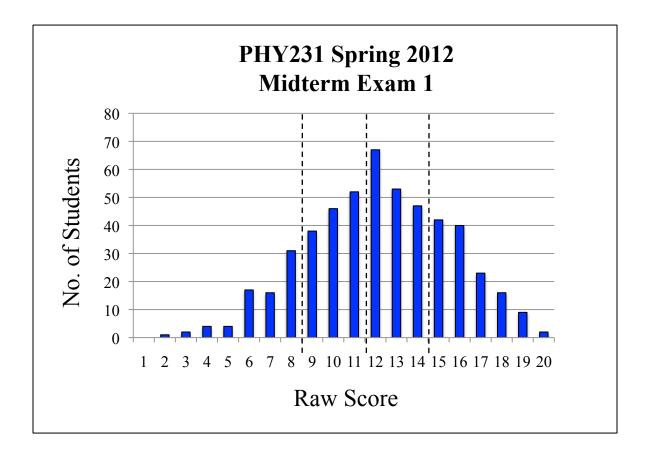
Exam 1 Solutions

Kinematics and Newton's laws of motion



1. In which one of the following situations does the car have a westward acceleration?

- A) The car travels westward at constant speed.
- B) The car travels eastward and speeds up.
- C) The car travels westward and slows down.
- D) The car travels eastward and slows down.
- E) The car starts from rest and moves toward the east.

east(+), initial velocity =
$$+v_0$$
, final velocity = $+v$

Slows down,
$$v_0 > v$$

Acceleration =
$$\frac{v - v_0}{t}$$
 is negative (west)

What about C)?

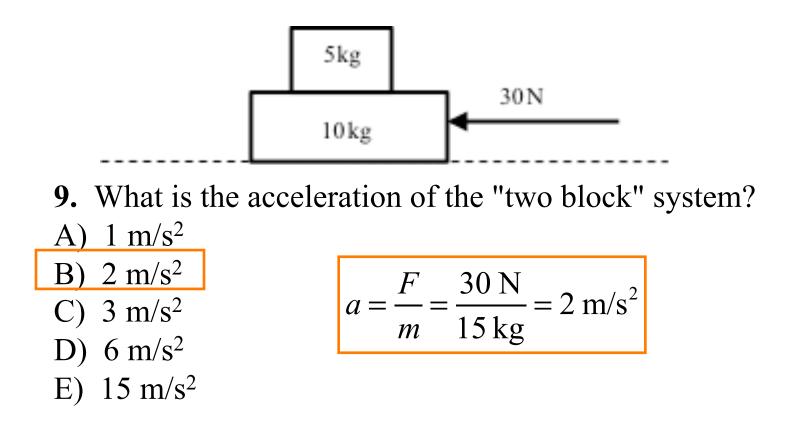
west(+), initial velocity = $+v_0$, final velocity = +vSlows down, $v_0 > v$ EASTWARD Acceleration = $\frac{v - v_0}{t}$ is negative (east) **1.** In which one of the following situations does the car have a westward acceleration?

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- B) The car travels eastward and speeds up.
- C) The car travels westward and slows down.
- D) The car travels eastward and slows down.
- E) The car starts from rest and moves toward the east.

In C) What if you choose west as negative?

west(-), initial velocity =
$$-v_0$$
, final velocity = $-v$
Slows down, $v_0 > v$
Acceleration = $\frac{(-v) - (-v_0)}{t} = \frac{v_0 - v}{t}$ is positive (east)
EASTWARE

If object travels in one direction and slows down, the acceleration is in the opposite direction!



10. What is the force of static friction between the top and bottom blocks of the previous problem?

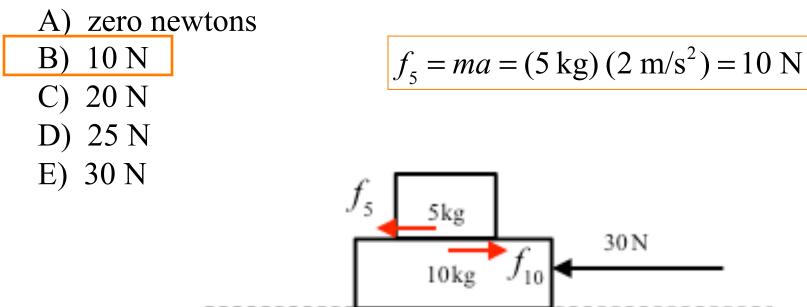
A) zero newtons
B) 10 N
C) 20 N
D) 25 N

E) 30 N

Acceleration of 5kg block must be the same as the combination.

$$f_5 = ma = (5 \text{ kg}) (2 \text{ m/s}^2) = 10 \text{ N}$$

10. What is the force of static friction between the top and bottom blocks of the previous problem?



Also, the 10 kg block must have the same acceleration f_5 and f_{10} are an "action-reaction" pair from Newton's 3rd law. Equal magnitudes, opposite directions on two objects in contact. left is +, $\sum \vec{F} = m\vec{a} = (10 \text{ kg})(+2 \text{ m/s}^2) = +20 \text{ N}$ $= +f_{10} + (30 \text{ N}) = +20 \text{ N}$ $f_{10} = -10 \text{ N}$ **20.** In a tug-of-war, each man on a 5-man team pulls with an average force of 500 N. What is the tension in the center of the rope?

