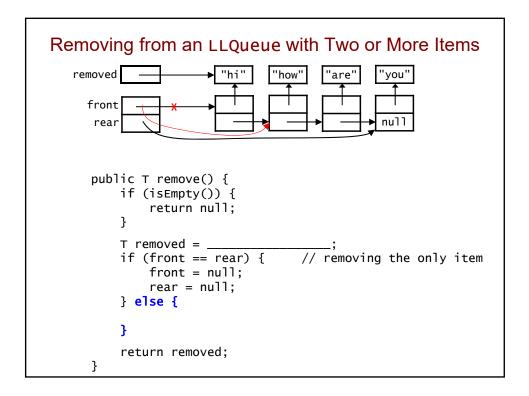




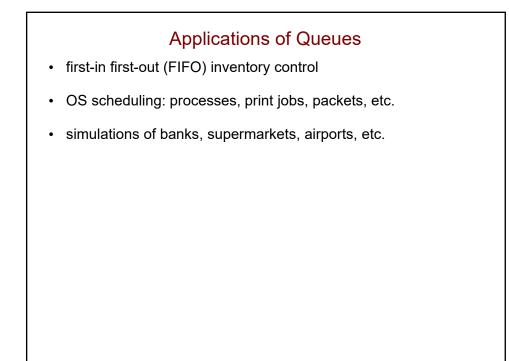


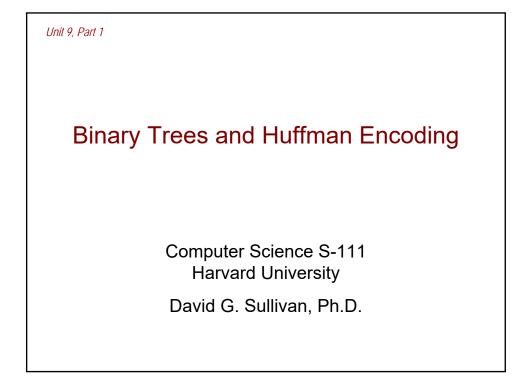






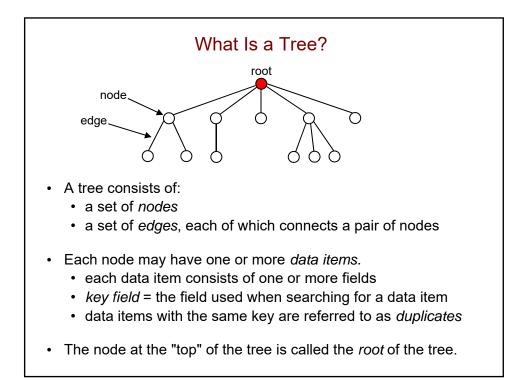
	ArrayQueue	LLQueue
insert()	O(1)	O(1)
remove()	<i>O</i> (1)	<i>O</i> (1)
peek()	<i>O</i> (1)	O(1)
space efficiency	O(m) where m is the anticipated maximum number of items	O(n) where n is the number of items currently in the queue

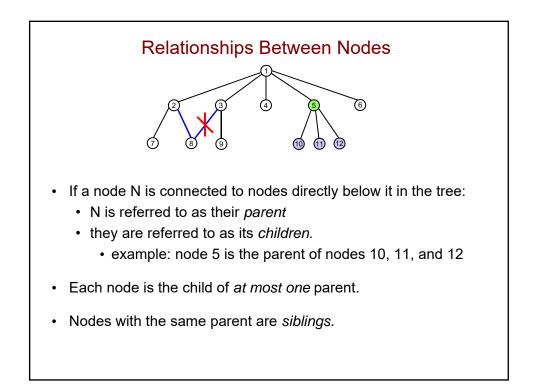


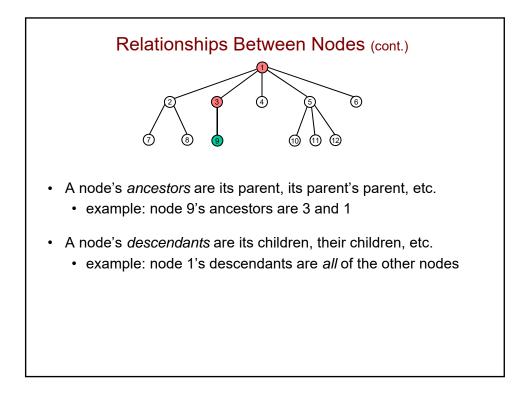


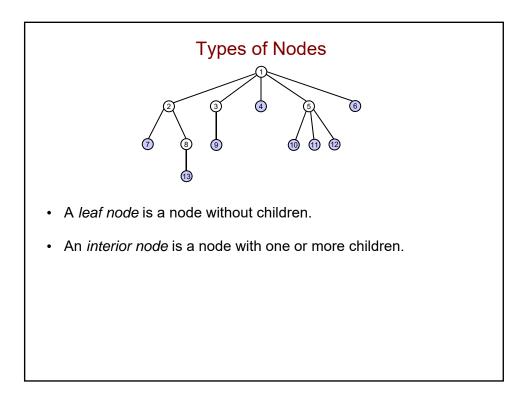
<ul> <li>A <i>data dictionary</i> is a collection of data with two main operations:</li> <li><i>search</i> for an item (and possibly delete it)</li> <li><i>insert</i> a new item</li> <li>If we use a <i>sorted</i> list to implement it, efficiency = <i>O</i>(n).</li> </ul>				
data structure	searching for an item	inserting an item		
a list implemented using an array	O(log n) using binary search	O(n) because we need to shift items over		
		<i>O</i> (n)		

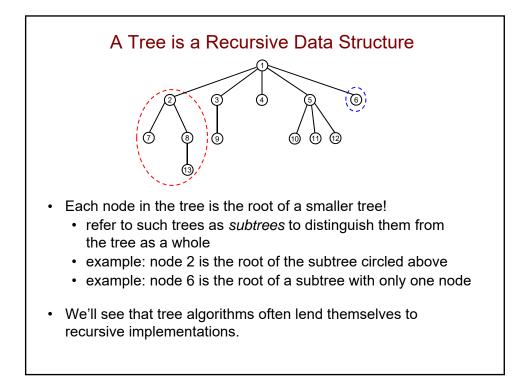
• We'll also look at other applications of trees.

