

Exploring Space Through MATH

Applications in Geometry



STUDENT
EDITION

Oh, Chute!

Background

A new Capsule Parachute Assembly System (CPAS), currently being designed and tested by engineers at NASA Johnson Space Center in Houston, Texas, is destined to become part of the new space vehicle, which will transport humans beyond Earth's orbit to places like the Moon, Mars, or even nearby asteroids. This parachute system will include a new crew return module with a capsule shape, much like the capsule used during the Apollo program (Figure 1). The CPAS will help the capsule decelerate (or reduce its speed) once it re-enters Earth's atmosphere, enabling it to land safely.



Figure 1: Shape comparison of a new crew module (left) and the previous Apollo capsule from the 1960's (right); not to scale.

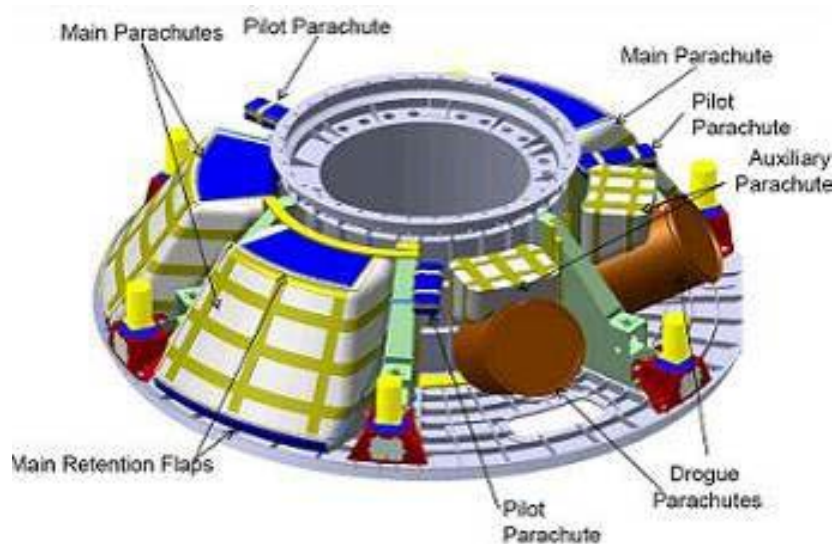


Figure 2: Artist's concept of the Capsule Parachute Assembly System (CPAS)



Figure 2 shows the configuration of CPAS as it is installed on the parachute compartment. The parachutes are stored around the transfer tunnel and it has a total of six parachute bays. Three of the bays are for the main parachutes and the other bays contain a combination of drogue, pilot, and auxiliary parachutes. Drogue parachutes are designed to slow the vehicle. Pilot parachutes help the vehicle to glide to a safe landing. The auxiliary parachutes are reserved in case other parachutes fail to deploy. A similar parachute system was used during the Apollo program in the 1960's and early 1970's to provide a safe water landing.



Figure 3: An Apollo Command Module nears splashdown in the South Pacific Ocean

As with any engineering design, the proposed CPAS will require adjustments to the design based on the results of thorough testing. Since testing the actual capsule could be very costly, engineers plan to instead attach the parachute system to a test structure. NASA has already created a test vehicle to replicate the weight, aerodynamics, and center of mass of the new capsule; however, it will be used only to test the parachute system when released from an aircraft (approximately 25,000 feet above the Earth's surface).

Instructional Objectives

You will

- use scale factor to complete a table;
- use the Pythagorean Theorem;
- calculate the volume of a cylinder;
- calculate the area of a circle;
- investigate how changes in scale factor affect volume; and
- investigate how changes in scale factor affect area.

**Problem**

The Systems Architecture and Integration Office at NASA Johnson Space Center is designing and testing the Capsule Parachute Assembly System (CPAS) using a test vehicle as the capsule. Figure 4 shows the parachute compartment (light-colored segment) sitting atop the test vehicle structure (dark-colored segment). Figure 5 is a picture of a small 3D model of the parachute compartment that has been scaled down to one-twelfth of the original size.



