## EXERCISE 33(A)

1.Marks scored by 30 students of class VI are as given below:
$38,46,33,45,63,53,40,85,52,75,60,73,62,22,69,43,45,33,47,41,29,43,37,49$, $83,44,55,22,35$ and 45. State:
(i) the highest marks scored
(ii) the lowest marks scored
(iii) the range of marks

Solution:
(i) The highest marks scored is 85
(ii) The lowest marks scored is 22
(iii) Range of marks = Difference between highest and lowest marks
$=85-22$
$=63$
Therefore, the range of marks is 63
2. For the following raw data, form a discrete frequency distribution:

30, 32, 32, 28, 34, 34, 32, 30, 30, 32, 32, 34, 30, 32, 32. 28, 32, 30, 28, 30, 32, 32, 30, 28 and 30
Solution:
The required frequency table is shown below

| Marks | Tally marks | Frequency |
| :--- | :---: | :---: |
| 28 | \||I| | 4 |
| 30 | $\mathbb{N}$ \||| | 8 |
| 32 | $\mathbb{N} \mathbb{N}$ | 10 |
| 34 | III | 3 |
| Total |  | 25 |

3. Define:
(i) data
(ii) frequency of an observation

## Solution:

(i) Data: Information in the form of numerical figures is known as data
(ii) Frequency of an observation: The number of times a particular observation occurs is known as its frequency
4. Rearrange the following raw data in descending order:
$5.3,5.2,5.1,5.7,5.6,6.0,5.5,5.9,5.8,6.1,5.5,5.8,5.7,5.9$ and 5.4. Then write the:
(i) highest value
(ii) lowest value
(iii) range of values

Solution:
The given numbers in descending order are as follows:
$6.1,6.0,5.9,5.9,5.8,5.8,5.7,5.7,5.6,5.5,5.5,5.4,5.3,5.2,5.1$
(i) Hence, the highest value is 6.1
(ii) Hence, the lowest value is 5.1
(iii) Range of values = Difference between highest value and lowest value

Hence,
Range of values $=$ highest value - lowest value
$=6.1-5.1$
$=1.0$
5. Represent the following data in the form of a frequency distribution:
$52,56,72,68,52,68,52,68,52,60,56,72,56,60,64,56,48,48$, 64 and 64
Solution:
The required frequency table for the given data is as follows:

Marks
48
52
56
60
64
68
72
Total

Frequency 2 44233

II
2
6. In a study of number of accidents per day, the observations for $\mathbf{3 0}$ days were obtained as follows:

| $\mathbf{6}$ | $\mathbf{3}$ | $\mathbf{5}$ | $\mathbf{6}$ | $\mathbf{4}$ | $\mathbf{3}$ | $\mathbf{2}$ | $\mathbf{5}$ | $\mathbf{4}$ | $\mathbf{2}$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathbf{4}$ | $\mathbf{0}$ | $\mathbf{5}$ | $\mathbf{3}$ | $\mathbf{6}$ | $\mathbf{1}$ | $\mathbf{5}$ | $\mathbf{5}$ | $\mathbf{2}$ | $\mathbf{6}$ |
| $\mathbf{2}$ | 1 | 2 | 2 | 0 | 5 | $\mathbf{4}$ | $\mathbf{6}$ | $\mathbf{1}$ | $\mathbf{6}$ |

Construct a suitable frequency distribution table.

## Solution:

The required frequency table is shown below:

| No. of accidents | Tally marks | Frequency |
| :--- | :---: | :---: |
| 0 | $\\| \mid$ | 2 |
| 1 | I\|| | 3 |
| 2 | $\mathbb{N}\|\mid$ | 6 |
| 3 | \||| | 3 |
| 4 | \|||| | 4 |
| 5 | $\mathbb{N}$ \| | 6 |
| 6 | $\mathbb{N}$ \| | 6 |
| Total |  | 30 |

7. The following data represents the weekly wages (in Rs) of 15 workers in a factory: $\mathbf{9 0 0}, 850,800,850,800,750,950,900,950,800,750,900,750,800$ and 850
Prepare a frequency distribution table. Now find,
(i) how many workers are getting less than Rs 850 per week?
(ii) how many workers are getting more than Rs 800 per week?

