# ESSENTIAL EXERCISES 

 YEAR 3 WATHS
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NOTE: The New Australian National Curriculum has been split into 3 major strands:
(A) Number \& Algebra
(B) Measurement \& Geometry
© Statistics \& Probability

In the Year 3 content descriptions, these 3 major strands have been further subdivided into the sub-strands shown above.

## THE NEW NATIONAL AUSTRALIAN CURRICULUM

The authors acknowledge the dedicated work of the Australian Curriculum Assessment and Reporting Authority (ACARA), and the many who have contributed to the development of the Australian curriculum in response to the aims of the 2008 Melbourne declaration on Educational Goals for Young Australians.

This book provides a summary and interpretation of their guidelines for those interested in developing mathematical understanding in Year 3 students.

The Australian National Curriculum, developed by ACARA, states that, by the end of Year 3, students should be able to do the following:
$\square$ recall number facts for single digit numbers.
$\square$ be familiar with collections up to 10000 .
$\square$ describe number patterns involving addition and subtraction.
$\square$ recognise the connection between multiplication and division.
$\square$ model and represent unit fractions.
$\square$ count the change required and represent money values in various ways.
$\square$ compare objects using familiar units.
$\square$ compare angle sizes.
$\square$ identify symmetry.
$\square$ tell the time.
$\square$ interpret positions and pathways on maps.
$\square$ conduct chance experiments and describe the possible outcomes.
$\square$ create, interpret and compare data displays.
THE MATHEMATICS CURRICULUM OPERATES ON ANOTHER LEVEL, THE SO CALLED PROFICIENCY LEVEL.

The Proficiency strands at this level include:

1. Understanding: the connecting of number calculations with counting sequences, partitioning and counting numbers flexibly, identifying and describing the relationship between addition and subtraction and between multiplication and division.
2. Fluency: the counting of numbers in sequences readily, using units iteratively to compare measurements, listing possible outcomes of chance events, describing and comparing time durations.
3. Problem solving: this includes formulating problems from authentic situations, making models and using number sentences that represent problem situations, planning routes on maps, and matching transformations with their original shape.
4. Reasoning: using known facts to derive strategies for unfamiliar calculations, comparing and contrasting related models of operations, describing connections between 2-D and 3-D representations, and creating and interpreting simple representations of data.

Understanding, Fluency, Problem Solving and Reasoning are a central part of Mathematics content across the three major strands as mentioned earlier (Number and Algebra, Measurement and Geometry, and Statistics and Probability).

## NUMBER AND PLACE VALUE (Part 1)

The "Australian Curriculum Mathematics" (ACM) references for this sub-strand of "Number and Algebra" (NA) are below:

Investigate the conditions required for a number to be odd or even and identify odd and even numbers (ACMNA 051).

Recognise, model, represent and order numbers to at least 10000 (ACMNA 052).
Apply place value to partition, rearrange and regroup numbers to at least 10000 to assist calculations and solve problems (ACMNA 053).

## THE ABACUS

Originating from China, this is a device for counting numbers. In schools we use a simplified version, like the picture below, to show place value. Each spike represents a different place value, and we place counters on the spikes to show different numbers. The abacus on the right shows the number 2574.

## BASE TEN WOODEN BLOCKS

These are used in schools to represent ones (units), tens and hundreds and thousands. These blocks are available at most educational stores.

A single cube represents one unit and is referred to as a SHORT.
A row of ten cubes joined together represents ten and is called a LONG.

A raft of ten longs joined together represents one hundred (10 longs or 100 shorts) and is referred to as a FLAT.


A large cube made from 10 flats joined together represents one thousand (10 flats or 100 longs or 1000 shorts) and is called a BLOCK.


## NUMBER OR NUMERAL EXPANDERS

A number or numeral expander is a simple learning aid made out of paper, or light cardboard strips, which can show place value, and also how to name a number.

| 7 | Thousands | 3 | Hundreds | 8 | Tens | 2 | Ones |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

The expander above clearly shows the numeral 7382 .

## EVEN NUMBERS AND ODD NUMBERS

$2,4,6,8,10,12,14,16,18,20,22$, etc.
Even numbers always end in $2,4,6,8$, or 0 . $1,3,5,7,9,11,13,15,17,19,21$, etc.
Odd numbers always end in $1,3,5,7$, or 9 .


