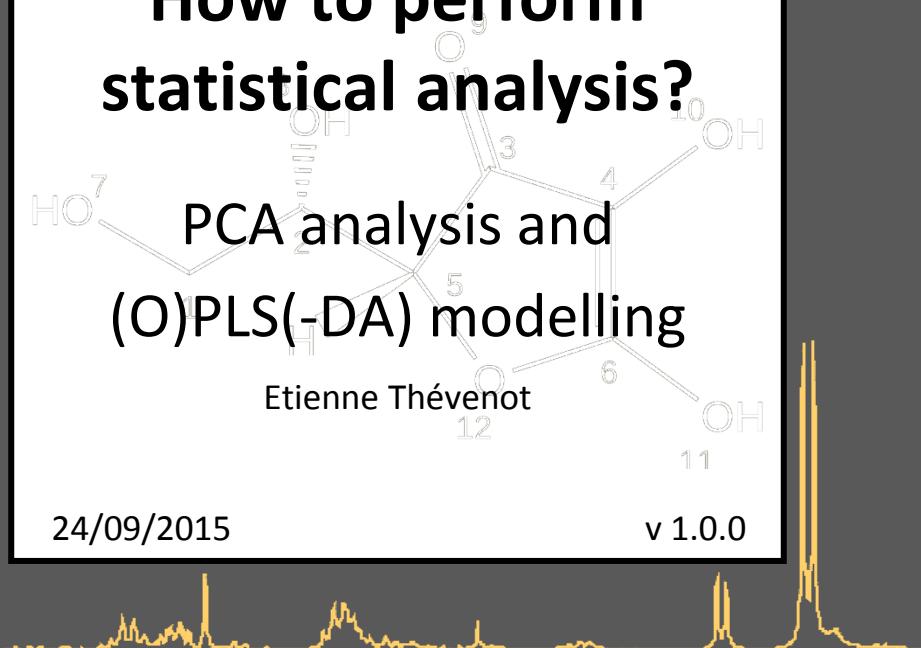


How to perform  
statistical analysis?  
PCA analysis and  
(O)PLS(-DA) modelling

Etienne Thévenot

24/09/2015

v 1.0.0



# The "Multivariate" module

Multivariate

- The "Multivariate" module allows you to perform:
  - Principal Component Analysis (**PCA**)
  - Partial Least-Squares regression (**PLS**) and discriminant analysis (**PLS-DA**)
  - Orthogonal Partial Least-Squares regression (**OPLS**) and discriminant analysis (**OPLS-DA**)
- It is available in the "Statistical Analysis" sections of LC-MS, GC-MS, and NMR

The screenshot shows the Galaxy web interface. At the top, there is a purple header bar with the word "Multivariate". Below the header, the main content area has a light blue background. On the left, there is a sidebar with various categories: "Tools", "search tools", "Upload File from your computer", "Export Data", "LC-MS", "Format Conversion", "Preprocessing", "Normalisation", "Quality Control", "Statistical Analysis", "Univariate statistics", and "Multivariate PCA, PLS and OPLS". The "Multivariate PCA, PLS and OPLS" link is highlighted with a green border. At the bottom of the page, there is a decorative footer featuring a yellow chromatogram-like pattern.

# The "Multivariate" module

Multivariate

- The Multivariate module uses internally the *ropels* R module from bioconductor

<http://bioconductor.org/packages/ropels>

- implements the original, NIPALS based, algorithms for PCA, PLS and OPLS
- diagnostics to detect outliers, overfitting
- graphics (scores, loadings, predictions)
- feature selection (VIP, regression coefficients)

Thévenot E.A., Roux A., Xu Y., Ezan E. and Junot C. (2015). Analysis of the human adult urinary metabolome variations with age, body mass index and gender by implementing a comprehensive workflow for univariate and OPLS statistical analyses. *Journal of Proteome Research*, **14**:3322-3335.

<http://dx.doi.org/10.1021/acs.jproteome.5b00354>

# Objectives

- Multivariate analysis:
    1. PCA [unsupervised]: Visualize the structure of the **dataMatrix**:  $\mathbf{X}$
    2. (O)PLS(-DA) [supervised]: How can a factor of interest (response; column of **sampleMetadata**) be explained as a linear combination of **all** the variables (predictors) from **dataMatrix**:  $\mathbf{y} = f(\mathbf{X})$ 
      - a. when the response  $\mathbf{y}$  is quantitative: (O)PLS regression
      - b. when  $\mathbf{y}$  is qualitative: (O)PLS(-DA) classification
- Complementary to univariate analysis (where variables are tested independently)

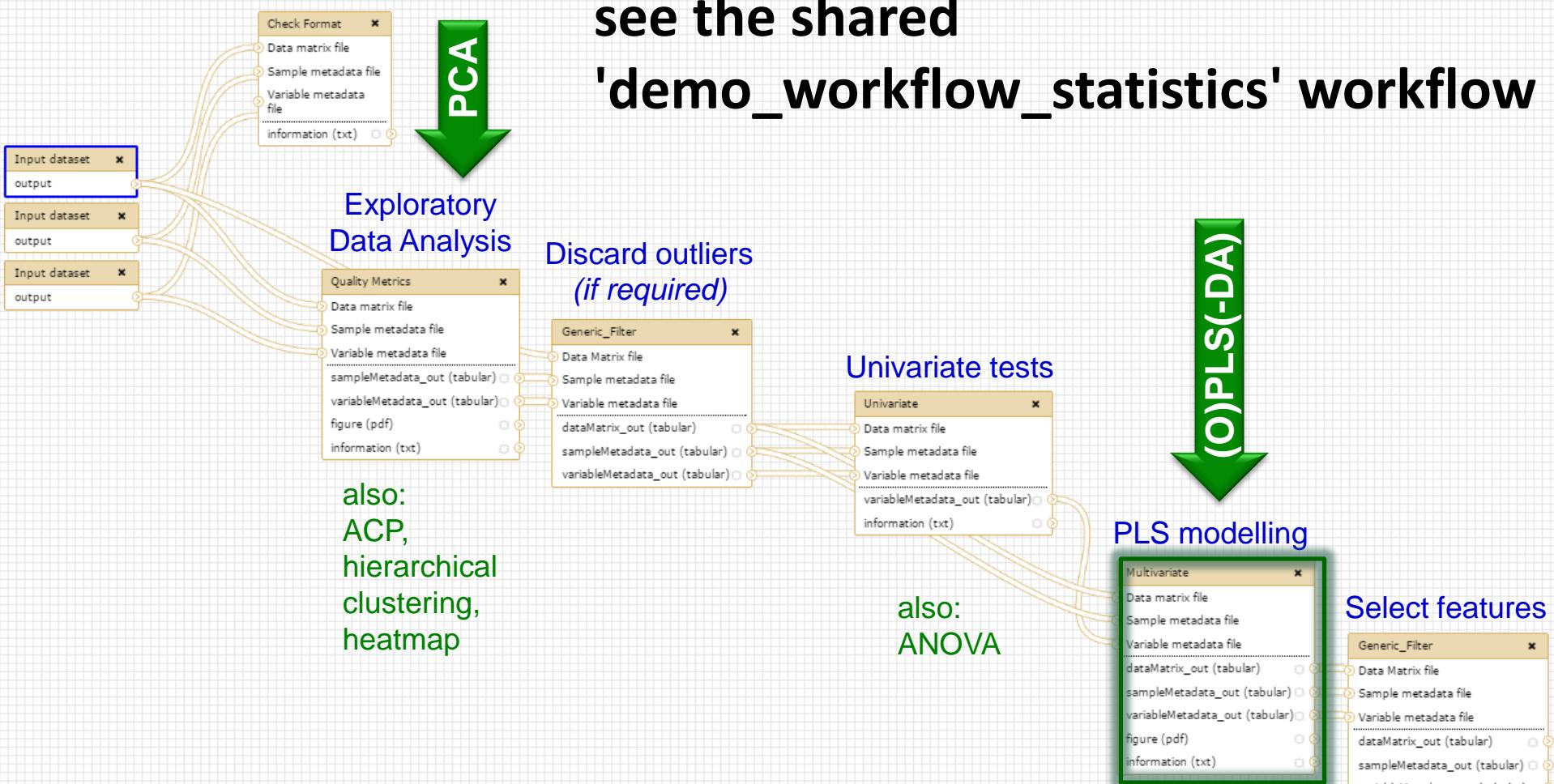


# Latent variable methods

- PCA and (O)PLS(-DA) are **latent variable** methods: new components are computed as linear combinations of the original variables
- The assumption is that a few components can efficiently represent the whole dataset (PCA) or model the factor of interest (O)PLS(-DA)
- **Other powerful multivariate methods** exist for regression and classification (Support Vector Machine, Random Forest, etc.)
  - soon available on W4M



# PCA and (O)PLS(-DA) steps in the analysis



# Open the "Multivariate" module

- and select your 3 files of interest:

Galaxy / 4 / Metabolomics    Analyze Data    Workflow    Shared Data ▾    Visualization ▾    Help ▾    User ▾    Using 2%

Tools   

search tools

**Upload File from your computer**

**Export Data**

LC-MS

Format Conversion

Preprocessing

Normalisation

Quality Control

**Statistical Analysis**

Univariate Univariate statistics

**Multivariate PCA, PLS and OPLS**

Anova N-way anova. With or Without interactions

ACP ellipsoid by factors

Hierarchical Clustering using ctc R package for java-treeview

Heatmap Heatmap of the dataMatrix

Multivariate (version 2015-04-25)

**Data matrix file:** 1: dataMatrix.tsv  
Variable x sample, decimal: ., missing: NA, mode: numerical, sep: tabular

**Sample metadata file:** 2: sampleMetadata.tsv  
sample x metadata, decimal: ., missing: NA, mode: character and numerical, sep: tabular

**Variable metadata file:** 3: variableMetadata.tsv  
variable x metadata, decimal: ., missing: NA, mode: character and numerical, sep: tabular

**Y Response (for PLS(-DA) and OPLS(-DA) only):**  
none

Notes: 1) PCA: keep the default (none); 2) PLS(-DA) and OPLS(-DA): indicate the name of the column of the sample table to be modeled

**Number of predictive components:**  
2

Notes: 1) PCA and PLS(-DA): NA can be selected to get a suggestion of the optimal number of predictive components; 2) OPLS(-DA) modeling: select 1 predictive component

**Number of orthogonal components (for OPLS(-DA) only):**  
0

Notes: 1) PCA and PLS(-DA): keep the default value (0); 2) OPLS(-DA): NA can be selected to get a suggestion of the optimal number of orthogonal components

**Advanced graphical parameters:**  
Use default

History

search datasets

**Unnamed history**

278.8 KB

4: Check Format information.txt

3: variableMetadata.tsv

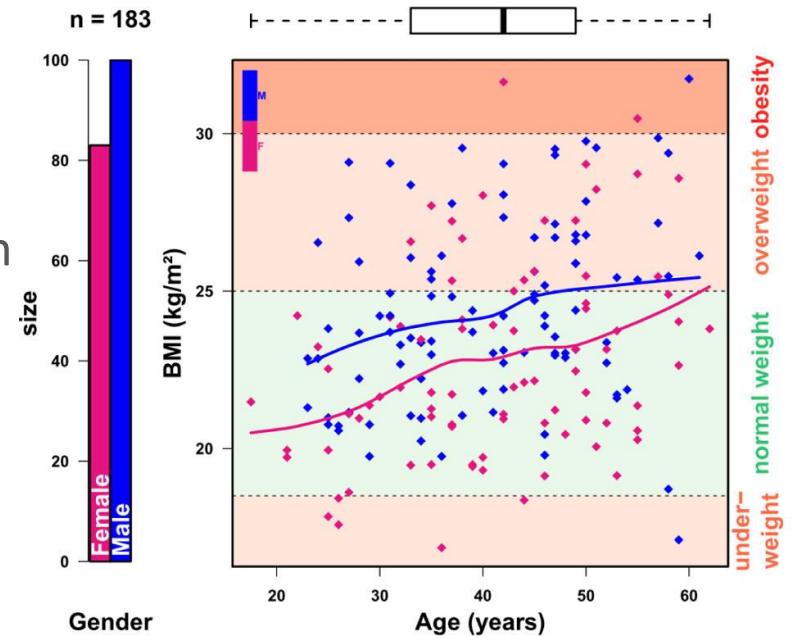
2: sampleMetadata.tsv

1: dataMatrix.tsv

- you are now ready to start your multivariate analyzes!

# Sacurine dataset

- Objective: influence of age, body mass index and gender on metabolite concentrations in urine
- Cohort: 183 employees from the CEA institute
- Analytics: LTQ-Orbitrap (negative ionization mode)
- Annotation: 109 metabolites were identified or annotated at the MSI level 1 or 2.
- Pre-processing:
  - XCMS followed by Quan Browser
  - Signal drift and batch effect correction
  - Normalization to the osmolality
  - log<sub>10</sub> transformation



Thévenot E.A., Roux A., Xu Y., Ezan E. and Junot C. (2015). Analysis of the human adult urinary metabolome variations with age, body mass index and gender by implementing a comprehensive workflow for univariate and OPLS statistical analyses. *Journal of Proteome Research*, 14:3322-3335.  
<http://dx.doi.org/10.1021/acs.jproteome.5b00354>

---

4

Wm

Workflow4metabolomics

# PRINCIPAL COMPONENT ANALYSIS (PCA)



# Objectives

- Visualize the dataMatrix
  - by selecting a few components which capture most of the spread (variance) of the cloud of samples
- Detect outliers
  - which may bias the computation of the component
- Detect clusters of samples
  - which may suggest an internal structuration of the data



# Unsupervised analysis

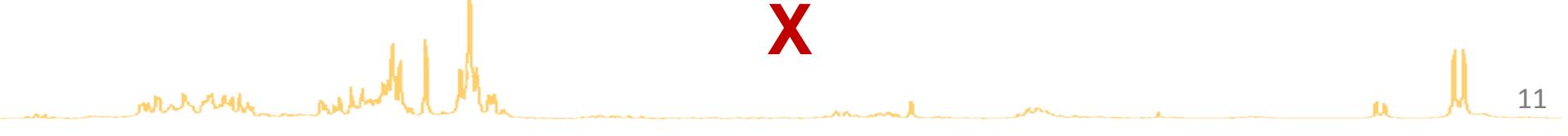
**p = 30 (quantitative) variables**

	1,7-Dimethyluric acid	Dehydroepiandrosterone sulfate	Acetaminophen glucuronide
H011	2114	29025	44
H023	43274	639	2
H033	22386	325	1933
H042	8185	13938	933
H052	22385	357	5004
H062	6380	292	1
H073	10012	22781	1
H083	30414	105	1
H092	6637	35156	1
H103	12100	2	1
H114	33362	149041	46
H124	11197	84536	1
H134	18698	34053	254
H145	14435	212398	52
H157	31732	19317	2200
H168	10221	78	475
H180	22936	463	1
H189	14423	1039	220
H199	2888	12272	37
H209	12563	100236	2

*n = 20 samples*

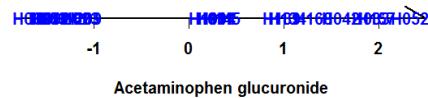
...

