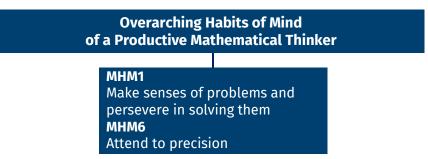


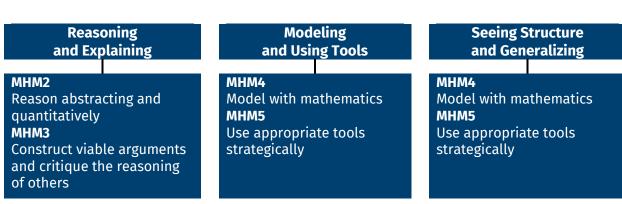
High School Algebra I

Overview of the West Virginia College- and Career-Readiness Standards for Mathematics

Included in Policy 2520.2B, the West Virginia College- and Career-Readiness Standards for Mathematics are two types of standards: the Mathematical Habits of Mind and the grade-level Mathematics Content Standards. These standards address the skills, knowledge, and dispositions that students should develop to foster mathematical understanding and expertise, as well as concepts, skills, and knowledge – what students need to understand, know, and be able to do. The standards also require that the Mathematical Habits of Mind and the grade-level Mathematics Content Standards be connected. These connections are essential to support the development of students' broader mathematical understanding, as students who lack understanding of a topic may rely too heavily on procedures. The Mathematical Habits of Mind must be taught as carefully and practiced as intentionally as the grade-level Mathematics Content Standards are. Neither type should be isolated from the other; mathematics instruction is most effective when these two aspects of the West Virginia College- and Career-Readiness Standards for Mathematics come together as a powerful whole.

Mathematical Habits of Mind





The eight Mathematical Habits of Mind (MHM) describe the attributes of mathematically proficient students and the expertise that mathematics educators at all levels should seek to develop in their students. The Mathematical Habits of Mind provide a vehicle through which students engage with and learn mathematics. As students move from elementary school through high school, the Mathematical Habits of Mind are integrated in the tasks as students engage in doing mathematics and master new and more advanced mathematical ideas and understandings.

The Mathematical Habits of Mind rest on important "processes and proficiencies" with longstanding importance in mathematics education. The first of these are the National Council of Teachers of Mathematics' process standards of problem solving, reasoning and proof, communication, representation, and connections. The second are the strands of mathematical proficiency specified in the National Research Council's report Adding it Up: adaptive reasoning, strategic competence, conceptual understanding, procedural fluency, and productive disposition (NGA/CCSSO 2010).

Ideally, several Mathematical Habits of Mind will be evident in each lesson as they interact and overlap with each other. The Mathematical Habits of Mind are not a checklist; they are the basis for mathematics instruction and learning. To help students persevere in solving problems (MHM1), teachers need to allow their students to struggle productively, and they must be attentive to the type of feedback they provide to students. Dr. Carol Dweck's research (Dweck 2006) revealed that feedback offering praise of effort and perseverance seems to engender a "growth mindset." In Dweck's estimation, growth-minded teachers tell students the truth about being able to close the learning gap between them and their peers and then give them the tools to close the gap (Dweck 2006).

Students who are proficient in the eight Mathematical Habits of Mind are able to use these skills not only in mathematics, but across disciplines and into their lives beyond school, college, and career.

Policy 2520.2B West Virginia College- and Career-Readiness Standards for Mathematics

Mathematical Habits of Mind

The Mathematical Habits of Mind (hereinafter MHM) describe varieties of expertise that mathematics educators at all levels should develop in their students.

MHM1. Make sense of problems and persevere in solving them.

Mathematically proficient students start by explaining to themselves the meaning of a problem and looking for entry points to its solution. They analyze givens, constraints, relationships and goals. They make conjectures about the form and meaning of the solution and plan a solution pathway rather than simply jumping into a solution attempt. They consider analogous problems and try special cases and simpler forms of the original problem in order to gain insight into its solution. They monitor and evaluate their progress and change course if necessary. Older students might, depending on the context of the problem, transform algebraic expressions or change the viewing window on their graphing calculator to get the information they need. Mathematically proficient students can explain correspondences between equations, verbal descriptions, tables and graphs or draw diagrams of important features and relationships, graph data and search for regularity or trends. Younger students might rely on using concrete objects or pictures to help conceptualize and solve a problem. Mathematically proficient students check their answers to problems using a different method and they continually ask themselves, "Does this make sense?" They can understand the approaches of others to solving complex problems and identify correspondences between different approaches.

MHM2. Reason abstractly and quantitatively.

Mathematically proficient students make sense of quantities and their relationships in problem situations. They bring two complementary abilities to bear on problems involving quantitative relationships: the ability to decontextualize—to abstract a given situation and represent it symbolically and manipulate the representing symbols as if they have a life of their own, without necessarily attending to their referents—and the ability to contextualize—to pause as needed during the manipulation process in order to probe into the referents for the symbols involved. Quantitative reasoning entails habits of creating a coherent representation of the problem at hand, considering the units involved, attending to the meaning of quantities, not just how to compute them, and knowing and flexibly using different properties of operations and objects.

