



North America Dynamic Wind Generator Modeling Update

Based on work performed by the WECC Wind Generator Modeling Group and the IEEE Dynamic Performance of Wind Power Generation Working Group

US Membership to the IEC TF88 WG27

Abraham Ellis

Sandia National Laboratories

aellis@sandia.gov

Yuriy Kazachkov

Siemens-PTI

yuriy.kazachkov@siemens.com

Eduard Muljadi

National Renewable Energy Laboratory

eduard.muljadi@nrel.gov

Juan Sanchez-Gasca, Nicholas Miller

GE Energy - PSLF

juan1.sanchez@ge.com, nicholas.miller@ge.com

Robert Zavadil

EnerNex Corporation

bobz@enernex.com

Pouyan Pourbeik

Electric power Research Institute

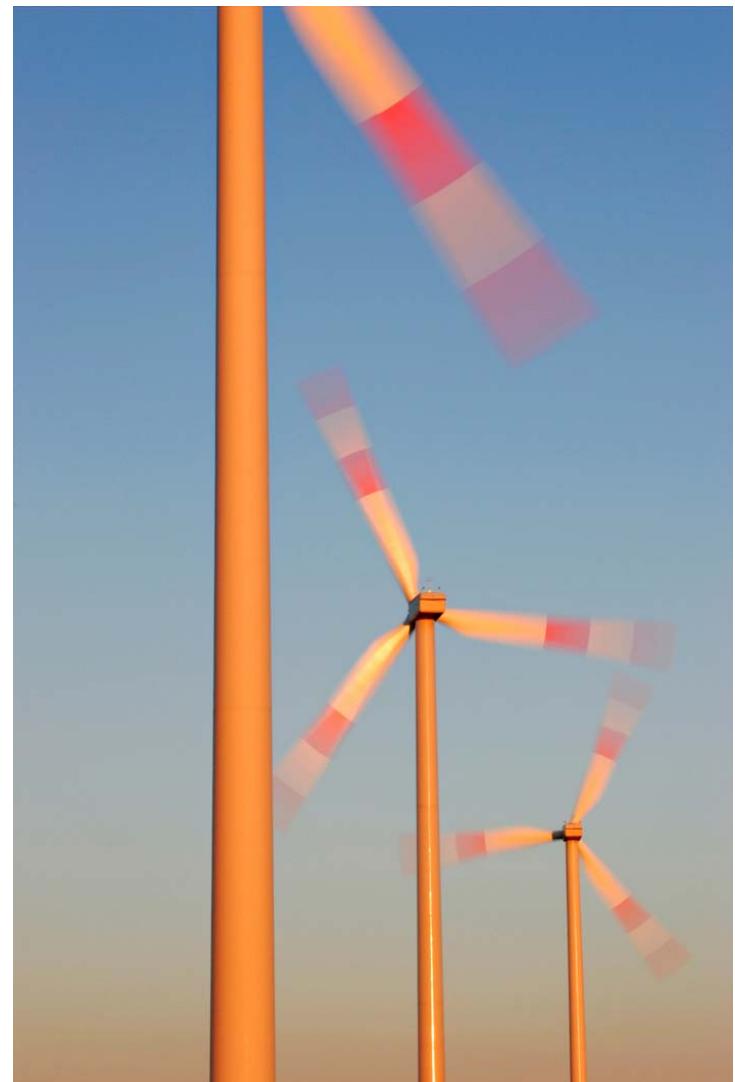
PPourbeik@epri.com

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Presentation Contents

1. Status of WECC WGMG generic modeling effort and related activities in IEEE & NERC.
2. Review of WECC generic model structures, testing and verification
3. Simplified aerodynamic conversion representation for generic models
4. Model validation and parameter identification
5. Wind power plant network equivalent for power flow and dynamic simulations



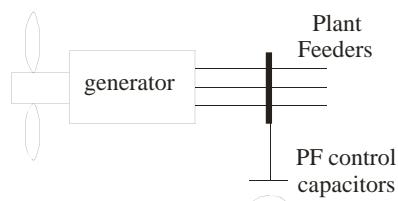


Wind Turbine Generator Topologies

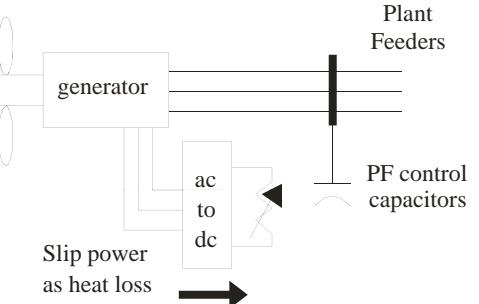
- **Four basic WTG types based on grid interface technology**

- Type 1 – Fixed-speed, conventional induction generator
- Type 2 – Variable slip, induction generators with variable rotor resistance
- Type 3 – Variable speed, doubly-fed asynchronous generators with rotor-side converter
- Type 4 – Variable speed, asynchronous generators with full converter interface

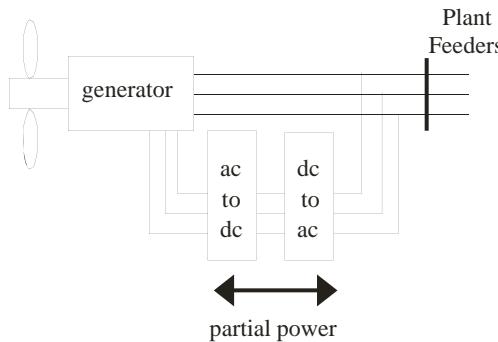
Type 1



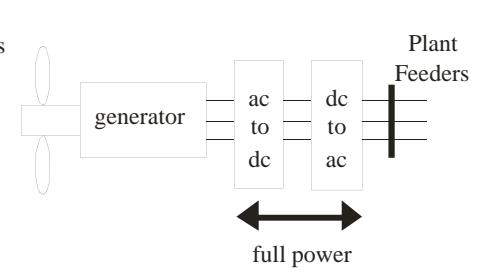
Type 2



Type 3



Type 4





WECC Generic Model Implementation

- Completed generic models implemented as standard-library models in PSSE/PSLF completed

PSLF/17

| Model Type | Type 1 | Type 2 | Type 3 | Type 4 |
|-------------------------------------|-------------|-------------|-------------|-------------|
| Generator | wt1g | wt2g | wt3g | wt4g |
| Excitation / Controller | | wt2e | wt3e | wt4e |
| Turbine | wt1t | wt2t | wt3t | |
| Pitch Controller/Pseudo Gov. | wt1p | wt2p | wt3p | |

PSSE/32

| Generic model | WT1 | WT2 | WT3 | WT4 |
|----------------------------------|--------------|--------------|-------------|-------------|
| Generator | WT1G | WT2G | WT3G | WT4G |
| EI. Controller | | WT2E | WT3E | WT4E |
| Turbine/shaft | WT12T | WT12T | WT3T | |
| Pitch control | | | WT3P | |
| Pseudo Gov/: aerodynamics | WT12A | WT12A | | |

- **Key Participants**
 - Siemens (PSSE), General Electric (PSLF), DOE (Sandia National Laboratories and NREL), Consultants, Universities, other stakeholders
- **Current focus**
 - Additional model validation, refinement, upgrade
 - Identification of generic model parameters



Partial List of WTG Types

| Type 1 | Type 2 | Type 3 | Type 4 |
|--|--------------------------------|--|-------------------------------------|
| Vestas NM72 1.65 MW, 50/60 Hz | Vestas V80 1.8 MW, 60Hz | GE 1.5 MW, 50/60 Hz | GE 2.5XL 2.0 MW, 50/60 Hz |
| Vestas V82 1.65 MW, 50/60Hz | Vestas V47 660 kW, 50/60 Hz | GE 3.6 MW, 50/60 Hz | Clipper 2.5 MW, 50/60 Hz |
| BONUS (now Siemens) 1.3 MW, 50/60 Hz | Gamesa G80 1.8 MW, 60 Hz | Gamesa G80 2 MW, 50 Hz | Enercon E66 1.8 MW, 50 Hz |
| BONUS (now Siemens) 2.3 MW, 50 Hz | Suzlon S88 2.1 MW, 50Hz | NORDEX N80 2.5 MW, 50Hz | Enercon E70 2.0 MW, 50 Hz |
| Mitsubishi MWT100a 1 MW, 60 Hz | | REPower MD70 and MD77 1.5 MW, 50Hz | Siemens, 2.3VS82, 2.3MW, 50/60Hz |
| Suzlon S66 1.25 MW, 50 Hz | | REPower MM70 and MM82 2.0 MW, 50Hz | Kennetech 33-MVS, 400kW, 60Hz |
| | | Mitsubishi MWT- 92/95 2.4 MW | |
| | | Fuhrlaender FL 2.5 MW, 60 Hz | |



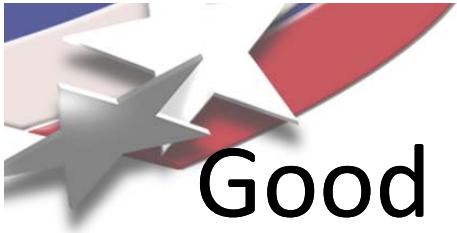
Related Activities

- **IEEE DPWPG Task Force**
 - Verification, enhancement of WECC generic models
 - Paper on Specifications for Wind Power Plant models
 - Paper on Validation Procedures for Wind Power Plant models
 - Outreach (Tutorials)
 - Coordination with WECC, NERC (IVGTF), UWIG, CIGRE, IEC, ...
- **UWIG/EnerNex (DOE funding)**
 - Develop user documentation for generic and turbine-specific wind turbine models; conduct training seminars
 - Verify performance of generic and vendor-specific models
 - Validate of models against field test results



Related Activities

- **NERC IVGTF Work Plan, Task 1.1 (Planning)**
 - Valid, generic, non-confidential, and public standard power flow and stability (positive-sequence) models [...] needed
 - Models should be readily validated and publicly available to power utilities and all other industry stakeholders
 - Model parameters should be provided by manufacturers
 - Common model validation standard [...] should be adopted
 - Review the Modeling, Data and Analysis (MOD) standards to identify any need modifications to address variable generation modeling and model validation



Good Progress, More Work Needed

- **Generic models emerging as the correct approach**
 - Pressure continues to build in North America, Europe
 - Several technical activities underway to validate, improve
 - Strong trend among manufacturers to replace custom models with adjusted generic models
- **Need to build on recent progress with generic models**
 - Include a more complete set of control options
 - Programmed inertia, frequency support features, LVRT details, etc.
 - Perform model validation, develop parameter sets
 - Develop model documentation and application guides
- **Coordination of related efforts is key**
- **Ultimate goal: full-featured, industry standard models**
 - In the meantime, manufacture models are still useful in cases where specific control features not available in the generic models have a substantial impact



Description of WECC Generic Models

References:

- Y. Kazachkov, S. Stapleton, “Do Generic Dynamic Simulation Wind Turbine Models Exist?”, WindPower 2005, Denver, Colorado, May 2005
- N. W. Miller, W. W. Price, J. J. Sanchez-Gasca, “Dynamic Model of GE’s 1.5 and 3.6 MW Wind Turbine Generators – Model Structure, Simulation Results, and Model Validation”, CIGRE Technical Brochure 328, *Modeling and Dynamic Performance of Wind Generation as it Relates to Power System Control and Dynamic Performance*, CIGRE WG C4.601, August, 2007
- WECC WGMG, “Generic Wind Plant Models for Power System Studies”, WindPower 2006, Pittsburgh, PA, June 2006
- WECC WGMG, “Development and Validation of WECC Variable Speed Wind Turbine Dynamic Models for Grid Integration Studies”, WindPower 2007, Los Angeles, CA, June 2007



WECC Generic Models

- **WECC WGMG Goals**

- Specify generic, non-proprietary models for large-scale power system simulations (positive-sequence models)
- Generic models are parametrically adjustable to any specific wind turbine of the same type in the market
- Models are simplified, but major dynamic behavior is maintained
 - Find balance between simplification and performance. For example, representation of aerodynamic conversion should be simplified to avoid using proprietary C_p curves. Too much simplification is not good: a model does not perform well if aerodynamics is ignored (e.g. constant mechanical power)
- Perform model testing and as much validation as possible
- Implement in PSSE and PSLF with full documentation and default parameter sets



WECC Generic Models

- **Technical Specifications**

- Application: electrical disturbances (not wind disturbances), primarily grid faults external to the plant, typically 3 to 6 cycle duration.
- Typical simulation time frame of interest are 20 to 30 seconds, with a $\frac{1}{4}$ cycle integration time step. Wind speed assumed to be constant.
- Model able to handle oscillatory modes from dc to 5 Hz.
- Initialize from power flow at full or partial power; able to handle user-specified wind speed
- Speed and voltage protection modeled separately
- Represent machine inertia and first shaft torsional mode characteristics
- The models should be applicable to strong and weak systems with a short circuit ratio of 2.5 and higher at the point of interconnection
- Shunt capacitors and any other reactive support equipment modeled separately with existing standard models



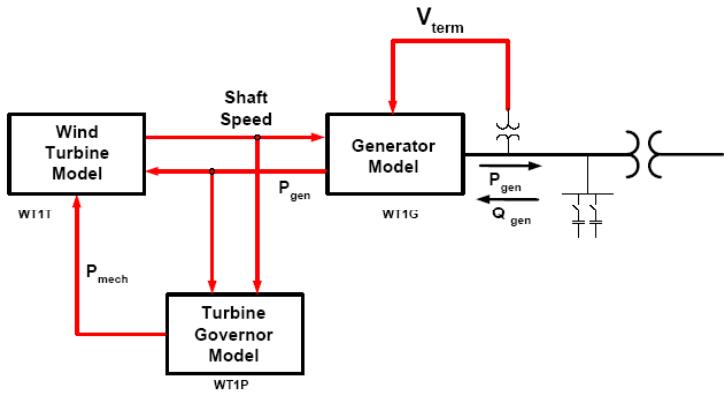
Response to Frequency Disturbances

- The generic WTG models were not developed with the intent of being accurate for the study of frequency excursions on the power system, or to reproduce the behavior of advanced power management features that are imminently becoming available from some WTG manufacturers (such as programmed inertia and 'spinning reserve' by spilling wind).
- We need to work further with Manufacturers to better understand response to frequency disturbances and thus improve the models.



WT1 Generic Model

Basic Description



Modules: WT1T, WT1P, WT1G

Generator model is conventional induction machine

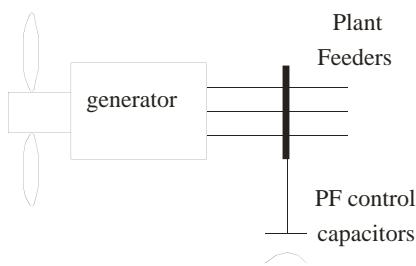
Default model data provided in documentation
(Mitsubishi MWT1000A)

Single or two-mass shaft model

Power factor correction capacitor must be provided
and initialized from load flow data

No special initialization or run-time script needed

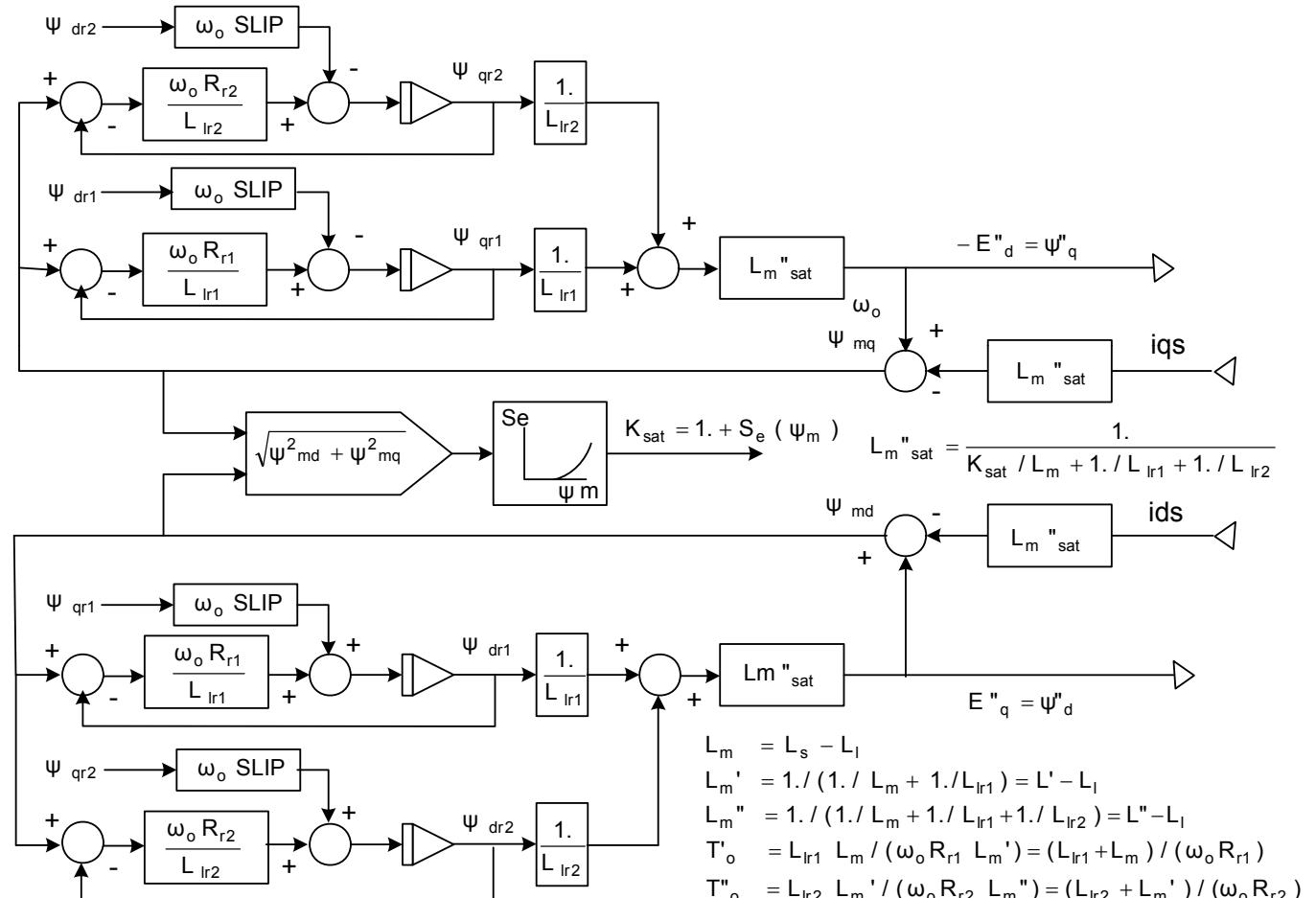
No special adjustment needed for wind farm representation





WT1G Induction Generator Model

WT1 Generic Model

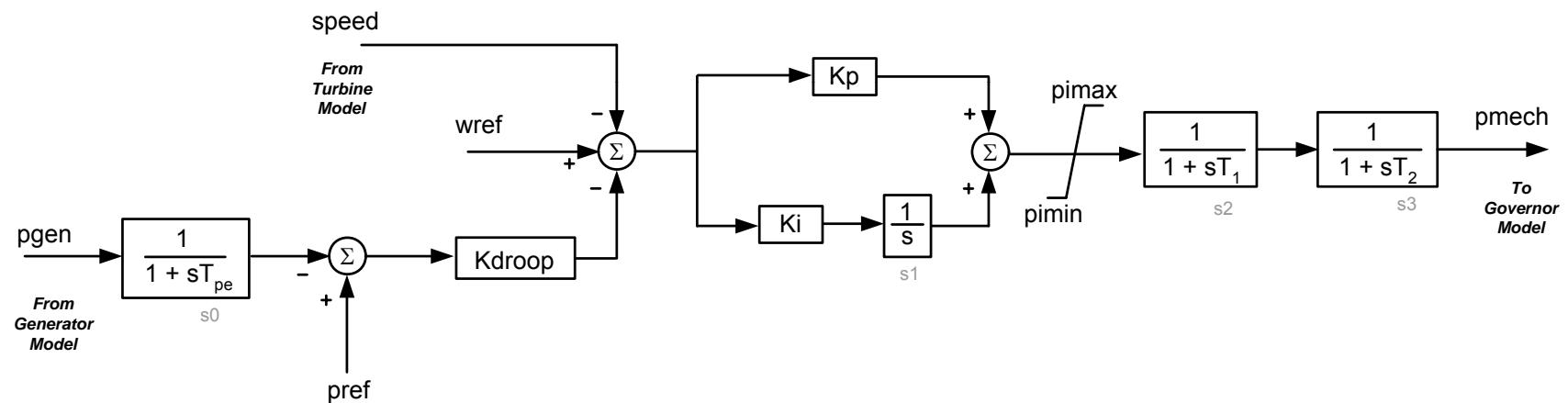


Model simulates a one-cage model if L_{pp} is equal to L_p . Otherwise, it simulates a two-cage induction generator.
If L_{pp} or T_{ppo} are 0., the model sets $L_{pp} = L_p$.



WT1 Generic Model

WT1P Pitch Control Model



Note: For disturbances involving frequency drops this is not necessarily accurate – should set pimax to rated turbine output to avoid any response from the turbine.



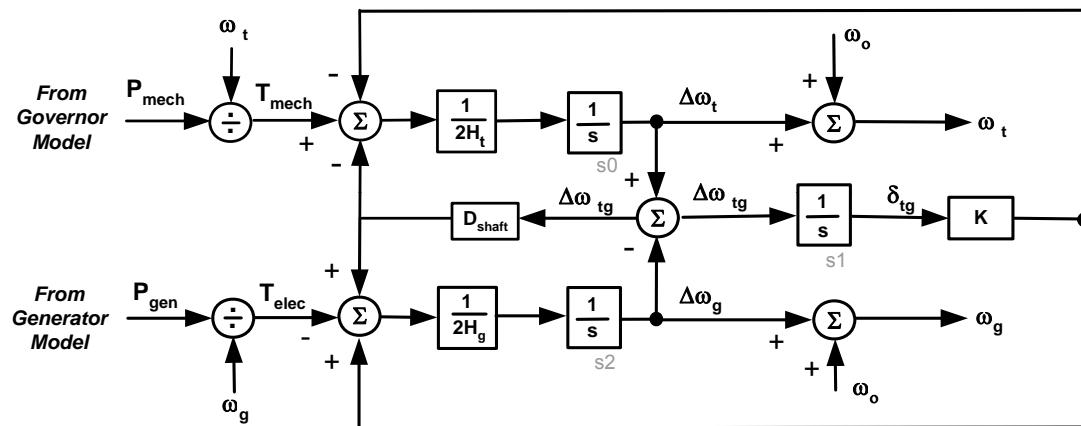
WT1 Generic Model

WT1T Two-mass model

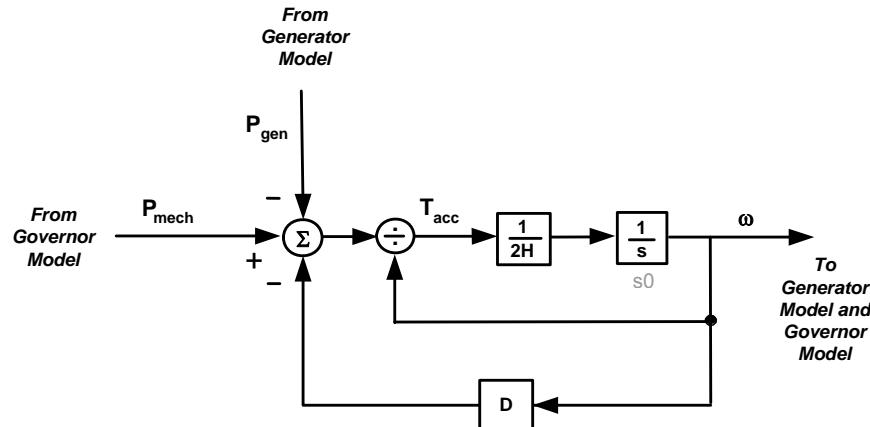
$$H_t = H_{tfrac} \cdot H$$

$$H_g = H - H_t$$

$$K = 2 (2\pi Freq1)^2 H_t \frac{H_g}{H}$$



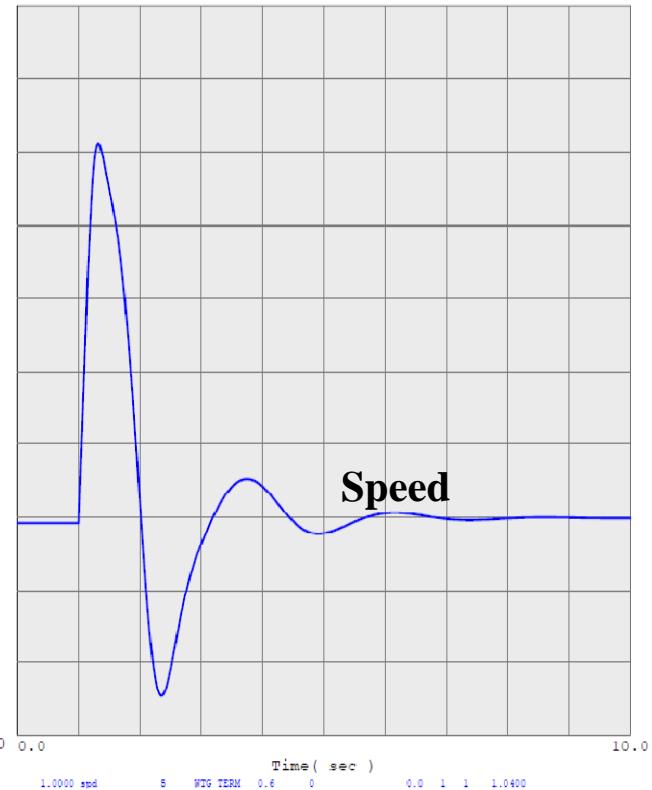
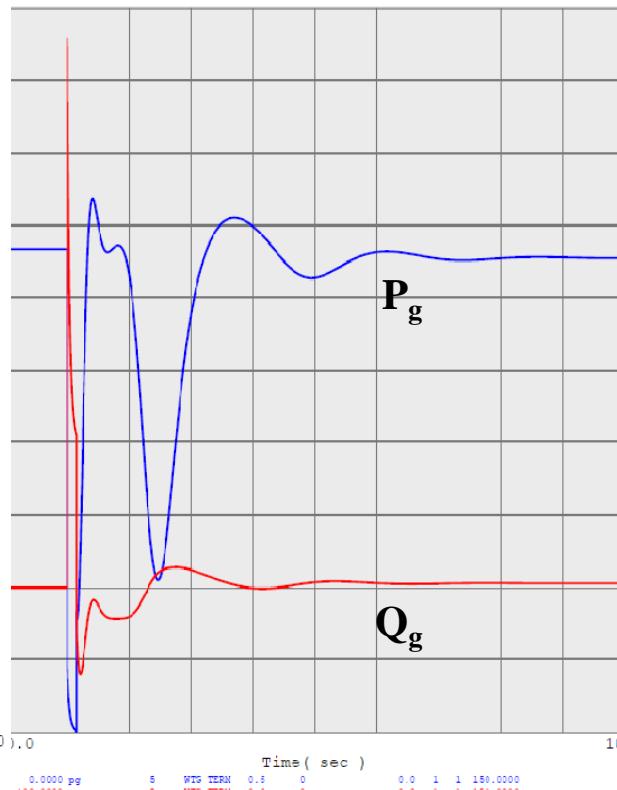
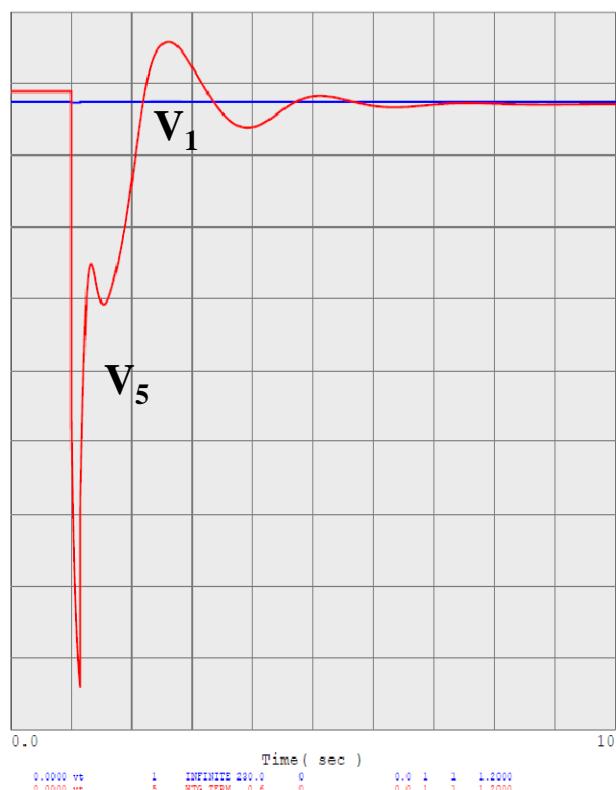
WT1T Single mass model ($H_{tfrac} = 0$)





