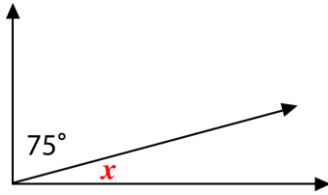


Angles Vocabulary

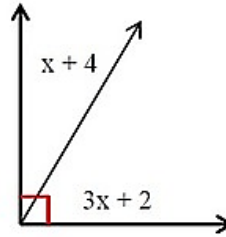
Congruent angles – two or more angles with the same measure.

Complementary Angles- two angles whose sum is 90° .

Ex.1

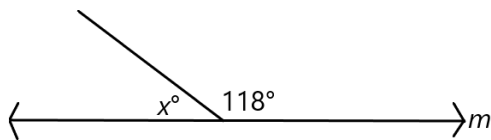


Ex.2

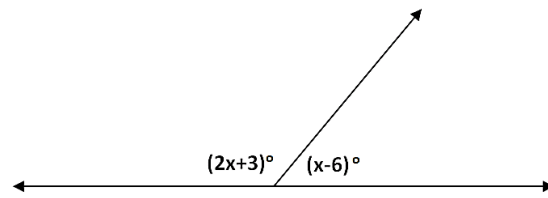


Supplementary Angles – two angles whose sum is 180° .

Ex.3

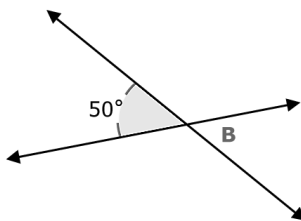


Ex.4

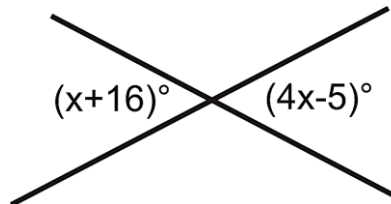


Vertical angle – Two angles that share a common vertex and their sides form two pairs of opposite rays. Vertical angles are **congruent**.

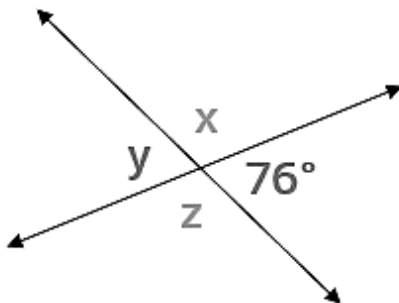
Ex.5



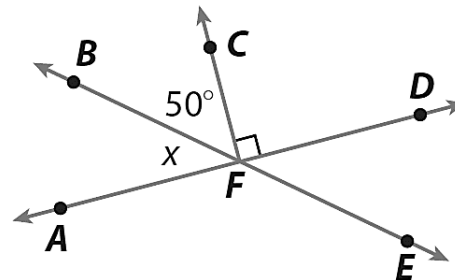
Ex.6



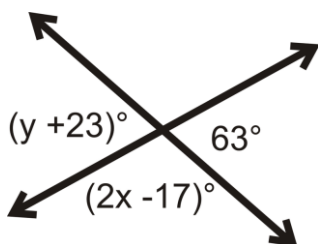
Ex.7



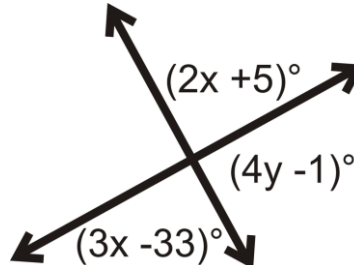
Ex.8



Ex.9

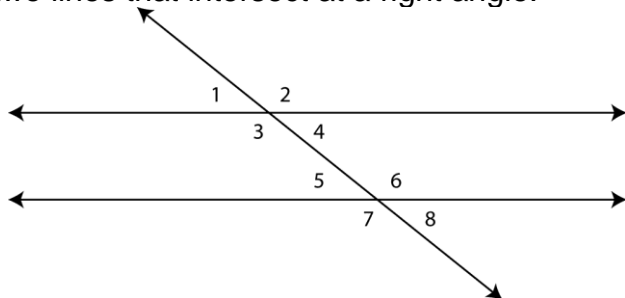


Ex.10



Transversal Notes

- A transversal is a line that intersects a system of two or more lines at different points.
- Two lines are parallel if they do not intersect.
- Perpendicular lines are two lines that intersect at a right angle.