X

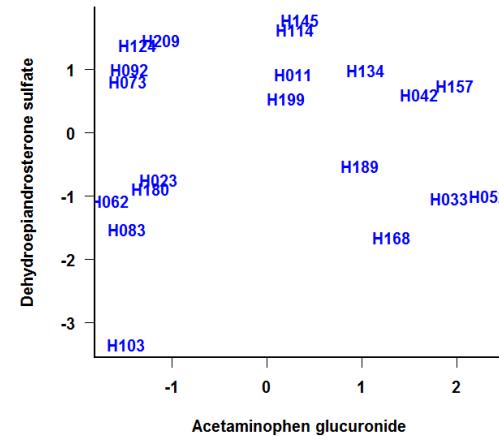


# How to visualize multivariate observations?

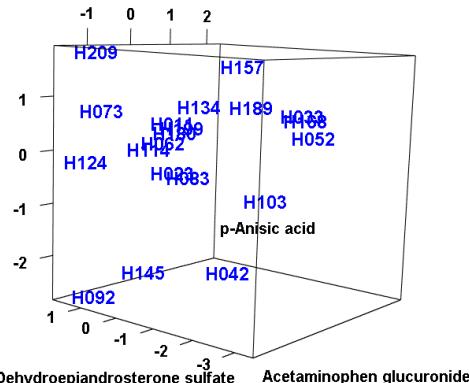
1 variable



2 variables



3 variables



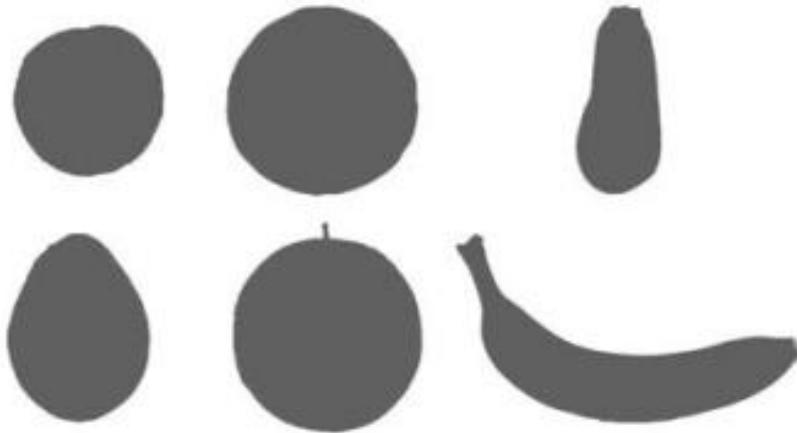
$p$  variables



=> Dimension reduction

# Projection

- Projected distances as high as possible

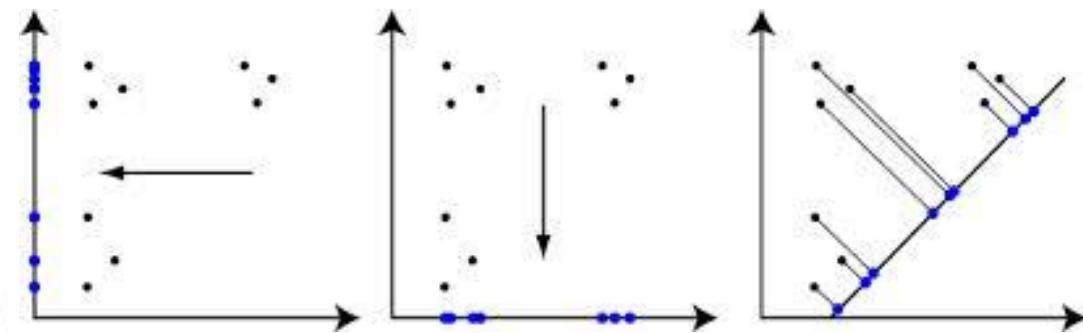
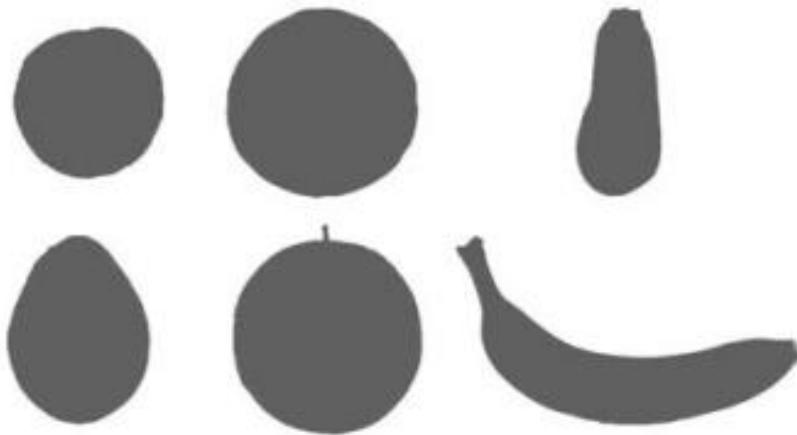


Husson and Pages (2011). Exploratory multivariate analysis by example using R.  
Chapman & Hall/CRC



# Projection on latent variables

- Projected distances as high as possible
- Define new variables as linear combination of original ones



Husson and Pages (2011). Exploratory multivariate analysis by example using R.  
Chapman & Hall/CRC



# Selection of PCA as the type of analysis

- Keep the "Y response" to 'none' for PCA (unsupervised analysis)

Galaxy / 4 / Metabolomics   Analyze Data   Workflow   Shared Data ▾   Visualization ▾   Help ▾   User ▾   Using 2%

Tools  

search tools  

Upload File from your computer

Export Data

LC-MS

Format Conversion

Preprocessing

Normalisation

Quality Control

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sample x metadata, decimal: '.', missing: NA, mode: character and numerical, sep: tabular

Variable metadata file: 3: variableMetadata.tsv  
variable x metadata, decimal: '.', missing: NA, mode: character and numerical, sep: tabular

**Y Response (for PLS(-DA) and OPLS(-DA) only):**   
Notes: 1) PCA; keep the default (none); 2) PLS(-DA) and OPLS(-DA): indicate the name of the column of the sample table to be modeled

**Number of predictive components:**   
Notes: 1) PCA and PLS(-DA): NA can be selected to get a suggestion of the optimal number of predictive components; 2) OPLS(-DA) modeling: select 1 predictive component

**Number of orthogonal components (for OPLS(-DA) only):**   
Notes: 1) PCA and PLS(-DA): keep the default value (0); 2) OPLS(-DA): NA can be selected to get a suggestion of the optimal number of orthogonal components

**Advanced graphical parameters:**

History

search datasets

Unnamed history  
278.8 KB

4: Check Format information.txt

3: variableMetadata.tsv

2: sampleMetadata.tsv

1: dataMatrix.tsv



15

# Automatic selection of the number of components

- Until the variance is less than the mean variance of all components

Galaxy / 4 / Metabolomics    Analyze Data    Workflow    Shared Data ▾    Visualization ▾    Help ▾    User ▾    Using 2%

History

Multivariate (version 2015-04-25)

Data matrix file: 1: dataMatrix.tsv  
variable x sample, decimal: '.', missing: NA, mode: numerical, sep: tabular

Sample metadata file: 2: sampleMetadata.tsv  
sample x metadata, decimal: '.', missing: NA, mode: character and numerical, sep: tabular

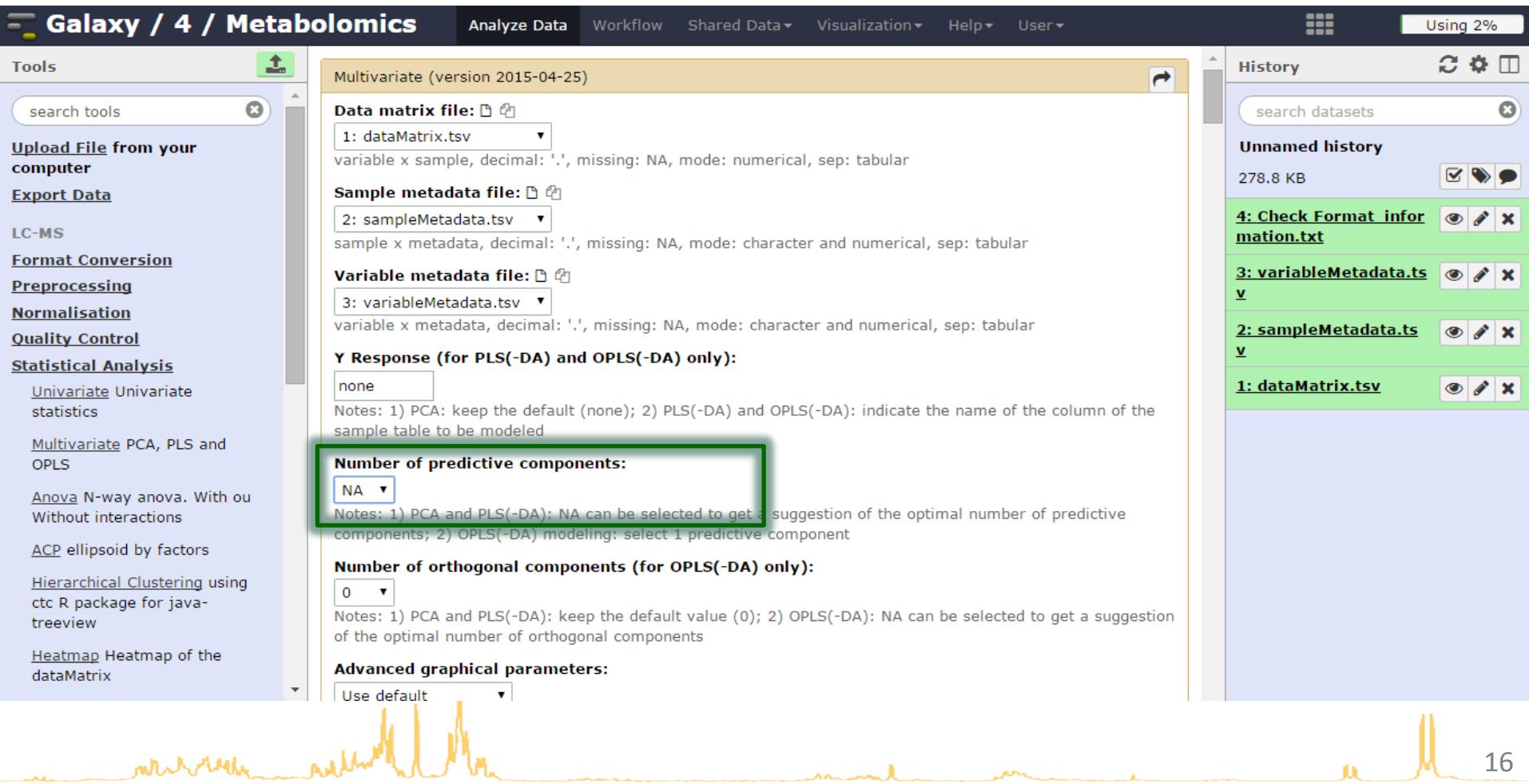
Variable metadata file: 3: variableMetadata.tsv  
variable x metadata, decimal: '.', missing: NA, mode: character and numerical, sep: tabular

Y Response (for PLS(-DA) and OPLS(-DA) only):  
none  
Notes: 1) PCA: keep the default (none); 2) PLS(-DA) and OPLS(-DA): indicate the name of the column of the sample table to be modeled

Number of predictive components:  
NA  
Notes: 1) PCA and PLS(-DA): NA can be selected to get a suggestion of the optimal number of predictive components; 2) OPLS(-DA) modeling: select 1 predictive component

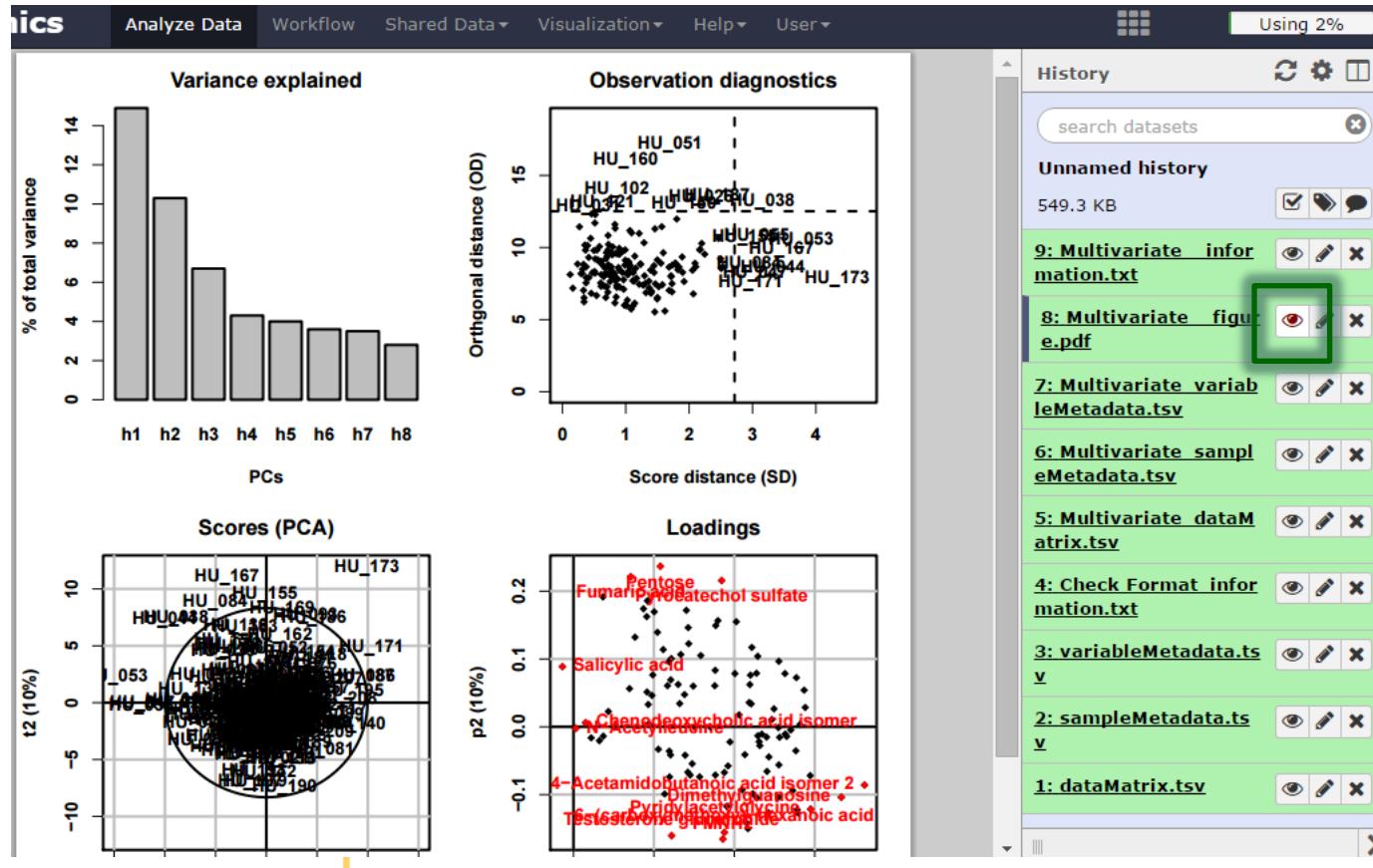
Number of orthogonal components (for OPLS(-DA) only):  
0  
Notes: 1) PCA and PLS(-DA): keep the default value (0); 2) OPLS(-DA): NA can be selected to get a suggestion of the optimal number of orthogonal components

Advanced graphical parameters:  
Use default



# Graphical results

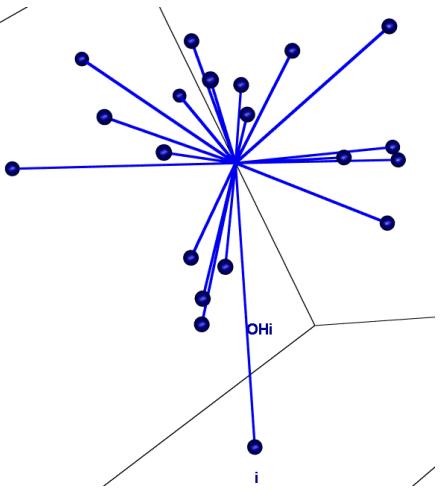
- scree plot, outliers, and the loading and score plots



