## Exploring Patterns

For each pattern, follow these instructions:

1. Study the pattern your teacher has provided.
2. Build step 4 .
3. Make a sketch of step 4 and step 5 . How many units make up each step?
4. Use the pattern you discover to sketch step 10. How many units make up step 10 ?
5. Describe any number patterns you notice.
6. Suggest other ways to describe how this pattern grows.

Function $\qquad$

| step 4 | step 5 | step 10 |
| :--- | :--- | :--- |
|  |  |  |
| units: ___ | units:___ |  |

What patterns do you notice? $\qquad$
Can you suggest other ways this pattern might grow? $\qquad$

## Function

$\qquad$

| step 4 | step 5 | step 10 |
| :--- | :--- | :--- |
|  |  |  |
| units: $\ldots$ | units: ___ | units: |

What patterns do you notice?
Can you suggest other ways this pattern might grow?

Furction

| step 4 | step 5 | step 10 |
| :--- | :--- | :--- |
| units: | units: _____ |  |

What patterns do you notice? $\qquad$
Can you suggest other ways this pattern might grow? $\qquad$
$\qquad$

## Function

$\qquad$

| step 4 | step 5 | step 10 |
| :--- | :--- | :--- |
| units: | units: $\quad . \quad$ | units: $\quad . \quad$ |

What patterns do you notice?
Can you suggest other ways this pattern might grow? $\qquad$

## Function

$\qquad$

| step 4 | step 5 | step 10 |
| :--- | :--- | :--- |
| units: | units:_______ |  |

What patterns do you notice?
Can you suggest other ways this pattern might grow? $\qquad$
$\qquad$
$\qquad$

## Exploring Patterms

For each pattern, sketch steps 4 and 5 . Then predict how many units would be in step 10. Describe the pattern.

Fumction 1. Count the toothpicks.


How many would be in step 10 ? $\qquad$
How is the pattern changing or growing? $\qquad$
Function 2. Count the toothpicks.
1

2

3

$\square$ 5

How many would be in step 10 ? $\qquad$
How is the pattern changing or growing? $\qquad$
Function 3. Count the toothpicks.
1




5

How many would be in step 10 ? $\qquad$
How is the pattern changing or growing? $\qquad$

Punction 4 . Count the toothpicks.


5

How many would be in step 10 ? $\qquad$
How is the pattern changing or growing? $\qquad$
Fanction 5. Count the tiles.


How many would be in step 10 ? $\qquad$
How is the pattern changing or growing? $\qquad$
Function 6. Count the tiles.


How many would be in step $10 ?$ $\qquad$
How is the pattern changing or growing? $\qquad$

Find the next three numbers in each pattern. Then find step 10.
Describe in words how the pattern is changing.

## Punction 7.

| step | 1 | 2 | 3 | 4 | 5 | 6 | $\ldots$ | 10 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| result | 8 | 12 | 16 | - | - | - |  | - |

Describe the pattern. $\qquad$

## Punction 8.

| step | 1 | 2 | 3 | 4 | 5 | 6 | $\cdots$ | 10 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| result | 7 | 11 | 15 | - | - | - |  | - |

Describe the pattern.

## Function 9.

| step | 1 | 2 | 3 | 4 | 5 | 6 | $\ldots$ | 10 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| result | 8 | 13 | 18 | - | - | - |  | - |

Describe the pattern. $\qquad$

## Function 10.

| step | 1 | 2 | 3 | 4 | 5 | 6 | $\ldots$ | 10 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| result | 15 | 23 | 31 | - | - | - |  | - |

Describe the pattern. $\qquad$

## Function 11.

| step | 1 | 2 | 3 | 4 | 5 | 6 | $\ldots$ | 10 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| result | 25 | 29 | 33 | - | - | - |  | - |

Describe the pattern. $\qquad$

## Fmerion 12

| step | 1 | 2 | 3 | 4 | 5 | 6 | $\cdots$ | 10 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| result | 57 | 63 | 69 | - | - | - |  | -1 |

Describe the pattern.