MHM3. Construct viable arguments and critique the reasoning of others.

Mathematically proficient students understand and use stated assumptions, definitions, and previously established results in constructing arguments. They make conjectures and build a logical progression of statements to explore the truth of their conjectures. They are able to analyze situations by breaking them into cases and can recognize and use counterexamples.

They justify their conclusions, communicate them to others, and respond to the arguments of others. They reason inductively about data, making plausible arguments that take into account the context from which the data arose. Mathematically proficient students are also able to compare the effectiveness of two plausible arguments, distinguish correct logic or reasoning from that which is flawed, and—if there is a flaw in an argument—explain what it is. Elementary students can construct arguments using concrete referents such as objects, drawings, diagrams and actions. Such arguments can make sense and be correct, even though they are not generalized or made formal until later grades. Later, students learn to determine domains to which an argument applies. Students at all grades can listen or read the arguments of others, decide whether they make sense and ask useful questions to clarify or improve the arguments.

MHM4. Model with mathematics.

Mathematically proficient students can apply the mathematics they know to solve problems arising in everyday life, society and the workplace. In early grades, this might be as simple as writing an addition equation to describe a situation. In middle grades, a student might apply proportional reasoning to plan a school event or analyze a problem in the community. By high school, a student might use geometry to solve a design problem or use a function to describe how one quantity of interest depends on another. Mathematically proficient students who can apply what they know are comfortable making assumptions and approximations to simplify a complicated situation, realizing that these may need revision later. They are able to identify important quantities in a practical situation and map their relationships using such tools as diagrams, two-way tables, graphs, flowcharts and formulas. They can analyze those relationships mathematically to draw conclusions. They routinely interpret their mathematical results in the context of the situation and reflect on whether the results make sense, possibly improving the model if it has not served its purpose.

MHM5. Use appropriate tools strategically.

Mathematically proficient students consider the available tools when solving a mathematical problem. These tools might include pencil and paper, concrete models, a ruler, a protractor, a calculator, a spreadsheet, a computer algebra system, a statistical package or dynamic geometry software. Proficient students are sufficiently familiar with tools appropriate for their grade or course to make sound decisions about when each of these tools might be helpful, recognizing both the insight to be gained and their limitations. For example, mathematically proficient high school students analyze graphs of functions and solutions generated using a graphing calculator. They detect possible errors by strategically using estimation and other mathematical knowledge. When making mathematical models, they know that technology can enable them to visualize the results of varying assumptions, explore consequences and compare predictions with data. Mathematically proficient students at various grade levels are able to identify relevant external mathematical resources, such as digital content located on a website and use them to pose or solve problems. They are able to use technological tools to explore and deepen their understanding of concepts.

MHM6. Attend to precision.

Mathematically proficient students try to communicate precisely to others. They try to use clear definitions in discussion with others and in their own reasoning. They state the meaning of the symbols they choose, including using the equal sign consistently and appropriately. They are careful about specifying units of measure, and labeling axes to clarify the correspondence with quantities in a problem. They calculate accurately and efficiently, express numerical answers with a degree of precision appropriate for the problem context. In the elementary grades, students give carefully formulated explanations to each other. By the time they reach high school they have learned to examine claims and make explicit use of definitions.

MHM7. Look for and make use of structure.

Mathematically proficient students look closely to discern a pattern or structure. Young students, for example, might notice that three and seven more is the same amount as seven and three more or they may sort a collection of shapes according to how many sides the shapes have. Later, students will see 7×8 equals the well-remembered $7 \times 5 + 7 \times 3$, in preparation for learning about the distributive property. In the expression $x^2 + 9x + 14$, older students can see the 14 as 2×7 and the 9 as 2 + 7. They recognize the significance of an existing line in a geometric figure and can use the strategy of drawing an auxiliary line for solving problems. They also can step back for an overview and shift perspective. They can see complicated things, such as some algebraic expressions, as single objects or as being composed of several objects. For example, they can see $5 - 3(x - y)^2$ as 5×6 minus a positive number times a square and use that to realize that its value cannot be more than 6×6 for any real numbers 6×6 and 6×6 minus a positive numbers 6×6 minus and 6×6 minus a positive number 6×6 minus and 6×6 minus and 6×6 minus and 6×6 minus a positive number 6×6 minus and 6×6 minus and

MHM8. Look for and express regularity in repeated reasoning.