## Solution:

The required frequency table is as follows:
Weekly
Tally marks
Frequency
wages in Rs
750
800
850
900
9503

Total no. of workers15
(i) Number of workers getting less than Rs 850 per week are, Number of workers getting Rs $750=3$ workers
Number of workers getting Rs $800=4$ workers
Hence, workers getting less than Rs $850=4+3$
$=7$ workers
Therefore, 7 workers are getting less than Rs 850 per week
(ii) Number of workers getting more than Rs 800 per week are,

Number of workers getting Rs $850=3$
Number of workers getting Rs $900=3$
Number of workers getting Rs $950=2$
So, number of workers getting more than Rs $800=3+3+2$
= 8 workers
Therefore, 8 workers are getting more than Rs 800 per week
8. Using the data, given below, construct a frequency distribution table:
$\mathbf{9 , 1 7}, 12,20,9,18,25,17,19,9,12,9,12,18,17,19,20,25,9$ and 12. Now answer the following:
(i) How many numbers are less than 19?
(ii) How many numbers are more than 20?
(iii) Which of the numbers, given above, is occurring most frequently?

## Solution:

The required frequency table is as follows:

| Marks | Tally marks | Frequency |
| :--- | :---: | :---: |
| 9 | $\mathbb{N}$ | 5 |
| 12 | IIII | 4 |
| 17 | III | 3 |
| 18 | $\\|$ | 2 |
| 19 | $\\|$ | 2 |
| 20 | II | 2 |
| 25 | II | 2 |
| Total |  | 20 |

(i) Total numbers less than $19=14$
(ii) Total numbers more than $20=2$
(iii) The number 9 occurs 5 times.

Hence, the number which is occurring most frequently is 9
10. Using the following data, construct a frequency distribution table: 46, 44, 42, 54, $52,60,50,58,56,62,50,56,54,58$ and 48
Now answer the following:
(i) What is the range of the numbers?
(ii) How many numbers are greater than 50 ?
(iii) How many numbers are between 40 and 50?

Solution:

Marks
42
44
46
48
50
52
54
56
58
60
62
Total

Tally marks


Frequency 1
1
1
1
2
1
2
2
2
1
1 15
(i) Range of numbers $=$ Highest number - Lowest number
$=62-42$
$=20$
(ii) There are 9 numbers which are greater than 50
(iii) There are 6 numbers which are between 40 and 50

## EXERCISE 33（B）

1．The sale of vehicles，in a particular city，during the first six months of the year 2016 is shown below：

| Month | Jan | Feb | March | April | May | June |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Number of | $\mathbf{3 0 0 0}$ | $\mathbf{2 5 0 0}$ | $\mathbf{4 0 0 0}$ | $\mathbf{1 0 0 0}$ | $\mathbf{1 5 0 0}$ | $\mathbf{3 5 0 0}$ |

vehicles sold
Draw a pictograph to represent the above data
Solution：
Let us consider one


Hence，the pictograph to represent the data is shown below

| Month | Number of vehicles sold |
| :---: | :---: |
| Jan | だs |
| Feb | ETs |
| March |  |
| April | స゙t |
| May | だst |
| June | だち |

2．The following pictograph shows the number of cars sold by four dealers $\mathrm{A}, \mathrm{B}, \mathrm{C}$ and $D$ in a city．Scale：

| Dealer | Number of c |
| :---: | :---: |
| A |  |
| B | 5-0 |
| C | Kobrom |
| D | 50 50 5-0 |

Using the pictograph, drawn above, answer the following questions:
(i) How many more cars has dealer A sold as compared to dealer D?
(ii) What is the total number of cars sold by all the dealers?

## Solution:

Given
One figure $=50$ cars
Hence, cars sold by dealer A and D can be calculated as below
Cars sold by $\mathrm{A}=6 \times 50$
$=300$ cars
Cars sold by $\mathrm{D}=4 \times 50$
$=200$ cars
Total cars sold by A than $\mathrm{D}=300-200$
= 100
Hence, A sold 100 more cars than D
(ii) Total number of cars $=23$

Scale $=50$ cars
Hence,
Total number of cars sold by all the dealers can be calculated as below
Total number of cars sold $=23 \times 50$
$=1150 \mathrm{cars}$
Hence, total number of cars sold by all the dealers is 1150 cars
3. The following pictograph shows the number of watches manufactured by a factory, in a particular weeks.
Day

Scale:


Find
(i) on which day were the least number of watches manufactured?
(ii) total number of watches manufactured in the whole week?