A) zero newtons

B) 100 N

C) 500 N

D) 2500 N E) 5000 N Each team pulls with a force of 2500 N. The rope pulls back with a Tension = 2500 N

on each team.

2500 N T = 2500 N

T = 2500 N 2500 N

Split the rope at the midpoint.

Attach the ends together with hooks.

How hard does each hook pull on the other? m

That is the tension at the midpoint.

2500 N

$$T = 2500 \text{ N}$$
 | $T = 2500 \text{ N}$

2500 N

"Action – Reaction" pair of forces of Newton's 3rd law.

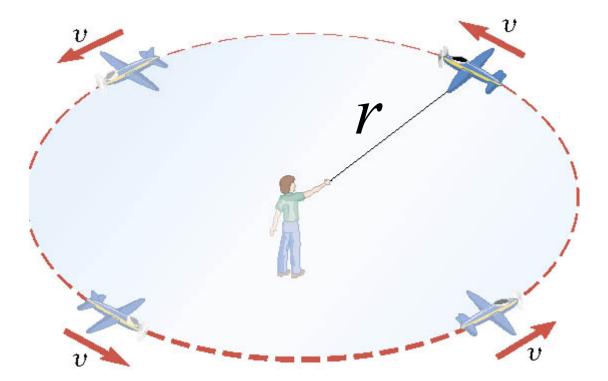
Chapter 5

Dynamics of Uniform Circular Motion

5.1 Uniform Circular Motion

DEFINITION OF UNIFORM CIRCULAR MOTION

Uniform circular motion is the motion of an object traveling at a constant speed on a circular path.

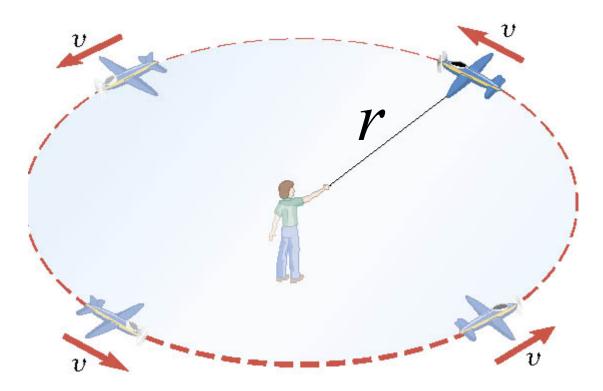


Circumference of the circle is $2\pi r$.

5.1 Uniform Circular Motion

The time it takes the object to travel once around the circle is *T* (a.k.a. the period)

Speed around the circle is, $v = \frac{2\pi r}{T}$.



5.1 Uniform Circular Motion

Example 1: A Tire-Balancing Machine

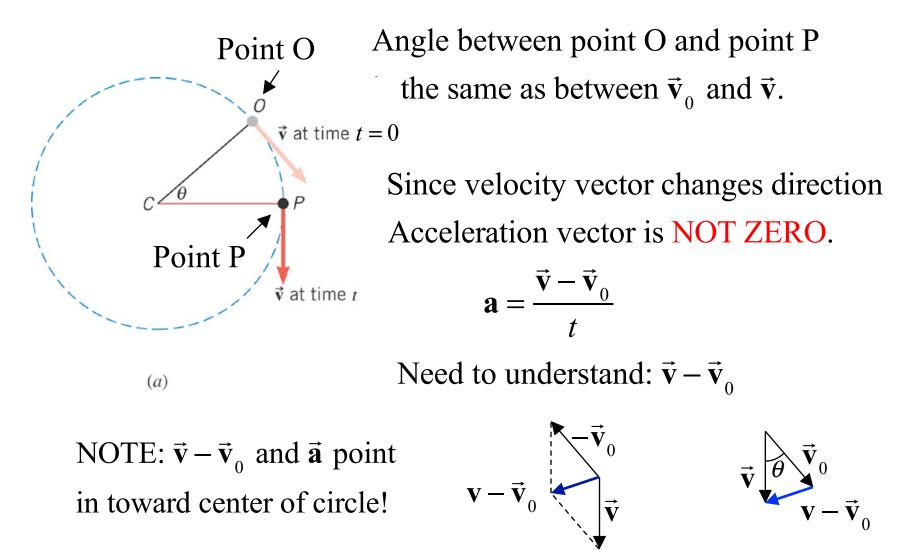
The wheel of a car has a radius of 0.29m and it being rotated at 830 revolutions per minute on a tire-balancing machine. Determine the speed at which the outer edge of the wheel is moving.

$$\frac{1}{830 \text{ revolutions/min}} = 1.2 \times 10^{-3} \text{ min/revolution}$$