Mathematically proficient students notice if calculations are repeated, and look both for general methods and for shortcuts. Upper elementary students might notice when dividing 25 by 11 that they are repeating the same calculations over and over again, and conclude they have a repeating decimal. By paying attention to the calculation of slope as they repeatedly check whether points are on the line through (1, 2) with slope 3, middle school students might abstract the equation (y-2)/(x-1)=3. Noticing the regularity in the way terms cancel when expanding (x-1)(x+1), $(x-1)(x^2+x+1)$ and $(x-1)(x^3+x^2+x+1)$ might lead them to the general formula for the sum of a geometric series. As they work to solve a problem, mathematically proficient students maintain oversight of the process, while attending to the details. They continually evaluate the reasonableness of their intermediate results.

Policy 2520.2B West Virginia College- and Career-Readiness Standards for Mathematics

Mathematics - High School Algebra I

All West Virginia teachers are responsible for classroom instruction that integrates content standards and mathematical habits of mind. Students in this course will focus on five critical units that deepen and extend understanding of linear and exponential relationships by contrasting them with each other and by applying linear models to data that exhibit a linear trend, and students engage in methods for analyzing, solving, and using quadratic functions. Mathematical habits of mind, which should be integrated in these content areas, include: making sense of problems and persevering in solving them, reasoning abstractly and quantitatively; constructing viable arguments and critiquing the reasoning of others; modeling with mathematics; using appropriate tools strategically; attending to precision, looking for and making use of structure; and looking for and expressing regularity in repeated reasoning. Students will continue developing mathematical proficiency in a developmentally-appropriate progressions of standards. Continuing the skill progressions from previous courses, the following chart represents the mathematical understandings that will be developed:

Relationships between Quantities and Reasoning with Equations

 Solve problems with a wide range of units and solve problems by thinking about units. (e.g., The Trans Alaska Pipeline System is 800 miles long and cost \$8 billion to build. Divide one of these numbers by the other. What is the meaning of the answer? Greenland has a population of 56,700 and a land area of 2,175,600 square kilometers. By what factor is the population density of the United States, 80 persons per square mile, larger than the population density of Greenland?)

Linear and Exponential Relationships

 Understand contextual relationships of variables and constants. (e.g., Annie is picking apples with her sister. The number of apples in her basket is described by n = 22t + 12, where t is the number of minutes Annie spends picking apples. What do the numbers 22 and 12 tell you about Annie's apple picking?)

Descriptive Statistics

 Use linear regression techniques to describe the relationship between quantities and assess the fit of the model. (e.g., Use the high school and

Expressions and Equations

 Interpret algebraic expressions and transform them purposefully to solve problems. (e.g., In solving a problem about a loan with interest rate r and university grades for 250 students to create a model that can be used to predict a student's university GPA based on his high school GPA.) principal P, seeing the expression P(1+r)ⁿ as a product of P with a factor not depending on P.)

Quadratic Functions and Modeling

 Solve real-world and mathematical problems by writing and solving nonlinear equations, such as quadratic equations (ax² + bx + c = 0).

Numbering of Standards

The following Mathematics Standards will be numbered continuously. The following ranges relate to the clusters found within Mathematics:

Relationships between Quantities and Reasoning with Equations	
Reason quantitatively and use units to solve problems.	Standards 1-3
Interpret the structure of expressions.	Standard 4
Create equations that describe numbers or relationships.	Standards 5-8
Understand solving equations as a process of reasoning and	Standard 9
explain the reasoning.	
Solve equations and inequalities in one variable.	Standard 10
Linear and Exponential Relationships	
Extend the properties of exponents to rational exponents.	Standards 11-12
Solve systems of equations.	Standards 13-14
Represent and solve equations and inequalities graphically.	Standards 15-17
Understand the concept of a function and use function notation.	Standards 18-20
Interpret functions that arise in applications in terms of a context.	Standards 21-23
Analyze functions using different representations.	Standards 24-25
Build a function that models a relationship between two	Standards 26-27
quantities.	
Build new functions from existing functions.	Standards 28
Construct and compare linear, quadratic, and exponential models	Standards 29-31
and solve problems.	
Interpret expressions for functions in terms of the situation they	Standard 32
model.	
Descriptive Statistics	
Summarize, represent, and interpret data on a single count or	Standards 33-35
measurement variable.	
Summarize, represent, and interpret data on two categorical and	Standards 36-37
quantitative variables.	
Interpret linear models.	Standards 38-40

Expressions and Equations	
Interpret the structure of equations.	Standards 41-42
Write expressions in equivalent forms to solve problems.	Standard 43
Perform arithmetic operations on polynomials.	Standard 44
Create equations that describe numbers or relationships.	Standards 45-47
Solve equations and inequalities in one variable.	Standard 48
Solve systems of equations.	Standard 49
Quadratic Functions and Modeling	
Use properties of rational and irrational numbers.	Standard 50
Interpret functions that arise in applications in terms of a context.	Standards 51-53
Analyze functions using different representations.	Standards 54-56
Build a function that models a relationship between two quantities.	Standards 57
Build new functions from existing functions.	Standard 58-59
Construct and compare linear, quadratic and exponential models and solve problems.	Standard 60

Relationships between Quantities and Reasoning with Equations

Cluster	Reason quantitatively and use units to solve problems.
M.A1HS.1	Use units as a way to understand problems and to guide the solution of multi-
	step problems; choose and interpret units consistently in formulas; choose and
	interpret the scale and the origin in graphs and data displays.
M.A1HS.2	Define appropriate quantities for the purpose of descriptive modeling.
	Instructional Note: Working with quantities and the relationships between them
	provides grounding for work with expressions, equations, and functions.
M.A1HS.3	Choose a level of accuracy appropriate to limitations on measurement when
	reporting quantities.