Corresponding Angles Postulate:

If two parallel lines are cut by a transversal, then the pairs of corresponding angles are congruent.

$$\begin{matrix} \angle _ = \angle _ & \angle _ = \angle _ \\ \angle _ = \angle _ & \angle _ = \angle _ \end{matrix}$$

Alternate Exterior Angles Theorem:

If two parallel lines are cut by a transversal, then the pairs of alternate exterior angles are congruent.

$$\begin{matrix} \angle _ = \angle _ \\ \angle _ = \angle _ \end{matrix}$$

Alternate Interior Angles Theorem:

If two parallel lines are cut by a transversal, then the pairs of alternate interior angles are congruent.

$$\begin{matrix} \angle _ = \angle _ \\ \angle _ = \angle _ \end{matrix}$$

Consecutive Exterior Angles Theorem: (Same Side Exterior Angles)

If two parallel lines are cut by a transversal, then the pairs of consecutive exterior angles are supplementary.

$$\begin{matrix} \angle _ + \angle _ = _ \\ \angle _ + \angle _ = _ \end{matrix}$$

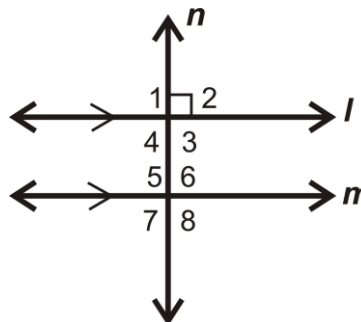
Consecutive Interior Angles Theorem: (Same Side Interior Angles)

If two parallel lines are cut by a transversal, then the pairs of consecutive interior angles are supplementary.

$$\begin{matrix} \angle _ + \angle _ = _ \\ \angle _ + \angle _ = _ \end{matrix}$$

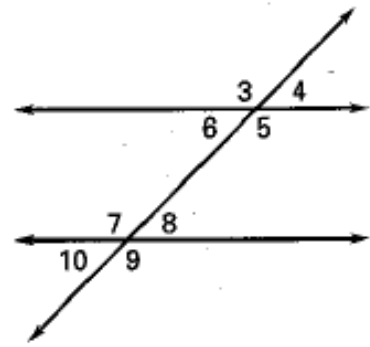
Perpendicular Transversal Theorem:

If a transversal is perpendicular to one of the two parallel lines, then it is perpendicular to the other.

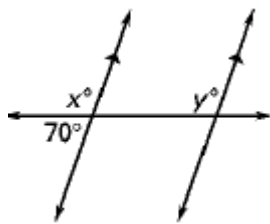


Ex.1 Identify the angles as corresponding, alternate interior, alternate exterior, consecutive interior, or consecutive exterior.

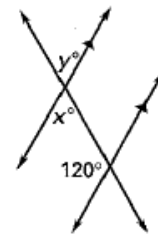
1. $\angle 3$ and $\angle 7$ _____
2. $\angle 4$ and $\angle 10$ _____
3. $\angle 5$ and $\angle 8$ _____
4. $\angle 8$ and $\angle 6$ _____
5. $\angle 9$ and $\angle 5$ _____
6. $\angle 5$ and $\angle 7$ _____