WT1 Fault Test

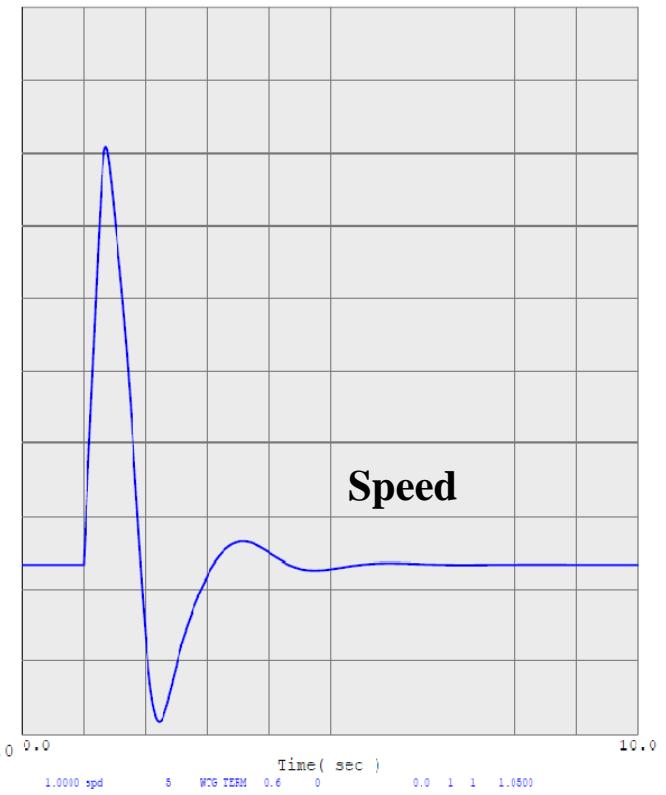
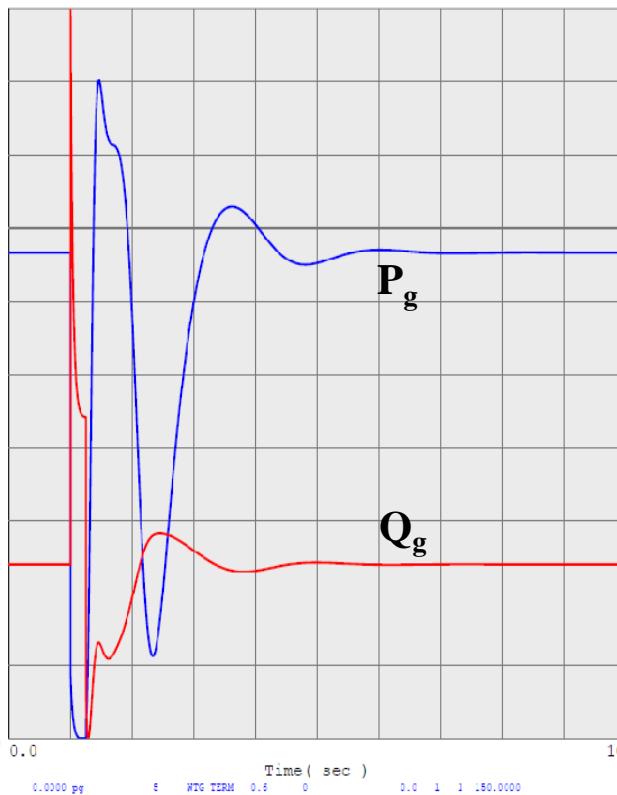
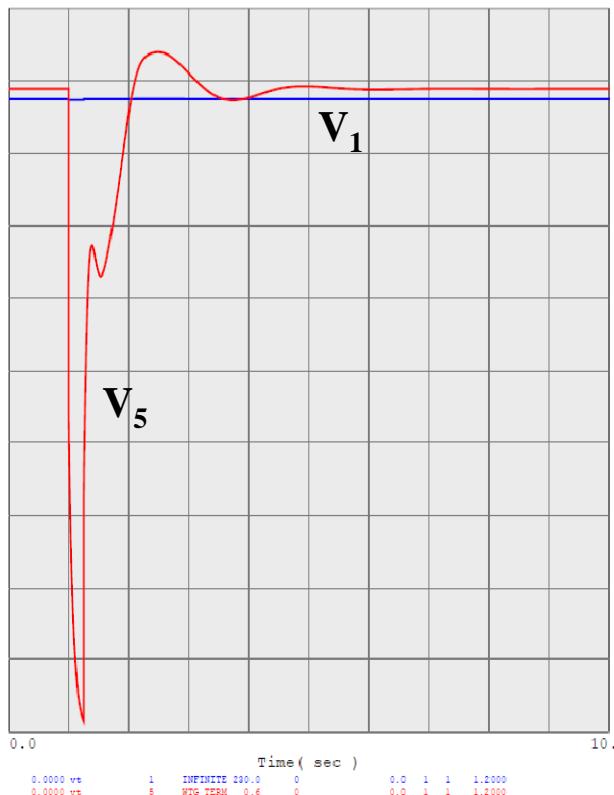
9-cycle, 3-phase fault at POI, clear fault by tripping line





WT1 Fault Test

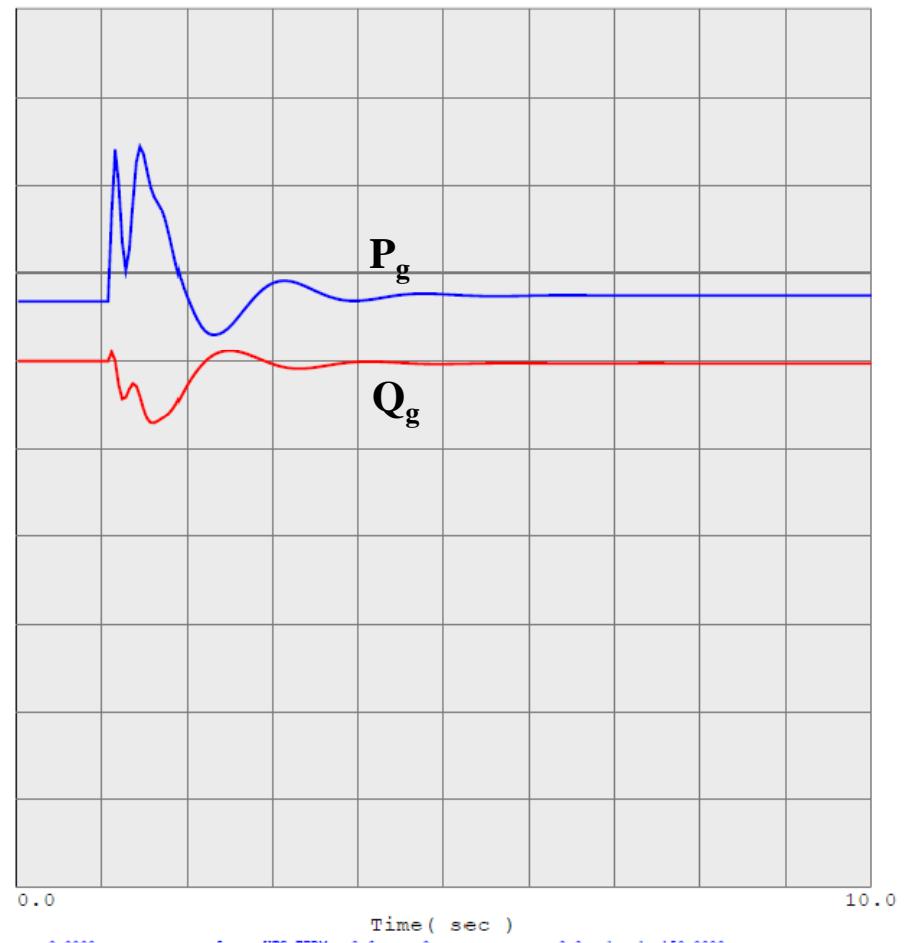
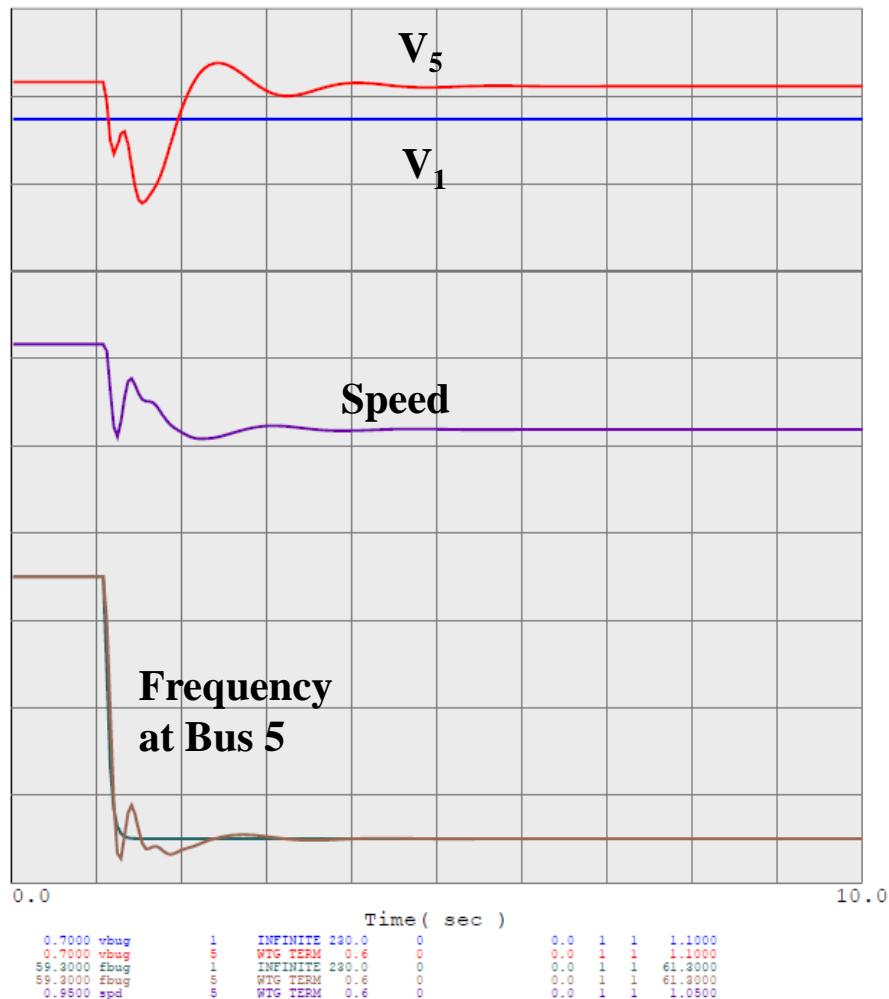
9-cycle, 3-phase fault at POI, Self-Clearing





WT1 Frequency Drop Test

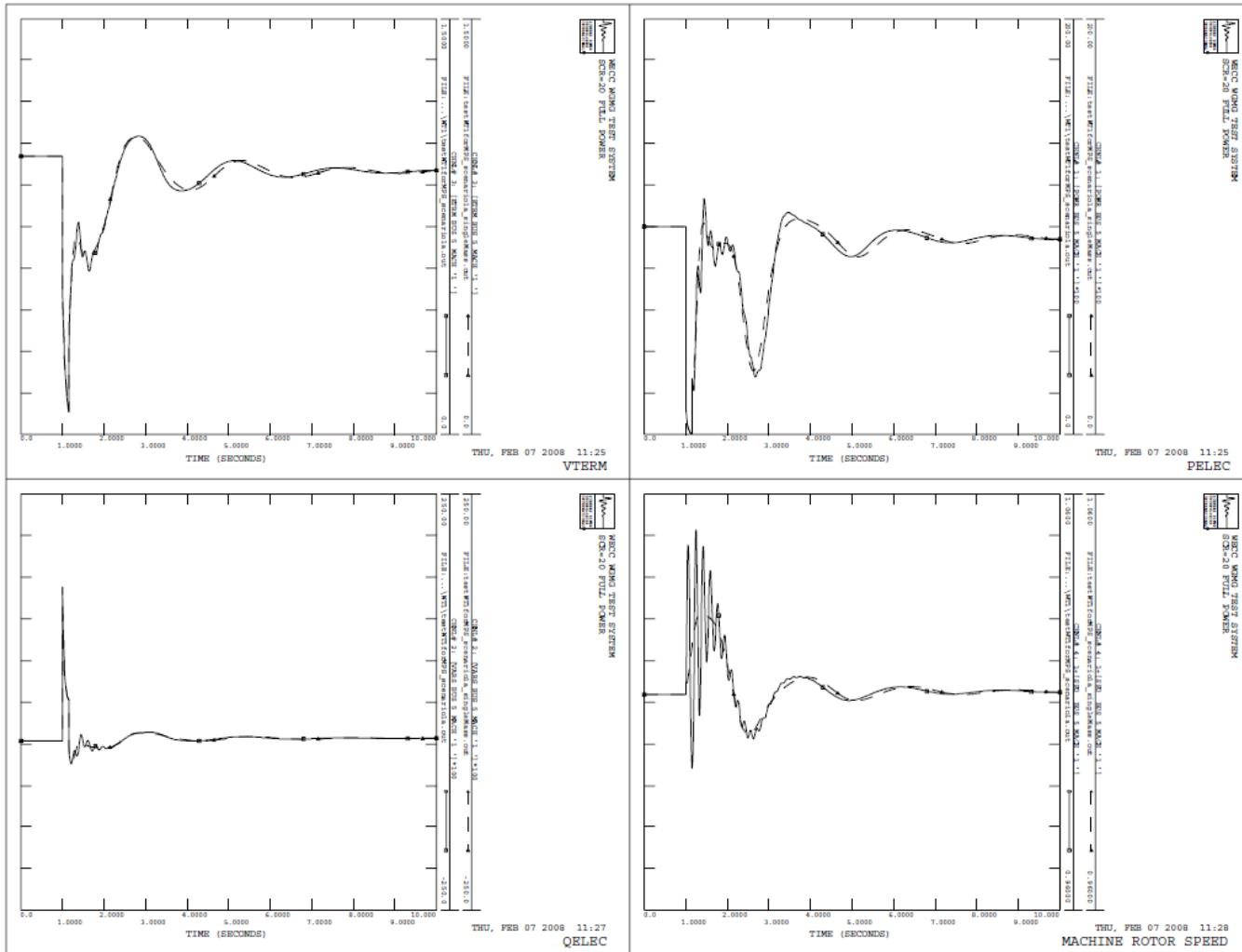
1% drop at t = 1 sec





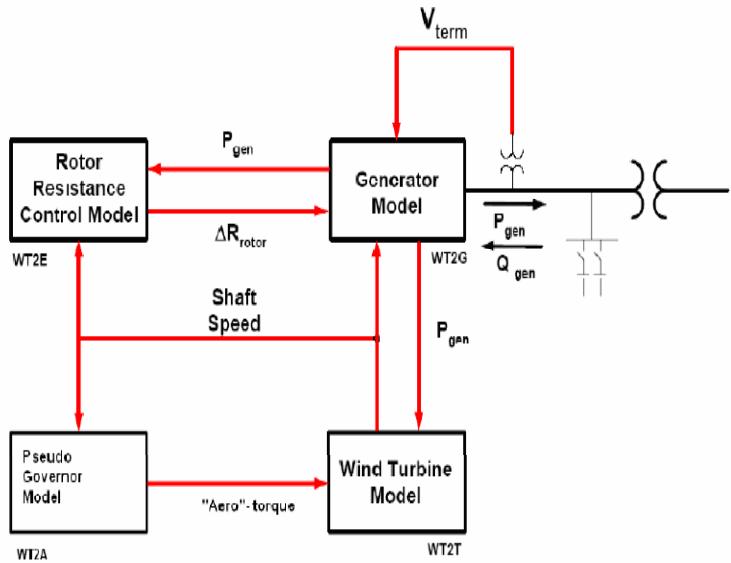
WT1 Model Comparison

Against Mitsubishi MWT1000A Manufacturer Model





WT2 Generic Model



Basic Description

Modules: WT2T, WT2E, WT2A/WT2P, WT2G

Generator model is conventional induction machine

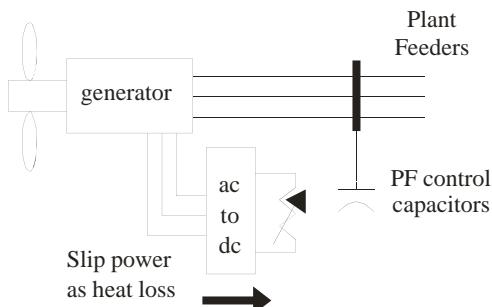
Default model data provided in documentation
(Vestas V80)

Single or two-mass shaft model

Power factor correction capacitor must be provided
and initialized from load flow data

No special initialization or run-time script needed

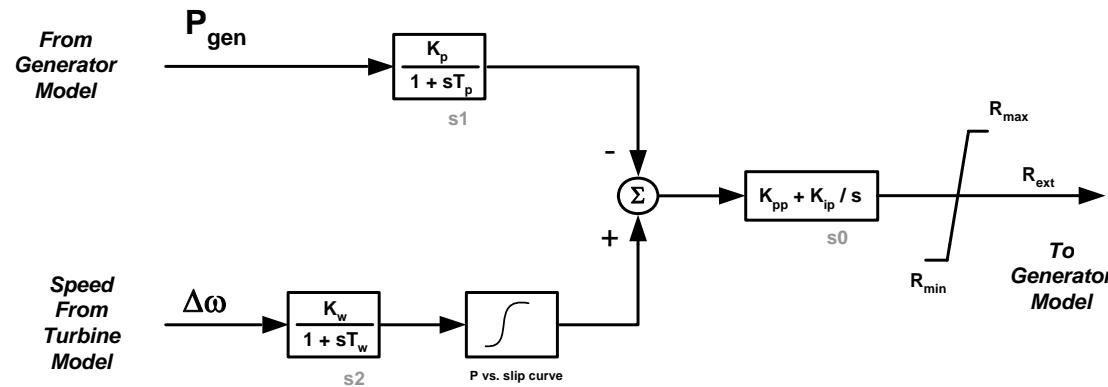
No special adjustment needed for wind farm representation



