

Deep Learning

Part 3

Yin Li

`yin.li@wisc.edu`

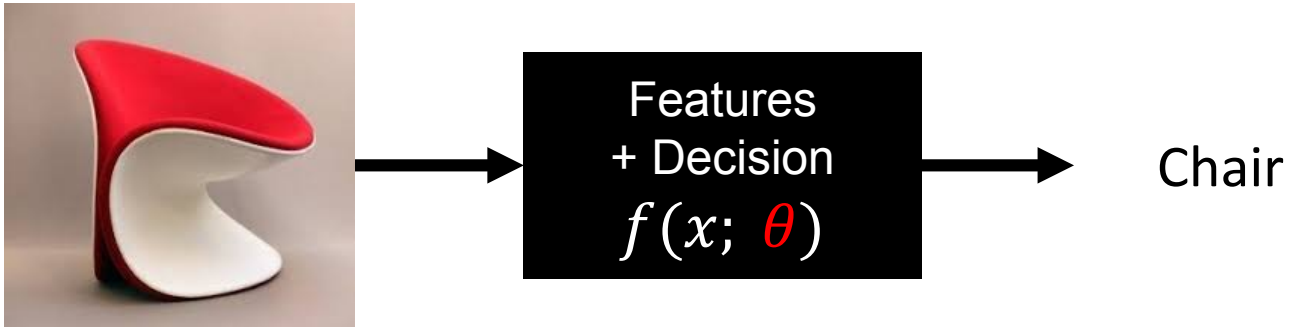
University of Wisconsin, Madison

[Some of the slides from Lana Lazebnik, Kaiming He and others]

Deep Learning = Deep Neural Networks

- **Deep Learning:** Composing a set of (nonlinear) functions g

$$f(\mathbf{x}; \boldsymbol{\theta}) = g_1(\dots g_{n-1}(g_n(\mathbf{x}; \boldsymbol{\theta}_n), \boldsymbol{\theta}_{n-1}) \dots, \boldsymbol{\theta}_1)$$

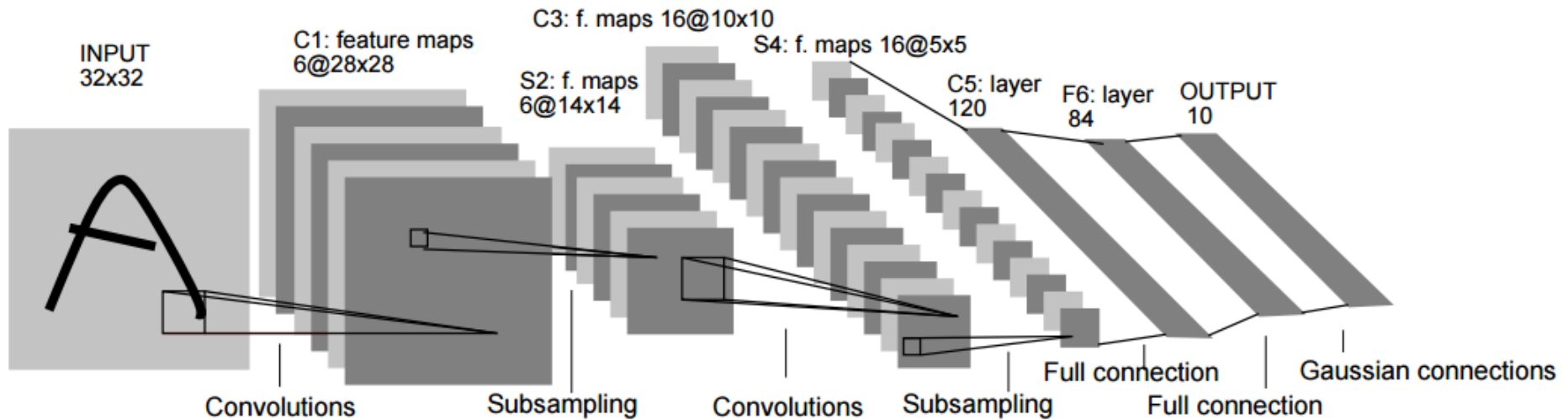


- Each of the function g is represented using a layer of a neural network
- **Key element:** Linear operations + Nonlinear activations, e.g., $\mathbf{a} = \sigma(\mathbf{W}^T \mathbf{x} + \mathbf{b})$

What we have talked about so far

- The linear functions
 - Fully connected layer: dense W
 - Convolutional layer: sparse and structured W
- The nonlinear activations
 - Sigmoid
 - Rectified linear unit (ReLU)
 - Many others ...
- Pooling
- Output normalization
- Loss functions

Case study: LeNet-5 (1998)

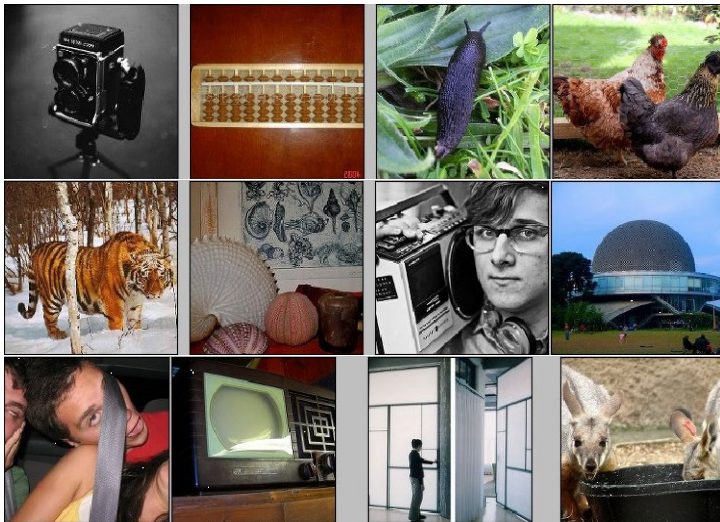


- convolutional layers + fully connected layers
- Sigmoid as the activation function
- [Conv + sigmoid + average pooling] x 2 + fully connected x 3

Figure from *Gradient-based learning applied to document recognition*,
by Y. LeCun, L. Bottou, Y. Bengio and P. Haffner

ImageNet challenge (2010-2017)

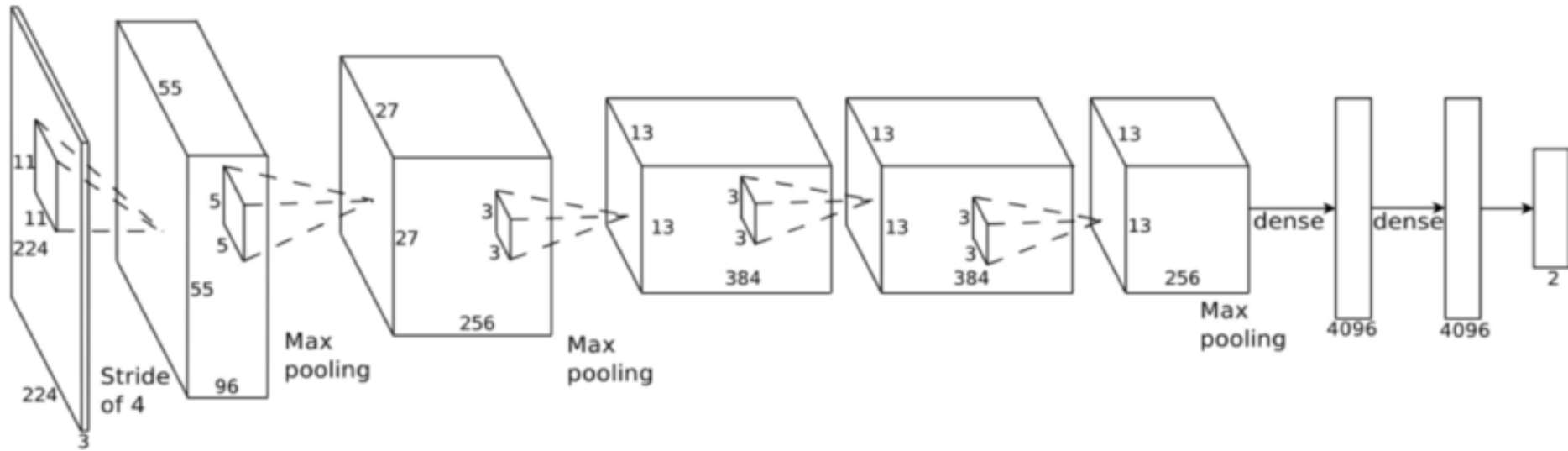
IMAGENET



- ~14 million labeled images, 20K classes
- Images gathered from Internet
- Labels provided by humans
- ImageNet Large-Scale Visual Recognition Challenge (ILSVRC):
 - 1.2 million training images, 1000 classes

www.image-net.org/challenges/LSVRC/

Case study: AlexNet (2012)



- A modern deep neural network
- Winner of ImageNet challenge 2012
- +10% better than everything else in 2012!

Case study: AlexNet (2012)

Input: 224 x 224 x 3
(color images)

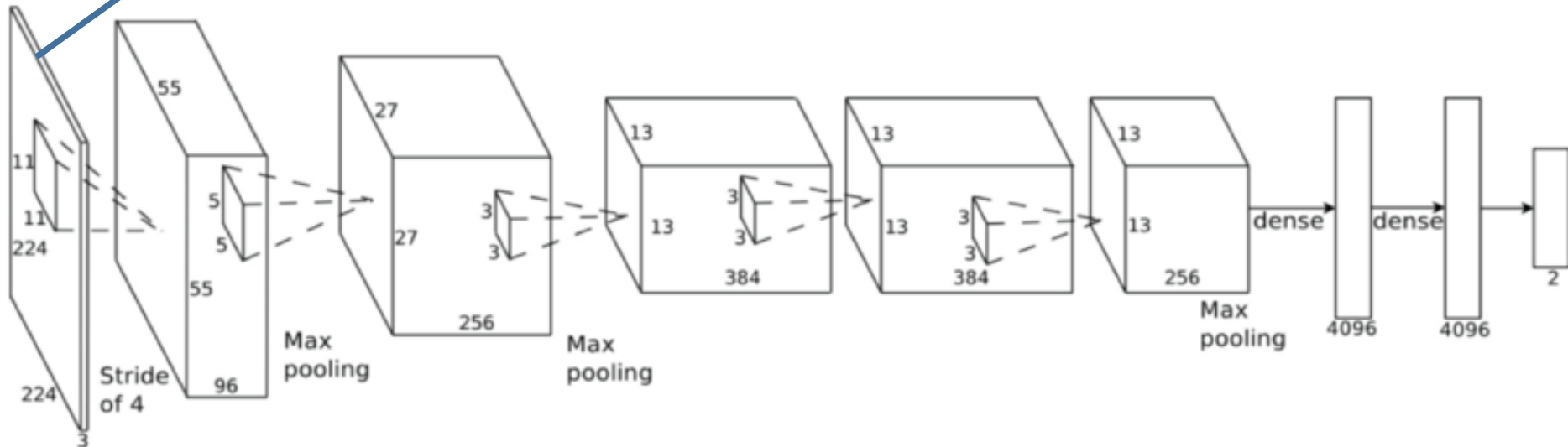


Figure from *ImageNet Classification with Deep Convolutional Neural Networks*, by A. Krizhevsky, I. Sutskever, and G. Hinton

Case study: AlexNet (2012)

Filter: 11x11x3, stride: 4x4,
#filters: 96
Activation: ReLU

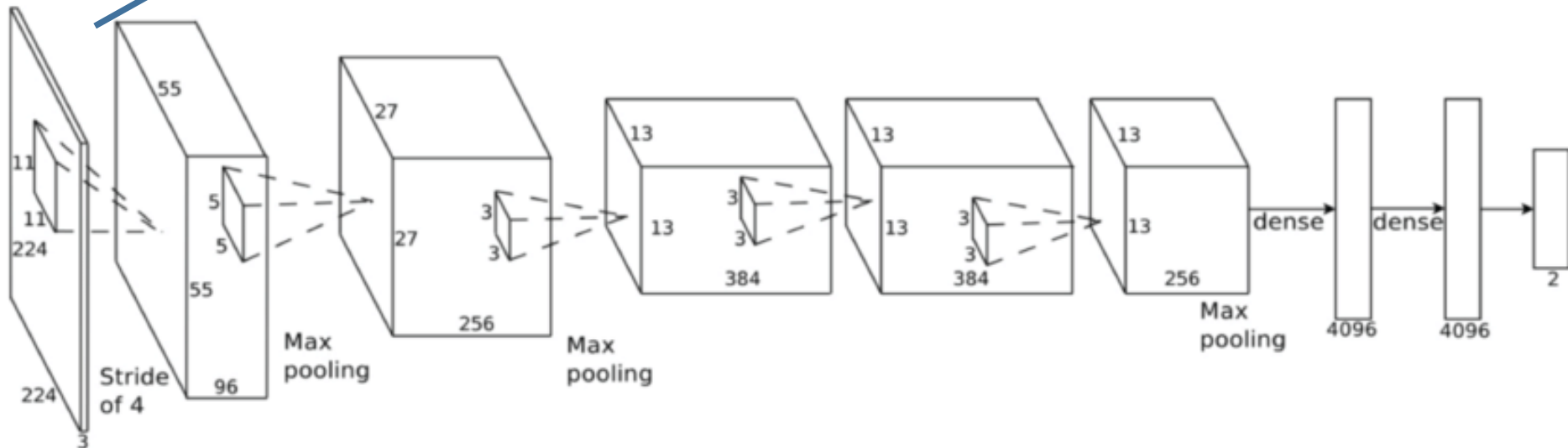


Figure from *ImageNet Classification with Deep Convolutional Neural Networks*,
by A. Krizhevsky, I. Sutskever, and G. Hinton