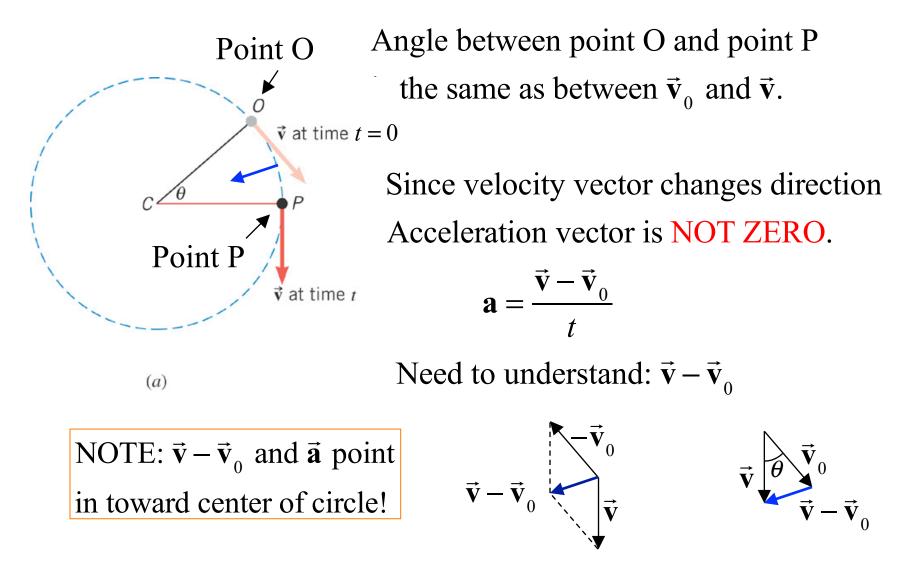
$$T = 1.2 \times 10^{-3} \text{ min} = 0.072 \text{ s}$$

$$v = \frac{2\pi r}{T} = \frac{2\pi (0.29 \text{ m})}{0.072 \text{ s}} = 25 \text{ m/s}$$

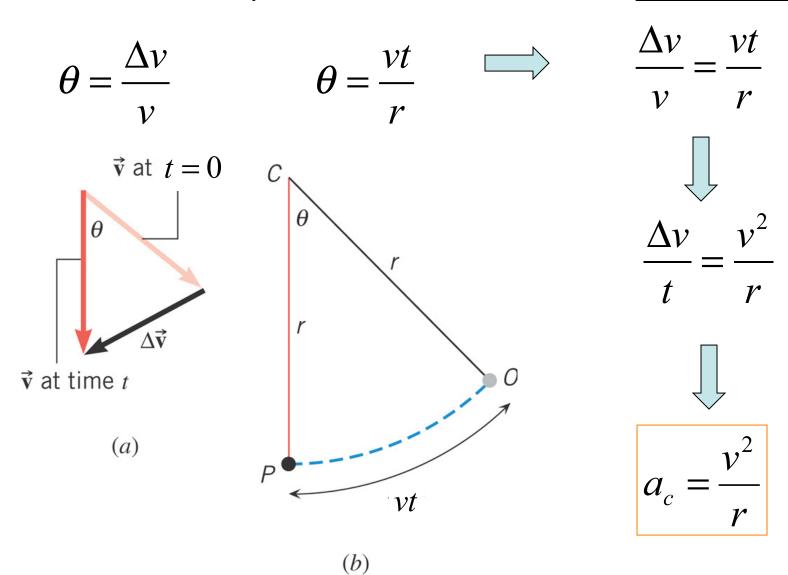
In uniform circular motion, the speed is *constant*, but the direction of the velocity vector is *not constant*.



In uniform circular motion, the speed is *constant*, but the direction of the velocity vector is *not constant*.

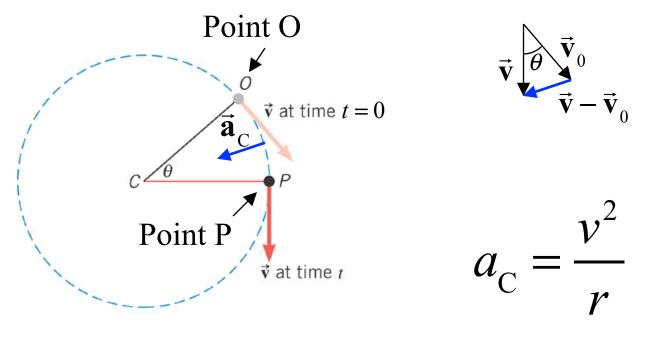


Compare geometry of velocity vectors and the portion of the circle.



Magnitudes

The direction of the centripetal acceleration is towards the center of the circle; in the same direction as the change in velocity.



