## COST VOLUME PROFIT

## Key Topics to Know

- CVP analysis is based on the interactions among the following five elements:
- Price or revenue of products
- Volume or level of activity
- Per units variable costs
- Total fixed costs.
- Mix of products sold (CVP analysis requires an assumption about sales mix)
- Contribution Margin
- Difference between gross margin and contribution margin
- Understand the relationship among:

Revenue, variable cost and contribution margin per unit Why fixed costs and operating income per unit are never used. Total revenue, variable cost, contribution margin and fixed costs Level of activity versus number of units sold

- Contribution Margin is the remaining amount of sales dollars available to cover fixed expenses and profit.
- Contribution Margin in Dollars = Sales Revenue - Variable Expenses.
- Contribution Margin per unit = Selling Price per unit - Variable Expense per unit or total contribution margin / units sold
- Contribution Margin Ratio (\%) = Contribution Margin / Sales
- Break-Even Point
- At the Break-even Point:
- Profit or operating income equals 0 .
- Total revenue equals total costs.
- Total contribution margin equals fixed expenses.
- The break-even point is measured in sales dollars and/or units sold.
- Break-even sales and units sold are related by the unit selling price.
- The break-even point may be calculated using either the Equation Method or the Contribution Margin Method:


## Equation Method :

In Units Sold:
sales \$ per unit X units sold = variable expense \$ per unit $X$ units sold + fixed expenses + profit of 0

## In Sales Dollars:

sales as a \% of sales = variable expenses as a \% of sales + fixed expenses + profit of 0

## Contribution Margin Method:

## In Units Sold:

In Sales Dollars:
(Fixed Expenses + Profit of 0) Contribution Margin per unit

Fixed expenses + Profit of 0 ) Contribution Margin ratio

- Calculate the break-even point in total sales dollars and total units sold for both single-product and multi-product companies. Sales mix, the relative combination in which a company's products are sold, is assumed to be constant for these companies.
- Breakeven point for multi-product companies is calculated based on total company sales, variable costs and fixed costs.
- Sales mix, the proportion of units sold for each product to the total units sold is assumed to remain constant.
- Changes in sales volume are assumed to increase or decrease according to the sales mix. That is, the change in total units sold is made up of changes in units sold for the individual products in proportion to the sales mix.
- Calculate the sales dollars and units sold necessary to achieve a target profit using the break-even formulas above and substituting the target profit for the breakeven profit of 0 .
- Understand how the revenue function, variable, fixed and total cost functions and the break-even point shift on the CVP graph when revenue and/or cost assumptions are changed
- Calculate the margin of safety. Margin of Safety is the excess of budgeted or actual sales over the break-even volume of sales.
- Margin of safety in dollars = Total sales - Break-even sales
- Margin of safety percentage = Margin of safety in dollars / Total sales
- Calculate the degree of leverage (leverage factor)
- Operating Leverage is a way to measure, at a given level of sales, how a percentage change in sales volume will affect profits.
- Use the leverage factor to calculate the percent change in operating income for given a percent change in sales
- Explain how leverage changes when sales increase or decrease.
- Degree of operating leverage = Contribution margin / Net income


## Problems

## Problem \#1

The Berman Company manufactures and sells a single product. The company's sales and expenses for last month were:

|  | $\underline{\text { Total }}$ | Per Unit | Percentage |
| :--- | ---: | ---: | ---: |
| Sales | $\$ 500,000$ | $\$ 25$ | $100 \%$ |
| Less: Variable expenses | $\underline{200,000}$ | $\underline{10}$ | $\underline{40 \%}$ |
| Contribution margin | 300,000 | 15 | $60 \%$ |
| Less: Fixed expenses | $\underline{270,000}$ |  |  |
| Net income | $\$ 30,000$ |  |  |

Required: a) Calculate the monthly break-even point in units sold and in sales dollars.

- using the equation method
- using the contribution margin method
- verify the answer by preparing a contribution income statement
b) Without any computations, what is the contribution margin at the break-even point?
c) How many units would have to be sold each month to earn a minimum target net income of $\$ 60,000$ ?
d) Verify the answer by preparing a contribution income statement at the target level of sales.
e) Refer to the original data above. Compute the company's margin of safety in both dollars and percentage.
f) Refer to the original data above.
- What is the company's Contribution Margin Ratio?
- If monthly sales increase by $\$ 25,000$ and there is no change in fixed expenses, by how much would net income be expected to increase?
g) Refer to the original data above. If the company were able to reduce its variable expenses by $\$ 1$ per unit,
- what would be the new monthly break-even point in units and sales dollars?
- verify the answer by preparing a contribution income statement.
h) Compute the company's degree of operating leverage. If sales increase by $10 \%$ how much should net income increase?