## Punction 13.

| step | 1 | 2 | 3 | 4 | 5 | 6 | $\ldots$ | 10 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| result | 101 | 115 | 129 | - | - | - |  | - |

Describe the pattern.

Function 14.

| step | 1 | 2 | 3 | 4 | 5 | 6 | $\ldots$ | 10 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| result | 68 | 64 | 60 | $\ldots$ | $\ldots$ | $\ldots$ |  | - |

Describe the pattern. $\qquad$

Function 15.

| step | 1 | 2 | 3 | 4 | 5 | 6 | $\ldots$ | 10 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| result | 8 | 10.5 | 13 | - | - | - |  | - |

Describe the pattern. $\qquad$

## Function 16.

| step | 1 | 2 | 3 | 4 | 5 | 6 | $\ldots$ | 10 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| result | 2 | 4 | 8 | - | - | - |  | - |

Describe the pattern.
$\qquad$

## Graphing Functions



Function $\qquad$ Function

$f(n)$


Function

| $n$ | $f(n)$ |
| :---: | :---: |
| 1 |  |
| 2 |  |
| 3 |  |
| 4 |  |
| 5 |  |
| $\vdots$ |  |
| 17 |  |
| $n$ |  |

Function


Function

$f(n)$

$\qquad$

## Graphing Functions

Construct a $T$-table for each of these functions from Homework 1:
Exploring Patterns. Then graph each function on the grid. Determine the value of the function at step 0 and put this in the table too.

Punction 1

| $n$ | $f(n)$ |
| :---: | :---: |
| 1 |  |
| 2 |  |
| 3 |  |
| 4 |  |
| 5 |  |
| $\vdots$ |  |
| 10 |  |
| $\vdots$ |  |
| 17 |  |
| $n$ |  |

Function 4

| $n$ | $f(n)$ |
| :---: | :---: |
| 1 |  |
| 2 |  |
| 3 |  |
| 4 |  |
| 5 |  |
| $\vdots$ |  |
| 10 |  |
| $\vdots$ |  |
| 17 |  |
| $n$ |  |

Function 2

| $n$ | $f(n)$ |
| :---: | :---: |
|  |  |
| 1 |  |
| 2 |  |
| 3 |  |
| 4 |  |
| 5 |  |
| $\vdots$ |  |
| 10 |  |
| $\vdots$ |  |
| 17 |  |
| $n$ |  |

Function 5

| $n$ | $f(n)$ |
| :---: | :---: |
|  |  |
| 1 |  |
| 2 |  |
| 3 |  |
| 4 |  |
| 5 |  |
| $\vdots$ |  |
| 10 |  |
| $\vdots$ |  |
| 17 |  |
| $n$ |  |

Punction 3

| $n$ | $f(n)$ |
| :---: | :---: |
| 1 |  |
| 2 |  |
| 3 |  |
| 4 |  |
| 5 |  |
| $\vdots$ |  |
| 10 |  |
| $\vdots$ |  |
| 17 |  |
| $n$ |  |

## Function 6

| $n$ | $f(n)$ |
| :---: | :---: |
|  |  |
| 1 |  |
| 2 |  |
| 3 |  |
| 4 |  |
| 5 |  |
| $\vdots$ |  |
| 10 |  |
| $\vdots$ |  |
| 17 |  |
| $n$ |  |



Construct a T-table for each of these functions from Homework 1:
Exploning Patterns. Then graph each function on the grid. Determine the value of the function at step 0 and put this in the table too.