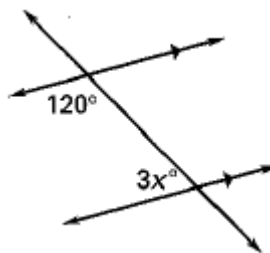
Ex.2



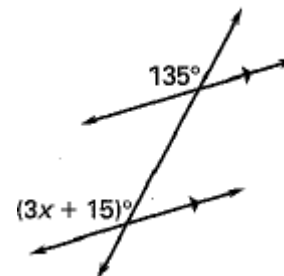
Ex.3



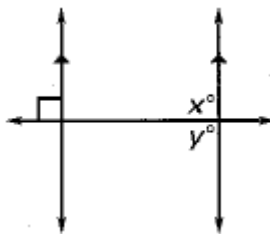
Ex.4



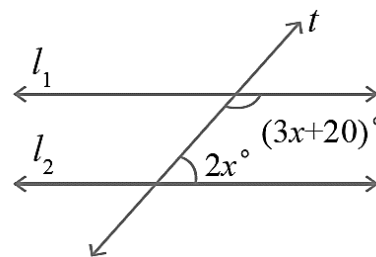
Ex.5



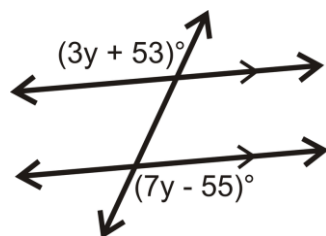
Ex.6



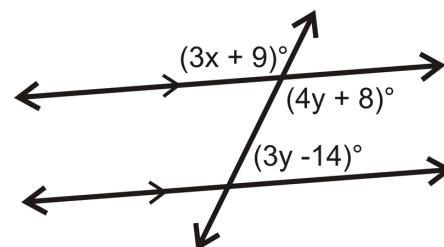
Ex.7



Ex.8



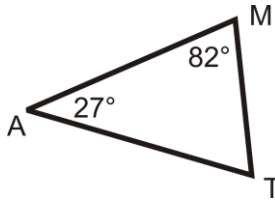
Ex.9



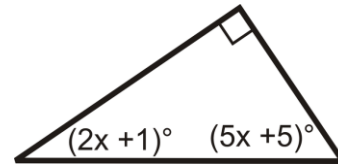
Triangle Notes

- **Triangle Sum Theorem**- the sum of the angle measures of a triangle is 180 degrees.
- A scalene triangle has no congruent sides.

Ex.1

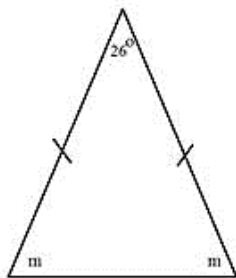


Ex.2

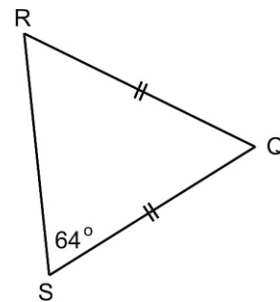


- An isosceles triangle has two congruent angles and two congruent sides.

Ex.3

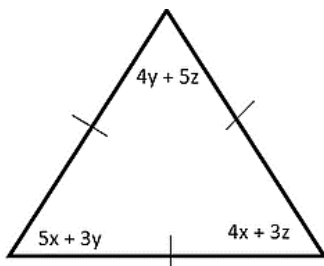


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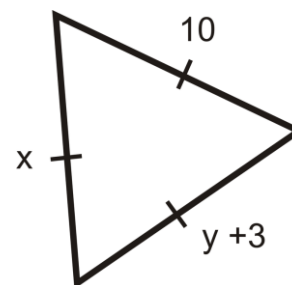


- An equilateral triangle has three congruent sides.
- An equiangular triangle has three congruent angles.
- If a triangle is equilateral then it is also equiangular and vice versa.

