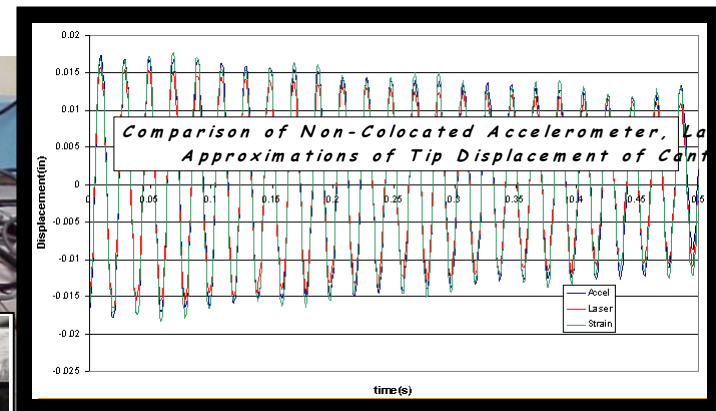
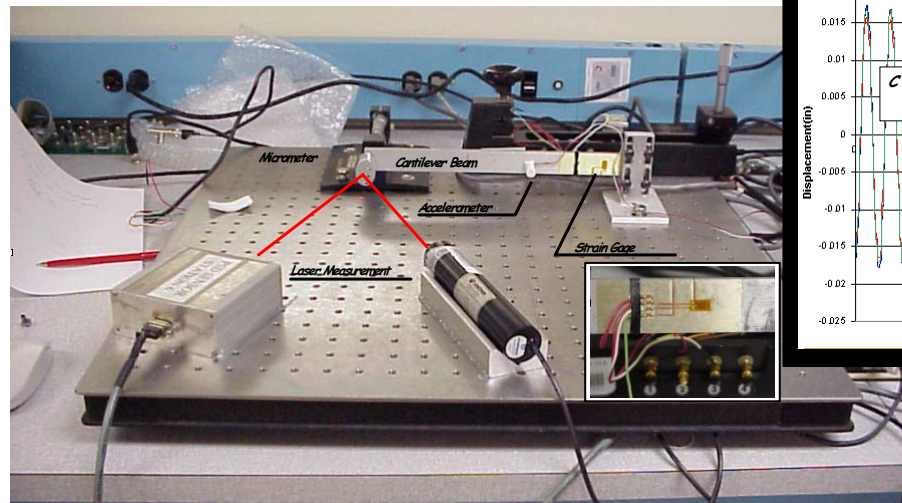




# DEVELOPMENT OF A MEASUREMENT SYSTEM FOR RESPONSE OF A SECOND ORDER DYNAMIC SYSTEM



*Dr. Peter Avitabile, Charles Goodman, Tracy Van Zandt  
Mechanical Engineering Department  
University of Massachusetts Lowell*





*Students rarely have the opportunity to make detailed measurements as part of their undergraduate curriculum*

*Laboratory experiments are an excellent opportunity for students to provide real-world practical solutions to problems that may not have an "answer at the back of the book".*





*Students must be afforded the experience of problems that require them to formulate solutions to problems with no specific straight-line structure to the solution*

*They must learn how to "think outside the box"*

*Students learn best with hands-on projects and problems with practical purpose*





*In laboratory courses, students are expected to understand and comprehend all of the pre-requisite STEM material.*

*Laboratory courses generally have some review material to summarize the basic underlying theory and methodology required for particular laboratories.*

*The laboratory course can then concentrate on various measurement techniques.*





*At UMASS Lowell, the laboratory courses are taught in a two semester sequence.*

*The first semester concentrates mainly on*

- basic measurement tools (oscilloscopes, multimeters, digital data acquisition, etc),*
- measuring devices (flow meters, manometers, pressure transducers, pitot tubes, strain gages, thermocouples, accelerometers, LVDTs, etc)*
- methods for data collection/reduction (regression analysis, curvefitting, numerical processing)*





*At UMASS Lowell, the laboratory courses are taught in a two semester sequence.*

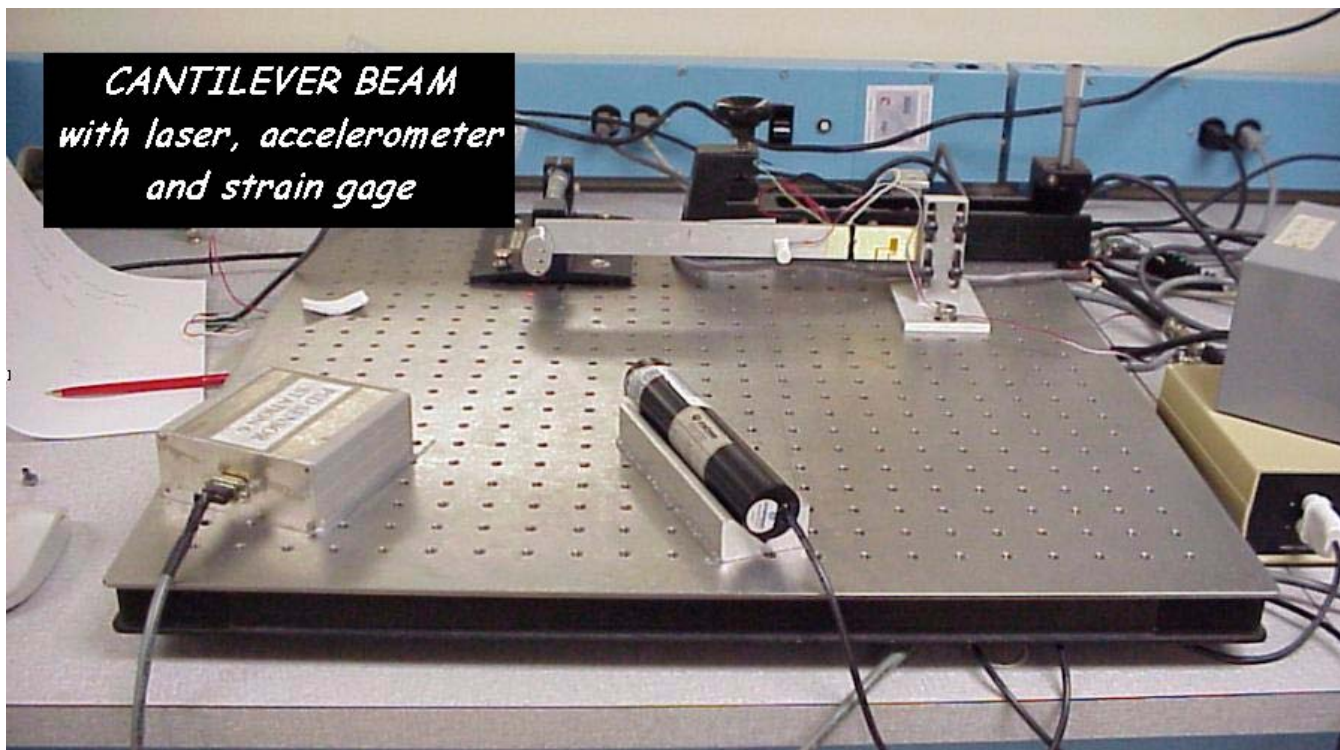
*The second semester is split into two halves*