Solution:
(i) The day on which the least number of watches are manufactured is Friday

Number of watches manufactured on Friday $=100 \times 5$
$=500$ watches
(ii) Total number of watches manufactured in the whole week can be calculated as below Total number of watches manufactured $=100 \times 42.5$
$=4250$ watches
4. The number or animals in five villages are as follows:

| Village | A | B | C | D | E |
| :---: | :---: | :---: | :---: | :---: | :---: |
| No. of <br> animals | $\mathbf{1 6 0}$ | $\mathbf{2 4 0}$ | $\mathbf{1 8 0}$ | $\mathbf{8 0}$ | $\mathbf{1 2 0}$ |

Prepare a pictograph of these animals using one symbol to represent 20 animals. Solution:

Let represents 20 animals
Hence, the pictograph representing animals in five villages are as follows:
Village
5. The following pictograph shows different subject books which are kept in a school library.


Taking symbol of one book $=50$ books, find:
(i) how many History books are there in the library?
(ii) how many Science books are there in the library?
(iii) Which books are maximum in number?

## Solution:

(i) Given

One book = 50 books
Hence, total number of History books can be calculated as below
Total number of History books $=50 \times 4$
$=200$ books
Therefore, there are 200 History books in the library
(ii) Given

One book $=50$ books
Hence, total number of Science books can be calculated as below
Total number of Science books $=50 \times 5.5$
$=275$ books
Therefore, there are 275 Science books in the library
(iii) From the given pictograph, English books are maximum in number in the library

Given
One book $=50$ books
Hence, total number of English books can be calculated as below
Total number of English books $=50 \times 9$
$=450$ books
Therefore, there are 450 English books in the library

## EXERCISE 33(C)

1. The following table gives the number of students in class VI in a school during academic years 2011-2012 to 2015-2016.

| Academic <br> years | $2011-2012$ | $2012-2013$ | $2013-2014$ | $2014-2015$ | $2015-2016$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| No. of <br> students | $\mathbf{8 0}$ | 120 | 130 | 150 | 180 |

Represent the above data by a bar graph.
Solution:
The bar graph to represent the above data is as follows:


Year
2. The attendance of a particular class for the six days of a week are as given below:

| Day | Monday | Tuesday | Wednesday | Thursday | Friday | Saturday |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Attendence | $\mathbf{4 8}$ | $\mathbf{4 4}$ | $\mathbf{4 0}$ | $\mathbf{3 6}$ | $\mathbf{3 9}$ | $\mathbf{4 3}$ |

Draw a suitable graph.
Solution:


Day
3. The total number of students present in class VI B, for the six day in a week were as given below. Draw a suitable bar graph.

| Day | Monday | Tuesday | Wednesday | Thursday | Friday | Saturday |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No. of <br> student <br> present | $\mathbf{4 0}$ | $\mathbf{3 0}$ | $\mathbf{3 5}$ | $\mathbf{2 5}$ | $\mathbf{1 0}$ | $\mathbf{2 0}$ |

[^0]

Day
4. The following table shows the population of a particular city at different years:

| Year | 1996 | 2001 | 2006 | 2011 | 2016 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Population <br> in Lakh | $\mathbf{4 5}$ | 57 | 70 | 90 | 110 |

Represent the above information with the help of a suitable bar graph.
Solution:

5. In a survey of $\mathbf{3 0 0}$ families of a colony, the number of children in each family was recorded and the data has been represented by the bar graph, given below:


Read the graph carefully and answer the following questions:
(i) How many families have 2 children each?
(ii) How many families have no child?
(iii) What percentage of families have 4 children?

## Solution:

(i) From the given figure, 60 families have 2 children each
(ii) From the given figure, all the families have children. Therefore, the answer is zero
(iii) The percentage of families having four children can be calculated as below

Percentage $=($ total no. of families having four children) $/($ total number of families
having children) $\times 100$
$=600 / 300 \times 100$
$=20 \%$
Hence, $20 \%$ of families have four children
6. Use the data, given in the following table, to draw a bar graph

| A | B | C | D | E | F |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathbf{2 5 0}$ | $\mathbf{3 0 0}$ | $\mathbf{2 2 5}$ | $\mathbf{3 5 0}$ | $\mathbf{2 7 5}$ | $\mathbf{3 2 5}$ |

Out of A, B, C, D, E and F
(i) Which has the maximum value.
(ii) Which is greater A+D or B+E.