Ex.5

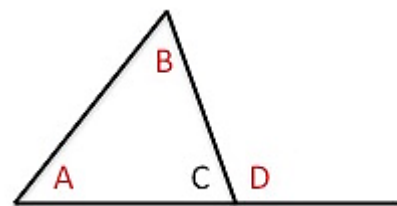


Ex.6

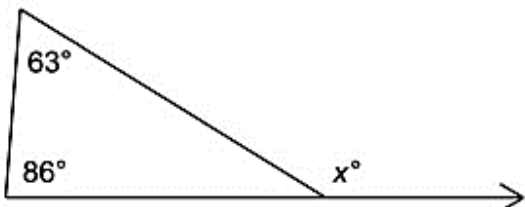


- **Exterior Angle Theorem** - the measure of an exterior angle of a triangle is equal to the sum of the measures of its remote interior angles.

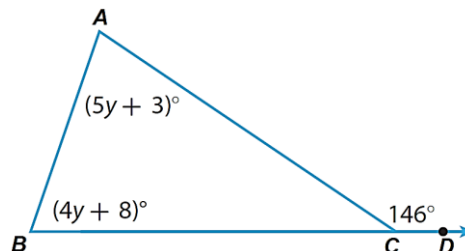
$$\angle A + \angle B = \angle D$$

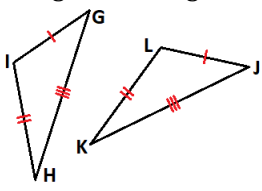
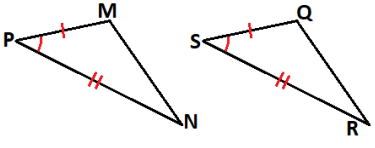
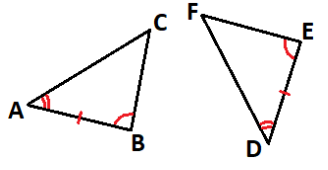
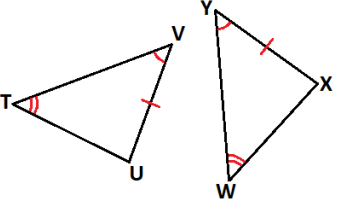
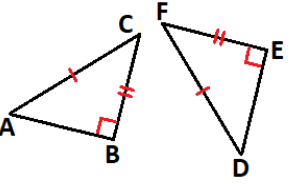


Ex.7

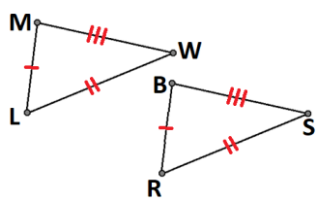
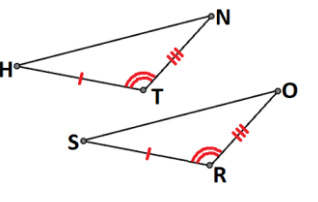
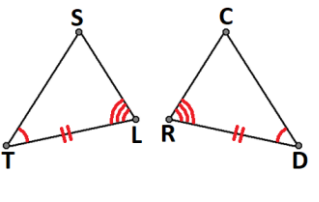
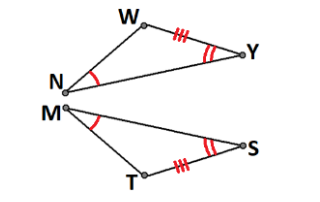
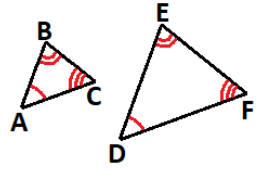
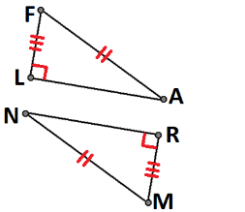
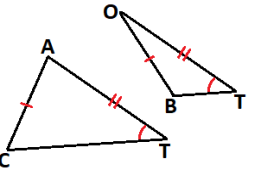
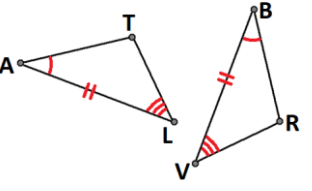