- first half continues the more structured lab environment but introduces more complicated labs*
- second half of the semester concentrates on the student development of a measurement system*





## Development of a Measurement System to Characterize a 2<sup>nd</sup> Order Dynamic System





## *General guidelines given:*

- required to select three non-located different measurement devices from LVDT, accelerometer, laser, eddy current probes, and strain gages*
- determine suitable locations for the transducers, identify digital data acquisition requirements, etc.*
- determine the "best" method to address problem*
- ultimately predict dynamic response of the beam*







# Phase I - Brainstorming

*First step take usually involves:*

- *determine what transducers are available*
- *issues of location, resolution, dynamic range*
- *struggle with concepts of spatial correlation of non-colocated devices*
- *consideration for comparing acceleration, displacement, strain and velocity measurements*





## *Phase II - Thinking is Required!*

*Initially students believe all they need to do is*

- make some measurements*
- calibrate transducers*
- write a final report*

*Ahhh - If life could be so easy !!!*





# *I don't remember taking that course*

## *An intermediate phase*

- *pulling hair out*

*Students MUST struggle with difficult concepts in order to appreciate and understand the basic STEM material taught in previous courses*



*STEM - Science, Technology, Engineering and Math*



# Phase II - Thinking is Required!

*You mean we have to know stuff from other course*

*Professor, why didn't you tell us that the material covered at the beginning of the semester was going to be really important for the labs we did ?*

*Hmmmmm...*

*Student views material in a disjointed fashion*

*Professor clearly sees how pieces fit together*



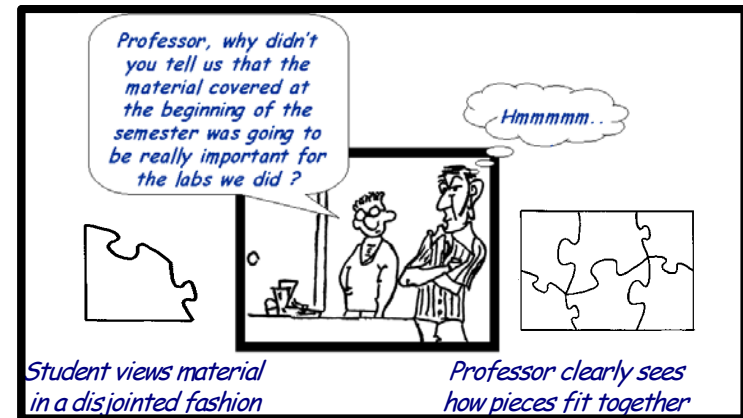


## Phase II - Thinking is Required!

*So those others courses we took are important !!!*

*The problem requires an understanding of*

- statics*
- strength of materials*
- dynamic systems*
- numerical methods*
- ordinary differential equations*
- and others ...*





## *Phase II a - He's got to be kidding!*

*Some typical student comments heard in the hallways provide amusement for the professor*

- Hey --- I thought this was just a lab course*
- Why do I need to use and know all this other stuff from these other courses?*
- I thought you were only allowed to ask me to do things that are related to lab???*
- I wonder if we can protest this through the student council*





## *Phase III - Analysis*

*Analytical models can be developed to address various aspects of the assessment to be performed*

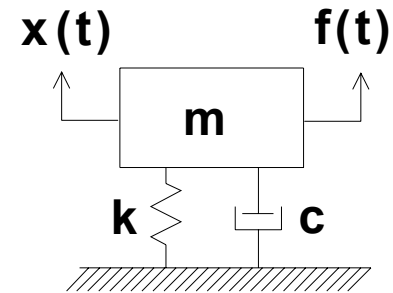
*Some material from previous courses contain material that are building blocks to the solution of this problem*

*MATLAB and Simulink are tools that assist in the development of an analytical model along with MATHCAD and spreadsheet tools*





*The beam can be modeled in an equivalent sense*

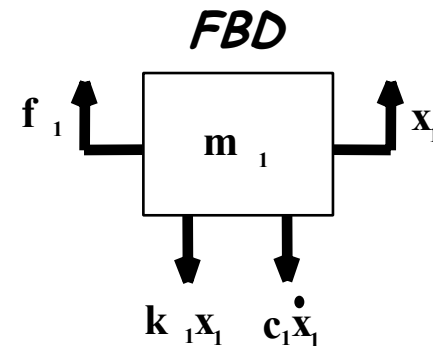


*Homogenous equation is*

$$m\ddot{x} + c\dot{x} + kx = 0$$

*and assuming an exponential solution form gives*

$$(ms^2 + cs + k)e^{st} = 0$$

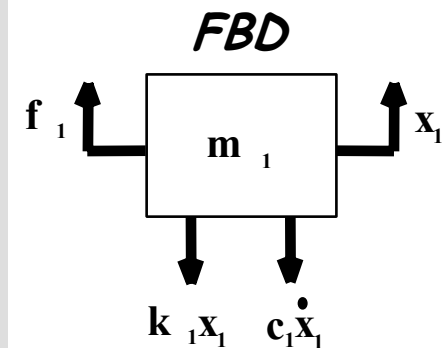
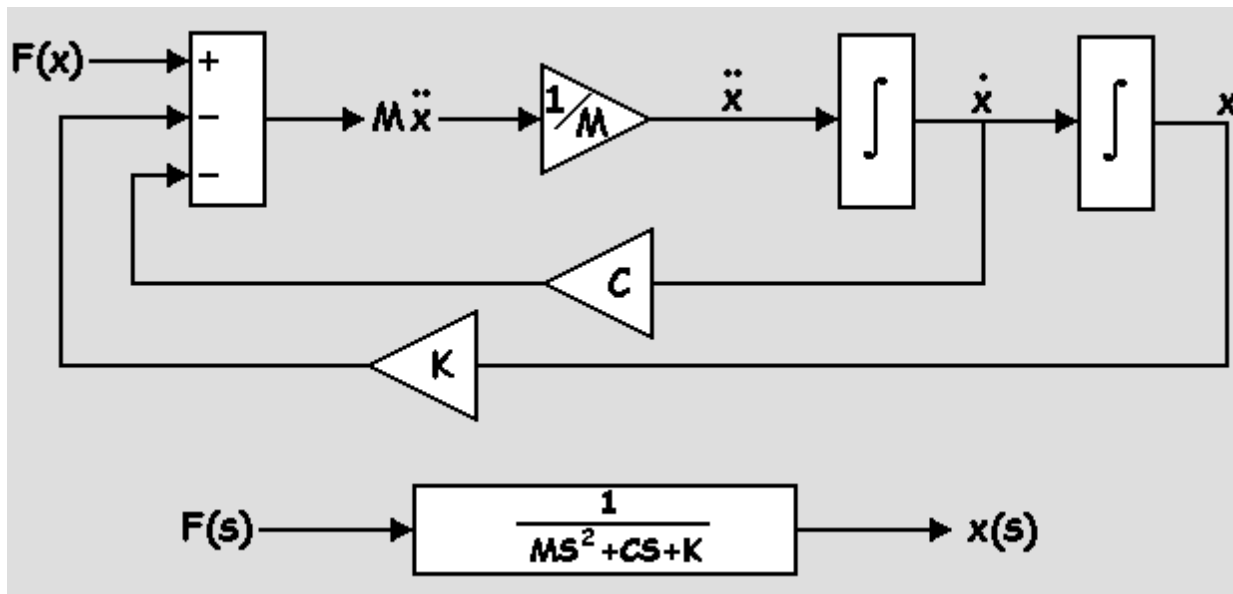