Figure 4: Parachute compartment atop the test vehicle structure



Figure 5: Parachute compartment scaled model

Directions: Show all work and justify your answers to questions 1-8. Discuss answers to be sure everyone understands and agrees on the solutions. Round all answers to the nearest thousandth and label them with the appropriate units.

1. An illustration of some of the key structural components on the parachute compartment is provided in Figure 6. Table 1 contains the dimensions for some components on the actual parachute compartment and the model.

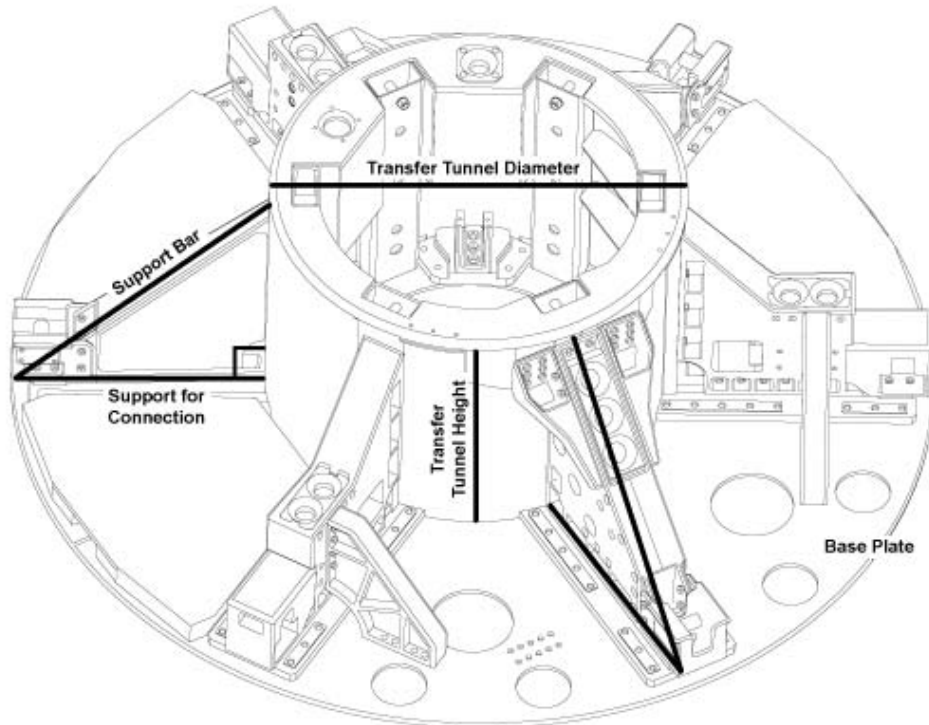


Figure 6: Engineer drawing of the parachute compartment

Table 1: Parachute compartment dimensions

Part name	Actual (m)	3D model (cm)
Base plate diameter	1.820	15.167
Transfer tunnel height		
Transfer tunnel diameter	1.000	
Support bar length		12.900
Support for connection length	0.410	

- a. The scale factor of the 3D model to the actual parachute compartment is $\frac{1}{12}$. Use this scale factor to complete Table 1.
- b. How can you use Figure 6 to find the actual height of the transfer tunnel?



- c. Calculate the actual height, h_0 of the transfer tunnel.

2. Astronauts use the transfer tunnel on the parachute compartment to move from one module to another. Calculate the actual volume, V_0 of the transfer tunnel.

3. Engineers have determined that the volume of the tunnel needs to increase for astronauts to move through it with ease. Use a scale factor of 1.500 to increase the volume of the tunnel.
 - a. Calculate the new radius, r_1 of the transfer tunnel.

 - b. Calculate the new height, h_1 of the transfer tunnel.

 - c. Calculate the new volume, V_1 of the transfer tunnel using h_1 and r_1 from the previous questions.

4. The parachute compartment must fit properly on the test vehicle. The recommended area of the base plate must be less than 2.7 m^2 . Use the dimensions in Table 1 to determine if the area of the base plate, A_0 meets the criteria.