# Diagnostics R2X: How much of the original inertia is still reflected by the model?

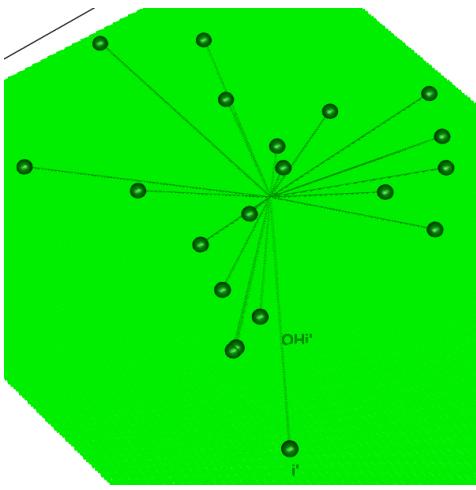
Total

$$TSS = \sum_{i=1}^n OH_i^2$$



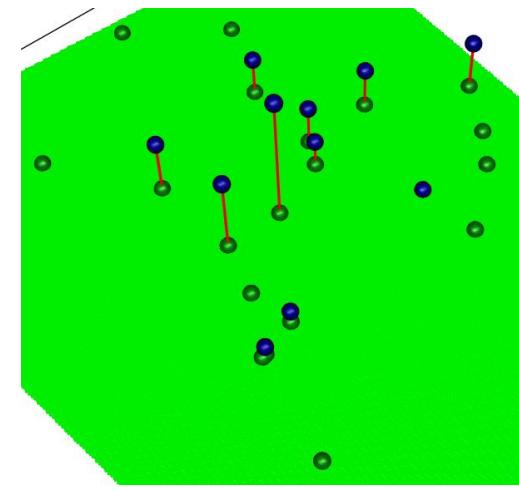
Explained

$$ESS = \sum_{i=1}^n OH'_i^2$$



Residual

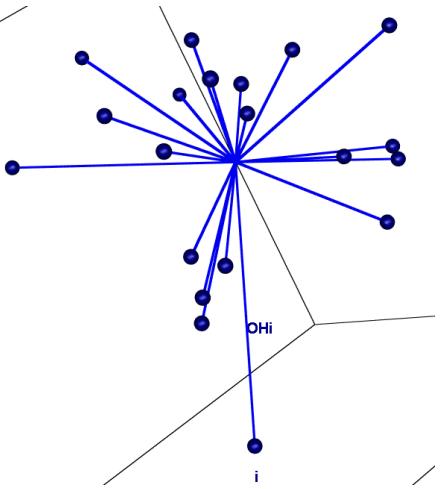
$$RSS = \sum_{i=1}^n HH'_i^2 = TSS - ESS$$



# Diagnostics R2X: How much of the original inertia is still reflected by the model?

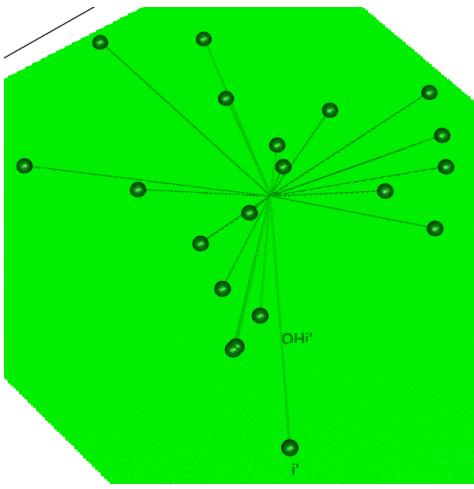
Total

$$TSS = \sum_{i=1}^n OH_i^2$$



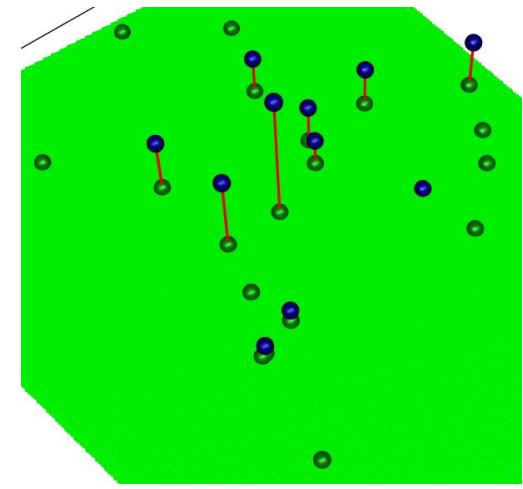
Explained

$$ESS = \sum_{i=1}^n OH'_i^2$$



Residual

$$RSS = \sum_{i=1}^n HH'_i^2 = TSS - ESS$$

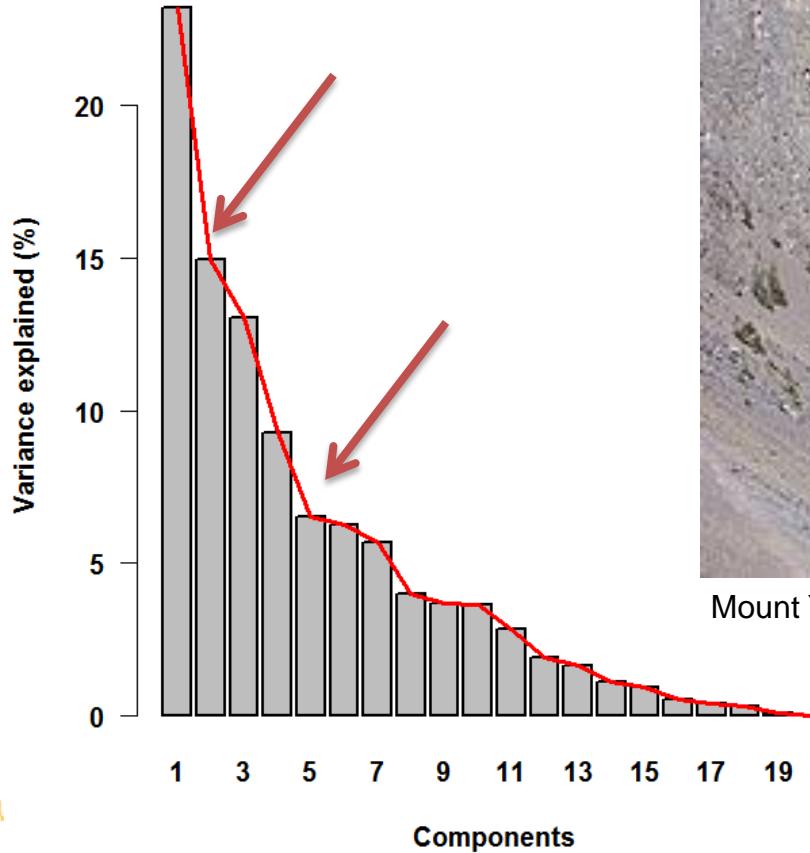


$$R2X = \frac{ESS}{TSS} = 1 - \frac{RSS}{TSS} \quad 0 \leq R2X \leq 1$$

- R2X increases with the number of components in the model
- For a given number of components, the higher the R2X, the more inertia is captured by the model (projection)

# Scree plot

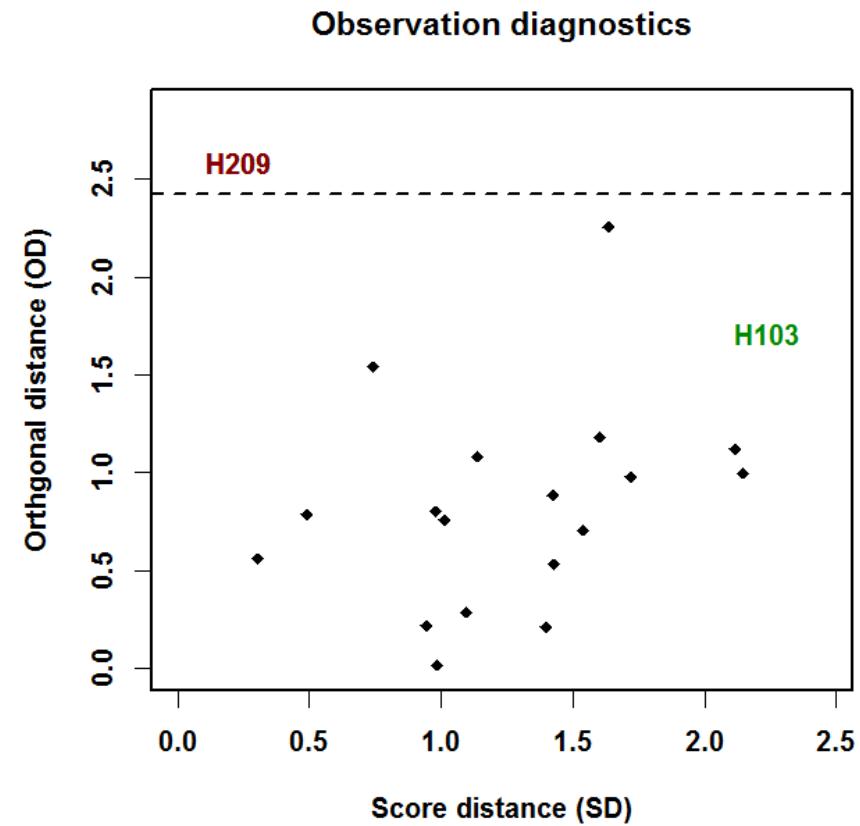
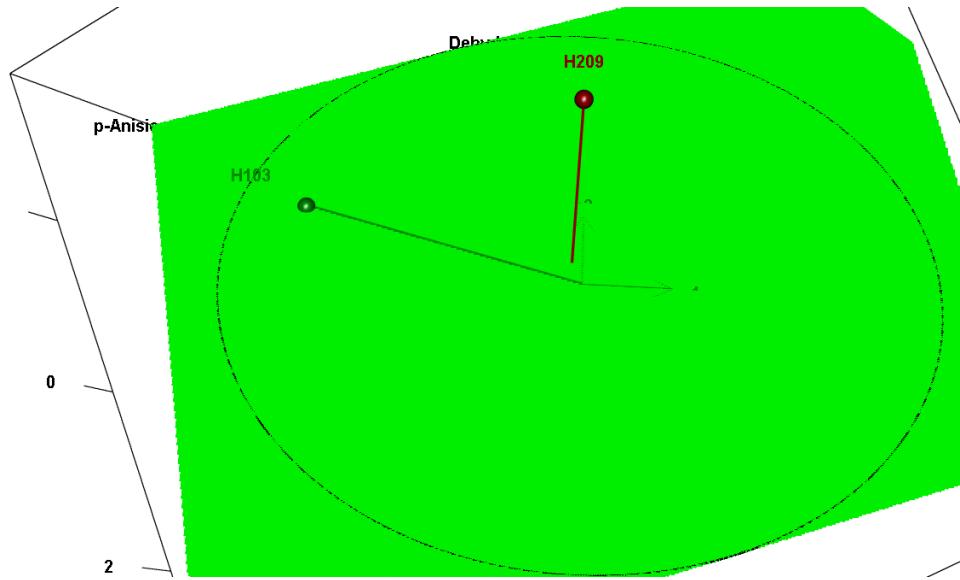
- Check that the first components capture most of the variance



Mount Yammuska, Alberta. Wikipedia

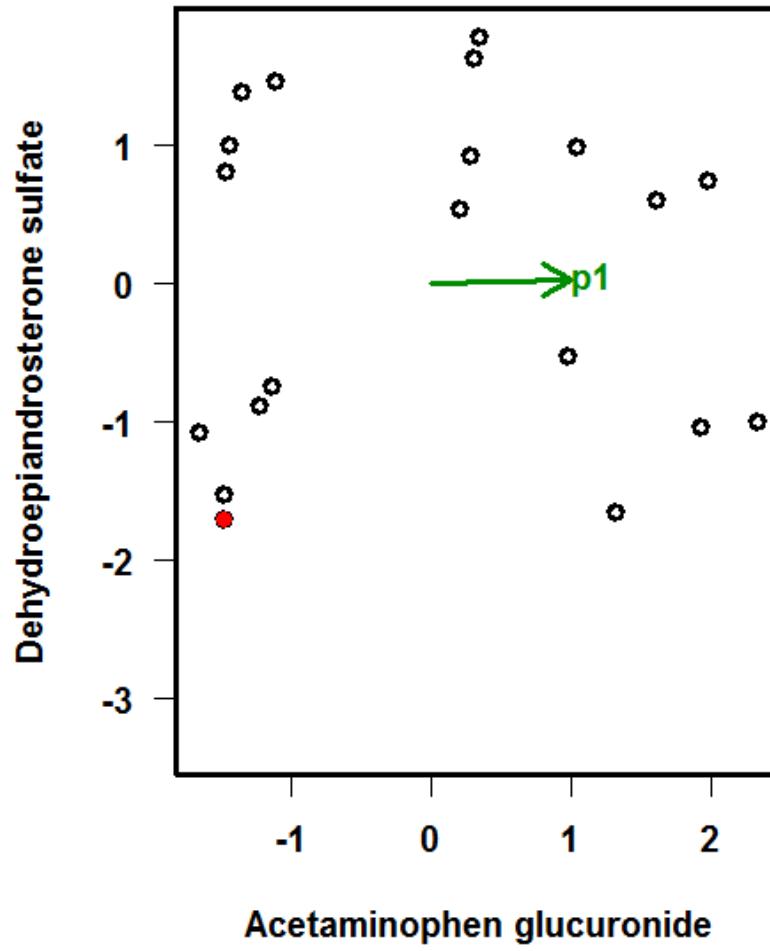
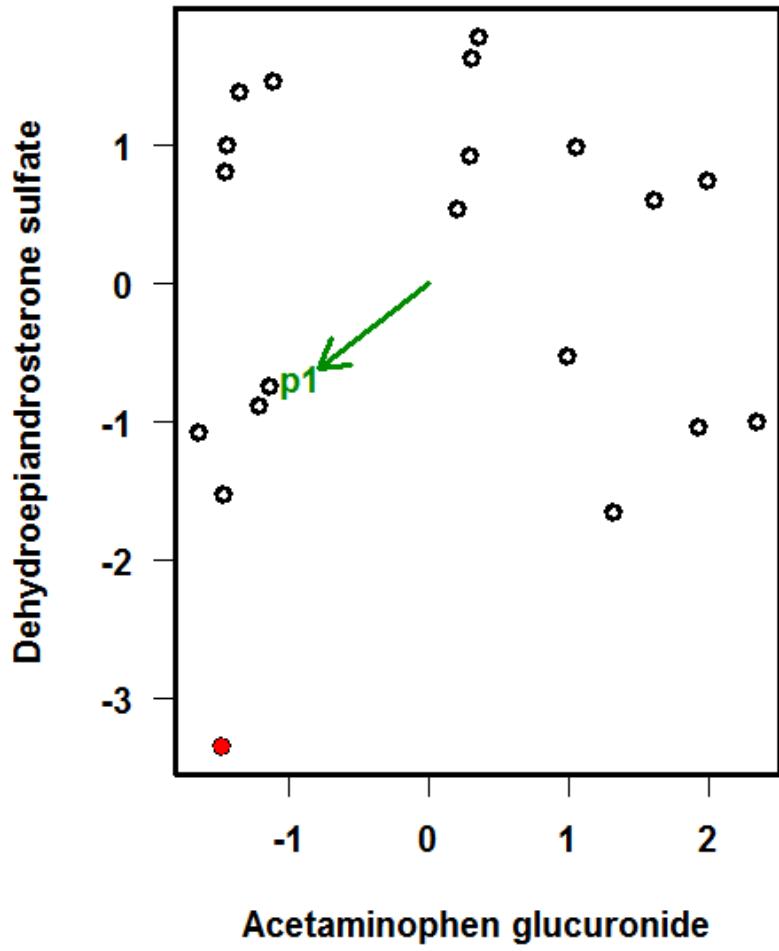
# Observation diagnostics

- Samples which may bias the PCA computation and/or may not be faithfully visualized by the score plot



Hubert M., Rousseeuw P. and Vanden Branden K. (2005). ROBPCA: a new approach to robust principal component analysis. *Technometrics*, 47:64-79. DOI: [10.1198/004017004000000563](https://doi.org/10.1198/004017004000000563)

# Sensitivity to outliers



# Numerical results

- Numerical results (including the percentage of explained inertia) can be viewed in the "information.txt" file

The screenshot shows the Workflow4metabolomics software interface. The main window displays PCA results:

```
PCA ('svd' algorithm)
Number of components: 8

Number of reference observations: 183 (100%)

Correlations between variables and components:
          h1    h2 cor_h1 cor_h2
Salicylic acid      -0.0069 NA -0.028   NA
N-Acetylleucine     0.0015 NA  0.006   NA
Chenodeoxycholic acid isomer 0.0075 NA  0.030   NA
Pyridylacetylglycine 0.1500 NA  0.590   NA
Dimethylguanosine    0.1700 NA  0.670   NA
4-Acetamidobutanoic acid isomer 2 0.1800 NA  0.730   NA
FMNH2                NA -0.17   NA -0.56
Testosterone glucuronide NA -0.16   NA -0.54
6-(carboxymethoxy)-hexanoic acid NA -0.16   NA -0.52
Pyrocatechol sulfate   NA  0.22   NA  0.72
Fumaric acid         NA  0.22   NA  0.74
Pentose              NA  0.24   NA  0.79
```

A green box highlights the "Model overview:" section:

Model overview:
R2X R2X(cum) Iter.
h1 0.149 0.149 0
h2 0.103 0.252 0
h3 0.067 0.319 0
h4 0.043 0.362 0
h5 0.040 0.402 0
h6 0.036 0.438 0
h7 0.035 0.473 0
h8 0.028 0.501 0

Below it, another green box highlights the "Model summary:" section:

Model summary:
R2X(cum) ncp nco
h8 0.501 8 0

The right side of the interface shows the History panel, listing recent datasets:

- 549.3 KB
- 9: Multivariate information.txt
- 8: Multivariate figure.pdf
- 7: Multivariate variableMetadata.tsv
- 6: Multivariate sampleMetadata.tsv
- 5: Multivariate dataMatrix.tsv
- 4: Check Format information.txt
- 3: variableMetadata.tsv
- 2: sampleMetadata.tsv
- 1: dataMatrix.tsv

A green box highlights the entry for "9: Multivariate information.txt".