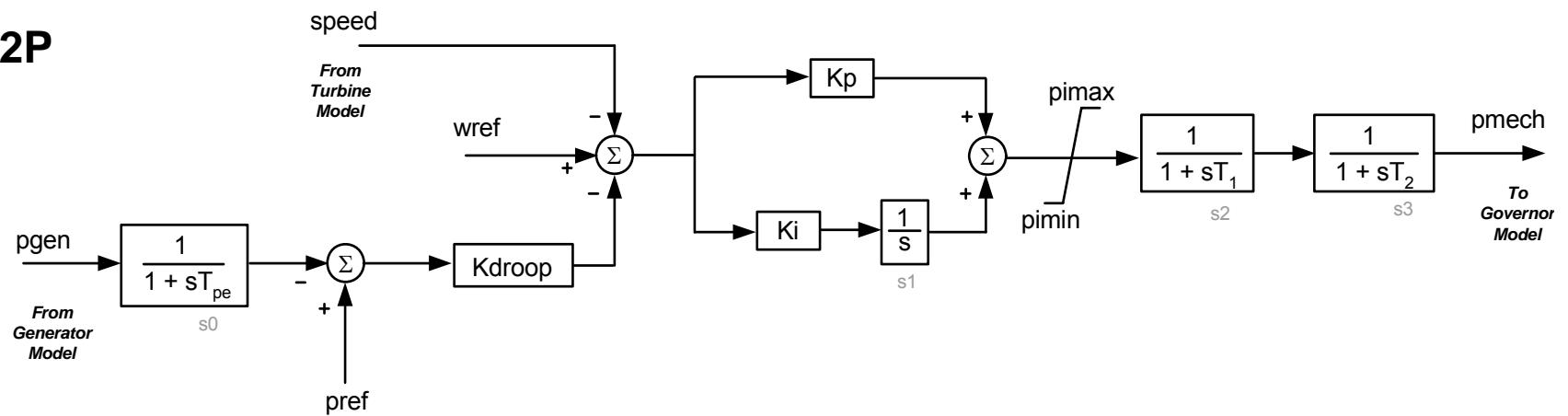


WT2 Generic Model

WT2E



WT2P





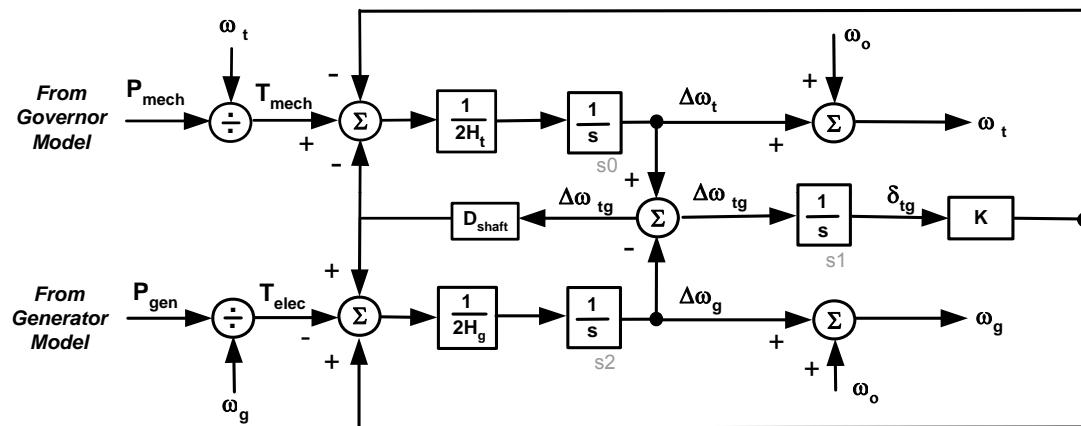
WT2 Generic Model

WT2T Two-mass model

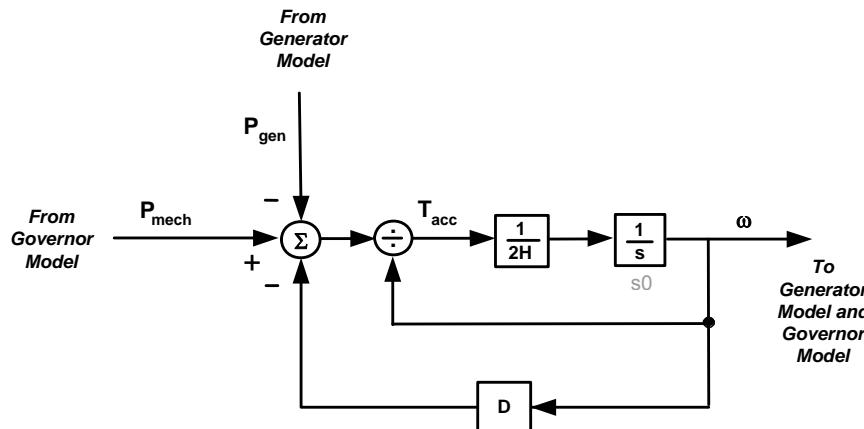
$$H_t = H_{tfrac} \cdot H$$

$$H_g = H - H_t$$

$$K = 2 (2\pi Freq1)^2 H_t \frac{H_g}{H}$$



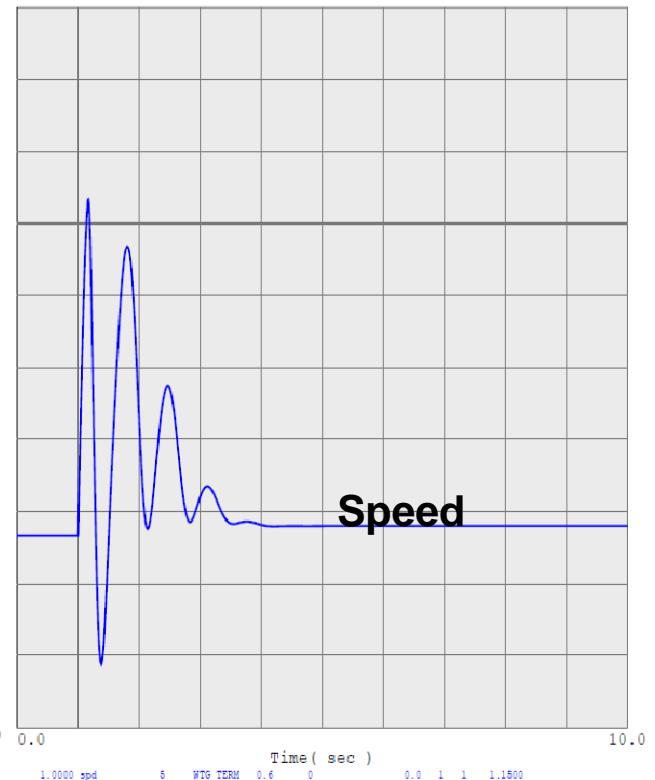
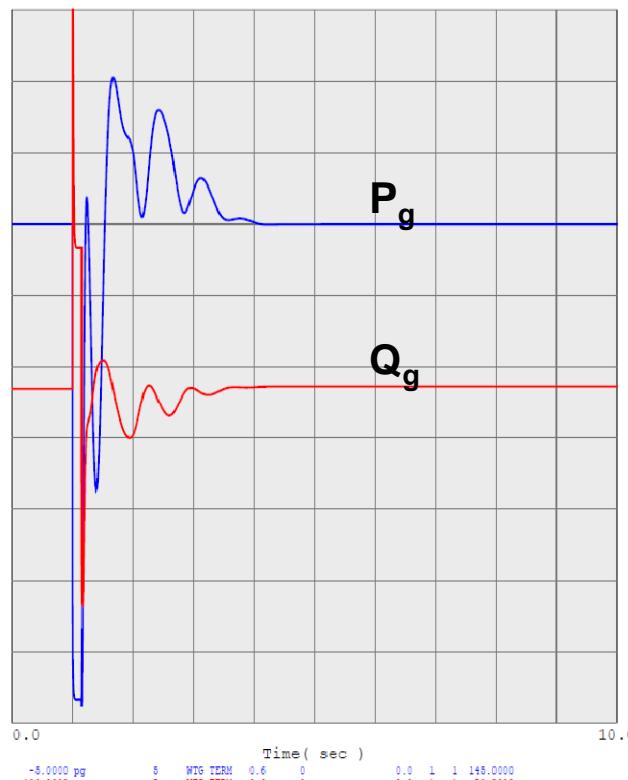
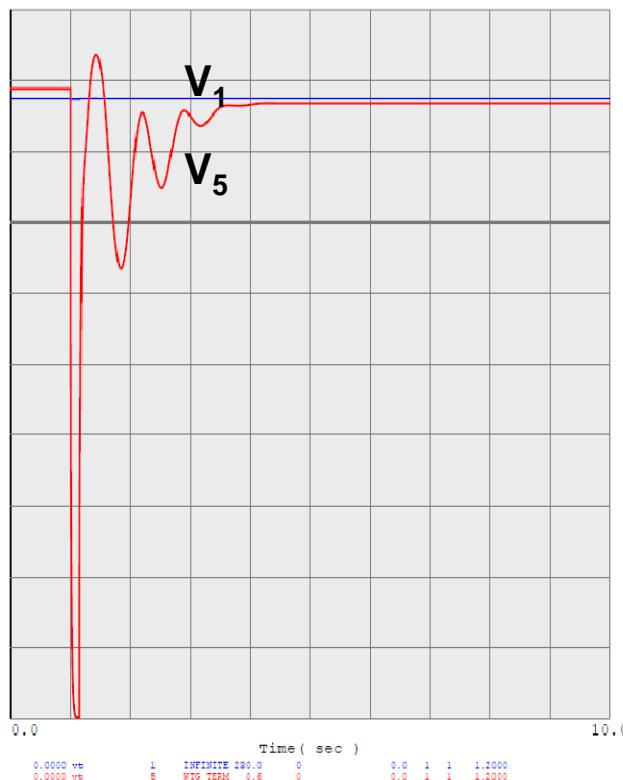
WT2T Single mass model ($H_{tfrac} = 0$)





WT2 Fault Test

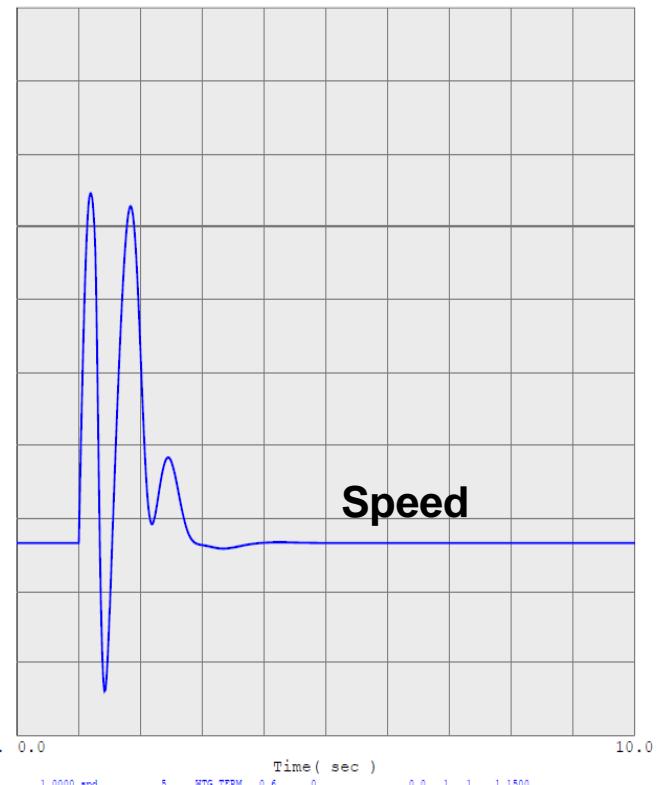
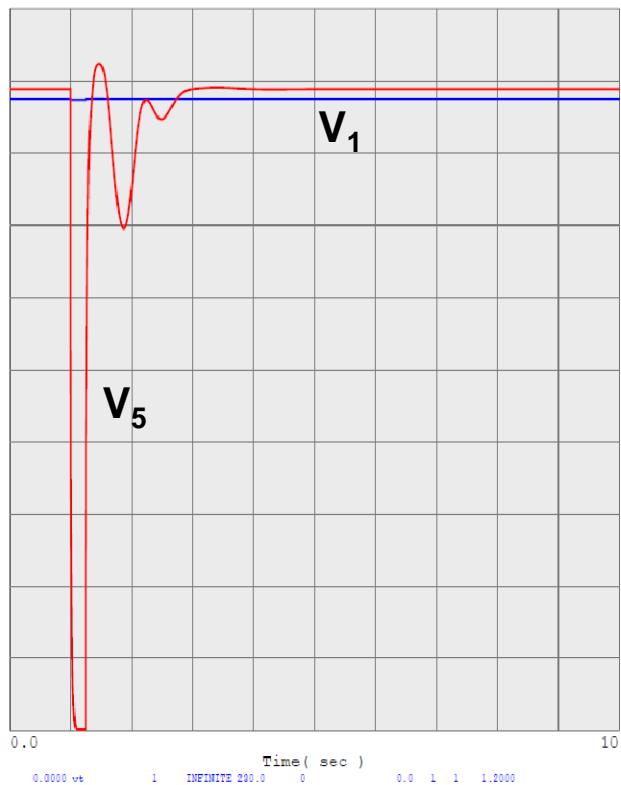
9-cycle, 3-phase fault at POI, clear fault by tripping line





WT2 Fault Test

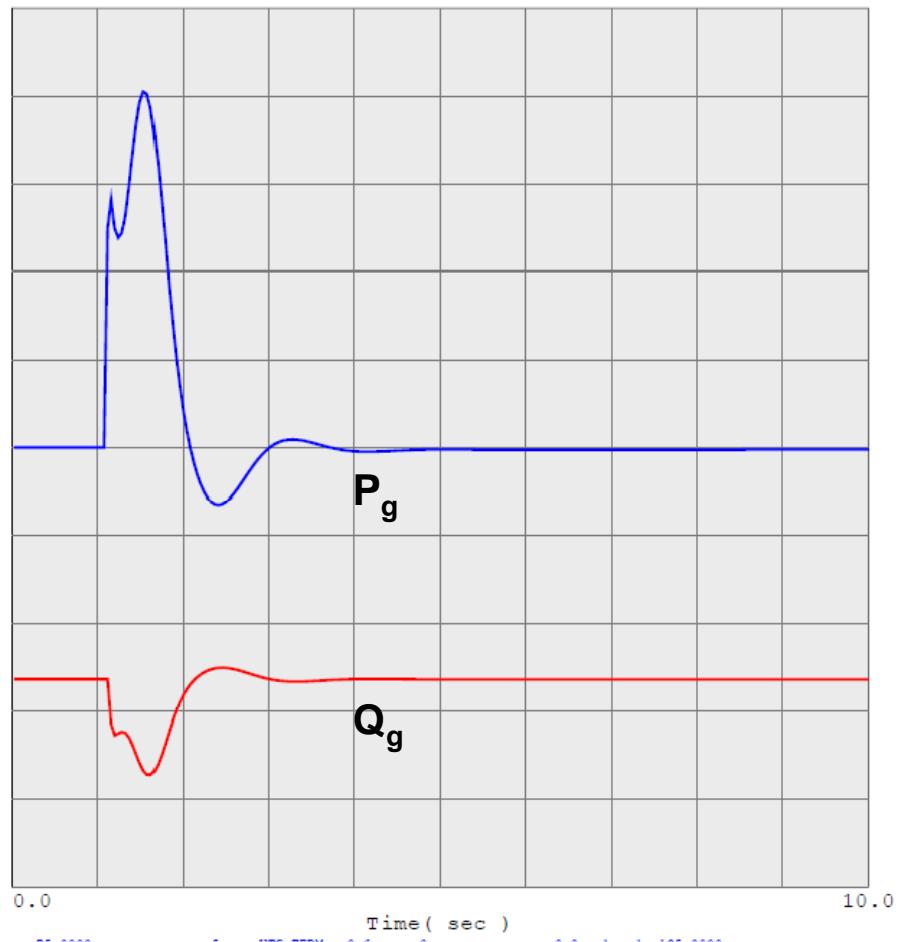
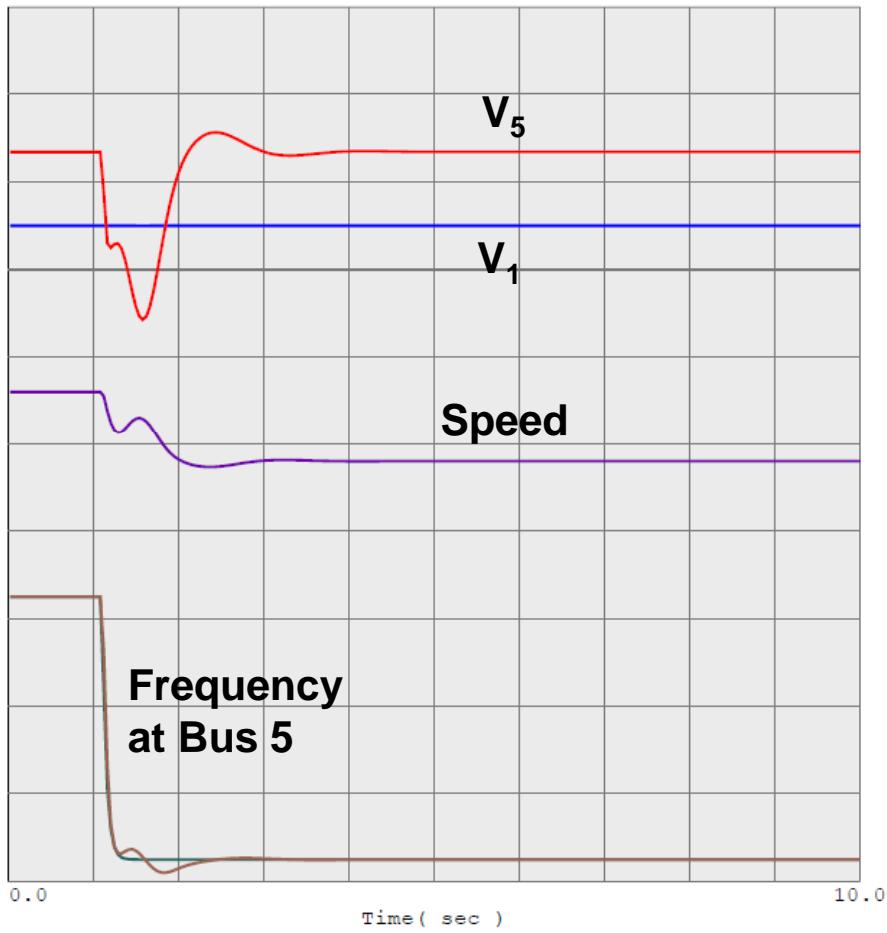
9-cycle, 3-phase fault at POI, self-clearing





WT2 Frequency Drop Test

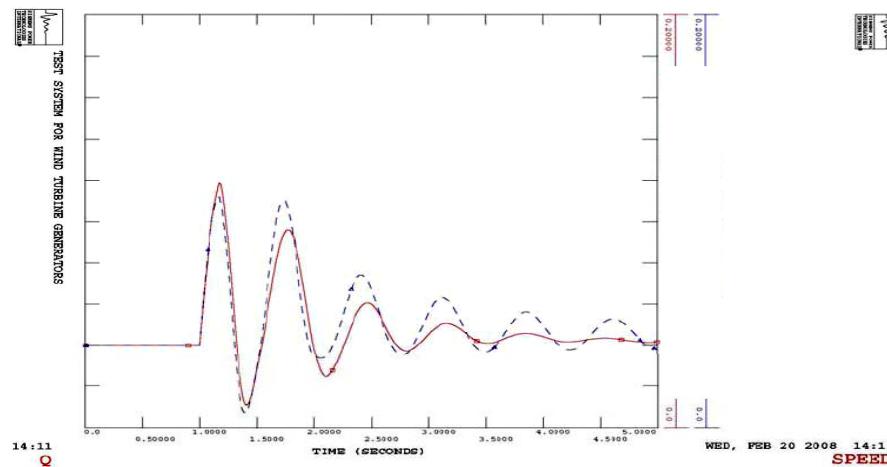
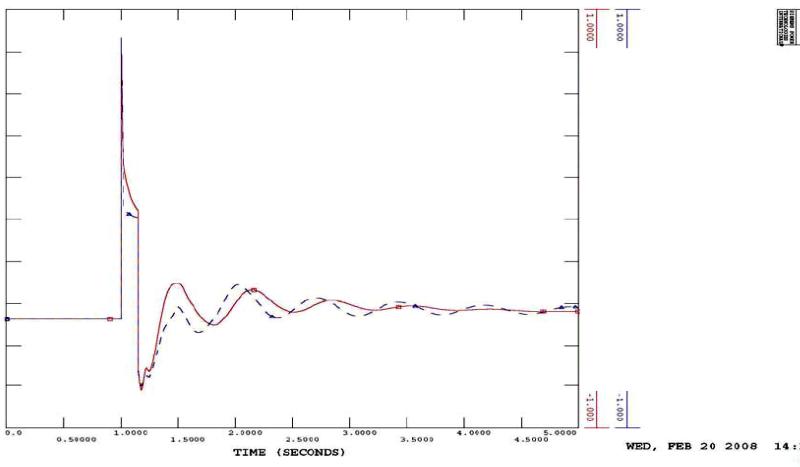
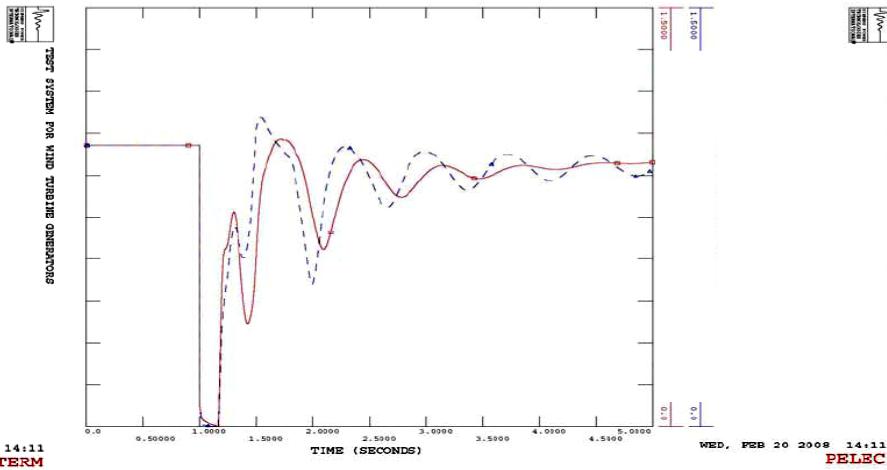
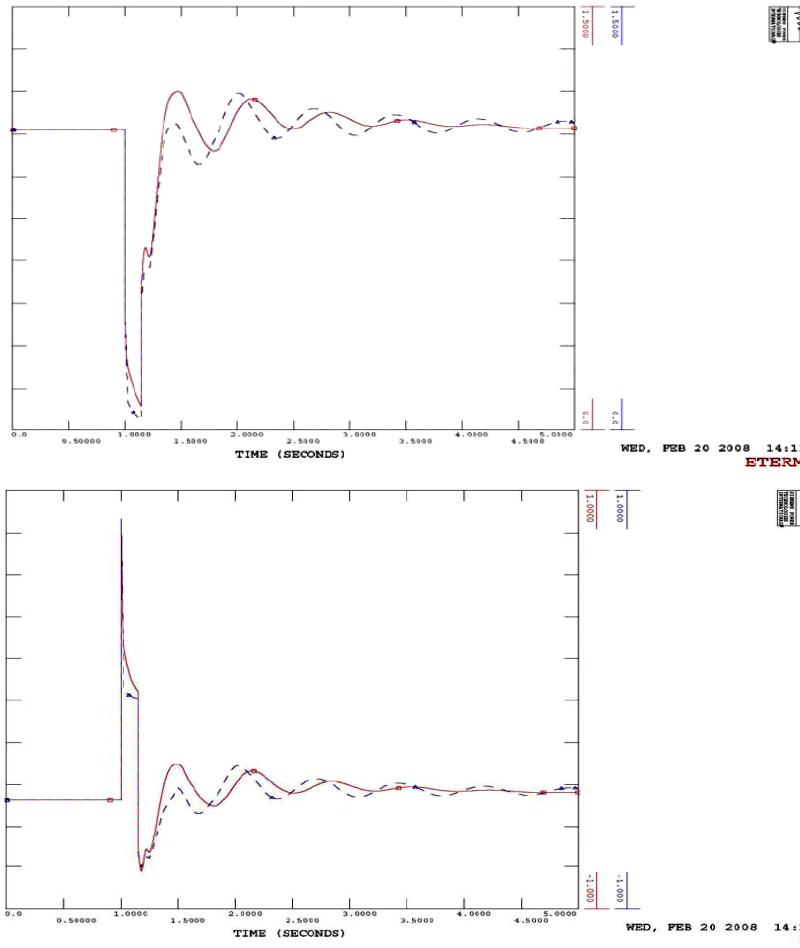
1% drop at t = 1 sec





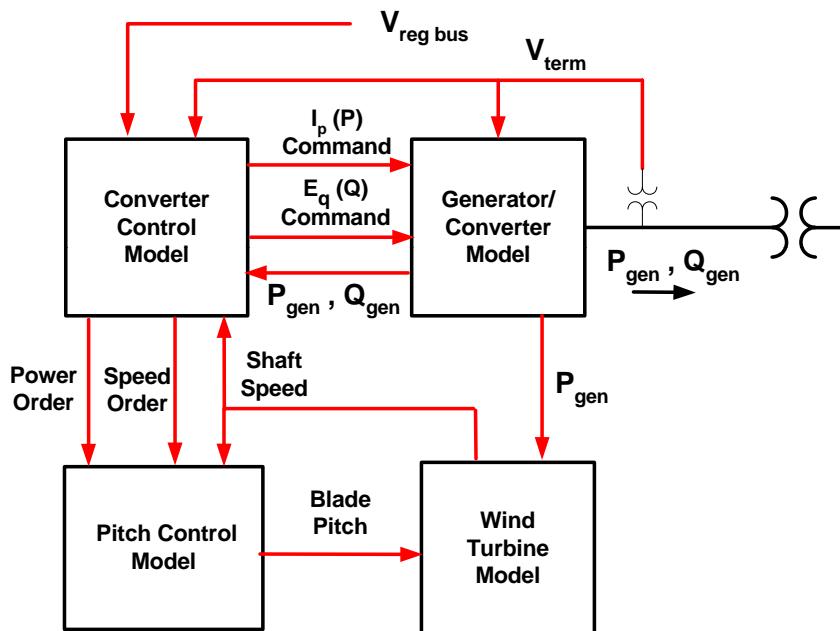
WT2 Model Comparison

Against Vestas V80 Manufacturer Model





WT3 Generic Model



Basic Description

Modules: WT3T, WT3E, WT3P, WT3G

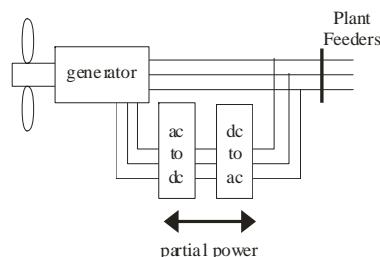
Generator is modeled as controlled current injection

Default model data provided in documentation (GE 1.5)

Single or two-mass shaft model

No special initialization or run-time script needed

Plant level reactive control options available for wind farm model (PF control, Q control and voltage control)





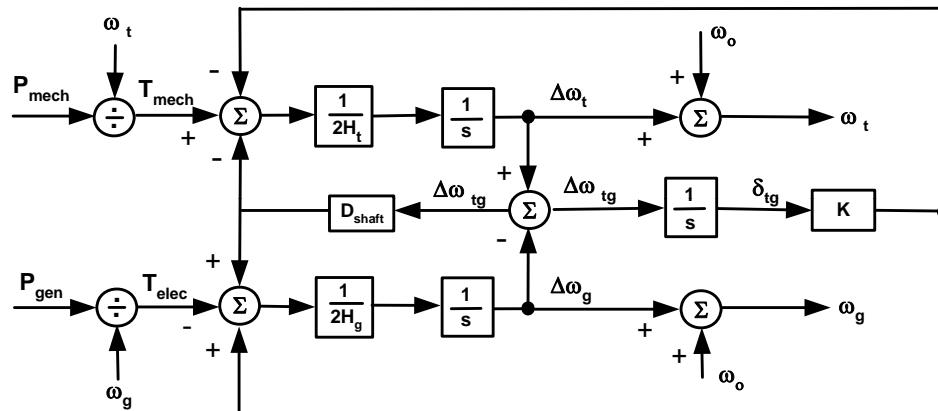
WT3 Generic Model

WT3T Two-mass model

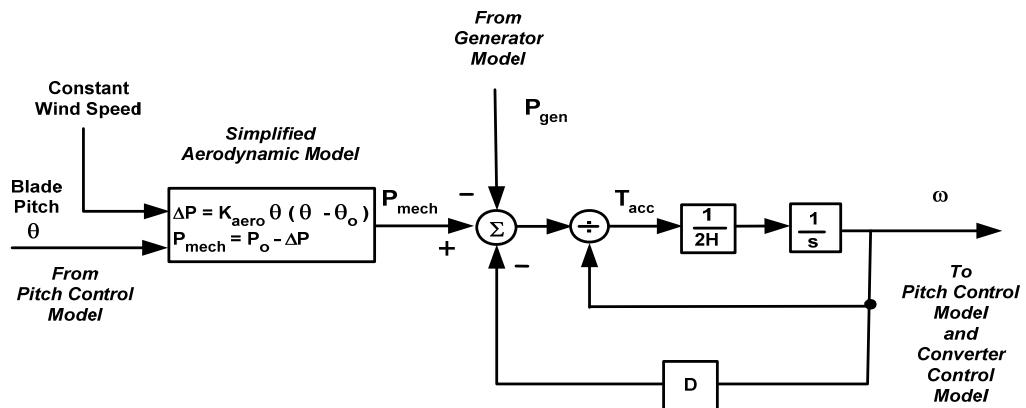
$$H_t = H_{tfrac} \cdot H$$

$$H_g = H - H_t$$

$$K = 2 (2\pi \text{ Freq1})^2 H_t \frac{H_g}{H}$$



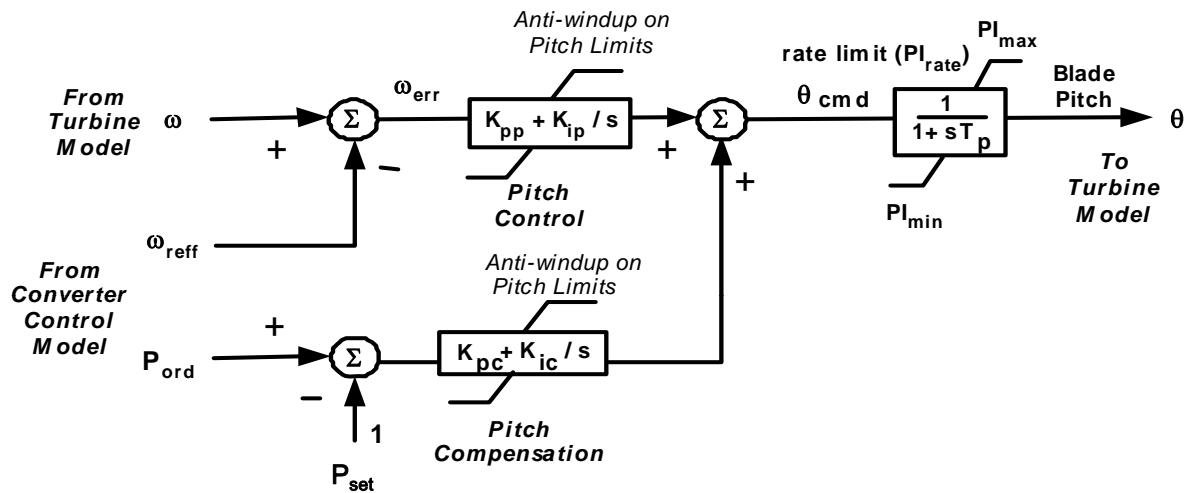
WT3T Single mass model ($H_{tfrac} = 0$)





