## Conversions in the Metric System

The metric system is a system of measuring. It is used for three basic units of measure: metres ( m ), litres ( L ) and grams ( g ).


What makes the metric system so useful is that all three units of measure are based on the powers of ten (including $0.000001,0.001,0.01,0.1,1,10,100,1000$ ).

Let's examine the METRIC SYSTEM CONVERSION chart to understand this idea better.

| Units | kilo- | hecto- | deka | base | deci | centi- | milli- | micro |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Values | 1,000 | 100 | 10 | 1 | 0.1 | 0.01 | 0.001 | 0.000001 |
| Prefix | k- | h - | da- | $\begin{aligned} & \hline \mathrm{m} \\ & \mathrm{~g} \\ & \mathrm{~L} \end{aligned}$ | d- | c- | m- | mc- or $\mu$ - |
| Values (compa red to base) | 1000x <br> bigger | 100x <br> bigger | 10x bigger | 1 | $\begin{gathered} \text { 10x } \\ \text { smaller } \end{gathered}$ | $\begin{gathered} \text { 100x } \\ \text { smaller } \end{gathered}$ | 1000x smaller | $\begin{aligned} & 1,000,000 \\ & \text { x smaller } \end{aligned}$ |

In this chart, the metre (m), gram (g), and litre (L) have a value of 1 . Units of measurement to the right of the base unit are becoming smaller and smaller. Units of measure to the left of the base unit are becoming larger and larger.

For example, given a metre we notice the following unit conversions to the right of the base unit:

| There are $\mathbf{1 0} \mathbf{d m}$ in a |  |  |
| :--- | :--- | :--- |
| metre, | There are $\mathbf{1 0 0} \mathbf{c m}$ in a | There are $\mathbf{1 0 0 0} \mathbf{~ m m ~ i n ~ a ~}$ |
| metre, |  |  |
| Thus, $1 \mathrm{dm}=1 / 10 \mathrm{~m}=$ | Thus, $1 \mathrm{~cm}=1 / 100 \mathrm{~m}=$ | Thus, $1 \mathrm{~mm}=1 / 1000 \mathrm{~m}=$ |
| 0.1 m | 0.01 m | 0.001 m |



Since the metric system of measurement is based on powers of ten (10) converting between units is a snap!

PART A - Ratio \& Proportion Method
Example 1: Convert 1.74 m into cm .
To convert meters to centimeters we need to first identify the larger unit. Looking at the Metric System chart we notice that a centimeter is 100 times smaller than a meter.

$$
\text { Thus, } 1 \mathrm{~m}=100 \mathrm{~cm}
$$

Knowing this we can set up a proportion to convert 1.74 m into cm .
Remember! A proportion is a comparison of two equal ratios in which order matters.
On the Left Hand Side (L.H.S.) of the proportion, list the ratio we know. On the Right Hand Side (R.H.S), list the ratio we are trying to find out. Solve for the unknown value using cross multiplication.

$$
\begin{gathered}
\frac{m}{c m}=\frac{m}{c m} \\
\frac{1 m}{100 c m} \frac{1.74 \mathrm{~m}}{x c m} \\
1(x)=1.74(100) \\
x=174 \mathrm{~cm}
\end{gathered}
$$

Thus, there are 174 cm in 1.74 m .

## Conversions in the Metric System

Example 2: Convert 4 g into mg .
First we need to identify the larger unit. Looking at the Metric System Chart we notice that a milligram is 1000 times smaller than a gram.

$$
\text { Thus, } 1 \mathrm{~g}=1000 \mathrm{mg} \text {. }
$$

Knowing this we can set up a proportion to convert 4 g into mg .
On the Left Hand Side (L.H.S.) of the proportion, list the ratio we know. On the Right Hand Side (R.H.S), list the ratio we are trying to find out. Solve for the unknown value using cross multiplication.

$$
\begin{gathered}
\frac{g}{m g}=\frac{g}{m g} \\
\frac{1 g \pi}{1000 \mathrm{mg}}=\lambda \frac{4 g}{x m g} \\
1(x)=4(1000) \\
x=4000 \mathrm{mg}
\end{gathered}
$$

Thus, there are 4000 mg in 4 g .

