<u>EECS150 - Digital Design</u> <u>Lecture 23 - FSMs & Counters</u>

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State Encoding

- One-hot encoding of states. Ex: 3 States.
- One FF per state.

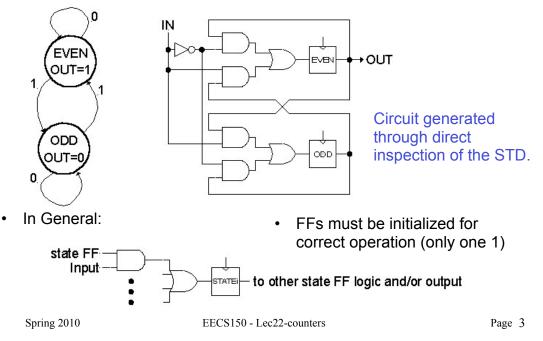
STATE1: 001 STATE2: 010 STATE3: 100 FF1 FF2 FF3

- Why one-hot encoding?
 - Simple design procedure.
 - Circuit matches state transition diagram (example next page).
 - Often can lead to simpler and faster "next state" and output logic.
- Why not do this?
 - Can be costly in terms of FFs for FSMs with large number of states.
- FPGAs are "FF rich", therefore one-hot state machine encoding is often a good approach.

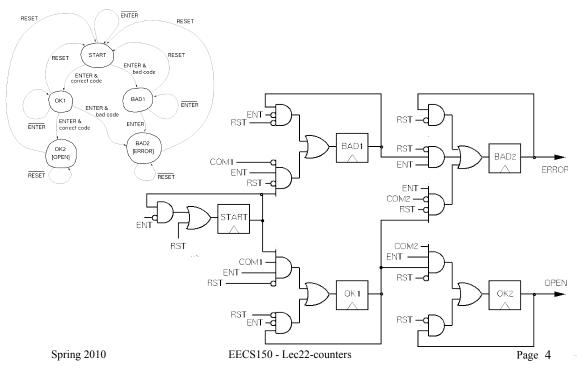
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One-hot encoded FSM

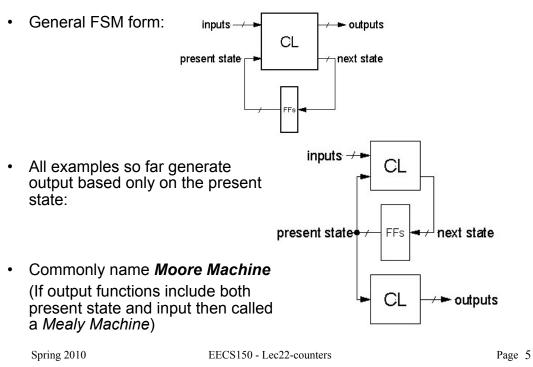
• Even Parity Checker Circuit:



One-hot encoded combination lock



FSM Implementation Notes

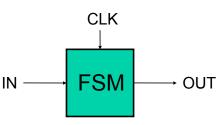


Finite State Machines

• Example: Edge Detector

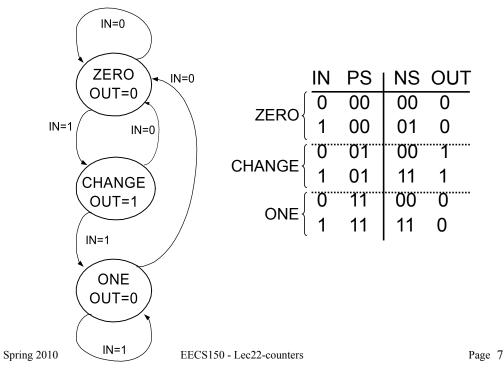
Bit are received one at a time (one per cycle), such as: $000111010 \longrightarrow time$

Design a circuit that asserts its output for one cycle when the input bit stream changes from 0 to 1.

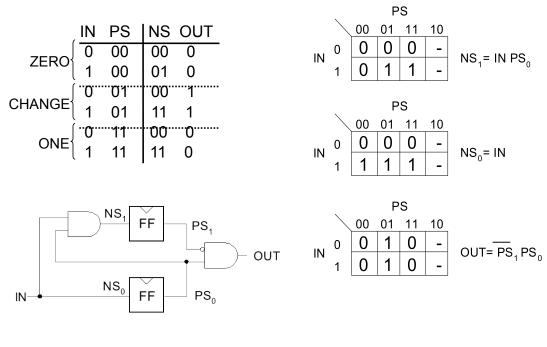


Try two different solutions.