Case study: AlexNet (2012)

Max pooling
Filter: 3x3, stride 2x2

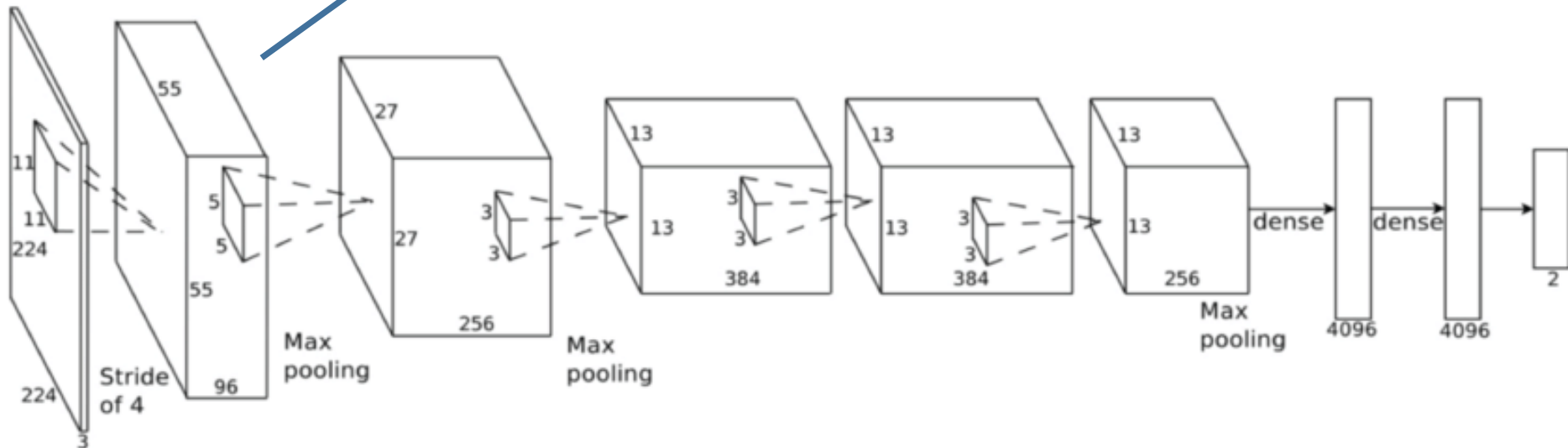


Figure from *ImageNet Classification with Deep Convolutional Neural Networks*, by A. Krizhevsky, I. Sutskever, and G. Hinton

Case study: AlexNet (2012)

Filter: 5x5x96, stride: 1x1,
#filters: 256
Activation: ReLU

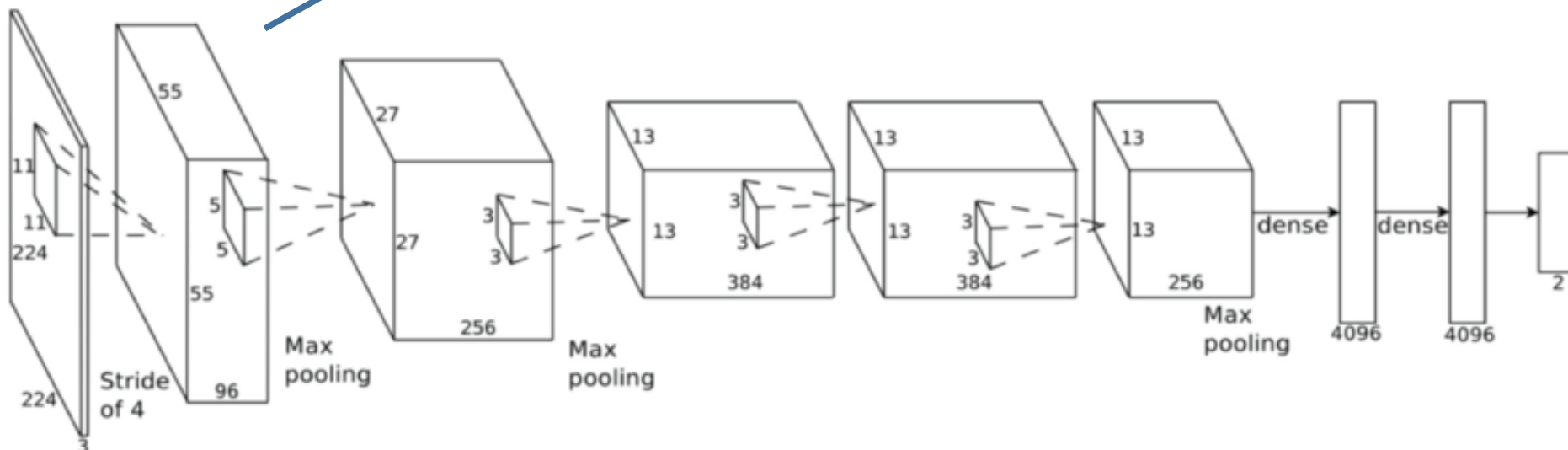


Figure from *ImageNet Classification with Deep Convolutional Neural Networks*,
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Case study: AlexNet (2012)

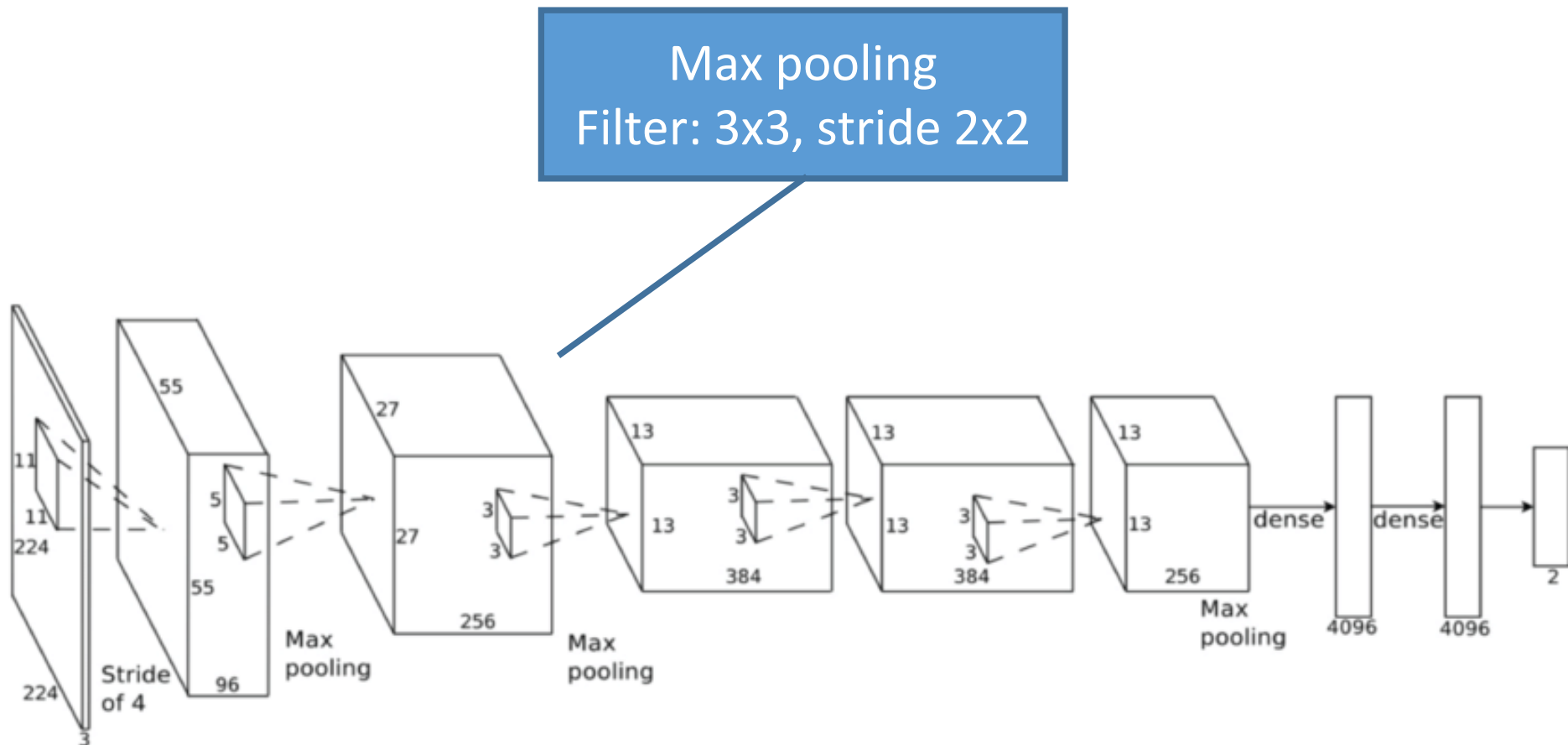


Figure from *ImageNet Classification with Deep Convolutional Neural Networks*,
by A. Krizhevsky, I. Sutskever, and G. Hinton

Case study: AlexNet (2012)

Filter: 3x3x256, stride: 1x1,
#filters: 384
Activation: ReLU

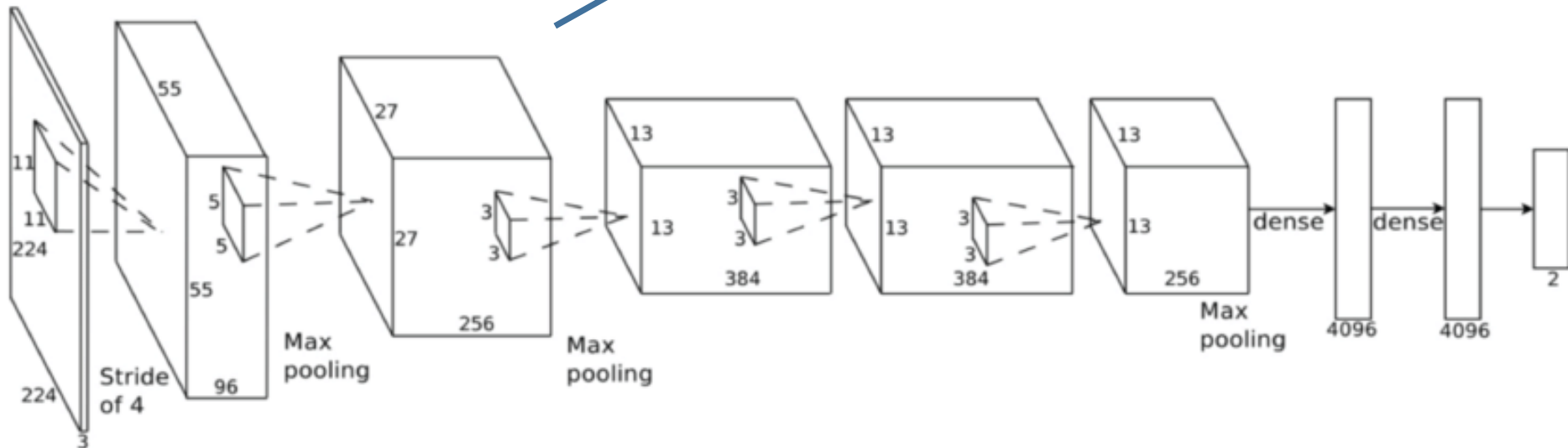


Figure from *ImageNet Classification with Deep Convolutional Neural Networks*,
by A. Krizhevsky, I. Sutskever, and G. Hinton

Case study: AlexNet (2012)

Filter: 3x3x384, stride: 1x1,
#filters: 384
Activation: ReLU

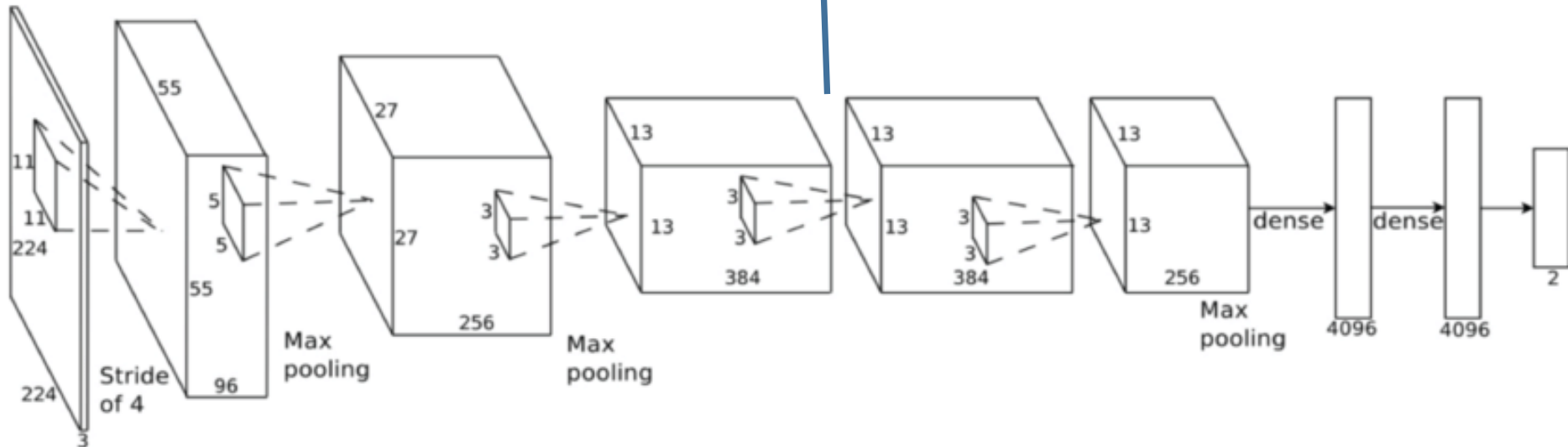


Figure from *ImageNet Classification with Deep Convolutional Neural Networks*, by A. Krizhevsky, I. Sutskever, and G. Hinton

