Test 5: Volume and Area (ch. 11)

Find the area of the following figures. Give answers in terms of pi when necessary, otherwise round to the nearest tenth.



- 14. Find the area of a circle if the circumference is 6π yd.
- **15.** Find the diameter of a circle if the area is 201.1 in^2
- **16.** Find the radius of a circle is the circumference is 62.8 mi.

For #17 – 23: Find the volume and surface area of the following figures. Give answers in terms of pi when necessary, otherwise round to the nearest tenth.





Test 4: Special Points and Segments in Triangles & Parallelograms (Ch. 6 and 7.1-7.2)

- 25. a) Given that XZ = 38, YX = 27, and YZ = 27, find ZW. b) Given that line p is the perpendicular bisector of \overline{XZ} ; c) *XY* = 4*n*, and *YZ* =14, find *n*.
- 26. a) Given that FG = HG and m<FEH = 58, find m<GEH. b) Given that \overrightarrow{EG} bisects $\angle FEH$ and $GF = \sqrt{2}$, find **GH**. c) Given that $\angle FEG \cong \angle HEG$, FG = 10z - 30, and HG = 7z + 6, find FG.
- **27.** Use the figure. \overline{SV} , \overline{TV} , and \overline{UV} are perpendicular bisectors of the sides of Δ*PQR*. Find each length.
 - a) RV b) TR
 - c) PR

5 in.

5 in.

- **28.** Use the figure. \overline{HK} and \overline{JK} are angle bisectors of Δ HIJ. Find each measure.
 - a) the distance from K to \overline{JI}
 - b) angle JHK
 - c) angle HJI



29. Use the figure. \overline{QU} , \overline{PT} and \overline{RS} are medians of ΔPQR . RS = 21 and VT = 5. Find each length.

- a) RV
- b) SV
- c) TP



- a) ST
- b) QR
- c) PU
- d) m<SUP



32. Determine if the quadrilateral is a parallelogram. Justify your answer.



24

33. Find the value of *n* in the triangle.



34. Compare incenter and circumcenter. How are they similar? How are they different? (Be detailed.)

E

9 *x* – 12

G

x + 6

- **35.** Draw ΔDEF on a piece of graph paper. Find the orthocenter of ΔDEF with vertices D(2, 3), E(2, -4), F(-4, -3). Include any relevant math. Label the orthocenter M.
- **36.** Draw \triangle ABC on a piece of graph paper. Find the centroid of \triangle ABC with vertices A(0, 1), B(4, 7), C(8, -2). Include any relevant math. Label the centroid K.
- **37.** For each parallelogram, find the missing variables.











Test 3: Proving Triangles Congruent (ch. 5)

For #41 – 49: Determine which postulate/theorem (if any) can be used to prove the given triangles congruent. Explain. Give a congruence statement, if applicable.







46.

49.









50. Find x.

51. Find w.









53. Write a two-column proof.

Given: $\overrightarrow{AB} \parallel \overrightarrow{CD}$, $\overrightarrow{AB} \cong \overrightarrow{CD}$, $\overrightarrow{AC} \cong \overrightarrow{BD}$, $\overrightarrow{AC} \perp \overrightarrow{CD}$, $\overrightarrow{DB} \perp \overrightarrow{AB}$ Prove: $\triangle ACD \cong \triangle DBA$



55. Write a two-column proof.





54. Write a two-column proof.

Given: \overline{JK} bisects $\angle MJN$. $\overline{MJ} \cong \overline{NJ}$ Prove: $\triangle MJK \cong \triangle NJK$



56. Write a two-column proof.

Given: $\overline{CD} \parallel \overline{BE}, \overline{DE} \parallel \overline{CB}$ Prove: $\angle D \cong \angle B$





Find the measure of each angle. Write the theorem that supports your answer.







62. Given: $\triangle DEF \cong \triangle LMN$. Find each value.



Find the value of x so that the triangles are congruent.



65. The Hatfield and McCoy families are feuding over some land. Neither family will be satisfied unless the two triangular fields are exactly the same size. You know that C is the midpoint of each of the intersecting segments. Write a two-column proof that will settle the dispute.

Given: *C* is the midpoint of \overline{AD} and \overline{BE} . **Prove:** $\triangle ABC \cong \triangle DEC$



66.Given: $\overline{PQ} \cong \overline{RQ}, \angle PQS \cong \angle RQS$ **Prove:** $\angle P \cong \angle R$



For 67 – 72: Find each value.





69. angle L







73. Some hikers come to a river in the woods. They want to cross the river but decide to find out how wide it is first. So they set up congruent right triangles. The figure shows the river and the triangles. Find the width of the river, *GH*, and give your reasoning.

5 m 3 m G K 3 m H

74. Identify and describe each of the following transformations according to their rules. Then tell whether or not the transformation is an isometry.

a) M: (x, y) → (x - 2, y + 3)	b) M: (x, y) → (-x, y)		
c) M: $(x, y) \rightarrow (-y, x)$	d) M: (x, y) → (3x, 3y)		

75. Draw the following polygon on a piece of graph paper: A (2, 3), B(-2, 5), C(-3, 0), D(1, -3), and E(4, -1). Then, translate the polygon 5 units down and 2 units right to get image 1. Next, reflect the polygon over the x-axis to get image 2. Finally rotate the polygon 180° to get image 3. Make sure to label all points appropriately.