# Score and loading values

- The score (resp. loading) values of the selected components have been added as columns in the **sampleMetadata** (resp. **variableMetadata**) files

The screenshot shows the Workflow4metabolomics software interface. On the left, there is a table titled "sampleMetadata" with columns: sampleMetadata, age, bmi, gender. A green box highlights the first two columns. To the right of this table is another table titled "variableMetadata" with columns: PCA\_XSCOR-h1, PCA\_XSCOR-h2. A green box highlights the first two columns of this table. On the right side of the interface, there is a "History" panel listing various workflow steps. The steps are numbered 1 through 9 from bottom to top. Step 1 is "1: dataMatrix.tsv". Step 2 is "2: sampleMetadata.tsv". Step 3 is "3: variableMetadata.tsv". Step 4 is "4: Check Format information.txt". Step 5 is "5: Multivariate dataMatrix.tsv". Step 6 is "6: Multivariate sampleMetadata.tsv". Step 7 is "7: Multivariate variableMetadata.tsv". Step 8 is "8: Multivariate figure.pdf". Step 9 is "9: Multivariate information.txt". Each step has a green box around it, and the numbers 1 through 9 are placed in these boxes.

sampleMetadata	age	bmi	gender	PCA_XSCOR-h1	PCA_XSCOR-h2
HU_011	29	19.75	M	-8.74400891504494	0.29249883857013
HU_014	59	22.64	F	-1.86532133217634	0.285366844636407
HU_015	42	22.72	M	-6.74648640072742	-0.561605063374045
HU_017	41	23.03	M	-4.23534187957954	-0.641487554413452
HU_018	34	20.96	M	1.59252091681441	-2.89331923169429
HU_019	35	23.41	M	-1.2535250688467	0.200242710800258
HU_020	59	17.1	M	-5.47756634951485	-0.378911997626029
HU_021	34	23.36	M	1.08538964511728	-4.94025884576605
HU_022	51	28.23	F	-3.66836013881533	5.14176542596851
HU_023	51	29.55	M	-4.66609702458129	-1.17204283780617
HU_024	57	29.86	M	-0.794642666784698	-1.22728974524632
HU_025	53	21.6	M	-2.2313493995232	-2.91021037882818
HU_026	34	23.46	F	-8.79694543308979	-0.000101601980933629
HU_027	37	24.82	M	-7.0432093146523	-1.70548152914905
HU_028	41	23.92	F	-0.443606341382212	-3.16113671135982
HU_029	37	27.78	M	-4.50849252383876	-1.54412237704366
HU_030	49	25.88	M	0.60173477063632	-2.47896644698659
HU_031	25	20.76	M	0.209079981357257	-1.36514244700848
HU_032	38	24.09	F	2.3788535799504	2.08848500995035
HU_033	44	18.36	F	1.87769511456898	2.57155836373107
HU_034	52	23.37	M	-3.22008044172578	2.86622150577896
HU_035	37	20.7	F	3.2801149214796	-1.24975766384474
HU_036	47	29.51	M	-2.47266540217536	4.88240826458344
HU_037	35	25.62	M	-4.74331054976355	-2.89213123664626
HU_038	52	22.72	M	-8.90649077106328	7.54124509052761
HU_039	45	24.9	M	-4.23718132839903	4.62422497226667

# Tuning the parameters

- You can recall the page with your parameters, modify them, and restart the analysis

The screenshot shows the Workflow4metabolomics software interface with several sections and numbered callouts:

- Sample metadata file:** Set to "2: sampleMetadata.tsv".
- Variable metadata file:** Set to "3: variableMetadata.tsv".
- Y Response (for PLS(-DA) and OPLS(-DA) only):** Set to "none".
- Number of predictive components:** Set to "3". (Callout 3)
- Notes:** 1) PCA and PLS(-DA): NA can be selected to get a suggestion of the optimal number of predictive components; 2) OPLS(-DA) modeling: select 1 predictive component.
- Number of orthogonal components (for OPLS(-DA) only):** Set to "0".
- Notes:** 1) PCA and PLS(-DA): keep the default value (0); 2) OPLS(-DA): NA can be selected to get a suggestion of the optimal number of orthogonal components.
- Advanced graphical parameters:** Set to "Use default".
- Advanced computational parameters:** Set to "Use defa". (Callout 4)
- History:** A list of recent files:
  - 9: Multivariate information.txt
  - 8: Multivariate figure.pdf (highlighted with green box, Callout 1)
  - 7: Multivariate variableMetadata.tsv
  - 6: Multivariate sampleMetadata.tsv
  - 5: Multivariate dataMatrix.tsv
  - 4: Check Format in formation.txt
  - 3: variableMetadata.tsv(Callout 2 points to the PDF file entry.)
- Execute:** A button at the bottom left.

# Advanced parameters: Scaling

- Variables are mean-centered for PCA
- By default, they are also unit-variance scaled
  - absence of variance scaling or changing to Pareto scaling can be selected in the advanced computational parameters

The screenshot shows the Workflow4metabolomics software interface. The top navigation bar includes 'omics' (selected), 'Analyze Data', 'Workflow', 'Shared Data', 'Visualization', 'Help', and 'User'. A note at the top states: 'Notes: 1) PCA: keep the default (none); 2) PLS(-DA) and OPLS(-DA): indicate the name of the column of the sample table to be modeled'. The main panel contains several configuration sections:

- Number of predictive components:** A dropdown set to 3.
- Number of orthogonal components (for OPLS(-DA) only):** A dropdown set to 0.
- Advanced graphical parameters:** A dropdown set to 'Use default'.
- Advanced computational parameters:** A dropdown set to 'Full parameter list'.
- Scaling:** A dropdown set to 'pareto'. This section is highlighted with a green box labeled '2'.
- Permutation testing: Number of permutations:** A dropdown set to 0.
- Log10 transformation:** A dropdown set to 'no'.

On the right side, there is a 'History' panel listing various workflow steps with their file names and preview icons. The steps include:

- 9: Multivariate\_inf ormation.txt
- 8: Multivariate\_fi gure.pdf
- 7: Multivariate\_var iableMetadata.tsv
- 6: Multivariate\_sa mpleMetadata.tsv
- 5: Multivariate\_dat aMatrix.tsv
- 4: Check Format\_in formation.txt
- 3: variableMetadata

A green box labeled '1' highlights the 'Advanced computational parameters' dropdown.

# Advanced parameters: Ellipses

- Indicate the column name of `sampleMetadata` to be used

Samples Analyze Data Workflow Shared Data Visualization Help User

Variable metadata file: 3: variableMetadata.tsv

variable x metadata, decimal: ',', missing: NA, mode: character and numerical, sep: tabular

Y Response (for PLS(-DA) and OPLS(-DA) only): none

Notes: 1) PCA: keep the default (none); 2) PLS(-DA) and OPLS(-DA): indicate the name of the column of the sample table to be modeled

Number of predictive components: 3

Notes: 1) PCA and PLS(-DA): NA can be selected to get a suggestion of the optimal number of predictive components; 2) OPLS(-DA) modeling: select 1 predictive component

Number of orthogonal components (for OPLS(-DA) only): 0

Notes: 1) PCA and PLS(-DA): keep the default value (0); 2) OPLS(-DA): NA can be selected to get a suggestion of the optimal number of orthogonal components

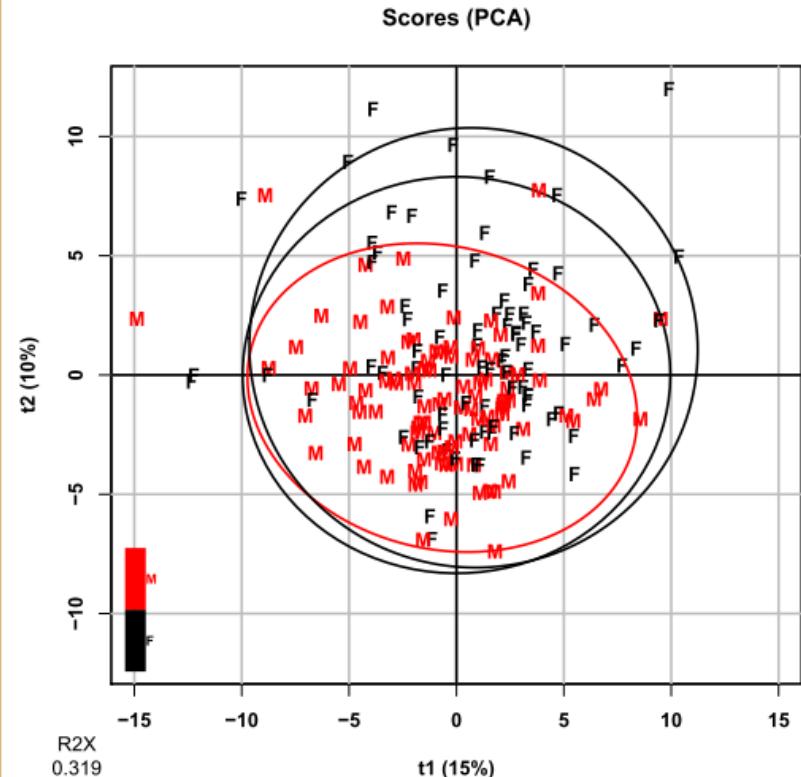
Advanced graphical parameters: Full parameter list 1

Graphic: x-score

Mahalanobis ellipses: gender 2

Notes: Indicate the sample metadata column with the classes to be used for drawing ellipses (for (O)PLS-DA: indicate the same name as the 'Response' argument above); If you do not want ellipses, keep the default, none

Sample colors: none



# References

- Husson F., Le S. and Pages J. (2011). Exploratory multivariate analysis by example using R. *Chapman & Hall/CRC*
- Ringner M. (2008). What is principal component analysis? *Nature Biotechnology*, **26**:303-304.  
<http://dx.doi.org/10.1038/nbt0308-303>
- Baccini A. (2010). Statistique descriptive multidimensionnelle (pour les nuls). [www.math.univ-toulouse.fr/~baccini/zpedago/asdm.pdf](http://www.math.univ-toulouse.fr/~baccini/zpedago/asdm.pdf)



---

4

Wm

Workflow4metabolomics

# PARTIAL LEAST SQUARES REGRESSION (**PLS**) AND DISCRIMINANT ANALYSIS (**PLS-DA**)



# PLS(-DA) modelling

- Powerful regression method when

$$n_{samples} < p_{variables}$$

- **Complementary to univariate hypothesis testing** (where variables are tested independantly)
- **Risk of overfitting:** i.e., building a model whose (apparently) good performances result from chance only



# Supervised analysis (i.e. with labels)

1 response

$p = 30$  (quantitative) variables

$n = 20$  samples

	bmi
H011	19.8
H023	29.6
H033	18.4
H042	19.8
H052	20.1
H062	22.2
H073	25.4
H083	29.8
H092	21.8
H103	26.8
H114	29.4
H124	22.2
H134	22.9
H145	29.1
H157	22.0
H168	20.8
H180	23.7
H189	19.4
H199	21.0
H209	21.5

	1,7-Dimethyluric acid	Dehydroepiandrosterone sulfate
H011	3.33	4.46
H023	4.64	2.81
H033	4.35	2.51
H042	3.91	4.14
H052	4.35	2.55
H062	3.80	2.47
H073	4.00	4.36
H083	4.48	2.02
H092	3.82	4.55
H103	4.08	0.21
H114	4.52	5.17
H124	4.05	4.93
H134	4.27	4.53
H145	4.16	5.33
H157	4.50	4.29
H168	4.01	1.89
H180	4.36	2.67
H189	4.16	3.02
H199	3.46	4.09
H209	4.10	5.00

...