Case study: AlexNet (2012)

Filter: 3x3x384, stride: 1x1,
#filters: 256
Activation: ReLU

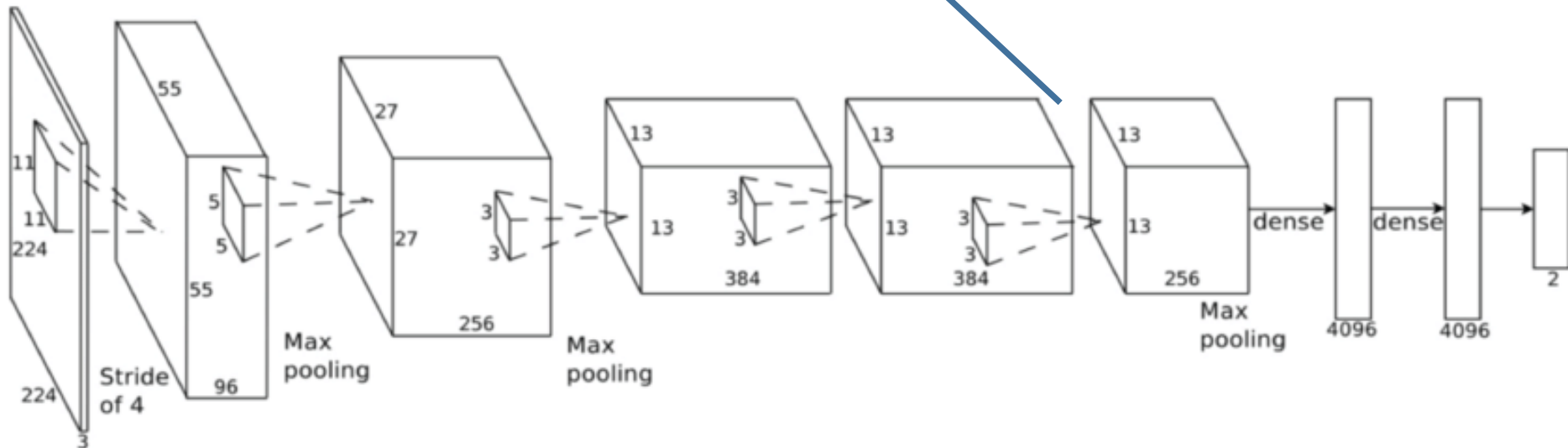


Figure from *ImageNet Classification with Deep Convolutional Neural Networks*,
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Case study: AlexNet (2012)

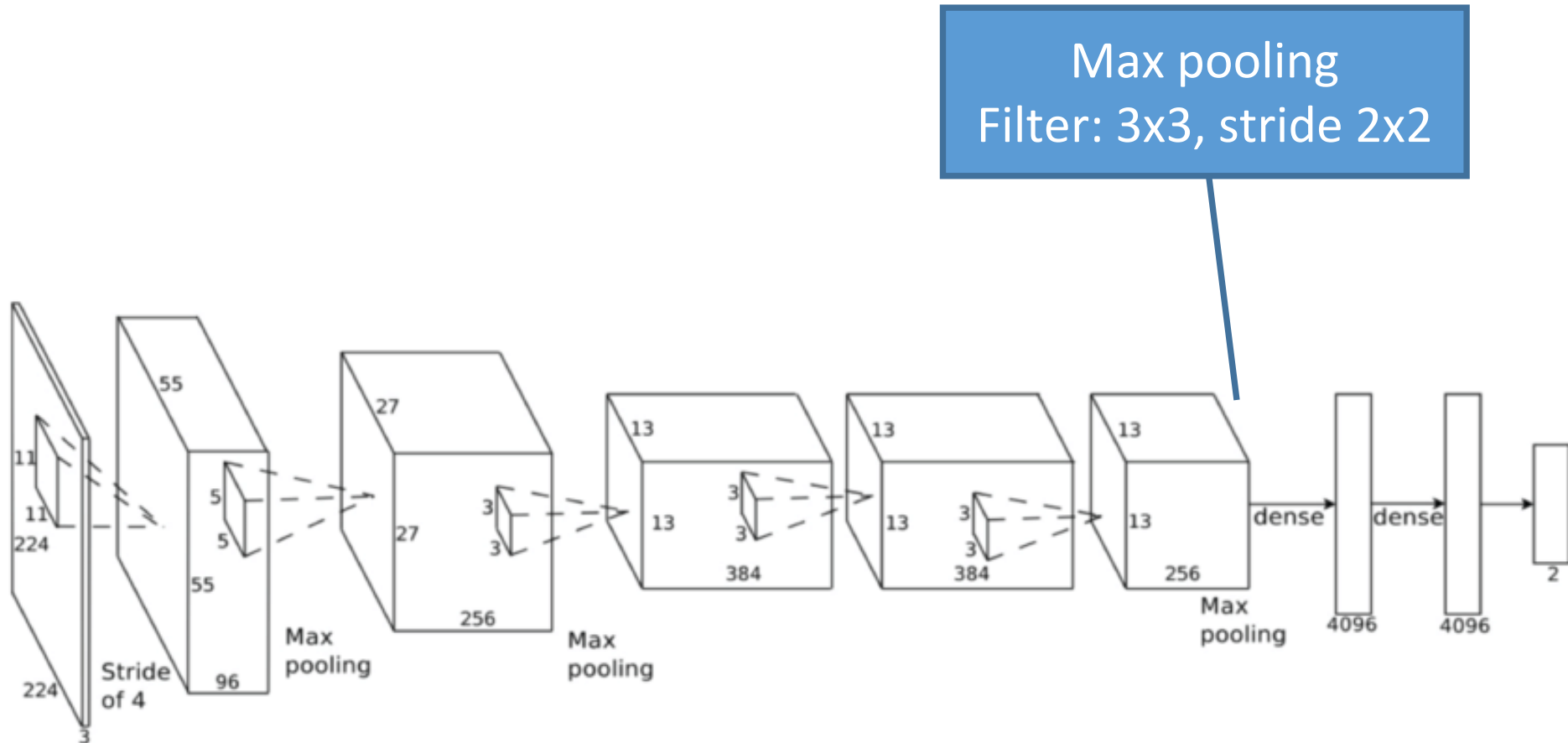


Figure from *ImageNet Classification with Deep Convolutional Neural Networks*,
by A. Krizhevsky, I. Sutskever, and G. Hinton

Case study: AlexNet (2012)

Weight matrix: 9216x4096
Activation: ReLU

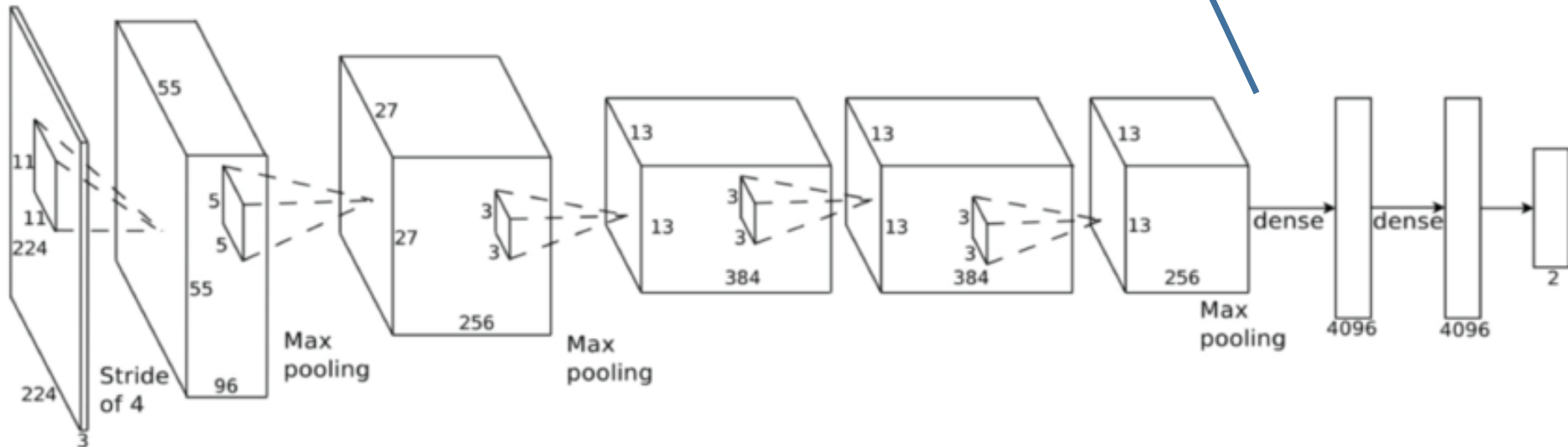


Figure from *ImageNet Classification with Deep Convolutional Neural Networks*, by A. Krizhevsky, I. Sutskever, and G. Hinton

Case study: AlexNet (2012)

Weight matrix: 4096x4096
Activation: ReLU

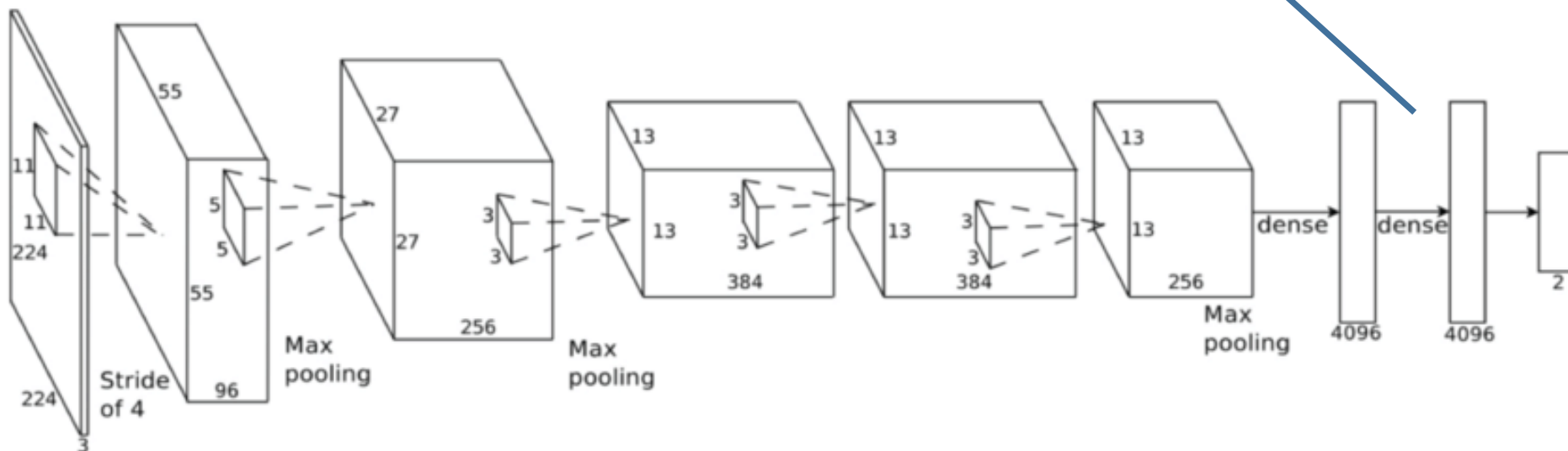


Figure from *ImageNet Classification with Deep Convolutional Neural Networks*, by A. Krizhevsky, I. Sutskever, and G. Hinton

Case study: AlexNet (2012)