WT3 Generic Model

WT3P Pitch Control Model

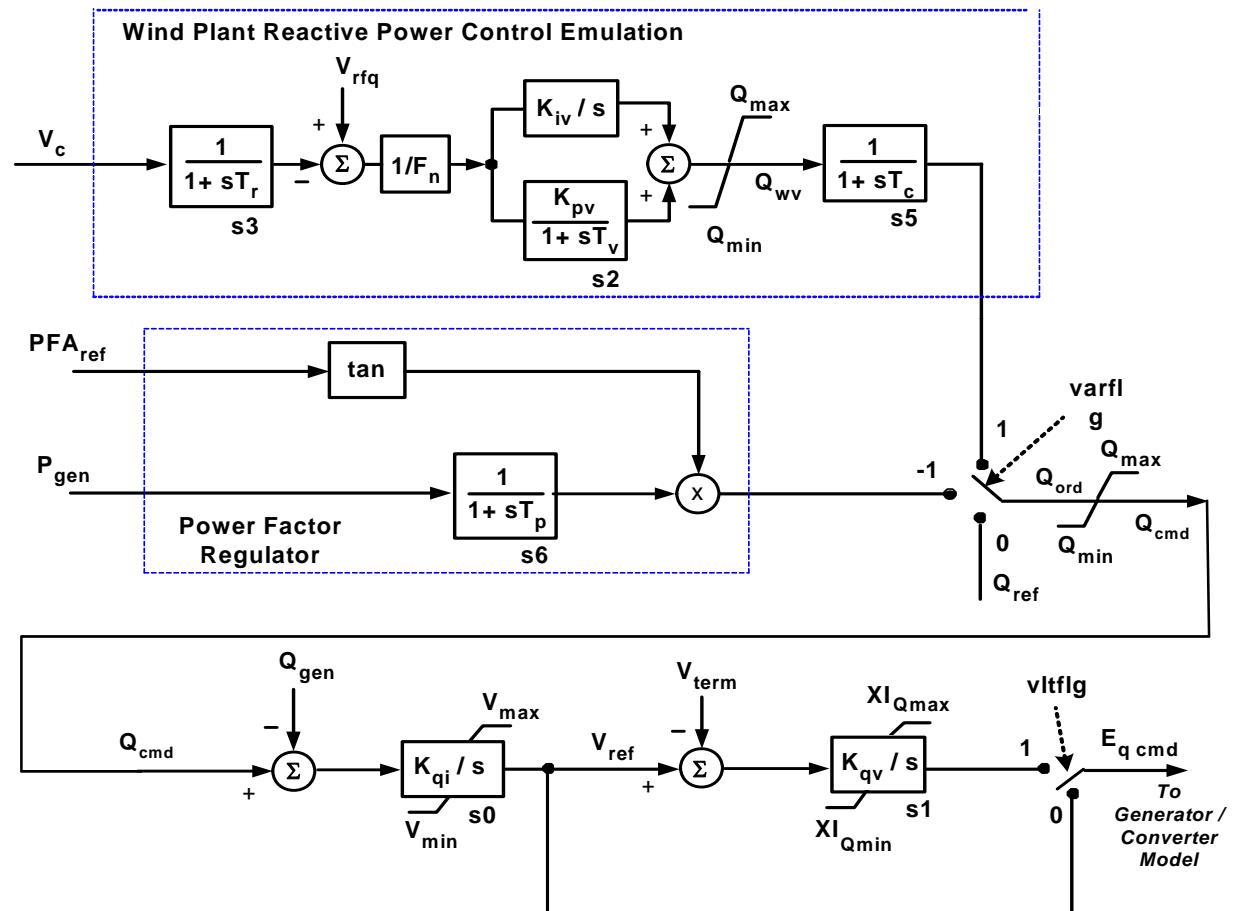


NOTE: P_{set} should normally be 1.0 unless it is controlled by a separate active power control model, e.g. to provide governing response. It must always be greater than or equal to the initial power output of the WTG.



WT3 Generic Model

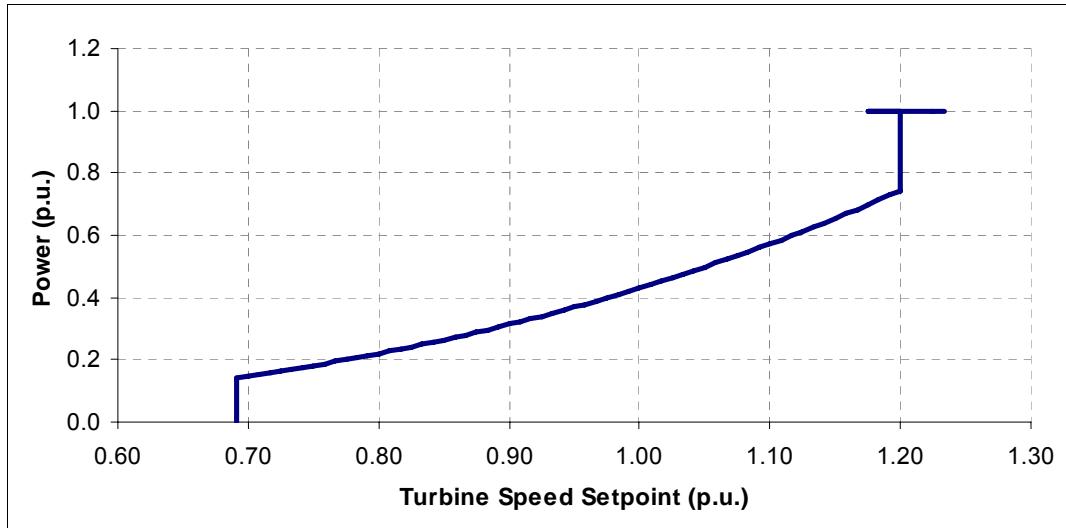
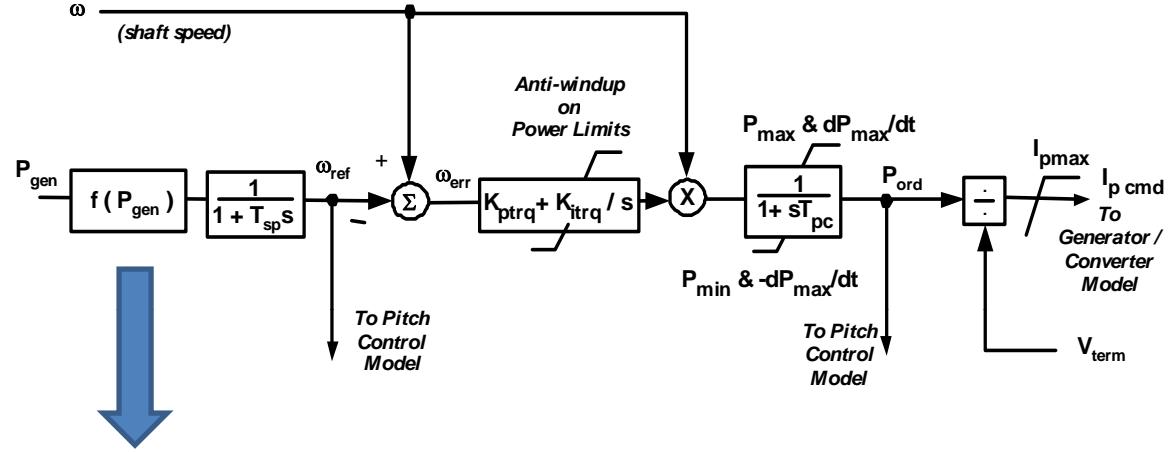
WT3E Reactive Power Control Model





WT3 Generic Model

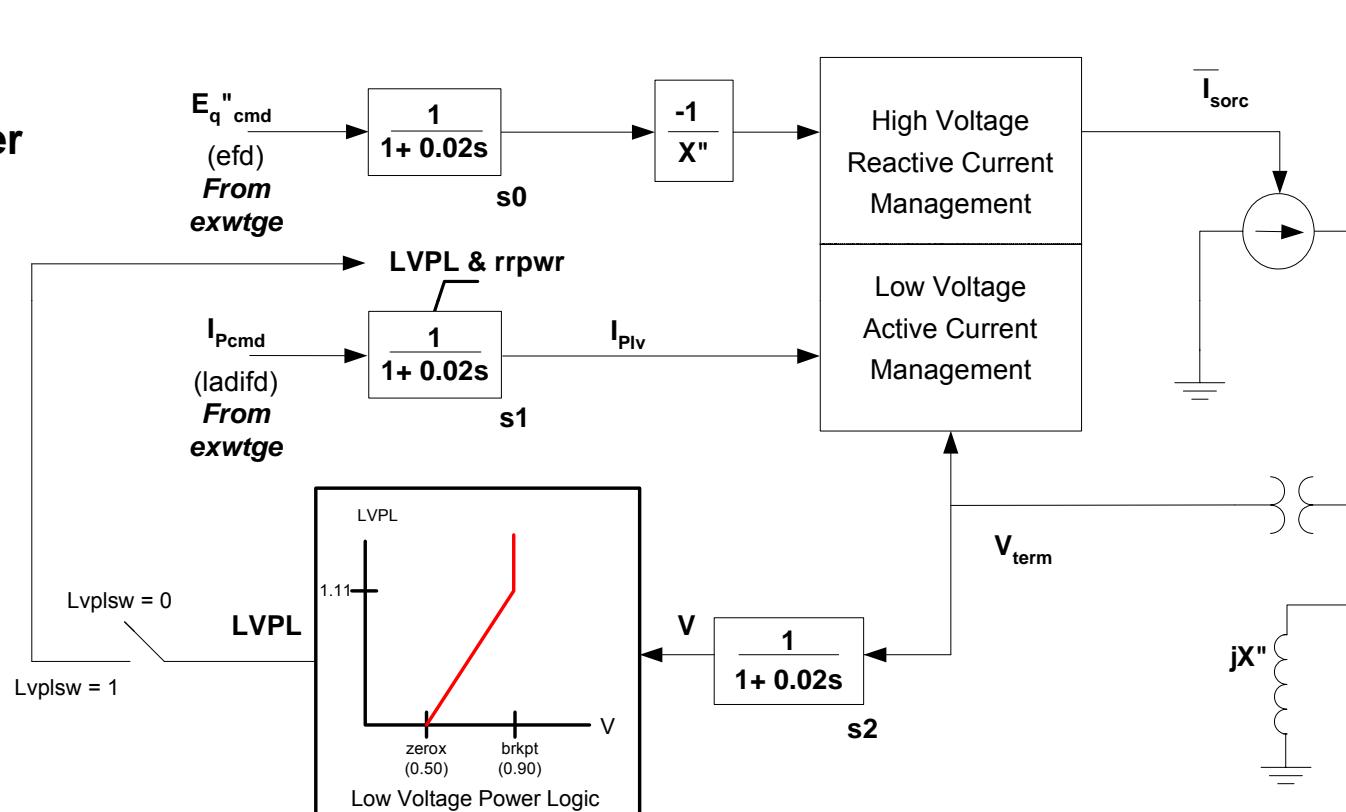
WT3E
Active Power (Torque)
Control Model





WT3 Generic Model

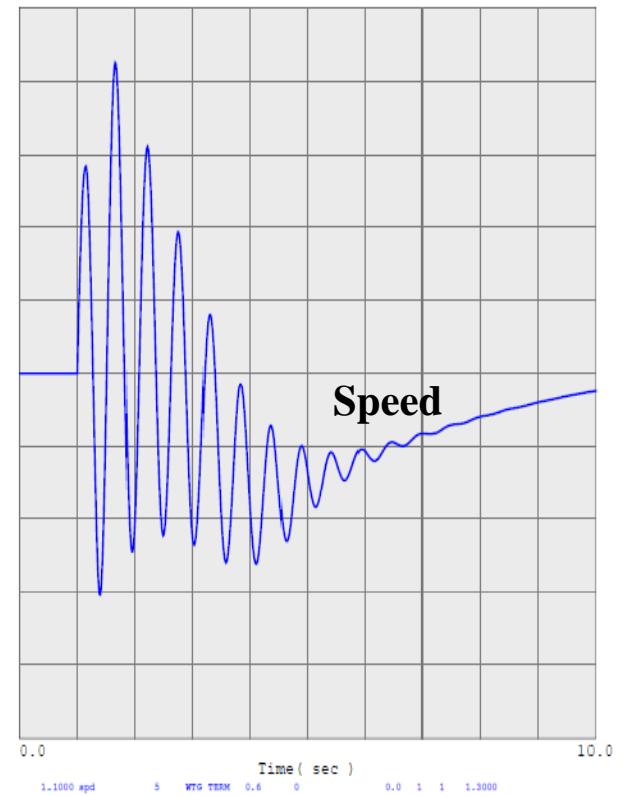
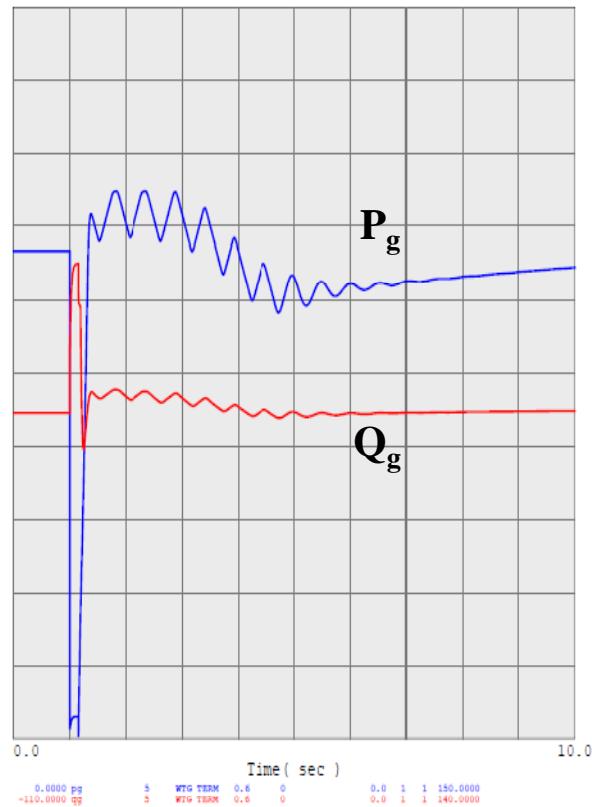
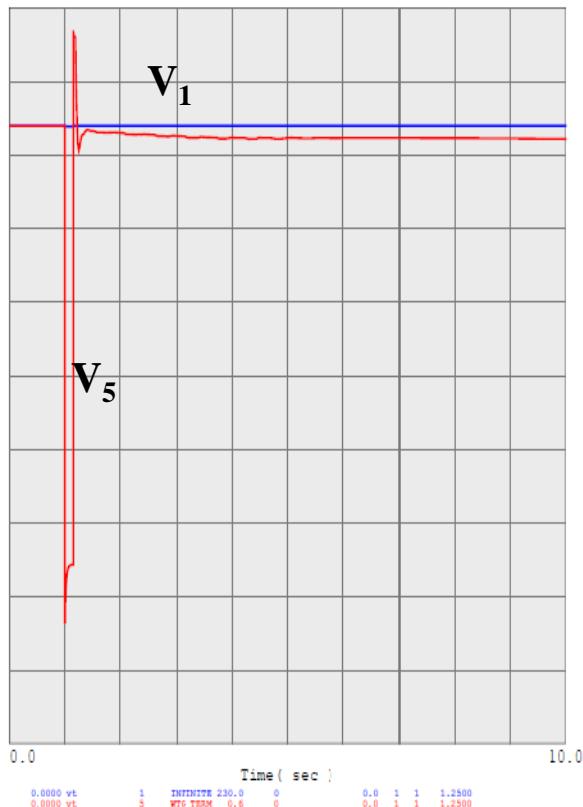
WT3G Generator / Converter Model





WT3 Fault Test

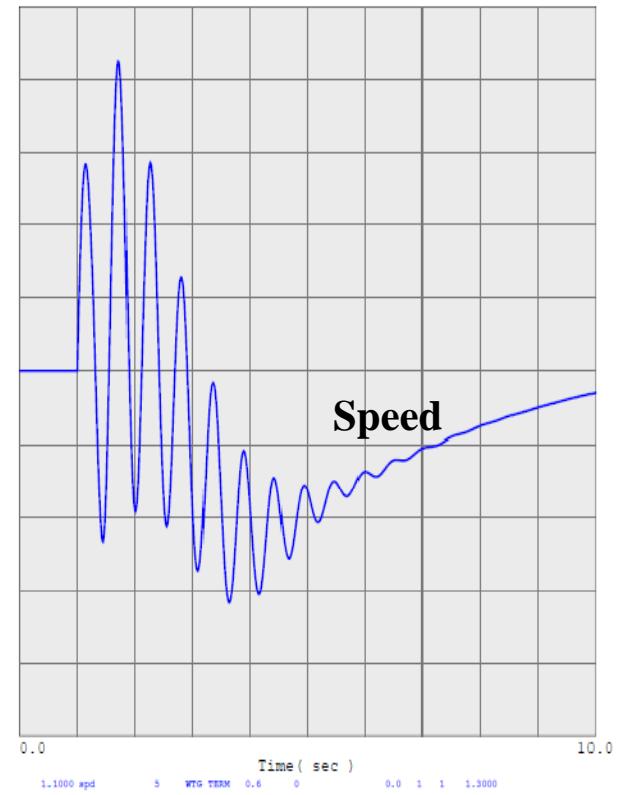
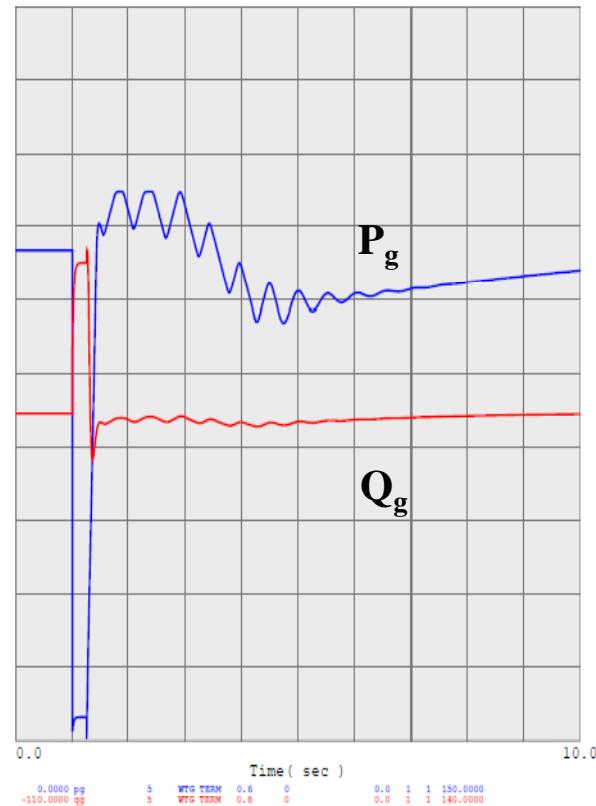
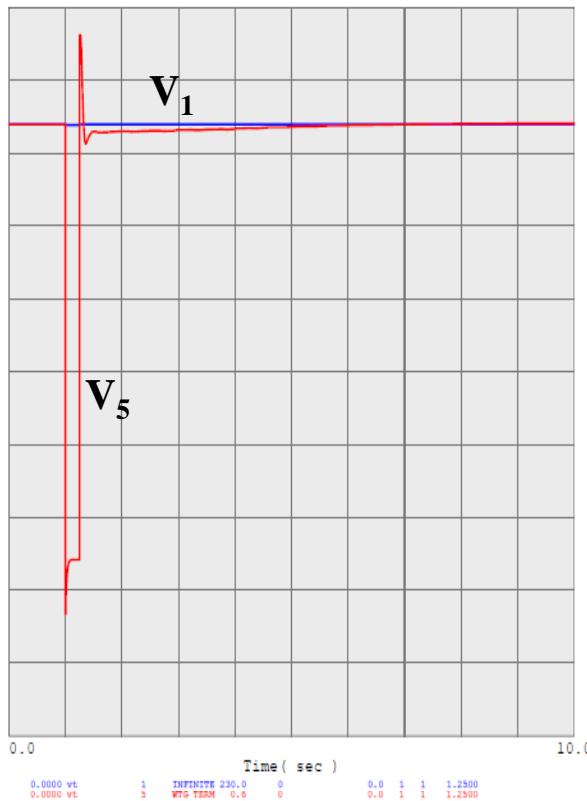
9-cycle, 3-phase fault at POI, clear fault by tripping line





WT3 Fault Test

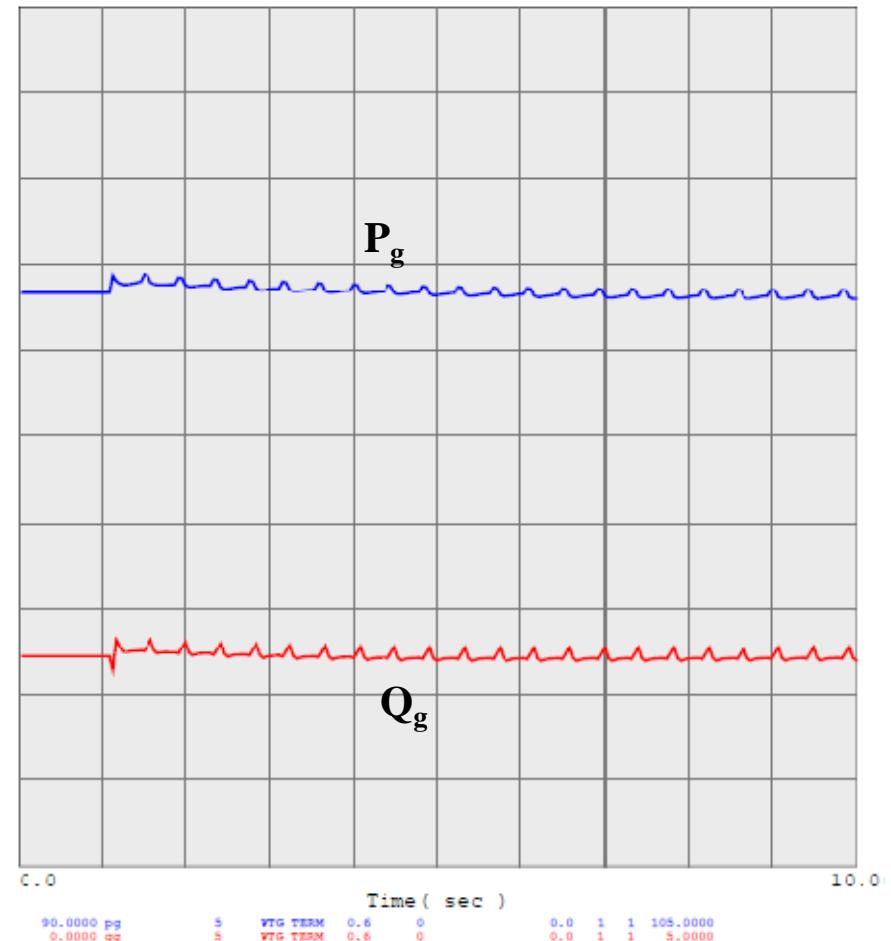
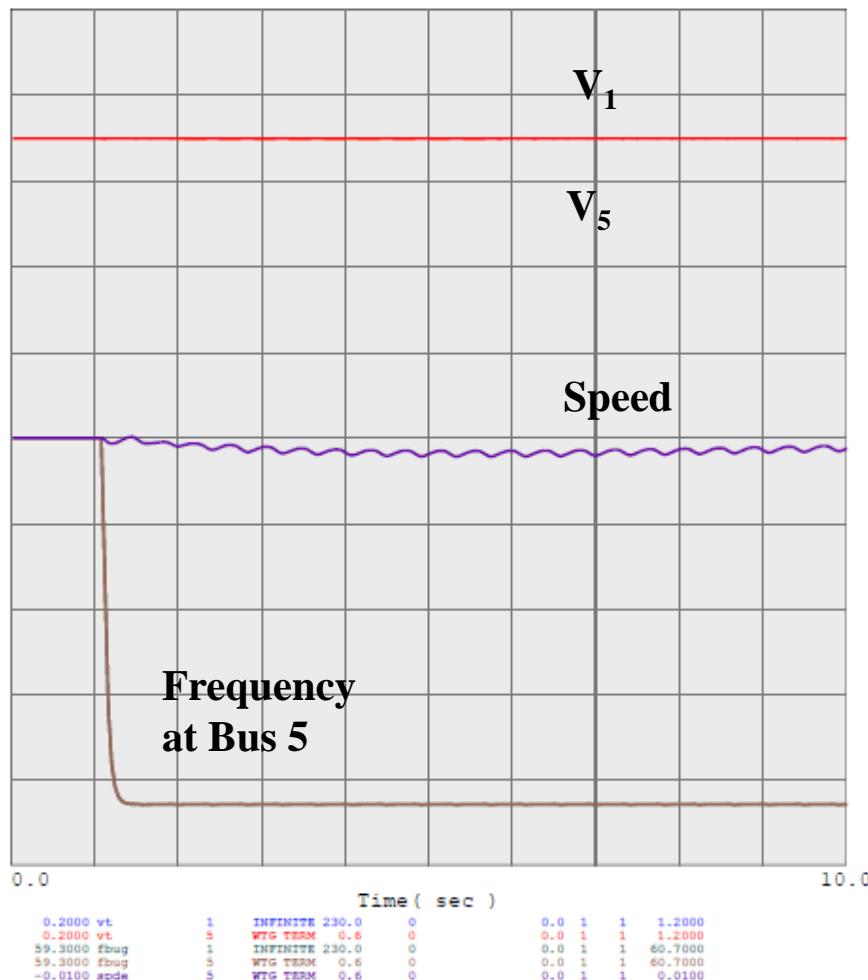
9-cycle, 3-phase fault at POI, self clearing





