

Skills, Practice, and Problem-Solving Applications

- Geometry
- Ratio and Proportional Relationships
- The Number System
- Expressions and Equations
- Statistics and Probability



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## Introduction to the Teacher

The time has come to raise the rigor in our children's mathematical education. The Common Core State Standards were developed to help guide educators and parents on how to do this by outlining what students are expected to learn throughout each grade level. The bar has been set high, but our students are up to the challenge.

This worktext is designed to help teachers and parents meet the challenges set forth by the Common Core State Standards. It is filled with skills practice and problem-solving practice exercises that correspond to each standard for mathematics. With a little time each day, your students will become better problem solvers and will acquire the skills they need to meet the mathematical expectations for their grade level.

Each page contains two "workouts." The first workout is a skills practice exercise, and the second is geared toward applying that skill to solve a problem. These workouts make great warmup or assessment exercises. They can be used to set the stage and teach the content covered by the standards. They can also be used to assess what students have learned after the content has been taught.

We hope that this book will help you help your students build their Common Core Math strength and become great problem solvers!

Karise Mace and Keegen Gennuso


Name:
Date:

## GEOMETRY - Scale Drawings

CCSS Math Content 7.G.A.1: Solve problems involving scale drawings of geometric figures, including computing actual lengths and areas from a scale drawing and reproducing a scale drawing at a different scale.

## SHARPEN YOUR SKILLS:

A scale drawing of Shen's backyard is shown. Each centimeter in the drawing represents 8 feet. What is the actual area of Shen's backyard? Show your work.
$10 \frac{1}{2} \mathrm{~cm}$


## APPLY YOUR SKILLS:

On your own paper, create a new scale drawing of Shen's backyard where $\frac{1}{2}$ inch represents 7 feet. What should the length and width of the scale drawing of the backyard be? Show your work.

Name:
Date: $\qquad$

## RATIOS AND PROPORTIONAL RELATIONSHIPS Constant of Proportionality

CCSS Math Content 7.RP.A.2b: Identify the constant of proportionality (unit rate) in tables, graphs, equations, diagrams, and verbal descriptions of proportional relationships.

## SHARPEN YOUR SKILLS:

1. Identify the constant of proportionality for the quantities given in the table. Explain how you determined your answer.

| $x$ | 2 | 3 | 6 | 10 | 14 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| $y$ | 16 | 24 | 48 | 80 | 112 |

$\qquad$
$\qquad$
$\qquad$
2. Identify the constant of proportionality for the quantities given in the graph. Explain how you determined your answer.


## APPLY YOUR SKILLS:



Use the graph to determine the amount Maya charges to babysit for one hour. Explain how you determined your answer.

Name:
Date: $\qquad$

## RATIOS AND PROPORTIONAL RELATIONSHIPS Constant of Proportionality

CCSS Math Content 7.RP.A.2b: Identify the constant of proportionality (unit rate) in tables, graphs, equations, diagrams, and verbal descriptions of proportional relationships.

SHARPEN YOUR SKILLS:

Identify the constant of proportionality in the given equation.

1. $y=2 x$
2. $y=\frac{5}{3} x$
3. A 5 -pound bag of apples costs $\$ 4.80$. What is the price for one pound of apples? Show your work.

4. A crayon factory can make about 35 million crayons in 7 days. How many crayons can the factory make in one day? Show your work.
$\qquad$

## APPLY YOUR SKILLS:

A $2 \frac{1}{2}$-pound bag of white grapes costs $\$ 4.70$. A $3 \frac{1}{4}$-pound bag of red grapes costs $\$ 5.98$. Which bag of grapes is a better deal? Explain how you determined your answer.

Name:
Date: $\qquad$

## RATIOS AND PROPORTIONAL RELATIONSHIPS Proportional Relationships

CCSS Math Content 7.RP.A.2c: Represent proportional relationships by equations.

## SHARPEN YOUR SKILLS:

Jody is observing fireflies. He catches one and places it in a jar. Then he counts the number of times it flashes in one minute and two minutes. Once he has recorded his observations, Jody releases the firefly, catches another, and counts the number of times it flashes in one and two minutes. He continues this process until he has observed 6 different fireflies. The tables show the relationship between time and the number of flashes for each of Jody's fireflies.
Table 1

| Firefly | A | B | C | D | E | F |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| Time (minutes) | 1 | 1 | 1 | 1 | 1 | 1 |
| Number of flashes | 15 | 13 | 18 | 19 | 12 | 14 |

Table 2

| Firefly | A | B | C | D | E | F |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Time (minutes) | 2 | 2 | 2 | 2 | 2 | 2 |
| Number of flashes | 28 | 26 | 32 | 30 | 25 | 29 |



1. Write an equation that represents the relationship between time, $t$, and the number of flashes, $f$, for each of the fireflies. Use the data from Table 1.
2. Write an equation that represents the relationship between time, $t$, and the number of flashes, $f$, for each of the fireflies. Use the data from Table 2.