Weight matrix: 4096x1000
Output normalization: Softmax

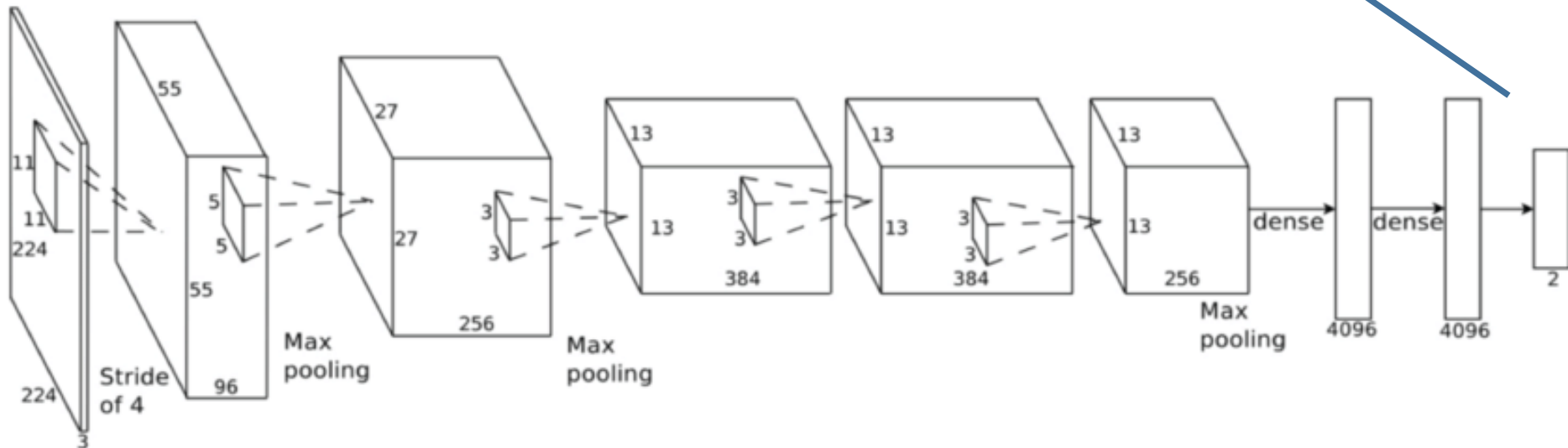
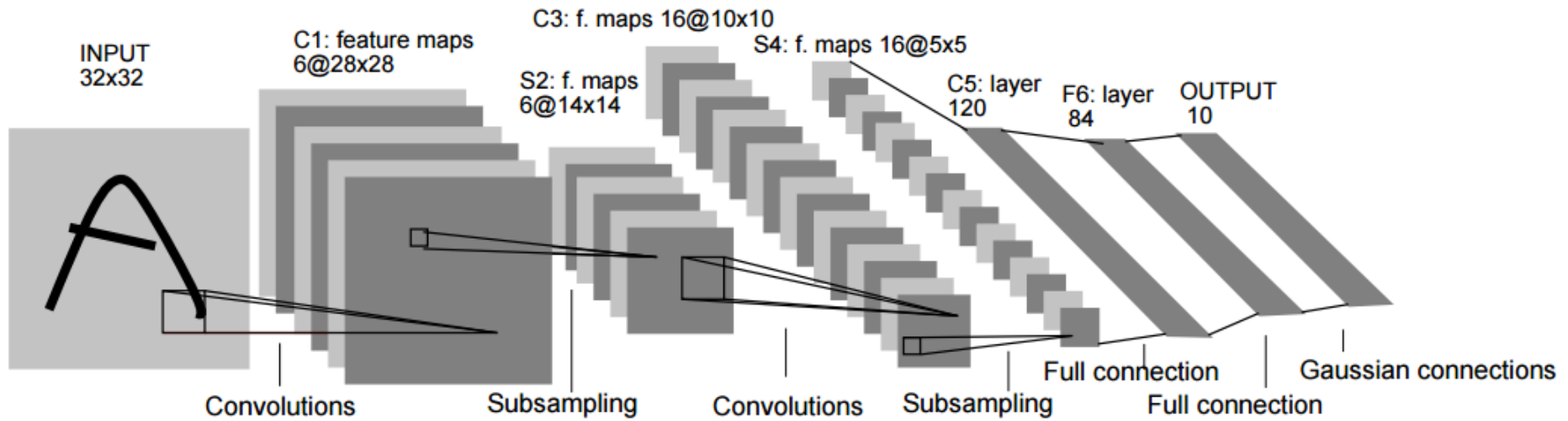


Figure from *ImageNet Classification with Deep Convolutional Neural Networks*, by A. Krizhevsky, I. Sutskever, and G. Hinton

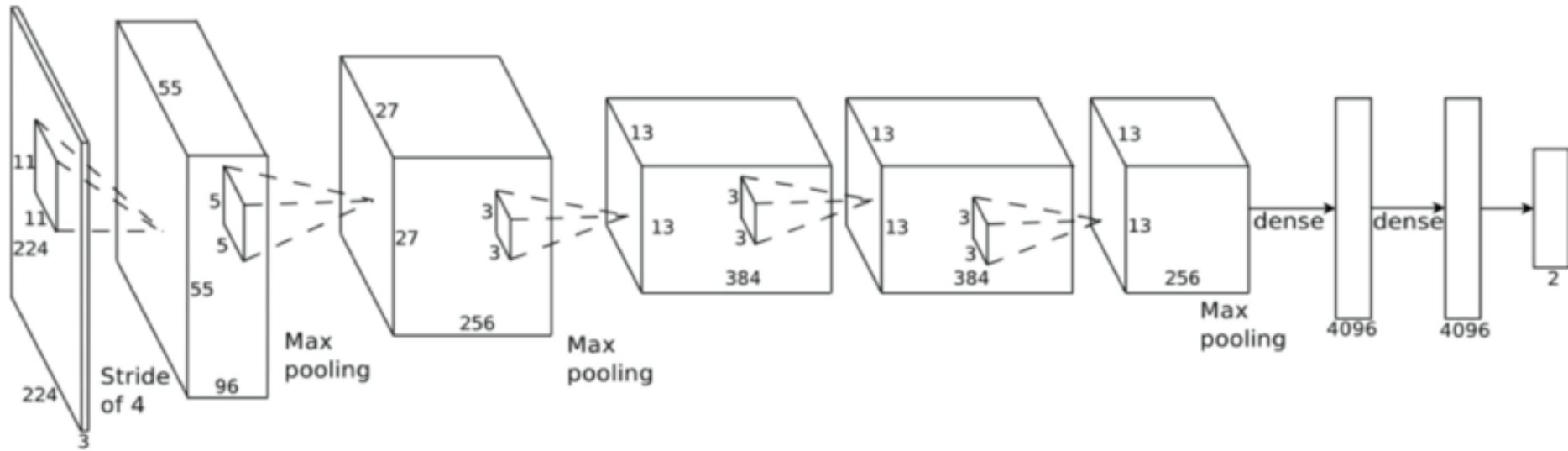
Case study: LeNet-5 (1998)



- convolutional layers + fully connected layers
- Sigmoid as the activation function
- [Conv + sigmoid + average pooling] x 2 + fully connected x 3
- Trained on MNIST with 60K training samples

Figure from *Gradient-based learning applied to document recognition*,
by Y. LeCun, L. Bottou, Y. Bengio and P. Haffner

Case study: AlexNet (2012)



- convolutional layers + fully connected layers
- **ReLU** as the activation function
- [Conv + ReLU + **max pooling**] x 5 + fully connected x 3
- Most importantly: **1.2 millions** of training images!

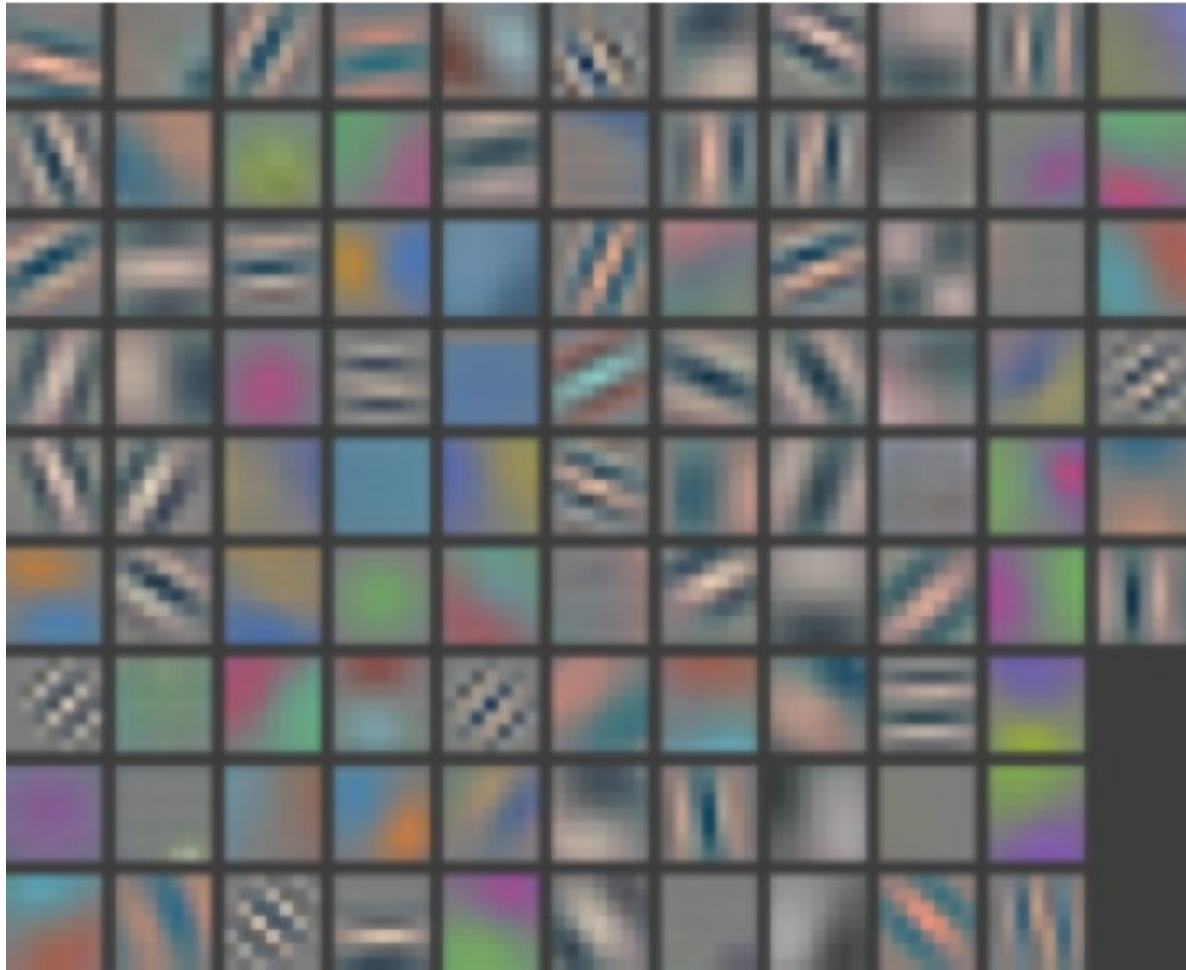
Deep convolutional networks: basic design

- [Conv + ReLU] + Pooling
- A few fully connected (FC) layers at the end
- Output normalization + Loss function
- Training: mini-batch stochastic gradient descent
- Inference: use the (normalized) outputs

Case study: AlexNet (2012)

- What makes deep learning work?
 - A modern design of neural network architectures
 - Large scale training dataset
 - A lot of computing power (GPUs)
- Why does deep learning work so well?
 - Still a mystery to a large extent
 - Intuitively, a deep neural network builds a hierarchical representation of data

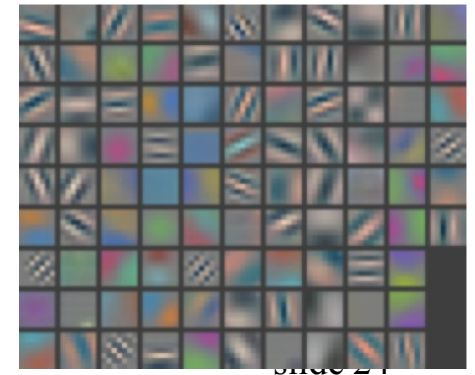
Layer 1 Filters



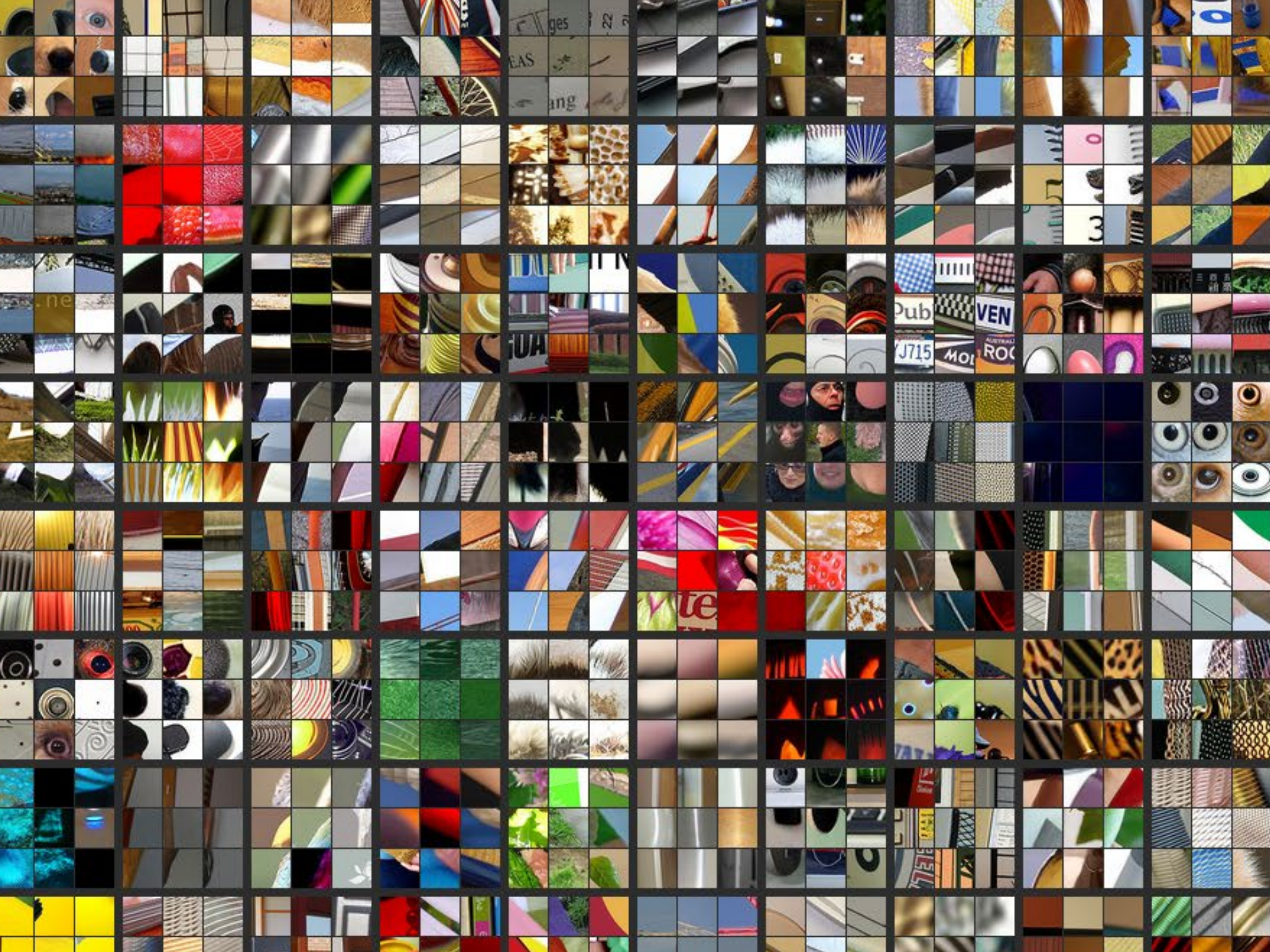
Figures from Visualizing and Understanding Convolutional Networks
by *M. Zeiler and R. Fergus*