State Transition Diagram Solution A

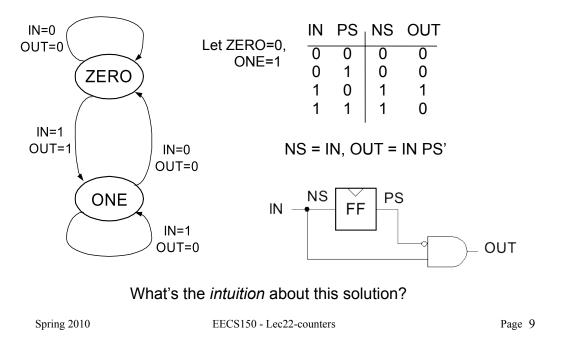


Solution A, circuit derivation

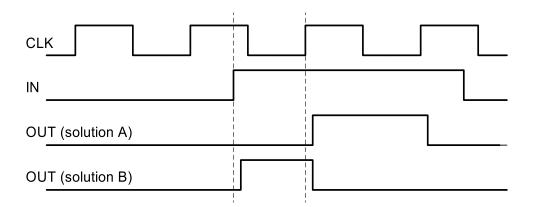


Solution B

Output depends not only on PS but also on input, IN



Edge detector timing diagrams



- Solution A: output follows the clock
- Solution B: output changes with input rising edge and is asynchronous wrt the clock.

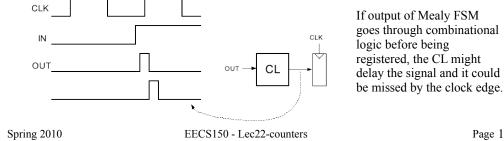
FSM Comparison

Solution A **Moore Machine**

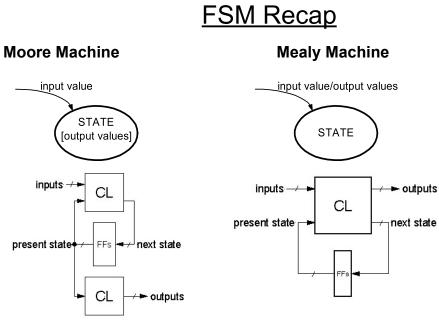
- output function only of PS •
- maybe more states (why?) •
- synchronous outputs •
 - no glitches
 - one cycle "delay"
 - full cycle of stable output

Solution B **Mealy Machine**

- output function of both PS & input
- maybe fewer states
- asynchronous outputs
 - if input glitches, so does output
 - output immediately available
 - output may not be stable long enough to be useful (below):





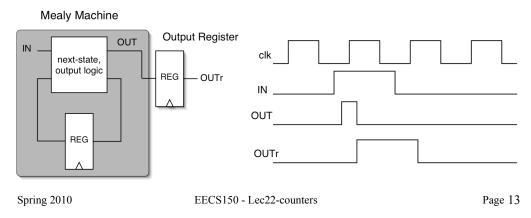


Both machine types allow one-hot implementations.

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Final Notes on Moore versus Mealy

- 1. A given state machine *could* have *both* Moore and Mealy style outputs. Nothing wrong with this, but you need to be aware of the timing differences between the two types.
- 2. The output timing behavior of the Moore machine can be achieved in a Mealy machine by "registering" the Mealy output values:



General FSM Design Process with Verilog

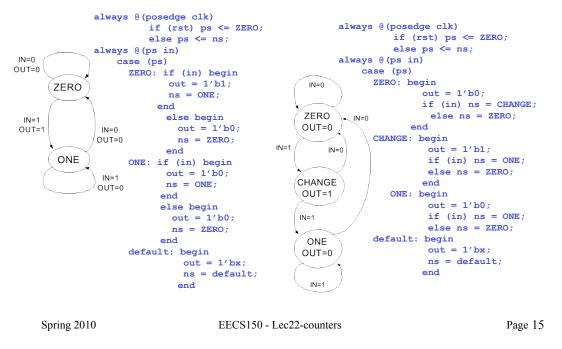
Design Steps: Implementation

- 1. Specify **circuit function** (English)
- 2. Draw state transition diagram
- 3. Write down symbolic state transition table
- 4. Assign encodings (bit patterns) to symbolic states
- 5. Code as Verilog behavioral description
- ✓ Use parameters to represent encoded states.
- ✓ Use separate always blocks for register assignment and CL logic block.
- ✓ Use case for CL block. Within each case section assign all outputs and next state value based on inputs. Note: For Moore style machine make outputs dependent only on state not dependent on inputs.

FSMs in Verilog



Moore Machine



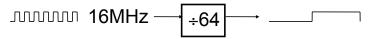
Counters

- Special sequential circuits (FSMs) that repeatedly sequence through a set of outputs.
- Examples:
 - binary counter: 000, 001, 010, 011, 100, 101, 110, 111, 000,
 - gray code counter: 000, 010, 110, 100, 101, 111, 011, 001, 000, 010, 110, ...
 - one-hot counter: 0001, 0010, 0100, 1000, 0001, 0010, ...
 - BCD counter: 0000, 0001, 0010, ..., 1001, 0000, 0001
 - pseudo-random sequence generators: 10, 01, 00, 11, 10, 01, 00, ...
- Moore machines with "ring" structure in State Transition Diagram:

S2

What are they used?

- Counters are commonly used in hardware designs because most (if not all) computations that we put into hardware include iteration (looping). Examples:
 - Shift-and-add multiplication scheme.
 - Bit serial communication circuits (must count one "words worth" of serial bits.
- Other uses for counter:
 - Clock divider circuits



- Systematic inspection of data-structures
 - Example: Network packet parser/filter control.
- Counters simplify "controller" design by:
 - providing a specific number of cycles of action,
 - sometimes used with a decoder to generate a sequence of timed control signals.
 - Consider using a counter when many FSM states with few branches.

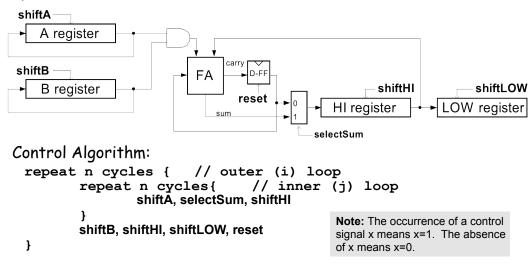
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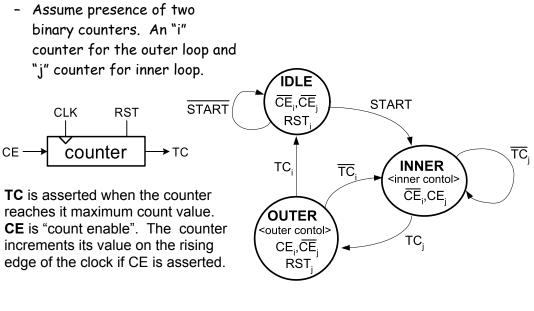
Controller using Counters

Example, Bit-serial multiplier (n² cycles, one bit of result per n cycles):



Controller using Counters

• State Transition Diagram:



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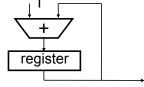
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Controller using Counters

Controller circuit Outputs: ٠ implementation: $CE_i = q_2$ $CE_i = q_1$ START -► q₀ IDLE $RST_i = q_0$ R $RST_i = q_2$ TCi shiftA = q_1 ▶ q₁ INNER R S shiftB = q_2 Global reset shiftLOW = q_2 shiftHI = $q_1 + q_2$ OUTER q_2 reset = q_2 TCj -R selectSUM = q_1

How do we design counters?

 For binary counters (most common case) incrementer circuit would work:



- In Verilog, a counter is specified as: x = x+1;
 - This does not imply an adder
 - An incrementer is simpler than an adder
 - And a counter is simpler yet.
- In general, the best way to understand counter design is to think of them as FSMs, and follow general procedure, however some special cases can be optimized.