## PLACE VALUE

The value of a digit depends on its position or place in the numeral.
In $81 \underline{7} 4$ the 7 has the value of 7 tens $=70$.
In $814 \underline{7}$ the 7 has the value of 7 ones $=7$.
In $\underline{7} 814$ the 7 has the value of 7 thousands $=7000$.
In $4 \underline{718}$ the 7 has the value of 7 hundreds $=700$.


## SERIES

Discover the pattern and find the missing numbers.
120, 122, 124, 126,
$\square$
37, 42, 47, 52, $\square$


## EXPANDED NOTATION

This means to rewrite the number as an addition sentence using thousands, hundreds, tens, and units.
$7326=(7 \times 1000)+(3 \times 100)+(2 \times 10)+(6 \times 1)$
$5902=(5 \times 1000)+(9 \times 100)+(0 \times 10)+(2 \times 1)$

## ROUNDING OFF

In some situations in Maths, particularly when using a calculator, we do not require the exact answer, but an approximate answer only. The question will then ask you to ROUND OFF the given number to the nearest ten, nearest hundred or nearest thousand.

## Example:

If we round off 73 to the nearest ten, then the answer is 70 , because 73 is closer to 70 than it is to 80 . If we round off 659 to the nearest hundred, then the answer is 700 , because 659 is closer to 700 than it is to 600 .


## ESTIMATING

When using a calculator, you will be surprised how easy it is to press the wrong button and then get a ridiculous answer which is way out from the correct answer. If we quickly and mentally estimate an approximate answer to begin with, then this will prevent us from making careless blunders.

Estimate the answer to $469+1728$
Therefore estimate $=500+1700$

$$
=2200
$$



[^0]1. Shade the even numbers and cross out the odd numbers.

numbers and numbers than can't be divided by 2 are odd numbers.
2. Write the following as ordinary numerals.
a) Five hundred and seventy nine =
b) Two thousand, four hundred and thirty eight =
3. Order the numbers from smallest to largest.
a) $1035,627,2448,962,456$
b) $3258,1792,599,2871,836$
4. Write the largest possible numbers using the digits given.
a) 2, 3, $1 \mathrm{~m} \Rightarrow$ $\qquad$ b) $3,4,9 \mathrm{~m} \Rightarrow$ $\qquad$
5. Count the beads on each abacus and write the number in numerals and in words.

b)

d)


6. Write the number shown by the Base Ten blocks, and fill in the numeral expanders.


|  | Thousands |  | Hundreds | Tens | Ones |
| :--- | :--- | :--- | :--- | :--- | :--- |


|  | Thousands |  | Hundreds |  | Tens |
| :--- | :--- | :--- | :--- | :--- | :--- |
|  | Ones |  |  |  |  |

7. How many digits are there in each number? Write your answer on the line.
a) $13 \mathrm{~m} \Rightarrow$
b) $126 \mathrm{~m} \Rightarrow$
c) 649
d) $1587 \mathrm{~m} \Rightarrow$
8. Write the place value of the underlined digits.
a) $87 \mathrm{~m} \Rightarrow$
b) $369 \mathrm{~m} \Rightarrow$
c) $8 \underline{556 m}$
d) $1246 \mathrm{~m} \Rightarrow$
e) 2943 픅
f) $\underline{4} 513 \mathrm{~m}$
9. Write the following in numerals.
a) $(7 \times 10)+(8 \times 1)=$
b) $(2 \times 100)+(7 \times 10)+(5 \times 1)=$
c) $(1 \times 1000)+(3 \times 100)+(5 \times 10)+(4 \times 1)=$
d) $(3 \times 1000)+(6 \times 100)+(2 \times 10)+(8 \times 1)=$
10. Write the numerals below in expanded notation.
a) $84=$
b) $432=$
c) $1246=$
d) $2461=$
11. Is 36 closer to 30 or 40 ? 36 is closer to 40 , therefore it is rounded up to 40 . Try this! Round off the following numbers to the nearest 10 .
a) $48 \mathrm{~m} \Rightarrow$
b) $53 \mathrm{~m} \Rightarrow$
c) $74 \mathrm{~m} \Rightarrow$
d) 85 nm
e) $121 \mathrm{~m} \Rightarrow$
f) 639 mm