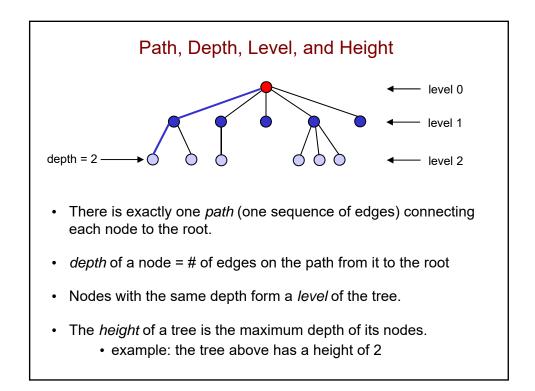


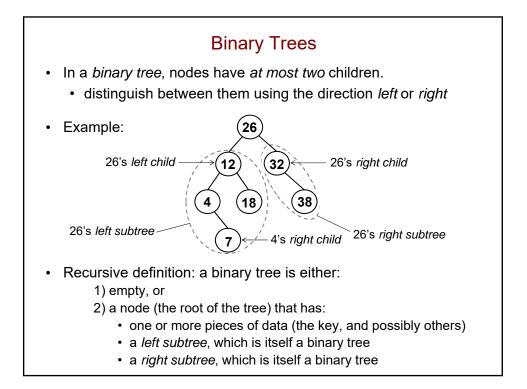


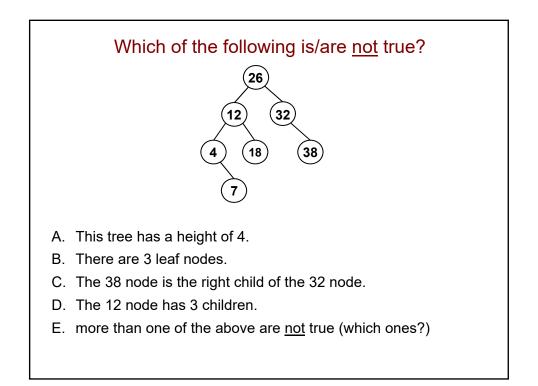


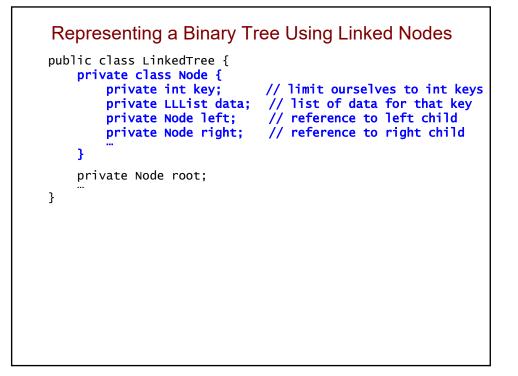


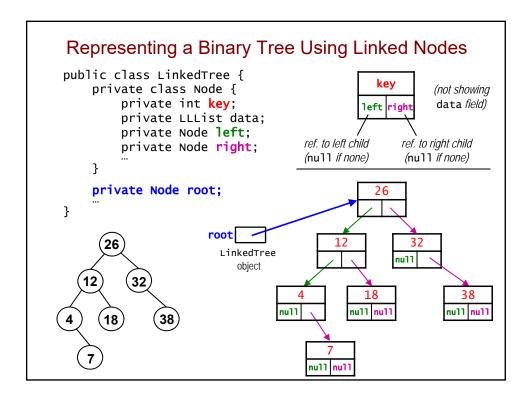


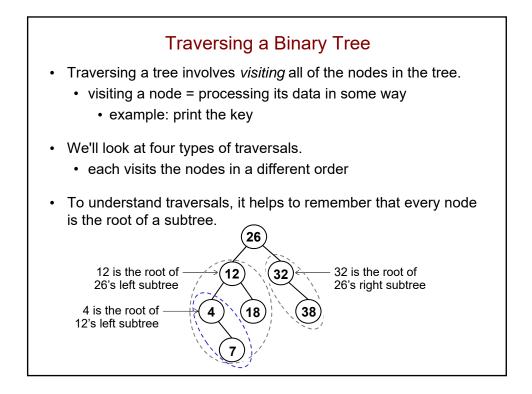


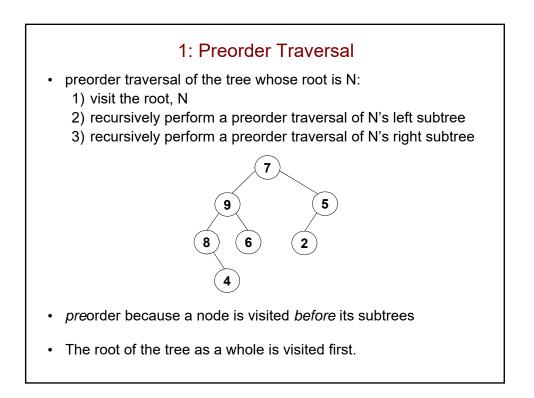


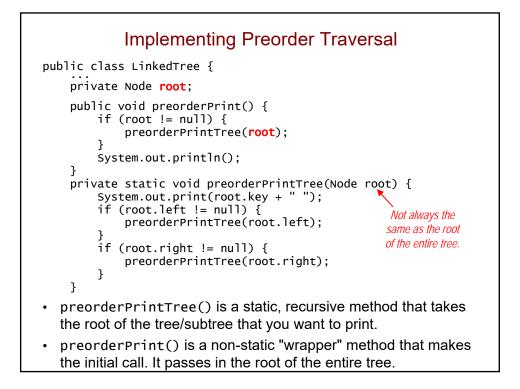


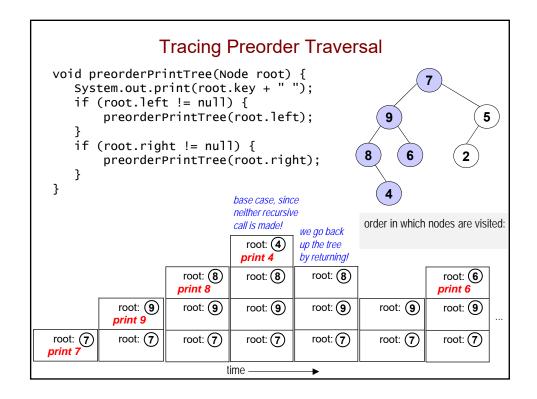


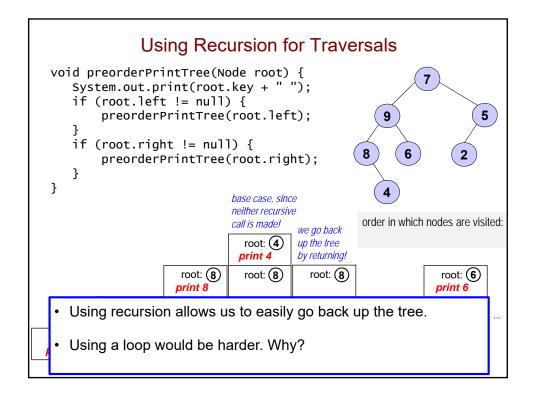


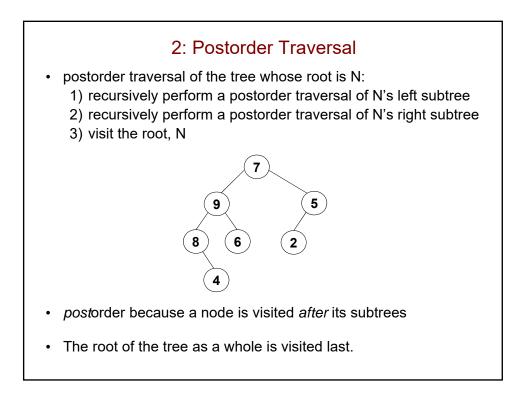


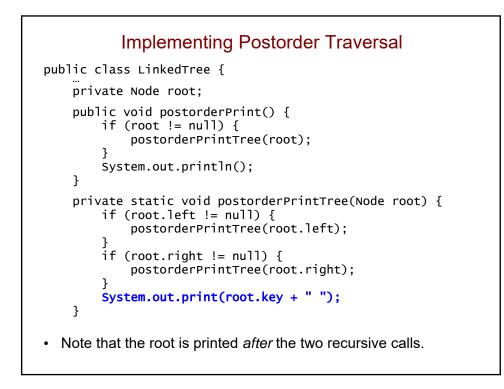


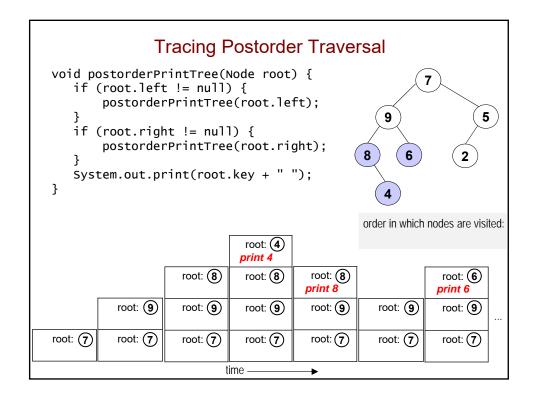


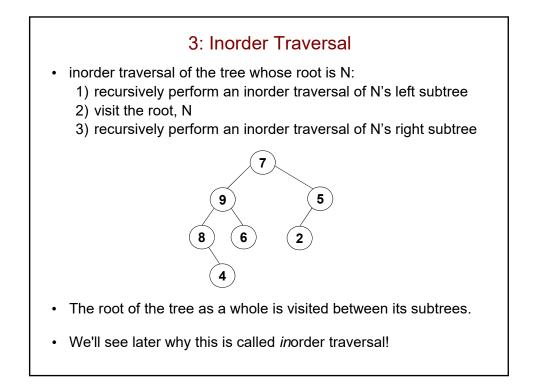


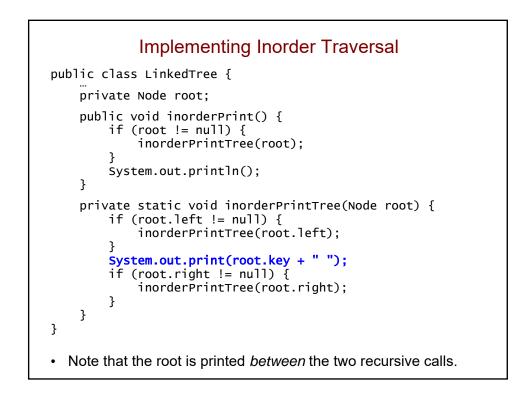


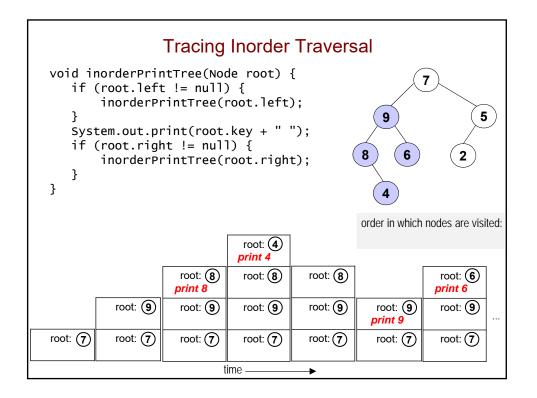


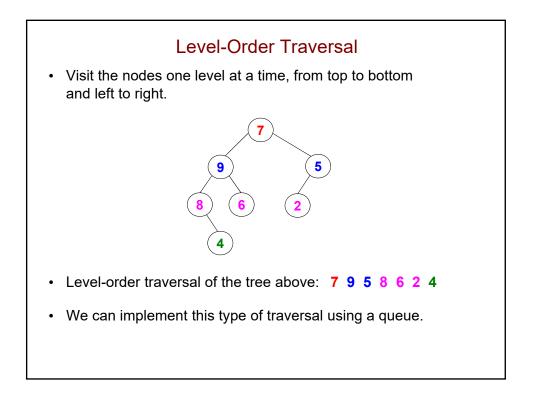


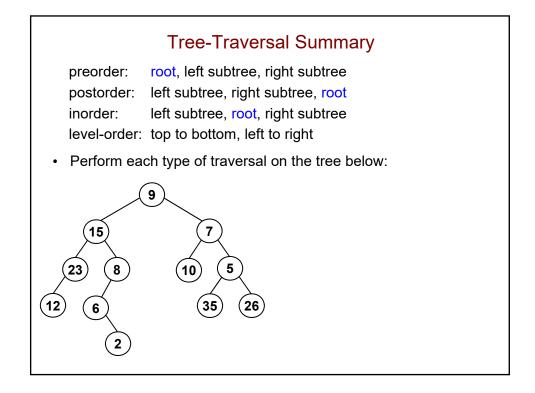




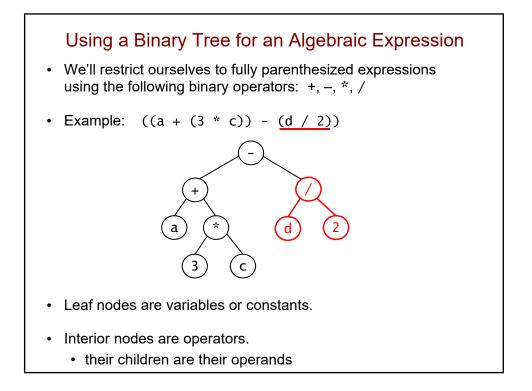


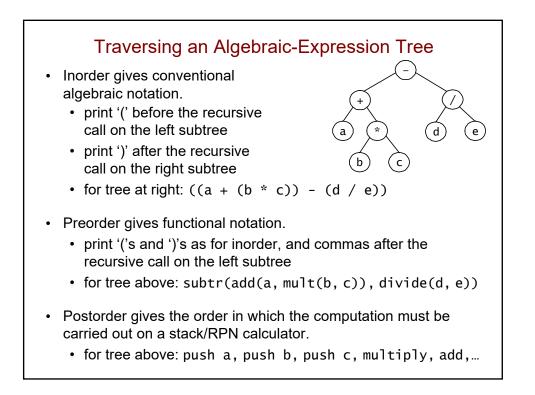


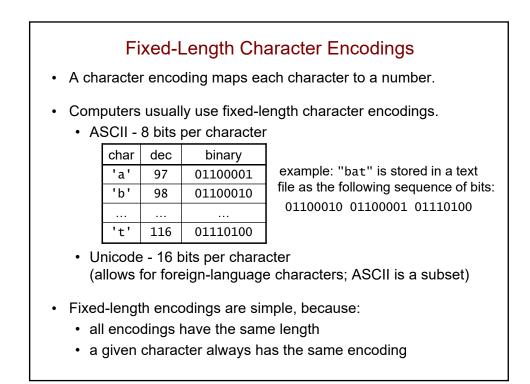


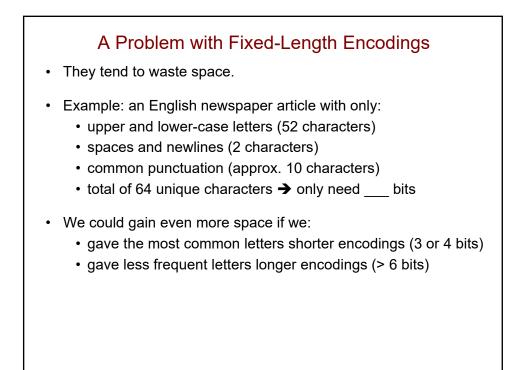


Tree Traversal Puzzle		
• preorder traversal: A M P K L D H T		
• inorder traversal: PMLKAHTD		
Draw the tree!		
<ul> <li>What's one fact that we can easily determine from one of the traversals?</li> </ul>		









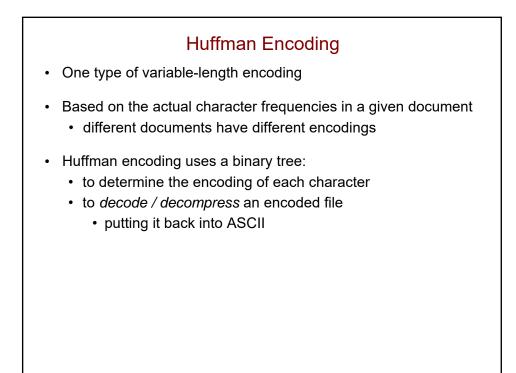
## Variable-Length Character Encodings

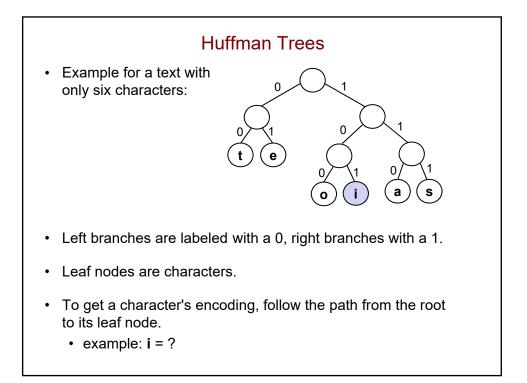
- Variable-length encodings compress a text file by:
  - · using encodings of different lengths for different characters
  - assigning shorter encodings to frequently occurring characters
- · Example: if we had only four characters

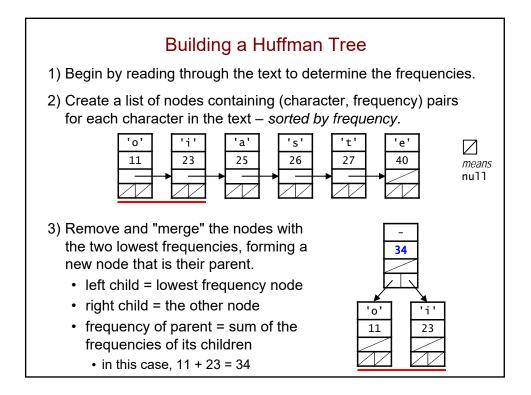
е	01
0	100
s	111
t	00

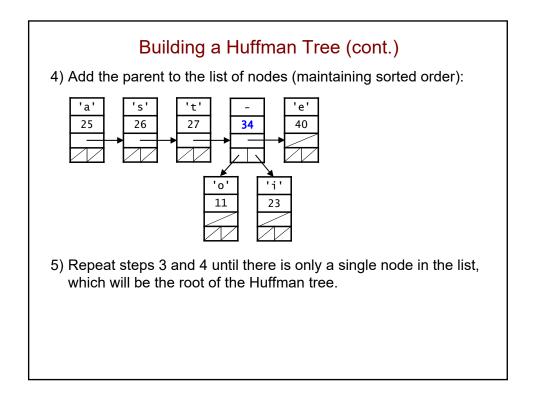
"test" would be encoded as 00 01 111 00 → 000111100

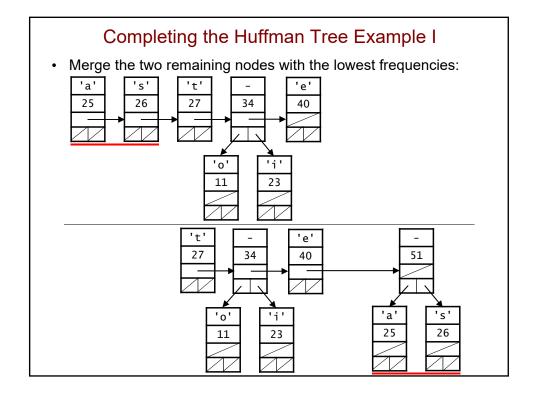
- Challenge: when reading a document, how do we determine the boundaries between characters?
  - · how do we know how many bits the next character has?
- One requirement: no character's encoding can be the prefix of another character's encoding (e.g., couldn't have 00 and 001).