Ex.8

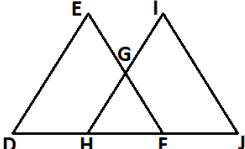
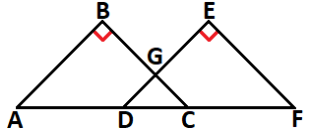
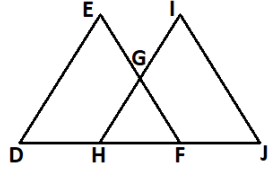


<p>Side-Side-Side</p> <p>If three corresponding sides are congruent in two triangles, then the triangles are congruent.</p>  <p>$\triangle GIH \cong \triangle$ _____ by _____</p>	<p>Side-Angle-Side</p> <p>If two corresponding sides and their included angle are congruent in two triangles, then the triangles are congruent.</p>  <p>$\triangle MPN \cong \triangle$ _____ by _____</p>	<p>Angle-Side-Angle</p> <p>If two corresponding angles and their included side are congruent in two different triangles, then the triangles are congruent.</p>  <p>$\triangle ABC \cong \triangle$ _____ by _____.</p>
<p>Angle-Angle-Side</p> <p>If two corresponding angles and their non-included side are congruent in two different triangles, then the triangles are congruent.</p>  <p>$\triangle TUV \cong \triangle$ _____ by _____.</p>	<p>Hypotenuse-Leg</p> <p>If two corresponding hypotenuses and legs are congruent in two right triangles, then the right triangles are congruent.</p>  <p>$\triangle ABC \cong \triangle$ _____ by _____.</p>	

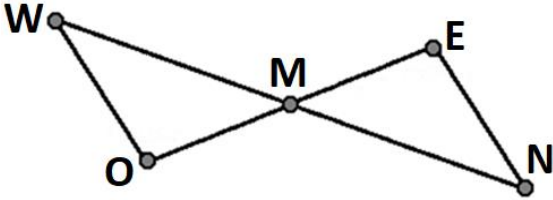
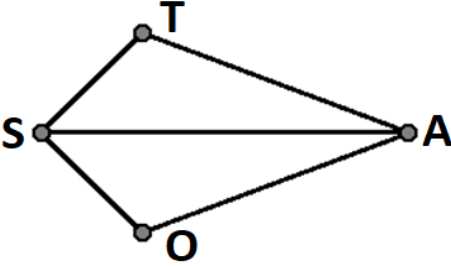
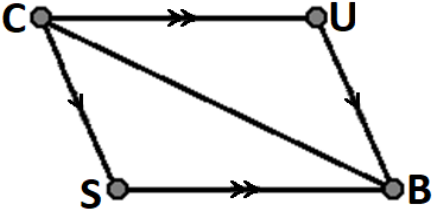
Complete the congruence statement and write the criteria (SSS, SAS, ASA, AAS, HL) for the congruent triangles.

<p>1.</p>  <p>$\triangle MLW \cong \triangle$ _____ by _____</p>	<p>2.</p>  <p>$\triangle HTN \cong \triangle$ _____ by _____</p>	<p>3.</p>  <p>$\triangle STL \cong \triangle$ _____ by _____</p>	<p>4.</p>  <p>$\triangle NWY \cong \triangle$ _____ by _____</p>
<p>5.</p>  <p>$\triangle ABC$ is not congruent to \triangle _____</p>	<p>6.</p>  <p>$\triangle FLA \cong \triangle$ _____ by _____</p>	<p>7.</p>  <p>$\triangle ACT$ is not congruent to \triangle _____</p>	<p>8.</p>  <p>$\triangle ATL \cong \triangle$ _____ by _____</p>

Name the additional information that is sufficient to prove that the triangles are congruent by the given criteria.