Function 11

| $n$ | $f(n)$ |
| :---: | :---: |
| 1 |  |
| 1 |  |
| 2 |  |
| 3 |  |
| 4 |  |
| 5 |  |
| $\vdots$ |  |
| 10 |  |
| $\vdots$ |  |
| 17 |  |
| $n$ |  |

Function 14

| $n$ | $f(n)$ |
| :---: | :---: |
| 1 |  |
| 2 |  |
| 3 |  |
| 4 |  |
| 5 |  |
| $\vdots$ |  |
| 10 |  |
| $\vdots$ |  |
| 17 |  |
| $n$ |  |

Function 15


Function 12

| 11 | $f(1)$ | 11 | $f(n)$ |
| :---: | :---: | :---: | :---: |
| 1 |  |  |  |
|  |  |  |  |
| 2 |  | 2 |  |
| 3 |  | 3 |  |
| 4 |  | 4 |  |
| 5 |  | 5 |  |
| : |  | : |  |
| 10 |  | 10 |  |
| : |  | : |  |
| 17 |  | 17 |  |

Function 16

| $n$ | $f(n)$ |
| :---: | :---: |
| 1 |  |
| 2 |  |
| 3 |  |
| 4 |  |
| 5 |  |
| $\vdots$ |  |
| 10 |  |
| $\vdots$ |  |
| 17 |  |
| $n$ |  |




| $n$ | $f(n)$ |
| :---: | :--- |
| 0 |  |
| 1 |  |
| 2 |  |
| 3 |  |
| $\vdots$ |  |
| 17 |  |
|  |  |

Name

## Working Backward

Below are ten functions and six pictures. Below each pictorial representation, write the letter of the matching function. On the back of this sheet, design a pictorial representation for the four functions that are not pictured. Label them with their functions.
a. $f(n)=4 n-3$
b. $f(n)=3 n+2$
c. $f(n)=2 n+2$
d. $f(n)=4 n+1$
e. $f(n)=2 n+3$
f. $f(n)=4 n+4$
h. $f(n)=6 n-5$
i. $f(n)=6 n-1$

1. count squares


Function $\qquad$ Function $\qquad$
5. count hexagons


Function $\qquad$
2. count circles


Function $\qquad$
6. count squares


Function $\qquad$

## Working Backward

Below are nine functions. For each one, design a pictorial representation and show three steps. Use polygons, lines, toothpicks, dots, or other shapes. Be creative.

| 1. $f(n)=2 n+1$ | 2. $f(n)=2 n$ | 3. $f(n)=4 n+2$ |
| :---: | :---: | :---: |
|  |  |  |
| 4. $f(n)=4 n$ | 5. $f(n)=4 n+4$ |  |
| 7. $f(n)=2 n+3$ |  | 6. $f(n)=5 n+3$ |
|  |  |  |



| $n$ | $f(n)$ |
| :---: | :---: |
| 0 |  |
| 1 |  |
| 2 |  |
| 3 |  |
| $\vdots$ |  |
| 23 |  |
| $n$ |  |

## Advanced Functions

Function


Function

| $n$ | $f(n)$ |
| :---: | :---: |
| 0 |  |
| 1 |  |
| 2 |  |
| 3 |  |
| $\vdots$ |  |
| 23 |  |
| $n$ |  |

Rumction $\qquad$

| $n$ | $f(n)$ |
| :---: | :---: |
| 0 |  |
| 1 |  |
| 2 |  |
| 3 |  |
| $\vdots$ |  |
| 23 |  |
| $n$ |  |

Function $\qquad$

| $n$ | $f(n)$ |
| :--- | :--- |
| 0 |  |
| 1 |  |
| 2 |  |
| 3 |  |
| $\vdots$ |  |
| 23 |  |
| $n$ |  |

Function $\qquad$

| $n$ | $f(n)$ |
| :--- | :--- |
| 0 |  |
| 1 |  |
| 2 |  |
| 3 |  |
| $\vdots$ |  |
| 23 |  |
| $n$ |  |



## Advanced Functions

Fill in a T-table for each function below. Then graph the function. Write the function's expression in the bottom of the table.

## Pumetion



Function 3


Punction 2


Function 4



Fill in a T-table for each function below. Then graph the function. Write the function's expression in the bottom of the table.

## Punction 3






Function 7



Fill in a T-table for each function below. Then graph the function. Write the function's expression in the bottom of the table.