Cluster	Interpret the structure of expressions.	
M.A1HS.4	Interpret expressions that represent a quantity in terms of its context.	
	a. Interpret parts of an expression, such as terms, factors, and coefficients.	
	b. Interpret complicated expressions by viewing one or more of their parts	
	as a single entity. (e.g., Interpret P(1 + r) ⁿ as the product of P and a factor	
	not depending on P. Instructional Note: Limit to linear expressions and	
	to exponential expressions with integer exponents.	

Cluster	Create equations that describe numbers or relationships.
M.A1HS.5	Create equations and inequalities in one variable and use them to solve
	problems. Include equations arising from linear and quadratic functions, and
	simple rational and exponential functions. Instructional Note: Limit to linear
	and exponential equations, and, in the case of exponential equations, limit to
	situations requiring evaluation of exponential functions at integer inputs.

M.A1HS.6	Create equations in two or more variables to represent relationships between quantities; graph equations on coordinate axes with labels and scales. Instructional Note: Limit to linear and exponential equations, and, in the case of exponential equations, limit to situations requiring evaluation of exponential functions at integer inputs.
M.A1HS.7	Represent constraints by equations or inequalities, and by systems of equations and/or inequalities, and interpret solutions as viable or non-viable options in a modeling context. (e.g., Represent inequalities describing nutritional and cost constraints on combinations of different foods.) Instructional Note: Limit to linear equations and inequalities.
M.A1HS.8	Rearrange formulas to highlight a quantity of interest, using the same reasoning as in solving equations. (e.g., Rearrange Ohm's law V = IR to highlight resistance R.) Instructional Note: Limit to formulas with a linear focus.

Cluster	Understand solving equations as a process of reasoning and explain the reasoning.
M.A1HS.9	Explain each step in solving a simple equation as following from the equality of numbers asserted at the previous step, starting from the assumption that the original equation has a solution. Construct a viable argument to justify a solution method. Instructional Note: Students should focus on and master linear equations and be able to extend and apply their reasoning to other types of equations in future courses. Students will solve exponential equations with logarithms in Algebra II.

Cluster	Solve equations and inequalities in one variable.
M.A1HS.10	Solve linear equations and inequalities in one variable, including equations with
	coefficients represented by letters. Instructional Note: Extend earlier work with
	solving linear equations to solving linear inequalities in one variable and to
	solving literal equations that are linear in the variable being solved for. Include
	simple exponential equations that rely only on application of the laws of
	exponents, such as $5^x = 125$ or $2^x = 1 / 16$.

Linear and Exponential Relationships

Cluster	Extend the properties of exponents to rational exponents.
M.A1HS.11	Explain how the definition of the meaning of rational exponents follows from
	extending the properties of integer exponents to those values, allowing for a
	notation for radicals in terms of rational exponents. (e.g., We define 51/3 to be the
	cube root of 5 because we want $(5^{1/3})^3 = 5^{(1/3)3}$ to hold, so $(5^{1/3})^3$ must equal 5.)
	Instructional Note: Address this standard before discussing exponential
	functions with continuous domains.
M.A1HS.12	Rewrite expressions involving radicals and rational exponents using the
	properties of exponents. Instructional Note: Address this standard before
	discussing exponential functions with continuous domains.

Cluster	Solve systems of equations.
M.A1HS.13	Prove that, given a system of two equations in two variables, replacing one
	equation by the sum of that equation and a multiple of the other produces a
	system with the same solutions.
M.A1HS.14	Solve systems of linear equations exactly and approximately (e.g., with graphs),
	focusing on pairs of linear equations in two variables. Instructional Note: Build
	on student experiences graphing and solving systems of linear equations from
	middle school to focus on justification of the methods used. Include cases
	where the two equations describe the same line (yielding infinitely many
	solutions) and cases where two equations describe parallel lines (yielding no
	solution); connect to standards in Geometry which require students to prove the
	slope criteria for parallel lines.