Layer 1: Top-9 Patches

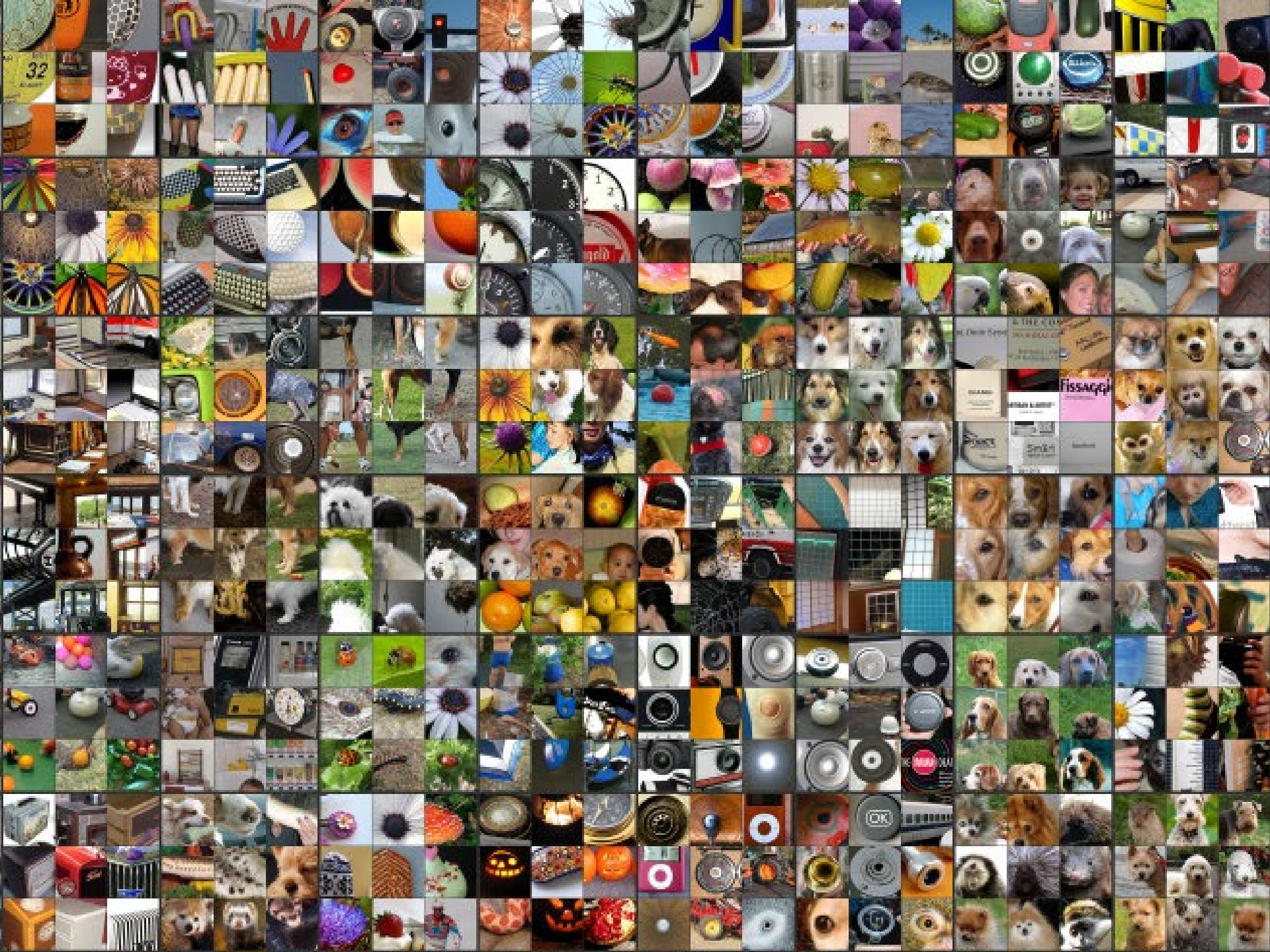
- Select patches on the validation set with maximum activation of a given convolutional filter / kernel

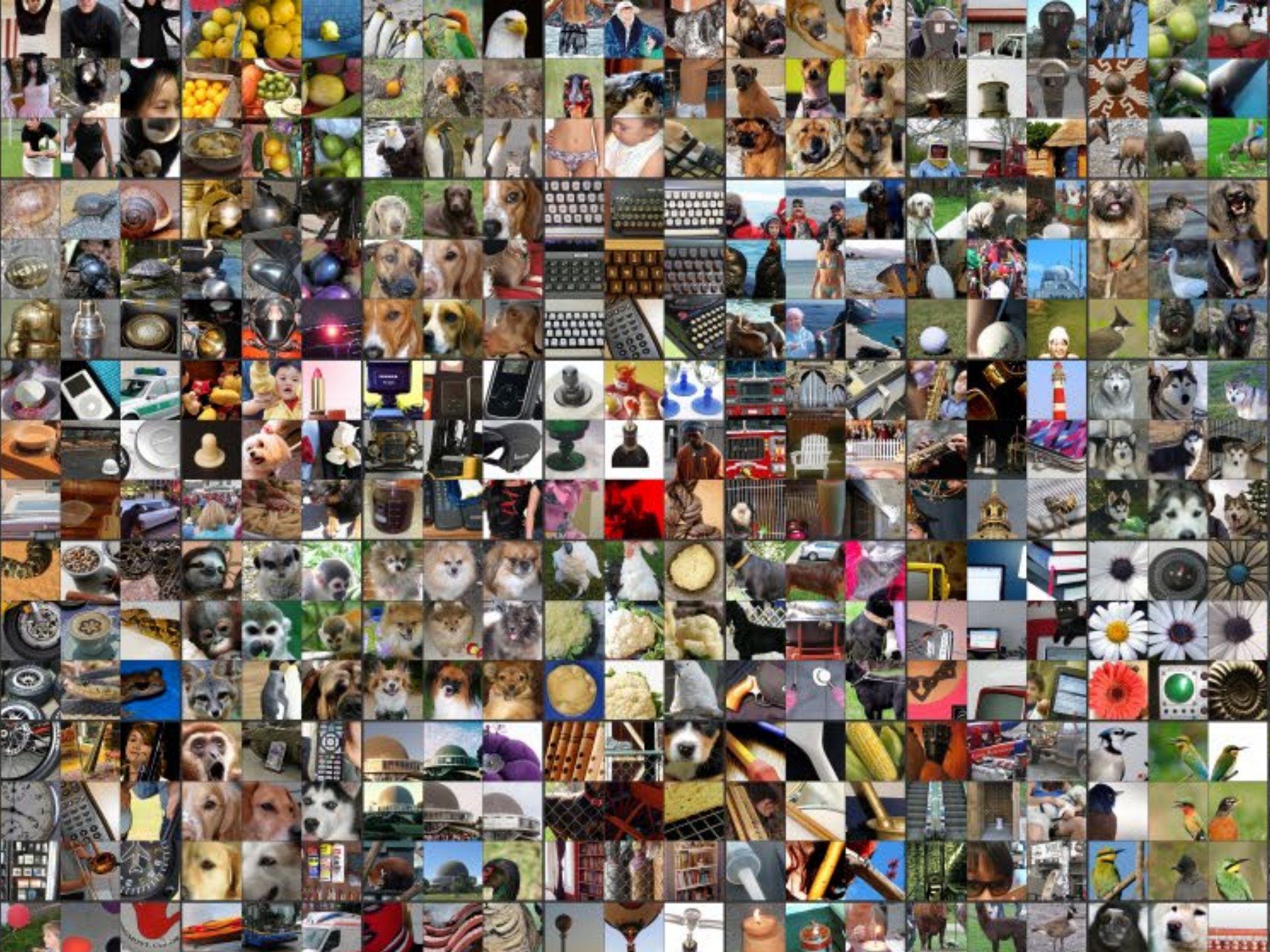


Layer 2 - 5: Top-9 Patches









Case study: VGGNet (2014)



- 2nd place in ImageNet challenge 2014
- Make the network deeper
 - AlexNet (5 conv + 3 FC)
 - VGGNet (12/14 conv + 3 FC)
- Use smaller filter / kernel size
 - AlexNet (11x11, 5x5, 3x3)
 - VGGNet (3x3)
- Large receptive fields replaced by successive layers of 3x3 convolutions (with ReLU in between)

Case study: GoogLeNet (2014)

- The Inception Module
 - Parallel paths with different receptive field sizes and operations

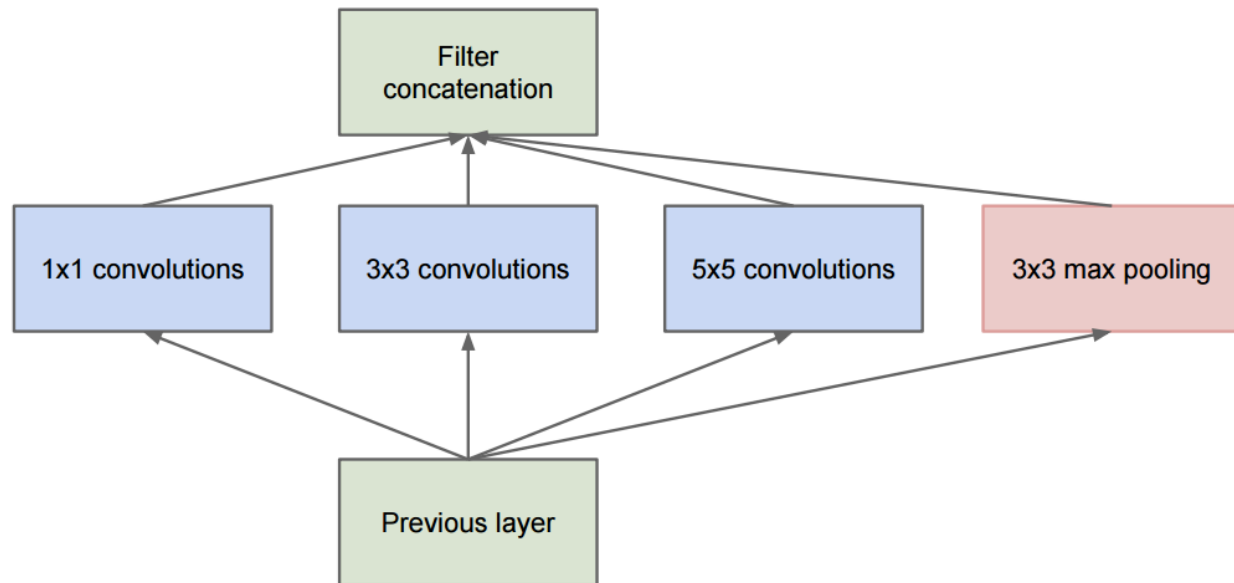


Figure from Going deeper with convolutions by *C. Szegedy et al.*

Case study: GoogLeNet (2014)

- The Inception Module
 - Parallel paths with different receptive field sizes and operations
 - Use 1x1 convolutions for dimensionality reduction before expensive convolutions