## APPLY YOUR SKILLS:

A recipe for granola calls for 2 cups of raisins and 3 cups of sunflower seeds. Mr. Stahler asks his students to write an equation that represents the relationship between raisins and sunflower seeds. Two students' equations are shown below. Do these equations represent the same relationship? Explain how you determined your answer.

$$
\text { Student 1: } s=\frac{3}{2} r \quad \text { Student 2: } r=\frac{2}{3} s
$$

Name: $\qquad$ Date:

## EXPRESSIONS AND EQUATIONS - <br> Manipulating Linear Expressions

CCSS Math Content 7.EE.A.1: Apply properties of operations as strategies to add, subtract, factor, and expand linear expressions with rational coefficients.

## SHARPEN YOUR SKILLS:

1. Factor the expression $\frac{5}{24} x+\frac{10}{36}$ completely. $\qquad$
2. Expand the expression $\frac{4}{9}\left(\frac{2}{5} b-\frac{3}{8}\right)$.
3. Factor the expression $\frac{6}{45}-\frac{8}{63} y$ completely. $\qquad$
4. Expand the expression $-\frac{2}{3}\left(\frac{8}{9}-\frac{2}{5} a\right)$.

## APPLY YOUR SKILLS:

Is there more than one way to factor the expression $\frac{24}{32} a+\frac{48}{56}$ ? Support your answer with mathematics.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

## Answer Keys

## GEOMETRY

## Scale Drawings（pg．1）

## SHARPEN YOUR SKILLS：

## Length of Shen＇s Backyard：

$8 \mathrm{ft} / \mathrm{cm} \times 10 \frac{1}{2} \mathrm{~cm}=\frac{8 \mathrm{ft}}{1 \mathrm{cmt}} \times \frac{21 \mathrm{smT}}{2}=\frac{168 \mathrm{ft}}{2}=84 \mathrm{ft}$ Width of Shen＇s Backyard：
$8 \mathrm{ft} / \mathrm{cm} \times 8 \frac{3}{4} \mathrm{~cm}=\frac{8 \mathrm{ft}}{1 \mathrm{~cm}} \times \frac{35 \mathrm{smt}}{4}=\frac{280 \mathrm{ft}}{4}=70 \mathrm{ft}$
Actual Area of Shen＇s Backyard：
$A=1 \times w \quad 84 \mathrm{ft} \times 70 \mathrm{ft}=5,880 \mathrm{ft}^{2}$
The actual area of Shen＇s backyard is 5,880 square feet．

## APPLY YOUR SKILLS：

Length of Scale Drawing of Shen＇s Backyard：
$\frac{\frac{1}{2} \mathrm{in} \text { ．}}{7 \text { 并 }} \times \frac{84 \text { \＃}}{1}=\frac{42 \mathrm{in} \text { ．}}{7}=6 \mathrm{in}$ ．
Width of Scale Drawing of Shen＇s Backyard：
$\frac{\frac{1}{2} \mathrm{in} .}{7 \text { 开 }} \times \frac{70 \text { 羊 }}{1}=\frac{35 \mathrm{in} \text { ．}}{7}=5 \mathrm{in}$ ．
The scale drawing should be 6 inches by 5 inches．

## Drawing and Constructing Geometric Shapes（pg．2） SHARPEN YOUR SKILLS：

The triangles that students draw will vary because they may choose differ－ ent side lengths．However，all of the triangles should have one angle that measures $21^{\circ}$ ，one that measures $42^{\circ}$ ，
 and one that measures $117^{\circ}$ ．

## APPLY YOUR SKILLS：

1．This statement is never true．If given three angles whose sum is $180^{\circ}$ ，you can draw many different tri－ angles，as the size of the angle has no affect on the length of the sides．For example，the triangles below have angles with the same measures，but their sides are different lengths．


2．This statement is always true．If given three angles whose sum is $180^{\circ}$ ，you can draw many different tri－ angles，as the size of the angle has no affect on the length of the sides．For example，the triangles below have angles with the same measures，but their sides are different lengths．


## About the Authors

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