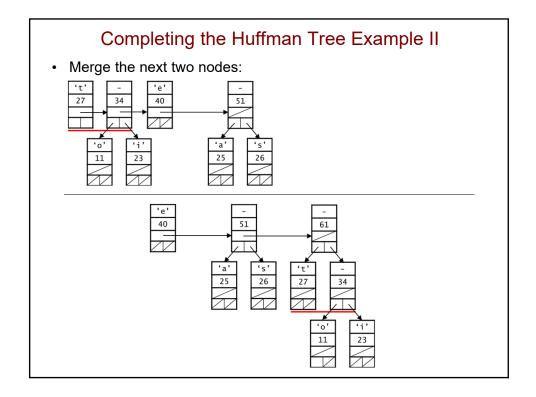


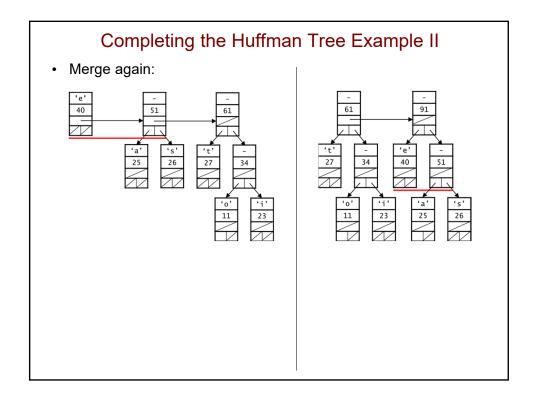


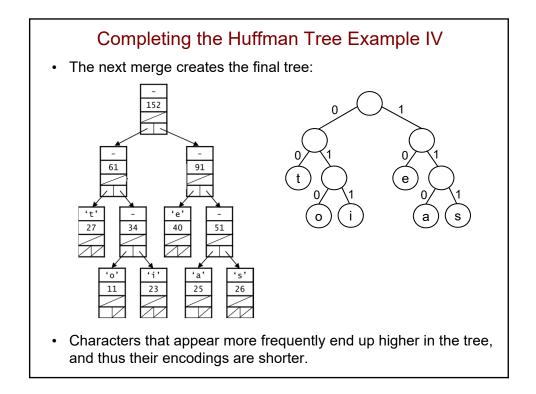


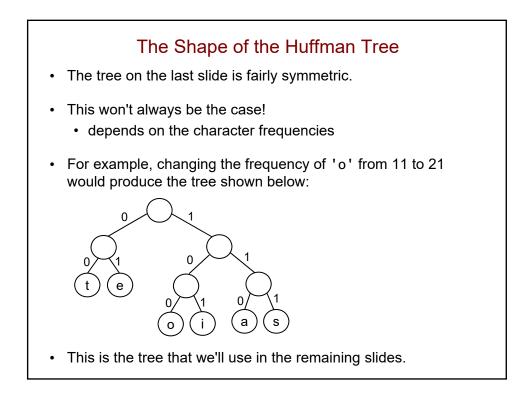


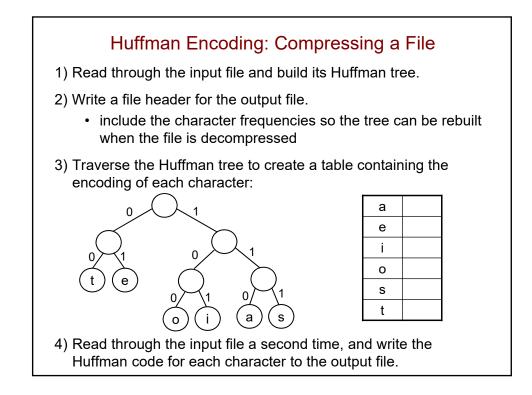


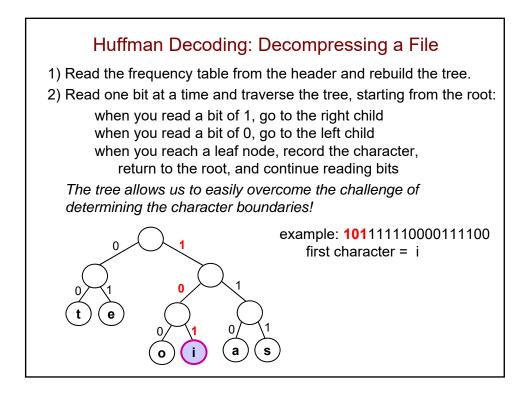


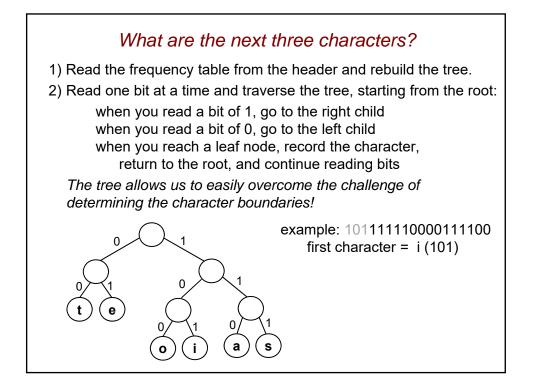




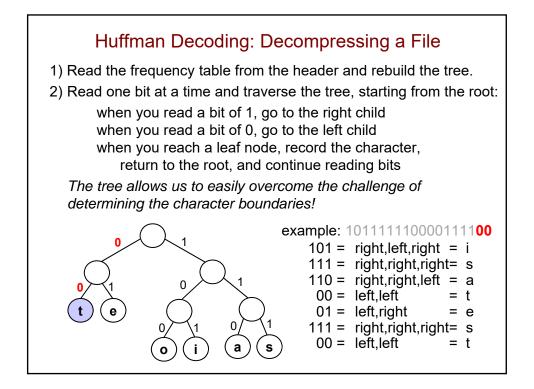


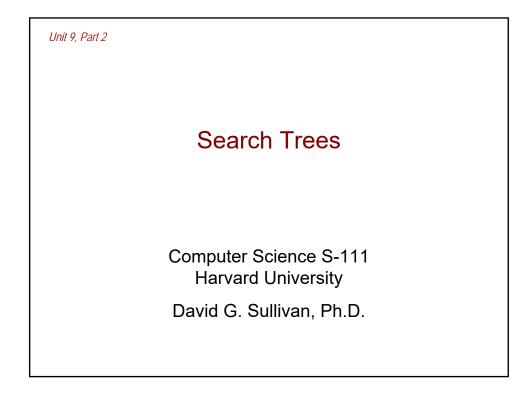


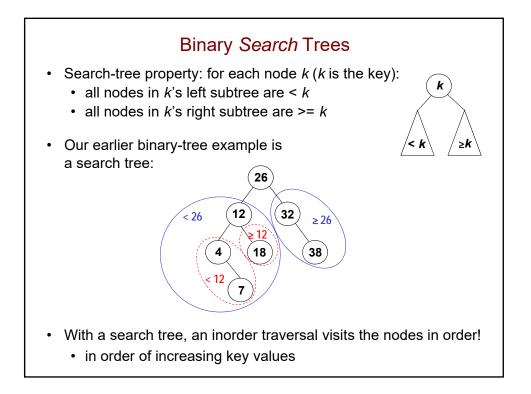


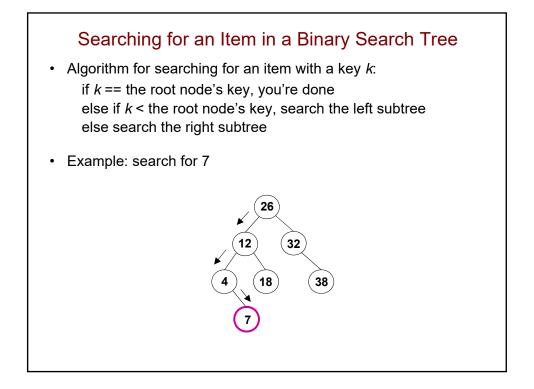




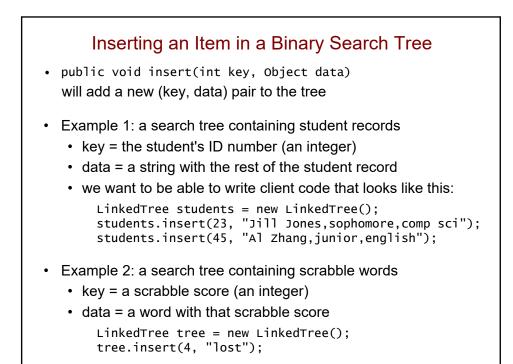


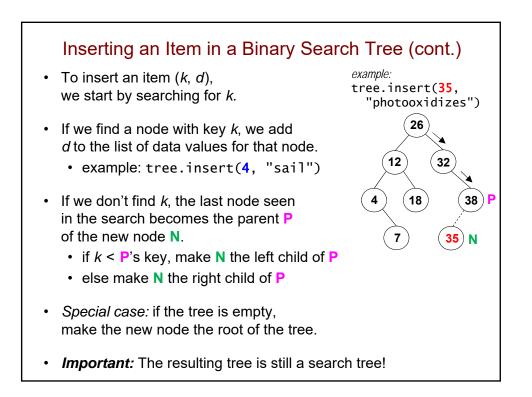


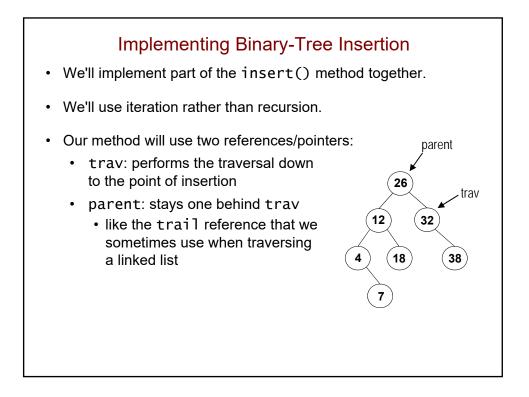


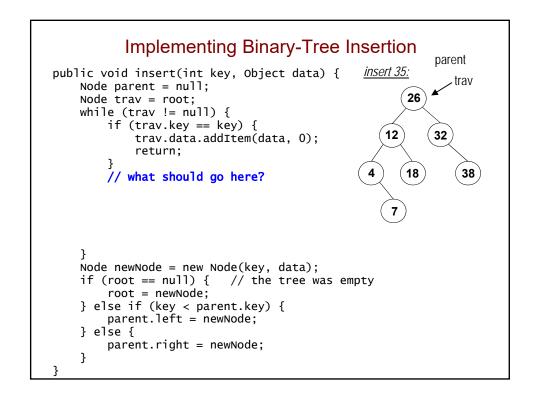


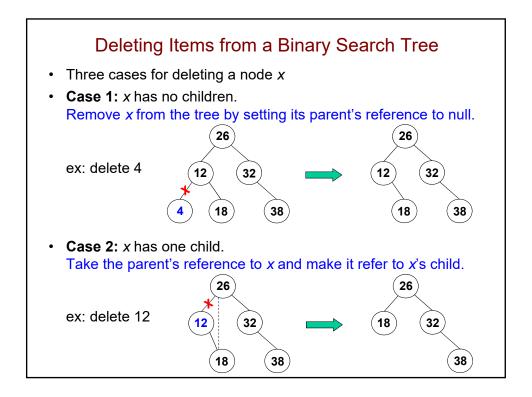
Implementing Binary-Tree Search			
<pre>public class LinkedTree { // Nodes have keys</pre>	<i>that are</i> int <i>s</i>		
private Node root;			
<pre>public LLList search(int key) { // "wr Node n = searchTree(root, key); // get if (n == null) { return null; // no such key } else { return n.data; // return list of } }</pre>	Node for key		
<pre>private static Node searchTree(Node root, int key) {     if (</pre>			
<pre>} else if ( ) {</pre>	<ul> <li>two base cases (order matters!)</li> </ul>		
<pre>} else if ( ) {</pre>	٦ آ		
} else {	two recursive cases		
}	J		