## Problem \#2

University Store, Inc.'s first quarter income statement is presented below:

| Sales |  | $\$ 800,000$ |
| :--- | :--- | ---: |
| Cost of Goods Sold |  | 560,000 |
| Gross Margin |  | 240,000 |
| Less: Operating Expenses: |  |  |
| $\quad$$\quad$ Selling Expenses  <br> $\quad$ Administrative Expenses $\underline{110,000}$ <br> Net Income  <br> 30,000  |  |  |

On average, a book sells for $\$ 40.00$. Variable selling expenses are $\$ 3.00$ per book; the remaining selling expenses are fixed. The variable administrative expenses are $5 \%$ of sales; the remainder of the administrative expenses is fixed.

Required: a) Prepare a contribution format income statement for the first quarter.
b) Prepare a breakeven income statement for the first quarter.
c) If 24,000 books are sold during the second quarter, calculate the company's expected contribution margin and net income.
d) If 22,000 books are sold during the second quarter, how much fixed expenses could increase if the company wanted to maintain a net income of $\$ 35,000$ ? Calculate the company's expected contribution margin.

## Problem \#3

Pricher Corporation's income statement for last year appears below:

Sales
$\$ 2,000,000$
Cost of goods sold:
Direct materials $\$ 500,000$
Direct labor (variable)
150,000
Variable manufacturing overhead
Fixed manufacturing overhead
Gross Profit
Selling and administrative expenses

$$
\text { Variable } \quad 100,000
$$

Fixed

50,000
600,000

200,000

Required: a) Calculate the breakeven point.
b) Calculate the degree of operating leverage.
c) If units sold double next year, calculate the degree of leverage.

## Problem \#4

In 2013, Goldblum Co. sold 160,000 units of its product at a selling price of $\$ 40$. The variable cost per unit was $\$ 30$, and Goldblum reported net income for the year of \$220,000.

Required: What was the amount of Goldblum's fixed costs for the year?

## Problem \#5

Heavener Company produces and sells storage sheds. Its current sales are $\$ 500,000$. The company's accountant provided the following cost information:

Manufacturing costs
Selling costs
Administrative costs
\$100,000 + 40\% sales
$\$ 30,000+10 \%$ sales
$\$ 45,000+10 \%$ sales

Required: a) Compute the product's contribution margin ratio.
b) Compute the company's current net income.
c) Compute the product's break-even point in dollars.
d) Compute the amount of revenue necessary to earn $\$ 60,000$ in profit.
e) Compute the company's current margin of safety ratio.
f) Should the company accept a proposal that increases sales by $20 \%$ and total fixed costs by $25 \%$ ?

## Problem \#6

The Parsons Company makes and sells two models of blenders, as follows:

|  | Smoothie Pro | Blendmaster |
| :--- | ---: | ---: |
| Selling price per unit | $\$ 50$ | $\$ 80$ |
| Variable cost per unit | $\$ 25$ | $\$ 45$ |

The Parsons Company expects to incur annual fixed costs of $\$ 151,250$. The relative sales mix of the products is 3 units of Smoothie Pro for every one unit of Blendmaster.

Required: a) Determine the total number of blenders (Smoothie Pro and Blendmaster combined) that Parsons must sell to break even.
b) What is the number of units of Smoothie Pro and of Blendmaster that Parsons would expect to sell at the break-even point?