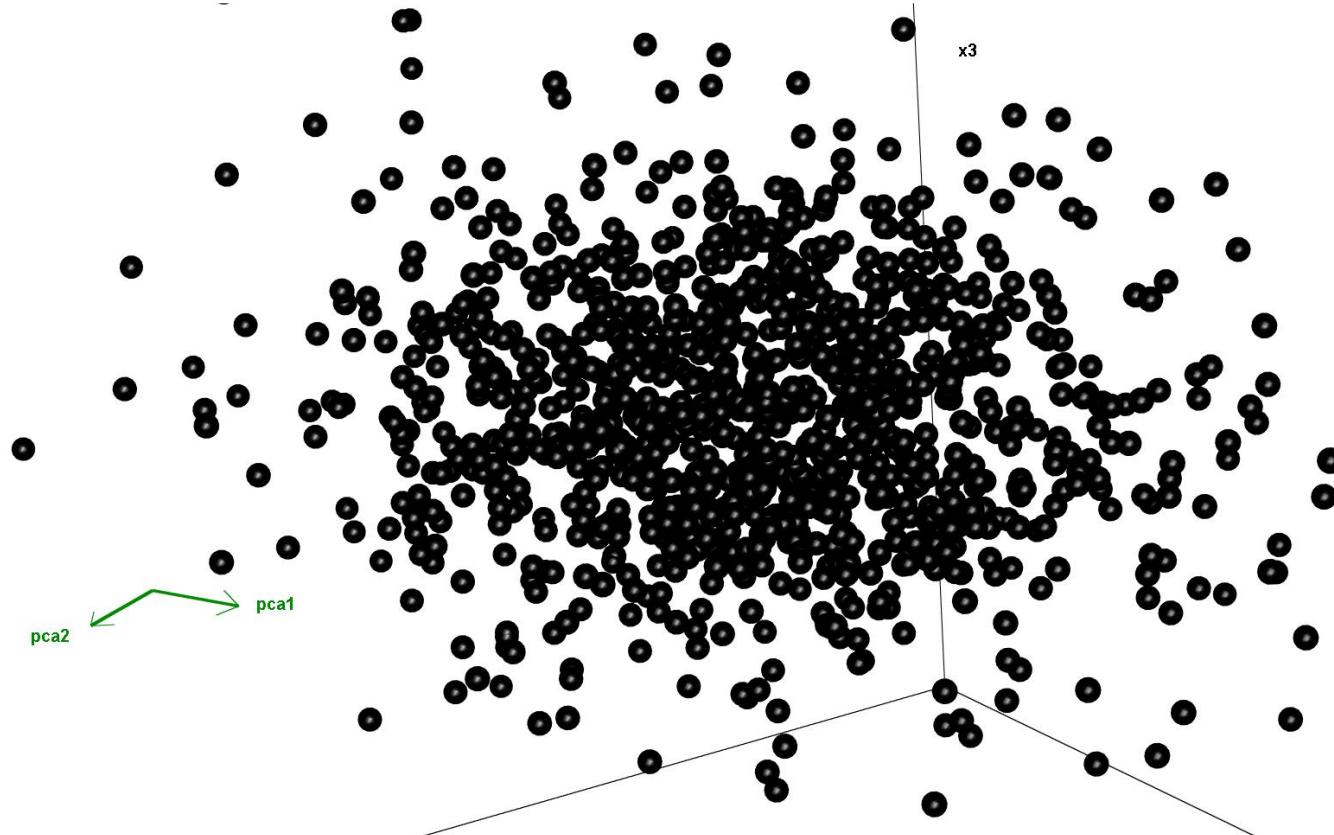
y



X

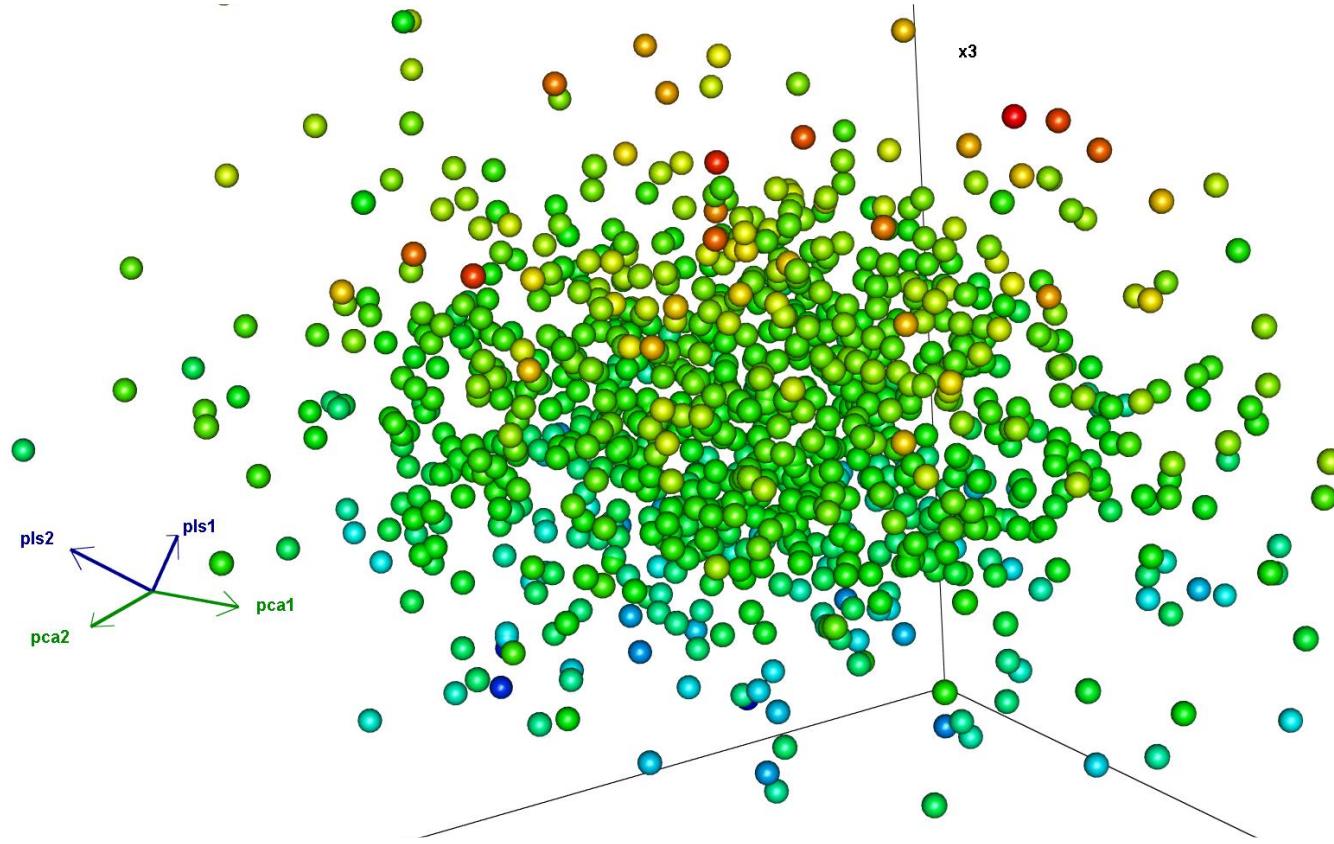
# PLS vs PCA

- PCA finds the directions of maximum variance



# PLS vs PCA

- PLS includes the labels into the model



# Selection of PLS(-DA) as the type of analysis

- Select the "Y response" to be modelled (column of sampleMetadata):
  - column of numbers (age, bmi): **PLS** regression
  - column of characters ('M'/'F', 'patient'/'control'): **PLS-DA** classification

Galaxy / 4 / Metabolomics      Analyze Data      Workflow      Shared Data      Visualization      Help      User

Using 2%

History

multivariate\_example

14 shown, 10 deleted

1.1 MB

14: Multivariate\_i nformation.txt

13: Multivariate\_fi gure.pdf

12: Multivariate\_var iableMetadata.tsv

11: Multivariate\_sa mpleMetadata.tsv

10: Multivariate\_dat aMatrix.tsv

9: Multivariate\_inf ormation.txt

8: Multivariate\_fi gure.pdf

15.1 KB

format: pdf, database: ?

Image in pdf format

7: Multivariate\_var iableMetadata.tsv

6: Multivariate\_sa mpleMetadata.tsv

5: Multivariate\_data

Tools

search tools

Upload File from your computer

Export Data

LC-MS

Format Conversion

Preprocessing

Normalisation

Quality Control

Statistical Analysis

Univariate Univariate statistics

Multivariate PCA, PLS and OPLS

Anova N-way anova. With or Without interactions

ACP ellipsoid by factors

Hierarchical Clustering using ctc R package for java-treeview

Heatmap Heatmap of the dataMatrix

Annotation

GC-MS

Preprocessing

Normalisation

Quality Control

Statistical Analysis

Annotation

NMD

Multivariate (version 2015-04-25)

Data matrix file: 1: dataMatrix.tsv  
variable x sample, decimal: '.', missing: NA, mode: numerical, sep: tabular

Sample metadata file: 2: sampleMetadata.tsv  
sample x metadata, decimal: '.', missing: NA, mode: character and numerical, sep: tabular

Variable metadata file: 3: variableMetadata.tsv  
variable x metadata, decimal: '.', missing: NA, mode: character and numerical, sep: tabular

**Y Response (for PLS(-DA) and OPLS(-DA) only):**  
bmi  
Notes: 1) PCA: keep the default (none); 2) PLS(-DA) and OPLS(-DA): indicate the name of the column of the sample table to be modeled

**Number of predictive components:**  
NA  
Notes: 1) PCA and PLS(-DA): NA can be selected to get a suggestion of the optimal number of predictive components; 2) OPLS(-DA) modeling: select 1 predictive component

**Number of orthogonal components (for OPLS(-DA) only):**  
0  
Notes: 1) PCA and PLS(-DA): keep the default value (0); 2) OPLS(-DA): NA can be selected to get a suggestion of the optimal number of orthogonal components

**Advanced graphical parameters:**  
Use default

**Advanced computational parameters:**  
Use default

Execute

Author Etienne Thevenot (etienne.thevenot@cea.fr)

# Automatic selection of the number of components

- A new component  $h$  is added to the model if:
  - $R^2Y_h \geq 1\%$
  - $Q^2Y_h \geq 0$  (or 5% if  $n_{samples} \leq 100$ )

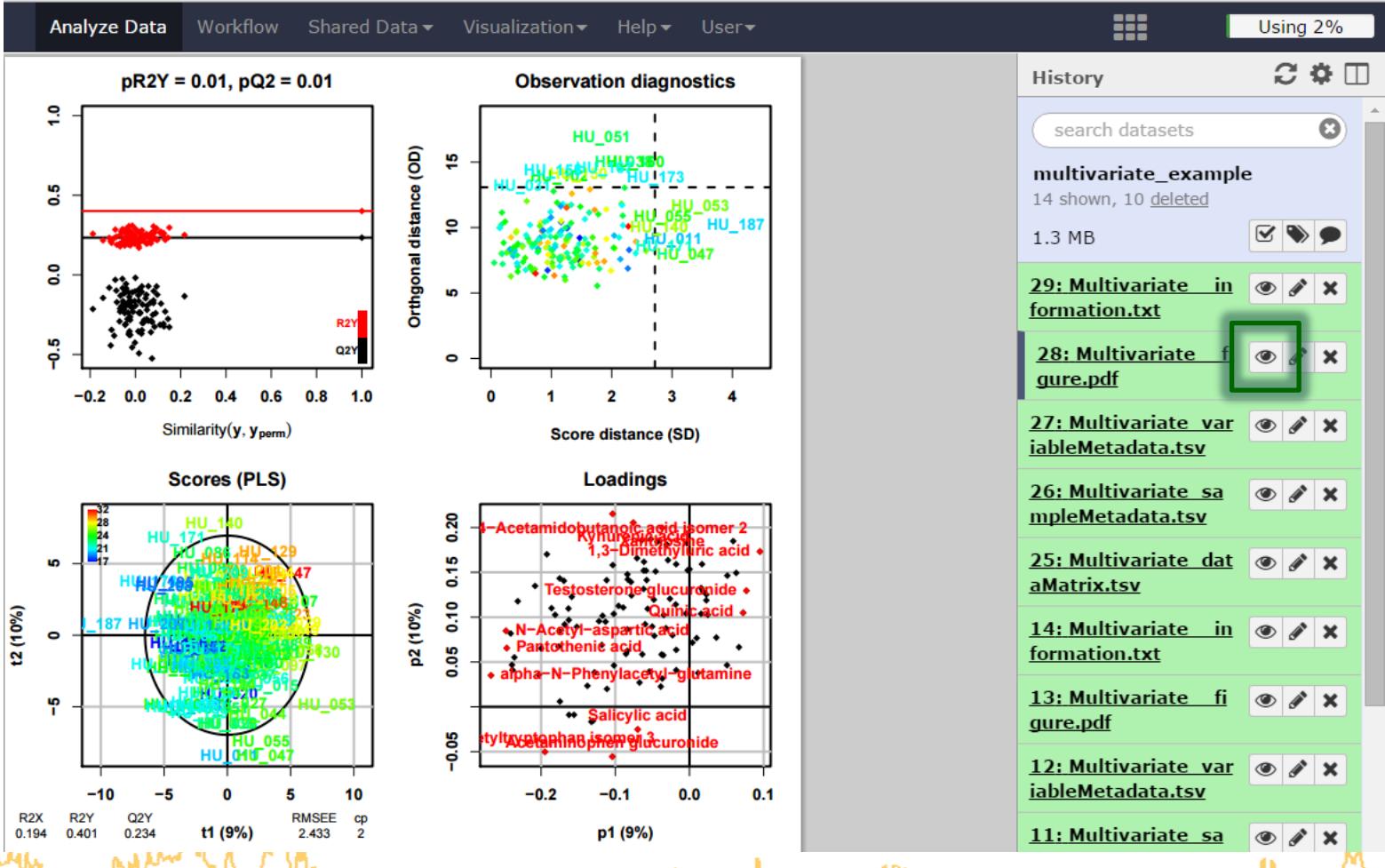
Note:  $Q^2Y_h = 1 - \frac{PRESS_h}{RSS_{h-1}}$  where  $PRESS_h$  is estimated by cross-validation

The screenshot shows the Galaxy platform interface with the following details:

- Header:** Galaxy / 4 / Metabolomics
- Tools Panel:** search tools, Upload File from your computer, Export Data, LC-MS, Format Conversion, Preprocessing, Normalisation, Quality Control, Statistical Analysis, Annotation, GC-MS, Preprocessing, Normalisation, Quality Control, Statistical Analysis, Annotation, NMR, Preprocessing.
- Multivariate Tool Panel:** Data matrix file: 1: dataMatrix.tsv (variable x sample, decimal: '.', missing: NA, mode: numerical, sep: tabular). Sample metadata file: 2: sampleMetadata.tsv (sample x metadata, decimal: '.', missing: NA, mode: character and numerical, sep: tabular). Variable metadata file: 3: variableMetadata.tsv (variable x metadata, decimal: '.', missing: NA, mode: character and numerical, sep: tabular). Y Response (for PLS(-DA) and OPLS(-DA) only): bmi. Number of predictive components: NA (Note: 1) PCA: keep the default (none); 2) PLS(-DA) and OPLS(-DA): indicate the name of the column of the sample table to be modeled. Number of orthogonal components (for OPLS(-DA) only): 0 (Note: 1) PCA and PLS(-DA): 0 can be selected to get a suggestion of the optimal number of orthogonal components; 2) OPLS(-DA) modeling: select 1 predictive component.
- History Panel:** search datasets, multivariate\_example (14 shown, 10 deleted), 1.3 MB, 14: Multivariate\_information.txt, 13: Multivariate\_figure.pdf, 12: Multivariate\_variableMetadata.tsv, 11: Multivariate\_sampleMetadata.tsv, 10: Multivariate\_dataMatrix.tsv, 9: Multivariate\_information.txt, 8: Multivariate\_figure.pdf, 7: Multivariate\_information.txt.
- Bottom Right:** Using 2%

# Graphical results

- permutation, overview, outlier, and score plots displayed as the default ('summary')



# Overfitting



- X:  $20 \times 2,000$  matrix of **random** numbers
  - Uniform distribution between 0 and 1
- Y:  $20 \times 1$  matrix of **random** labels
  - 0 or 1 values