<p>9. $\triangle DEF \cong \triangle JIH$ by SSS $DE \cong JI, EF \cong IH, ?$</p>  <p>Additional information: _____ \cong _____</p>	<p>10. $\triangle ABC \cong \triangle FED$ by SAS $BC \cong ED, \angle B \cong \angle E, ?$</p>  <p>Additional information: _____ \cong _____</p>	<p>11. $\triangle DEF \cong \triangle JIH$ by ASA $\angle D \cong \angle J, DE \cong JI, ?$</p>  <p>Additional information: _____ \cong _____</p>
--	---	---

- **Reflexive property:** any quantity is equal to itself.
- **Midpoint:** a point that divides a segment into two congruent segments.
- **Bisect:** divide into two equal parts
- If two or more triangles are proven congruent, then all of their corresponding parts are congruent.
- **CPCTC:** corresponding parts of corresponding triangles are congruent

<p>Ex.1 Prove: ΔWMO and ΔNME congruent</p> <p>Given: M is the midpoint of \overline{WN}, M is the midpoint of \overline{OE}, $\angle W \cong \angle N$</p> 	<table border="1"> <thead> <tr> <th>Statement</th> <th>Reason</th> </tr> </thead> <tbody> <tr><td> </td><td> </td></tr> <tr><td> </td><td> </td></tr> <tr><td> </td><td> </td></tr> <tr><td> </td><td> </td></tr> <tr><td> </td><td> </td></tr> <tr><td> </td><td> </td></tr> <tr><td> </td><td> </td></tr> <tr> <td>$\Delta WMO \cong \Delta$ _____</td> <td> </td> </tr> <tr style="background-color: #cccccc;"> <td colspan="2"> </td> </tr> </tbody> </table>	Statement	Reason															$\Delta WMO \cong \Delta$ _____					
Statement	Reason																						
$\Delta WMO \cong \Delta$ _____																							
<p>Ex.2 Prove: ΔTSA and ΔOSA congruent</p> <p>Given: \overline{SA} is the angle bisector of $\angle TSO$, \overline{AS} is the angle bisector of $\angle TAO$</p> 	<table border="1"> <thead> <tr> <th>Statement</th> <th>Reason</th> </tr> </thead> <tbody> <tr><td> </td><td> </td></tr> <tr><td> </td><td> </td></tr> <tr><td> </td><td> </td></tr> <tr><td> </td><td> </td></tr> <tr><td> </td><td> </td></tr> <tr><td> </td><td> </td></tr> <tr><td> </td><td> </td></tr> <tr> <td>$\Delta TSA \cong \Delta$ _____</td> <td> </td> </tr> <tr style="background-color: #cccccc;"> <td colspan="2"> </td> </tr> </tbody> </table>	Statement	Reason															$\Delta TSA \cong \Delta$ _____					
Statement	Reason																						
$\Delta TSA \cong \Delta$ _____																							
<p>Ex.3 Prove $\overline{CS} \cong \overline{BU}$</p> <p>Given: \overline{CU} is parallel to \overline{SB}, \overline{CS} is parallel to \overline{UB}</p> 	<table border="1"> <thead> <tr> <th>Statement</th> <th>Reason</th> </tr> </thead> <tbody> <tr><td> </td><td> </td></tr> <tr><td> </td><td> </td></tr> <tr><td> </td><td> </td></tr> <tr><td> </td><td> </td></tr> <tr><td> </td><td> </td></tr> <tr><td> </td><td> </td></tr> <tr><td> </td><td> </td></tr> <tr> <td>$\Delta CUB \cong \Delta$ _____</td> <td> </td> </tr> <tr> <td>$CS \cong BU$</td> <td> </td> </tr> <tr style="background-color: #cccccc;"> <td colspan="2"> </td> </tr> </tbody> </table>	Statement	Reason															$\Delta CUB \cong \Delta$ _____		$CS \cong BU$			
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