Cluster	Represent and solve equations and inequalities graphically.
M.A1HS.15	Recognize that the graph of an equation in two variables is the set of all its solutions plotted in the coordinate plane, often forming a curve (which could be a line). Instructional Note: Focus on linear and exponential equations and be able to adapt and apply that learning to other types of equations in future courses.
M.A1HS.16	Explain why the x-coordinates of the points where the graphs of the equations $y = f(x)$ and $y = g(x)$ intersect are the solutions of the equation $f(x) = g(x)$; find the solutions approximately (e.g., using technology to graph the functions, make tables of values or find successive approximations). Include cases where $f(x)$ and $f(x)$ are linear, polynomial, rational, absolute value, exponential and logarithmic functions. Instructional Note: Focus on cases where $f(x)$ and $f(x)$ are linear or exponential.
M.A1HS.17	Graph the solutions to a linear inequality in two variables as a half-plane (excluding the boundary in the case of a strict inequality), and graph the solution set to a system of linear inequalities in two variables as the intersection of the corresponding half-planes.

Cluster	Understand the concept of a function and use function notation.
M.A1HS.18	Recognize that a function from one set (called the domain) to another set
	(called the range) assigns to each element of the domain exactly one element of
	the range. If f is a function and x is an element of its domain, then f(x) denotes
	the output of f corresponding to the input x. The graph of f is the graph of the
	equation y = f(x). Instructional Note: Students should experience a variety of
	types of situations modeled by functions. Detailed analysis of any particular
	class of function at this stage is not advised. Students should apply these
	concepts throughout their future mathematics courses. Draw examples from
	linear functions and exponential functions having integral domains.

M.A1HS.19	Use function notation, evaluate functions for inputs in their domains and
	interpret statements that use function notation in terms of a context.
	Instructional Note: Students should experience a variety of types of situations
	modeled by functions. Detailed analysis of any particular class of function at
	this stage is not advised. Students should apply these concepts throughout
	their future mathematics courses. Draw examples from linear functions and
	exponential functions having integral domains.
M.A1HS.20	Recognize that sequences are functions, sometimes defined recursively, whose
	domain is a subset of the integers. (e.g., The Fibonacci sequence is defined
	recursively by $f(0) = f(1) = 1$, $f(n+1) = f(n) + f(n-1)$ for $n \ge 1$. Instructional Note:
	Students should experience a variety of types of situations modeled by
	functions. Detailed analysis of any particular class of function at this stage is
	not advised. Students should apply these concepts throughout their future
	mathematics courses. Draw examples from linear functions and exponential
	functions having integral domains. Draw connection to M.A1HS.27, which
	requires students to write arithmetic and geometric sequences. Emphasize
	arithmetic and geometric sequences as examples of linear and exponential
	functions.

Cluster	Interpret functions that arise in applications in terms of a context.
M.A1HS.21	For a function that models a relationship between two quantities, interpret key features of graphs and tables in terms of the quantities, and sketch graphs showing key features given a verbal description of the relationship. Key features include: intercepts; intervals where the function is increasing, decreasing, positive, or negative; relative maximums and minimums; symmetries; end behavior; and periodicity. Instructional Note: Focus on linear and exponential functions.
M.A1HS.22	Relate the domain of a function to its graph and where applicable, to the quantitative relationship it describes. (e.g., If the function h(n) gives the number of person-hours it takes to assemble n engines in a factory, then the positive integers would be an appropriate domain for the function.) Instructional Note: Focus on linear and exponential functions.
M.A1HS.23	Calculate and interpret the average rate of change of a function (presented symbolically or as a table) over a specified interval. Estimate the rate of change from a graph. Instructional Note: Focus on linear functions and exponential functions whose domain is a subset of the integers. The Unit on Quadratic Functions and Modeling in this course and the Algebra II course address other types of functions.

Cluster	Analyze functions using different representations.
M.A1HS.24	Graph functions expressed symbolically and show key features of the graph, by
	hand in simple cases and using technology for more complicated cases.

- a. Graph linear and quadratic functions and show intercepts, maxima, and minima.
- b. Graph exponential and logarithmic functions, showing intercepts and end behavior and trigonometric functions, showing period, midline and amplitude.

Instructional Note: Focus on linear and exponential functions. Include comparisons of two functions presented algebraically. For example, compare the growth of two linear functions, or two exponential functions such as $y = 3^n$ and $y = 100^{2n}$)

M.A1HS.25

Compare properties of two functions each represented in a different way (algebraically, graphically, numerically in tables, or by verbal descriptions). (e.g., Given a graph of one quadratic function and an algebraic expression for another, say which has the larger maximum.) Instructional Note: Focus on linear and exponential functions. Include comparisons of two functions presented algebraically. For example, compare the growth of two linear functions, or two exponential functions such as $y = 3^n$ and $y = 100^{2n}$)

Cluster	Build a function that models a relationship between two quantities.
M.A1HS.26	Write a function that describes a relationship between two quantities.
	a. Determine an explicit expression, a recursive process, or steps for
	calculation from a context.
	b. Combine standard function types using arithmetic operations. (e.g., Build
	a function that models the temperature of a cooling body by adding a
	constant function to a decaying exponential, and relate these functions to
	the model.)
	Instructional Note: Limit to linear and exponential functions.
M.A1HS.27	Write arithmetic and geometric sequences both recursively and with an explicit
	formula, use them to model situations, and translate between the two forms.
	Instructional Note: Limit to linear and exponential functions. Connect
	arithmetic sequences to linear functions and geometric sequences to
	exponential functions.