WT3 Frequency Drop Test

1% drop at t = 1 sec

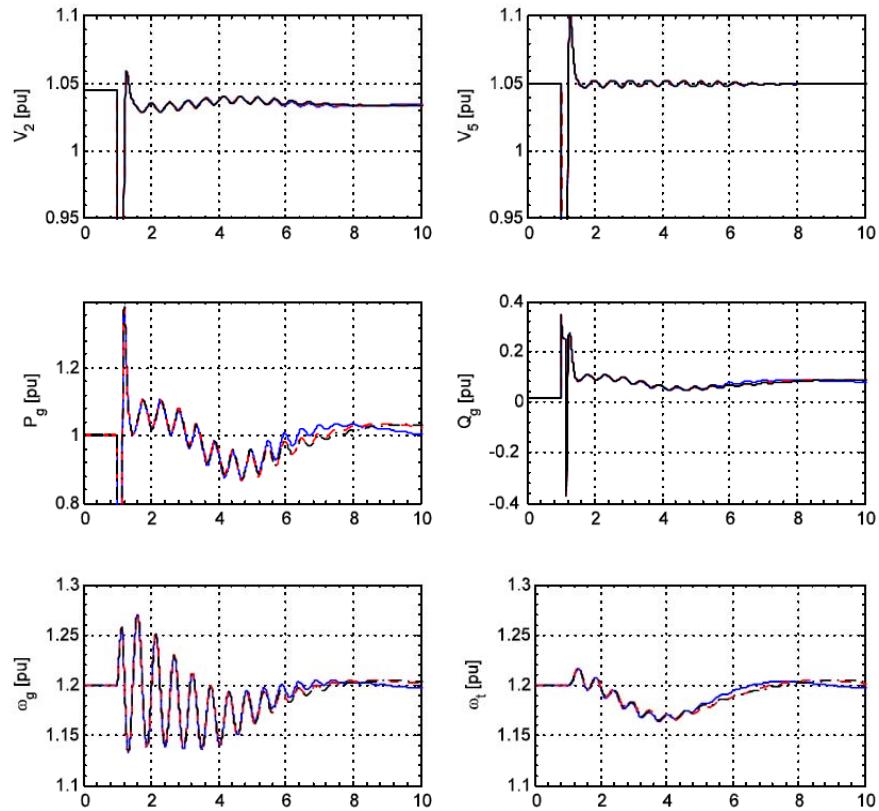




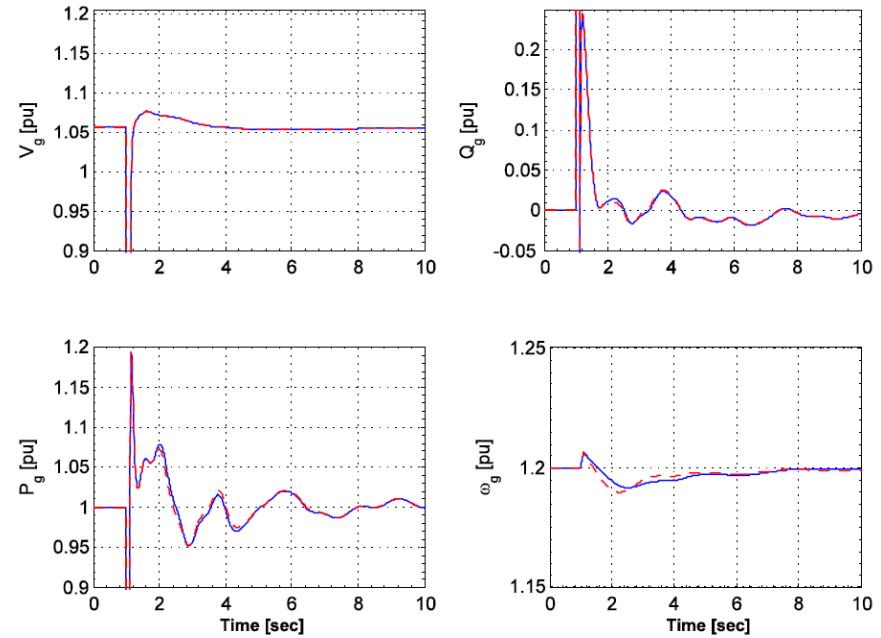
WT3 Model Comparison

Against GE1.5 Manufacturer Model

Small System



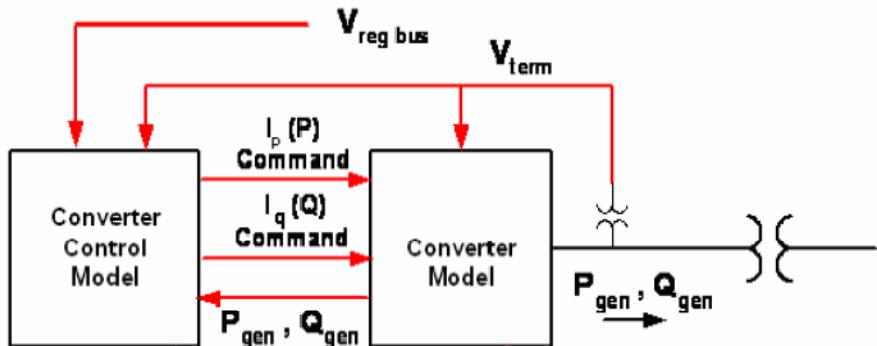
Large System





WT4 Generic Model

Basic Description



Modules: WT4T, WT4E, WT4G

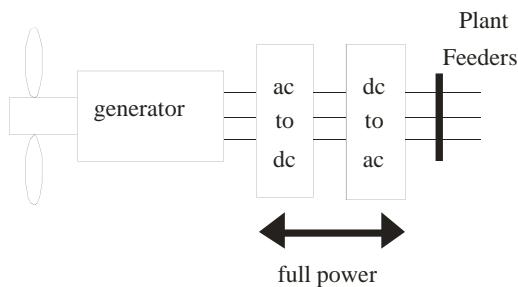
No generator model. Just converter represented as controlled current injection

Default model data provided in documentation (GE 2.x)

Machine dynamics not modeled (it decoupled from the grid by the converter)

No special initialization or run-time script needed

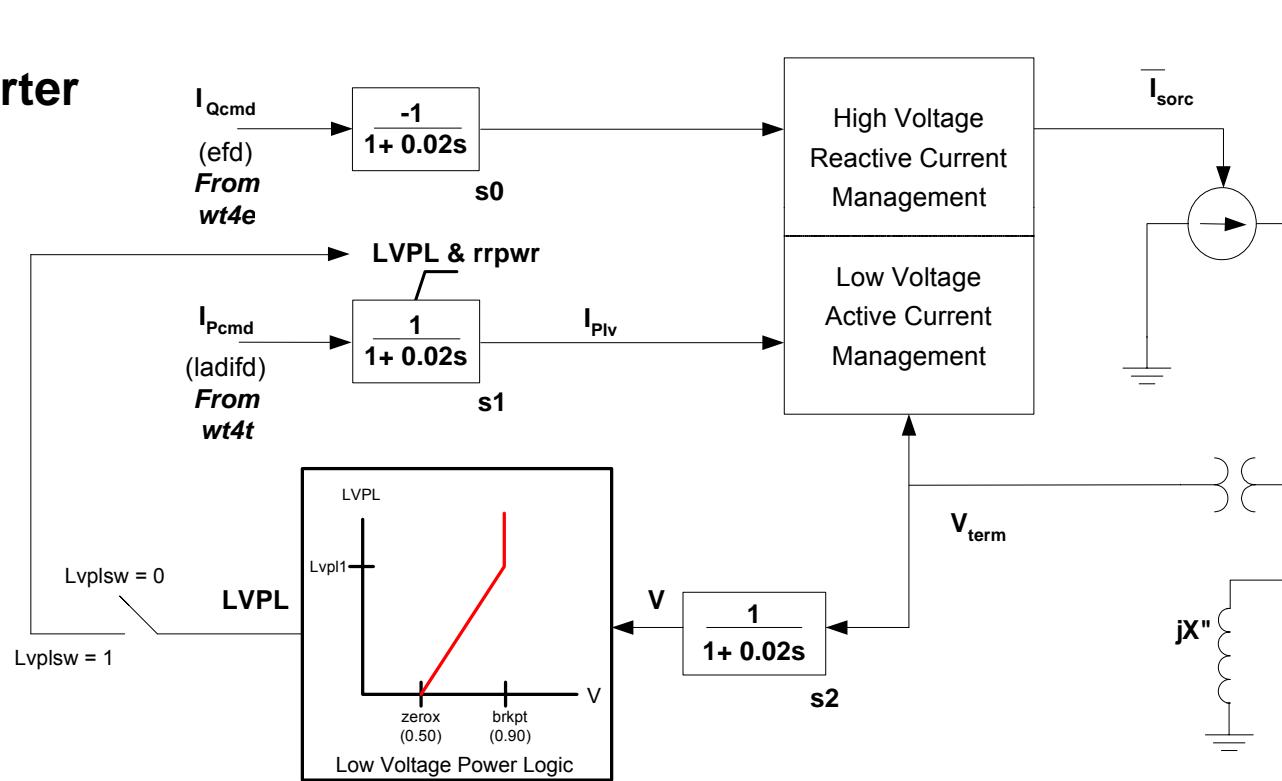
Plant level reactive control options available for wind farm model (PF control, Q control and voltage control)





WT4 Generic Model

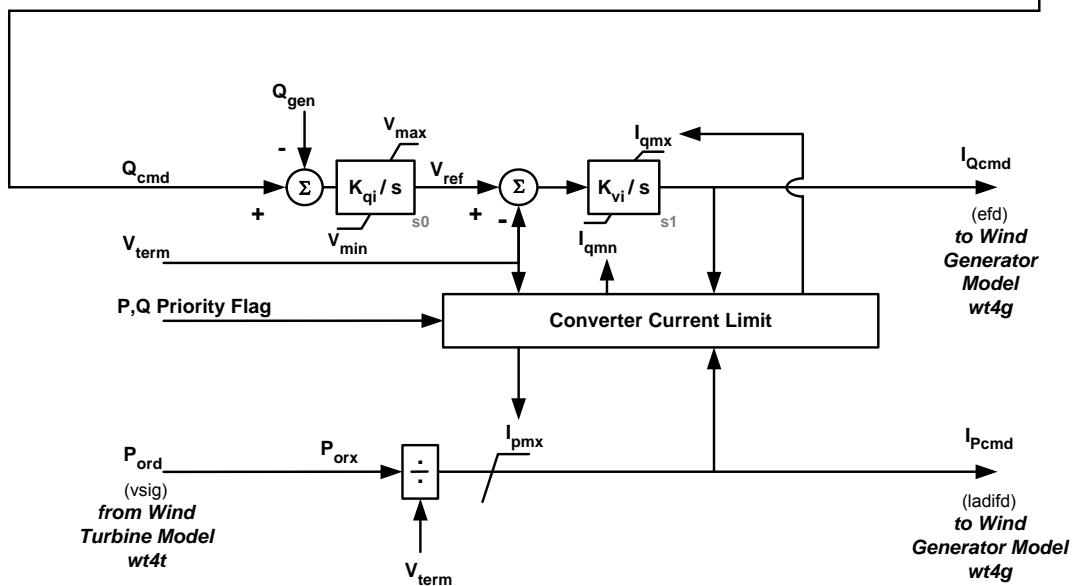
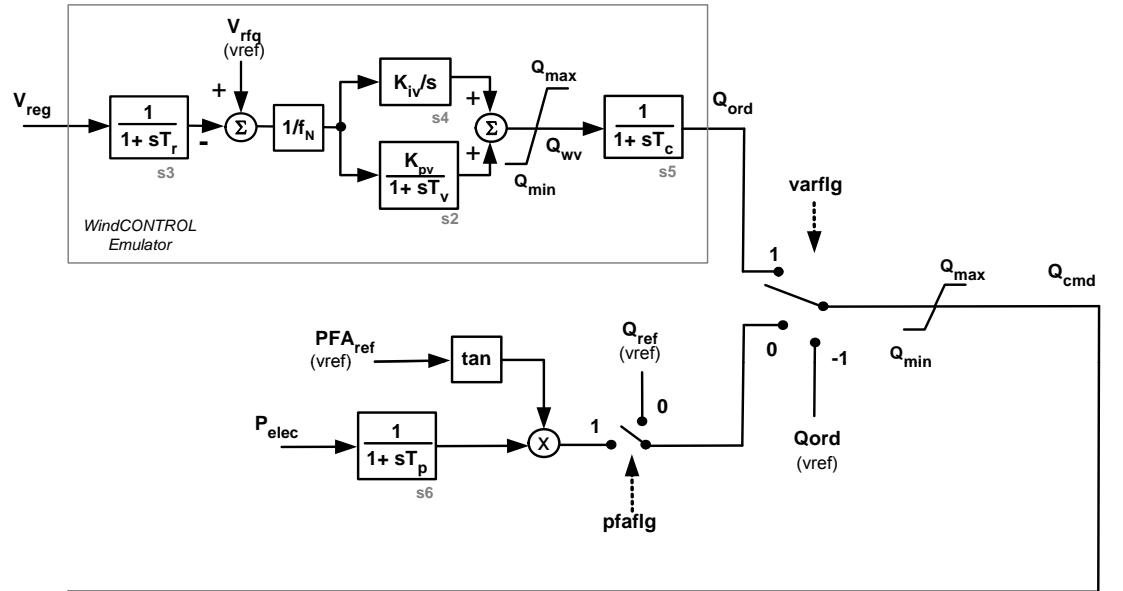
WT4G Generator/Converter Model





WT4 Generic Model

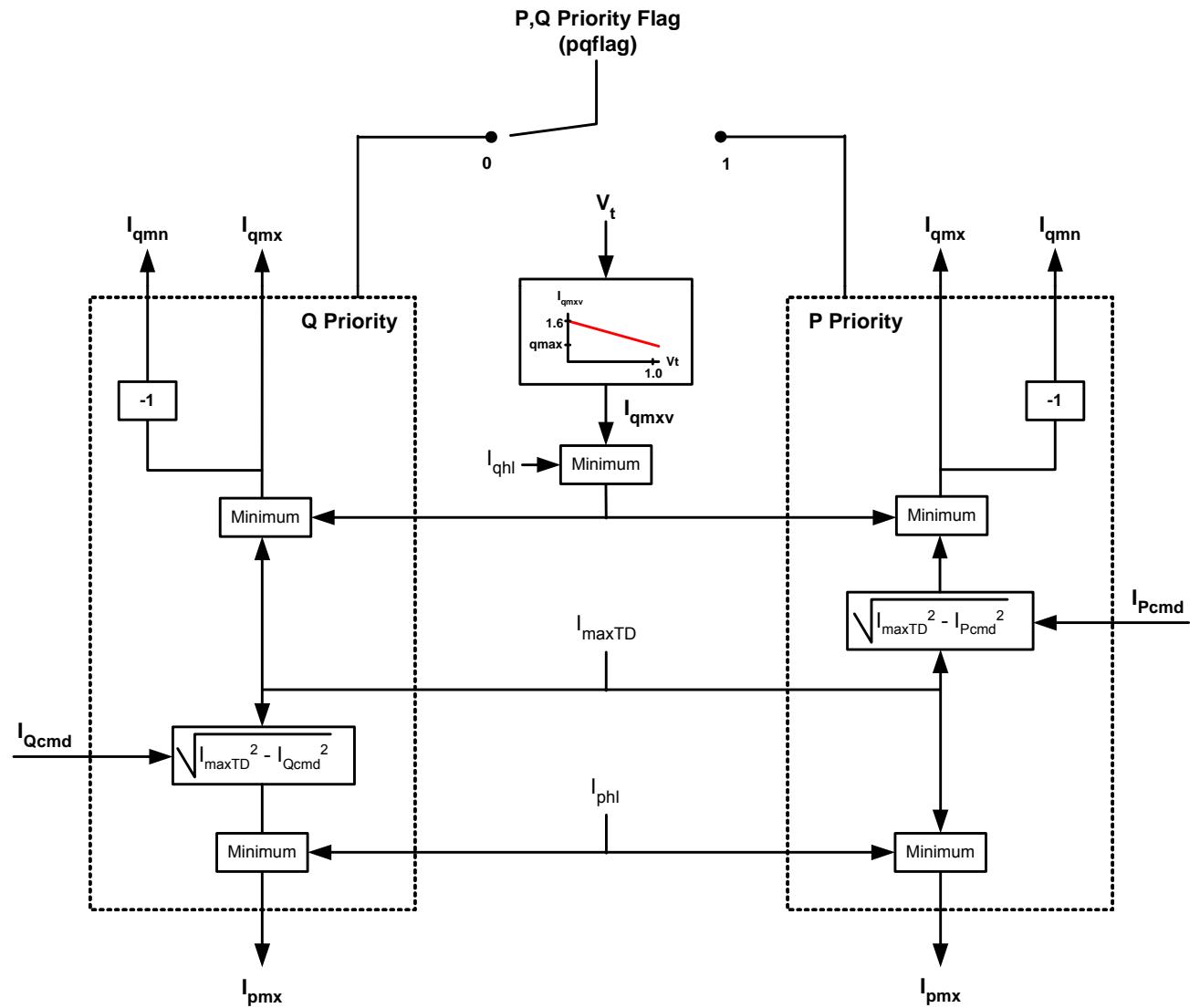
WT4E Converter Electrical Control Model





WT4 Generic Model

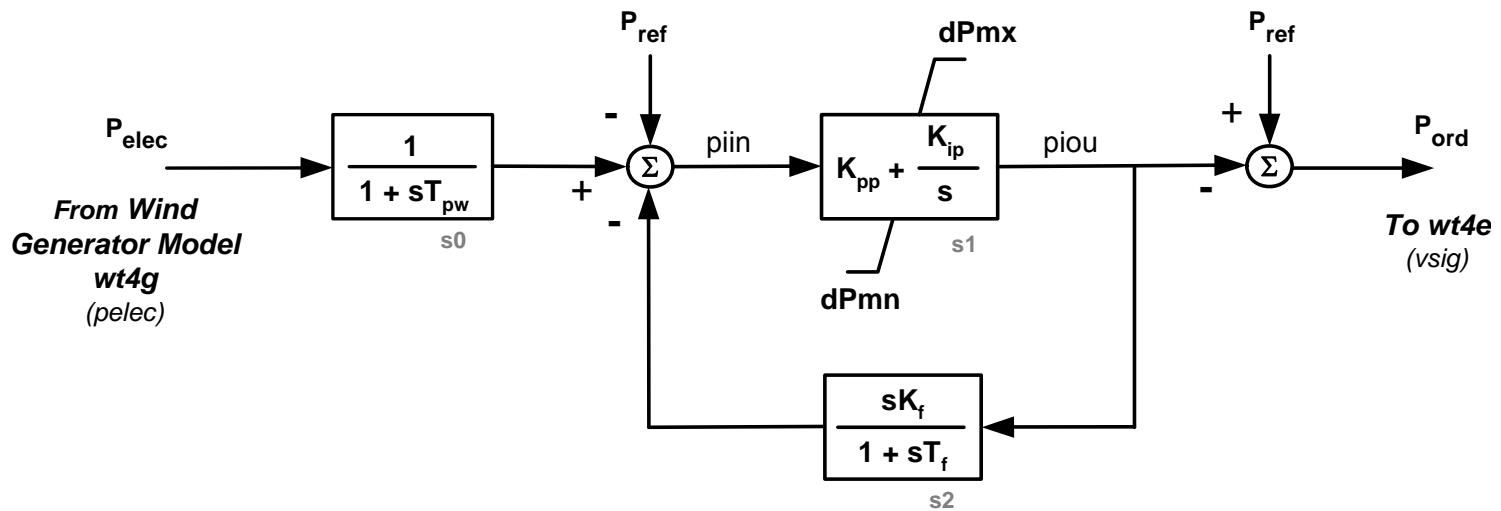
WT4E Converter Current Limiter Model





WT4 Generic Model

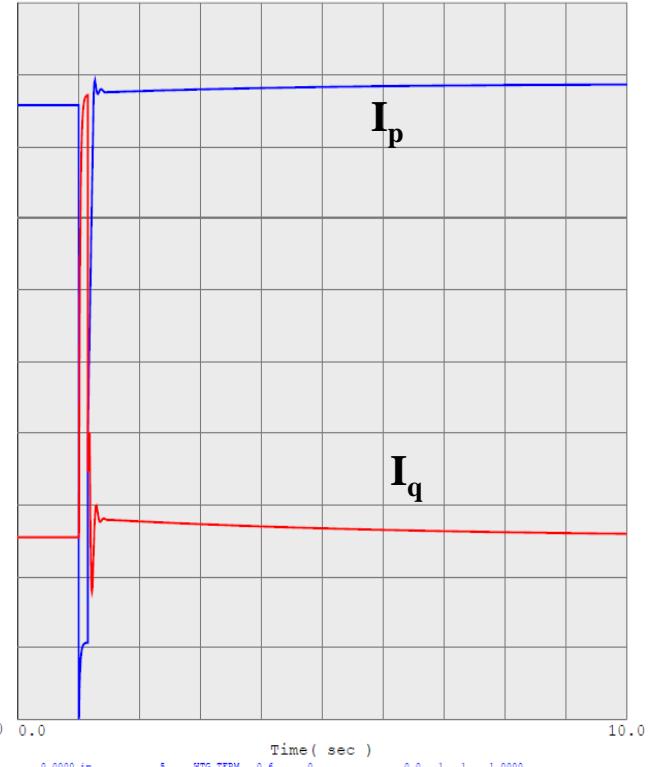
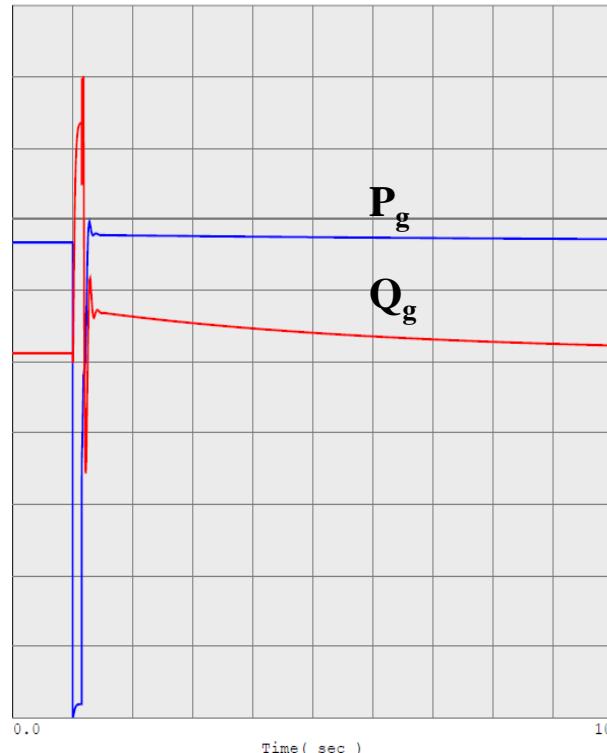
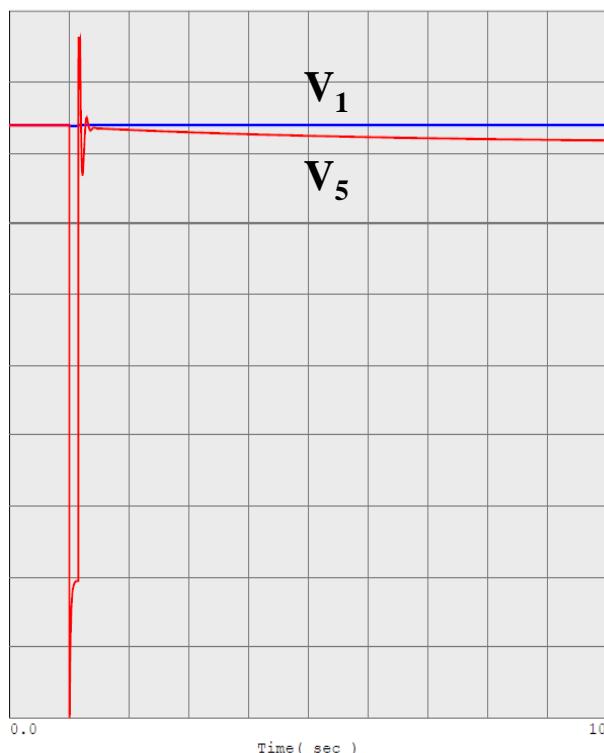
WT4T Turbine Model





WT4 Fault Test

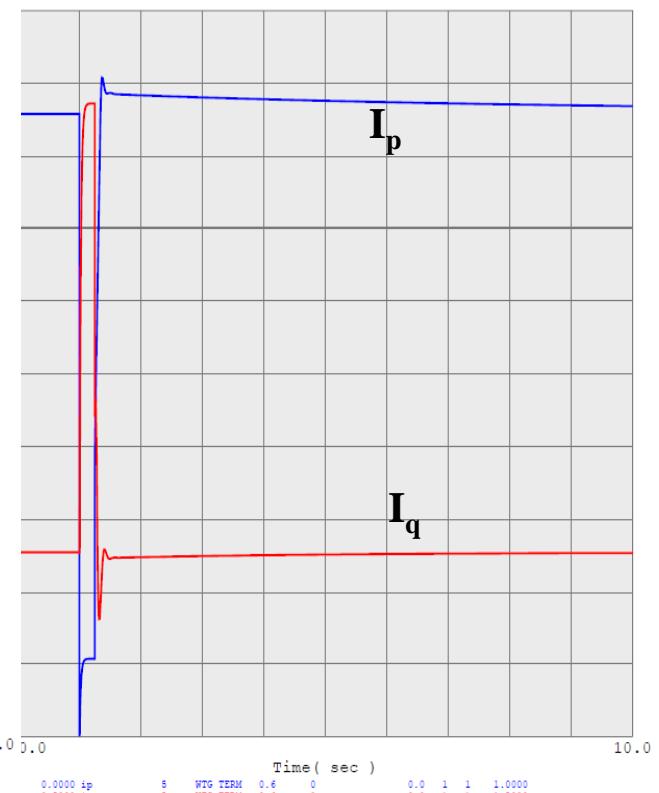
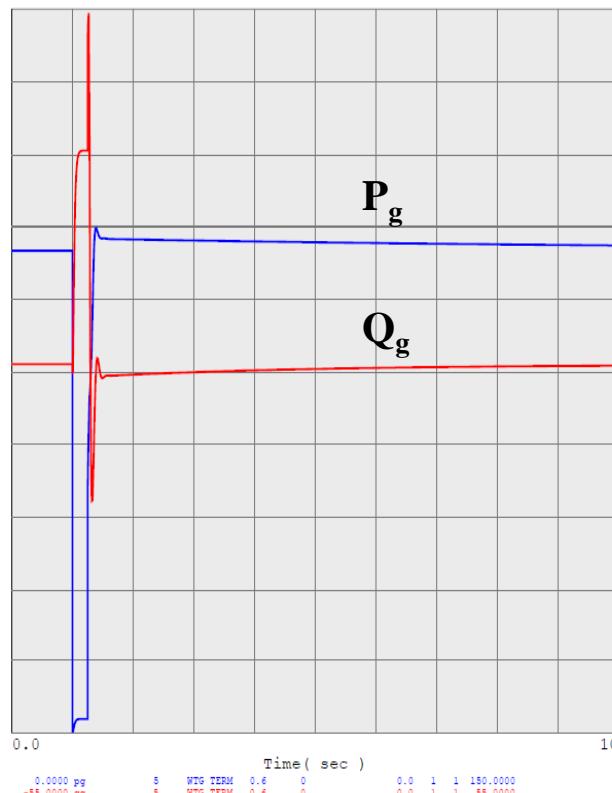
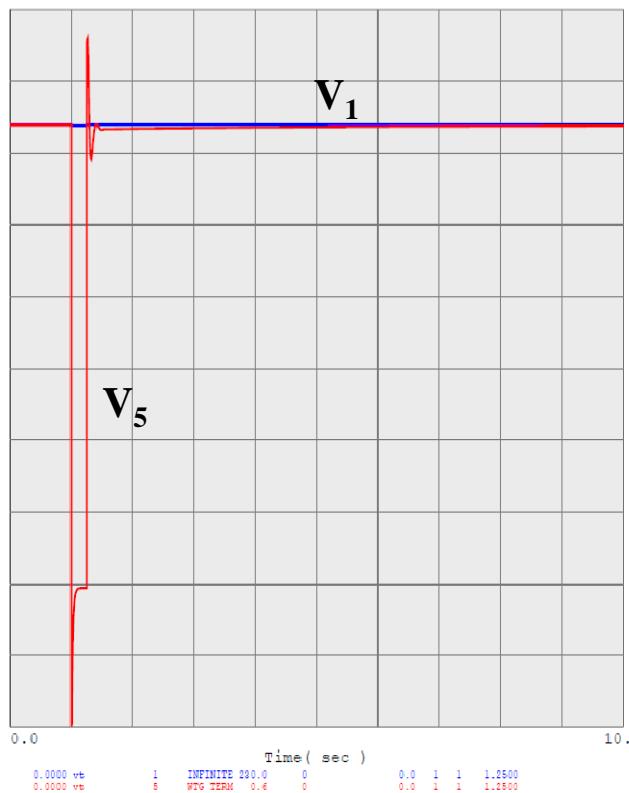
9-cycle, 3-phase fault at POI, clear fault by tripping line





WT4 Fault Test

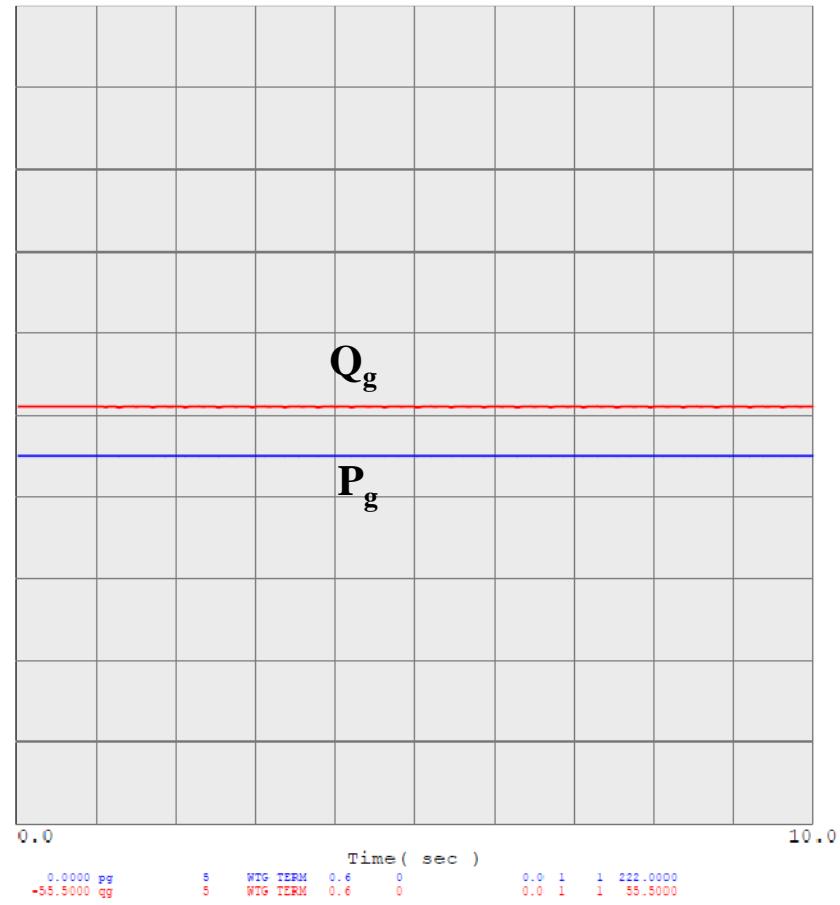
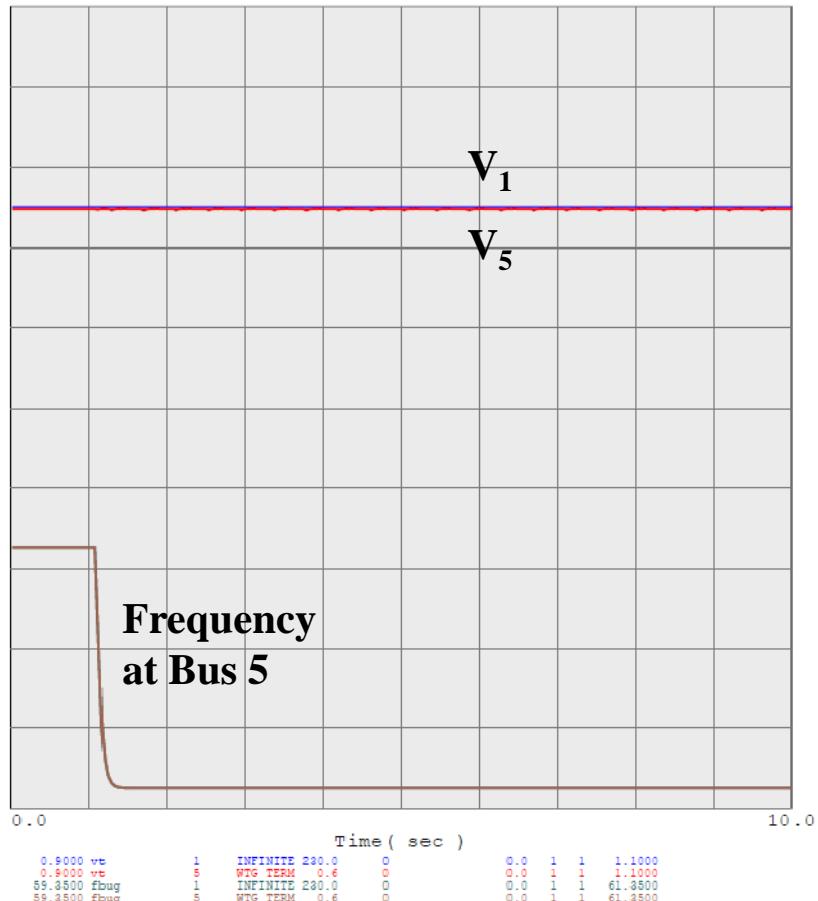
9-cycle, 3-phase fault at POI, clear fault by tripping line





WT4 Frequency Drop Test

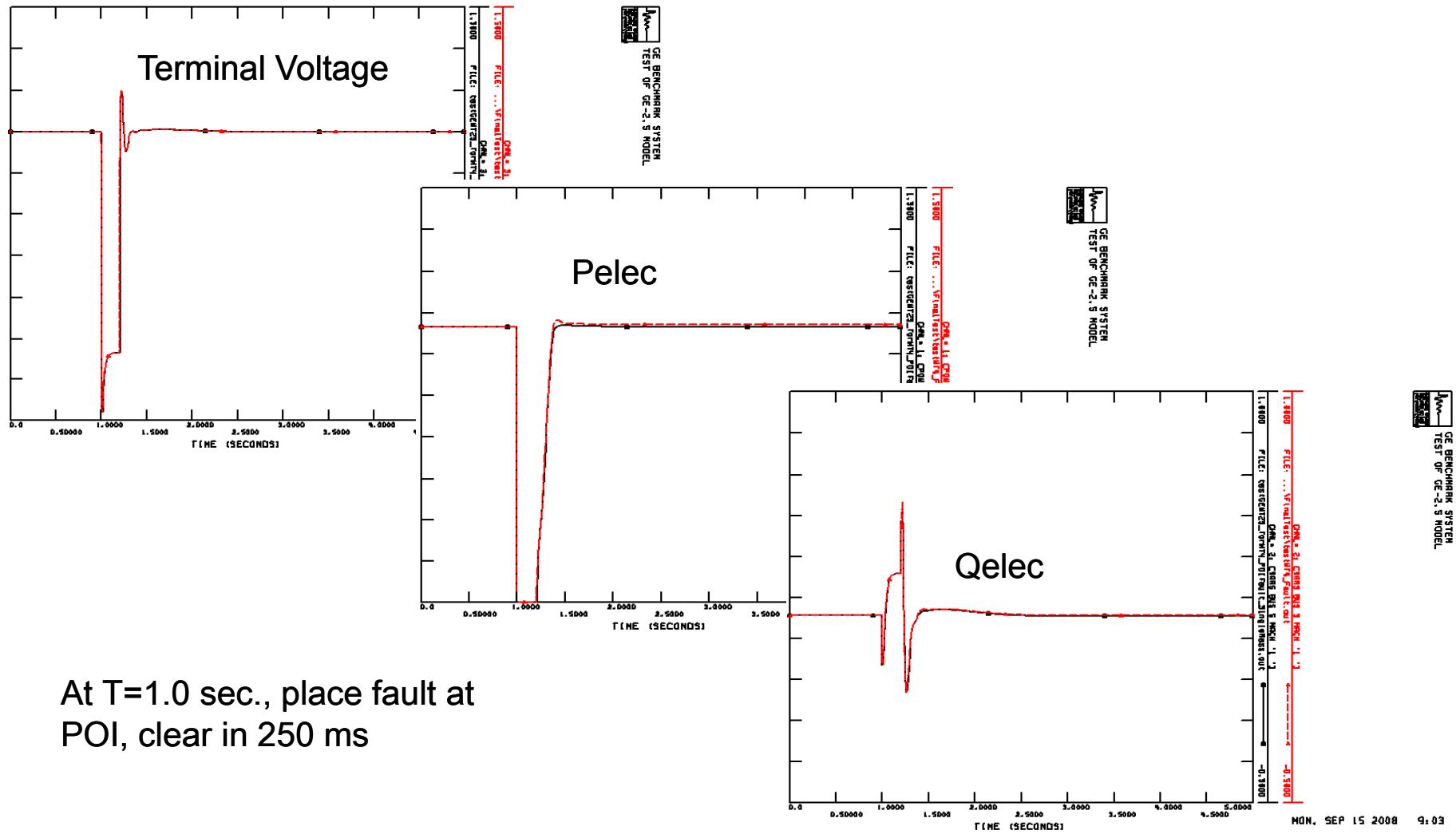
1% drop at t = 1 sec





WT4 Model Comparison

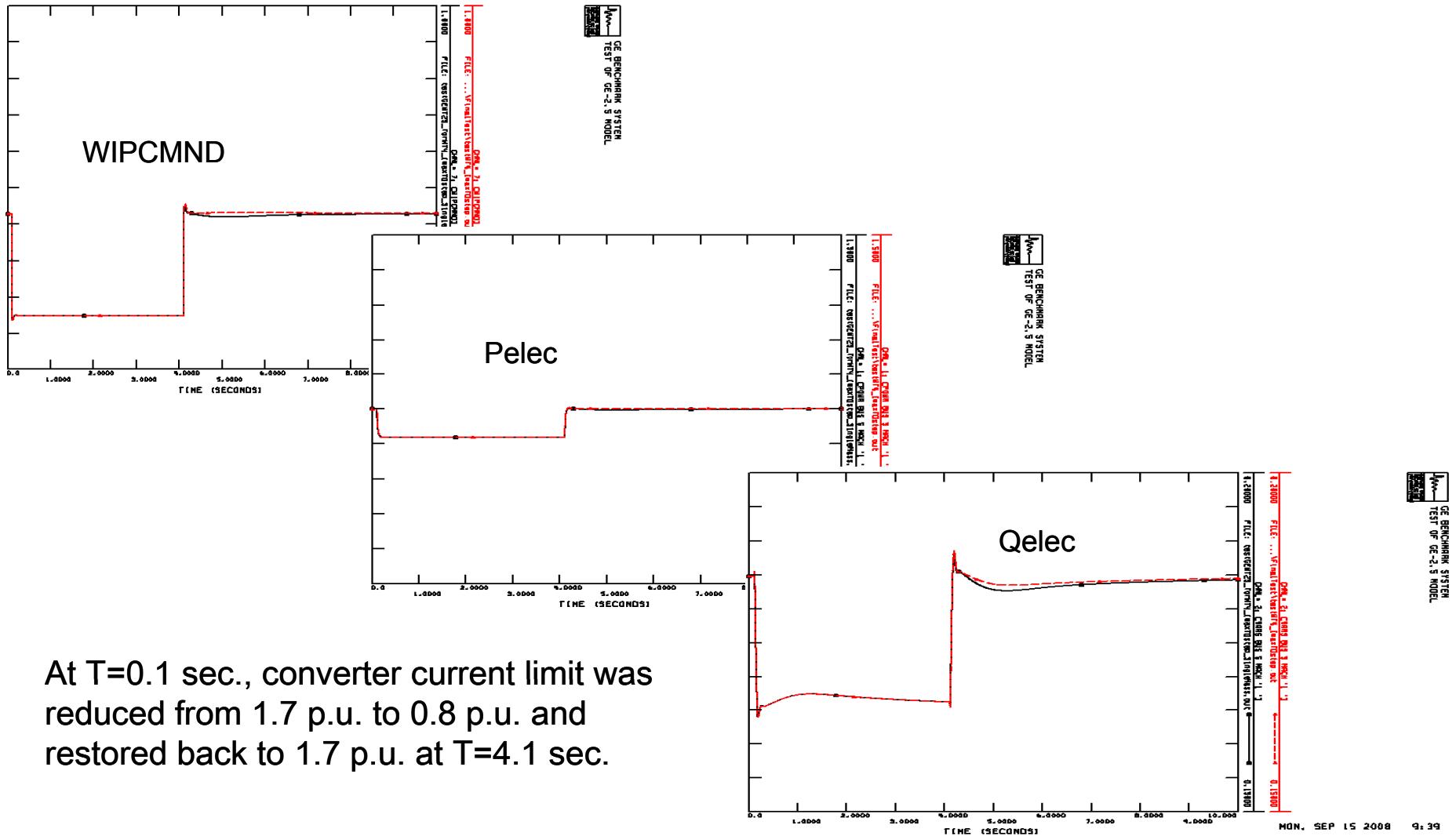
Against GE 2.5 MW Manufacturer Model





WT4 Model Testing

Against GE 2.5 MW Manufacturer Model

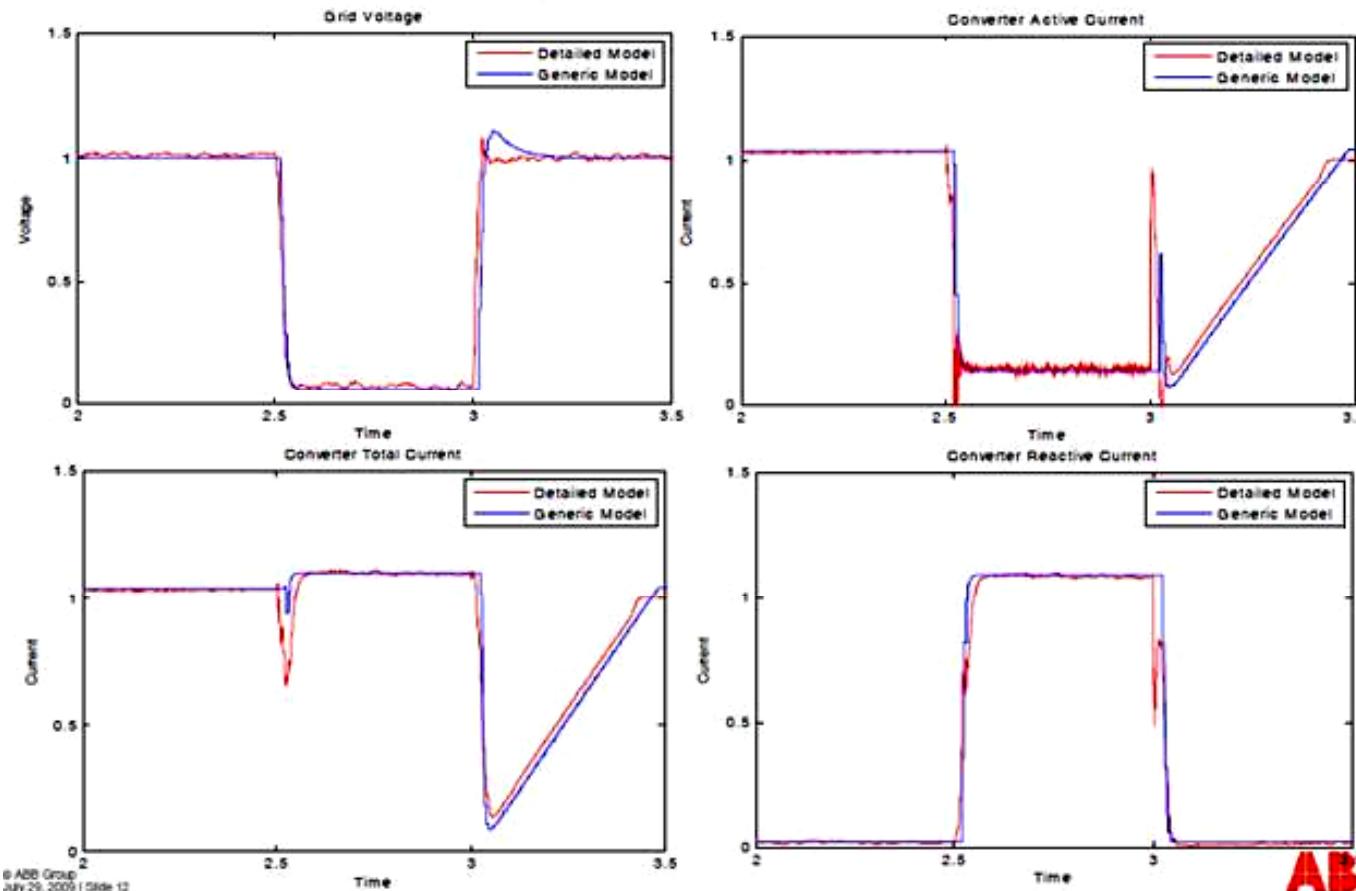




WT4 Model Verification

Against ABB Converter PSCAD Model

Full-converter WTD under 3-ph dip, Detailed model $T_s=0.5 \mu\text{s}$, Generic model $T_s=5 \text{ ms}$



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July 29, 2009 | slide 12

ABB

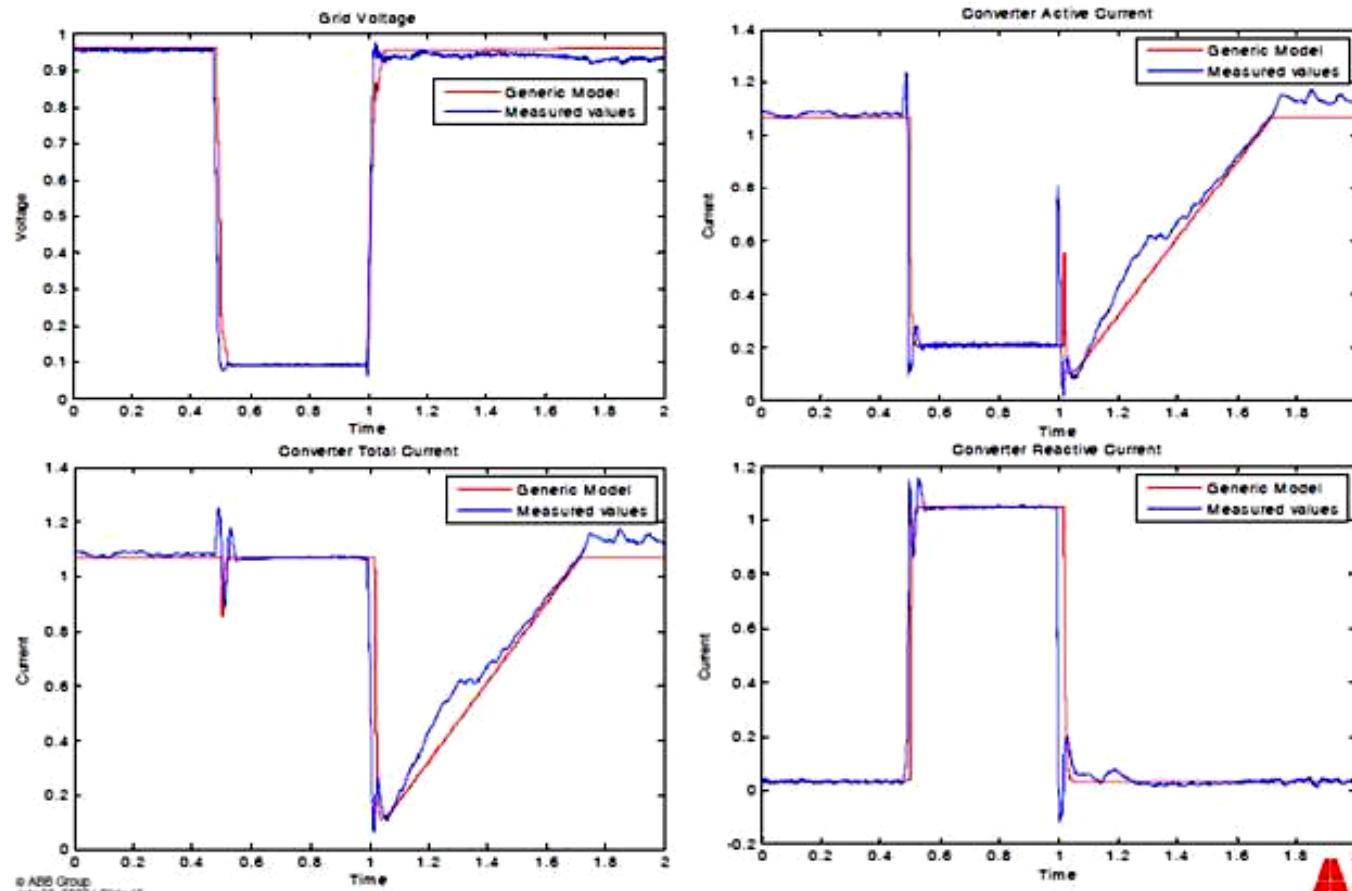
From “WECC - Model Specifications, Validation”, presentation by Slavomir Seman, 7/29/09 at the IEEE PES General Meeting, Calgary, Canada.



WT4 Model Verification

Against ABB Converter Full Power Test

Full converter WTD under 3-ph dip , Generic model Ts = 5 ms



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ABB

From "WECC - Model Specifications, Validation", presentation by Slavomir Seman, 7/29/09 at the IEEE PES General Meeting, Calgary, Canada.



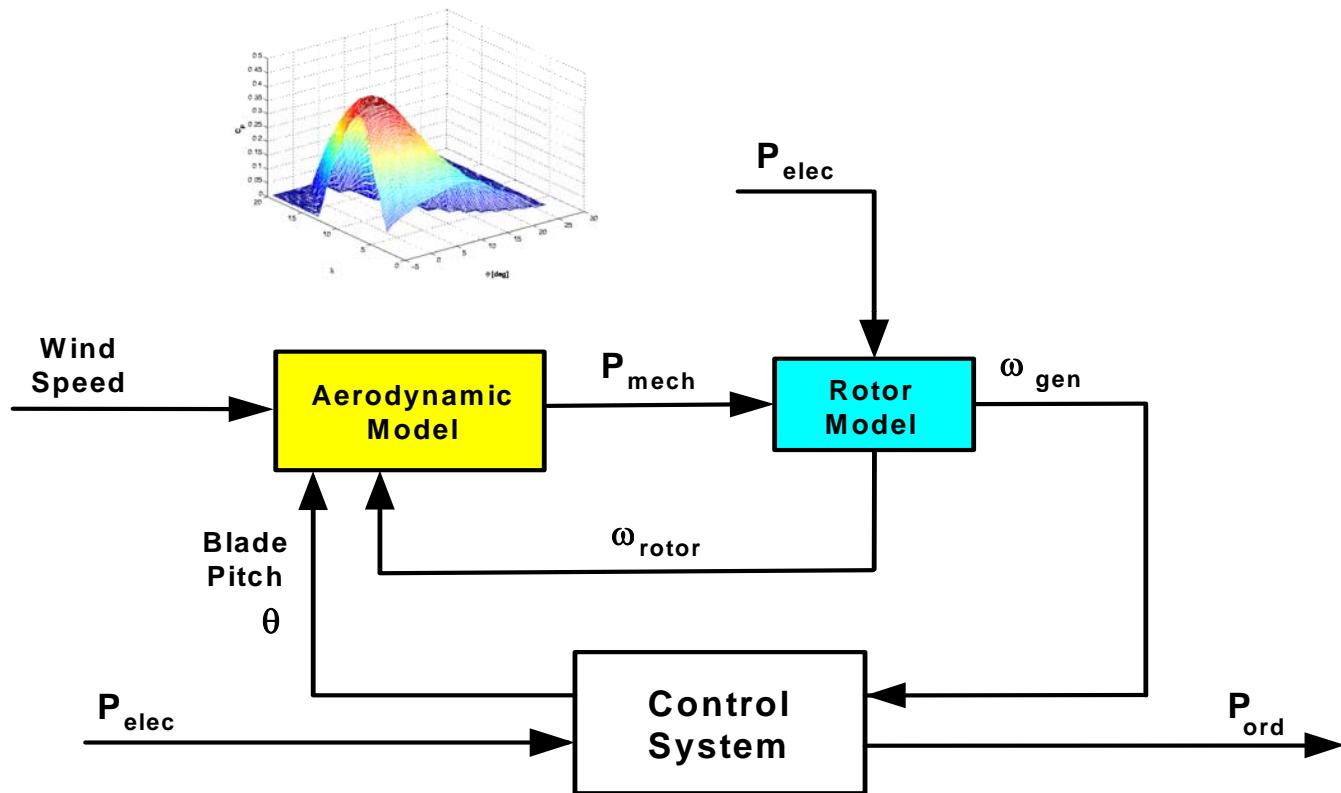
On Aerodynamic Simplification used in WECC Generic Type 3 model

References:

- W. W. Price, J.J. Sanchez-Gasca, “Simplified Wind Turbine Generator Aerodynamic Models for Transient Stability Studies” Proc. IEEE PES PSCE, Atlanta, Georgia, October-November 2006
- M. Behnke, A. Ellis, Y. Kazachkov, T. McCoy, E. Muljadi, W. Price, J. Sanchez-Gasca, “Development and Validation of WECC Variable Speed Wind Turbine Dynamic Models for Grid Integration Studies”, AWEA WindPower, Los Angeles, California, June 2007



Aerodynamic Conversion



$$P_{mech} = \frac{\rho}{2} A_r v^3 C_p(\lambda, \theta)$$



Aerodynamic Simplification

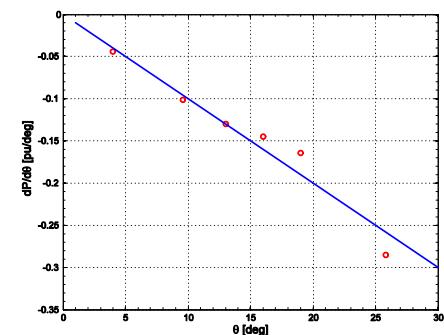
- Assume wind speed is constant for the duration of the typical period of interest in dynamic simulations (up to about 20 seconds)
- For variable speed Type 3 it was noticed that
 - Rate of change of mechanical power (P_{mech}) varies linearly with respect to pitch angle (θ) in the range $0 < \theta < 30$ deg
 - P_{mech} varies linearly with respect to wind speed (V_w) from cut-in to rated wind speed
 - θ varies linearly with respect to V_w for wind speeds above rated



Detailed 3-D Cp Curve.

2-D Cp Curve used in
detailed models

Linear relations
allow for simplifications





Example for GE 1.5 WTG

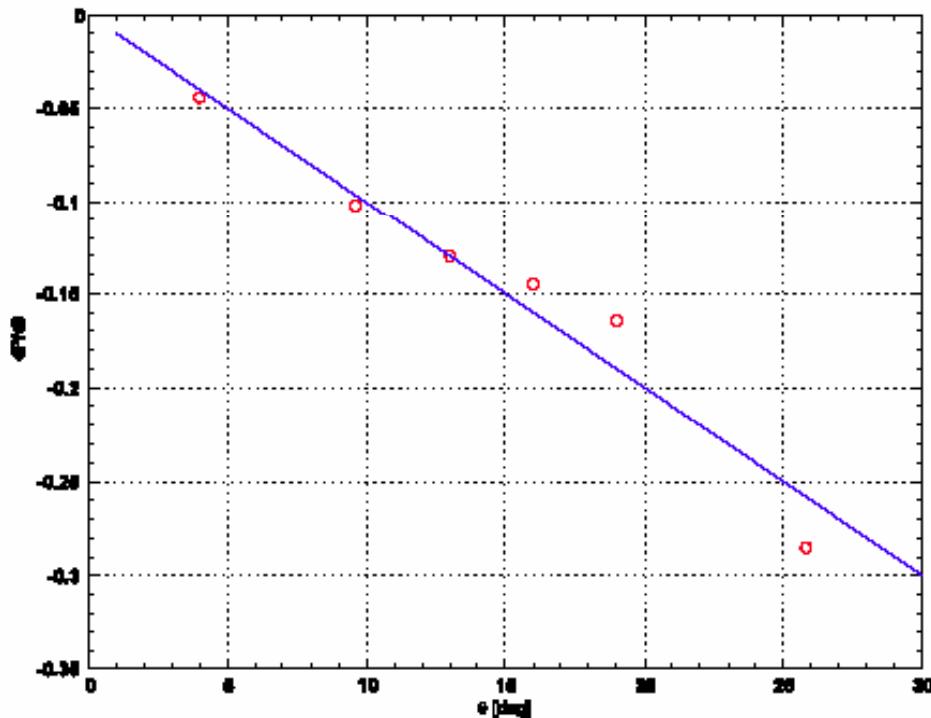


Figure 7. Rate of Change in Mechanical Power vs. Pitch Angle

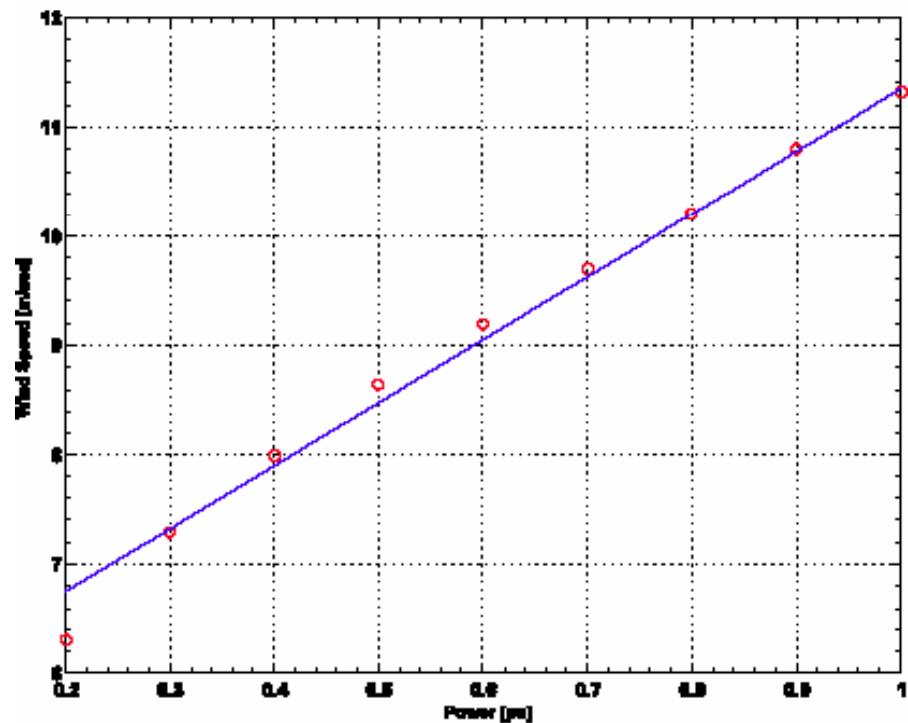


Figure 8. Wind Speed vs. Mechanical Power
Solid Line: Linear Fit $V_w = 5.75 \cdot P_{\text{mech}} + 5.60$



Example for GE 1.5 WTG

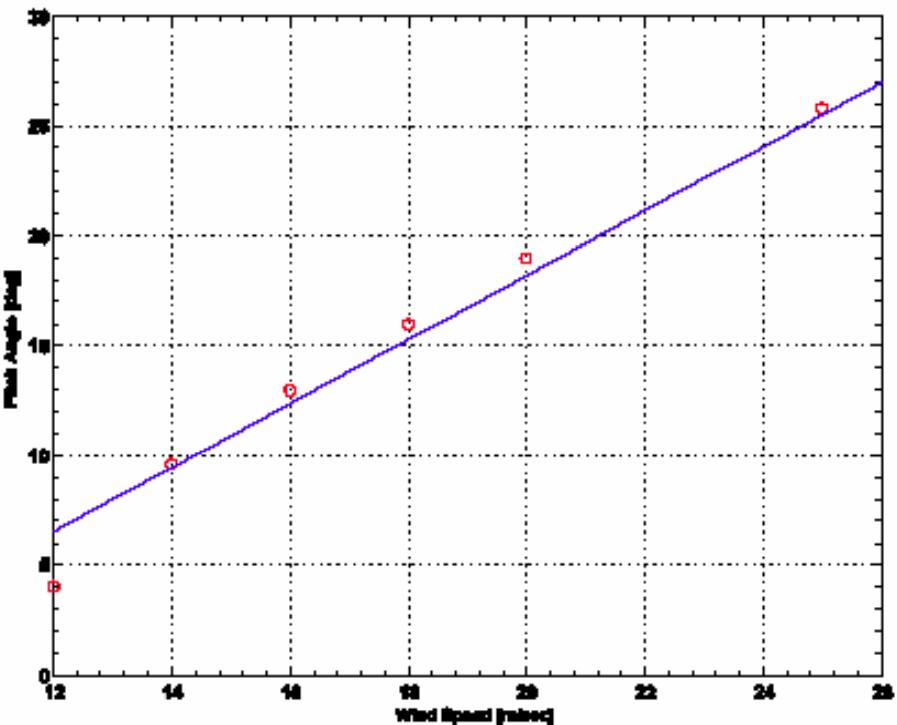


Figure 9. Pitch Angle vs. Wind Speed
Solid Line: Linear Fit $\theta = 1.46 \cdot Vw - 11.0$

“Aerodynamic governor” model

$$P_m = P_{m_o} - \theta (\theta - \theta_o) / 100$$

Initialization:

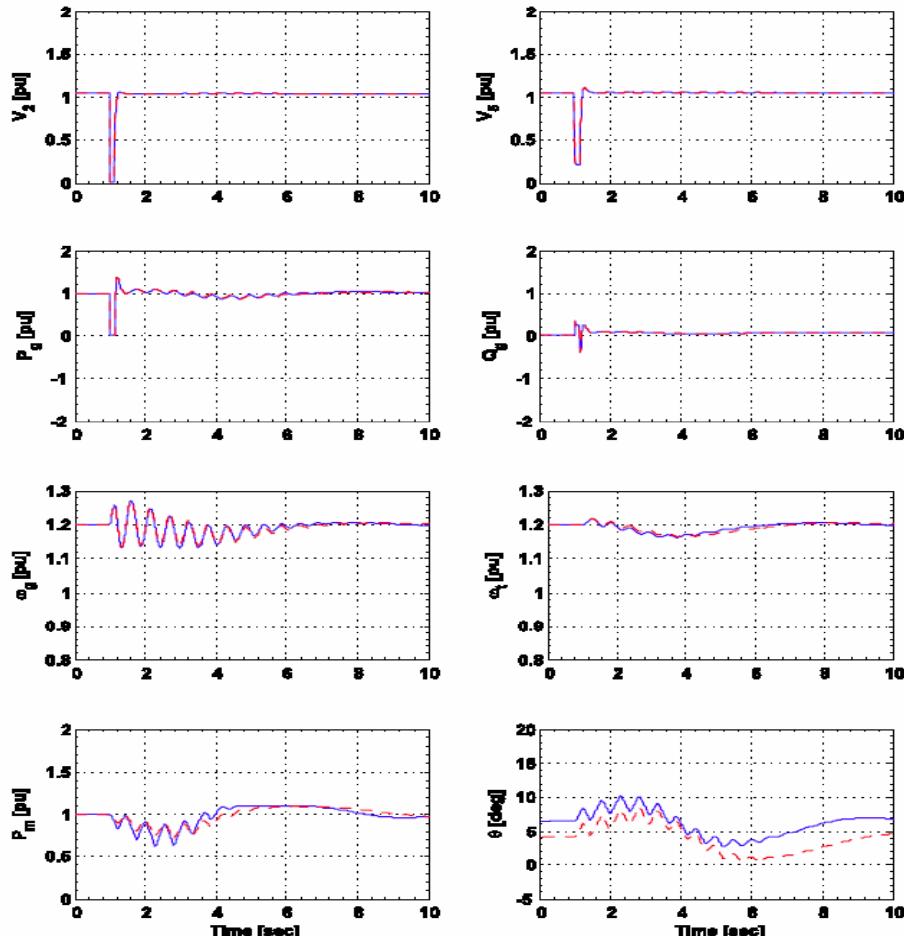
- $P_{m_o} = P_{elec}$ (from power flow)
- Use Fig. 8 to find V_w for $\theta_o = 0$
- Use Fig. 9 to compute θ_o if $P_e = P_{rated}$ and user-input
 V_w is greater than rated wind speed



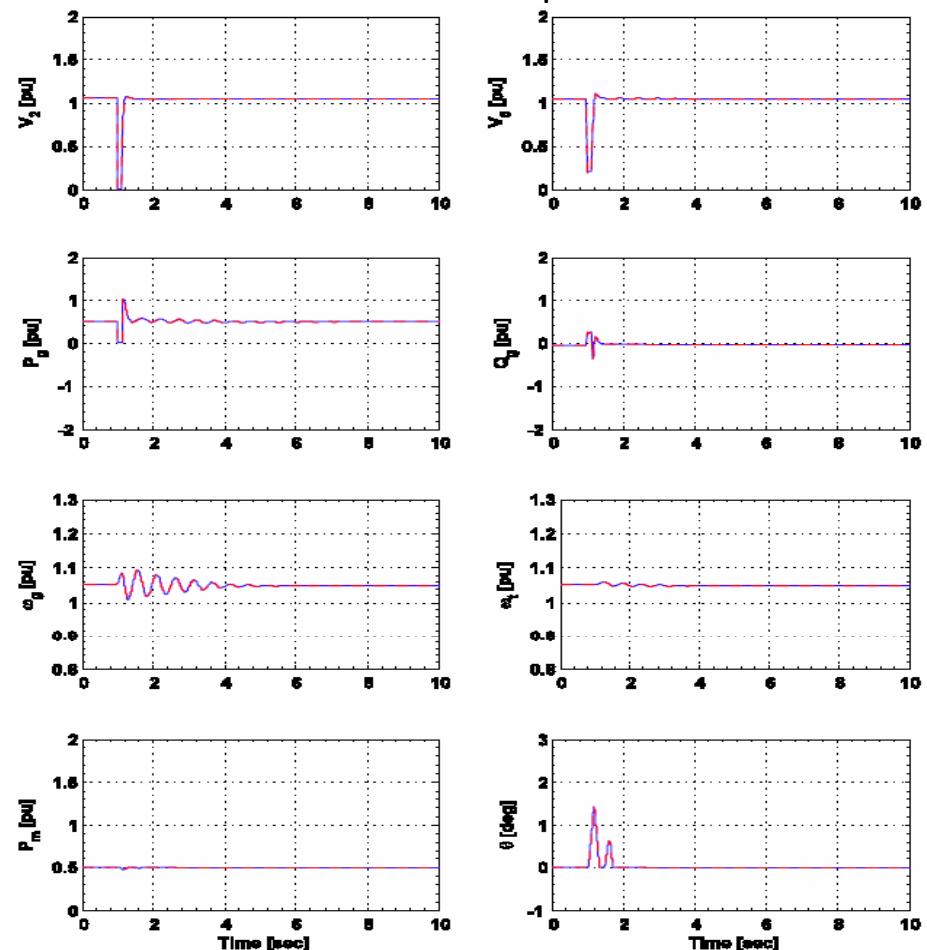
Testing of Aerodynamic Simplification

Against GE1.5 Manufacturer Model

At rated output



At 50% output



Blue = manufacturer standard model, Red = WECC WT3 generic model



On Identification of WTG Model Parameters and Model Validation Efforts



Efforts Underway in North America

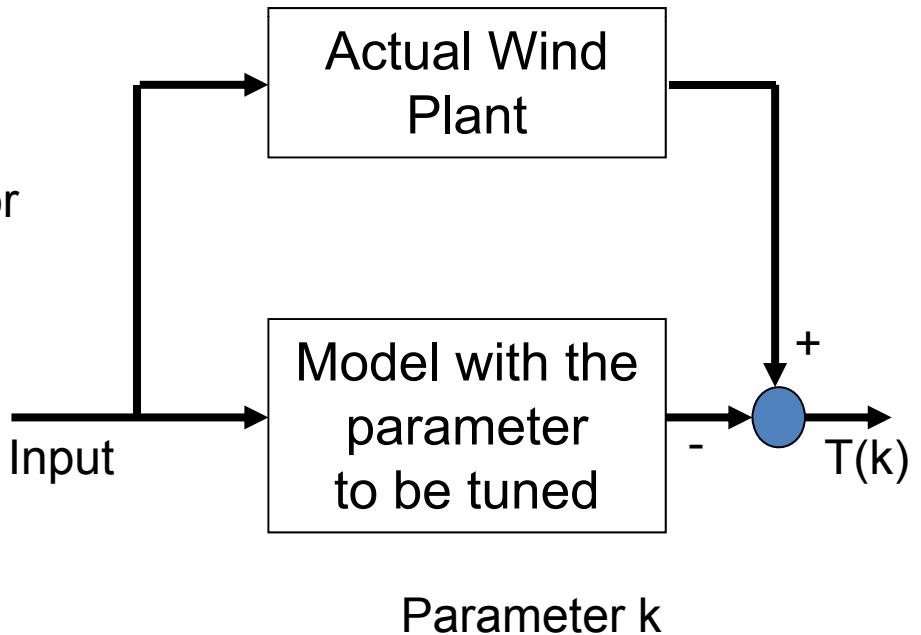
- NREL Model Parameter Identification Project
 - Tune parameters to match performance of manufacturer models) using parameter trajectory sensitivity approach
 - Parameters to be published in WECC WGMG guide
- IEEE DPWPGMG
 - Collaboration with several WTG manufacturers and industry stakeholders in the US and Europe
 - Develop specifications and test systems for model validation (underway)
- UWIG/EnerNex
 - Document generic model validation against measurements
- Hydro Quebec
 - Has done some work in this area
- PSLF and PSSE software developers and consultants



Parameter Sensitivity Approach

- The output of the simulation and the measured data can be used to find the total error of the measurement.
- $P_{\text{err}} = |P_{\text{meas.}} - P_{\text{simulated}}|$
- $Q_{\text{err}} = |Q_{\text{meas.}} - Q_{\text{simulated}}|$
- The error and the sensitivity parameter k_1 with respect to the error can be computed.
- Use the other parameters k_1, k_2, k_3, k_4 etc
- The parameter sensitivity can be observed from the results.
- The trend can be used to drive the changes of the parameters.

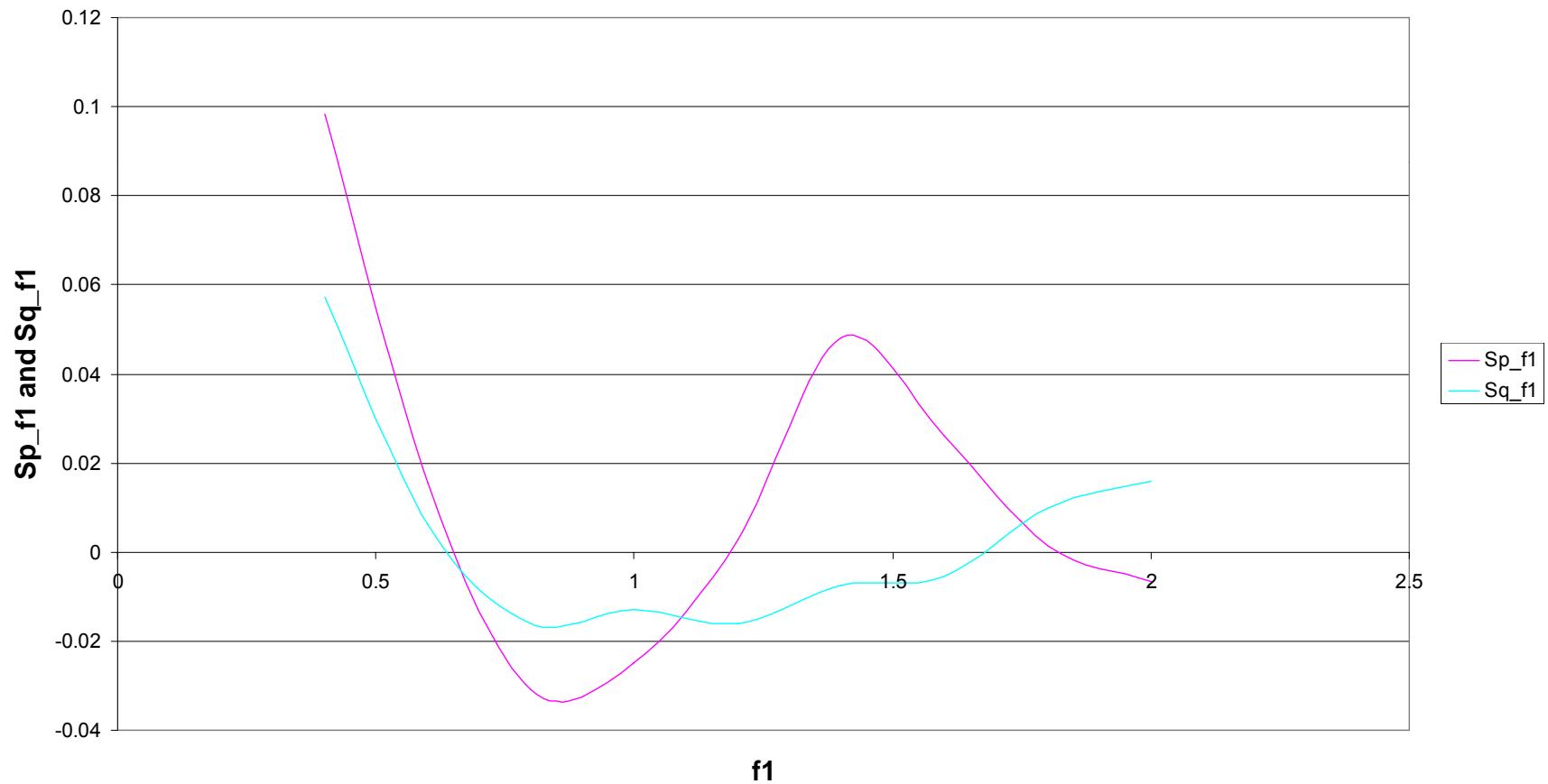
$$S_k \frac{T(k)}{dk} := \frac{dT(k)}{dk} \cdot \frac{k}{T(k)}$$

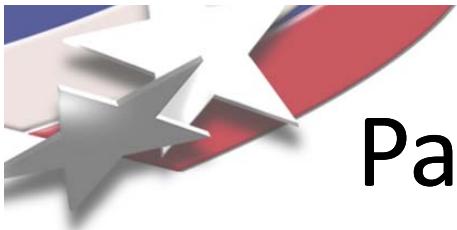




Parameter Sensitivity Approach

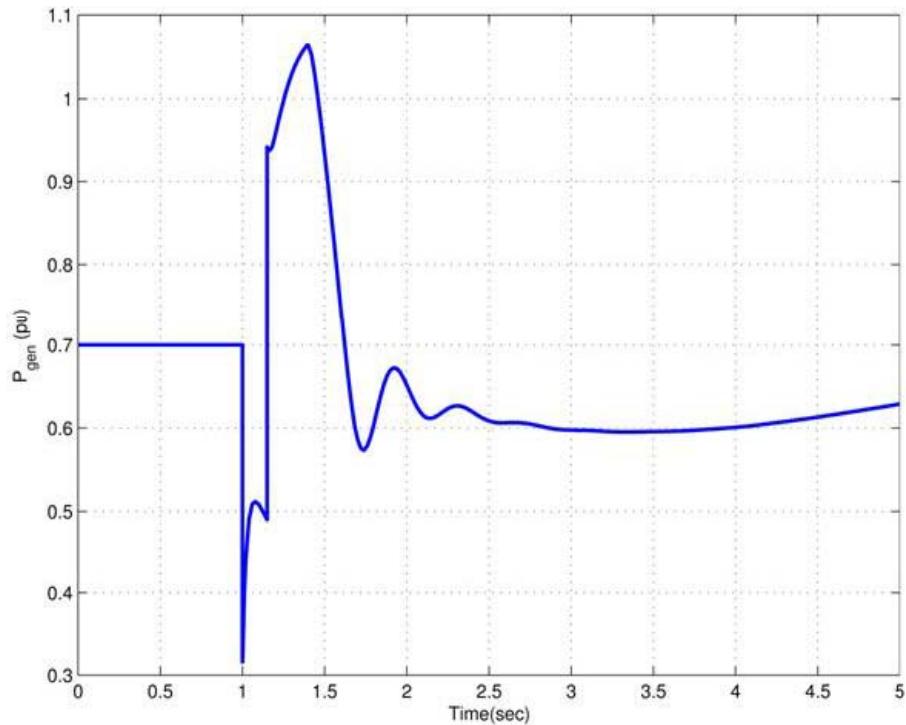
Sensitivity of parameter f_1 (S_{f1}) to P_{error} and Q_{error}



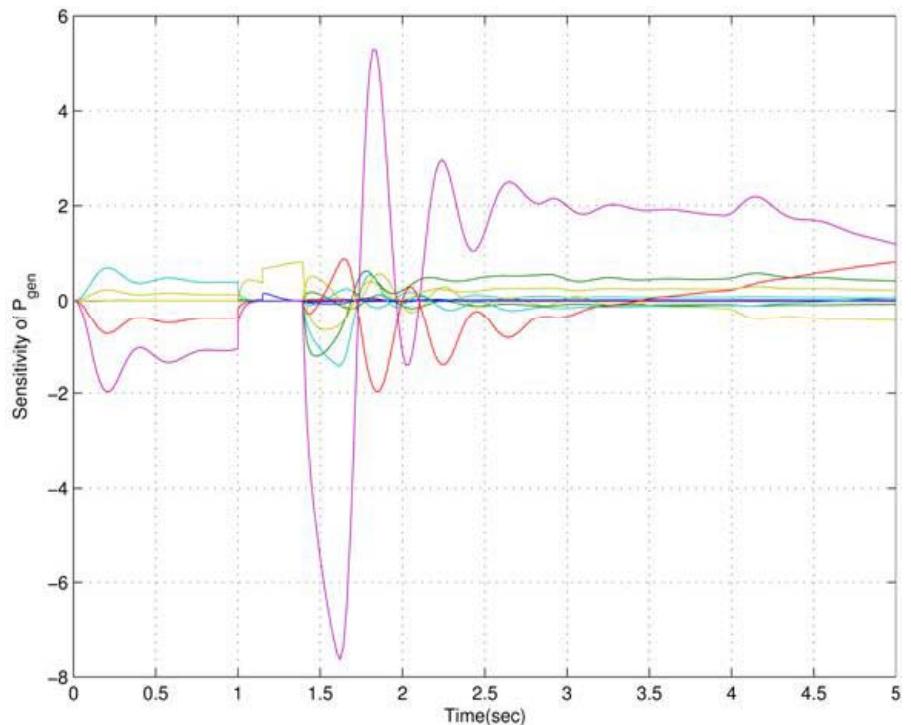


Parameter Sensitivity Approach

Example for WECC WT3 Generic Model



Response of P output



Sensitivity of P output to a range of parameters

- Qualitatively similar results for other outputs.
- Note that a lot of parameters have small and/or correlated influence.
- Sensitivities obtained as a by-product of running the simulation.



On Representation of Wind Farms With WECC Generic WTG Models

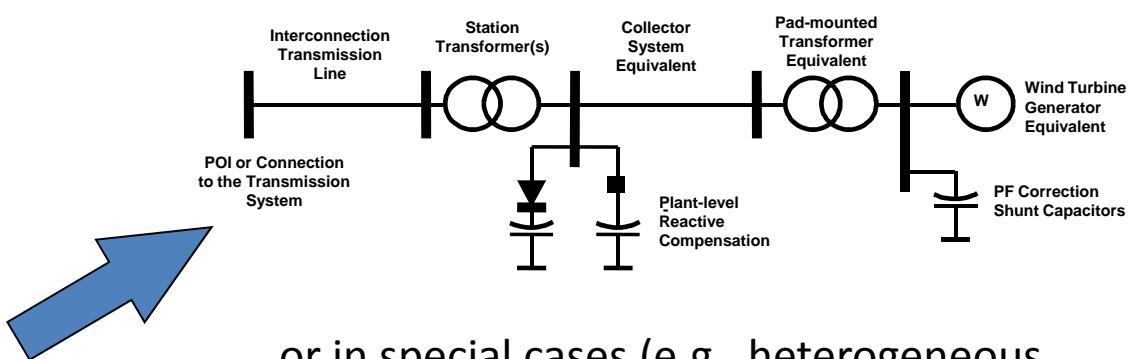
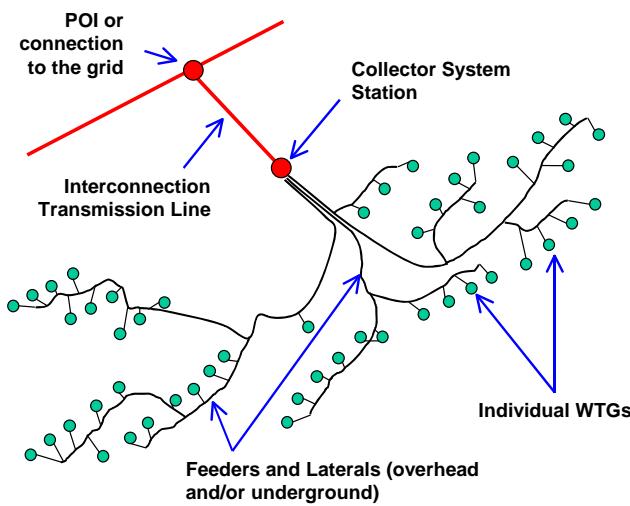
References:

- E. Muljadi, C.P. Butterfield, B. Parsons, A. Ellis, "Characteristics of Variable Speed Wind Turbines Under Normal and Fault Conditions", IEEE PES GM, Tampa, Florida, June 2007.
- J. Brochu, R. Gagnon, C. Larose, "Validation of the WECC Single-Machine Equivalent Power Plant", Presented at the IEEE PSCE DPWPG-WG Meeting, Seattle, Washington, March 2009.
- WECC Wind Generation Power Flow Modeling Guide

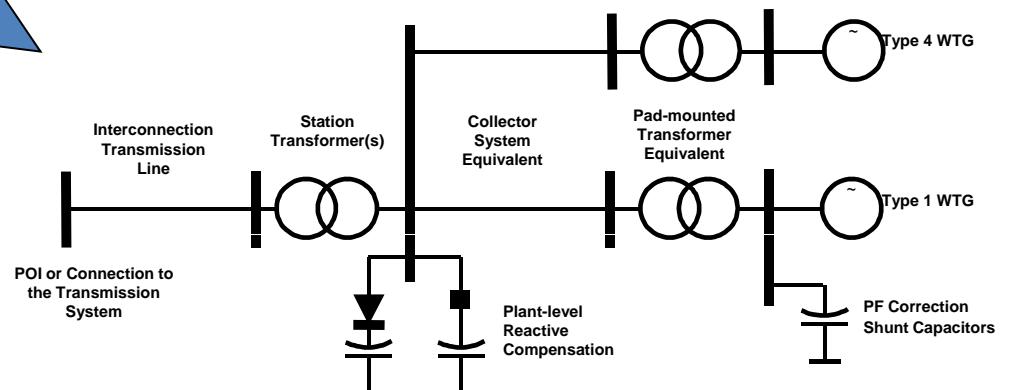


Wind Power Plant Representation

- WECC WGMG recommendation is to use a single-machine equivalent for power flow and dynamic representation of Wind Power Plants



...or in special cases (e.g., heterogeneous feeders or WTGs of different types)...



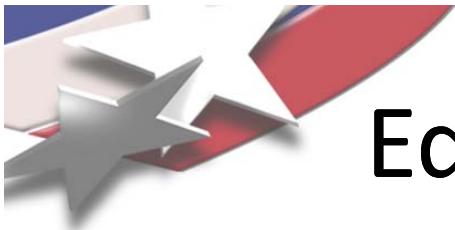


Equivalent Collector System

- Depends on feeder type (OH/UG) and WPP size
- Z_{eq} and B_{eq} , can be computed from WPP conductor schedule, if available
 - For radial feeders with N WTGs and I branches:

$$Z_{eq} = R_{eq} + jX_{eq} = \frac{\sum_{i=1}^I Z_i n_i^2}{N^2} \quad B_{eq} = \sum_{i=1}^I B_i$$

- Where n_i is the number of WTGs connected upstream of the i -th branch
- This can be implemented easily on a spreadsheet



Equivalent Collector System

- Example with $N=18$ and $I=21$:

| From | To | R | X | B | n | $R n^2$ | $X n^2$ |
|------|-----|--------|--------|--------|----|---------|---------|
| 1 | 2 | 0.0035 | 0.0263 | 0.0000 | 1 | 0.0035 | 0.0263 |
| 2 | 3 | 0.0018 | 0.0254 | 0.0013 | 2 | 0.0071 | 0.1015 |
| 3 | 4 | 0.0080 | 0.0226 | 0.0008 | 3 | 0.0722 | 0.2030 |
| 4 | 5 | 0.0023 | 0.0193 | 0.0005 | 4 | 0.0364 | 0.3080 |
| 5 | 51 | 0.0074 | 0.0248 | 0.0000 | 5 | 0.1861 | 0.6200 |
| 6 | 7 | 0.0031 | 0.0171 | 0.0014 | 1 | 0.0031 | 0.0171 |
| 7 | 8 | 0.0061 | 0.0143 | 0.0015 | 2 | 0.0244 | 0.0572 |
| 8 | 9 | 0.0069 | 0.0107 | 0.0004 | 3 | 0.0617 | 0.0965 |
| 9 | 51 | 0.0070 | 0.0033 | 0.0004 | 4 | 0.1113 | 0.0525 |
| 10 | 11 | 0.0078 | 0.0371 | 0.0003 | 1 | 0.0078 | 0.0371 |
| 11 | 12 | 0.0001 | 0.0005 | 0.0004 | 2 | 0.0005 | 0.0021 |
| 12 | 52 | 0.0083 | 0.0259 | 0.0004 | 3 | 0.0747 | 0.2330 |
| 13 | 14 | 0.0049 | 0.0349 | 0.0004 | 1 | 0.0049 | 0.0349 |
| 14 | 15 | 0.0041 | 0.0483 | 0.0008 | 2 | 0.0163 | 0.1931 |
| 15 | 16 | 0.0059 | 0.0116 | 0.0002 | 3 | 0.0528 | 0.1040 |
| 16 | 17 | 0.0079 | 0.0002 | 0.0003 | 4 | 0.1262 | 0.0029 |
| 17 | 18 | 0.0089 | 0.0146 | 0.0007 | 5 | 0.2224 | 0.3656 |
| 18 | 53 | 0.0018 | 0.0342 | 0.0008 | 6 | 0.0664 | 1.2302 |
| 51 | 52 | 0.0074 | 0.0034 | 0.0011 | 9 | 0.5957 | 0.2778 |
| 52 | POI | 0.0049 | 0.0456 | 0.0002 | 12 | 0.7102 | 6.5633 |
| 53 | POI | 0.0003 | 0.0338 | 0.0012 | 6 | 0.0125 | 1.2177 |

Sum = B_{EQ}

0.0132

R_{EQ}

2.3962

11.7438

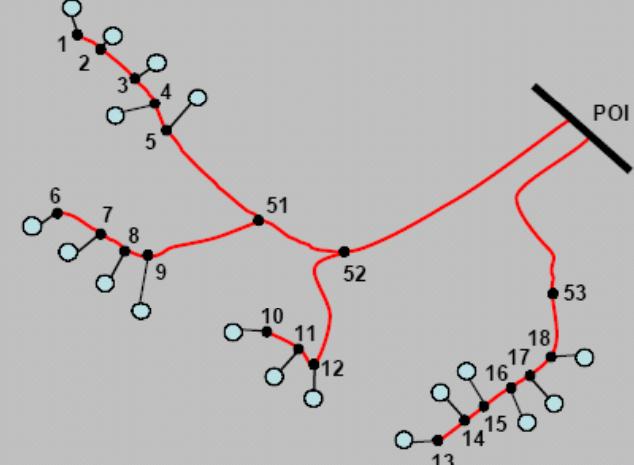
0.0074

0.0362

NOTES:

Branch R, X and B parameters are random numbers in this example.

Parameters should be in per-unit at 100 MVA and collector system kV.



Partial sum

Partial sum divided by total number
of WTG (18 in this case) squared

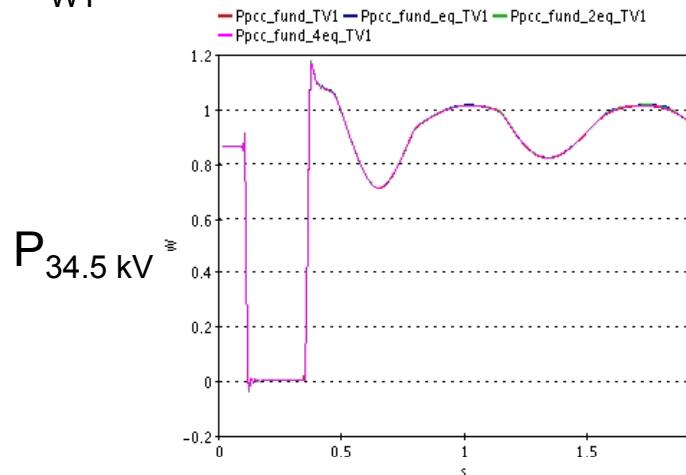


Detailed Vs. Single-Machine Representation

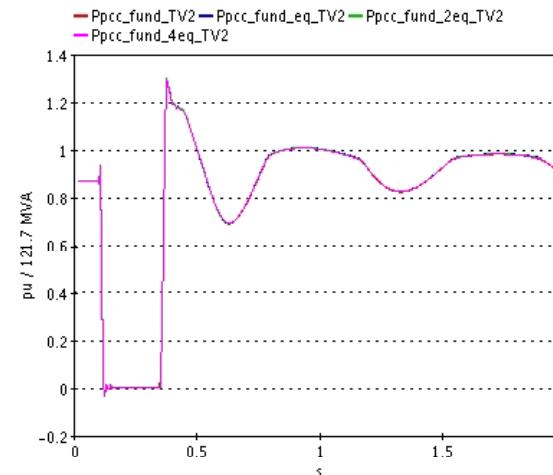
3-phase fault, all WTGs at 12 m/sec

$$Q_{WT} =$$

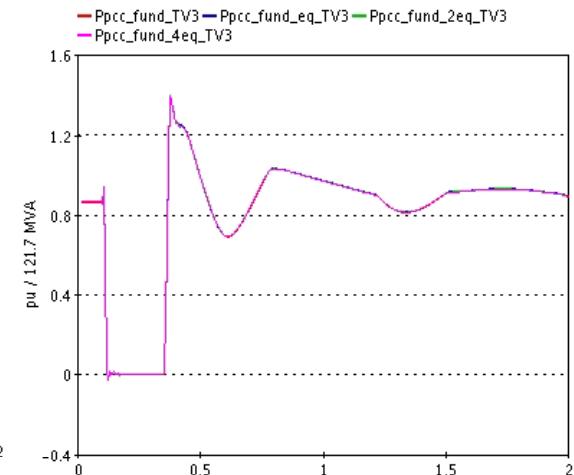
$$0.435$$



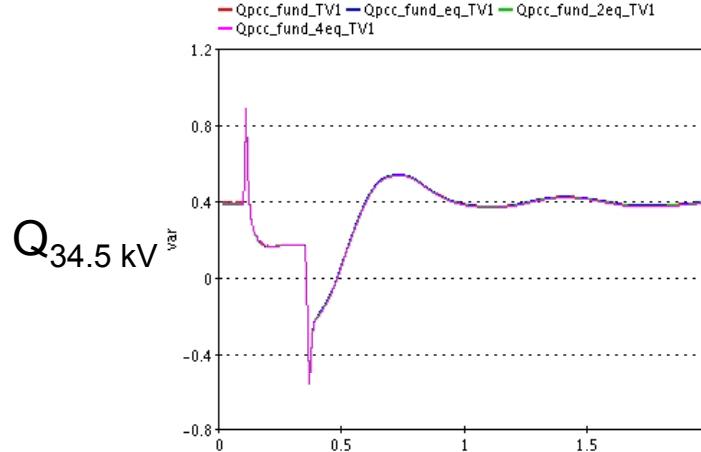
$$0$$



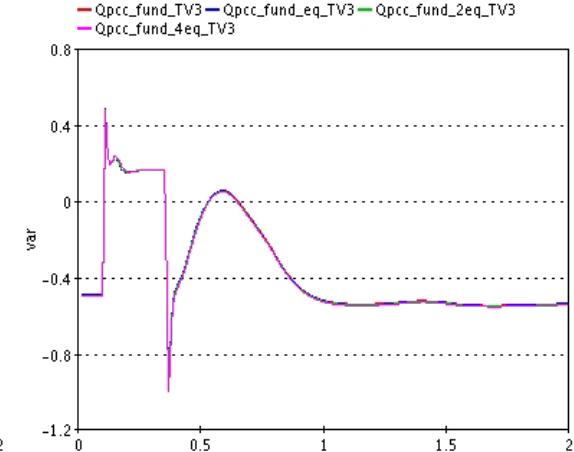
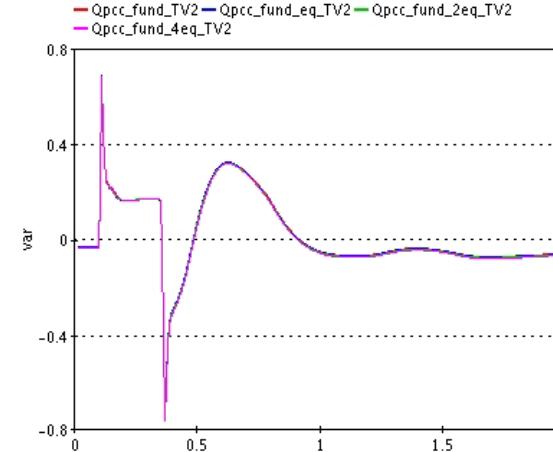
$$-0.435$$



$$P_{34.5 \text{ kV}}$$



$$Q_{34.5 \text{ kV}}$$



From « Validation of the WECC Single-Machine Equivalent Power Plant », Presented DPWPG-WG Meeting at IEEE PSCE, March 2009 - Jacques Brochu, Richard Gagnon, Christian Larose, Hydro Quebec

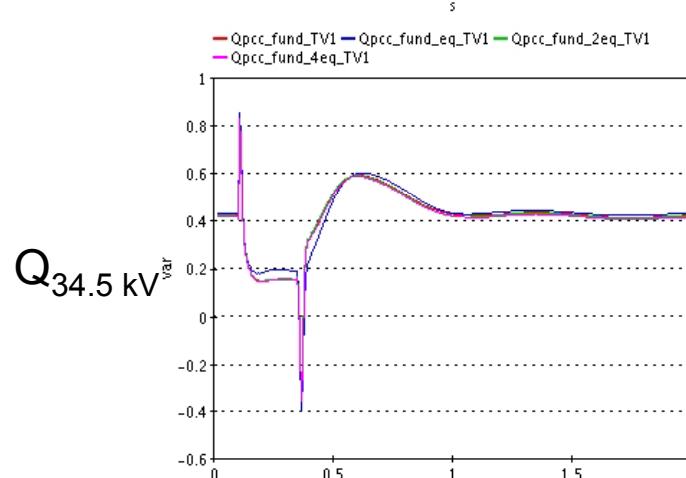
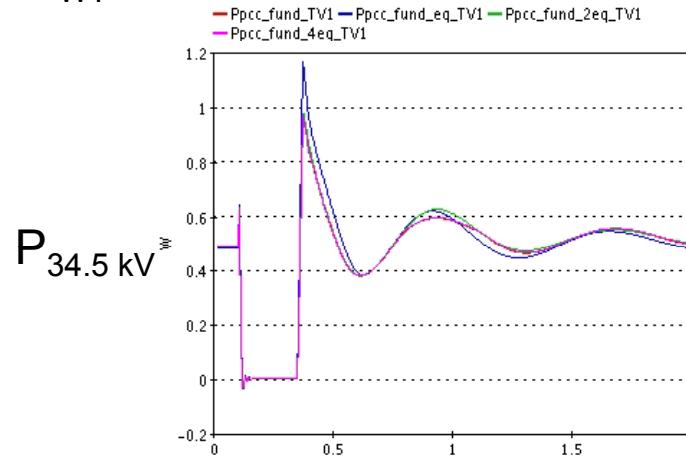


Detailed Vs. Single-Machine Representation

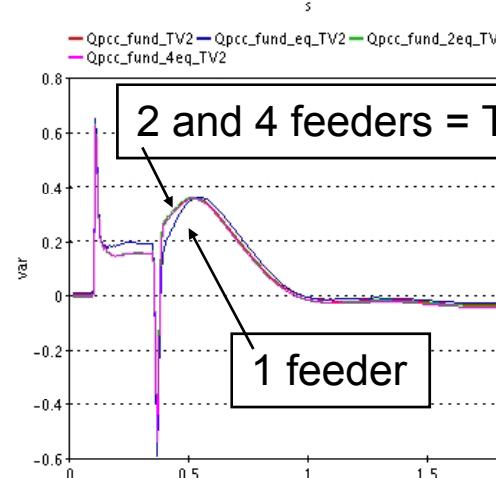
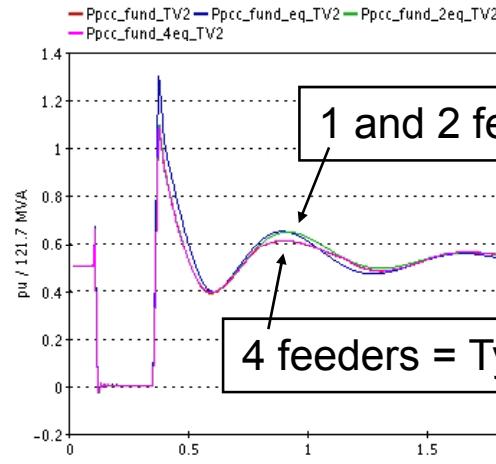
3-phase fault, different wind speed for each feeder

$$Q_{WT} =$$

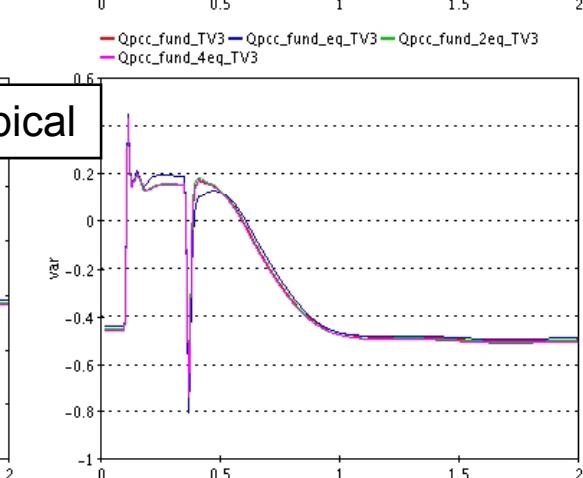
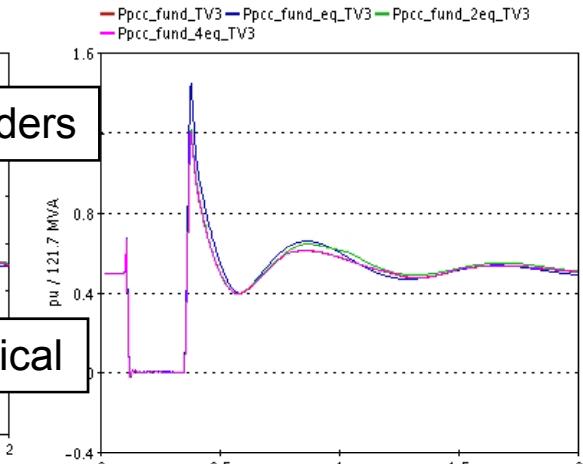
$$0.435$$



$$0$$



$$-0.435$$



From « Validation of the WECC Single-Machine Equivalent Power Plant », Presented DPWPG-WG Meeting at IEEE PSCE, March 2009 - Jacques Brochu, Richard Gagnon, Christian Larose, Hydro Quebec



Questions and Discussion