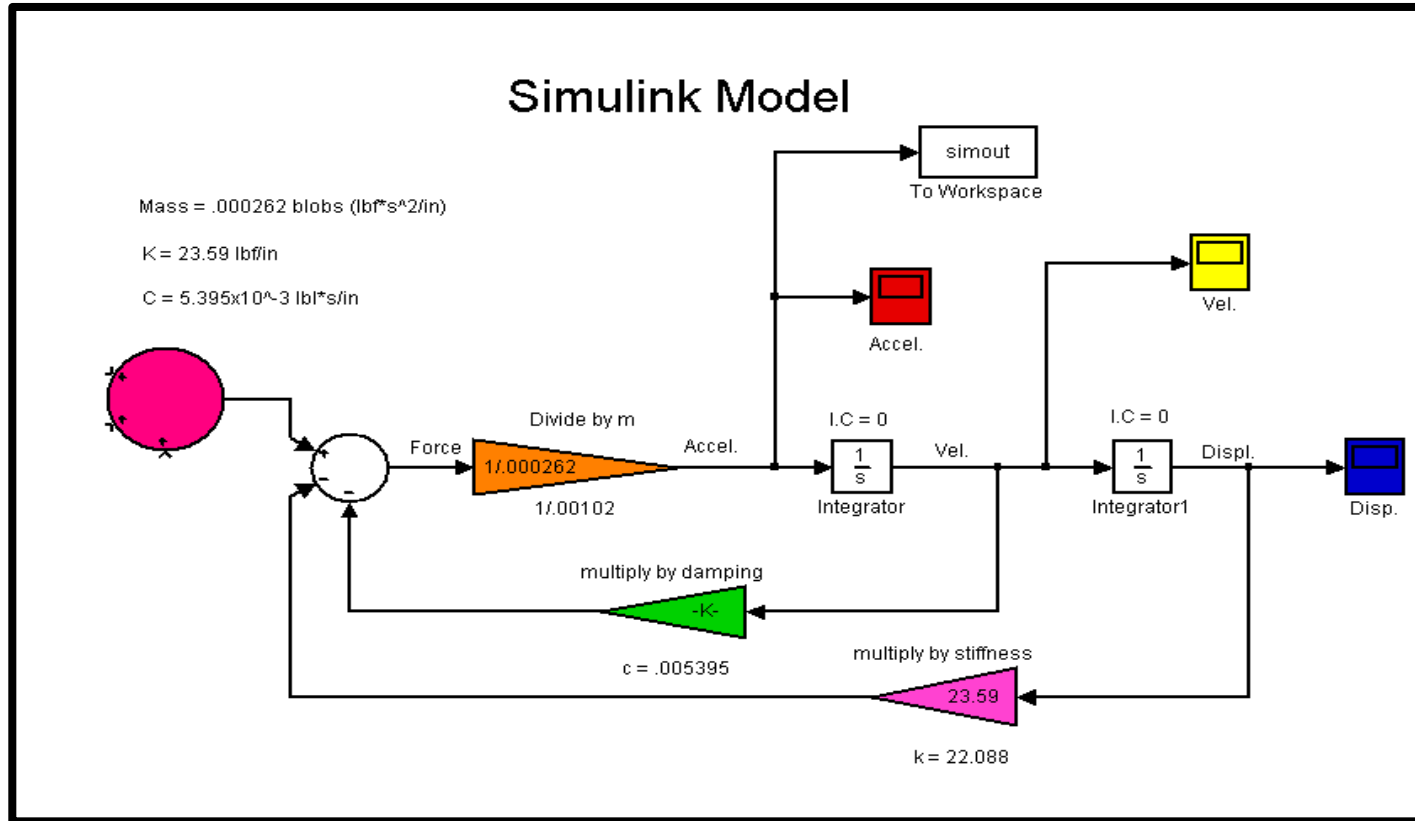
# Phase III - Analysis

The system can be modeled in block diagram form



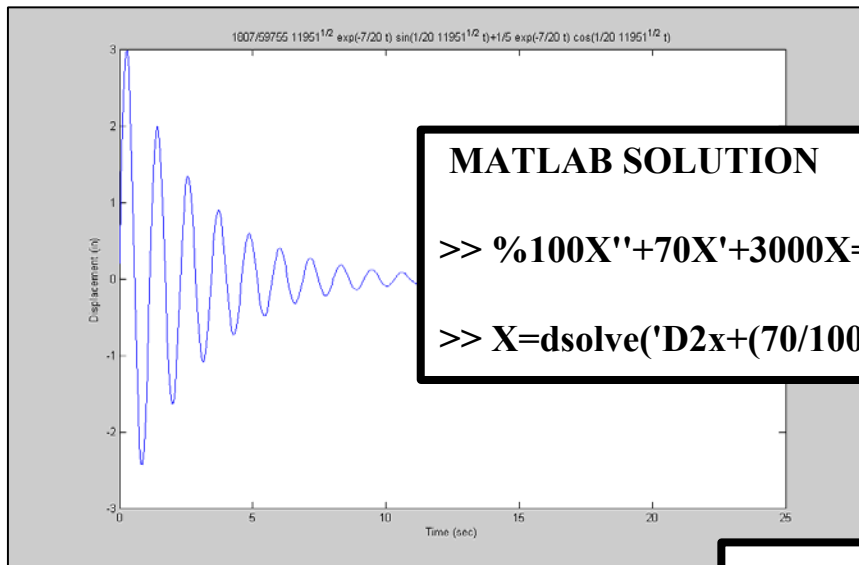


# Phase III - Analysis





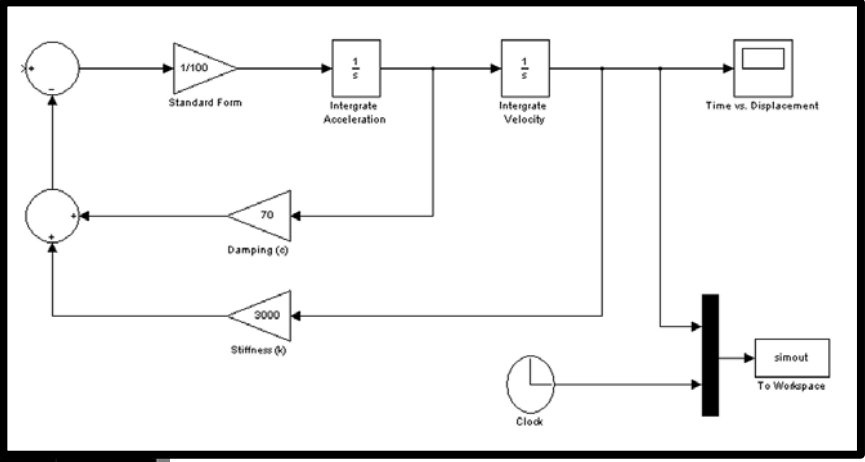
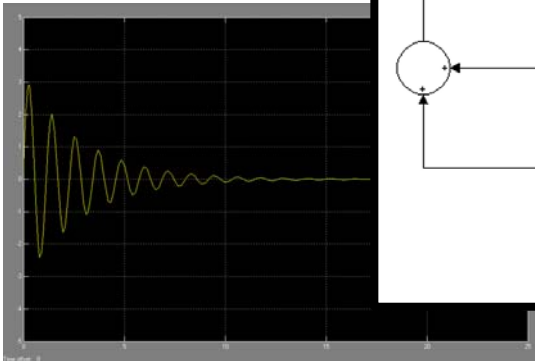
# Phase III - Analysis



**MATLAB SOLUTION**

```
>> %100X''+70X'+3000X=f(t)   where: X(0)=.2 X'(0)=18 f(t)=0
>> X=dsolve('D2x+(70/100)*Dx+(3000/100)*x=0','Dx(0)=18','x(0)=.2','t')
```

## SIMULINK SOLUTION





## *Phase III - Analysis*

*Analytical models are developed to identify the spatial response characteristics of displacement, velocity and acceleration that are "expected" to be observed on the system.*

*This assists in the specification of transducers required - at particular locations - that provide sufficient voltage - to optimize the ADC of the data acquisition system*

*WOW - there's a lot to this problem!*





## *Phase IV - Measurement Issues*

*Analytical models are great but the lab environment is riddled with other contaminates*

- measurement problems (noise, DC bias, drift)*
- digital data acquisition (quantization errors, sampling rate, AC coupling, etc)*
- numerical processing (integration/differentiation)*





## *Phase V - The Real Work Begins*

DYNAMIC  
SYSTEMS

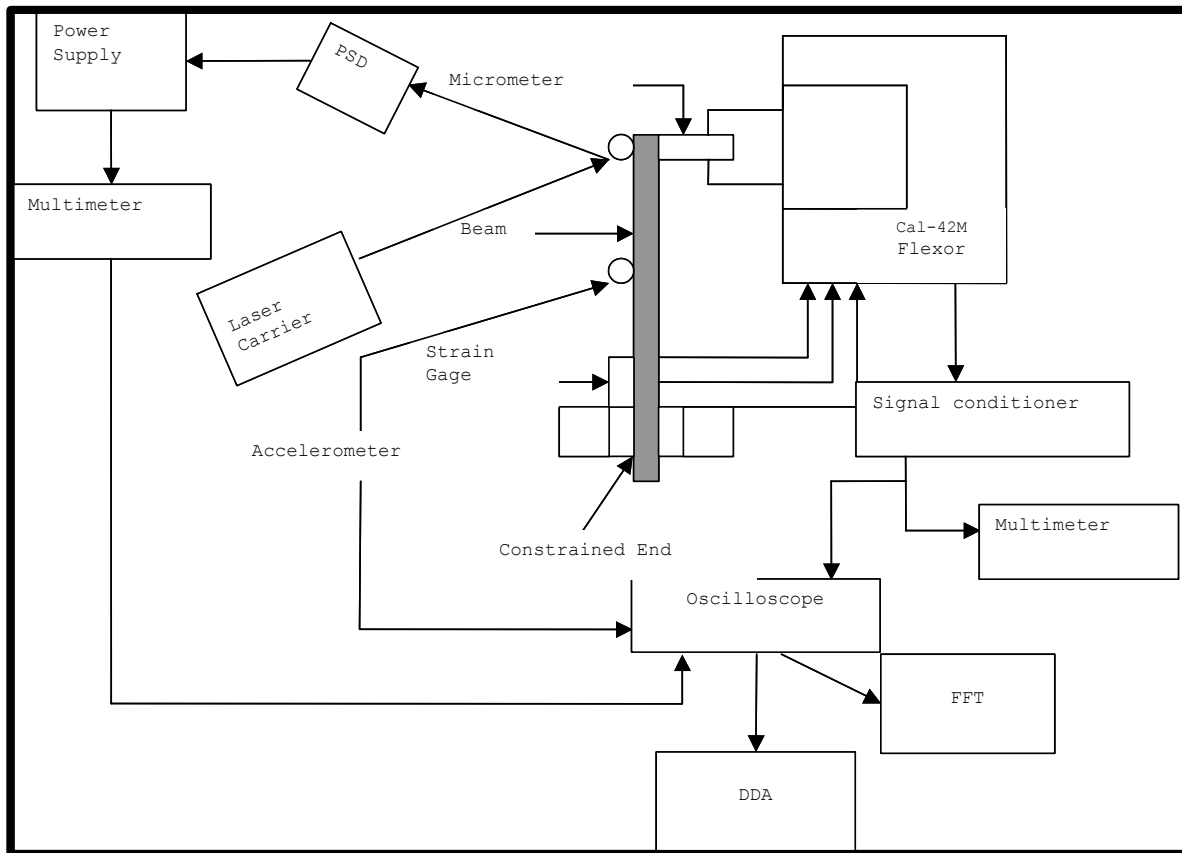
### *Issues to be addressed*

- *calibration of all transducers selected*
- *model beam and verify frequency response*
- *filter noise - analog or digital filter*
- *correlate responses from non-colocated positions*