(a)

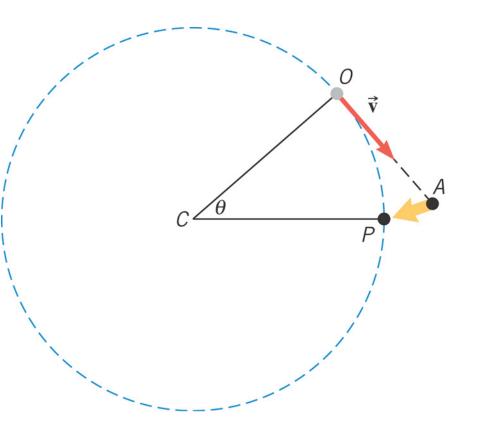
Centripetal acceleration vector points *inward* at ALL points on the circle

Conceptual Example 2: Which Way Will the Object Go?

An object (•) is in uniform circular motion. At point *O* it is released from its circular path.

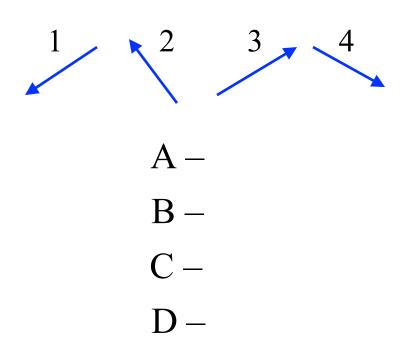
Does the object move along the (A) Straight path between O and A or

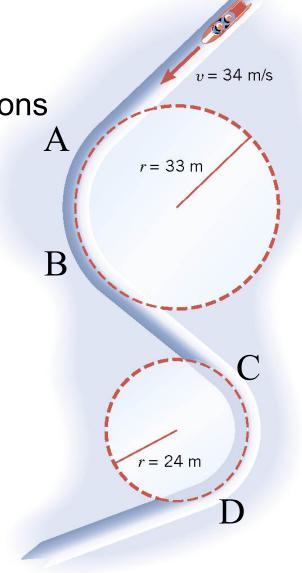
(B) Along the circular arc between points O and P?



Example 3: The Effect of Radius on Centripetal Acceleration

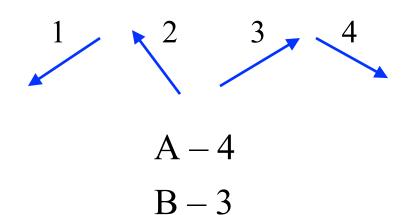
The bobsled track contains turns with radii of 33 m and 24 m. Match the acceleration vector directions below to the points A,B,C,D. A





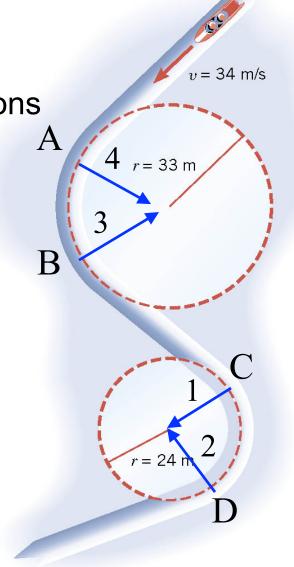
Example 3: The Effect of Radius on Centripetal Acceleration

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C – 1

D-2

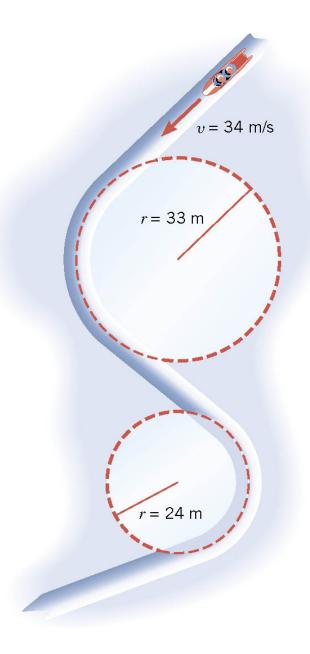


$$a_{\rm C} = v^2/r$$

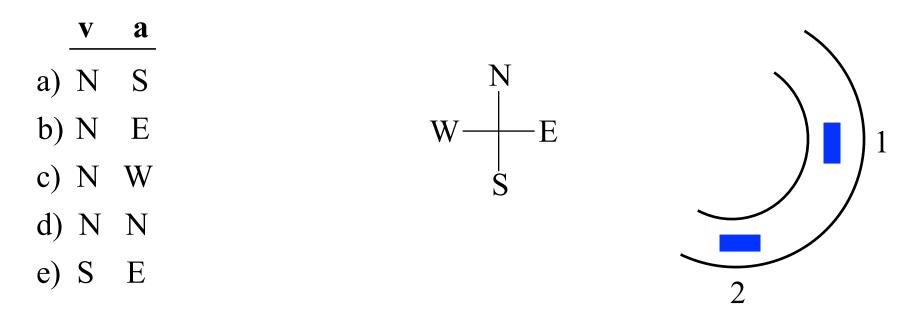
Find the centripetal acceleration at each turn for a speed of 34 m/s. Express answers as multiples of $g = 9.8 \text{ m/s}^2$.