PART B - Ladder Method


Note: When moving down the stairs we are multiplying by 10, 100, 1000 or 1000000. When moving up the stairs we are dividing by 10,100, 1000 , or 1000000.

Example 3: Convert 0.0254 L into mL .


Beginning at the base unit litre (L), we have to take three steps DOWN the stairs to reach milliliters (mL).

Thus, we will multiply 0.0254 by 1000 by moving the decimal point three spaces to the right.

$$
0.0254 \times 1000=0.025 .4
$$

Thus, there are 25.4 mL in 0.0254 L .
Example 4: Convert 35809.2 mg into kg .
Beginning at milligrams (mg), we have to take six steps up the stairs to reach kilograms (kg).

Thus, we will divide 35809.2 mg by 1000000 by moving the decimal point six spaces to the left.

$$
35809.2 \div 1000000=\sim^{5} \underbrace{0.9} \cdot 2
$$

Thus, there is 0.0358092 kg in 35809.2 mg .
Notice that both starting units ( mm and cm ) cancel out and you are left with the desired unit (dm).

## Exercises:

1. Convert the following larger units of the Metric System to the equivalent smaller units.
a) $5 \mathrm{~g}=$
mg
f) $1 \mathrm{~g}=$
mg
b) $2 L=$
mL
g) $54 \mathrm{~g}=$
mg
c) $3.5 \mathrm{~g}=$
mg
h) $2.5 \mathrm{~L}=$
mL
d) $0.03 \mathrm{~g}=$
mg
i) $3.6 \mathrm{~cm}=$
mm
e) $0.002 \mathrm{~L}=$
mL
j) $18 \mathrm{~cm}=$
mm
2. Convert the following smaller units of the Metric System to the equivalent larger units.
a) $610 \mathrm{~mL}=$
L
f) $90 \mathrm{mg}=$
g
b) $306 \mathrm{~mm}=$
cm
g) $115 \mathrm{~mL}=$
L
c) $1520 \mathrm{~g}=$
kg
h) $68 \mathrm{~mL}=$
i) $110 \mathrm{mg}=\quad \mathrm{g}$
d) $890 \mathrm{mg}=\mathrm{g}$
j) $500 \mathrm{mg}=\quad \mathrm{g}$
e) $2500 \mathrm{~mL}=$
L

## Solutions:

1. a) $5 \mathrm{~g}=5000 \mathrm{mg}$
b) $2 \mathrm{~L}=2000 \mathrm{~mL}$
c) $3.5 \mathrm{~g}=3500 \mathrm{mg}$
d) $0.03 \mathrm{~g}=30 \mathrm{mg}$
e) $0.002 \mathrm{~L}=2 \mathrm{~mL}$
2. a) $610 \mathrm{~mL}=0.61 \mathrm{~L}$
b) $306 \mathrm{~mm}=30.6 \mathrm{~cm}$
c) $\quad 1520 \mathrm{~g}=1.52 \mathrm{~kg}$
d) $890 \mathrm{mg}=0.89 \mathrm{~g}$
e) $2500 \mathrm{~mL}=2.5 \mathrm{~L}$
f) $1 \mathrm{~g}=1000 \mathrm{mg}$
g) $54 \mathrm{~g}=54000 \mathrm{mg}$
h) $2.5 \mathrm{~L}=2500 \mathrm{~mL}$
i) $3.6 \mathrm{~cm}=36 \quad \mathrm{~mm}$
j) $18 \mathrm{~cm}=180 \mathrm{~mm}$
f) $\quad 90 \mathrm{mg}=0.09 \mathrm{~g}$
g) $115 \mathrm{~mL}=0.115 \mathrm{~L}$
h) $68 \mathrm{~mL}=0.068 \mathrm{~L}$
i) $110 \mathrm{mg}=0.11 \mathrm{~g}$
j) $500 \mathrm{mg}=0.5 \mathrm{~g}$