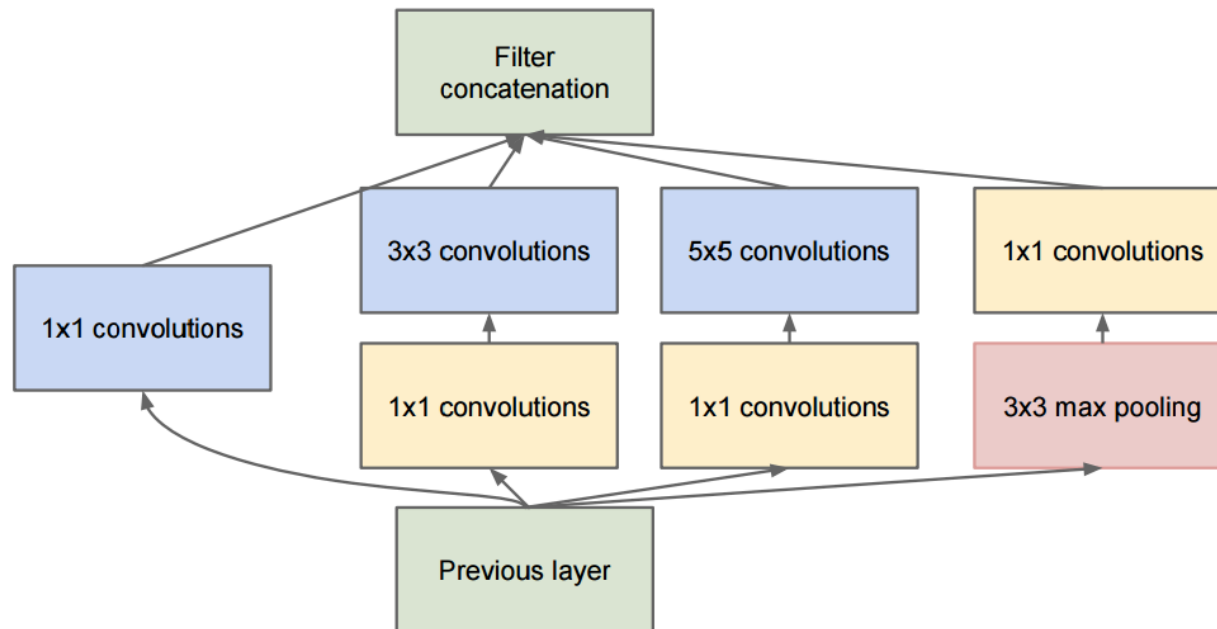
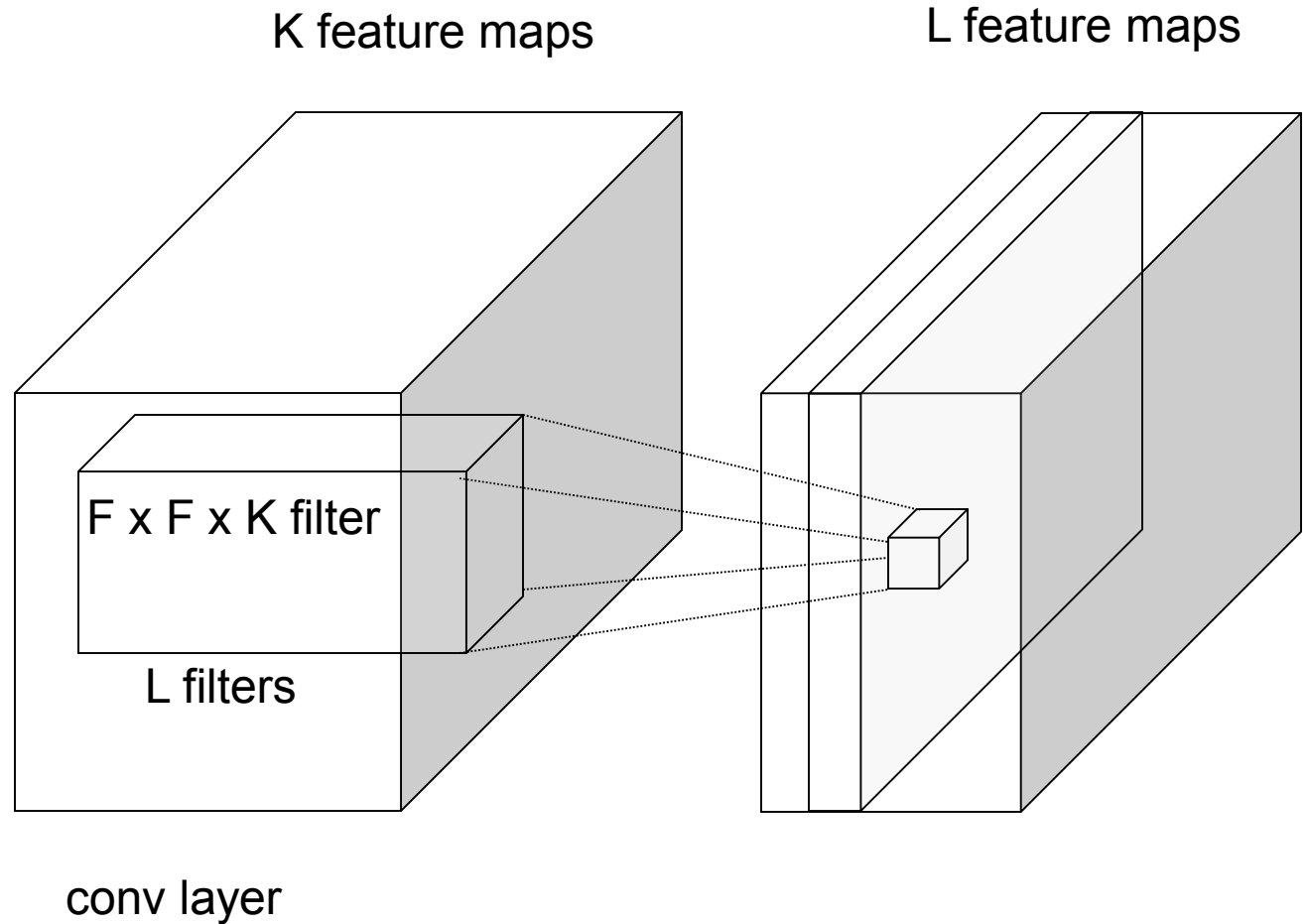
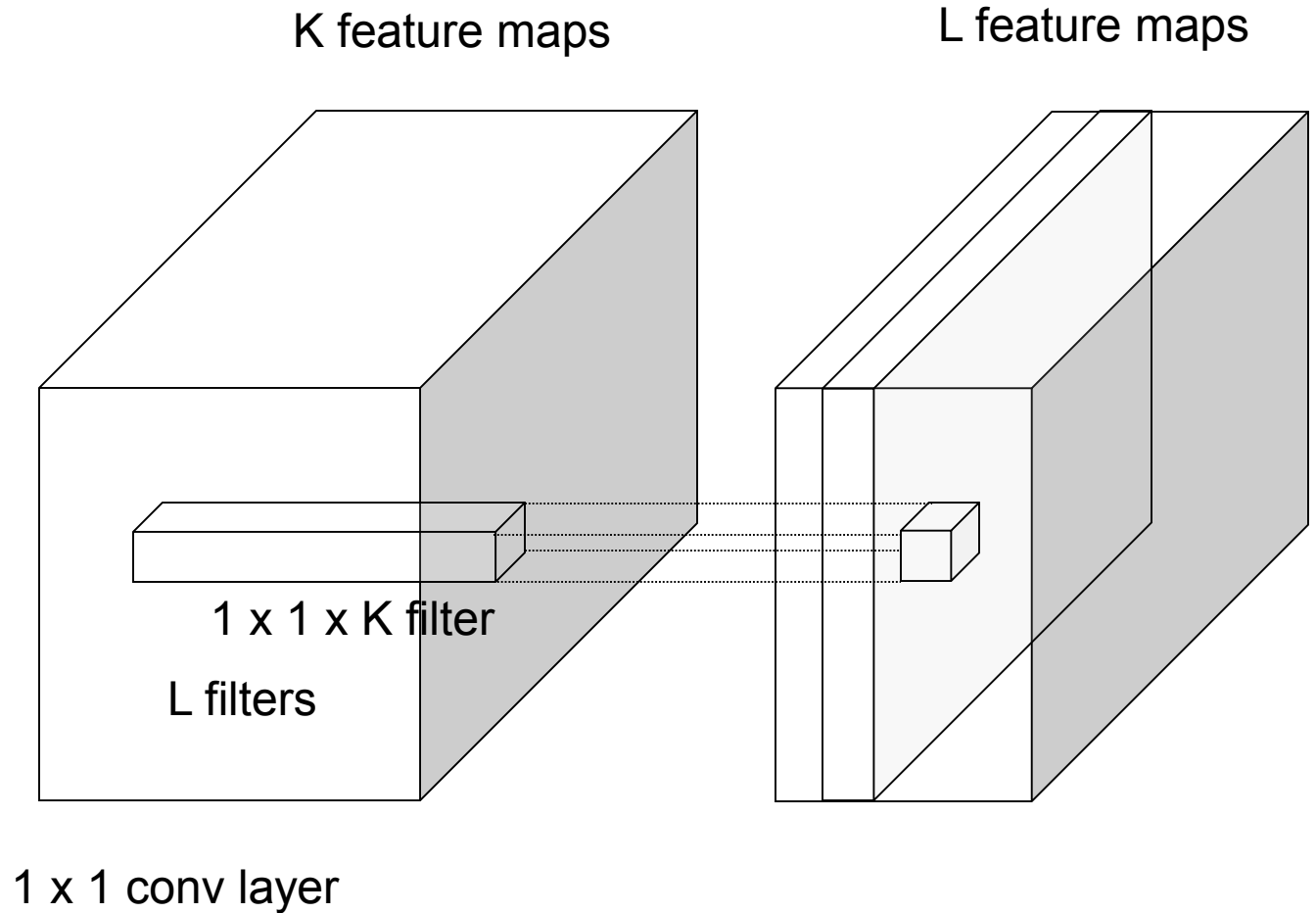


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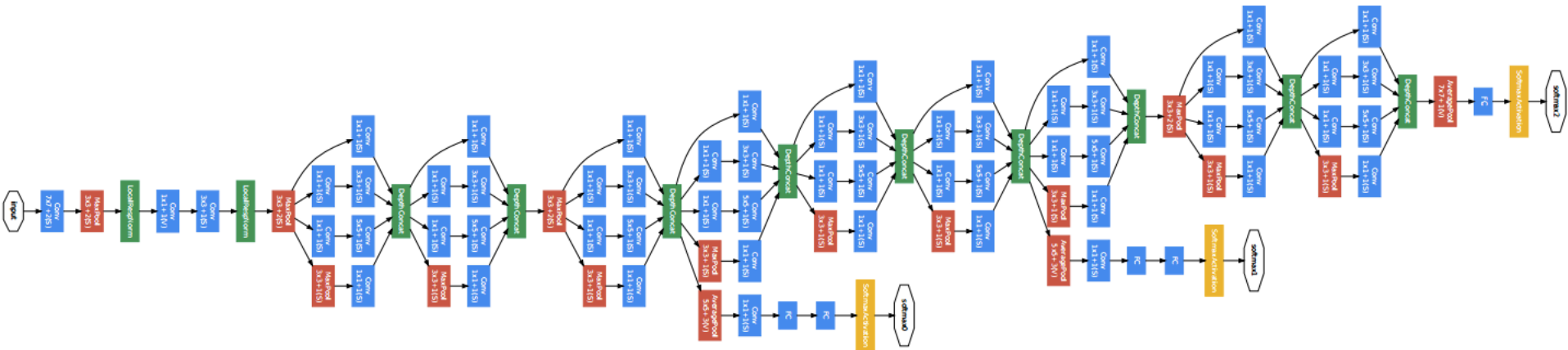
FxF convolutions



1x1 convolutions



Case study: GoogLeNet (2014)



Inception module

Figure from Going deeper with convolutions by *C. Szegedy et al.*

Case study: GoogLeNet (2014)