Test 2: Proving Theorems about Lines and Angles (ch. 3 and 4)

Find each angle measure. Write the theorem that justifies how you found your answer.



80. Use the figure for the following questions. Tell whether lines *m* and *n* must be parallel from the given information. If they are, state your reasoning.

- a) $\angle 7 \cong \angle 5$ b) $\angle 7 \cong \angle 6$
- c) $\angle 1 \cong \angle 5$ d) $\angle 2 \cong \angle 8$

81. <u>Segment Constructions</u>: (a) Draw a line segment label the endpoints F and G. Construct the perpendicular bisector. (b) Draw a line segment label the endpoints K and L. Construct a congruent segment labeled M and N.



82. <u>Angle Constructions</u>: (a) Draw an angle label it A. Construct the angle bisector. (b) Draw an angle, label B. Construct a congruent angle to B and label it C.

83. Draw line *m*. Construct a line parallel to line *m*.





85. Name the shortest segment from the point to the line and write an inequality for *x*.



87.

Test 1: Tools of Geometry/Algebraic & Geometric Proofs (ch. 1 and 2)

86. Find the length of the segment EC, BD, BE using the Ruler Postulate.



88. Find LM.



- H is the midpoint of IJ. 90. IJ = 9.4.Find IH.
- 92. Name each of the angles in as many ways as possible.



 $m \angle PQR = (10x - 7)^\circ$, $m \angle RQT = 5x^\circ$, and $m \angle PQT = (4x + 6)^\circ$

- 89. GJ bisects $\angle FGH$, m $\angle FGJ = (7x - 9)^\circ$, and m $\angle HGJ = (2x + 36)^\circ$. What is m∠FGH?
- 91. What is the next letter in the sequence?

D, H, L, P, . . .

93. Complete the conjecture. Provide at least three examples.

The square of any negative number is _____.



96. Using the conditional below: Negate the conditional statement, then write the converse and the inverse. *"If a figure has four sides, then it is a square."*

- **97.** Use the indicated property to complete each statement.
 - a) Reflexive Property of Congruence: 9 2x = _____
 - b) Division Property of Equality: If 5x = 30, then ______.
 - c) Symmetric Property of Equality: If x = -2, then _____
 - d) Transitive Property of Congruence: $\angle A \cong \angle B$ and $\angle B \cong \angle C$, so ______.

98. Name the property that justifies each of the following statements.

a) $3 - x = 3 - x$	b)
c) If x – 2 = 2, then x = 4	d) $\overline{EF} \cong \overline{EF}$
e) If a = 2, and 2 = p, then a = p	f)
g) If x + 2 = 6, then x = 4	h) If 3(x - 9), then 3x – 27
i) If a = 2, then 2 can be plugged in for a in a	ny expression
j) <a <a="" <b="" <c,="" <c.<="" and="" p="" so="" ≌="">	k) <1 ≌ <2, so <2 ≌ <1.
I) If $a = b$, then $a - c = b - c$	m) If $a = b$ and $c \neq 0$, then $\frac{a}{c} = \frac{b}{c}$

99. Solve the following equations. Show all your steps and write a justification for each step.

a)
$$\frac{2}{5}(m+10) = -4$$
 b) $4y - 1 = 27$ c) $60 = 2(x + 12)$

100. Write a two-column proof for the problem below.

Given: $\angle HKJ$ is a straight angle. \overrightarrow{KI} bisects $\angle HKJ$. **Prove:** $\angle IKJ$ is a right angle.

2



 $D = \frac{11}{2} + 1 E 7 F$ DE + EF = DF

101. Complete the following algebraic proof.

$$\begin{pmatrix} \frac{1}{3}x + 1 \end{pmatrix} + 7 = 11$$

$$\frac{1}{3}x + 8 = 11$$

$$\frac{1}{3}x = 3$$

$$\underline{x} = 9$$

102. Write a two-column proof for the problem below.

Given: $\angle 4 \cong \angle 3$ Prove: $m \angle 1 = m \angle 2$ **103.** Write a two-column proof for the problem below.



104. Write a two-column proof for the problem below. **Given:** $m \angle 1 + m \angle 3 = 180^{\circ}$ **Prove:** $\angle 1 \cong \angle 4$

105. Use the given plan to write a two-column proof.

Given: ∠1 and ∠2 form a linear pair, and ∠3 and ∠4 form a linear pair.

Prove: $m \angle 1 + m \angle 2 + m \angle 3 + m \angle 4 = 360^{\circ}$

Plan: The Linear Pair Theorem shows that ∠1 and ∠2 are supplementary and ∠3 and ∠4 are supplementary. The definition of supplementary says that m∠1 + m∠2 = 180° and m∠3 + m∠4 = 180°. Use the Addition Property of Equality to make the conclusion.



106. Write a two-column proof for the problem below. **Given:** $m \angle BAC = m \angle EAF$, $m \angle CAD = m \angle DAE$ **Prove:** $m \angle BAD = m \angle DAF$



107. Miguel breaks a 17-centimeter-long pencil into two pieces. One of the pieces is 9 centimeters long. Use the given paragraph proof to complete the two-column proof showing that the other piece is 8 centimeters long.

Given: <i>AC</i> = 17, <i>AB</i> = 9	1		-17	
Prove: <i>BC</i> = 8	A	9	В	Ĉ