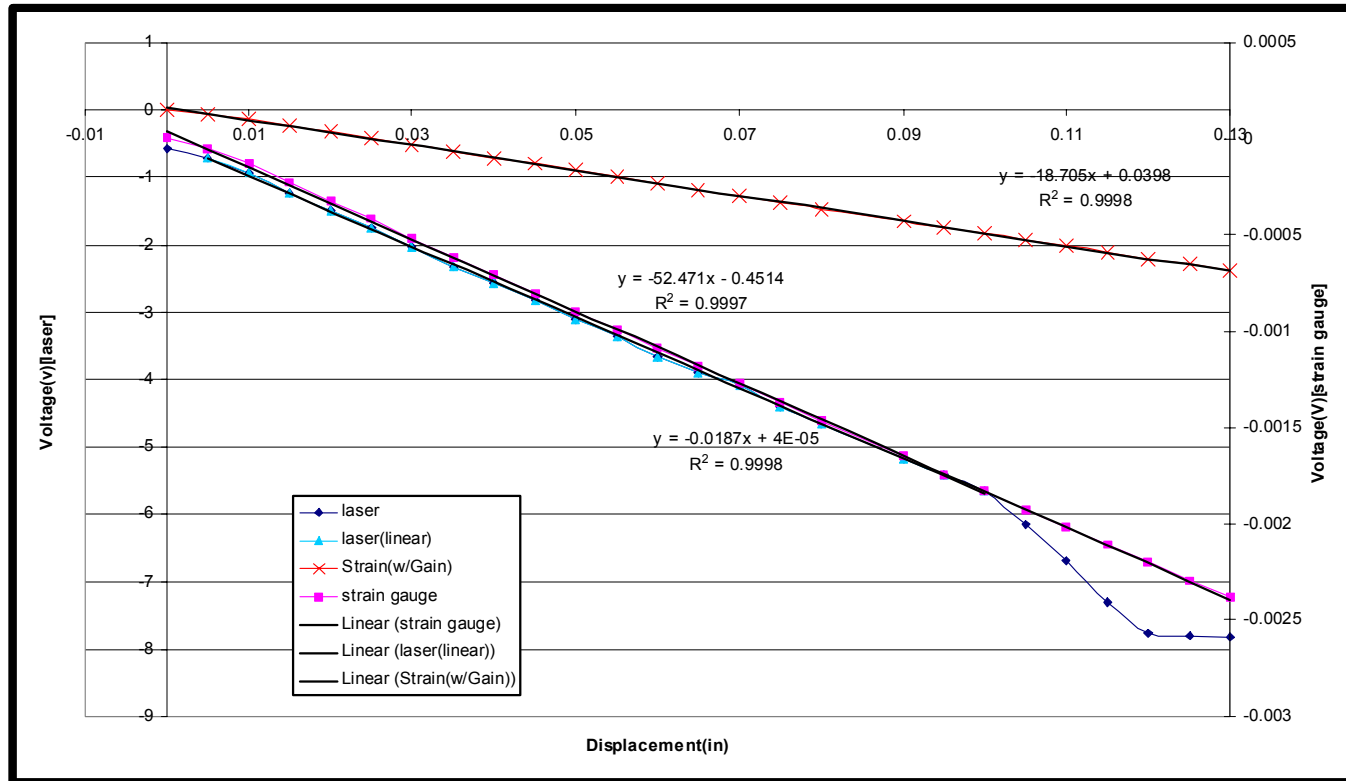
## Selection and layout of instrumentation