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Synchronous Counters

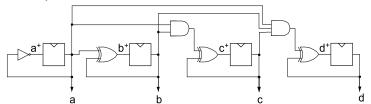
All outputs change with clock edge.

a+ = a' • Binary Counter Design: c b a c + b + a + b⁺ = a ⊕ b σ 00 00 1 Start with 3-bit version and 001 0 1 0 cb 0 10 011 generalize: a \ 00 01 11 10 1 1 100 0 0 0 0 1 1 0 0 1 101 1 0 1 0 1 0 1 1 1 0 1 1 1 1 1 1 0 $c^+ = a'c + abc' + b'c$ 1 1 1 000 = c(a'+b') + c'(ab)= c(ab)' + c'(ab)= c ⊕ ab C а b С

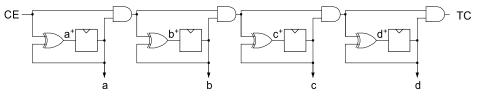
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Synchronous Counters

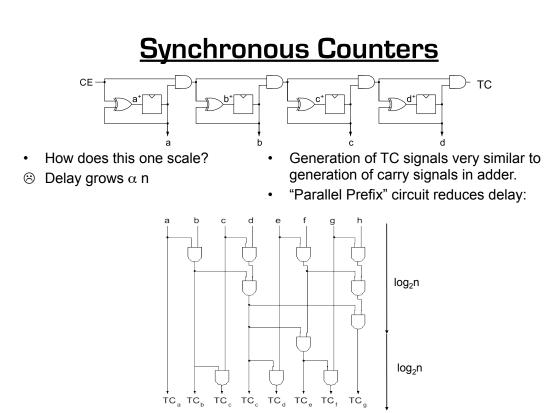
- How do we extend to n-bits?
- Extrapolate c⁺: d⁺ = d \oplus abc, e⁺ = e \oplus abcd



• Has difficulty scaling (AND gate inputs grow with n)

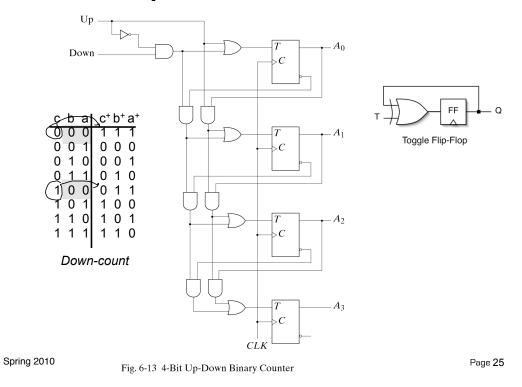


- · CE is "count enable", allows external control of counting,
- TC is "terminal count", is asserted on highest value, allows cascading, external sensing of occurrence of max value. Spring 2010 EECS150 - Lec22-counters



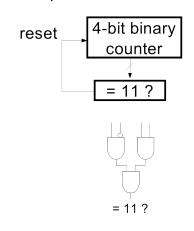
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Up-Down Counter

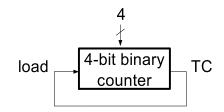


Odd Counts

- Extra combinational logic can be added to terminate count before max value is reached:
- Example: count to 12



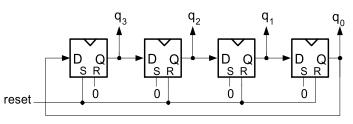
• Alternative:



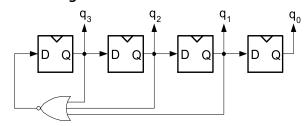
Ring Counters

- "one-hot" counters
- What are these good for?

0001, 0010, 0100, 1000, 0001, ...



"Self-starting" version:

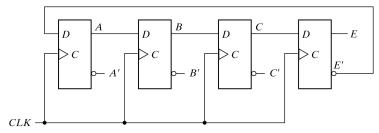


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Johnson Counter



(a) Four-stage switch-tail ring counter

Sequence number	Flip-flop outputs				AND gate required
	Ā	В	С	E	for output
1	0	0	0	0	A'E'
2	1	0	0	0	AB'
3	1	1	0	0	BC'
4	1	1	1	0	CE'
5	1	1	1	1	AE
6	0	1	1	1	A'B
7	0	0	1	1	B'C
8	0	0	0	1	C'E

(b) Count sequence and required decoding