Cluster Build new functions from existing functions.

M.A1HS.28

Identify the effect on the graph of replacing f(x) by f(x) + k, k f(x), f(kx), and f(x + k) for specific values of k (both positive and negative); find the value of k given the graphs. Experiment with cases and illustrate an explanation of the effects on the graph using technology. Include recognizing even and odd functions from their graphs and algebraic expressions for them. Instructional Note: Focus on vertical translations of graphs of linear and exponential functions. Relate the vertical translation of a linear function to its y-intercept. While applying other transformations to a linear graph is appropriate at this level, it may be difficult for students to identify or distinguish between the effects of the other transformations included in this standard.

Cluster	Construct and compare linear, quadratic, and exponential models and solve
	problems.
M.A1HS.29	Distinguish between situations that can be modeled with linear functions and
	with exponential functions.
	a. Prove that linear functions grow by equal differences over equal intervals;
	exponential functions grow by equal factors over equal intervals.
	b. Recognize situations in which one quantity changes at a constant rate per
	unit interval relative to another.
	c. Recognize situations in which a quantity grows or decays by a constant
	percent rate per unit interval relative to another.
M.A1HS.30	Construct linear and exponential functions, including arithmetic and geometric
	sequences, given a graph, a description of a relationship or two input-output
	pairs (include reading these from a table). Instructional Note: In constructing
	linear functions, draw on and consolidate previous work in Grade 8 on finding
	equations for lines and linear functions.
M.A1HS.31	Observe using graphs and tables that a quantity increasing exponentially
	eventually exceeds a quantity increasing linearly, quadratically, or (more
	generally) as a polynomial function. Instructional Note: Limit to comparisons
	between exponential and linear models.

Cluster	Interpret expressions for functions in terms of the situation they model.
M.A1HS.32	Interpret the parameters in a linear or exponential function in terms of a
	context. Instructional Note: Limit exponential functions to those of the form $f(x) = b^x + k$.

Descriptive Statistics

Cluster	Summarize, represent, and interpret data on a single count or measurement
	variable.
M.A1HS.33	Represent data with plots on the real number line (dot plots, histograms, and
	box plots).
M.A1HS.34	Use statistics appropriate to the shape of the data distribution to compare
	center (median, mean) and spread (interquartile range, standard deviation) of
	two or more different data sets. Instructional Note: In grades 6 – 8, students
	describe center and spread in a data distribution. Here they choose a summary
	statistic appropriate to the characteristics of the data distribution, such as the
	shape of the distribution or the existence of extreme data points.
M.A1HS.35	Interpret differences in shape, center, and spread in the context of the data sets,
	accounting for possible effects of extreme data points (outliers). Instructional
	Note: In grades 6 – 8, students describe center and spread in a data
	distribution. Here they choose a summary statistic appropriate to the
	characteristics of the data distribution, such as the shape of the distribution or
	the existence of extreme data points.

Cluster	Summarize, represent, and interpret data on two categorical and quantitative
	variables.
M.A1HS.36	Summarize categorical data for two categories in two-way frequency tables.
	Interpret relative frequencies in the context of the data (including joint,
	marginal and conditional relative frequencies). Recognize possible associations
	and trends in the data.
M.A1HS.37	Represent data on two quantitative variables on a scatter plot, and describe
	how the variables are related.
	a. Fit a function to the data; use functions fitted to data to solve problems in
	the context of the data. Use given functions or choose a function
	suggested by the context. Emphasize linear and exponential models.
	b. Informally assess the fit of a function by plotting and analyzing residuals.
	Instructional Note: Focus should be on situations for which linear models
	are appropriate.
	c. Fit a linear function for scatter plots that suggest a linear association.
	Instructional Note: Students take a more sophisticated look at using a linear
	function to model the relationship between two numerical variables. In addition
	to fitting a line to data, students assess how well the model fits by analyzing
	residuals.

Cluster	Interpret linear models.
M.A1HS.38	Interpret the slope (rate of change) and the intercept (constant term) of a linear
	model in the context of the data. Instructional Note: Build on students' work
	with linear relationships in eighth grade and introduce the correlation
	coefficient. The focus here is on the computation and interpretation of the
	correlation coefficient as a measure of how well the data fit the relationship.
M.A1HS.39	Compute (using technology) and interpret the correlation coefficient of a linear
	fit. Instructional Note: Build on students' work with linear relationships in
	eighth grade and introduce the correlation coefficient. The focus here is on the
	computation and interpretation of the correlation coefficient as a measure of
	how well the data fit the relationship.
M.A1HS.40	Distinguish between correlation and causation. Instructional Note: The
	important distinction between a statistical relationship and a cause-and-effect
	relationship is the focus.