## Multiple Choice Questions

1. The formula for break-even point in terms of units is
a) Total variable costs/Unit contribution margin
b) Total fixed costs/Contribution margin ratio
c) Total fixed costs/Unit contribution margin
d) Total variable costs/Total fixed costs
2. The formula for break-even point in terms of revenue is
a) Total variable costs/Contribution margin ratio
b) Total fixed costs/Contribution margin ratio
c) Total fixed costs/Unit contribution margin
d) Total variable costs/Total fixed costs
3. Alfred Corp has a selling price of $\$ 15$, variable costs of $\$ 10$ per unit, and fixed costs of $\$ 25,000$. How many units must be sold to break-even?
a) 5,000
b) 10,000
c) 2,500
d) 1,667
4. Piazza Corp has sales of $\$ 400,000$, a contribution margin ratio of $40 \%$, and a profit of $\$ 40,000$. If 20,000 units were sold, what is the break-even point in units?
a) 12,000
b) 8,000
c) 20,000
d) 15,000
5. Last month Kallina Company had a $\$ 30,000$ profit on sales of $\$ 250,000$. Fixed costs are $\$ 60,000$ a month. How much would sales have to decrease for Calico to break even?
a) $\$ 90,000$
b) $\$ 83,333$
c) $\$ 166,667$
d) $\$ 280,000$
6. Last month Kironina Company had a $\$ 60,000$ loss on sales of $\$ 300,000$. Fixed costs are $\$ 120,000$ a month. What revenue is needed to break even?
a) $\$ 360,000$
b) $\$ 480,000$
c) $\$ 600,000$
d) $\$ 420,000$
7. Perisia, Inc. has fixed costs of $\$ 200,000$ and a contribution margin ratio of $40 \%$. How much sales revenue must be earned for a profit of $\$ 50,000$ ?
a) $\$ 125,000$
b) $\$ 500,000$
c) $\$ 625,000$
d) $\$ 1,000,000$
8. Bench Corp has sales of $\$ 300,000$, a contribution margin ratio of $30 \%$, and a profit of $\$ 30,000$. If 20,000 units were sold, what is the variable cost per unit?
a) $\$ 15.00$
b) $\$ 10.50$
c) $\$ 4.50$
d) $\$ 2.00$
9. Pearl Company sold 20,000 units, had variable costs of $\$ 12$ per unit, fixed costs of $\$ 100,000$, and profits of $\$ 60,000$. What is the selling price per unit?
a) $\$ 8$
b) $\$ 17$
c) $\$ 20$
d) $\$ 32$
10. Degree of operating leverage is used to
a) calculate sales change given profit change.
b) calculate profit change given sales change.
c) calculate break-even sales given sales change.
d) calculate break-even sales given profit change.
11. Which of the following companies would have the highest proportion of variable costs in its cost structure?
a) Public utility
b) Airline
c) Fast food outlet
d) Architectural firm
12. Contribution margin is the amount remaining after:
a) variable expenses have been deducted from sales revenue.
b) fixed expenses have been deducted from sales revenue.
c) fixed expenses have been deducted from variable expenses
d) cost of goods sold has been deducted from sales revenues.
13. If a company decreases the variable expense per unit while increasing the total fixed expenses, the total expense line relative to its previous position will:
a) shift downward and have a steeper slope.
b) shift downward and have a flatter slope
c) shift upward and have a flatter slope.
d) shift upward and have a steeper slope
14. Bowe Corporation's fixed monthly expenses are $\$ 21,000$ and its contribution margin ratio is $61 \%$. Assuming that the fixed monthly expenses do not change, what is net operating income in a month when sales are $\$ 74,000$ ?
a) $\$ 7,860$
b) $\$ 45,140$
c) $\$ 24,140$
d) $\$ 53,000$
15. Cleckley Corporation's operating leverage is 5.9. If the company's sales increase by 19\%, its net operating income should increase by about:
a) $5.9 \%$
b) $31.1 \%$
c) $19.0 \%$
d) $112.1 \%$
16. Garth Corporation sells a single product. If the selling price per unit and the variable expense per unit both increase by $10 \%$ and fixed expenses do not change, then:

| Contribution | Contribution | Break-even |
| :---: | :---: | :---: |
| margin per unit | margin ratio | in units |
| Increases | Increases | Decreases |
| No change | No change | No change |
| No change | Increases | No change |
| Increases | No change | Decreases |

a) A
b) $B$
c) C
d) $D$
17. Lepage Corporation has provided its contribution format income statement for January. The company produces and sells a single product.

Sales (4,400 units)
Variable expenses
Contribution margin
Fixed expenses
Net operating income
\$211,200
127,600
83,600
66,400
$\$ 17,200$

If the company sells 4,700 units, total contribution margin should be:
a) $\$ 83,600$
b) $\$ 18,373$
c) $\$ 89,300$
d) $\$ 98,000$
18. Data concerning Hitchens Inc. two products for the most recent month is:

|  | Product V06Z | Product U85C |
| :--- | ---: | ---: |
| Sales | $\$ 18,000$ | $\$ 17,000$ |
| Variable expenses | $\$ 8,820$ | $\$ 1,330$ |

The fixed expenses of the entire company were $\$ 24,010$. The break-even point for the entire company is closest to:
a) $\$ 33,817$
b) $\$ 10,990$
c) $\$ 34,160$
d) $\$ 24,010$
19. Mason Enterprises has prepared the following budget for the month of July:

Product A
Product B
Product C

Selling Price Variable Cost
$\frac{\text { per Unit }}{\$ 10}$
\$15
\$18
per Unit
\$4
\$8
\$9

Unit Sales
15,000
20,000
5,000

Assuming that total fixed expenses will be $\$ 150,000$ and the sales mix remains constant, the break-even point would be closest to:
a) $\$ 276,008$
b) $\$ 235,292$
c) $\$ 294,545$
d) $\$ 141,278$
20. Upchurch Corporation produces and sells a single product. Data concerning that product appear below:

$$
\begin{array}{lr}
\text { Selling price per unit } & \$ 100.00 \\
\text { Variable expense per unit } & \$ 34.00 \\
\text { Fixed expense per month } & \$ 312,180
\end{array}
$$

Assume the company's target profit is $\$ 12,000$. The unit sales to attain that target profit is closest to:
a) 3,242
b) 4,912
c) 9,535
d) 5,896
21. Callicott Corporation produces a product that sells for $\$ 120$ per unit. The product's current sales are 25,400 units and its break-even sales are 18,542 units. What is the margin of safety in dollars?
a) $\$ 822,960$
b) $\$ 2,032,000$
c) $\$ 3,048,000$
d) $\$ 2,225,040$
22. Moccio Enterprises, Inc., produces and sells a single product whose selling price is $\$ 120.00$ per unit and whose variable expense is $\$ 37.20$ per unit. The company's monthly fixed expense is $\$ 356,040$. Assume the company's target profit is $\$ 15,000$. The dollar sales to attain that target profit is closest to:
a) $\$ 371,040$
b) $\$ 537,739$
c) $\$ 701,894$
d) $\$ 1,196,903$
23. Froio Corporation produces and sells two products. Data concerning those products for the most recent month appear below:

|  | Product M06M | Product Q20I |
| :--- | ---: | ---: |
|  | $\$ 11,000$ | $\$ 38,000$ |
| Sariabs expenses | $\$ 2,420$ | $\$ 16,690$ |

Fixed expenses for the entire company were $\$ 26,570$. The break-even point for the entire company is closest to:
a) $\$ 43,557$
b) $\$ 26,570$
c) $\$ 22,430$
d) $\$ 45,680$

## Solutions to Problems

## Problem \#1

a) Monthly break-even point in units and sales dollars:

Sales Dollars
Equation method: $\quad X=.40 \mathrm{X}+\$ 270,000$
. $6 \mathrm{X}=\$ 270,000$
$X=\$ 450,000$
CM method: $\quad \$ 270,000 / .6=\$ 450,000$
$\$ 270,000 / \$ 15=18,000$ units

Proof: $\quad 18,000$ units $X \$ 25=\$ 450,000$
b) The contribution margin is $\$ 270,000$, equal to the fixed expenses

Sales \$450,000
Less: Variable expenses
Contribution margin
less: Fixed expenses
Net income
180,000
270,000
270,000
$\$ 0$
c) Target level of sales:
$(270,000+60,000) / 15=22,000$ units
22,000 units $\mathrm{X} \$ 25=\$ 550,000$
d) Income statement:

| Sales | $\$ 550,000$ |
| :--- | ---: |
| Less: Variable expenses | $\underline{220,000}$ |
| Contribution margin | 330,000 |
| less: Fixed expenses | $\underline{270,000}$ |
| Net income | $\$ 60,000$ |

e) Margin of safety:
\$500,000-\$450,000 = \$50,000
$\$ 50,000 / \$ 500,000=.10$ or $10 \%$
f) Increase in net income

Contribution margin ratio is $60 \%(300,000 / 500,000=.60$ or $60 \%)$
Net income should increase by $\$ 15,000$ ( $60 \%$ of $\$ 25,000$ )
g) New breakeven point

New contribution margin is $\$ 16$ per unit ( $\$ 25.00-(\$ 10.00-\$ 1.00)$ )
New break-even point is $\$ 270,000 / \$ 16=16,875$ units $\times \$ 25.00=\$ 421,875$
Proof:
Sales \$421,875
Less: Variable expenses $\quad 151,875$
Contribution margin 270,000
less: Fixed expenses
Net income
270,000
\$0
h) Degree of operating leverage

Degree of operating leverage is $10 ;(\$ 300,000 / \$ 30,000=10)$
Net income should increase by 100\%; ( $10 \times 10 \%=100 \%$ )
Proof: Compare original data with income statement in d) above. Sales increased $10 \%$ from $\$ 500,000$ to $\$ 550,000$ and net income increased $100 \%$, from $\$ 30,000$ to $\$ 60,000$.