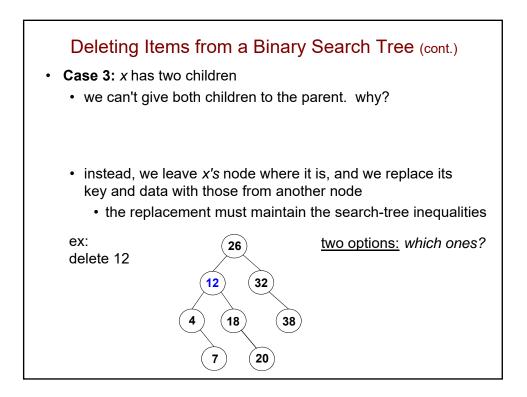


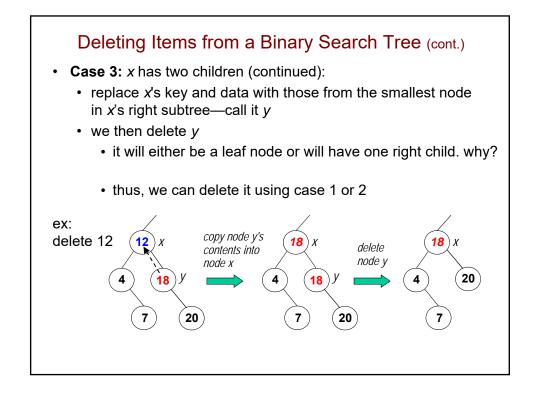


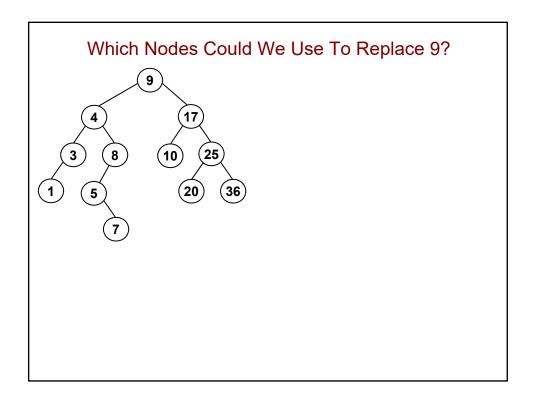


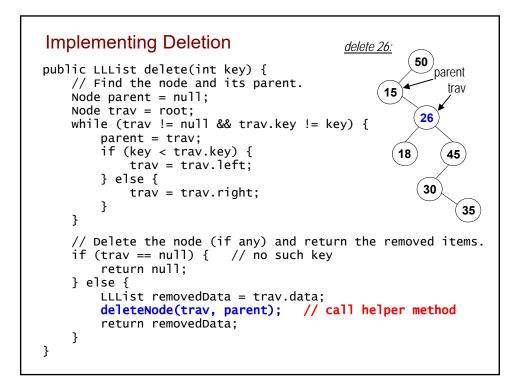


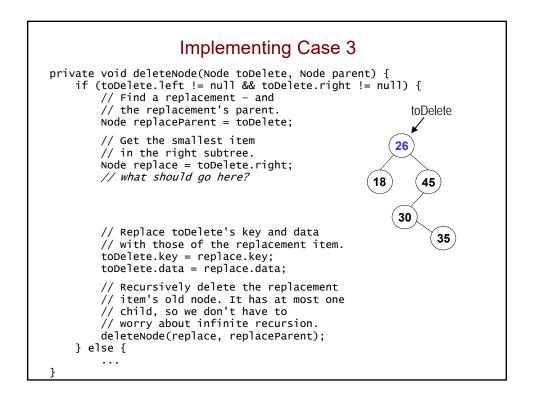


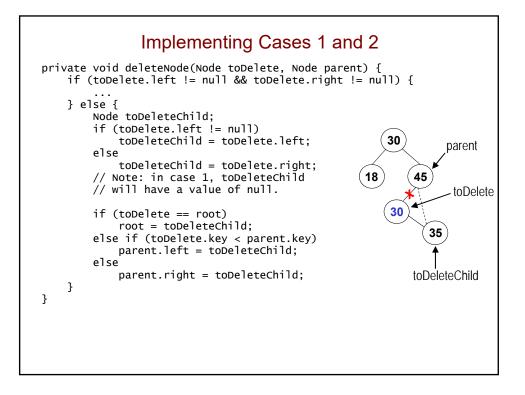


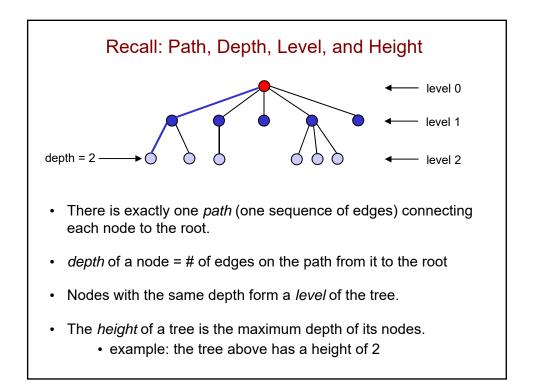


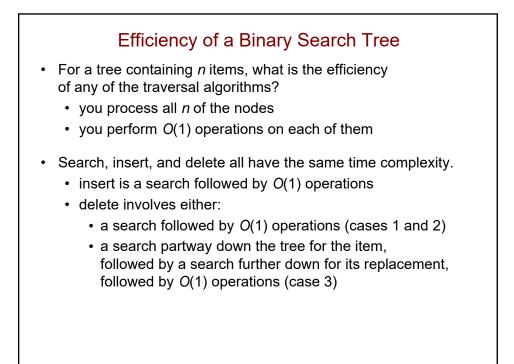


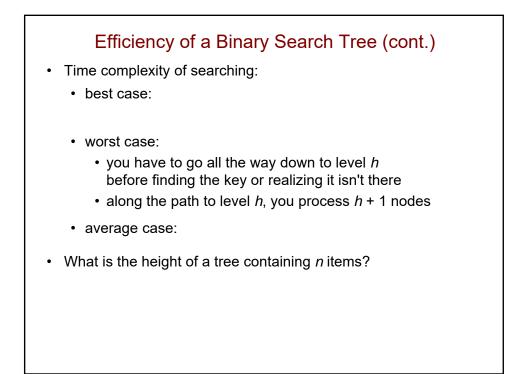


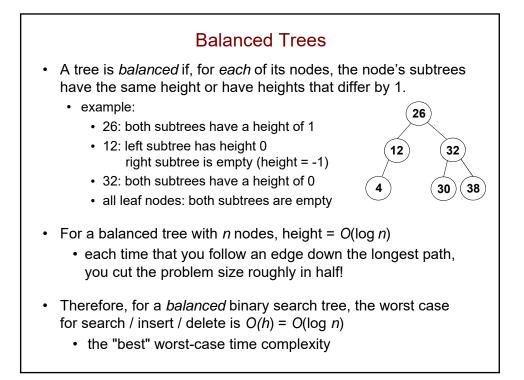


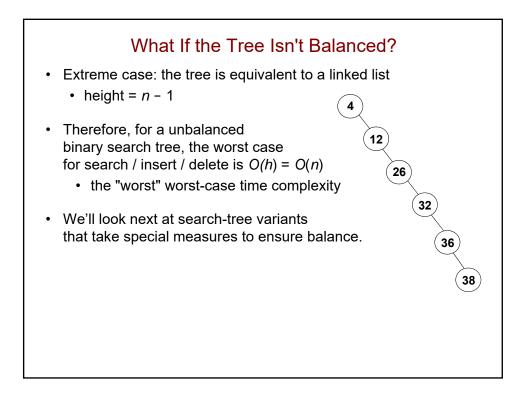


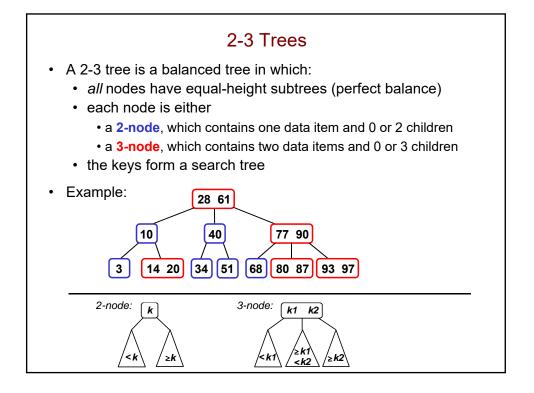


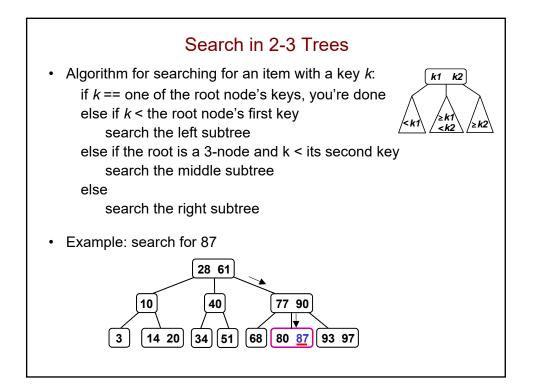


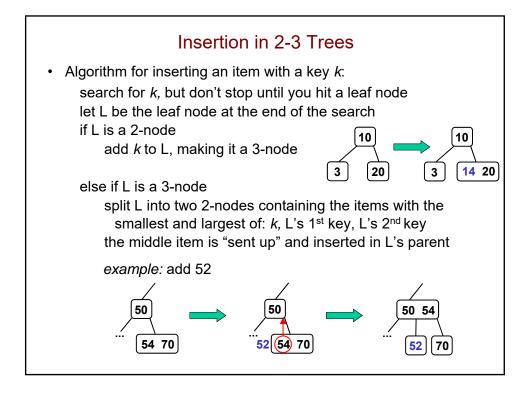


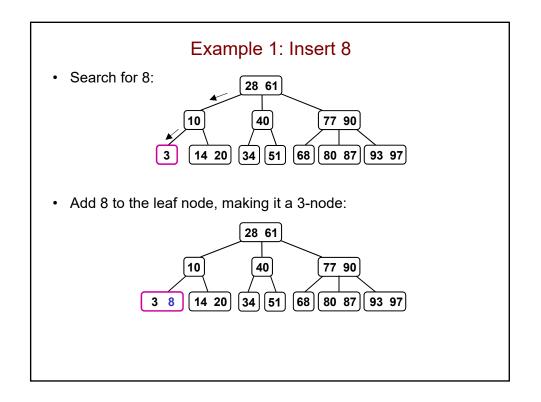


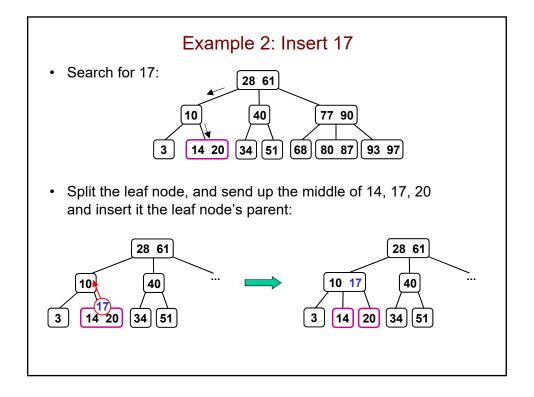


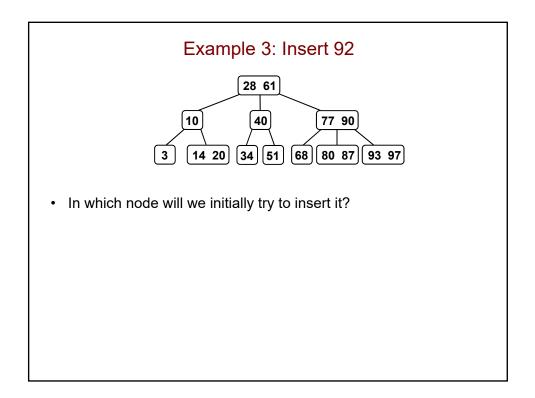


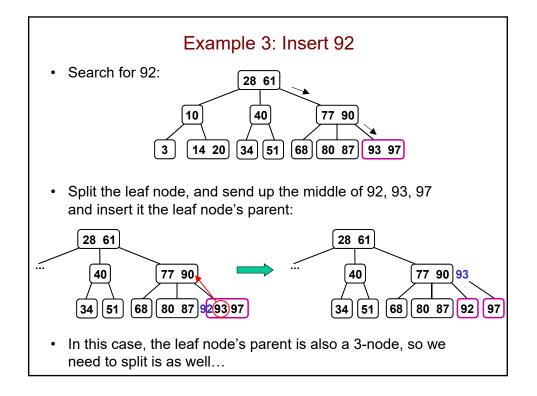


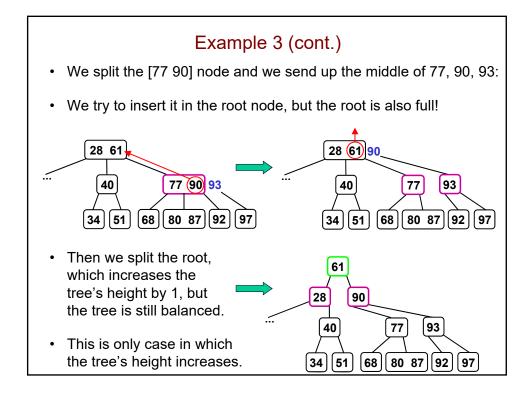


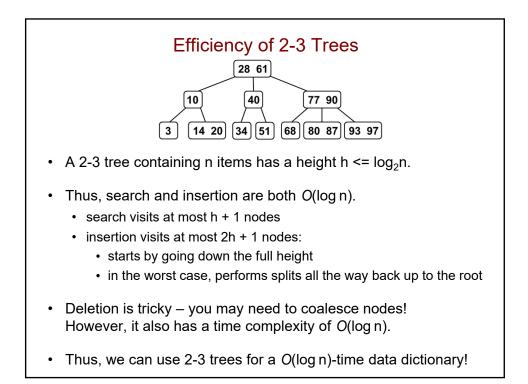


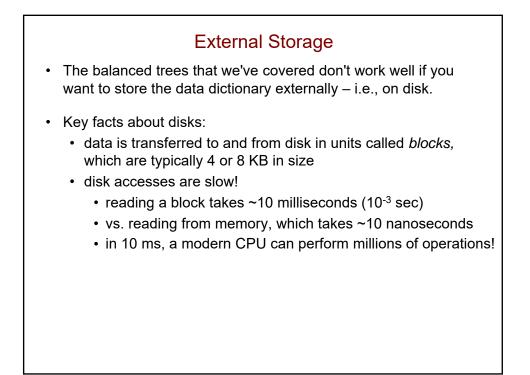






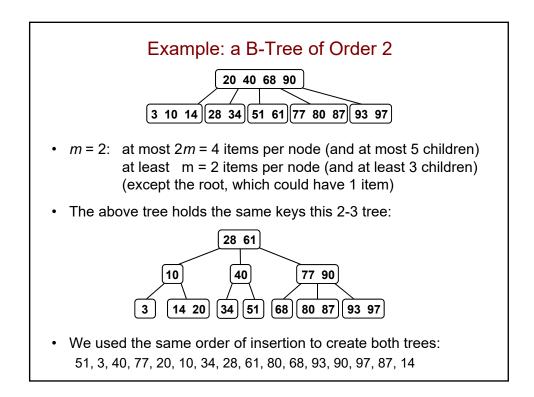


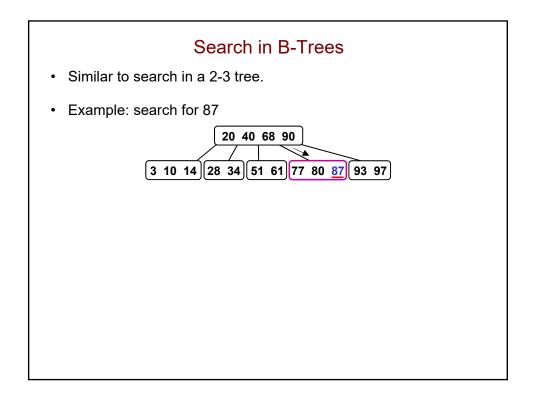


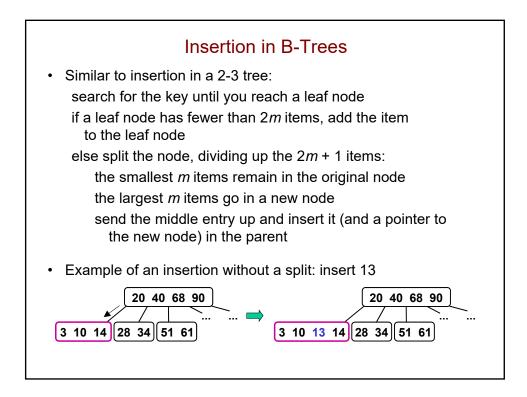


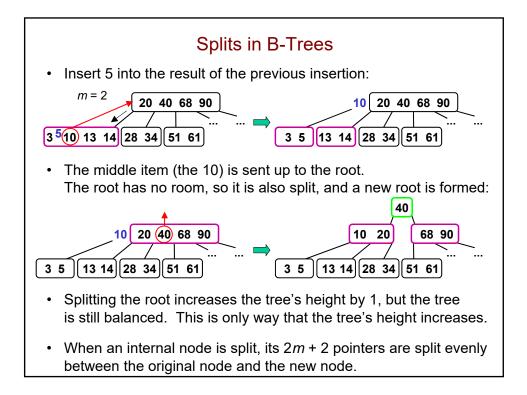
## **B-Trees**

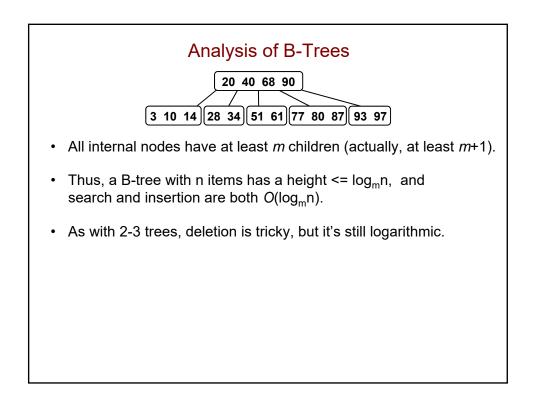
- A B-tree of order *m* is a tree in which each node has:
  - at most 2m entries (and, for internal nodes, 2m + 1 children)
  - at least *m* entries (and, for internal nodes, *m* + 1 children)
  - · exception: the root node may have as few as 1 entry
  - a 2-3 tree is essentially a B-tree of order 1
- To minimize the number of disk accesses, we make *m* as large as possible.
  - each disk read brings in more items
  - the tree will be shorter (each level has more nodes), and thus searching for an item requires fewer disk reads
- A large value of *m* doesn't make sense for a memory-only tree, because it leads to many key comparisons per node.
- These comparisons are less expensive than accessing the disk, so large values of *m* make sense for on-disk trees.











## Search Trees: Conclusions

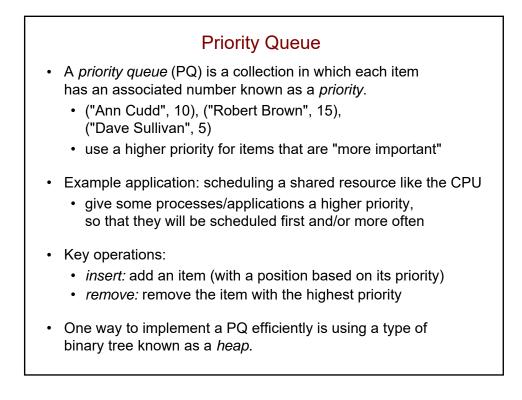
- Binary search trees can be  $O(\log n)$ , but they can degenerate to O(n) running time if they are out of balance.
- 2-3 trees and B-trees are *balanced* search trees that guarantee O(log n) performance.
- When data is stored on disk, the most important performance consideration is reducing the number of disk accesses.
- B-trees offer improved performance for on-disk data dictionaries.

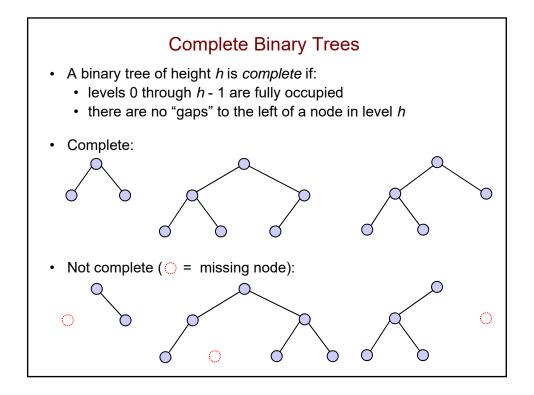


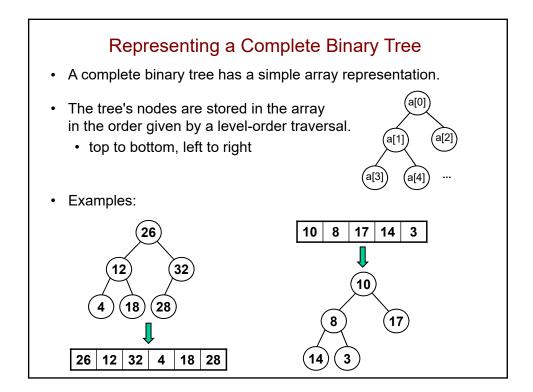
## Heaps and Priority Queues

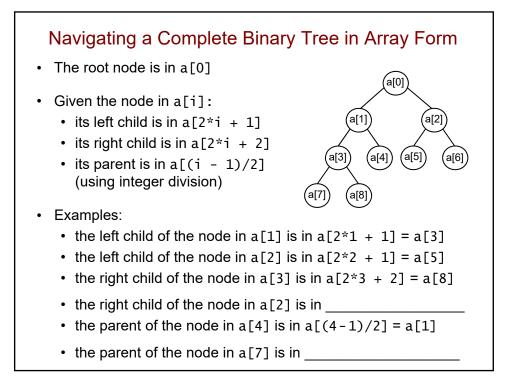
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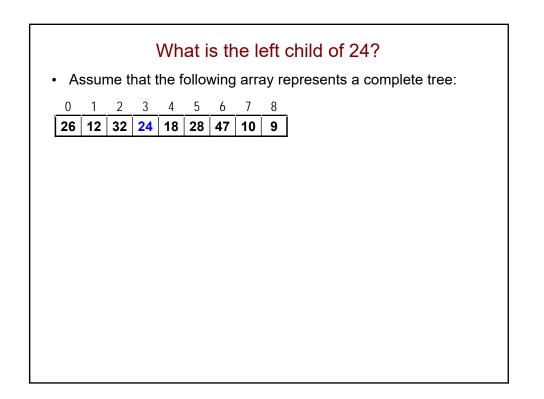
David G. Sullivan, Ph.D.

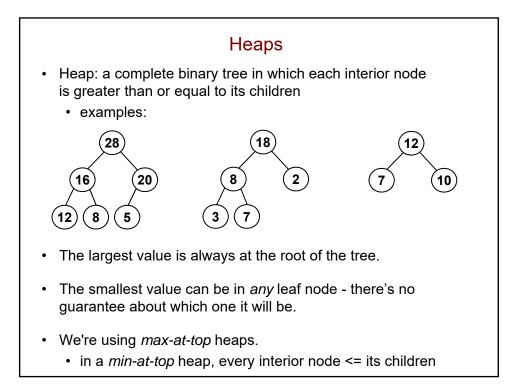


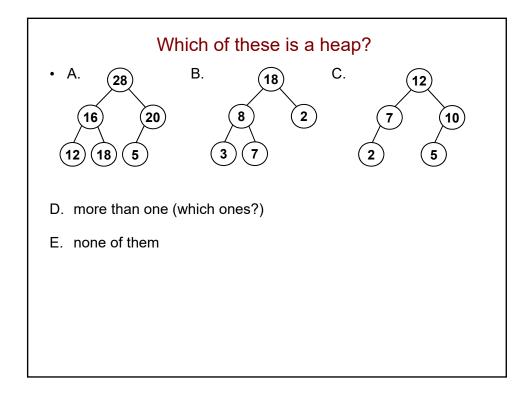


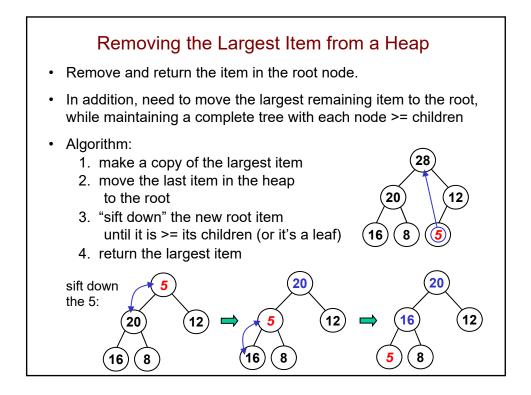


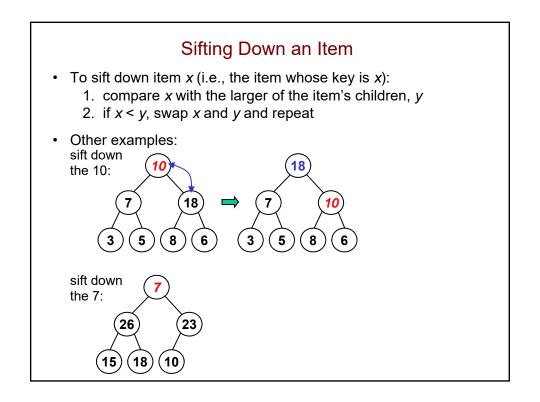


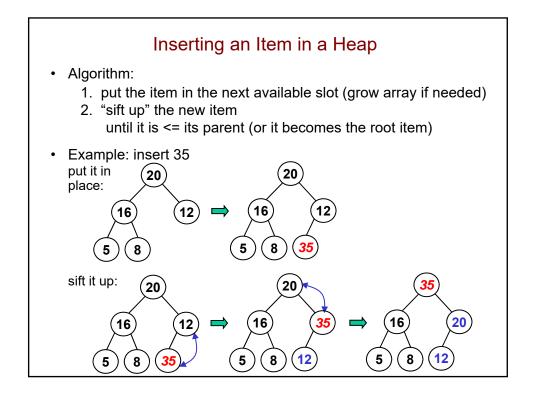


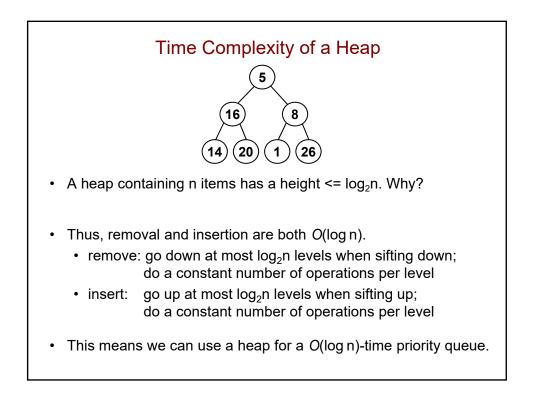


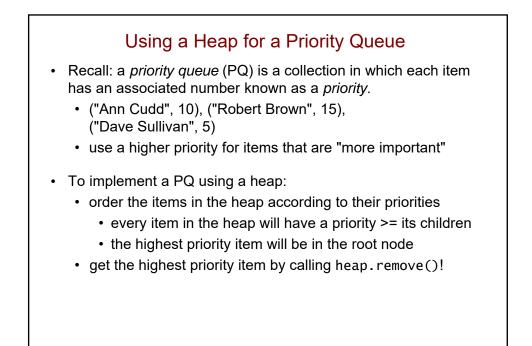




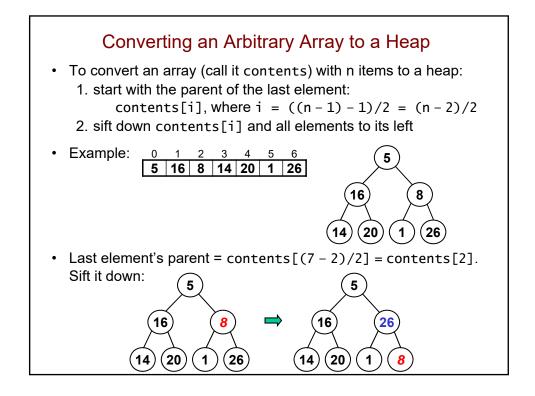


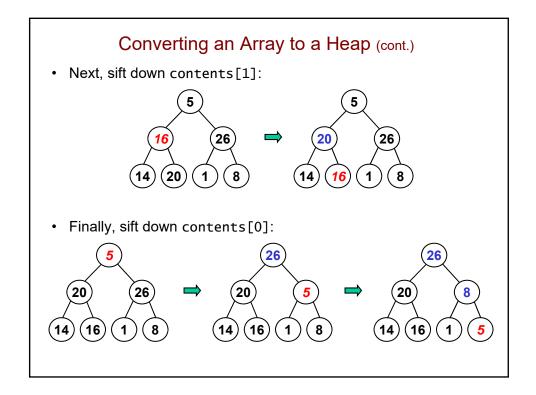






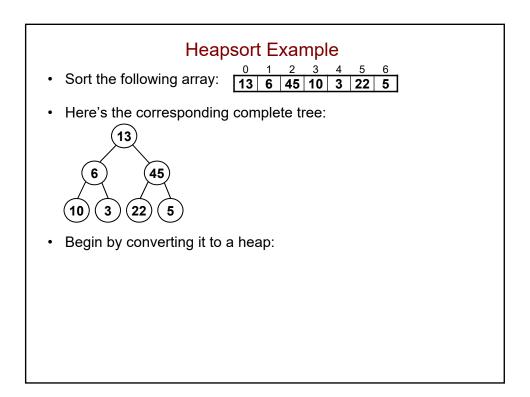
Using a Heap to Sort an Array
• Recall selection sort: it repeatedly finds the smallest remaining element and swaps it into place: 0 1 2 3 4 5 6 5 16 8 14 20 1 26 0 1 2 3 4 5 6 1 16 8 14 20 5 26 0 1 2 3 4 5 6 1 5 8 14 20 5 26
<ul> <li>It isn't efficient, because it performs a linear scan to find the smallest remaining element (<i>O</i>(n) steps per scan).</li> <li>Heapsort is a sorting algorithm that repeatedly finds the <i>largest</i> remaining element and puts it in place.</li> </ul>
<ul> <li>It <i>is</i> efficient, because it turns the array into a heap.</li> <li>it can find/remove the largest remaining in O(log n) steps!</li> </ul>

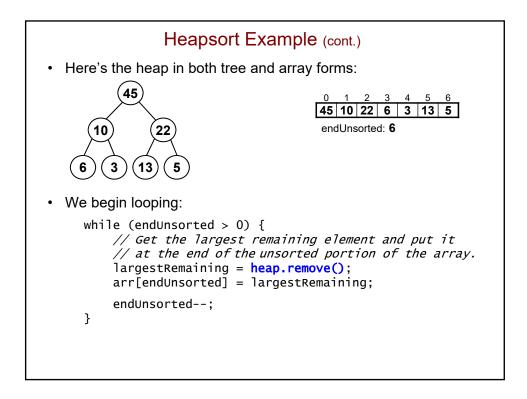


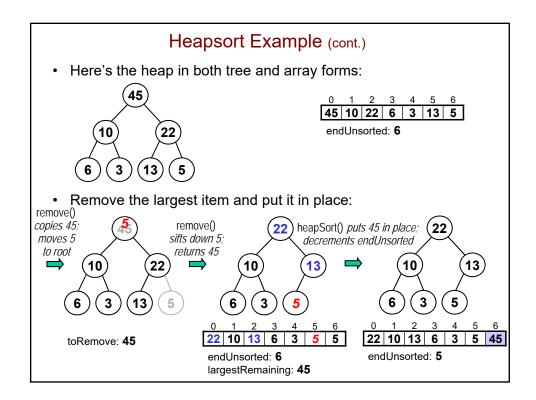


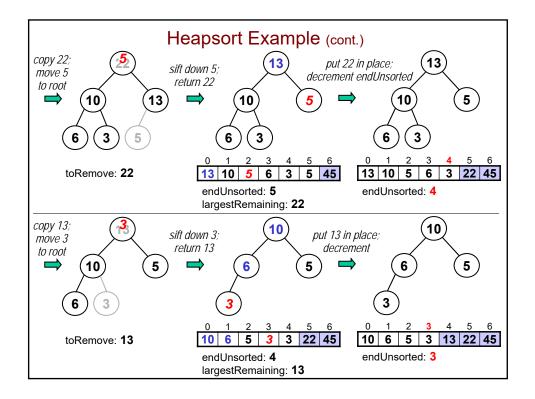
## Heapsort

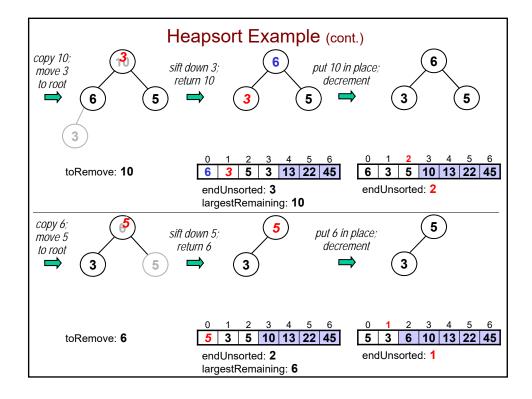
```
• Pseudocode:
heapSort(arr) {
    // Turn the array into a max-at-top heap.
heap = new Heap(arr);
    endUnsorted = arr.length - 1;
    while (endUnsorted > 0) {
        // Get the largest remaining element and put it
        // at the end of the unsorted portion of the array.
        largestRemaining = heap.remove();
        arr[endUnsorted] = largestRemaining;
        endUnsorted--;
    }
}
```

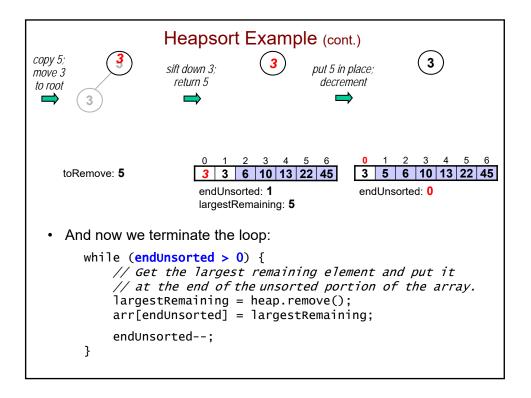


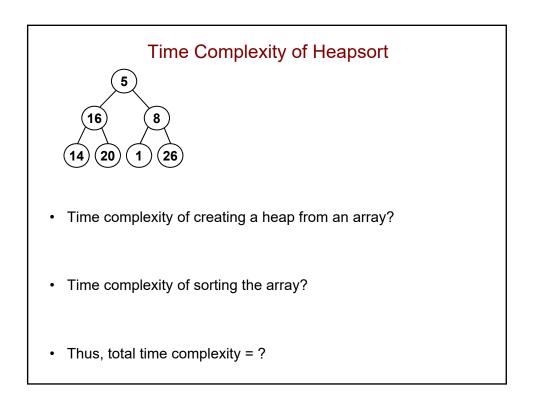










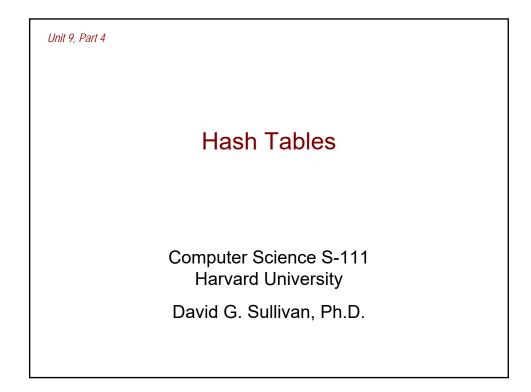


algorithm	best case	avg case	worst case	extra memory
selection sort	O(n <sup>2</sup> )	O(n <sup>2</sup> )	O(n <sup>2</sup> )	0(1)
insertion sort	0(n)	O(n <sup>2</sup> )	O(n <sup>2</sup> )	0(1)
Shell sort	O(n log n)	O(n <sup>1.5</sup> )	O(n <sup>1.5</sup> )	0(1)
bubble sort	O(n <sup>2</sup> )	O(n <sup>2</sup> )	O(n <sup>2</sup> )	0(1)
quicksort	O(n log n)	O(n log n)	O(n <sup>2</sup> )	O(log n) worst: O(n)
mergesort	O(n log n)	O(n log n)	O(nlogn)	0(n)
heapsort	O(n log n)	O(n log n)	O(nlogn)	0(1)

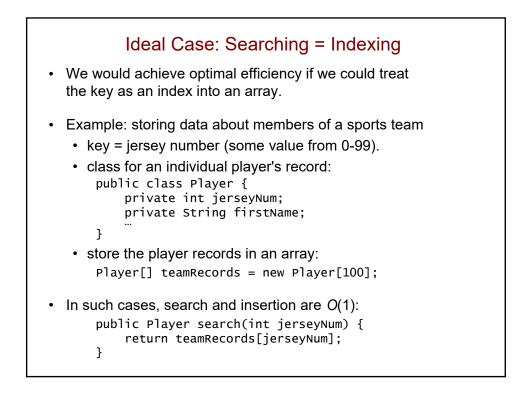
• Heapsort matches mergesort for the best worst-case time complexity, but it has better space complexity.

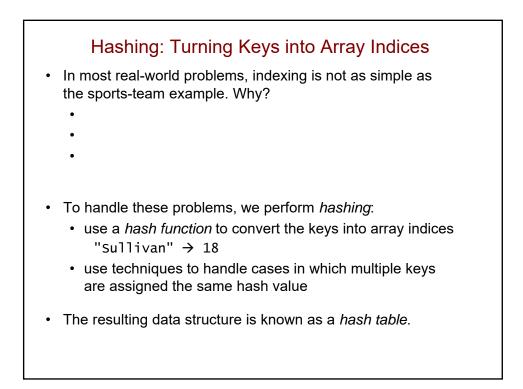
• Insertion sort is still best for arrays that are almost sorted.

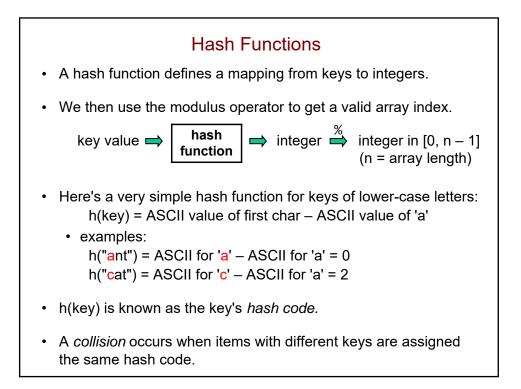
- heapsort will scramble an almost sorted array before sorting it!
- Quicksort is still typically fastest in the average case.

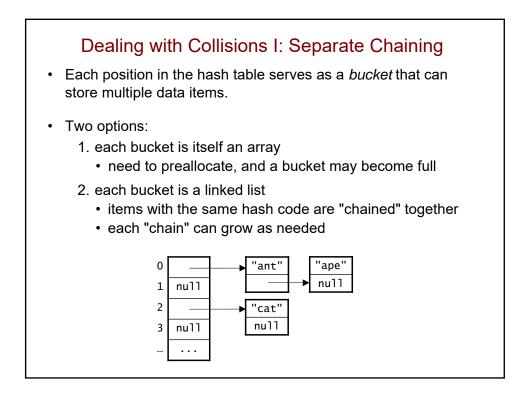


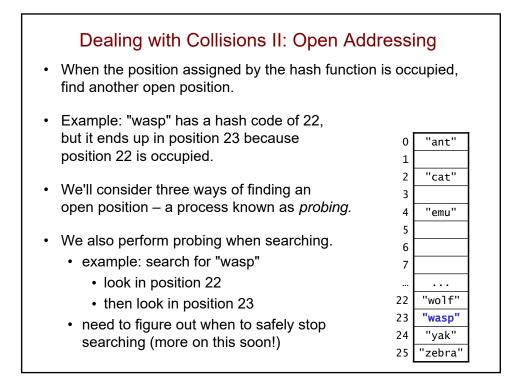
data structure	searching for an item	inserting an item
a list implemented using an array	O(log n) using binary search	<i>O</i> (n)
a list implemented using a linked list	<i>O</i> (n) using linear search	<i>O</i> (n)
binary search tree		
balanced search trees (2-3 tree, B-tree, others)		



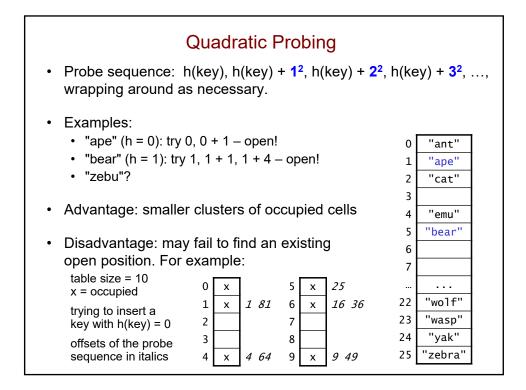




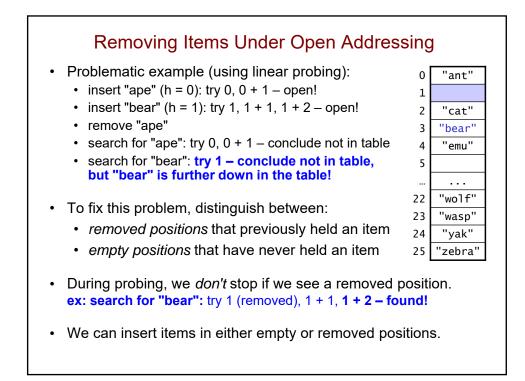


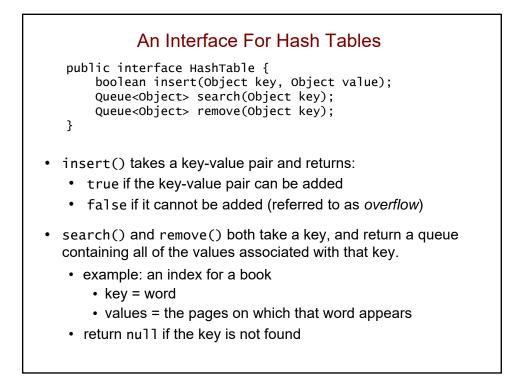


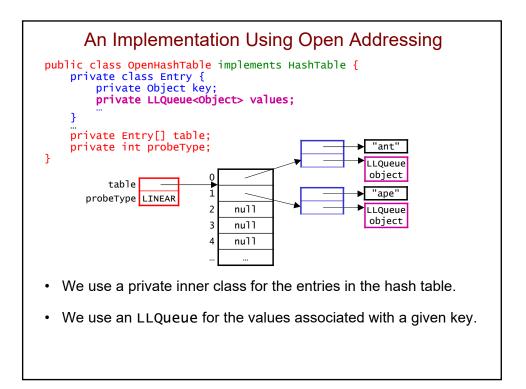
Linear Probing		
<ul> <li>Probe sequence: h(key), h(key) + 1, h(key) + 2,</li> <li>wrapping around as necessary.</li> </ul>	.,	
<ul> <li>Examples:</li> <li>"ape" (h = 0) would be placed in position 1, because position 0 is already full.</li> <li>"bear" (h = 1): try 1, 1 + 1, 1 + 2 - open!</li> <li>where would "zebu" end up?</li> </ul>	0 1 2 3 4	"ant" "ape" "cat" "bear" "emu"
<ul> <li>Advantage: if there is an open cell, linear probing will eventually find it.</li> </ul>	5 6 7	
<ul> <li>Disadvantage: get "clusters" of occupied cells that lead to longer subsequent probes.</li> <li>probe length = the number of positions considered during a probe</li> </ul>	 22 23 24 25	 "wolf" "wasp" "yak" "zebra"

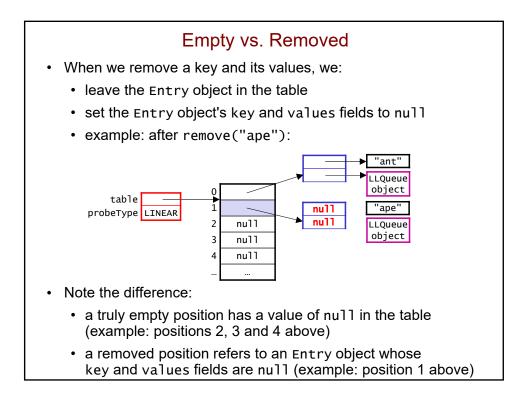


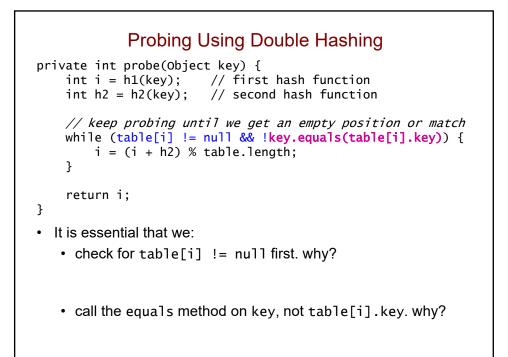
Double Hashing	
Use two hash functions:	
<ul> <li>h1 computes the hash code</li> </ul>	
<ul> <li>h2 computes the increment for probing</li> </ul>	
• probe sequence: h1, h1 + h2, h1 + 2*h2,	
	0 "ant"
• Examples:	1 "bear"
<ul> <li>h1 = our previous h</li> </ul>	2 "cat"
<ul> <li>h2 = number of characters in the string</li> </ul>	3 "ape"
<ul> <li>"ape" (h1 = 0, h2 = 3): try 0, 0 + 3 - open!</li> <li>"bear" (h1 = 1, h2 = 4): try 1 - open!</li> <li>"zebu"?</li> </ul>	4 "emu"
	5
	6
• Zebu ?	7
• Combines good features of linear and quadratic:	
<b>.</b>	22 "wolf"
reduces clustering	23 "wasp"
<ul> <li>will find an open position if there is one,</li> </ul>	24 "yak"
provided the table size is a prime number	25 "zebra"

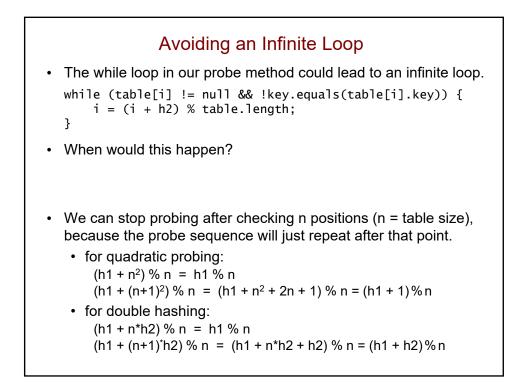










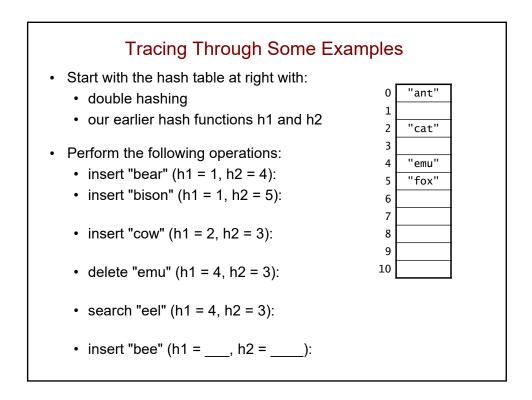


```
Avoiding an Infinite Loop (cont.)
private int probe(Object key) {
                        // first hash function
   int i = h1(key);
   int h^2 = h^2(key);
                       // second hash function
   int numChecked = 1;
   // keep probing until we get an empty position or a match
   while (table[i] != null && !key.equals(table[i].key)) {
        if (numChecked == table.length) {
            return -1;
        }
        i = (i + h2) \% table.length;
        numChecked++;
   }
   return i;
}
```

```
Search and Removal
public LLQueue<Object> search(Object key) {
    // throw an exception if key == null
    int i = probe(key);
    if (i == -1 || table[i] == null) {
        return null;
    } else {
        return table[i].values;
    }
}
public LLQueue<Object> remove(Object key) {
    // throw an exception if key == null
    int i = probe(key);
    if (i == -1 || table[i] == null) {
        return null;
    }
    LLQueue<Object> removedVals = table[i].values;
    table[i].key = null;
    table[i].values = null;
    return removedVals;
}
```

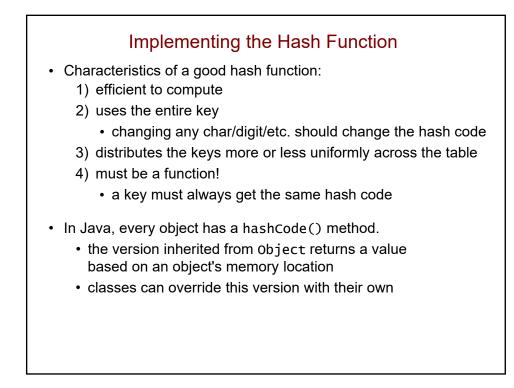
## Insertion

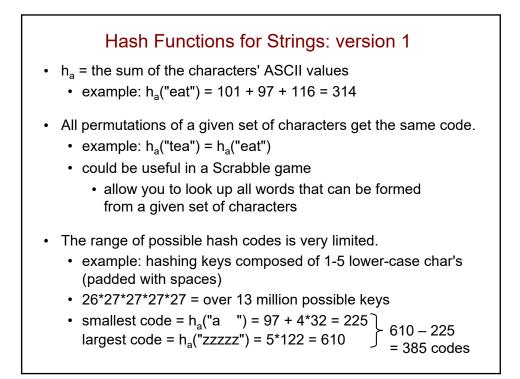
- We begin by probing for the key.
- Several cases:
  - the key is already in the table (we're inserting a duplicate)
     → add the value to the values in the key's Entry
  - 2. the key is not in the table: three subcases:
    - a. encountered 1 or more removed positions while probing
      - → put the (key, value) pair in the *first* removed position seen during probing. why?
    - b. no removed position; reached an empty position
       → put the (key, value) pair in the empty position
    - c. no removed position or empty position
       → overflow; return false

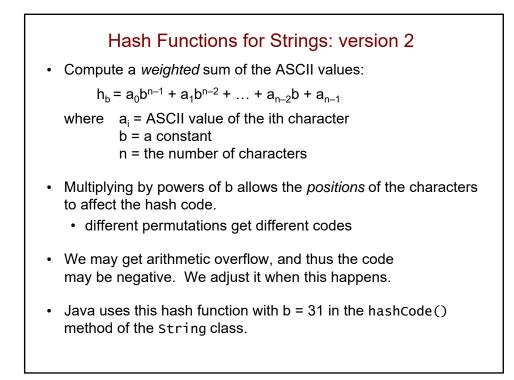


## Dealing with Overflow

- Overflow = can't find a position for an item
- When does it occur?
  - · linear probing:
  - quadratic probing:
  - double hashing:
    - if the table size is a prime number: same as linear
    - if the table size is not a prime number: same as quadratic
- To avoid overflow (and reduce search times), grow the hash table when the % of occupied positions gets too big.
  - problem: we need to rehash all of the existing items. why?

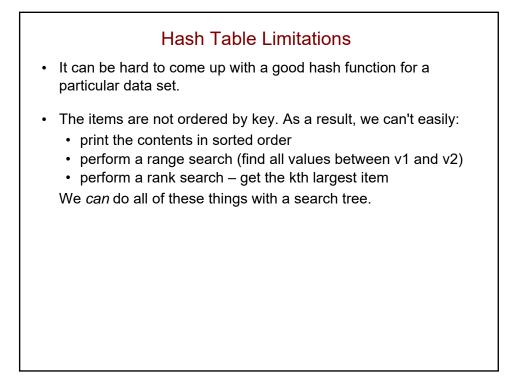


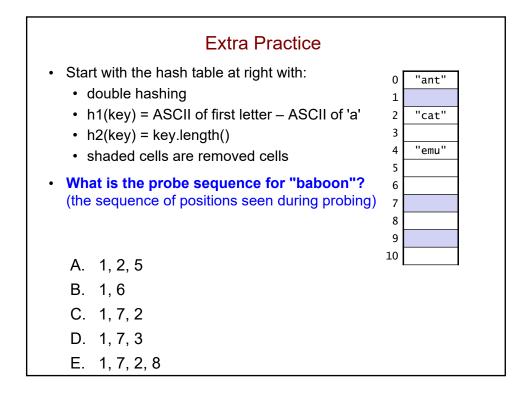


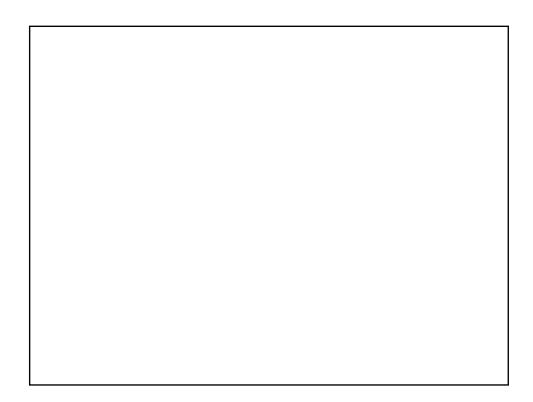


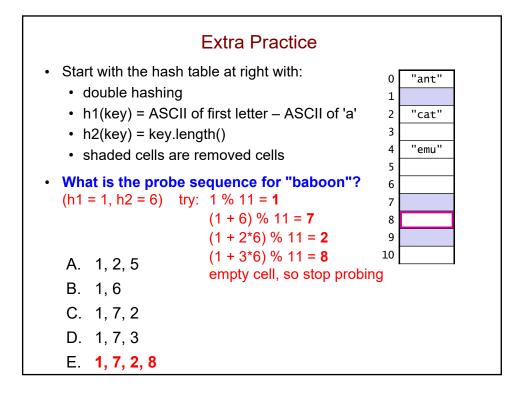
## Hash Table Efficiency

- In the best case, search and insertion are O(1).
- In the worst case, search and insertion are linear.
  - open addressing: *O*(m), where m = the size of the hash table
  - separate chaining: O(n), where n = the number of keys
- With good choices of hash function and table size, complexity is generally better than *O*(log n) and approaches *O*(1).
- *load factor* = # keys in table / size of the table.
   To prevent performance degradation:
  - open addressing: try to keep the load factor < 1/2
  - separate chaining: try to keep the load factor < 1
- Time-space tradeoff: bigger tables have better performance, but they use up more memory.

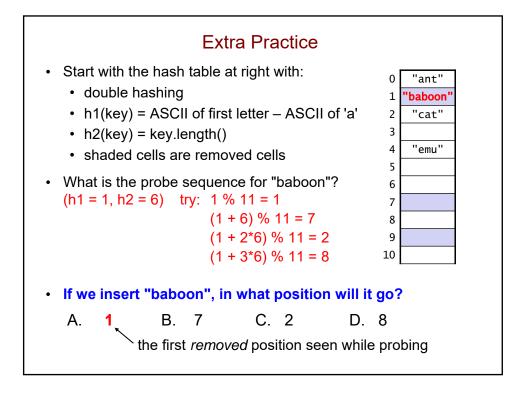


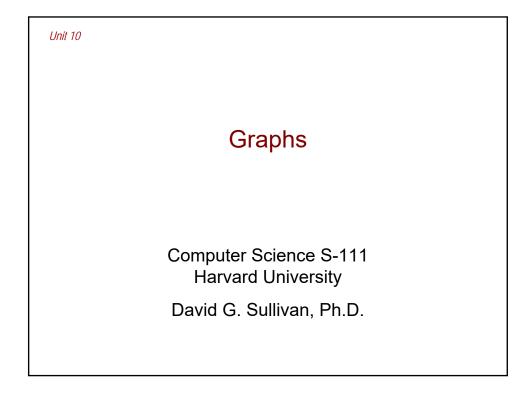


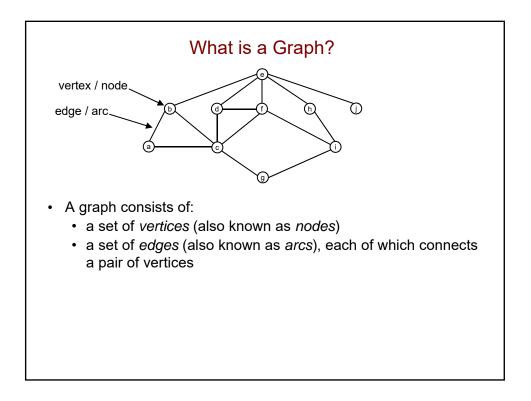


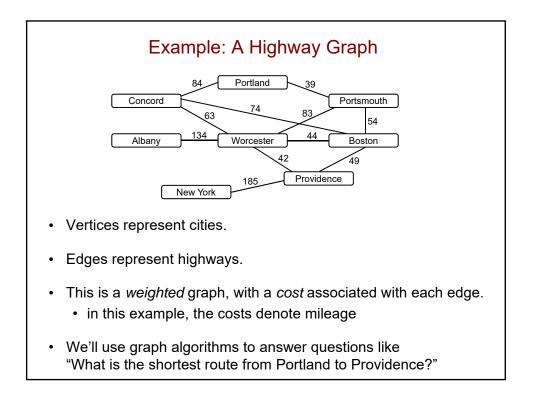


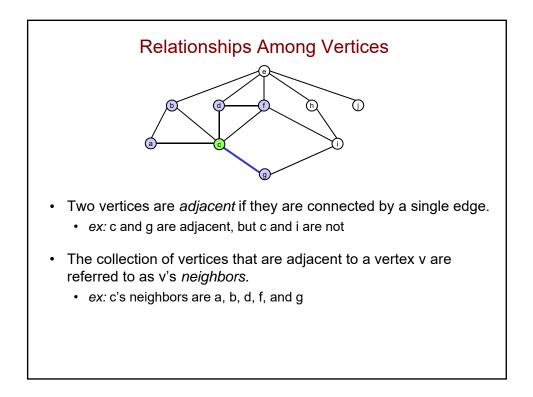
<ul> <li>Start with the hash table at right with:</li> </ul>	_	
6	0 '	'ant"
double hashing	1	
<ul> <li>h1(key) = ASCII of first letter – ASCII of 'a'</li> </ul>		'cat"
<ul> <li>h2(key) = key.length()</li> </ul>		
<ul> <li>shaded cells are removed cells</li> </ul>	4 '	'emu"
• What is the probe sequence for "baboon"?		
(h1 = 1, h2 = 6) try: 1 % 11 = 1	7	
(1 + 6) % 11 = 7	8	
(1 + 2*6) % 11 = 2	9	
(1 + 3*6) % 11 = 8	10	
If we insert "baboon", in what position will it	•	
A. 1 B. 7 C. 2 D.	8	