# Phase V - The Real Work Begins

## Calibration of transducers

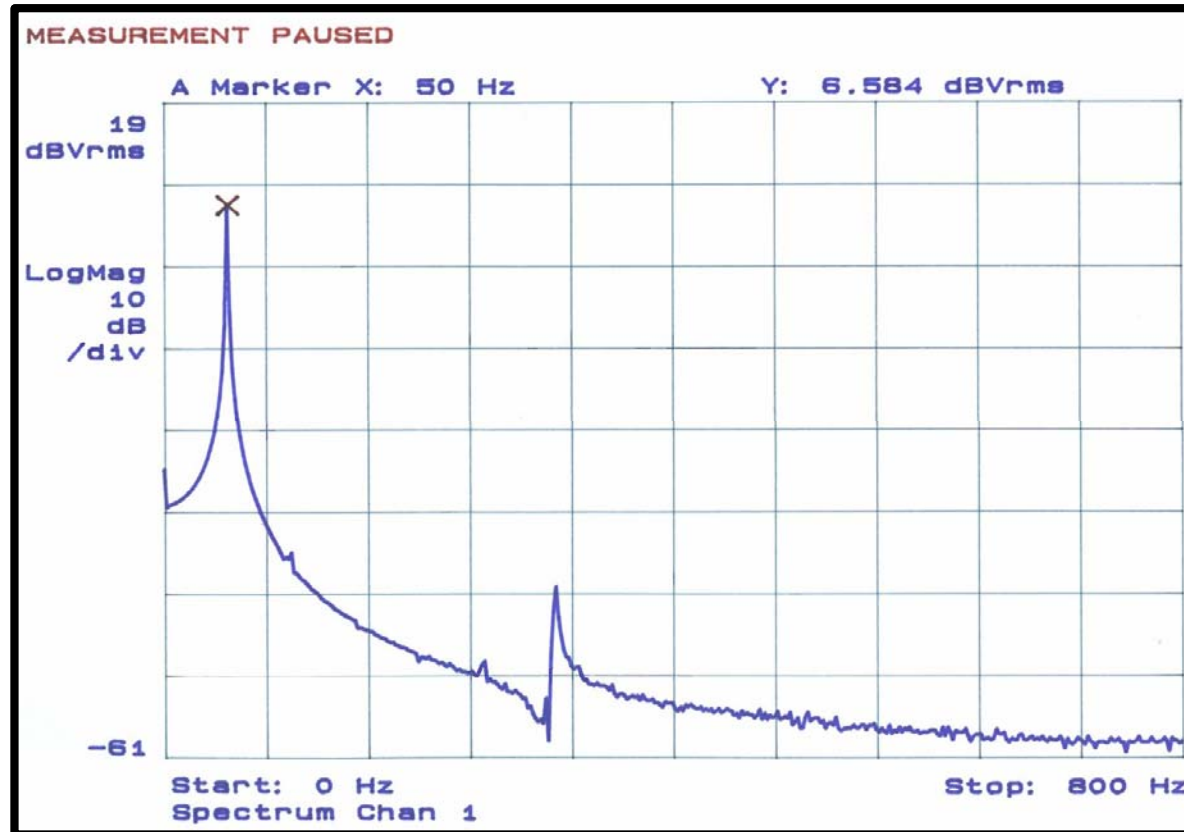






# Phase V - The Real Work Begins

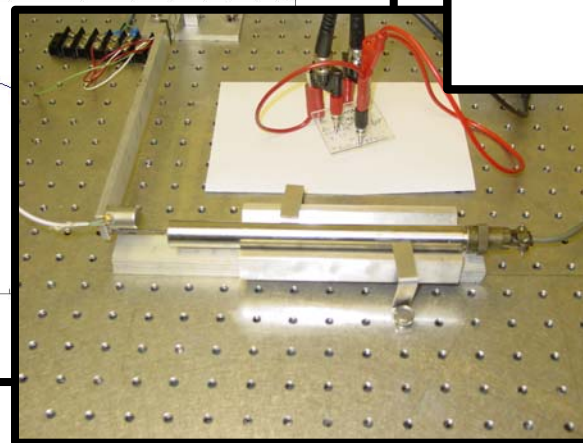
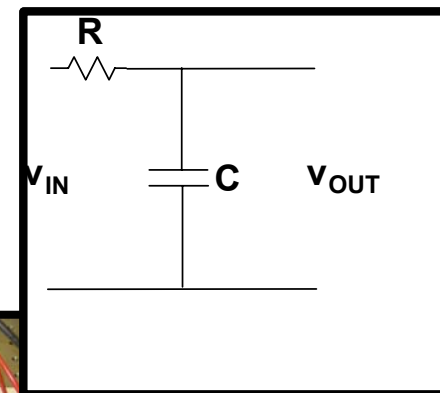