## Problem \#2

Units sold
Sales
Variable expenses:
Cost of goods sold
Selling
Administrative
Contribution margin a)
Fixed expenses:
Additional S\&A
Selling
Administrative
Operating income b)

| Per Unit | $\%$ |
| ---: | :--- |
| 1 | b) Total \$ |
| 20,000 |  |

$\$ 40.00 \quad 100.0 \quad \$ 800,000$
c) Total \$ 15,715 \$628,600 d) Total \$ e) Total \$ \$960,000 \$880,000 $28.00 \quad 70.0 \quad 560,000$

440,020
616,000

$$
\begin{array}{llllll}
3.00 & 7.5 & 60,000 & 47,145 & 72,000 & 66,000
\end{array}
$$

$$
\frac{2.00}{700} \quad \frac{5.0}{175}
$$

$$
17.5
$$

$$
\frac{40,000}{140,000}
$$

$$
\begin{array}{r}
672,000 \\
72,000 \\
48,000 \\
168,000
\end{array}
$$

$$
\begin{array}{r}
31,430 \\
110,005
\end{array}
$$

44,000
154,000
$\frac{70,000}{\$ 0} \quad \underline{70,000}$

## Problem \#3

| Sales |  | $\$ 2,000,000$ |
| :--- | ---: | ---: |
| $\quad$ Direct materials | $\$ 500,000$ |  |
| Direct labor (variable) | 150,000 |  |
| Variable manufacturing overhead | 50,000 |  |
| Variable selling and administrative | $\underline{100,000}$ | $\underline{800,000}$ |
| Contribution margin |  | $1,200,000$ |

a) CM ratio $=1,200,000 / 2,000,000=60 \%$

Breakeven point $=300,000 / 60 \%=\$ 500,000$
b) Degree of leverage $=1,200,000 / 400,000=3$
c) Degree of leverage $=(1,200,000+1,200,000) /(400,000+$ $1,200,000)=1.5$

## Problem \#4

Contribution margin per unit
Total contribution margin
Net income
Fixed expenses

| $\$ 40-\$ 30=$ | $\$ 10$ |
| :---: | ---: |
| $\$ 10 \times 160,000=$ | $\$ 1,600,000$ |
| 220,000 |  |
|  | $\$ 1,380,000$ |

\$1,600,000
\$1,380,000

## Problem \#5

| a) | Contribution margin ratio | $100 \%-40 \%-10 \%-10 \%$ |
| :--- | :---: | ---: |
| b) | Net income | $40 \%$ |
|  | Contribution margin | $\$ 500,000 \times 40 \%=$ |
|  |  | $\$ 200,000$ |
|  | Fixed expenses | $\underline{175,000}$ |
| c) | Breakeven sales | $\$ 175,000 / 40 \%=$ |
| d) Sales for $\$ 60,000$ income | $(\$ 175,000+\$ 60,000) / 40 \%=$ | $\$ 437,500$ |
| e) Unit contribution margin | $\$ 40-\$ 30=$ | $\$ 10$ |
| f) Margin of safety ratio | $(\$ 500,000-\$ 437,500)$ | $12.5 \%$ |
|  | $\$ 500,000$ |  |

g) No; a sales increase of $\$ 100,000$ will generate an additional $\$ 40,000$ in contribution margin but total fixed costs will increase by \$43,750.
Therefore, income will be reduced by $\$ 3,750$.

## Problem \#6

a) Weighted average contribution margin
Breakeven units
b) Units of Blendmaster

| $\frac{(3 \times \$ 25)+(1 \times \$ 35)}{4 \text { units }}$ | $\$ 27.50$ |
| :---: | :---: |
| $\frac{\$ 151,250}{\$ 27.50}$ | 5,500 units |
| $\frac{1}{4} \times 5,500=$ | 1,375 units |


| 1. | C |
| :--- | :--- |
| 2. | B |
| 3. | A |
| 4. | D |
| 5. | B |
| 6. | C |
| 7. | C |
| 8. | B |
| 9. | C |
| 10. | B |
| 11. | C |
| 12. | A |
| 13. | C |
| 14. | C |
| 15. | D |
| 16. | D |
| 17. | C |
| 18. | A |
| 19. | C |
| 20. | B |
| 21. | A |
| 22. | B |
| 23. | A |