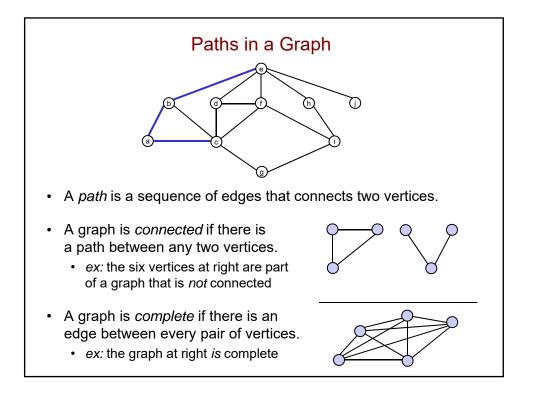


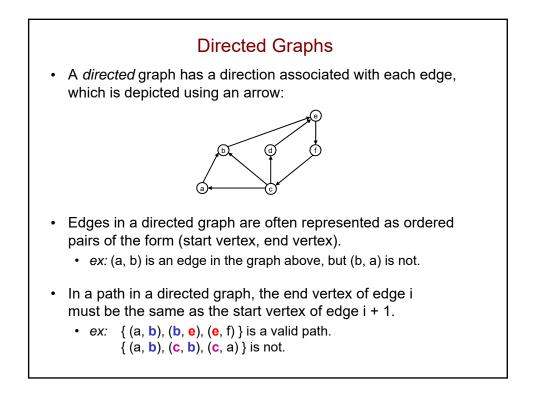


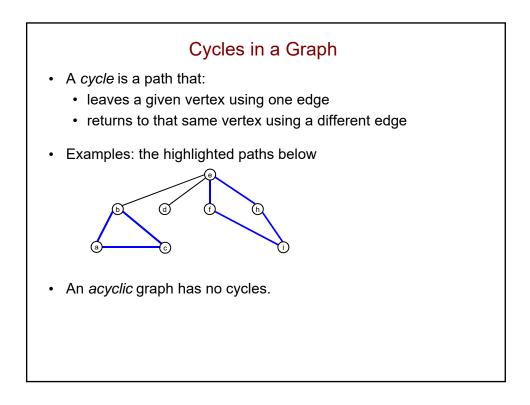


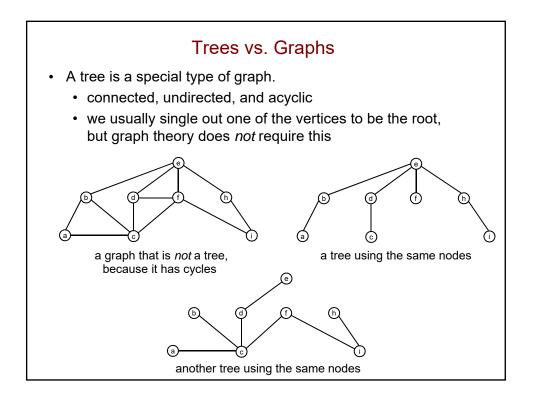


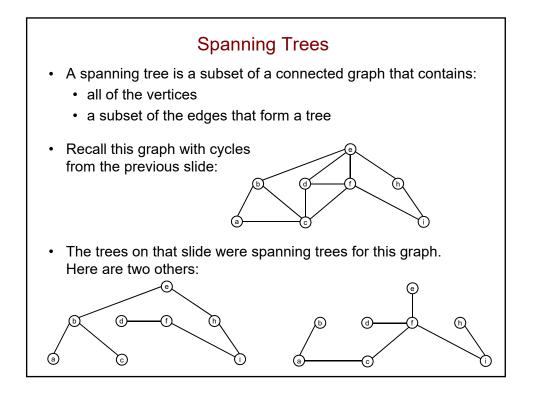


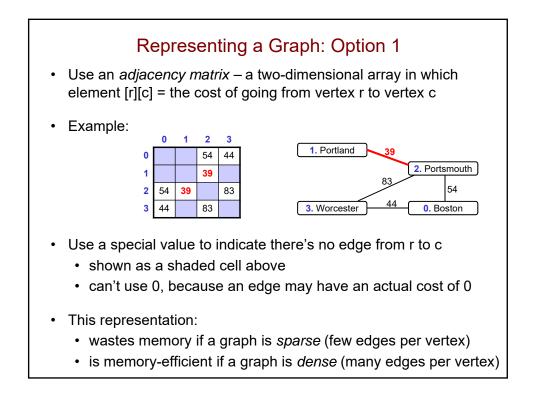


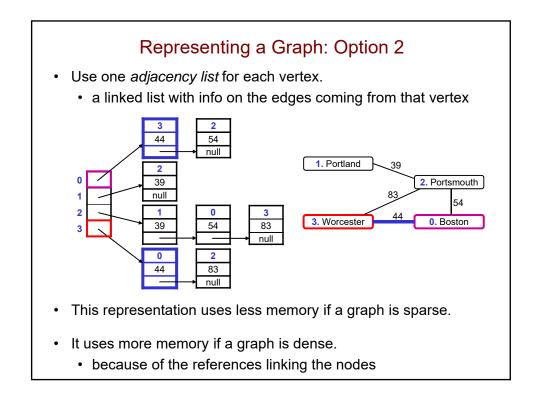


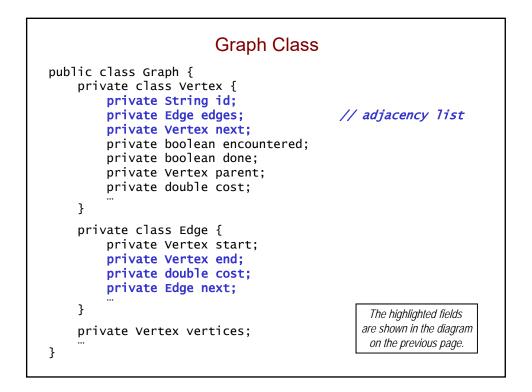


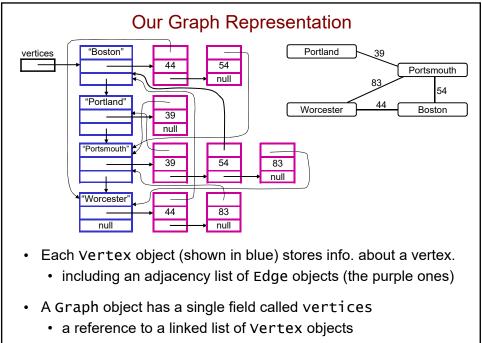




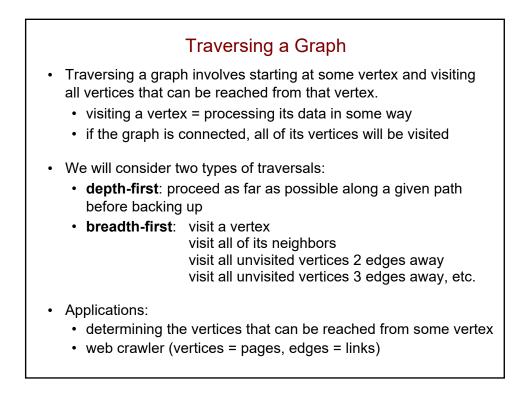


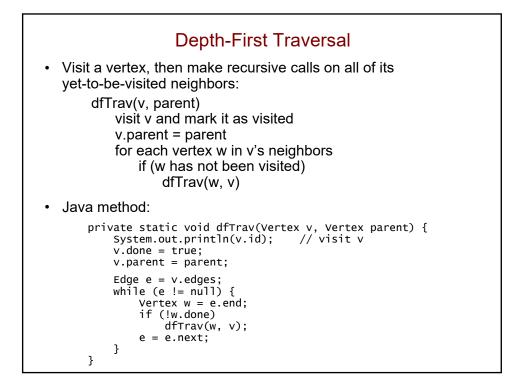


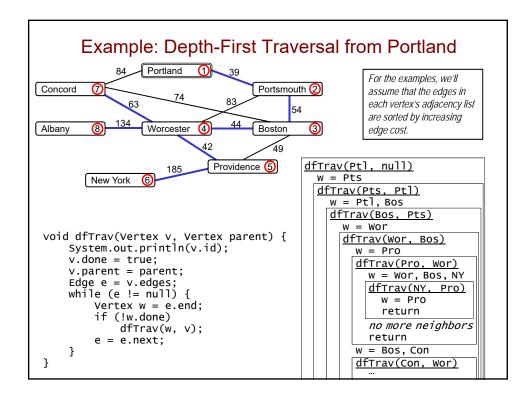


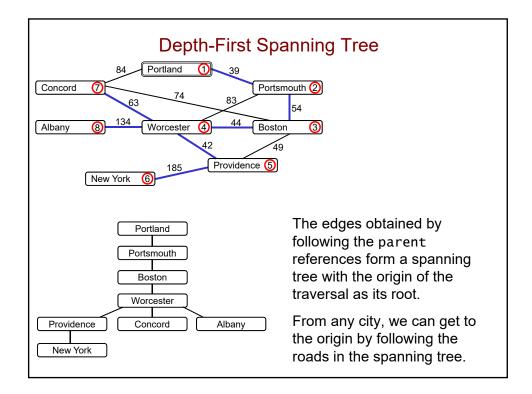


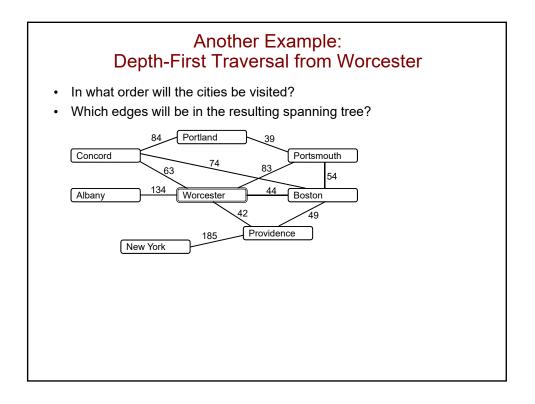
• a linked list of linked lists!

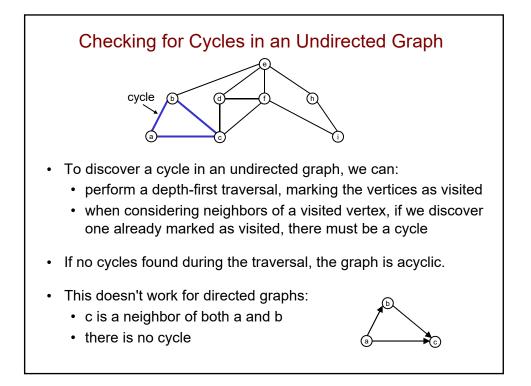




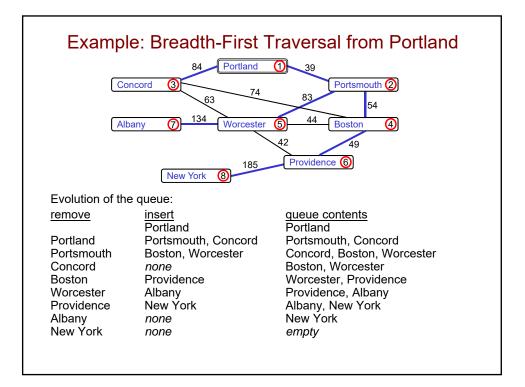


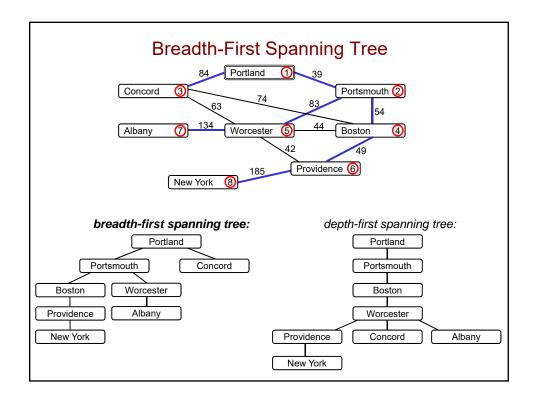


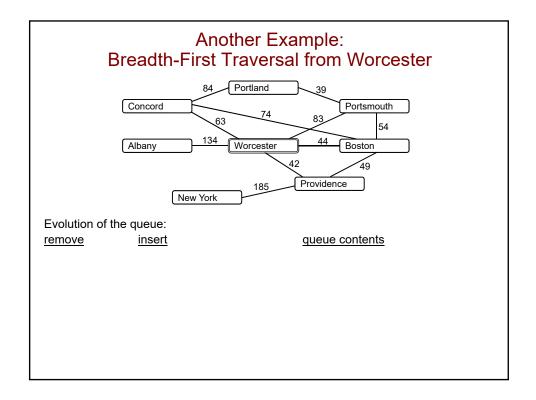


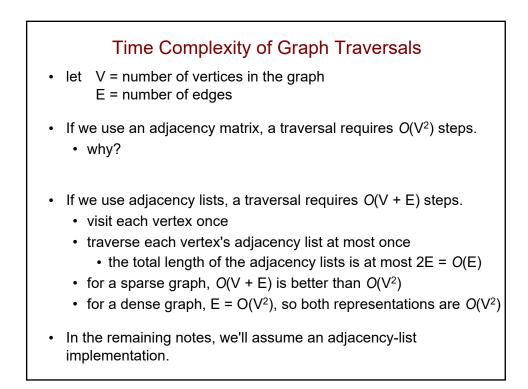


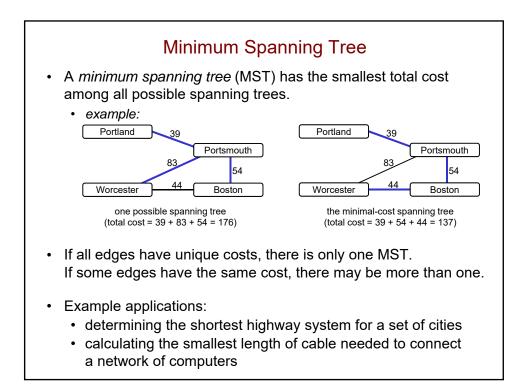
Breadth-First Traversal			
<ul> <li>Use a queue to store vertices we've seen but not yet visited: private static void bfTrav(Vertex origin) { origin.encountered = true; origin.parent = null; Queue<vertex> q = new LLQueue<vertex>(); q.insert(origin);</vertex></vertex></li> </ul>			
<pre>while (!q.isEmpty()) {     Vertex v = q.remove();     System.out.println(v.id); // Visit v.</pre>			
<pre>// Add v's unencountered neighbors to the queue. Edge e = v.edges; while (e != null) { Vertex w = e.end; if (!w.encountered) { w.encountered = true; w.parent = v; q.insert(w); } e = e.next; } </pre>			

