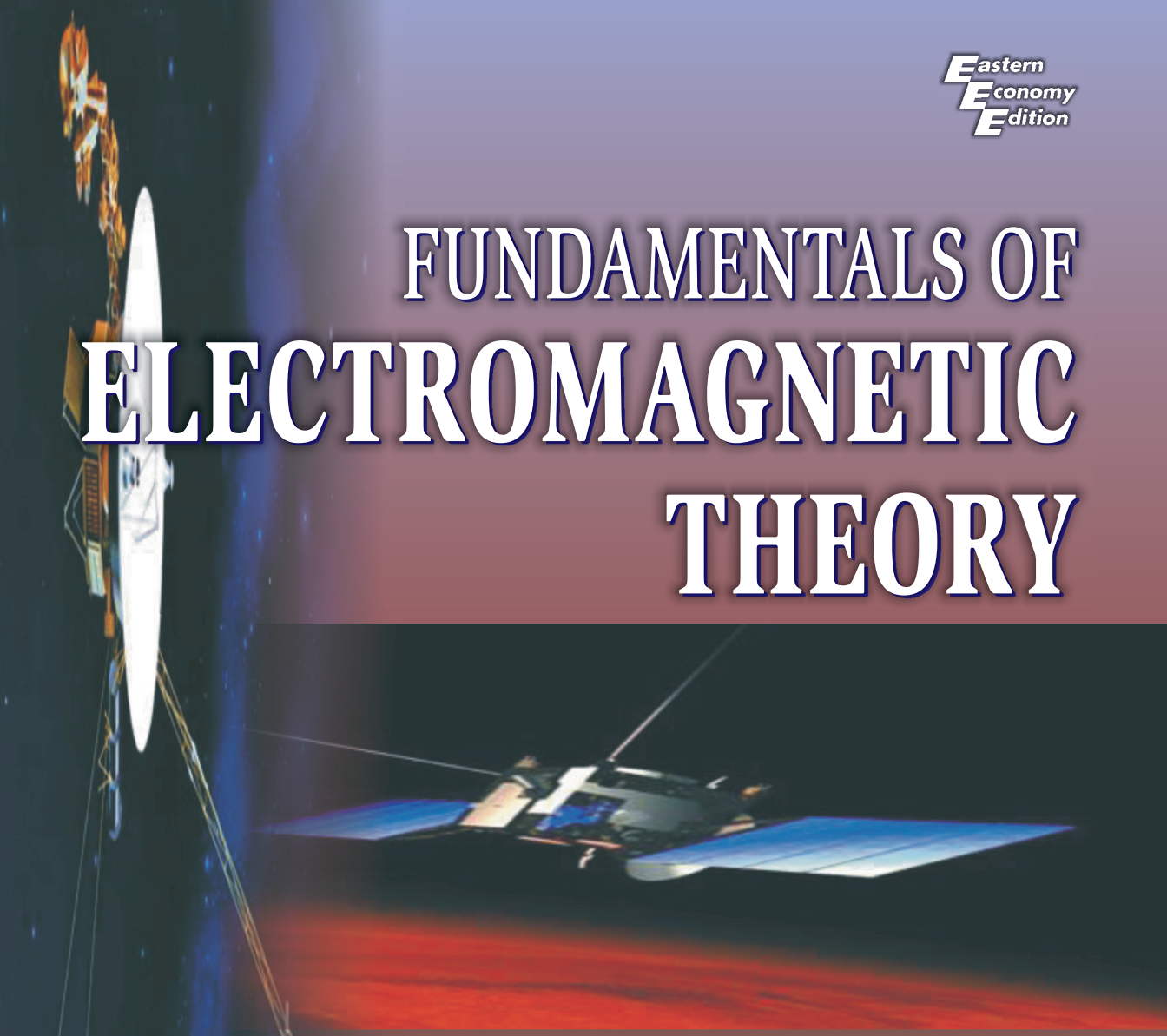
Eastern Economy Edition

FUNDAMENTALS OF ELECTROMAGNETIC THEORY



Saroj K. Dash • Smruti R. Khuntia

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Fundamentals of ELECTROMAGNETIC THEORY

SECOND EDITION

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FUNDAMENTALS OF ELECTROMAGNETIC THEORY, Second Edition
Saroj Kumar Dash and Smruti Ranjan Khuntia

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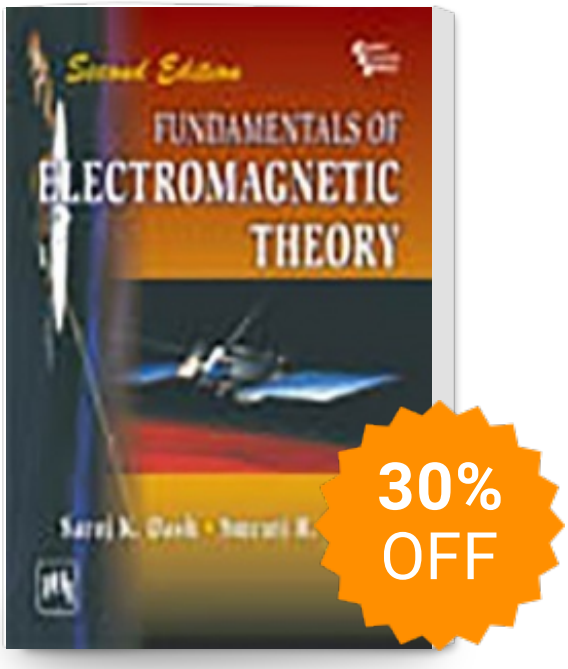
Fundamentals Of Electromagnetic Theory



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