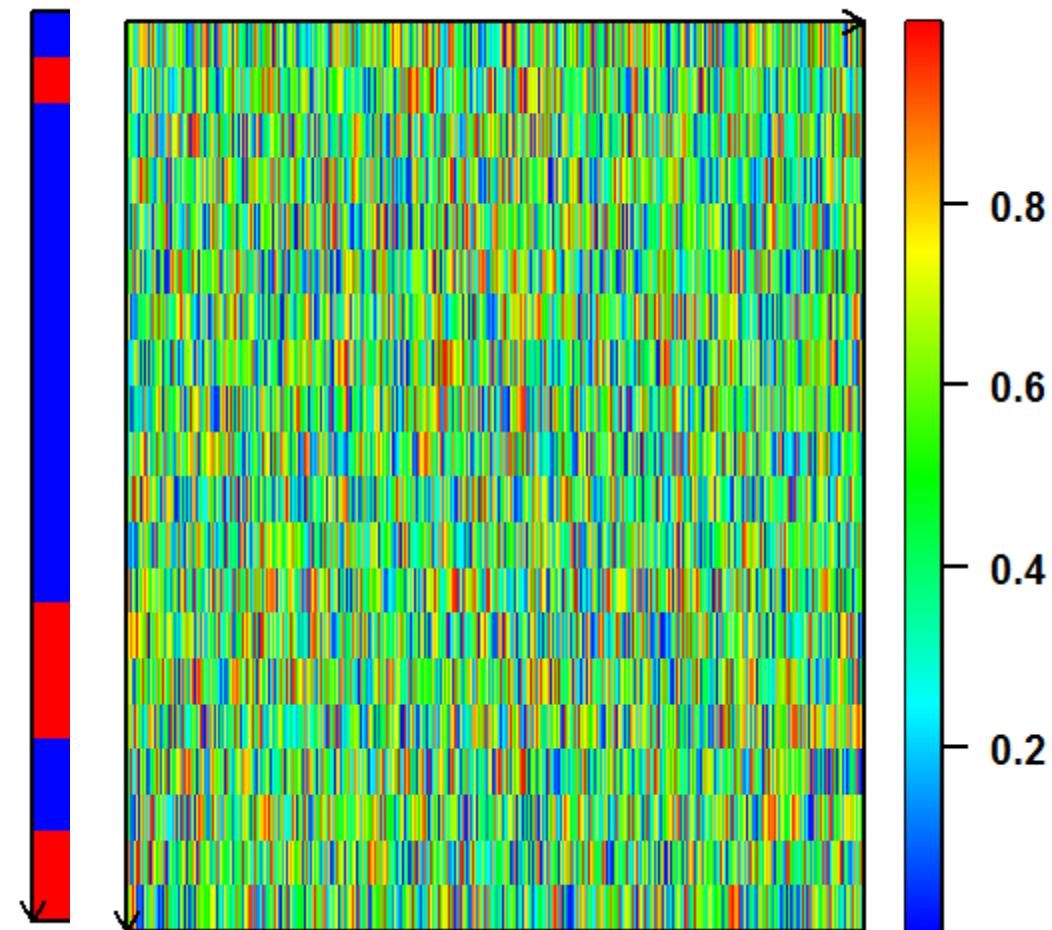
Y random

X random

[1] [1] [2000]

[1]

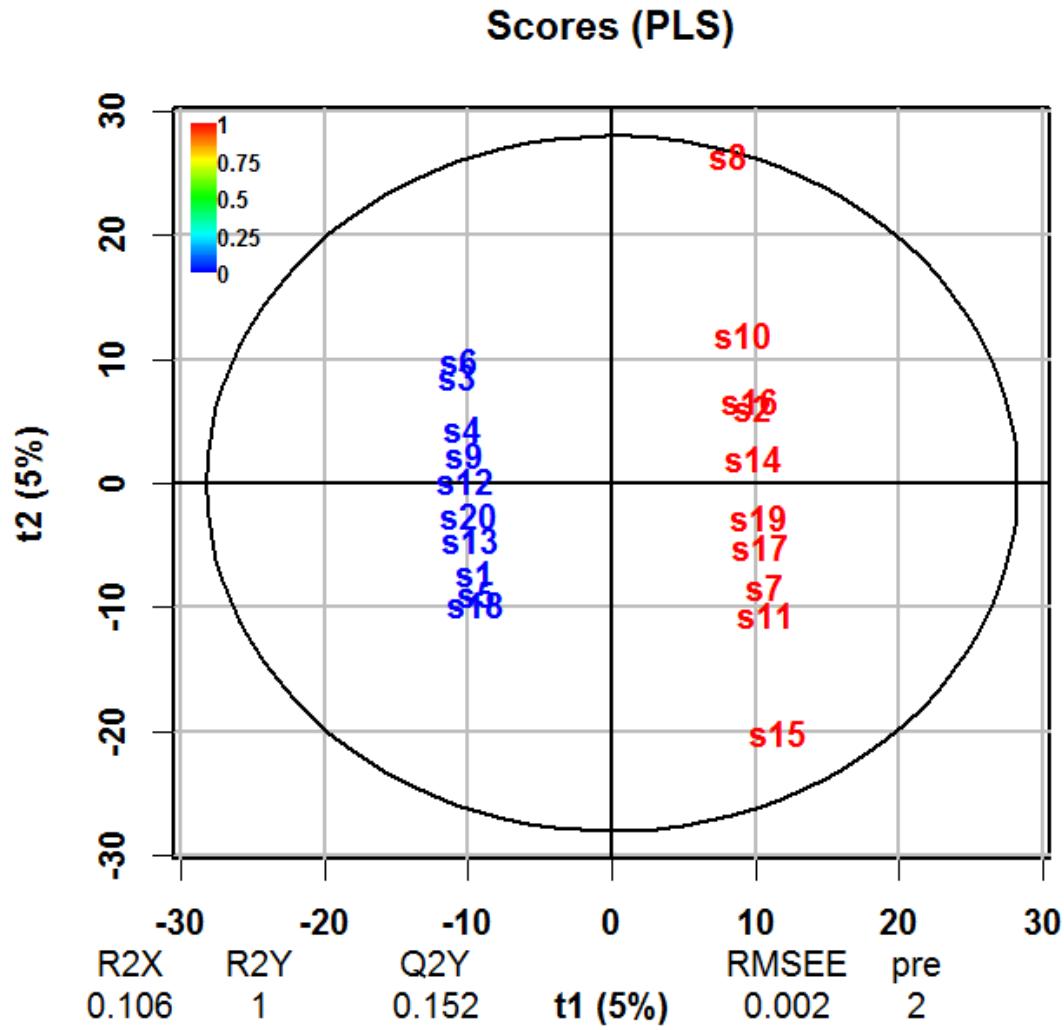
[20]



adapted from Wehrens (2011).  
Chemometrics with R. Springer.



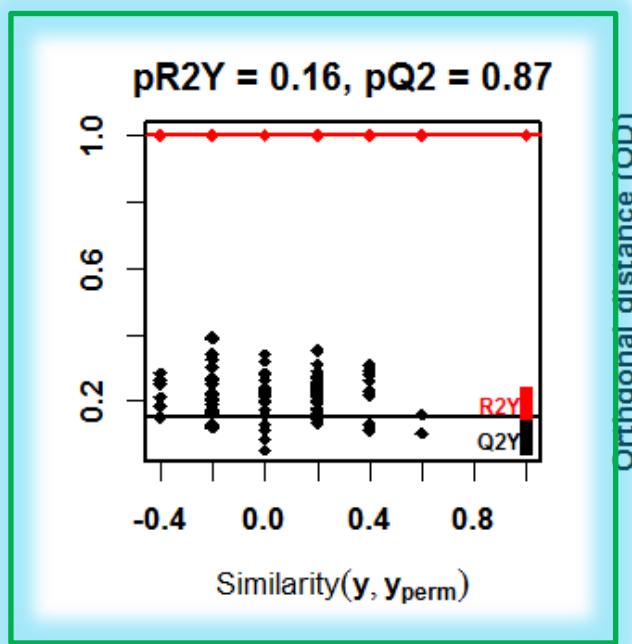
# Score plot!



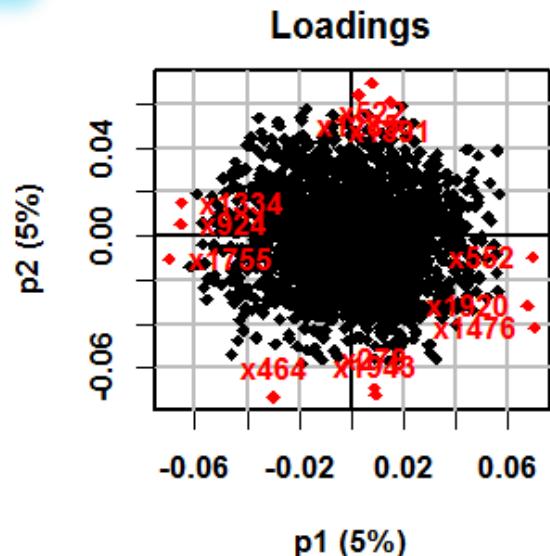
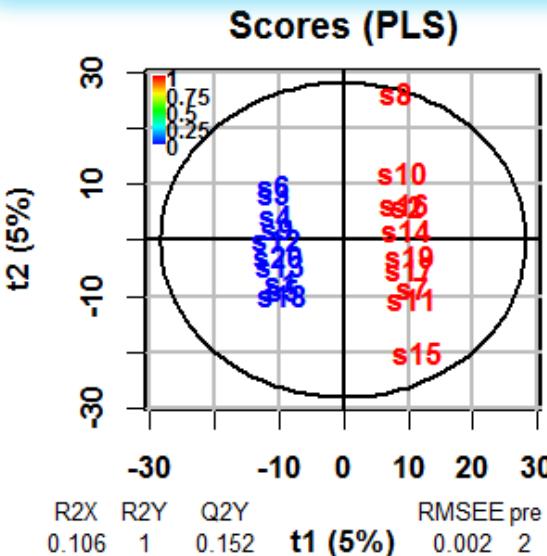
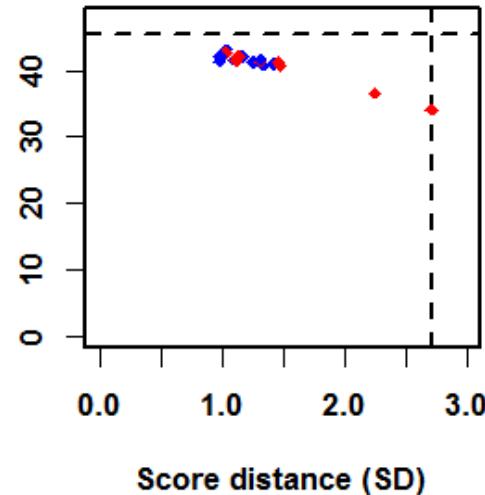
# Importance of diagnostics



- Permutation testing: comparing the R<sub>2Y</sub> and Q<sub>2Y</sub> values of the model built with the true Y labels with  $n_{perm}$  models built with random permutation of Y labels



Observation diagnostics



Szymanska E., Saccenti E., Smilde A. and Westerhuis J. (2012). Double-check: validation of diagnostic statistics for PLS-DA models in metabolomics studies. *Metabolomics*, 8:3-16. DOI: [10.1007/s11306-011-0330-3](https://doi.org/10.1007/s11306-011-0330-3)



# Risk of overfitting when $n < p$



**variables**  
—  
**samples**

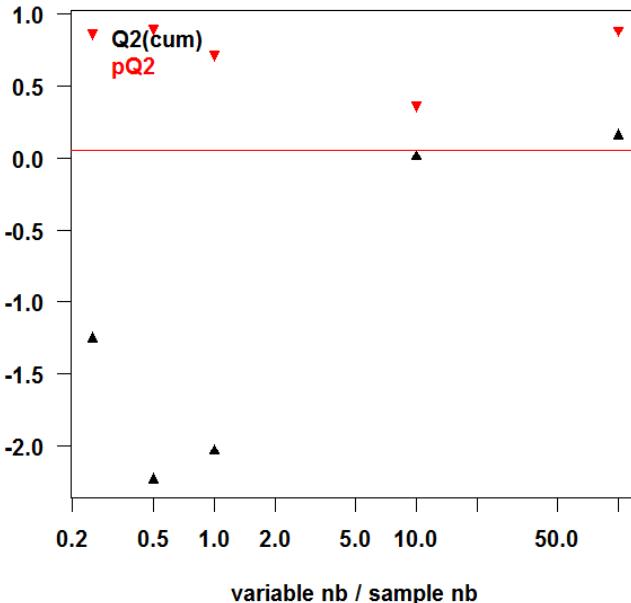
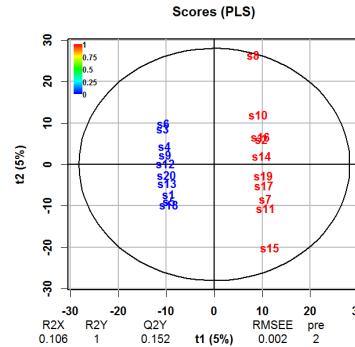
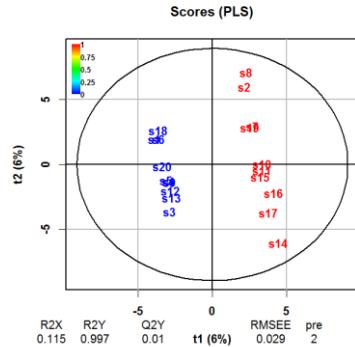
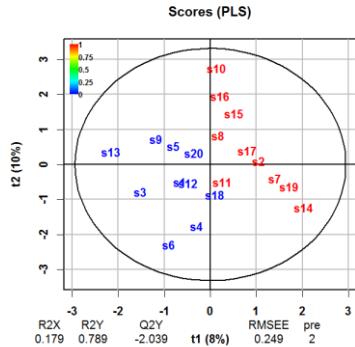
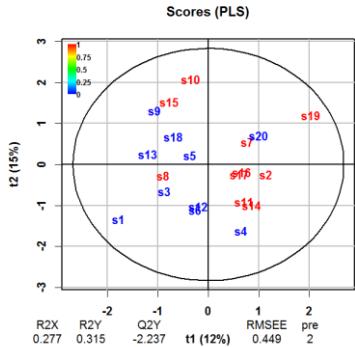
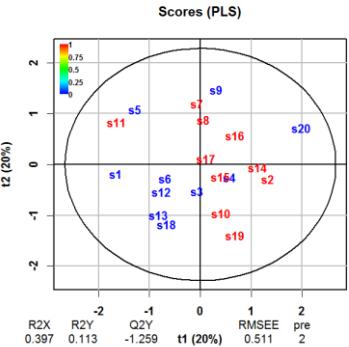
0.2

0.5

1

10

100



# Significance of the model

- The algorithm randomly permutes the **y** labels, builds the models and computes the  $R^2X$ ,  $R^2Y$ ,  $Q^2Y$

1 response

$p = 30$  (quantitative) variables

	bmi
H011	19.8
H023	29.6
H033	18.4
H042	19.8
H052	20.1
H062	22.2
H073	25.4
H083	29.8
H092	21.8
H103	26.8
H114	29.4
H124	22.2
H134	22.9
H145	29.1
H157	22.0
H168	20.8
H180	23.7
H189	19.4
H199	21.0
H209	21.5



	1,7-Dimethyluric acid	Dehydroepiandrosterone sulfate
H011	3.33	4.46
H023	4.64	2.81
H033	4.35	2.51
H042	3.91	4.14
H052	4.35	2.55
H062	3.80	2.47
H073	4.00	4.36
H083	4.48	2.02
H092	3.82	4.55
H103	4.08	0.21
H114	4.52	5.17
H124	4.05	4.93
H134	4.27	4.53
H145	4.16	5.33
H157	4.50	4.29
H168	4.01	1.89
H180	4.36	2.67
H189	4.16	3.02
H199	3.46	4.09
H209	4.10	5.00

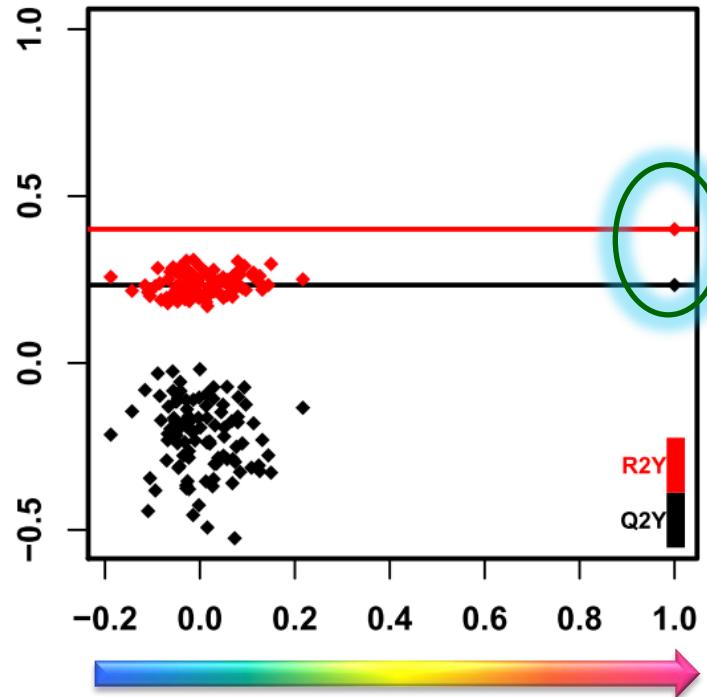
X

...