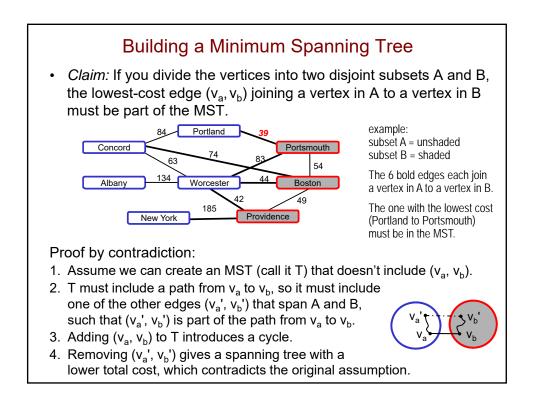


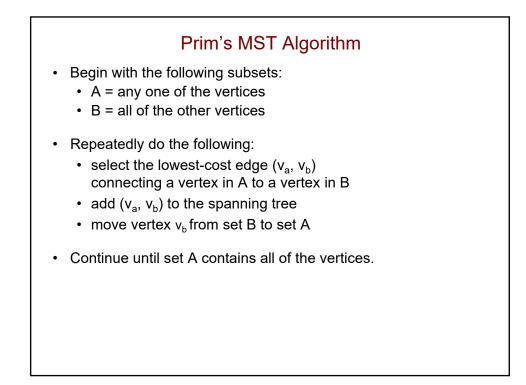


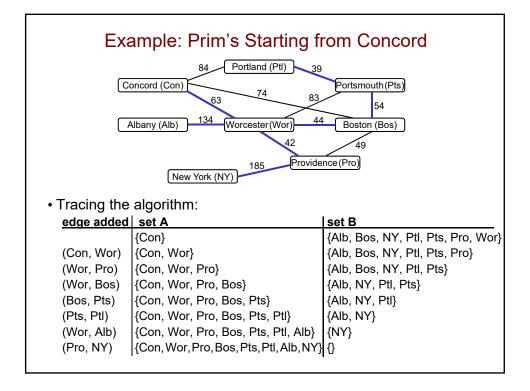


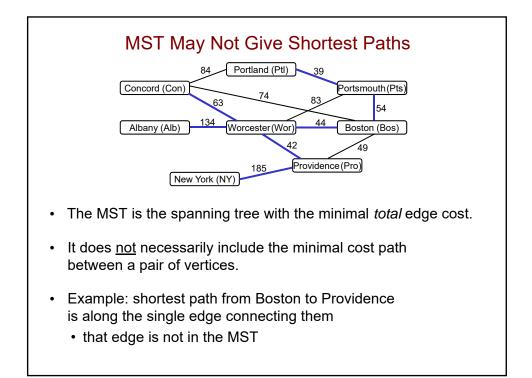


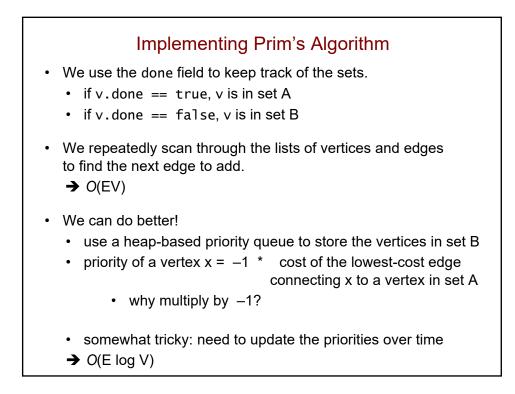






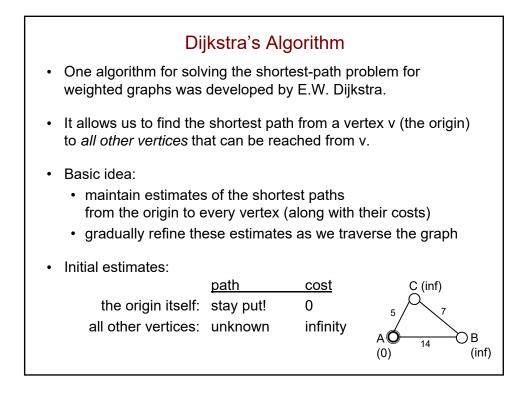


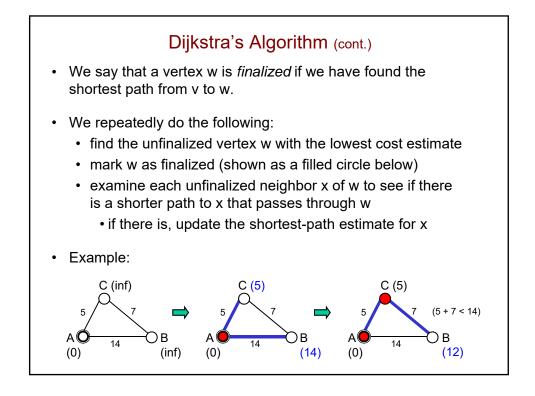


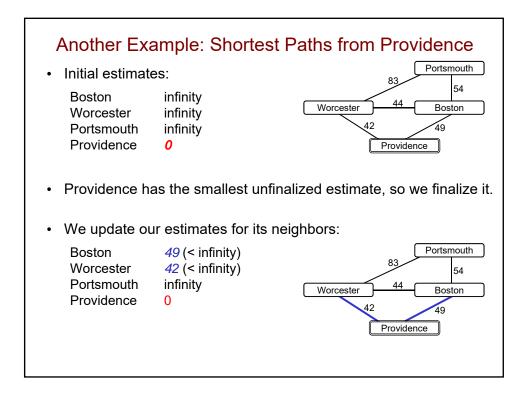


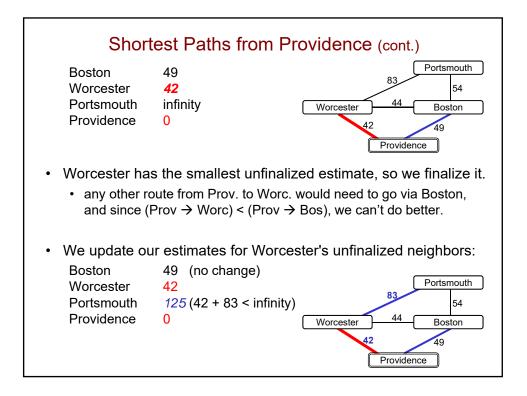
## The Shortest-Path Problem

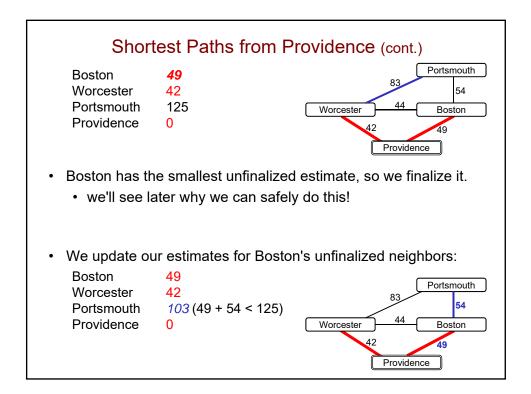
- It's often useful to know the shortest path from one vertex to another – i.e., the one with the minimal total cost
  - example application: routing traffic in the Internet
- For an *unweighted* graph, we can simply do the following:
  - start a breadth-first traversal from the origin, v
  - · stop the traversal when you reach the other vertex, w
  - the path from v to w in the resulting (possibly partial) spanning tree is a shortest path
- A breadth-first traversal works for an unweighted graph because:
  - · the shortest path is simply one with the fewest edges
  - a breadth-first traversal visits cities in order according to the number of edges they are from the origin.
- Why might this approach fail to work for a *weighted* graph?

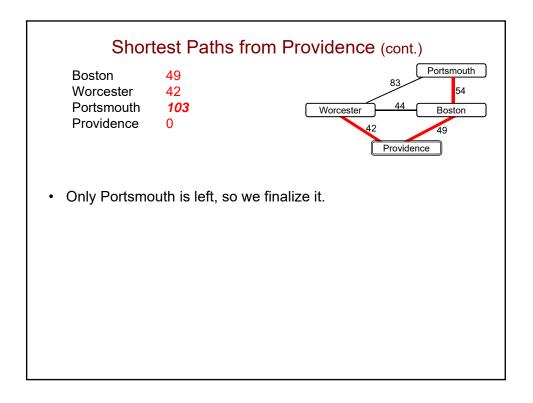


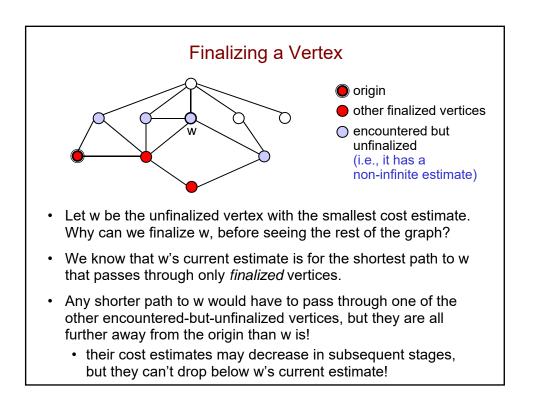


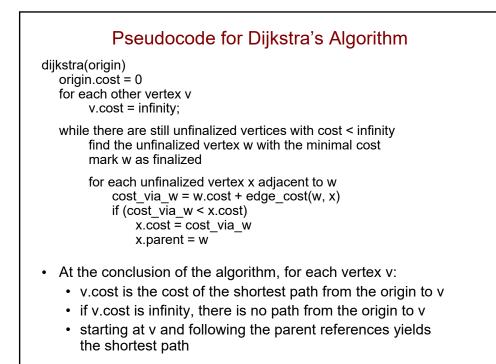


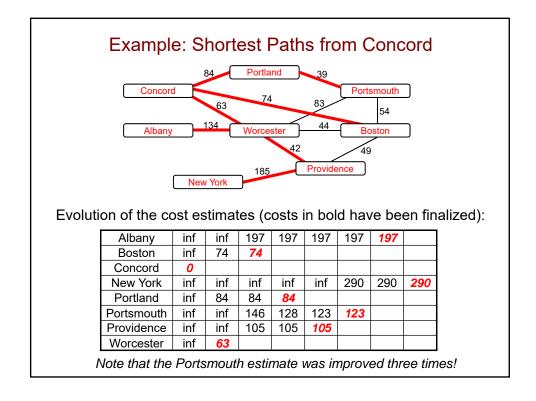


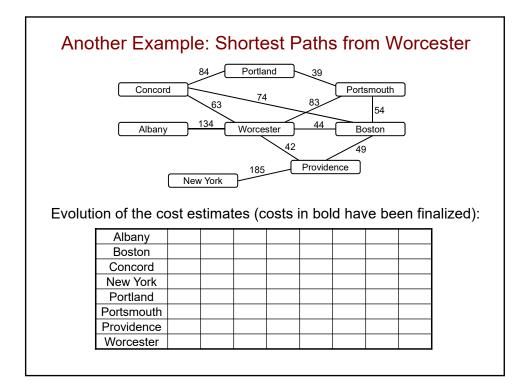


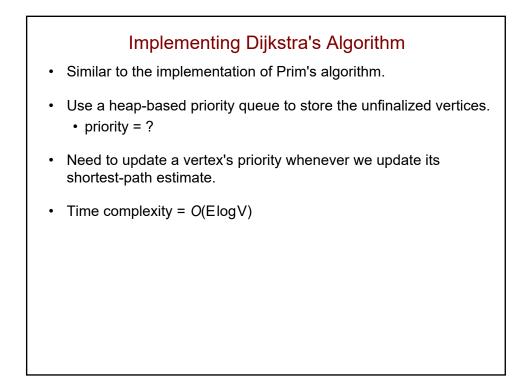


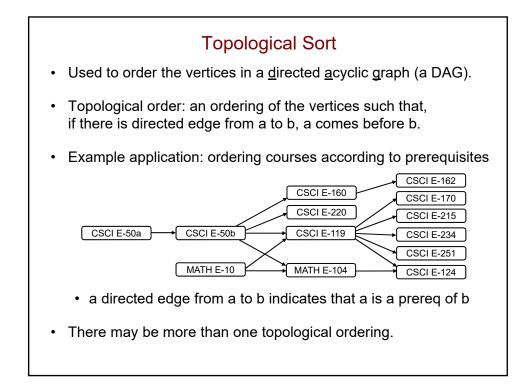


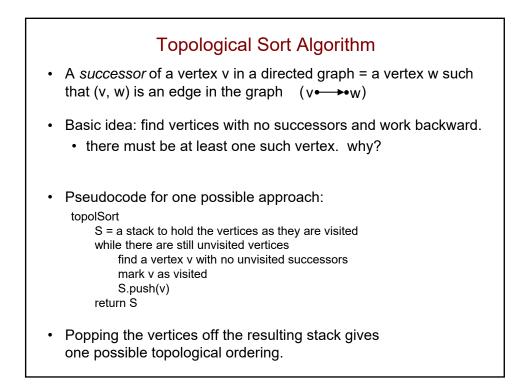


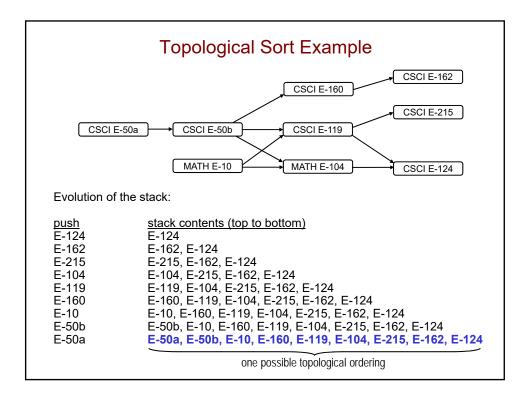


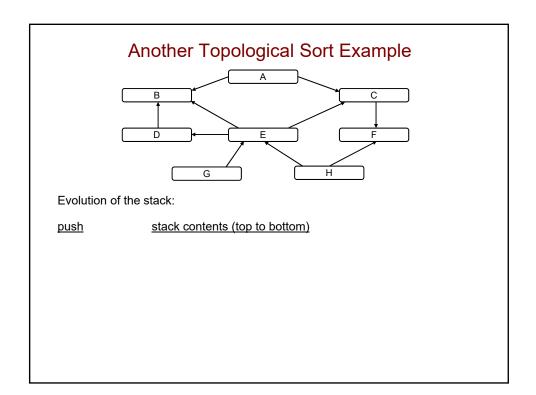


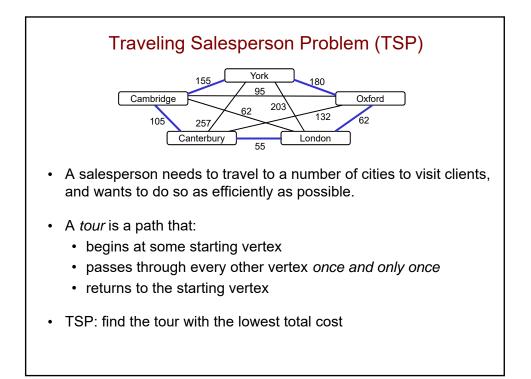


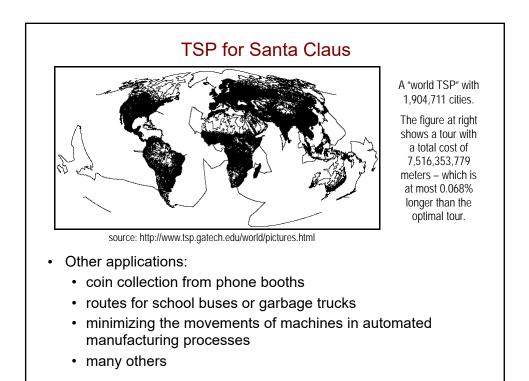


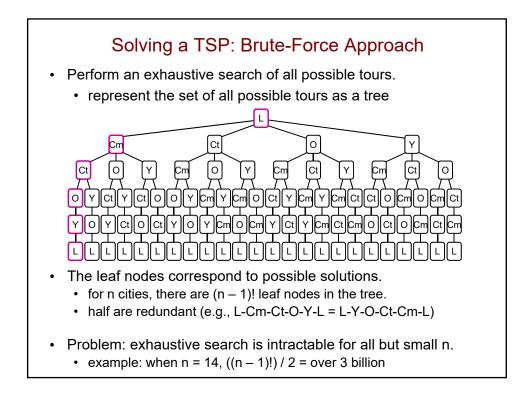


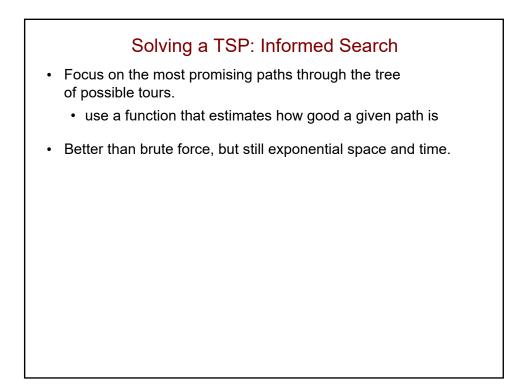


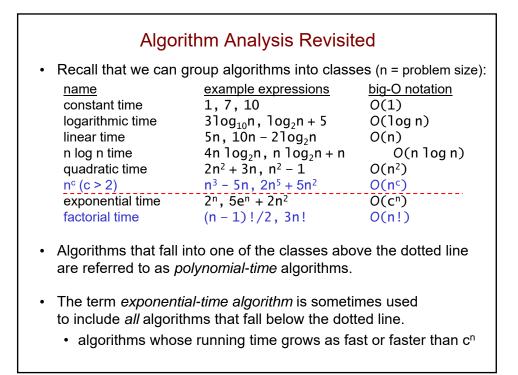












Classifying	Problem	าร	
<ul> <li>Problems that can be solved using a polynomial-time algorithm are considered "easy" problems.</li> </ul>			
<ul> <li>we can solve large problem instances in a reasonable amount of time</li> </ul>			
<ul> <li>Problems that don't have a polynomial-time solution algorithm are considered "hard" or "intractable" problems.</li> <li>they can only be solved exactly for small values of n</li> </ul>			
<ul> <li>Increasing the CPU speed doesn't help much for intractable problems:</li> </ul>			
		CPU 2	
	<u>CPU 1</u>	<u>(1000x faster)</u>	
max problem size for <i>O</i> (n) alg:	Ν	1000N	
O(n²) alg:	Ν	31.6 N	
O(2 <sup>n</sup> ) alg:	Ν	N + 9.97	

## Dealing With Intractable Problems

- When faced with an intractable problem, we resort to techniques that quickly find solutions that are "good enough".
- Such techniques are often referred to as *heuristic* techniques.
  - heuristic = rule of thumb
  - there's no guarantee these techniques will produce the optimal solution, but they typically work well

## Take-Home Lessons

- Computer science is the science of solving problems using computers.
- Java is one programming language we can use for this.
- The key concepts transcend Java:
  - · flow of control
  - · variables, data types, and expressions
  - · conditional execution
  - procedural decomposition
  - · definite and indefinite loops
  - recursion
  - console and file I/O
  - memory management (stack, heap, references)

## Take-Home Lessons (cont.)

- Object-oriented programming allows us to capture the abstractions in the programs that we write.
  - creates reusable building blocks
  - key concepts: encapsulation, inheritance, polymorphism
- Abstract data types allow us to organize and manipulate collections of data.
  - · a given ADT can be implemented in different ways
  - fundamental building blocks: arrays, linked nodes
- Efficiency matters when dealing with large collections of data.
  - some solutions can be much faster or more space efficient
  - what's the best data structure/algorithm for *your* workload?
    example: sorting an almost sorted collection

Take-Home Lessons (cont.)
<ul> <li>Use the tools in your toolbox!</li> <li>interfaces, generic data structures</li> <li>lists/stacks/queues, trees, heaps, hash tables</li> <li>recursion, recursive backtracking, divide-and-conquer</li> </ul>
<ul> <li>Use built-in/provided collections/interfaces:         <ul> <li>java.util.ArrayList<t> (implements List<t>)</t></t></li> <li>java.util.LinkedList<t> (implements List<t> and Queue<t>)</t></t></t></li> <li>java.util.Stack<t></t></li> <li>java.util.TreeMap<k, v=""> (a balanced search tree)</k,></li> <li>java.util.HashMap<k, v=""> (a hash table)</k,></li> <li>java.util.PriorityQueue<t> (a heap)</t></li> </ul> </li> </ul>
<ul> <li>But use them intelligently!</li> <li>ex: LinkedList maintains a reference to the last node in the list</li> <li>list.add(item, n) will add item to the end in O(n) time</li> <li>list.addLast(item) will add item to the end in O(1) time!</li> </ul>