## Solution:

(i) From the given data, D has the maximum value of 350
(ii) $\mathrm{A}+\mathrm{D}=250+350$

We get,
$=600$
$B+E=300+275$
We get,
$=575$
We know that, 600 is greater than 575
Hence, $\mathrm{A}+\mathrm{D}$ is greater than $\mathrm{B}+\mathrm{E}$
7. The bar graph drawn below shows the number of tickets sold during a fair by 6 students A, B, C, D, E and F


Using the Bar graph, answer the following question:
(i) Who sold the least number of tickets?
(ii) Who sold the maximum number of tickets?
(iii) How many tickets were sold by A, B and C taken together?
(iv) How many tickets were sold by D, E and F taken together?
(v) What is the average number of tickets sold per student?

## Solution:

(i) From the given graph, the student D sold the least number of tickets i.e 7 tickets
(ii) From the given graph, the student E sold the maximum number of tickets i.e 24 tickets
(iii) From the given graph, total number of tickets sold by the student A, B and C can be calculated as below
Tickets sold by A, B and C taken together $=($ Tickets sold by A$)+($ Tickets sold by B$)+$ (Tickets sold by C)
$=16+9+20$
We get,
$=45$
Therefore, total tickets sold by A, B and C together is 45 tickets
(iv) From the given graph, total number of tickets sold by the student D, E and F can be calculated as below
Tickets sold by D, E and F = (Tickets sold by D) $+($ Tickets sold by E) $+($ Tickets sold by F)
$=7+24+14$
We get,
$=45$

Hence, total tickets sold by D, E and F together is 45 tickets
(v) Average number of tickets sold per student can be calculated as below

Average tickets sold per student $=($ tickets sold by $\mathrm{A}+\mathrm{B}+\mathrm{C}+\mathrm{D}+\mathrm{E}+\mathrm{F}) / 6$
$=(16+9+20+7+24+14) / 6$
We get,
$=90 / 6$
$=15$
Hence, average tickets sold per student is 15 tickets
8. The following bar graph shows the number of children, in various classes, in a school in Delhi.


Using the given bar graph, find:
(i) the number of children in each class.
(ii) the total number of children from Class 6 to Class 8
(iii) how many more children there are in Class 5 compared to Class 6?
(iv) the total number of children from Class 1 to Class 8
(v) the average number of children in a class

## Solution:

(i) From the given graph, the number of students in each class is as follows:

Class $1=100$ students
Class $2=90$ students
Class $3=100$ students
Class $4=80$ students
(ii) From the given graph, the number of students from Class 6 to Class 8 is as follows:

Class $6=90$ students
Class $7=70$ students
Class $8=50$ students
Hence, total number of students in Class 6 to Class 8 can be calculated as below:
Total students $=$ Students in Class 6 to Class 8
$=90+70+50$
We get,
$=210$
Hence, total number of students in Class 6, 7 and 8 are 210
(iii) From the given graph, students in Class 5 and Class 6 are as follows:

Class $5=120$ students
Class $6=90$ students
More students in Class 5 can be calculated as below
More students in Class 5 = 120-90
$=30$
Hence, number of more students in Class 5 are 30
(iv) Total number of students in class 1 to 8 can be calculated as below

Total number of students $=100+90+100+80+120+90+70+50$
We get,
$=700$ students
Hence, there are 700 students in class 1 to 8
(v) Average number of students in each class can be calculated as below

Average number of students in each class = (Total number of students in classes) /
Number of classes
$=700 / 8$
We get,
$=87.5$
9. The column graph, given above, shows the number of patients, examined by Dr.
V.K. Bansal, on different days of a particular week.

Use the graph to answer the following:
(i) On which day were the maximum number of patients examined?
(ii) On which day were the least number of patients examined?
(iii) On which days were equal number of patients examined?
(iv) What is the total number of patients examined in the week?


Solution:
(i) From the given graph, the maximum number of patients is examined on Tuesday
(ii) From the given graph, the minimum number of patients is examined on Friday
(iii) From the given graph, equal number of patients is examined on Sunday and

Thursday
(iv) Total number of patients examined in a week can be calculated as given below

Total number of patients examined in a week $=50+40+70+60+50+30$
We get,
$=300$ students
Hence, 300 patients are examined in a week
10. A student spends his pocket money on various items, as given below:

Books: Rs 380, Postage: Rs 30, Toilet items: Rs 240, Stationary: Rs 220 and
Entertainment: Rs 120
Draw a bar graph to represent his expenses.
Solution:
Given
The amount spent on items is as follows:
Books $=$ Rs 380
Postage $=$ Rs 30
Toilet items = Rs 240
Stationary = Rs 220
Entertainment = Rs 120
The bar graph of the above given data is as follows



[^0]:    Solution:

