## Geometry



## Name

| Word | Definition/Explanation | Examples/Helpful Tips |
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Labelling Parts of a Right Triangle
Given the following triangle
a) Label the hypotenuse "hyp"
b) Label the side opposite <A "opp"
c) Label the side adjacent to <A "adj"


Trigonometric Ratios

|  |  |  |
| :--- | :--- | :--- |
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## Practice

Match the following.
a) $\qquad$ Opposite Leg to $\angle \mathbf{A}$
b) $\qquad$ Sine Ratio of $\angle C$
c) $\qquad$ Opposite Angle to $\overline{A B}$
d) $\qquad$ The Hypotenuse
e) $\qquad$ Adjacent Leg to $\angle \mathrm{A}$
f) $\qquad$ Tangent Ratio of $\angle \mathrm{C}$


1. $\angle \mathrm{A}$
2. $\frac{B C}{A C}$
3. $\angle \mathrm{B}$
g) ___ Reference angle if $\frac{B C}{A C}$ is the Cosine Ratio.
4. $\angle \mathrm{C}$
5. $\frac{A B}{A C}$
h) $\qquad$ Adjacent Leg to $\angle \mathrm{C}$
6. $\overline{A B}$
i) $\qquad$ Cosine Ratio of $\angle A$
j) $\qquad$ The Longest Side
7. $\overline{B C}$
8. $\frac{B C}{A B}$
k) ___ Reference angle if $\frac{B C}{A C}$ is the Sine Ratio.
9. $\overline{A C}$
10. $\frac{A B}{B C}$
(20)

|  | 11. | 12. |
| :---: | :---: | :---: |
| 13. | 14. | 15. |
| 16. | 17. | 18. |

(20)

| 28. | 29. | 30. |
| :---: | :---: | :---: |

(20)

(20)
(25.

Extra Practice

1. Label the sides based of the triangle using the reference angle -- (O) for Opposite, (A) for Adjacent and $(H)$ for Hypotenuse. After you have labeled the triangle, then choose which trigonometric ratio that you would use to solve for the missing info.
a)

b)

c)

d)

SIN COS TAN SIN COS TAN SIN COS TAN SIN COS TAN
e)

f)

g)

h)


SIN COS TAN SIN COS TAN SIN COS TAN SIN COS TAN
2. Solve the angle. (Round all final answers to 2 decimals places)
a)

b)
c)

$\boldsymbol{\theta} \approx$ $\qquad$
$\boldsymbol{\theta} \approx$ $\qquad$
$\boldsymbol{\theta} \approx$ $\qquad$
d)

$\theta \approx$ $\qquad$
3. Solve for the side $x$. (Round all final answers to 2 decimals places)
a)

b)

c)

$\mathbf{x} \approx$ $\qquad$ $\mathbf{x} \approx$ $\qquad$ $\mathbf{x} \approx$ $\qquad$
d)

)
$\mathbf{x} \approx$ $\qquad$
4. Solve for the side $x$. (Round all final answers to 2 decimals places)
a)

b)

d)


$$
\mathbf{x}=
$$

$\qquad$
$\mathbf{x}=$ $\qquad$
c)

$\mathbf{x}=$ $\qquad$

$$
\rightarrow-1
$$

5. Solve for the missing information. (Round all final answers to $\mathbf{2}$ decimals places)
a)

b)

c)

d)

$\mathbf{x} \approx$ $\qquad$
e)

$\boldsymbol{\theta}=$ $\qquad$
i)

j)

k)

I)

$\mathbf{x} \approx$ $\qquad$
m)

n)


$$
\mathbf{x} \approx
$$

$\qquad$
$\qquad$
$\mathbf{x} \approx$ $\qquad$
$\mathbf{x} \approx$
$\mathbf{x} \approx$ $\qquad$
p)

o)


Angle of Elevation vs. Angle of Depression

|  |  |
| :--- | :--- |
|  |  |
|  |  |


a) the angle of elevation from the CAR to the top of the DINER is $\qquad$ .
b) the angle of depression from the top of the TALL BUILDING to the DINER is $\qquad$ .
c) the angle of elevation from the PLANE to the HELICOPTER is $\qquad$ .
d) the angle of depression from the top of the DINER to the BOY is $\qquad$ .
e) the angle of depression from the HELICOPTER to the PLANE is $\qquad$ .
f) the angle of depression from the PLANE to the top of the DINER is $\qquad$ .
g) the angle of elevation from the BOY to the top of the DINER is $\qquad$ .
h) the angle of depression from the top of the TALL BUILDING to the top of the CAR is $\qquad$ .
i) the angle of depression from the HELICOPTER to the top of the TALL BUILDING is $\qquad$ .
j) the angle of elevation from the top of the DINER to the top of the TALL BUILDING is $\qquad$ .
k) the angle of elevation from the top of the DINER to the PLANE is $\qquad$ .
I) the angle of depression from the top of the DINER to the CAR is $\qquad$ .
m ) the angle of elevation from the BOY to the front of the PLANE is $\qquad$ .
n) the angle of elevation from the CAR to the top of the DINER is $\qquad$ .
o) the angle of depression from the front of the PLANE to the BOY is $\qquad$ .
p) the angle of elevation from the TALL BUILDING to the HELICOPTER is $\qquad$ -
(150
(20)

Circle (or Draw) the side or angle that is represented by the description:
a) The Leaning Ladder


Height on the wall that the ladder reaches.
b) The Leaning Ladder


The distance from the foot of the ladder to the wall.
c) The Leaning Ladder


The angle the ladder forms with the wall.
d) The Shadow


The length of his shadow.

Circle (or Draw) the side or angle that is represented by the description:


## Practice Problems

b) A helicopter is hovering over a landing pad 100 m from where you are standing. The helicopter's angle of elevation with the ground is $15^{\circ}$. What is the altitude of the helicopter?

d) A 15 m pole is leaning against a wall. The foot of the pole is 10 m from the wall. Find the angle that the pole makes with the ground.

a) A young boy lets out 30 ft of string on his kite. If the angle of elevation from the boy to his kite is $27^{\circ}$, how high is the kite?
b) A 20 ft ladder leans against a wall so that it can reach a window 18 ft off the ground. What is the angle formed at the foot of the ladder?

| DIAGRAM |  |
| :--- | :--- |
|  |  |

c) To support a young tree, Jack attaches a guy wire from the ground to the tree. The wire is attached to the tree 4 ft above the ground. If the angle formed between the wire and the tree is $70^{\circ}$, what is the length of the wire?
d) A helicopter is directly over a landing pad. If Billy is 110 ft from the landing pad, and looks up to see the helicopter at $65^{\circ}$ to see it. How high is the helicopter?

| DIAGRAM | DIAGRAM |
| :--- | :--- |
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An Extra Step and a Self-Assessing Exit Ticket
a) How long is the guy wire? b) What is the angle formed between the guy wire and the ground?


Practice

1. A tree casts a shadow 21 m long. The angle of elevation of the sun is $55^{\circ}$. What is the height of the tree?

2. A helicopter is hovering over a landing pad 100 m from where you are standing. The helicopter's angle of elevation with the ground is $15^{\circ}$. What is the altitude of the helicopter?

3. A 15 m pole is leaning against a wall. The foot of the pole is 10 m from the wall. Find the angle that the pole makes with the ground.

4. A guy wire reaches from the top of a 120 m television transmitter tower to the ground. The wire makes a $68^{\circ}$ angle with the ground. Find the length of the guy wire.

5. A lighthouse operator sights a sailboat at an angle of depression of $12^{\circ}$. If the sailboat is 80 m away, how tall is the lighthouse?

6. An airplane climbs at an angle of $16^{\circ}$ with the ground. Find the ground distance the plane travels as it moves 2500 m through the air.

7. a) How long is the guy wire?
b) What is the angle formed between the guy wire and the ground?

8. a) What is the length of the line of sight from the man to the helicopter?

What is the angle of elevation from the man to the helicopter?
10. a) A field has a length of 12 m and a diagonal of 13 m . What is the width?
b) What is the angle formed between the diagonal and the width of the field?
11. a) A 5 ft 11 inch women casts 3 ft shadow.
b) What is the angle that the sun's rays make with the ground?

12. a) A ramp is 18 m long. If the horizontal distance of the ramp is 17 m , what is the vertical distance?
b) What is the angle of elevation of the ramp?


## Extra Practice

Draw a diagram, label, and solve for the missing part:

1. Find to the nearest meter the height of a building if its shadow is 37 m long when the angle of elevation of the sun contains $42^{\circ}$.
2. A 5-foot wire attached to the top of a tent pole reaches a stake in the ground 3 feet from the foot of the pole. Find to the nearest degree the measure of the angle made by the wire with the ground.
3. While flying a kite, Doris let out 400 feet of string. Assuming that the string is stretched taut and it makes an angle of $48^{\circ}$ with the ground, find to the nearest foot how high the kite is.
4. The angle of elevation from a ship to the top of a 50 m lighthouse on the coast measures $13^{\circ}$. How far from the coast is the ship?
5. A ladder leaning against a wall. The foot of the ladder is 6.5 feet from the wall. The ladder makes an angle of $74^{\circ}$ with the level ground. How high, to the nearest foot, on the wall does the ladder reach?
6. Find to the nearest meter the height of a building
if its shadow is 67 m long when the angle of elevation of the sun contains $26^{\circ}$.
7. A 8-foot wire attached to the top of a tent pole reaches a stake in the ground 5 feet from the foot of the pole. Find to the nearest degree the measure of the angle made by the wire with the ground.
8. While flying a kite, Doris let out 250 feet of string. Assuming that the string is stretched taut and it makes an angle of $54^{\circ}$ with the ground, find to the nearest foot how high the kite is.
9. In rectangle ABCD , a diagonal AC is drawn. If $\mathrm{m} \angle \mathrm{BAC}=62^{\circ}$ and BC is 20 , find to the nearest integer the length of AB and AC .
10. The angle of elevation from a ship to the top of a 48 m lighthouse on the coast measures $21^{\circ}$. How far from the coast is the ship?
11. A kite is flying at the end of a 136 m string that is straight. The string makes an angle of $52^{\circ}$ with the ground. How high above the ground is the kite?
12. A ramp is 360 m long. It rises a vertical distance of 48 m . Fine the measure of its angle of elevation.

13. A 23 foot pole that is leaning against a wall reaches a point that is 17 feet above the ground. Find to the nearest degree the number of degrees contained in the angle that the pole makes with the ground.
14. To reach the top of a hill that is 3 kilometer high, one must travel 9 kilometers up a straight road that leads to the top. Find to the nearest degree the number of degrees contained in the angle that the road makes with the horizontal?
15. A point on the ground 47 m from the foot of a tree, the angle of elevation of the top of the tree contains $36^{\circ}$. Find the height of the tree to the nearest meter.
16. A ladder leaning against a wall. The foot of the ladder is 8.2 feet from the wall. The ladder makes an angle of $93^{\circ}$ with the level ground. How high, to the nearest foot, on the wall does the ladder reach?
17. A boy visiting New York City views the Empire State Building from a point on the ground, which is 865 feet from the foot of the building. The angle of elevation contains $51^{\circ}$. Find the height of the building to the nearest foot.
18. Find to the nearest meter the height of a building that cast a shadow of 12 m long when the angle of elevation of the sun contains $41^{\circ}$.
19. From an apartment window 24 m above the ground, the angle of depression of the base of a nearby building is $38^{\circ}$ and the angle of elevation of the top is $63^{\circ}$. Find the height of the nearby building (to the nearest meter).

20. From a lighthouse 1000 ft above sea level, the angle of depression to a boat (A) is $29^{\circ}$. A little bit later the boat has moved closer to the shore (B) and the angle of depression measures $44^{\circ}$. How far (to the nearest foot) has the boat moved in that time?

21. A flagpole is at the top of a building. 400 ft from the base of the building, the angle of elevation of the top of the pole is $22^{\circ}$ and the angle of elevation of the bottom of the pole is $20^{\circ}$. Determine the length of the flagpole (to the nearest foot).

22. Two trees are 100 m apart. From the exact middle between them, the angles of elevation of their tops are $12^{\circ}$ and $16^{\circ}$. How much taller is one tree than the other ( 2 decimal places)?

23. A firefighter on the ground sees the fire break through a window. The angle of elevation to the windowsill is $32^{\circ}$. The angle of elevation to the top of the building is $40^{\circ}$. If the firefighter is 72 ft from the building, what is the distance from the roof to the window sill?

24. Jack and Jill are on either side of the church and 50 m apart. Jack sees the top of the steeple at $40^{\circ}$ and Jill sees the top of the steeple at $32^{\circ}$. How high is the steeple?

25. Jack and Jill are 20 m apart. Jack sees the top of the building at $30^{\circ}$ and Jill sees the top of the building at $40^{\circ}$. What is the height of building?

26. A flagpole is at the top of a building. 300 ft from the base of the building, the angle of elevation of the top of the pole is $32^{\circ}$ and the angle of elevation of the bottom of the pole is $30^{\circ}$. Determine the length of the flagpole (to the nearest foot).


Do Now:

1) In the following triangle, $A B=1$.

Determine the lengths of, $A C$ and $B C$.

2) Write the equation for the $\sin (30)$ :
3) Write the equations for the $\cos (60)$ :

Let's try it again with another triangle!

1) In the following triangle, $A B=1$.

Determine the lengths of, $B C$ and $A C$.

2) Write the equation for the $\sin (45)$ :
3) Write the equations for the $\cos (45)$ :

## Co-Functions

Sine and Cosine are co-functions
Determine the value of the following (4 decimal places):

$$
\begin{array}{ll}
\sin (10)= & \cos (80)= \\
\sin (15)= & \cos (75)= \\
\sin (20)= & \cos (70)= \\
\sin (25)= & \cos (65)= \\
\sin (80)= & \cos (10)=
\end{array}
$$

Compare the values. Are there any values that are the same? If so, what do you notice about the relationship between the angle measures?

1) Solve the following:
a) $\sin 42^{\circ}=\cos$ $\qquad$ ${ }^{\circ}$
b) $\cos 12^{\circ}=\sin$ $\qquad$ ${ }^{\circ}$
c) $\sin 45^{\circ}=\cos$ $\qquad$ ${ }^{\circ}$
2) Solve for $x$ :
a) $\sin (x-5)=\cos (35)$
b) $\sin (2 x-17)=\cos (x-4)$
c) $\sin \left(\frac{3}{4} x\right)=\cos \left(\frac{1}{4} x\right)$
3) If $\sin A=2 / 3$, then $\cos A$ is what?
4) If $\sin (6 A)=\cos (9 A)$, then the measure of $<A$ is what?
5) If $\cos (2 x-1)=\sin (3 x+6)$, then what is the value of $x$ ?

Practice

1) Solve the following:
d) $\cos 0^{\circ}=\sin$ $\qquad$ ${ }^{\circ}$
e) $\cos 65^{\circ}=\sin$ $\qquad$ $\circ$
f) $\sin 78.5^{\circ}=\cos$ $\qquad$ ${ }^{\circ}$
2) Solve for $x$ :
d) $\sin (x)=\cos (x)$
e) $\sin (5 x-22)=\cos (x-10)$
f) $\sin \left(\frac{3}{4} x-3\right)=\cos (66)$

Special Right Triangles
Intro

1) Find the missing angle of the following triangles:

2) Find the missing side of the following triangles:
(hint: what kind of triangles are given?)
a)

b)


2 Types of Special Right Triangles

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Multiplying and Diving Radicals

| P\| |  |
| :--- | :--- |

Take it a Step Further


## Do Now

Three triangles are given below. Determine the areas for each triangle, if possible. If it is not possible to find the area with the provided information, describe what is needed in order to determine the area.


## Finding the Area of a Triangle without a Given Height

To find the area of a triangle when you are not given the height, you must:
1)
2)


## Examples/Practice

1. Find the area of the accompanying triangle. Round to the nearest tenth.

12

2. Determine the area of the accompanying triangle. Round your answer to the nearest hundredth.

3. Find the area of the accompanying triangle. Round your answer to the nearest tenth.

4. A landscape designer is designing a flower garden for a triangular area that is bounded on two sides by the client's house and driveway. The length of the edges of the garden along the house and driveway are 18 ft . and 8 ft ., respectively, and the edges come together at an angle of $80^{\circ}$. Draw a diagram, and then find the area of the garden to the nearest square foot.
5. In $\triangle A B C, \mathrm{AB}=15, \mathrm{BC}=20$, and $m \angle B=63^{\circ}$. Determine the area of the triangle. Round to the nearest tenth.

## Take it a step further...

6. An angle of a parallelogram measures $100^{\circ}$. The lengths of its sides are 8 and 18 . Determine the area of the parallelogram. Round your answer to the nearest hundredth.


## Homework

1. Given the triangle at the right, find its area. Express the area to the nearest thousandth.

2. Given the parallelogram at the right, find its EXACT area. Round your answer to the nearest hundredth

3. In an isosceles $\Delta$, the two equal sides each measure 8 meters, and they include an angle of $27^{\circ}$. Find the area of the isosceles triangle, to the nearest square meter.
4. In $\triangle P Q R, P Q=12, P R=3$, and $\mathrm{m}<\mathrm{P}=78^{\circ}$. Find the area of $\triangle \mathrm{PQR}$, to the nearest tenth of a square unit.
5. Find the area of the triangle. Round your answer to the nearest tenth


## Do Now



Law of Sines


## Examples

1. Find the value of $x$, to the nearest hundredth.
a.

b.

2. Given $\triangle A B C$, find $m \angle B$.

3. Given $\triangle D E F$, find the lengths of sides $e$ and $f$ to the nearest hundredth.

4. Find the lengths of the missing sides of $\Delta R S T$ if $m<R=40^{\circ}, m<S=55^{\circ}$ and $r=6$. Round your answers to the nearest hundredth.
5. In triangle $A B C, \sin A=0.8, \sin B=0.3$, and $a=24$. Find the length of side $b$.

Directions: Solve for $x$. Round to the nearest tenth
6.

7.

8.

10.

9.

11.

12. Cathy wants to determine the height of the flagpole shown in the diagram below. She uses a survey instrument to measure the angle of elevation to the top of the flagpole, and determines it to be $34.9^{\circ}$. She walks 8 meters closer and determines the new measure of the angle of elevation to be $52.8^{\circ}$. At each measurement, the survey instrument is 1.7 meters above the ground.


Determine and state, to the nearest tenth of a meter, the height of the flagpole.

## Do Now

The bus drops you off at the corner of H Street and $1^{\text {st }}$ Street, approximately $\mathbf{3 0 0} \mathbf{f t}$. from school. You plan to walk to your friend Janette's house after school to work on a project. Aproximately how many feet will you have to walk from school to Janette's house? Round your answer to the nearest foot.


## Classwork/Notes

1. Joanna borrowed some tools from a friend so that she could precisely, but not exactly, measure the corner space in her backyard to plant some vegetables. She wants to build a fence to prevent her dog from digging up the seeds that she plants. Joanna returned the tools to her friend before making the most important measurement: the one that would give the length of the fence! See the diagram below to help you with this question.
a. Joanna decided that she could just use the Pythagorean theorem to find the length of the fence she would need. Is the Pythagorean theorem applicable in this situation? Explain.
b. Use another method to solve for the length of the fence to the nearest foot.

2. The measurements of the triangle given are rounded to the
nearest hundredth.
Calculate the missing side length to the nearest hundredth.

3. Given triangle $D E F$, find $\boldsymbol{D E}$ to the nearest hundredth.

4. Find the length of $C B$ to the nearest tenth.

5. Find the length of $C B$ to the nearest hundredth.


Homework
6. Find the length of $C A$ to the nearest thousandth.

7. Find the length of $C B$ to the nearest tenth.

8. Find the length of $A C$ to the nearest tenth.

9. Find the length of $C B$ to the nearest tenth.