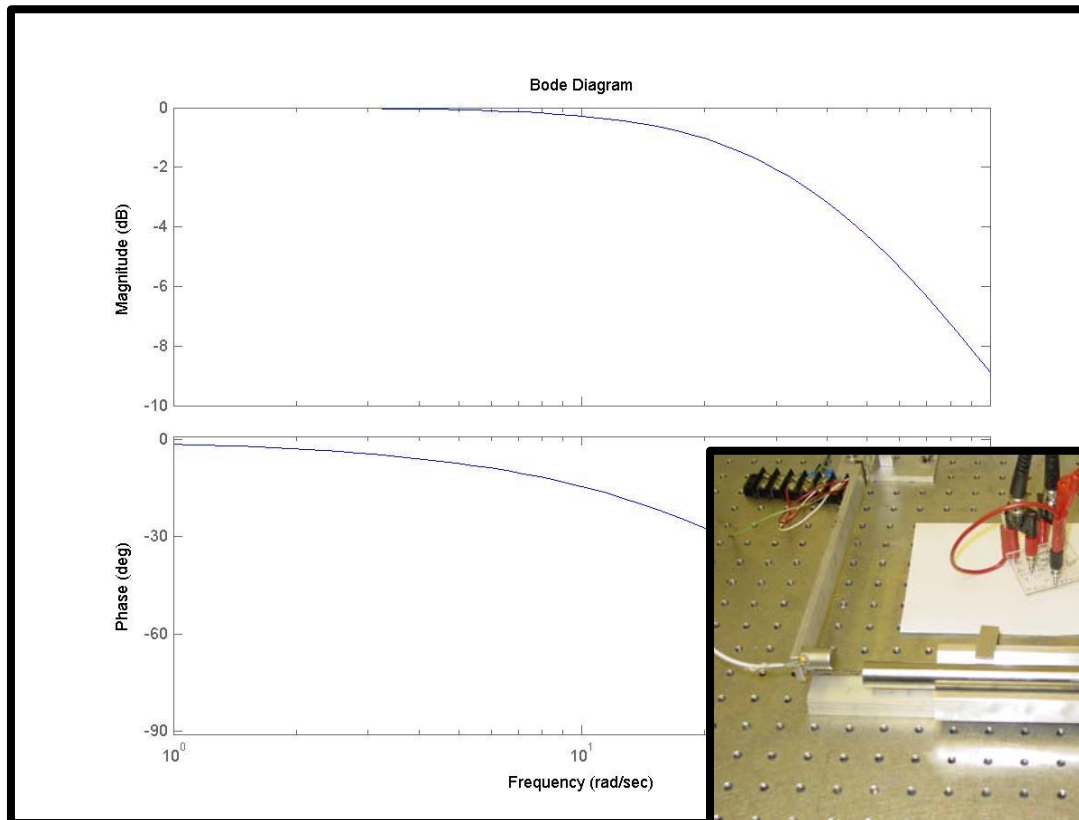
## Frequency response verification





# Phase V - The Real Work Begins

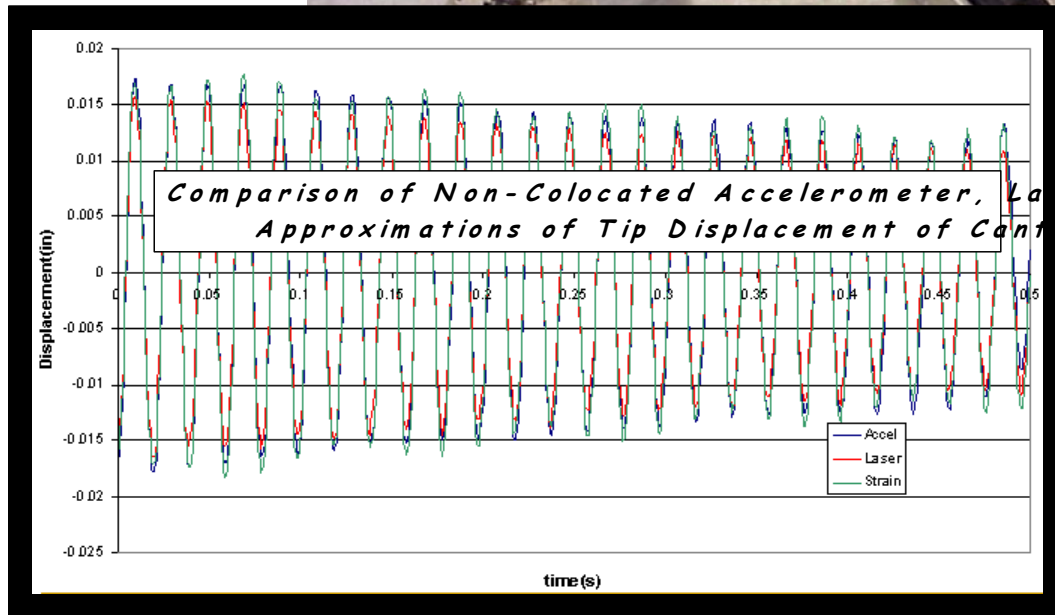
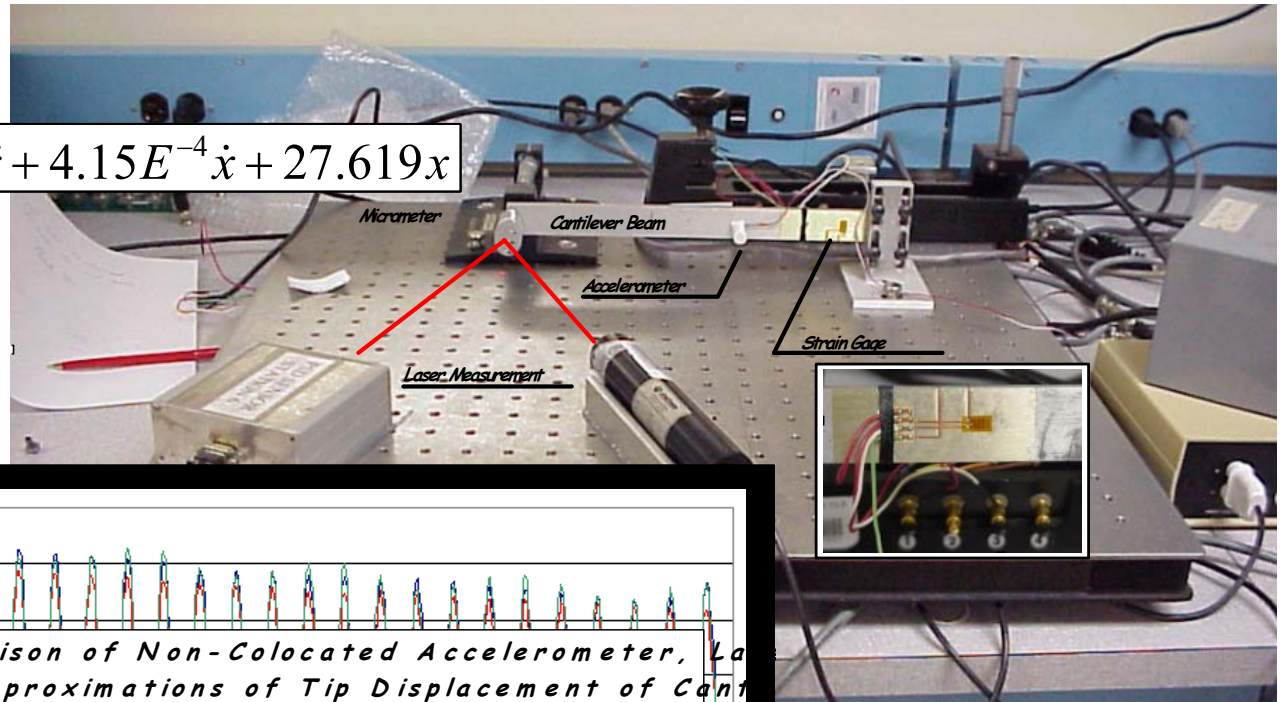
## Noise filter - design RC circuit