## Function 9



Function 11

| 1 | 5.7 | $n$ | $f(n)$ |
| :--- | :--- | :---: | :---: |
| 2 | 8 | 0 |  |
| 3 | 10.3 | 1 |  |
|  |  | 3 |  |
|  |  | 37 |  |
|  |  | $n$ |  |

Runction 10


## Function 12




1. Randy already has $\$ 70$ in his savings account. He will add $\$ 40$ per month. How much money will he have?
A) How much money will he have after the first five months?
B) How much money will he have after the tenth month?
c) How much money will he have after the eighteenth month?
2. Angela already has $\$ 310$ in her savings account. She will add $\$ 35$ per month. How many months will it take before she and Randy have the same amount of money in their accounts? How much will each of them have?
3. Randy wants to know when he will have at least $\$ 1,000$. Find a way to determine this for him.
4. Angela finds she has exactly $\$ 1,220$. How many months has she been saving?

Name

## Banking on Algebra

1. Derek has $\$ 75$ in his savings account. He will add $\$ 25$ every month. Use this T-table to show how Derek's account will grow. Write an expression or formula and make a graph below.

| Derek's Account <br> month |  | principal |
| :--- | :---: | :---: |
| 0 |  |  |
| 1 |  |  |

2. Rosa has $\$ 306$ in her savings account. She will add $\$ 14$ every month. Use this T-table to show how Rosa's account will grow. Write an expression or formula and make a graph below.

| Rosa's Account |  |
| :---: | :---: |
| month | principal |
| 0 |  |
| 1 |  |
| 2 |  |
| 3 |  |
| 4 |  |
| 5 |  |
| $m$ |  |

3. When will Derek have $\$ 700$ ? $\qquad$
4. When will Rosa and Derek have the same amount of money? $\qquad$
5. How much money will they each have then? $\qquad$


What scale has been used for the horizontal axis? One unit $=$ $\qquad$ .

What scale has been used for the vertical axis? One unit $=$ $\qquad$ .
6. San wants to buy a bicycle for $\$ 295$. He currently has $\$ 72$ in his account. If he adds $\$ 27$ each month, when will he have enough money for the bike? $\qquad$

| San's Account |  |
| :---: | :---: |
| month | principal |
| 0 |  |
| 1 |  |
| 2 |  |
| 3 |  |
| 4 |  |
| 5 |  |
| $m$ |  |

7. Keisha wants the same bike that San wants. If she already has $\$ 115$ in her account, and she adds $\$ 16$ per month, can she buy her bike before San can buy his? $\qquad$
Keisha's Account

| month | principal |
| :---: | :---: |
| 0 |  |
| 1 |  |
| 2 |  |
| 3 |  |
| 4 |  |
| 5 |  |
| $m$ |  |

Graph the function for problems 6 and 7 on this grid. Choose a scale that allows the data to fit. Label each function on the graph with its formula.

8. Chris has $\$ 39$ in the bank. He add $\$ 32$ to it each month. He wants to buy a bike that costs $\$ 435$. Every month the bike's price is reduced by $\$ 10$. How many months will it take for Chris to afford the bike? $\qquad$

| Chris's Account <br> month | principal |
| :---: | :--- | :---: | :---: |$\quad$| Bike Sale |  |  |
| :---: | :---: | :---: |
| month | bike price |  |
| 0 |  | 0 |
| 1 |  | $\$ 435$ |
| 2 |  | $\$$ |
| 3 | 3 |  |
| 4 |  | 4 |
| 5 | 5 |  |
| $m$ |  | $m$ |

Graph the function for problem 8 on this grid. Choose a scale that allows the data to fit. Label each function on the graph with its formula.


What scale did you use for the horizontal axis?

One unit = $\qquad$ .

What scale did you use for the vertical axis? One unit $=$ $\qquad$ .