# Significance of the model

- Counting the number of  $R^2Y$  (and  $Q^2Y$ ) metrics from random models which are superior to the values of the true model gives an indication of the significance of the PLS modelling

$pR^2Y = 0.01, pQ^2 = 0.01$



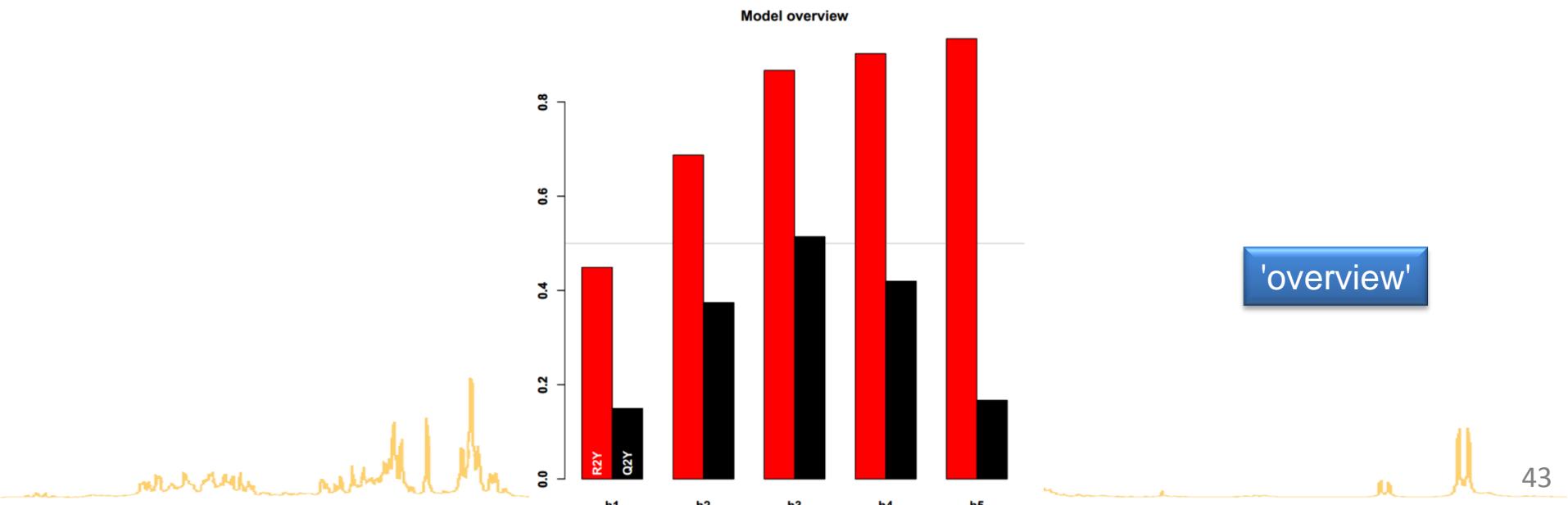
$R^2Y$  and  $Q^2Y$  of the model  
with the true  $y$  values

'permutation'

Similarity between  $y_{true}$  and  $y_{random}$

# Diagnostic metrics

- $0 \leq R^2X \leq 1$ : percentage of X inertia explained by the model
- $0 \leq R^2Y \leq 1$ : percentage of Y inertia explained by the model
- $0 \leq Q^2Y \leq 1$ : estimation of the predictive performance of the model by cross-validation
- $R^2X$  and  $R^2Y$  increase with the number of components while  $Q^2Y$  reaches a maximum (due to overfitting):



# Numerical results

- The details of the  $R2X$ ,  $R2Y$ , and  $Q2Y$  values are stored in the "information.txt" file

olomics Analyze Data Workflow Shared Data ▾ Visualization ▾ Help ▾ User ▾ Using 2%

Y: mean-centering and unit-variance scaling

PLS ('nipals' algorithm)  
Number of predictive components: 3

Number of reference observations: 183 (100%)

Correlations between variables and components:

	h1	h2	cor_h1	cor_h2
alpha-N-Phenylacetyl-glutamine	-0.220	NA	-0.64	NA
Phe-Tyr-Asp (and isomers)	-0.220	NA	-0.63	NA
Glucuronic acid and/or isomers	-0.220	NA	-0.62	NA
Asp-Leu/Ile isomer 1	0.080	NA	0.22	NA
6-(carboxymethoxy)-hexanoic acid	0.097	NA	0.27	NA
Testosterone glucuronide	0.180	NA	0.50	NA
Acetaminophen glucuronide	NA	-0.093	NA	-0.240
p-Anisic acid	NA	-0.066	NA	-0.180
Malic acid	NA	-0.030	NA	-0.078
p-Hydroxymandelic acid	NA	0.200	NA	0.520
1-Methyluric acid	NA	0.200	NA	0.530
Porphobilinogen	NA	0.200	NA	0.530

Model overview:

	R2X	R2X(cum)	R2Y	R2Y(cum)	Q2	Q2(cum)	Signif.	Iter.
h1	0.0984	0.0984	0.4791	0.479	0.401	0.401	R1	1
h2	0.0861	0.1846	0.1892	0.668	0.256	0.555	R1	1
h3	0.0907	0.2752	0.0615	0.730	0.065	0.584	R1	1

Model summary:

	R2X(cum)	R2Y(cum)	Q2(cum)	RMSEE	ncp	nco
h3	0.275	0.73	0.584	0.262	3	0

History

search datasets

multivariate\_example  
14 shown, 10 deleted

2.1 MB

39: Multivariate\_information.txt

38: Multivariate\_figure.pdf

37: Multivariate\_variableMetadata.tsv

36: Multivariate\_sampleMetadata.tsv

35: Multivariate\_dataMatrix.tsv

34: Multivariate\_information.txt

33: Multivariate\_figure.pdf

32: Multivariate\_variableMetadata.tsv



1

# Scores, loadings and VIPs

- The score (resp. loading and VIPs) of the selected components have been added as columns in the **sampleMetadata** (resp. **variableMetadata**) files

The screenshot shows the Workflow4metabolomics software interface. On the left, there is a table of sample metadata with columns for msiLevel, hmdb, and chemicalClass. In the center, there is a table of variable metadata with columns for gender\_PLSDA\_XLOAD-h1, gender\_PLSDA\_XLOAD-h2, and gender\_PLSDA\_VIP. On the right, there is a history panel listing various datasets and files, each with an edit icon and a delete icon. Two specific entries in the history panel are highlighted with green boxes and numbered 1 and 2.

msiLevel	hmdb	chemicalClass
2		Organic
2		AA-peptides
1	HMDB03099	AroHeP:Xenobi
1	HMDB10738	AroHeP
1	HMDB01857	AroHeP
1	HMDB11103	AroHeP
2		AroHoM
1	HMDB00510	AA-peptides
1	HMDB59709	AroHoM
1	HMDB00402	Organic
1	HMDB11723	AA-peptides:AcyGly
1		Lipids
1	HMDB59712	AroHoM
1	HMDB00440	AroHoM
2	HMDB13189	Carbohydrates
1	HMDB00491	Lipids
1	HMDB00459	AA-peptides:AcyGly
1	HMDB02441	Lipids
1	HMDB01336	AroHoM
2		AroHoM
1	HMDB01982	AroHeP
2		Lipids

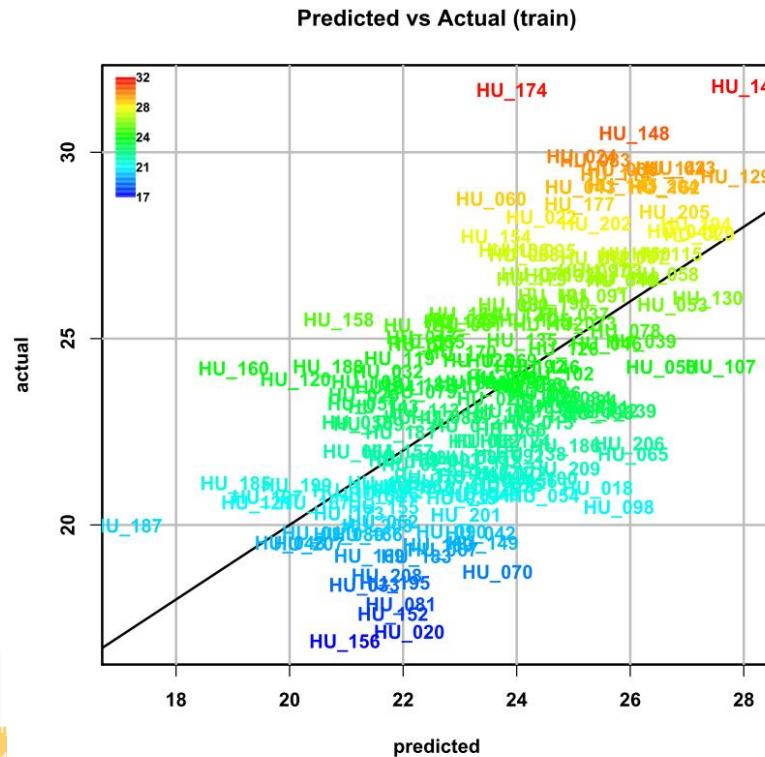
gender_PLSDA_XLOAD-h1	gender_PLSDA_XLOAD-h2	gender_PLSDA_VIP
-0.0398502158539864	-0.0118906818365882	0.413402576648655
0.045506179215717	0.189853829891156	1.48654320826344
-0.0892685224945862	0.200473082255006	0.994358885831879
-0.0925960283984577	0.166237293630931	0.909198577023911
-0.0533869298019096	0.166793890177945	0.703482789417141
-0.105555888603966	0.129654344183481	0.68032554007513
-0.139031345364493	0.0256580978838288	0.930587981757499
-0.123797451802098	0.122573314497015	0.901219803935142
-0.0859289153376191	0.080533734055351	0.550144194269479
-0.00500169475467362	0.164041655306413	1.1135503438424
-0.146406017195434	0.00205394318915884	1.15042106154043
-0.00866480699319381	0.117644113800042	0.543551532664842
-0.0550063618628605	0.0437260467146582	0.65956729426584
-0.0910480750747919	0.0263696450305611	0.594653447171177
-0.00243590621997017	0.0588028800259373	0.747217045999356
0.0464961899862177	0.112804940847864	0.820925594575721
-0.128640803025914	0.0765010378278105	0.879948860811061
-0.0572183256960898	0.113224239823584	0.495244006648848
-0.0760295060324308	0.0379713701648879	0.754733936526486
-0.137003034145239	0.0383124974603868	1.0070259405318
-0.0287380299762852	0.179401841616721	0.797138454685613
-0.043696294430725	0.18755264988441	0.737596864407318

History:

- multivariate\_example (29 shown, 10 deleted)
- 39: Multivariate\_information.txt
- 38: Multivariate\_figure.pdf
- 37: Multivariate\_variableMetadata.tsv
- 36: Multivariate\_sampleMetadata.tsv
- 35: Multivariate\_dataMatrix.tsv
- 34: Multivariate\_information.txt
- 33: Multivariate\_figure.pdf

# Advanced parameters: Graphics

- Several types of graphics are available:
    - e.g., predict-train and predict-test (the latter being available only if the train/test partition has been selected)



## 'predict-train'

# PLS-DA

- The two response levels are encoded as numbers

**Qualitative**

	gender
H011	M
H023	M
H033	F
H042	M
H052	F
H062	M
H073	M
H083	M
H092	M
H103	M
H114	M
H124	M
H134	M
H145	M
H157	F
H168	F
H180	F
H189	F
H199	M
H209	F

**Quantitative**

	gender
HU_017	0.5
HU_028	0.5
HU_034	-0.5
HU_051	0.5
HU_060	-0.5
HU_078	0.5
HU_091	0.5
HU_093	0.5
HU_099	0.5
HU_110	0.5
HU_130	0.5
HU_134	0.5
HU_138	0.5
HU_149	0.5
HU_152	-0.5
HU_175	-0.5
HU_178	-0.5
HU_185	-0.5
HU_204	0.5
HU_208	-0.5

**Quantitative**

	gender
H011	0.40
H023	0.10
H033	-0.61
H042	0.39
H052	-0.47
H062	0.46
H073	0.36
H083	0.11
H092	0.47
H103	0.23
H114	0.25
H124	0.56
H134	0.12
H145	0.93
H157	-0.19
H168	-0.49
H180	-0.20
H189	0.00
H199	0.54
H209	0.05

**Qualitative**

	pred
H011	M
H023	M
H033	F
H042	M
H052	F
H062	M
H073	M
H083	M
H092	M
H103	M
H114	M
H124	M
H134	M
H145	M
H157	F
H168	F
H180	F
H189	M
H199	M
H209	M

**n = 20 samples**



**PLS**



**y**

**y**

**y<sub>fitted</sub>**

**y<sub>fitted</sub>**

# PLS-DA

- Automatically selected when the response is qualitative (i.e. the column of **sampleMetadata** only contains characters)

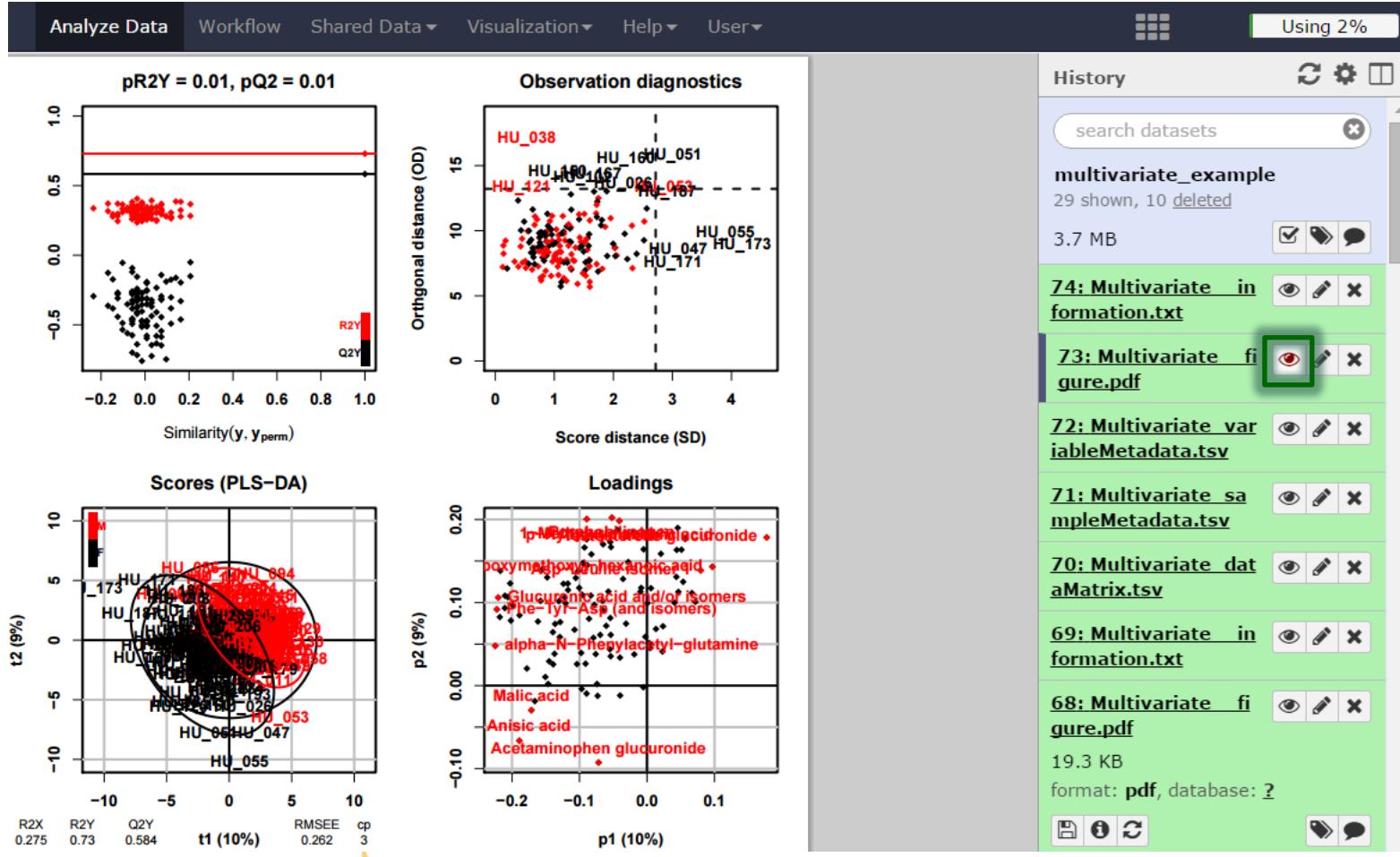
The screenshot shows the Workflow4metabolomics software interface with the following details:

- Multivariate (version 2015-04-25)** tab is active.
- Data matrix file:** 1: dataMatrix.tsv (variable x sample, decimal: '.', missing: NA, mode: numerical, sep: tabular).
- Sample metadata file:** 2: sampleMetadata.tsv (sample x metadata, decimal: '.', missing: NA, mode: character and numerical, sep: tabular).
- Variable metadata file:** 3: variableMetadata.tsv (variable x metadata, decimal: '.', missing: NA, mode: character and numerical, sep: tabular).
- Y Response (for PLS(-DA) and OPLS(-DA) only):** gender (highlighted with a green box).
- Number of predictive components:** NA (highlighted with a green box). Notes: 1) PCA, keep the default (none); 2) PLS(-DA) and OPLS(-DA): indicate the name of the column of the sample table to be modeled.
- Number of orthogonal components (for OPLS(-DA) only):** 0 (highlighted with a green box). Notes: 1) PCA and PLS(-DA): NA can be selected to get a suggestion of the optimal number of predictive components; 2) OPLS(-DA) modeling: select 1 predictive component.
- History:** A list of recent datasets:
  - multivariate\_example (29 shown, 10 deleted, 3.7 MB)
  - 74: Multivariate\_information.txt
  - 73: Multivariate\_figure.pdf
  - 72: Multivariate\_variableMetadata.tsv
  - 71: Multivariate\_sampleMetadata.tsv
  - 70: Multivariate\_dataMatrix.tsv
  - 69: Multivariate\_information.txt
  - 68: Multivariate\_figure.pdf (19.3 KB)



Warning: Use balanced datasets (similar proportions of samples in each of the two classes)

# PLS-DA



---

4

Wm

Workflow4metabolomics

# ORTHOGONAL PARTIAL LEAST SQUARES REGRESSION (**OPLS**) AND DISCRIMINANT ANALYSIS (**OPLS-DA**)



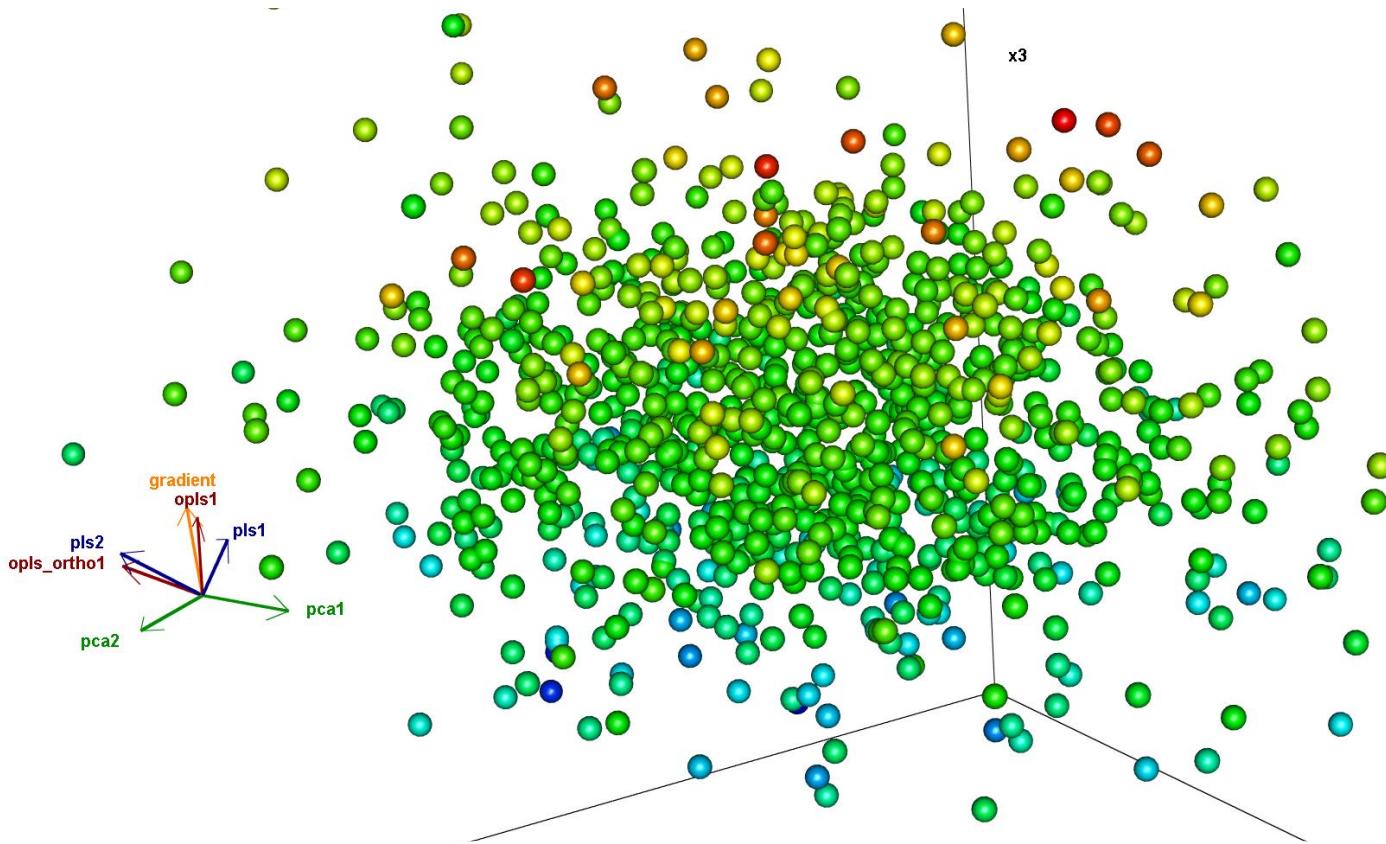
# Principles

- Separately models the variations of the predictors correlated and orthogonal to the response
- Improves the interpretation of the components but not the overall predictive performance of the model
- Only one predictive component required for single response models
- Note: As with PLS, care should be taken to avoid too many (orthogonal) components (which would result in overfitting)



# OPLS vs PLS

- Variation not correlated to the response (e.g., technical bias) is modelled separately by the orthogonal component(s)
- => The first predictive component is strongly correlated to the response



# Selection of OPLS(-DA) as the type of analysis

- Set the number of predictive component to 1
- Select the number of orthogonal components (e.g., NA)

Galaxy / 4 / Metabolomics      Analyze Data      Workflow      Shared Data ▾      Visualization ▾      Help ▾      User ▾

History      search datasets      multivariate\_example  
29 shown, 10 deleted  
2.6 MB

Multivariate (version 2015-04-25)

Data matrix file: 1: dataMatrix.tsv  
variable x sample, decimal: '.', missing: NA, mode: numerical, sep: tabular

Sample metadata file: 2: sampleMetadata.tsv  
sample x metadata, decimal: '.', missing: NA, mode: character and numerical, sep: tabular

Variable metadata file: 3: variableMetadata.tsv  
variable x metadata, decimal: '.', missing: NA, mode: character and numerical, sep: tabular

Y Response (for PLS(-DA) and OPLS(-DA) only): bmi

Notes: 1) PCA: keep the default (none); 2) PLS(-DA) and OPLS(-DA): indicate the name of the column of the sample table to be modeled.

Number of predictive components: 1

Notes: 1) PCA and PLS(-DA): NA can be selected to get a suggestion of the optimal number of predictive components; 2) OPLS(-DA) modeling: select 1 predictive component.

Number of orthogonal components (for OPLS(-DA) only): NA

Notes: 1) PCA and PLS(-DA): keep the default value (0); 2) OPLS(-DA): NA can be selected to get a suggestion of the optimal number of orthogonal components

Advanced graphical parameters: Use default

Advanced computational parameters: Use default

Execute

Tools

search tools

Upload File from your computer

Export Data

LC-MS

Format Conversion

Preprocessing

Normalisation

Quality Control

Statistical Analysis

Annotation

GC-MS

Preprocessing

Normalisation

Quality Control

Statistical Analysis

Univariate Univariate statistics

Multivariate PCA, PLS and OPLS

Anova N-way anova. With or Without interactions

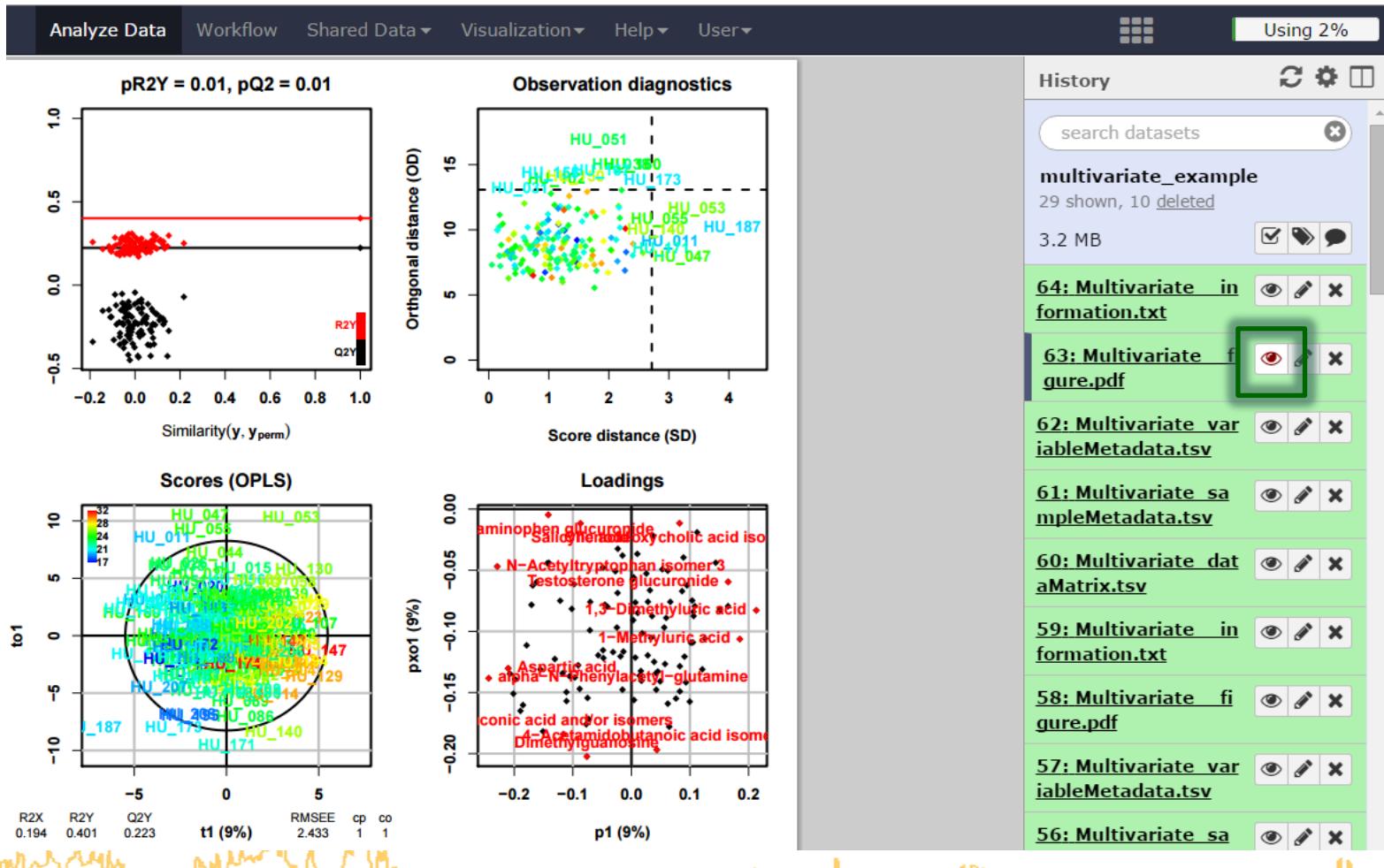
ACP ellipsoid by factors

Hierarchical Clustering using ctc R package for java-treeview

Heatmap Heatmap of the dataMatrix

# Graphical results

- permutation, overview, outlier, and score plots displayed as the default ('summary')



# Numerical results

- The details of the  $R^2X$ ,  $R^2Y$ , and  $Q^2Y$  values are stored in the "information.txt" file

**olomics** Analyze Data Workflow Shared Data ▾ Visualization ▾ Help ▾ User ▾ Using 2%

Max. : 4.804 Max. : 5.428 Max. : 5.56739

X: mean-centering and unit-variance scaling

Number of Y variables: 1

Y: mean-centering and unit-variance scaling

OPLS ('nipals' algorithm)

Number of orthogonal components: 1

Number of predictive components: 1

Number of reference observations: 183 (100%)

Correlations between variables and components:

	h1	o1	cor_h1	cor_o1
alpha-N-Phenylacetyl-glutamine	-0.24	NA	-0.54	NA
N-Acetyltryptophan isomer 3	-0.23	NA	-0.51	NA
Aspartic acid	-0.21	NA	-0.47	NA
Testosterone glucuronide	0.17	NA	0.37	NA
1-Methyluric acid	0.19	NA	0.41	NA
1,3-Dimethyluric acid	0.21	NA	0.47	NA
Dimethylguanosine	NA	-0.2000	NA	-0.680
4-Acetamidobutanoic acid isomer 2	NA	-0.2000	NA	-0.660
Gluconic acid and/or isomers	NA	-0.1800	NA	-0.610
Salicylic acid	NA	-0.0120	NA	-0.039
Chenodeoxycholic acid isomer	NA	-0.0120	NA	-0.039
Acetaminophen glucuronide	NA	-0.0047	NA	-0.016

Model overview:

	R2X	R2X(cum)	R2Y	R2Y(cum)	Q2	Q2(cum)	Signif.
h1	0.0930	0.0930	0.285	0.285	0.1796	0.1796	R1
rot	-0.0396	0.0534	NA	0.401	NA	0.2232	<NA>
o1	0.1410	0.1410	0.116	0.116	0.0436	0.0436	R1
sum	NA	0.1944	NA	0.401	NA	0.2232	<NA>

Model summary:

	R2X(cum)	R2Y(cum)	Q2(cum)	RMSEE	ncp	nco
sum	0.194	0.401	0.223	2.43	1	1

History

search datasets

multivariate\_example  
29 shown, 10 deleted  
3.2 MB

64: Multivariate information.txt

63: Multivariate figure.pdf

62: Multivariate variableMetadata.tsv

61: Multivariate sampleMetadata.tsv

60: Multivariate dataMatrix.tsv

59: Multivariate information.txt

58: Multivariate figure.pdf

57: Multivariate variableMetadata.tsv

56: Multivariate sampleMetadata.tsv

55: Multivariate dataMatrix.tsv

54: Multivariate information.txt

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