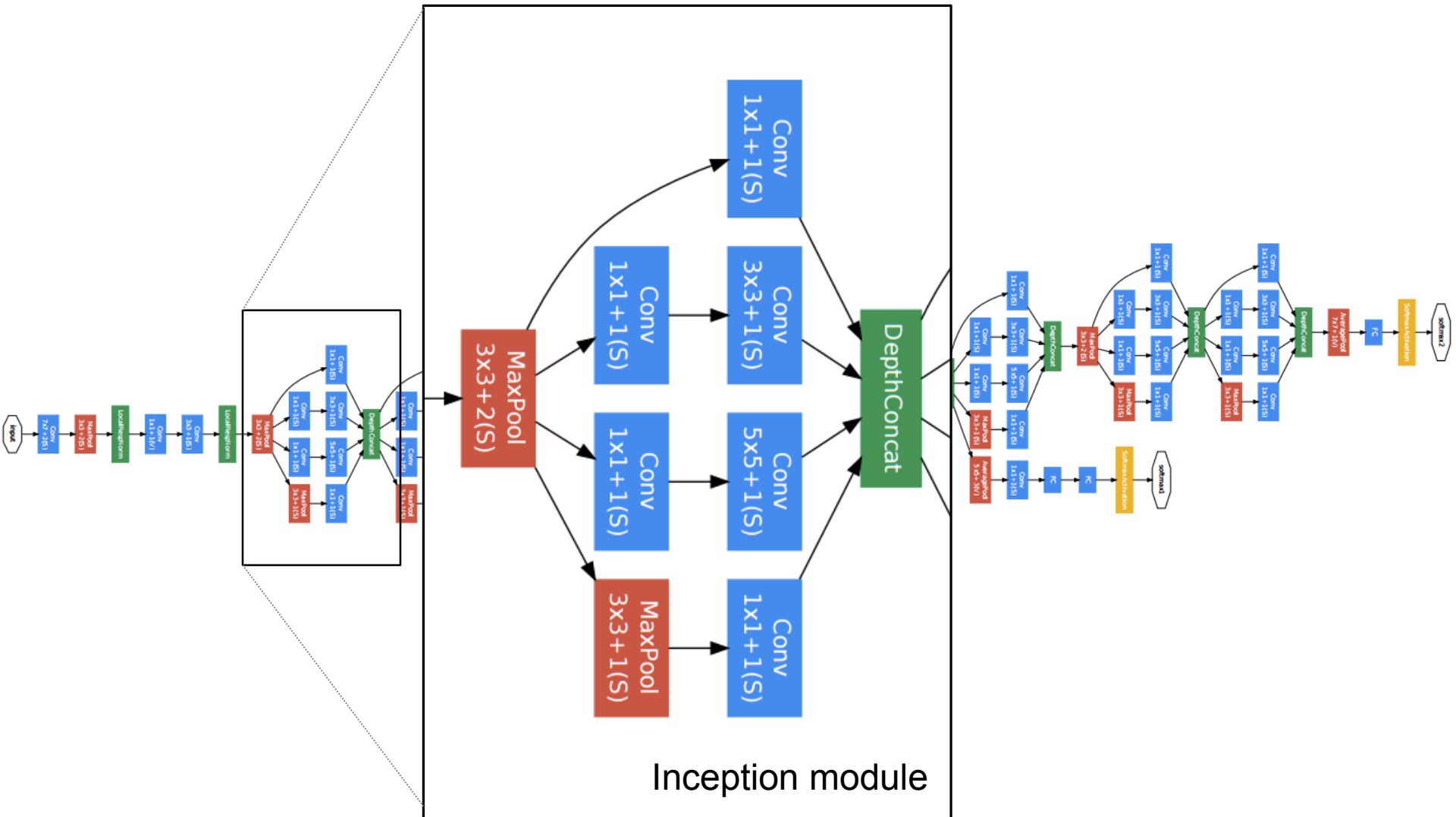


Figure from Going deeper with convolutions by *C. Szegedy et al.*

Case study: GoogLeNet (2014)

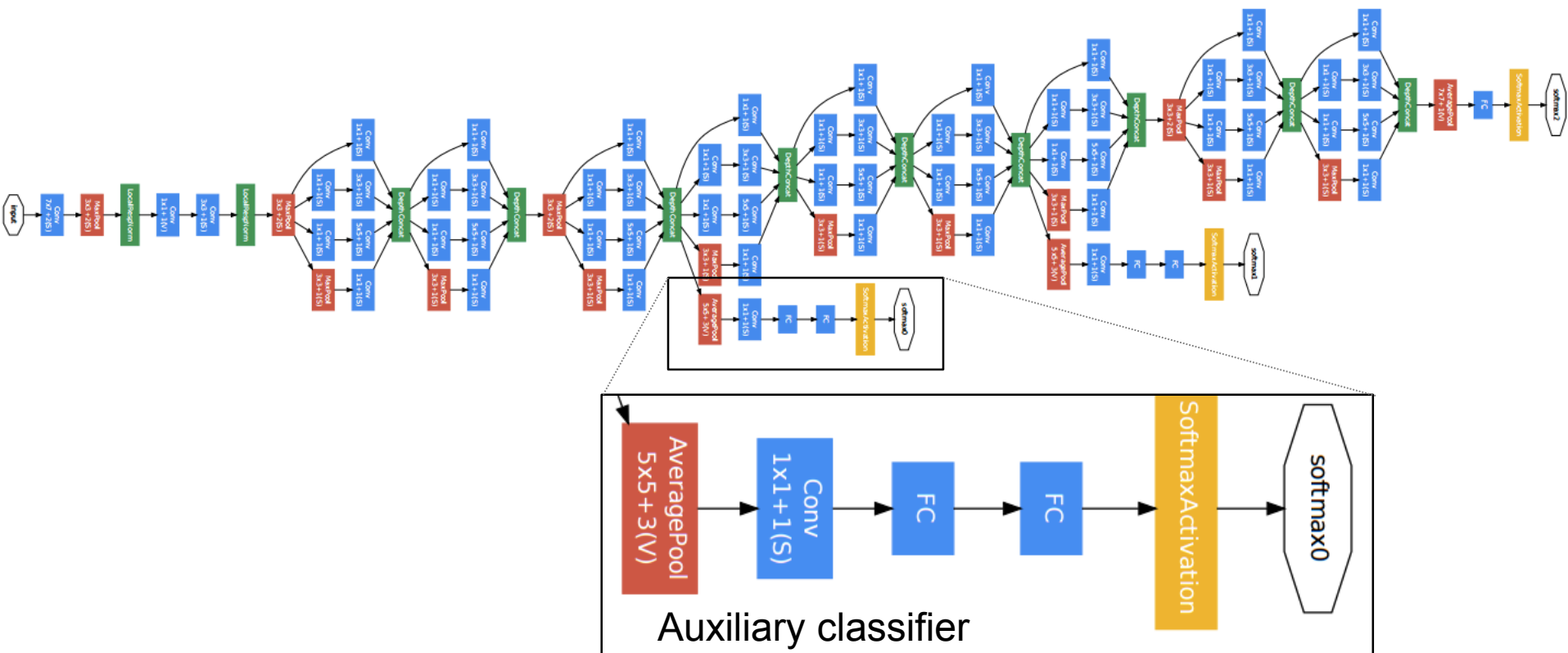


Figure from Going deeper with convolutions by C. Szegedy et al.

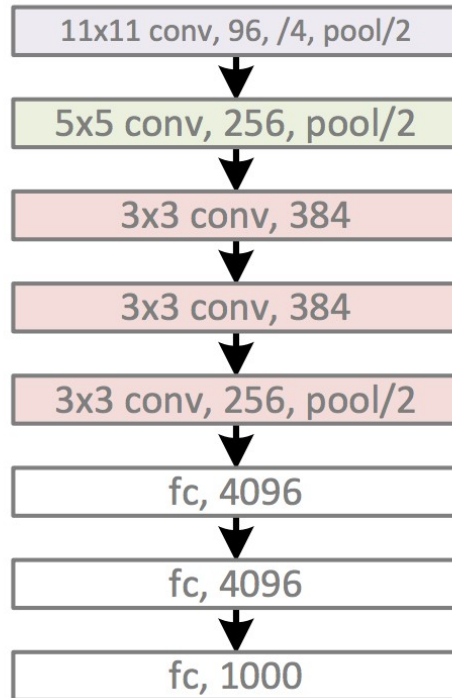
ImageNet challenge 2012-2014

| Team | Year | Place | Error (top-5) | External data |
|-------------------------------------|------|-------|---------------|---------------|
| SuperVision – Toronto (8 layers) | 2012 | - | 16.4% | no |
| SuperVision | 2012 | 1st | 15.3% | ImageNet 22k |
| Clarifai – NYU (7 layers) | 2013 | - | 11.7% | no |
| Clarifai | 2013 | 1st | 11.2% | ImageNet 22k |
| VGG – Oxford (16/19 layers) | 2014 | 2nd | 7.32% | no |
| GoogLeNet (22 layers) | 2014 | 1st | 6.67% | no |
| Human expert* | | | 5.1% | |

Convolutional networks: depth

Revolution of Depth

AlexNet, 8 layers
(ILSVRC 2012)

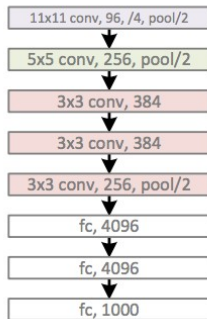


Kaiming He, Xiangyu Zhang, Shaoqing Ren, & Jian Sun. "Deep Residual Learning for Image Recognition". arXiv 2015.

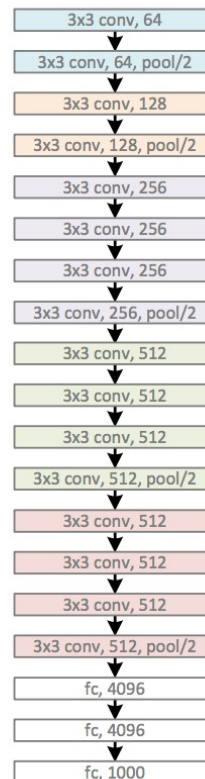
Convolutional networks: depth

Revolution of Depth

AlexNet, 8 layers
(ILSVRC 2012)



VGG, 19 layers
(ILSVRC 2014)



GoogleNet, 22 layers
(ILSVRC 2014)



Kaiming He, Xiangyu Zhang, Shaoqing Ren, & Jian Sun. "Deep Residual Learning for Image Recognition". arXiv 2015.

Case study: ResNet (2015)

AlexNet, 8 layers
(ILSVRC 2012)



VGG, 19 layers
(ILSVRC 2014)



Case study: ResNet (2015)

AlexNet, 8 layers
(ILSVRC 2012)



VGG, 19 layers
(ILSVRC 2014)



ResNet, 152 layers
(ILSVRC 2015)

- Winner of ImageNet challenge 2015



**I WAS WINNING
IMAGENET**



**UNTIL A
DEEPER MODEL
CAME ALONG**

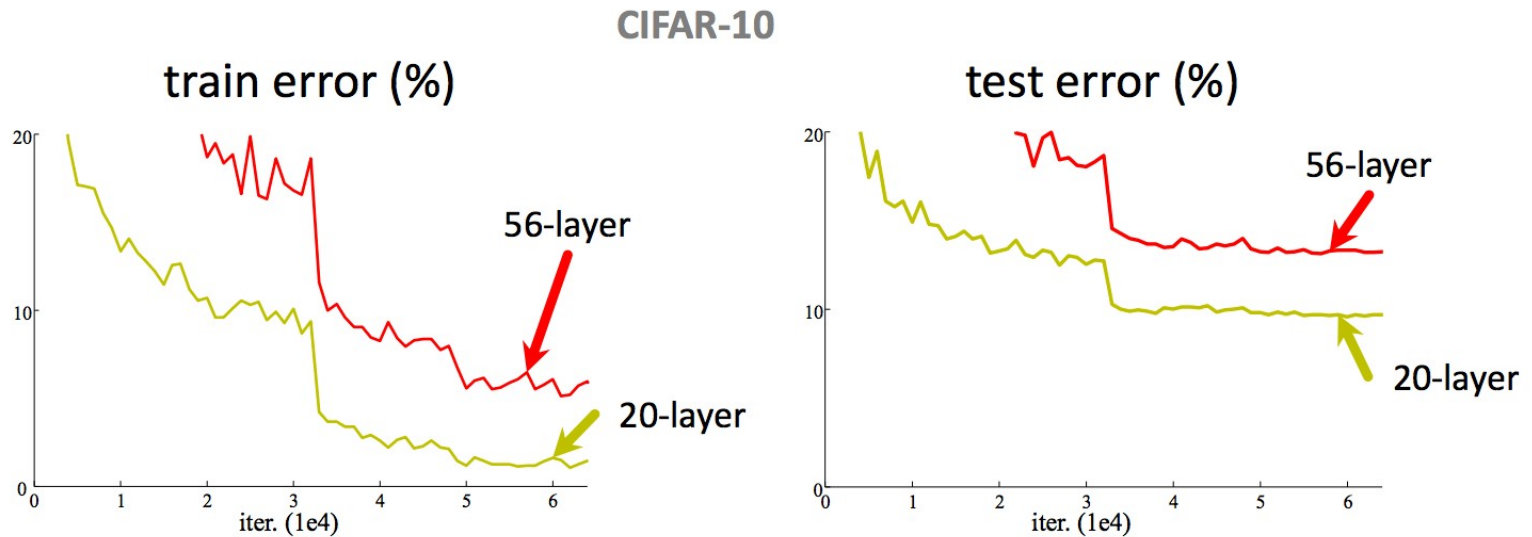
imgflip.com

[Source \(?\)](#)

slide 43

Convolutional networks: depth

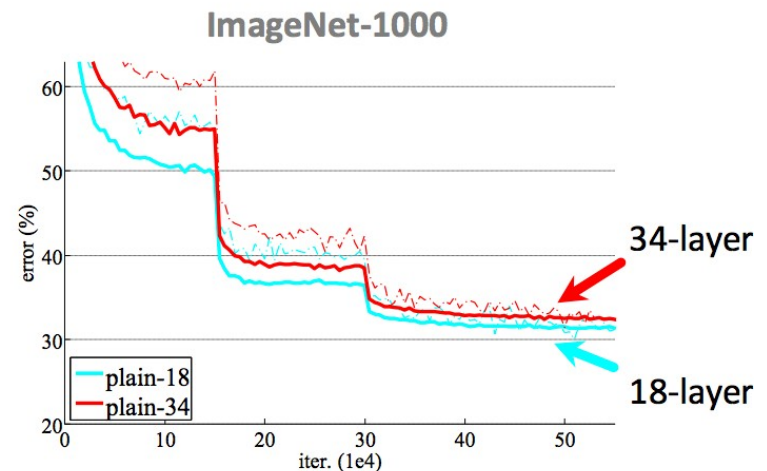
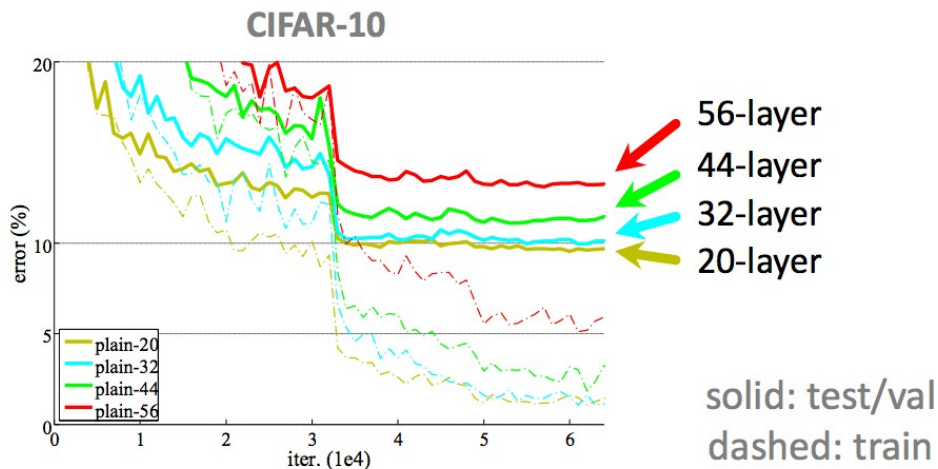
Simply stacking layers?