$$a_{\rm C} = \frac{\left(34\,{\rm m/s}\right)^2}{33\,{\rm m}} = 35\,{\rm m/s^2} = 3.6g$$

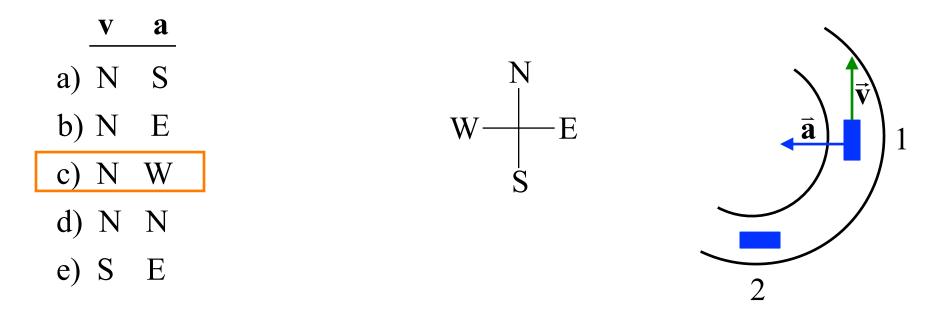
$$a_{\rm C} = \frac{\left(34\,{\rm m/s}\right)^2}{24\,{\rm m}} = 48\,{\rm m/s^2} = 4.9g$$



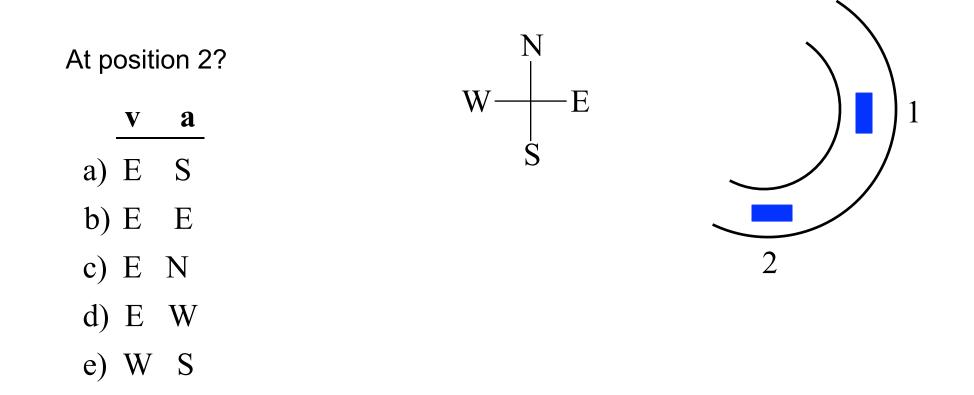
A car is moving counter-clockwise around a circular section of road at constant speed. What are the directions of its velocity and acceleration at position 1.



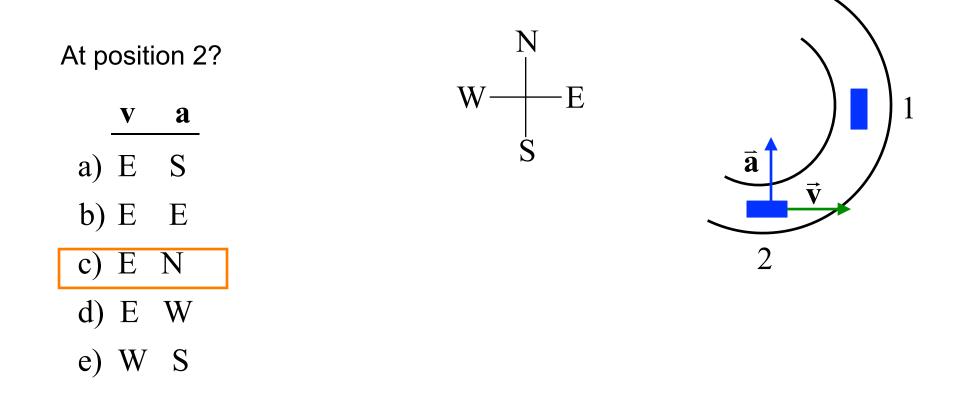
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Newton's Second Law

When a net external force acts on an object of mass *m*, the acceleration that results is directly proportional to the net force and has a magnitude that is inversely proportional to the mass. The direction of the acceleration is the same as the direction of the net force.



Thus, in uniform circular motion there must be a net force to produce the centripetal acceleration.

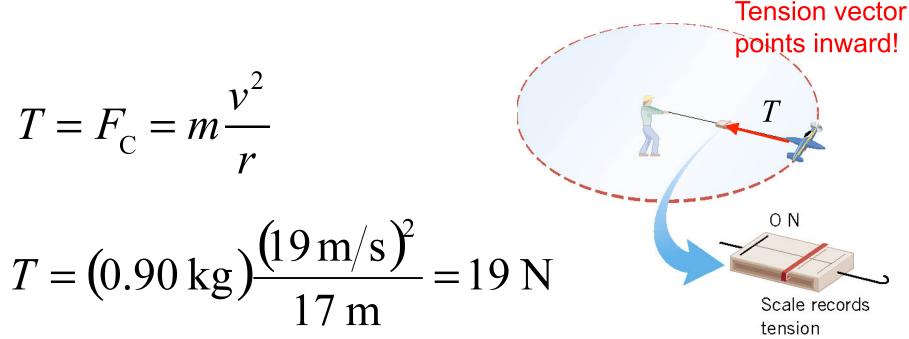
The centripetal force is the name given to the net force required to keep an object moving on a circular path.