Expressions and Equations

Cluster	Interpret the structure of equations.
M.A1HS.41	Interpret expressions that represent a quantity in terms of its context.
	a. Interpret parts of an expression, such as terms, factors, and coefficients.
	b. Interpret complicated expressions by viewing one or more of their parts
	as a single entity. For example, interpret P(1 + r) ⁿ as the product of P and
	a factor not depending on P. Instructional Note: Exponents are extended
	from the integer exponents found in the unit on Relationships between

	Quantities and Reasoning with Equations to rational exponents focusing
	on those that represent square or cube roots.
	Instructional Note: Focus on quadratic and exponential expressions.
M.A1HS.42	Use the structure of an expression to identify ways to rewrite it. For example,
	see $x^4 - y^4$ as $(x^2)^2 - (y^2)^2$, thus recognizing it as a difference of squares that can
	be factored as $(x^2 - y^2)(x^2 + y^2)$. Instructional Note: Focus on quadratic and
	exponential expressions.

Cluster	Write expressions in equivalent forms to solve problems.
M.A1HS.43	Choose and produce an equivalent form of an expression to reveal and explain
	properties of the quantity represented by the expression.
	a. Factor a quadratic expression to reveal the zeros of the function it
	defines.
	b. Complete the square in a quadratic expression to reveal the maximum or
	minimum value of the function it defines.
	c. Use the properties of exponents to transform expressions for exponential
	functions. For example the expression 1.15 t can be rewritten as (1.15 $^{1/12}$) 12t \approx
	1.012 ^{12t} to reveal the approximate equivalent monthly interest rate if the
	annual rate is 15%.
	Instructional Note: It is important to balance conceptual understanding and
	procedural fluency in work with equivalent expressions. For example,
	development of skill in factoring and completing the square goes hand-in-hand
	with understanding what different forms of a quadratic expression reveal.

Cluster	Perform arithmetic operations on polynomials.
M.A1HS.44	Recognize that polynomials form a system analogous to the integers, namely,
	they are closed under the operations of addition, subtraction, and
	multiplication; add, subtract, and multiply polynomials. Instructional Note:
	Focus on polynomial expressions that simplify to forms that are linear or
	quadratic in a positive integer power of x.

Cluster	Create equations that describe numbers or relationships.
M.A1HS.45	Create equations and inequalities in one variable and use them to solve
	problems. Include equations arising from linear and quadratic functions, and
	simple rational and exponential functions. Instructional Note: Extend work on
	linear and exponential equations in the Relationships between Quantities and
	Reasoning with Equations unit to quadratic equations.
M.A1HS.46	Create equations in two or more variables to represent relationships between
	quantities; graph equations on coordinate axes with labels and scales.
	Instructional Note: Extend work on linear and exponential equations in the
	Relationships between Quantities and Reasoning with Equations unit to
	quadratic equations.

M.A1HS.47	Rearrange formulas to highlight a quantity of interest, using the same reasoning
	as in solving equations. (e.g., Rearrange Ohm's law V = IR to highlight resistance
	R. Instructional Note: Extend work on linear and exponential equations in the
	Relationships between Quantities and Reasoning with Equations unit to
	quadratic equations. Extend this standard to formulas involving squared
	variables.

Cluster	Solve equations and inequalities in one variable.
M.A1HS.48	Solve quadratic equations in one variable.
	a. Use the method of completing the square to transform any quadratic
	equation in x into an equation of the form $(x - p)^2 = q$ that has the same
	solutions. Derive the quadratic formula from this form.
	b. Solve quadratic equations by inspection (e.g., for x² = 49), taking square roots, completing the square, the quadratic formula and factoring, as appropriate to the initial form of the equation. Recognize when the quadratic formula gives complex solutions and write them as a ± bi for real numbers a and b.
	Instructional Note: Students should learn of the existence of the complex number system, but will not solve quadratics with complex solutions until Algebra II.

Cluster	Solve systems of equations.
M.A1HS.49	Solve a simple system consisting of a linear equation and a quadratic equation
	in two variables algebraically and graphically. For example, find the points of
	intersection between the line $y = -3x$ and the circle $x^2 + y^2 = 3$. Instructional
	Note: Include systems consisting of one linear and one quadratic equation.
	Include systems that lead to work with fractions. For example, finding the
	intersections between $x^2 + y^2 = 1$ and $y = (x+1)/2$ leads to the point (3/5, 4/5) on
	the unit circle, corresponding to the Pythagorean triple $3^2 + 4^2 = 5^2$.

Quadratic Functions and Modeling

Cluster	Use properties of rational and irrational numbers.
M.A1HS.50	Explain why the sum or product of two rational numbers is rational; that the
	sum of a rational number and an irrational number is irrational; and that the
	product of a nonzero rational number and an irrational number is irrational.
	Instructional Note: Connect to physical situations (e.g., finding the perimeter
	of a square of area 2).