Schedulle of Rates


|  |  |  | 镸 Evening |  | $\square$ Night |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| From: <br> Redding | $\begin{gathered} 1 \text { st } \\ \min . \end{gathered}$ | add'l. min. | 1st <br> min. | add'1. <br> min. | 1st min. | add'l. <br> min. |
| TO: |  |  |  |  |  |  |
| Alturas | \$0.11 | \$0.07 | \$0.09 | \$0.06 | \$0.07 | \$0.04 |
| Challenge | 0.12 | 0.10 | 0.10 | 0.07 | 0.08 | 0.05 |
| Millville | 0.13 | 0.11 | 0.11 | 0.09 | 0.08 | 0.06 |
| Oroville | 0.14 | 0.12 | 0.13 | 0.10 | 0.09 | 0.07 |
| Red Bluff | 0.15 | 0.13 | 0.13 | 0.11 | 0.10 | 0.07 |

## The Long-Distance Cominection

## Schedull or Rates

|  | M | Tu | W | Th | Su |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $8 \mathrm{AM}-5 \mathrm{PM}$ |  | 5效 |  |  |  |
| $5 \mathrm{PM}-11 \mathrm{PM}$ |  |  |  | \| |  |
| $11 \mathrm{PM}-8 \mathrm{AM}$ | $\square$ |  |  |  |  |


| Fronis: Redding | 517ex Day |  |  |  | $\square$ Night |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\begin{gathered} \text { 1st } \\ \text { min. } \end{gathered}$ | add'l. <br> min. | $\begin{aligned} & \text { 1st } \\ & \text { min. } \end{aligned}$ | add'l. <br> min. | $\begin{gathered} 1 \mathrm{st} \\ \text { min. } \end{gathered}$ | add'l. <br> min. |
| Alturas | \$0.11 | \$0.07 | \$0.09 | \$0.06 | \$0.07 | \$0.04 |
| Challenge | 0.12 | 0.10 | 0.10 | 0.07 | 0.08 | 0.05 |
| Millville | 0.13 | 0.11 | 0.11 | 0.09 | 0.08 | 0.06 |
| Oroville | 0.14 | 0.12 | 0.13 | 0.10 | 0.09 | 0.07 |
| Red Bluff | 0.15 | 0.13 | 0.13 | 0.11 | 0.10 | 0.07 |

3. Fill in the T-tables to compare the phone rates of calls from Redding to Oroville.

| Day |  | Evening |  | Night |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| min. | price | min. | price | min. | price |
| 0 |  | 0 |  | 0 |  |
| 1 |  | 1 |  | 1 |  |
| 2 |  | 2 |  | 2 |  |
| 3 |  | 3 |  | 3 |  |
| : |  | : |  | . |  |
| 13 |  | 13 |  | 13 |  |
| $m$ |  | m |  | $m$ |  |

2. Fill in the T-tables to compare the phone rates of calls from Redding to Red Bluff.

| Day |  | Evening |  | Night |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| min. | price | min. | price | min. | price |
| 0 |  | 0 |  | 0 |  |
| 1 |  | 1 |  | 1 |  |
| 2 |  | 2 |  | 2 |  |
| 3 |  | 3 |  | 3 |  |
| : |  | : |  | : |  |
| 13 |  | 13 |  | 13 |  |
| $m$ |  | $m$ |  | $m$ |  |

3. Fill in the T-tables to compare the phone rates of calls from Redding to Challenge.

| Day |  |
| :---: | :---: |
| min. | price |
| 0 |  |
| 1 |  |
| 2 |  |
| 3 |  |
| $\vdots$ |  |
| 13 |  |
| $m$ |  |


| Evening |  |
| :---: | :---: |
| min. | price |
| 0 |  |
| 1 |  |
| 2 |  |
| 3 |  |
| $\vdots$ |  |
| 13 |  |
| $m$ |  |

Night

| min. | price |
| :---: | :---: |
| 0 |  |
| 1 |  |
| 2 |  |
| 3 |  |
| $\vdots$ |  |
| 13 |  |
| $m$ |  |