The direction of the centripetal force always points toward the center of the circle and continually changes direction as the object moves.

$$F_{\rm C} = ma_{\rm C} = m \frac{v^2}{r}$$
 Magnitudes

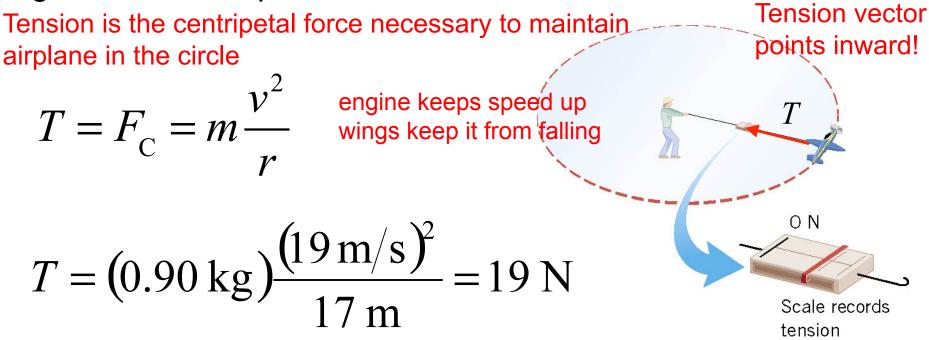
Example 5: The Effect of Speed on Centripetal Force

The model airplane has a mass of 0.90 kg and moves at constant speed on a circle that is parallel to the ground. The path of the airplane and the guideline lie in the same horizontal plane because the weight of the plane is balanced by the lift generated by its wings. Find the tension in the 17 m guideline for a speed of 19 m/s.



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Conceptual Example 6: A Trapeze Act

In a circus, a man hangs upside down from a trapeze, legs bent over and arms downward, holding his partner. Is it harder for the man to hold his partner when the partner hangs straight down and is stationary or when the partner is swinging through the straight-down position?



Tension in arms maintains circular motion but also must counter the gravitational force (weight)

Conceptual Example 6: A Trapeze Act

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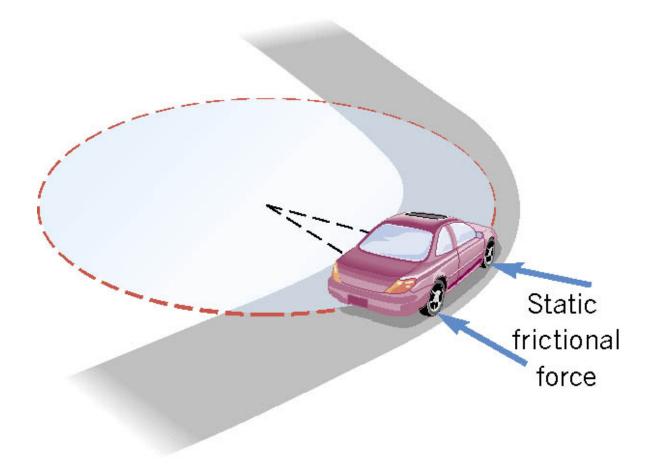


Tension in arms maintains circular motion but also must counter the gravitational force (weight)

$$\sum \vec{\mathbf{F}} = +T - W = F_{C}$$
$$T = W + F_{C}$$

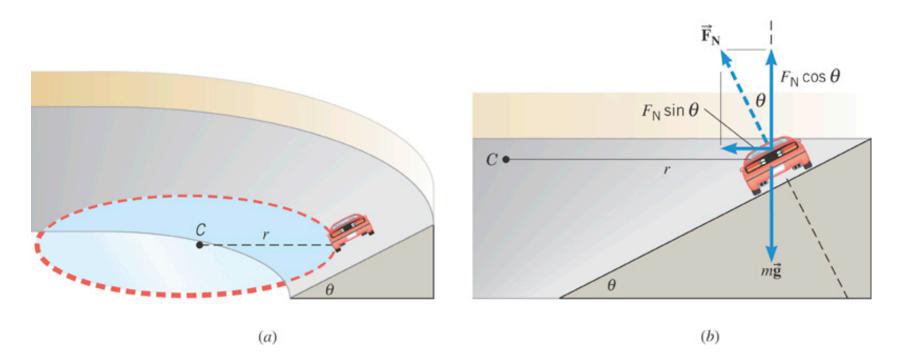
5.4 Banked Curves

On an unbanked curve, the static frictional force provides the centripetal force.