12. First, round off the numbers to the nearest 10, and then estimate the answers.
a) $34+17$
b) $\begin{array}{r}46 \\ \square \\ \square\end{array}$ Round off
 Round off
$\square$ Estimate $\square$ Estimate
 Estimate

## Level 2

1. Fill in the boxes with the next even numbers.
a) $12, \square$
b) $50, \square$
c) 234 ,

d) 890 , $\square$ e) 1256 , $\square$ f) 3578 ,
2. Fill in the boxes with the next odd numbers.
a) 21 , $\square$
b) 99, $\square$ c) 561, $\square$
d) 745 , $\square$ e) 2707

3. Use > OR < to compare the numbers.
a) $48 \square 39$
c) 372 $\square$ 427
b) 81
 97
d) 785 $\square$ 628
4. Write the smallest possible numbers using the given digits.
a) 5, 1, $3 \mathrm{~m} \Rightarrow$ $\qquad$ b) 4,2, 6 m
$\qquad$
5. Order the numbers from largest to smallest.
a) 3847,2 916, $5467,1929,6310$
b) $2850,5619,8374,4956,3798$
6. Write the numbers shown by the Base Ten blocks in numerals and in words.
a)



$\square$
b)

7. Draw the beads on the abacus using the number shown below each abacus, and fill in the numeral expanders.
a)

1563
b)

2748

| Thousands |  | Hundreds |  | Tens |  |
| :--- | :--- | :--- | :--- | :--- | :--- |


|  | Thousands |  | Hundreds |  | Tens |
| :--- | :--- | :--- | :--- | :--- | :--- |
|  | Ones |  |  |  |  |

8. Write the value of the underlined digits.
a) $\quad 720 \mathrm{~m} \Rightarrow$
b) $138 \underline{4} \mathrm{~m} \Rightarrow$
c) $55 \underline{6} 6 \mathrm{~m} \Rightarrow$
d) $\underline{2} 423 \mathrm{~mm}$
e) $9 \underline{475} \Rightarrow$
f) $\underline{7} 482 \mathrm{~m} \Rightarrow$
9. Write the numbers below as numerals.
a) $(9 \times 100)+(7 \times 10)+(3 \times 1)=$
b) $(2 \times 1000)+(8 \times 100)+(5 \times 10)+(4 \times 1)=$
c) $(4 \times 1000)+(2 \times 100)+(1 \times 10)+(8 \times 1)=$
d) $(6 \times 1000)+(1 \times 100)+(7 \times 10)+(5 \times 1)=$
10. Write the numbers below in expanded notation.
a) $1234=$
b) $3596=$
c) $4118=$
d) $7862=$
11. Is 135 closer to 100 or 200? 135 is closer to 100 , therefore it is rounded down to 100 .

## Try these!

Round off the following numbers to the nearest 100.

a) $160 \mathrm{~m} \Rightarrow$
b) $214 \mathrm{~m} \Rightarrow$
c) $475 \mathrm{~m} \Rightarrow$
d) 682 mm
e) $350 \mathrm{~m} \Rightarrow$
f) $1928 \mathrm{~m} \Rightarrow$
12. First, round off the numbers to the nearest 100, and then estimate the answers.
a) $224+369$
b) $473+192$
$\square$ Round Off $\square$ Round Off
Estimate
 These are the answers!

1. Shade the even numbers and cross out the odd numbers.


Remember! Numbers that can be divided by 2 are even numbers and numbers than can't be divided by 2 are odd numbers.
2. Write the following as ordinary numerals.
a) Five hundred and seventy nine $=579$
b) Two thousand, four hundred and thirty eight $=2438$
3. Order the numbers from smallest to largest.
a) $1035,627,2448,962,456$
b) $3258,1792,599,2871,836$
456, 627, 962, 1035,2448 599, 836, 1 792, 2 871, 3258
4. Write the largest possible numbers using the digits given.
a) 2, 3, $1 \mathrm{~m} \Rightarrow$ $\qquad$ b) $3,4,9 \Rightarrow$ 943
$\qquad$
5. Count the beads on each abacus and write the number in numerals and in words.
a)

c)


2119
b)

d)



[^0]:    (T)For further reference, see 'Understanding Year 3 Maths' by W. Marlin