- *Plain* nets: stacking 3x3 conv layers...
- 56-layer net has **higher training error** and test error than 20-layer net

Convolutional networks: depth

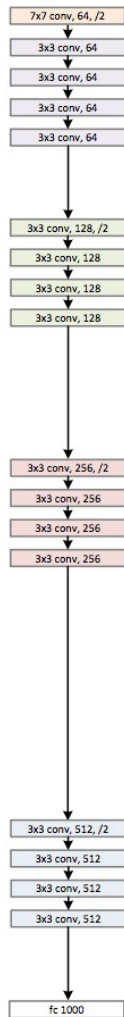
Simply stacking layers?



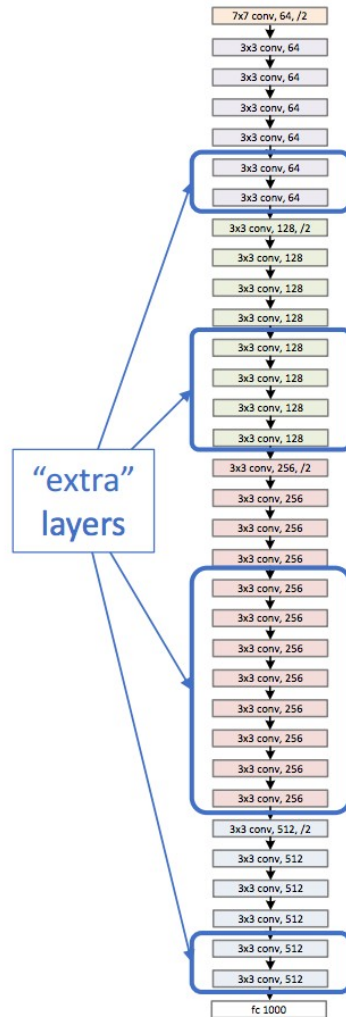
- “Overly deep” plain nets have **higher training error**
- A general phenomenon, observed in many datasets

Convolutional networks: depth

a shallower model
(18 layers)



a deeper counterpart
(34 layers)

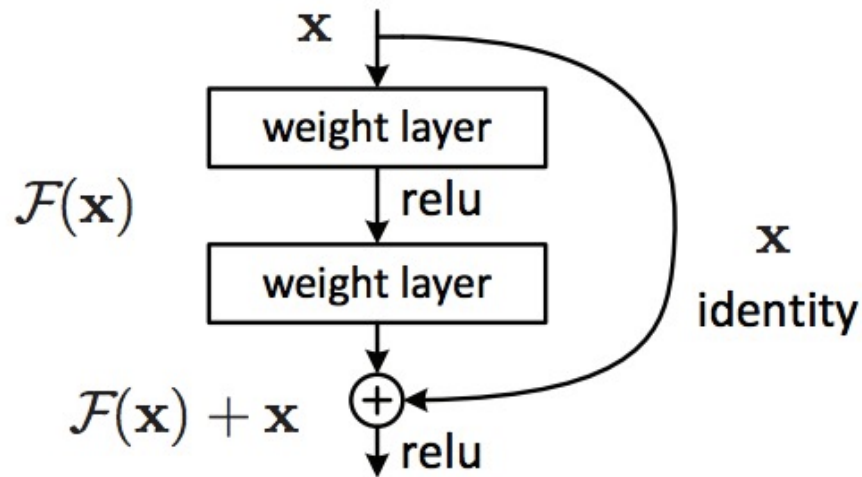


- A deeper model should not have **higher training error**
- A solution *by construction*:
 - original layers: copied from a learned shallower model
 - extra layers: set as **identity**
 - at least the same training error
- **Optimization difficulties**: solvers cannot find the solution when going deeper... *e.g., Gradient vanishing?*

Kaiming He, Xiangyu Zhang, Shaoqing Ren, & Jian Sun. "Deep Residual Learning for Image Recognition". arXiv 2015.

Case study: ResNet (2015)

- The residual module
 - Introduce *skip* or *shortcut* connections (existing before in various forms in literature)
 - Make it easy for network layers to represent the identity mapping
 - Also produce better gradients during training



Case study: ResNet (2015)

- Architectures for ImageNet:

| layer name | output size | 18-layer | 34-layer | 50-layer | 101-layer | 152-layer |
|------------|-------------|---|---|---|--|--|
| conv1 | 112×112 | 7×7, 64, stride 2 | | | | |
| | | 3×3 max pool, stride 2 | | | | |
| conv2_x | 56×56 | $\begin{bmatrix} 3 \times 3, 64 \\ 3 \times 3, 64 \end{bmatrix} \times 2$ | $\begin{bmatrix} 3 \times 3, 64 \\ 3 \times 3, 64 \end{bmatrix} \times 3$ | $\begin{bmatrix} 1 \times 1, 64 \\ 3 \times 3, 64 \\ 1 \times 1, 256 \end{bmatrix} \times 3$ | $\begin{bmatrix} 1 \times 1, 64 \\ 3 \times 3, 64 \\ 1 \times 1, 256 \end{bmatrix} \times 3$ | $\begin{bmatrix} 1 \times 1, 64 \\ 3 \times 3, 64 \\ 1 \times 1, 256 \end{bmatrix} \times 3$ |
| conv3_x | 28×28 | $\begin{bmatrix} 3 \times 3, 128 \\ 3 \times 3, 128 \end{bmatrix} \times 2$ | $\begin{bmatrix} 3 \times 3, 128 \\ 3 \times 3, 128 \end{bmatrix} \times 4$ | $\begin{bmatrix} 1 \times 1, 128 \\ 3 \times 3, 128 \\ 1 \times 1, 512 \end{bmatrix} \times 4$ | $\begin{bmatrix} 1 \times 1, 128 \\ 3 \times 3, 128 \\ 1 \times 1, 512 \end{bmatrix} \times 4$ | $\begin{bmatrix} 1 \times 1, 128 \\ 3 \times 3, 128 \\ 1 \times 1, 512 \end{bmatrix} \times 8$ |
| conv4_x | 14×14 | $\begin{bmatrix} 3 \times 3, 256 \\ 3 \times 3, 256 \end{bmatrix} \times 2$ | $\begin{bmatrix} 3 \times 3, 256 \\ 3 \times 3, 256 \end{bmatrix} \times 6$ | $\begin{bmatrix} 1 \times 1, 256 \\ 3 \times 3, 256 \\ 1 \times 1, 1024 \end{bmatrix} \times 6$ | $\begin{bmatrix} 1 \times 1, 256 \\ 3 \times 3, 256 \\ 1 \times 1, 1024 \end{bmatrix} \times 23$ | $\begin{bmatrix} 1 \times 1, 256 \\ 3 \times 3, 256 \\ 1 \times 1, 1024 \end{bmatrix} \times 36$ |
| conv5_x | 7×7 | $\begin{bmatrix} 3 \times 3, 512 \\ 3 \times 3, 512 \end{bmatrix} \times 2$ | $\begin{bmatrix} 3 \times 3, 512 \\ 3 \times 3, 512 \end{bmatrix} \times 3$ | $\begin{bmatrix} 1 \times 1, 512 \\ 3 \times 3, 512 \\ 1 \times 1, 2048 \end{bmatrix} \times 3$ | $\begin{bmatrix} 1 \times 1, 512 \\ 3 \times 3, 512 \\ 1 \times 1, 2048 \end{bmatrix} \times 3$ | $\begin{bmatrix} 1 \times 1, 512 \\ 3 \times 3, 512 \\ 1 \times 1, 2048 \end{bmatrix} \times 3$ |
| | 1×1 | average pool, 1000-d fc, softmax | | | | |
| FLOPs | | 1.8×10^9 | 3.6×10^9 | 3.8×10^9 | 7.6×10^9 | 11.3×10^9 |

ImageNet challenge 2012-2016

| Team | Year | Place | Error (top-5) | External data |
|--|------|-------|---------------|---------------|
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| GoogLeNet (22 layers) | 2014 | 1st | 6.67% | no |
| ResNet (152 layers) | 2015 | 1st | 3.57% | |
| Human expert* | | | 5.1% | |

Summary: Deep Convolutional Networks

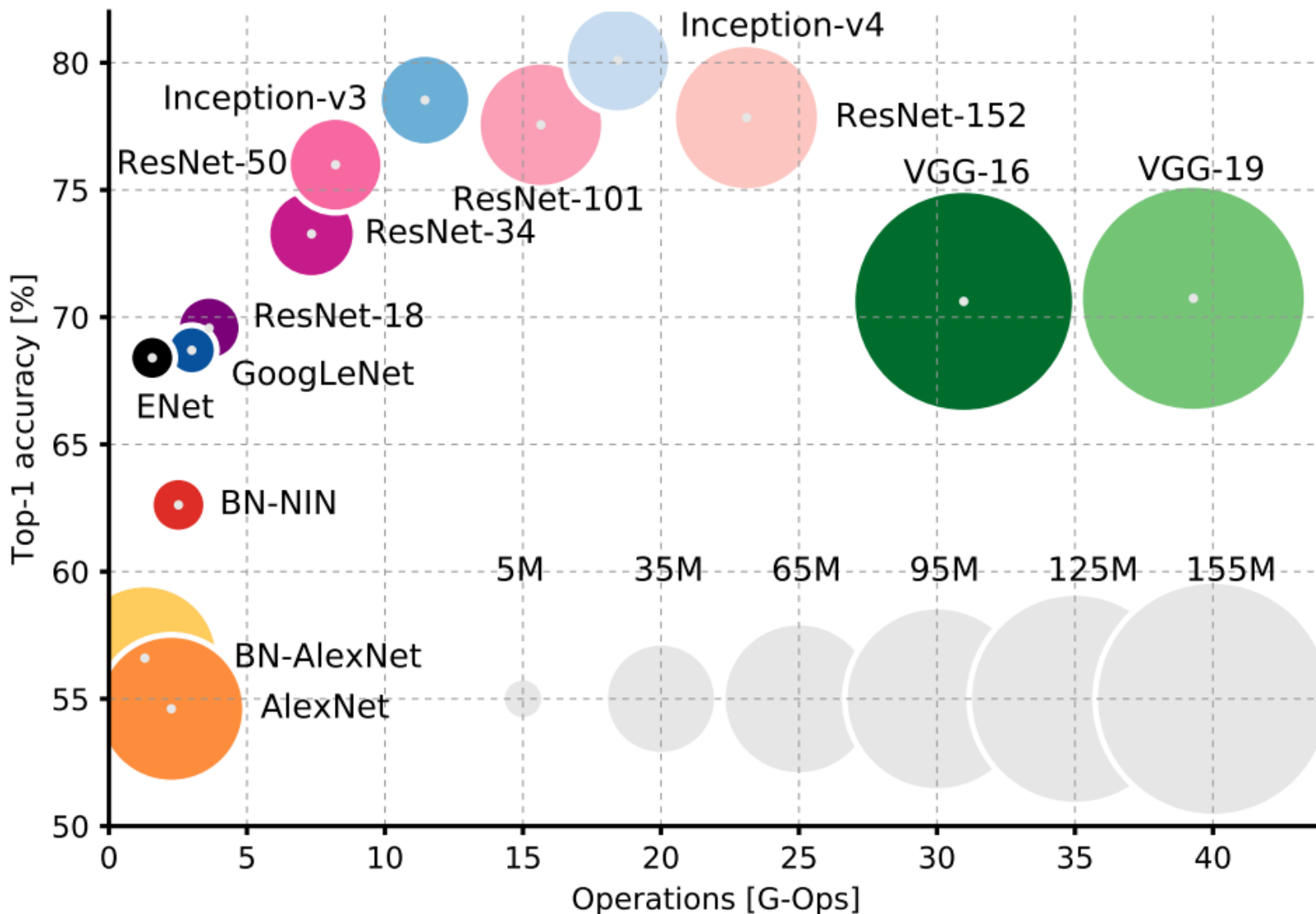


Figure from An Analysis of Deep Neural Network Models for Practical Applications by A. Canziani, A. Paszke, E. Culurciello