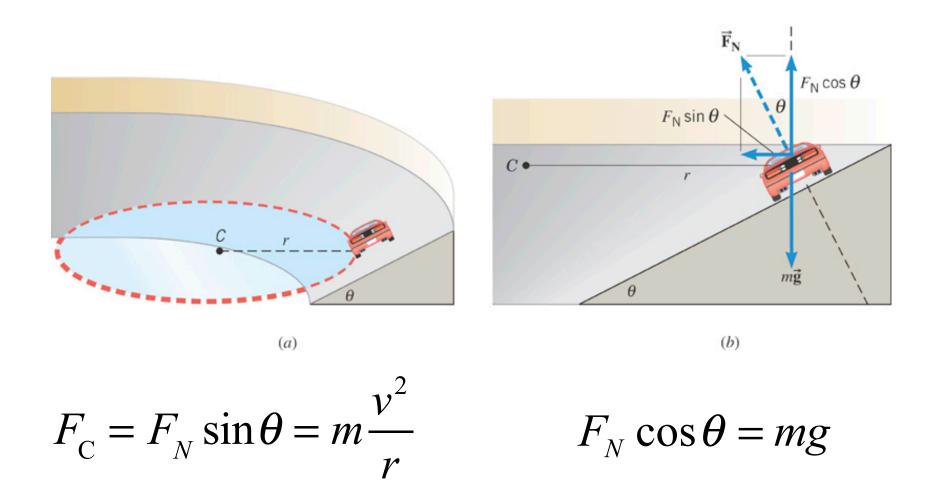
5.4 Banked Curves

On a frictionless banked curve, the centripetal force is the horizontal component of the normal force. The vertical component of the normal force balances the car's weight.



Compression of the banked road provides the normal force. The normal force pushes against the car to 1) support the weight and 2) provide the centripetal force to keep the car moving in a circle.

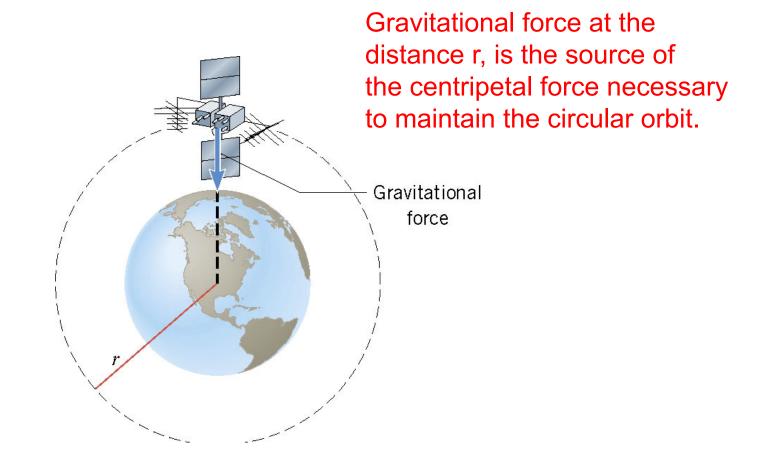
5.4 Banked Curves



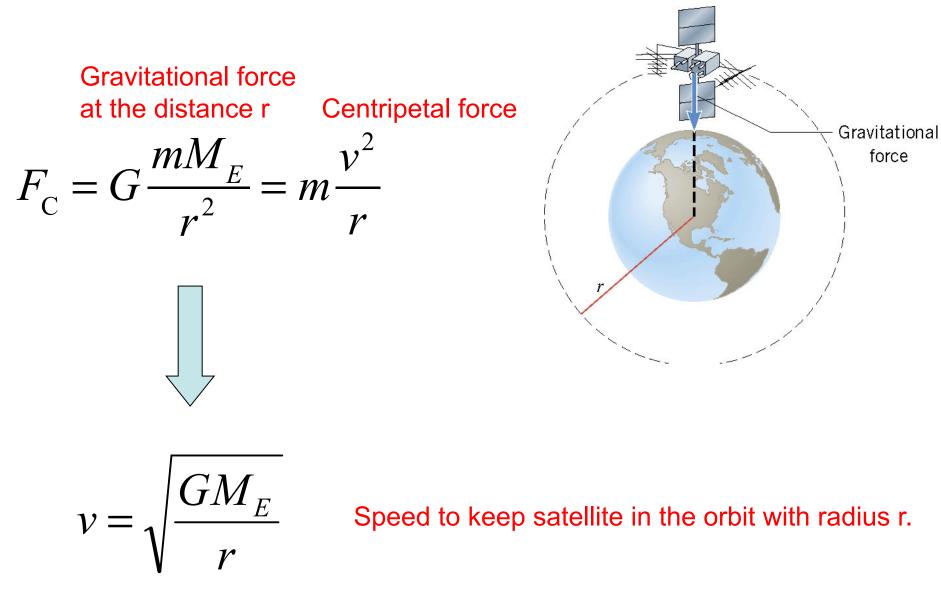
Combining the two relationships can determine the speed necessary to keep the car on the track with the given angle

5.5 Satellites in Circular Orbits

There is only one speed that a satellite can have if the satellite is to remain in an orbit with a fixed radius.

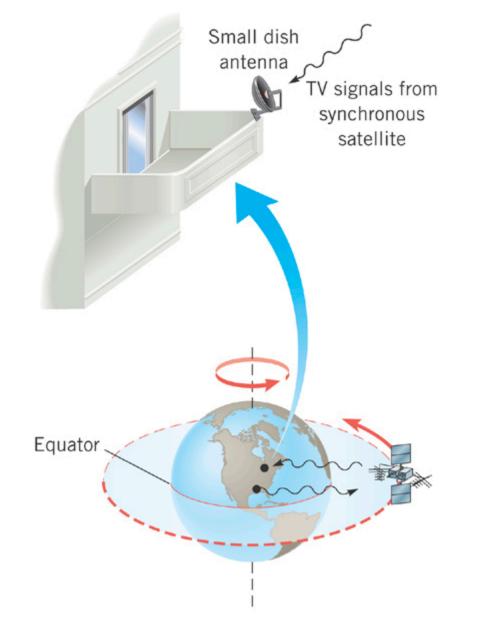


5.5 Satellites in Circular Orbits



5.5 Satellites in Circular Orbits

There is a radius where the speed will make the satellite go around the earth in exactly 24 hours. This keeps the satellite at a fixed point in the sky.



5.6 Apparent Weightlessness and Artificial Gravity

Can you feel gravity? We previously determined that you can't.

Hanging from a 100 m high diving board
 your arms feel stretched by the bending of the board.

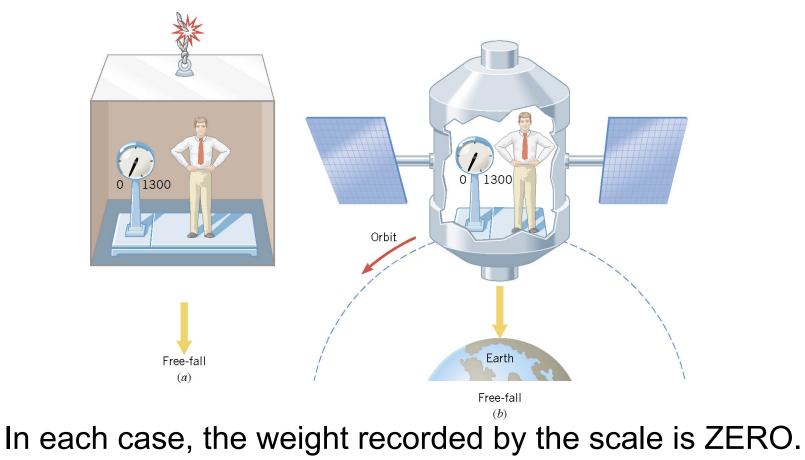
2) Standing on a bed – your legs feel compressed by the springs in the mattress.

The bent diving board or the compressed springs provide the force to balance the gravitational force on you.

When you let go of the diving board and before you hit the ground the ONLY force on you is gravity. It makes you accelerate downward, but it does not stretch or compress your body.

In free fall one cannot feel the force of gravity!

5.6 Apparent Weightlessness and Artificial Gravity

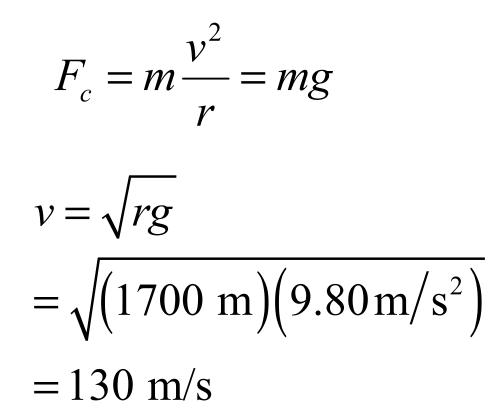


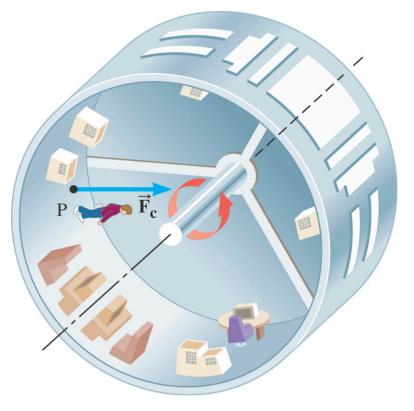
Gravitational force acts on the body and on the satellite to provide the centripetal force necessary to keep both in orbit. Gravitational force makes both the elevator and the body fall with the same acceleration.

5.6 Apparent Weightlessness and Artificial Gravity

Example 13: Artificial Gravity

At what speed must the surface of a space station move so that an astronaut experiences a push on the feet equal to the weight on earth? The radius is 1700 m.





5.7 Vertical Circular Motion

Normal forces are created by stretching of the hoop.

