## ChemActivity 3

## Coulombic Potential Energy

(What Is Attractive about Chemistry?)

## Model 1: Two Charged Particles Separated by a Distance "d".



According to Coulomb, the potential energy $(V)$ of two stationary charged particles is given by the equation above, where $q_{1}$ and $q_{2}$ are the charges on the particles (for example: -1 for an electron), $d$ is the separation of the particles (in pm ), and $k$ is a positive-valued proportionality constant.

$$
1 \mathrm{pm}=10^{-12} \mathrm{~m}
$$

## Critical Thinking Questions

1. Assuming that $q_{1}$ and $q_{2}$ remain constant, what happens to the magnitude of $V$ if the separation, $d$, is increased?
2. If the two particles are separated by an infinite distance (that is, $d=\infty$ ), what is the value of $V$ ?
3. If $d$ is finite, and the particles have the same charge (that is, $q_{1}=q_{2}$ ), is $V>0$ or is $V<0$ ? Explain your answer.
4. If $q$ for an electron is -1 ,
a) what is $q$ for a proton?
b) what is $q$ for a neutron?
c) what is $q$ for the nucleus of a C atom?
5. Recall that a ${ }^{1} \mathrm{H}$ atom consists of a proton as the nucleus and an electron outside of the nucleus. Is the potential energy, $V$, of a hydrogen atom a positive or negative number? Explain your answer.

## Model 2: Ionization Energy.

The ionization energy (IE) is the amount of energy needed to remove an electron from an atom and move it infinitely far away. Ionization energies are commonly measured in joules, J.

Figure 1. Ionization of a hypothetical atom $L$ with one proton and one stationary electron.


Adding $0.231 \times 10^{-18} \mathrm{~J}$ to Atom L results in a bare proton and a free electron.

$$
\mathrm{IE}=0.231 \times 10^{-18} \mathrm{~J}
$$

Atom $\mathrm{L}+0.231 \times 10^{-18} \mathrm{~J} \longrightarrow \mathrm{p}^{+}+\mathrm{e}^{-}$

Figure 2. Ionization energies of two hypothetical atoms, each with one proton and one stationary electron separated by distance " $d$ ".


$$
d=500 \mathrm{pm}
$$

$$
\mathrm{IE}=0.462 \times 10^{-18} \mathrm{~J}
$$



$$
d=200 \mathrm{pm}
$$

$$
\mathrm{IE}=1.16 \times 10^{-18} \mathrm{~J}
$$

Table 1. Ionization energies of several hypothetical atoms, each with one proton and one stationary electron separated by distance " $d$ ".

| Hypothetical <br> Atom | $d$ <br> $(\mathrm{pm})$ | IE <br> $\left(10^{-18} \mathrm{~J}\right)$ | $V$ <br> $\left(10^{-18} \mathrm{~J}\right)$ |
| :---: | :---: | :---: | :---: |
| A | $\infty$ | 0 |  |
| E | 5000. | 0.0462 |  |
| L | 1000. | 0.231 |  |
| Q | 500.0 | 0.462 |  |
| T | 200.0 | 1.16 |  |
| Z | 100.0 | 2.31 |  |

## Critical Thinking Questions

6. Do you expect the potential energy, $V$, of the hypothetical atoms in Table 1 to be positive or negative numbers? Explain your reasoning.
7. Without using a calculator, predict what trend (if any) you expect for the values of $V$ for these hypothetical atoms.
8. Calculate the potential energies of the hypothetical atoms to complete Table 1. Use the value $k=2.31 \times 10^{-16} \mathrm{~J} \cdot \mathrm{pm}$.
9. What is the relationship between IE and $V$ for these hypothetical atoms?
10. Which of the following systems will have the larger ionization energy? Explain your reasoning.
a) an electron at a distance of 500 pm from a nucleus with charge +2
b) an electron at a distance of 700 pm from a nucleus with charge +2
11. Which of the following systems will have the larger ionization energy? Explain your reasoning.
a) an electron at a distance $d_{1}$ from a nucleus with charge +2
b) an electron at a distance $d_{1}$ from a nucleus with charge +1
12. How many times larger is the larger of the two ionization energies from CTQ 11? Show your work.
13. Consider a hydrogen atom and a helium ion, $\mathrm{He}^{+}$. Which of these do you expect to have the larger ionization energy? Explain your reasoning, including any assumptions you make.

## Exercises

1. For a hypothetical atom (as in Table 1) with $V=-5.47 \times 10^{-18} \mathrm{~J}$, what would the IE be?
2. Which of the following systems will have the larger ionization energy? Show your work.
a) an electron at a distance $d_{1}$ from a nucleus with charge +2
b) an electron at a distance $2 d_{1}$ from a nucleus with charge +1
3. Which of the following systems has the larger ionization energy?
a) an electron at a distance $5 d_{1}$ from a nucleus with a charge of +6
b) an electron at a distance $6 d_{1}$ from a nucleus with a charge of +7

## Problems

1. According to the Coulombic Potential Energy equation, if a particle with a charge of -1 is extremely close to a particle with a charge of +2 , the potential energy is: a) large and positive b) large and negative c) small and negative d) small and positive
2. Two electrons and one helium nucleus are arranged in a straight line as shown below. The electron on the left is 300 nm from the nucleus; the electron on the right is 400 nm from the nucleus. Write the three Coulombic Potential Energy terms for this arrangement of charges.