# Phase V - Results Achieved

$$2.96E^{-4}\ddot{x} + 4.15E^{-4}\dot{x} + 27.619x$$





*This project has been integrated into the second semester of the Mechanical Engineering laboratory for several years now.*

*The students are seniors when taking this required course and generally have had supporting courses*

*Dynamic Systems and Numerical Methods where dynamic models have been evaluated using tools such as MATLAB and Simulink*





*Laboratory time for each group is limited to 3 to 4 hour slots, once a week.*

*Students must do substantial "pre-work" to optimize their time available in the lab.*

*Usually 2 to 3 setups available for the AM and PM laboratory time slots, two days a week (normally Tuesday and Thursday lab times).*

*Additional time can be scheduled upon request*

*Students advised to utilize their time efficiently.*





*Project lasts 5 weeks at the end of the semester*

*Students work in teams of 3 to 4 people*

*Meet once a week with their professor to provide status, problems encountered, items to be performed next, etc.*

*Meetings conducted in an "employee/ supervisor" styled interaction.*





*Students need to organize their material and budget time in order to complete the project.*

*The professor's role is mainly to supervise and mentor the group.*

*A full format report is generated and an oral presentation is given.*





*The students generally learn a tremendous amount of material in an integrated fashion to solve this problem. The task is not trivial.*

*The students generally enjoy the laboratory-based, hands-on project.*

*The real measurements tend to help the students clearly understand the need for basic STEM material to solve real engineering problems.*







## Summary

*A complete measurement system is designed to obtain the response of a second order mechanical system.*

*Students work in teams to measure the dynamic response at the tip of a cantilever beam using three non-colocated measurement devices.*

*Models are developed using spreadsheet calculations, MATLAB and/or SIMULINK to aid in the determination of the dynamic system response and provide a baseline for the expected results.*





## Summary

*The students select three measurement devices from five possible types of transducers (including LVDT, accelerometer, laser, eddy current probe, and strain gage) and determine suitable locations for the transducers on the beam.*

*They must consider signal type, transducer sensitivity, etc. to provide the "maximum" signal for the ADC to be used for data acquisition.*





## Summary

*The non-colocated measurements are then spatially adjusted and integrated/differentiated to predict the tip displacement and acceleration of the cantilever beam.*

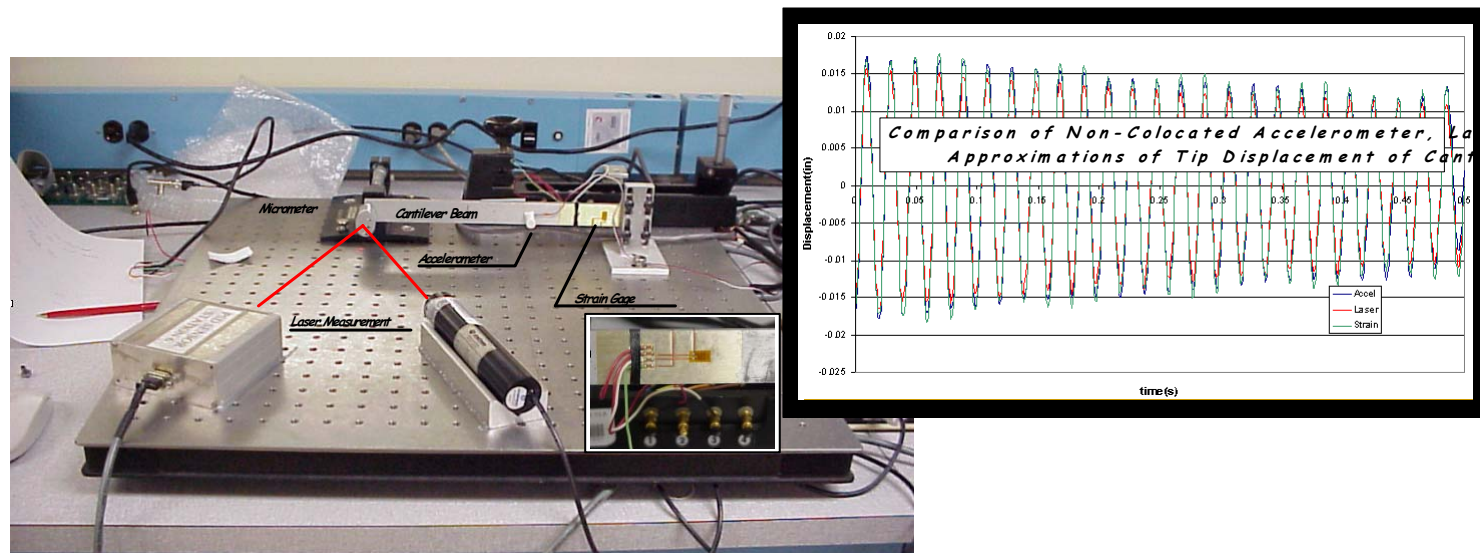
*A full formal report is prepared to document all aspects of the project effort along with a formal presentation.*