Cluster	Interpret functions that arise in applications in terms of a context.
M.A1HS.51	For a function that models a relationship between two quantities, interpret
	key features of graphs and tables in terms of the quantities, and sketch
	graphs showing key features given a verbal description of the relationship.
	Key features include: intercepts; intervals where the function is increasing,

	decreasing, positive, or negative; relative maximums and minimums;
	symmetries; end behavior; and periodicity. Instructional Note: Focus on
	quadratic functions; compare with linear and exponential functions studied
	in the Unit on Linear and Exponential Relationships.
M.A1HS.52	Relate the domain of a function to its graph and, where applicable, to the
	quantitative relationship it describes. For example, if the function h(n) gives
	the number of person-hours it takes to assemble n engines in a factory, then
	the positive integers would be an appropriate domain for the function.
	Instructional Note: Focus on quadratic functions; compare with linear and
	exponential functions studied in the Unit on Linear and Exponential
	Relationships.
M.A1HS.53	Calculate and interpret the average rate of change of a function (presented
	symbolically or as a table) over a specified interval. Estimate the rate of
	change from a graph. Instructional Note: Focus on quadratic functions;
	compare with linear and exponential functions studied in the Unit on Linear
	and Exponential Relationships.

Cluster	Analyze functions using different representations.
M.A1HS.54	Graph functions expressed symbolically and show key features of the graph,
	by hand in simple cases and using technology for more complicated cases.
	a. Graph linear and quadratic functions and show intercepts, maxima,
	and minima.
	b. Graph square root, cube root, and piecewise-defined functions,
	including step functions and absolute value functions.
	Instructional Note: Compare and contrast absolute value, step and
	piecewise-defined functions with linear, quadratic, and exponential
	functions. Highlight issues of domain, range, and usefulness when examining
	piecewise-defined functions. Extend work with quadratics to include the
	relationship between coefficients and roots, and that once roots are known,
	a quadratic equation can be factored.
M.A1HS.55	Write a function defined by an expression in different but equivalent forms to
	reveal and explain different properties of the function.
	a. Use the process of factoring and completing the square in a quadratic
	function to show zeros, extreme values, and symmetry of the graph,
	and interpret these in terms of a context.
	b. Use the properties of exponents to interpret expressions for
	exponential functions. For example, identify percent rate of change in
	functions such as y = (1.02) ^t , y = (0.97) ^t , y = (1.01) ^{12t} , y = (1.2) ^{t/10} , and
	classify them as representing exponential growth or decay.
	Instructional Note: Extend work with quadratics to include the relationship
	between coefficients and roots, and that once roots are known, a quadratic
	equation can be factored. This standard extends the work begun in the

	Linear and Exponential Relationships unit on exponential functions with
	integer exponents.
M.A1HS.56	Compare properties of two functions each represented in a different way
	(algebraically, graphically, numerically in tables, or by verbal descriptions).
	For example, given a graph of one quadratic function and an algebraic
	expression for another, say which has the larger maximum. Instructional
	Note: Highlight issues of domain, range, and usefulness when examining
	piecewise-defined functions. Extend work with quadratics to include the
	relationship between coefficients and roots, and that once roots are known,
	a quadratic equation can be factored.

Cluster	Build a function that models a relationship between two quantities.
M.A1HS.57	Write a function that describes a relationship between two quantities.
	a. Determine an explicit expression, a recursive process, or steps for
	calculation from a context.
	b. Combine standard function types using arithmetic operations. For
	example, build a function that models the temperature of a cooling
	body by adding a constant function to a decaying exponential, and
	relate these functions to the model.
	Instructional Note: Focus on situations that exhibit a quadratic relationship.

Cluster	Build new functions from existing functions.
M.A1HS.58	Identify the effect on the graph of replacing $f(x)$ by $f(x) + k$, k $f(x)$, $f(kx)$, and
	f(x + k) for specific values of k (both positive and negative); find the value of k
	given the graphs. Experiment with cases and illustrate an explanation of the
	effects on the graph using technology. Include recognizing even and odd
	functions from their graphs and algebraic expressions for them. Instructional
	Note: Focus on quadratic functions, and consider including absolute value
	functions.
M.A1HS.59	Find inverse functions. Solve an equation of the form $f(x) = c$ for a simple
	function f that has an inverse and write an expression for the inverse. For
	example, $f(x) = 2 x^3$ or $f(x) = (x+1)/(x-1)$ for $x \ne 1$. Instructional Note: Focus on
	linear functions but consider simple situations where the domain of the
	function must be restricted in order for the inverse to exist, such as $f(x) = x^2$,
	x > 0.

Cluster	Construct and compare linear, quadratic and exponential models and solve problems.
M.A1HS.60	Observe using graphs and tables that a quantity increasing exponentially eventually exceeds a quantity increasing linearly, quadratically, or (more generally) as a polynomial function. Instructional Note: Compare linear and exponential growth to quadratic growth.