# Outcome - Better Overall Understanding

## DEVELOPMENT OF A MEASUREMENT SYSTEM FOR RESPONSE OF A SECOND ORDER DYNAMIC SYSTEM



*Dr. Peter Avitabile, Charles Goodman, Tracy Van Zandt  
Mechanical Engineering Department  
University of Massachusetts Lowell*

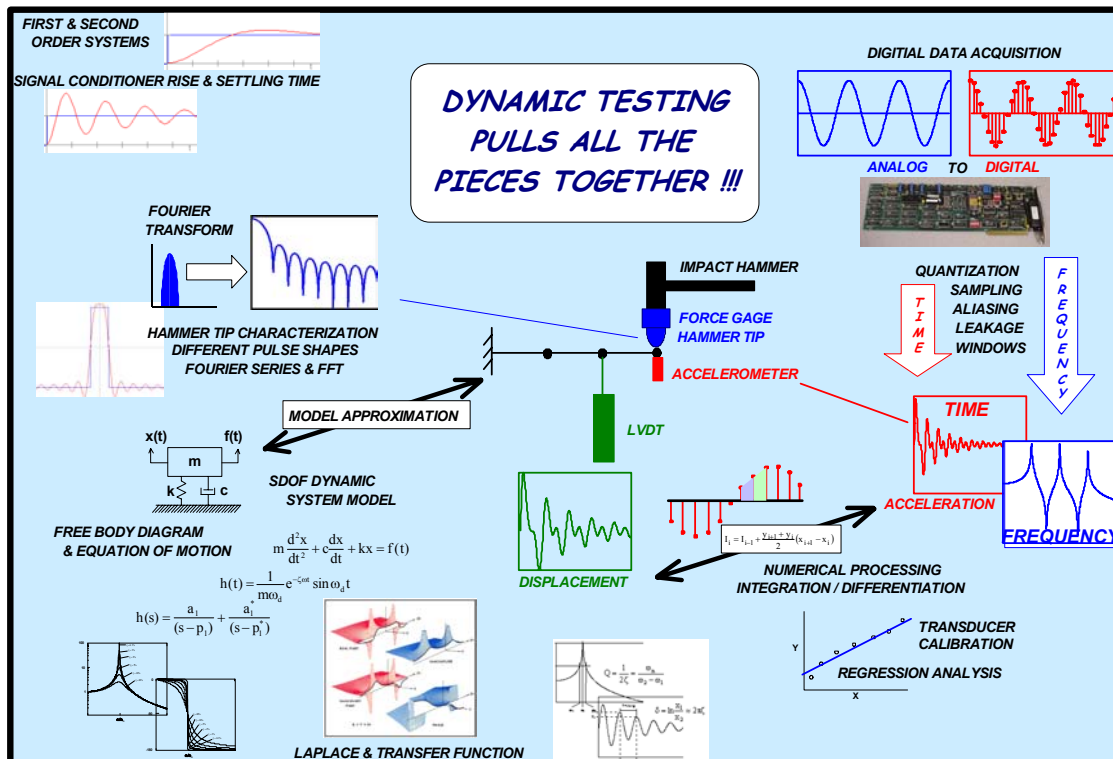




# Acknowledgements

*This project is partially supported by NSF Engineering Education Division Grant EEC-0314875*

*Multi-Semester Interwoven Project for Teaching Basic Core STEM Material Critical for Solving Dynamic Systems Problems*



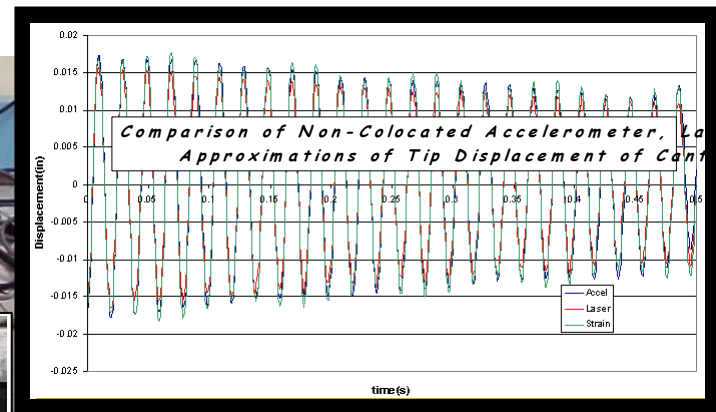
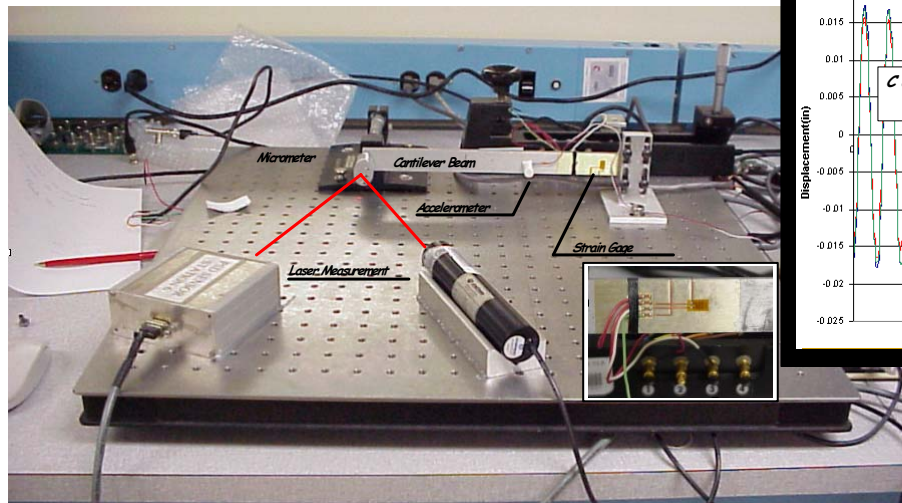
*Peter Avitabile, John White, Stephen Pennell*





# Outcome - Better Overall Understanding

## DEVELOPMENT OF A MEASUREMENT SYSTEM FOR RESPONSE OF A SECOND ORDER DYNAMIC SYSTEM



*Dr. Peter Avitabile, Charles Goodman, Tracy Van Zandt  
Mechanical Engineering Department  
University of Massachusetts Lowell*

