

# Image Stitching - a Brief Review

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# Overview

1 Image Stitching Basics

2 Novel Methods

3 References

# Image Stitching Basics

# Motivation

## Image Stitching and Geo-correction

- Large scale ( $\sim 7000 - 10000$ )
- Low overlap (30% horizontally, 9% vertically)
- Geo-Referencing is important
- Commercial softwares break



# Image Stitching

**Image Alignment and Stitching:** Process of finding geometric relation between overlapping images and generating a final image with larger field of view by mosaicing and blending the individual images into a specific frame.

- Image acquisition platforms
  - Hand-held cameras
  - Satellite Imagery
  - Aerial Imagery
  - Drone Imagery
  - Ground Vehicles
- Applications
  - Remote Sensing
  - Agriculture management
  - Disaster management
  - Panorama generation

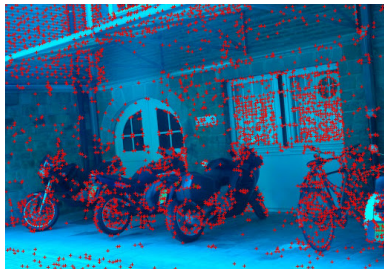
# Image Stitching Components

- Keypoint/Feature Detection
- Keypoint/Feature Correspondence Calculation (Matching)
- Transformation Estimation
  - Intensity based
  - Feature based
- Image Alignment
- Image Warping and Stitching
- Image Blending and Seamless Stitching

# Keypoint/Feature Detection

Visually important points on the image.

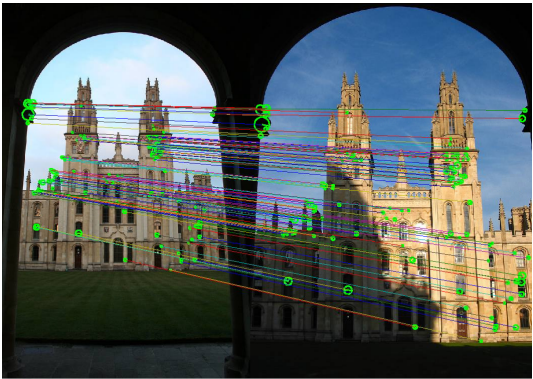
- HARRIS
- SIFT
- SURF



# Keypoint/Feature Matching

## Finding Correspondences

- KNN
- Voronoi diagrams + Cross correlation





# Transformation Estimation

Geometric relation of images depends on many things:

- Homography (Perspective Projection)
  - Scene is planar (or far away)
  - Camera rotating around optical center
- Similarity
  - Leveled camera (no tilting)
- Translation

# Transformation Estimation

- Using correspondences to estimate transformation
  - Simple LSQ
- Be robust to outliers
  - RANSAC
  - BAY-SAC

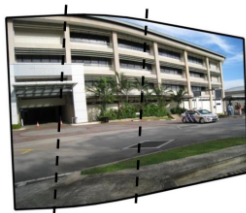
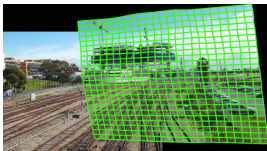
# Transformation Estimation

More complex warps and transformations

- Address the non-planar scenes
- Parallax effects

Warps:

- As-projective-as-possible
- Shape-preserving half-projective



# Image Alignment

**Major challenge in stitching multiple images:** Accumulation of minor errors → Drift. Can be solved by:

- Global alignment (such as bundle adjustment)
- Incorporating prior knowledge

# Image Blending and Seamless Stitching

Generate visually pleasant mosaics:

- Seamless Stitching
  - Graph cut method
- Blending techniques
  - Linear averaging
  - Multi-band blending



# Multiple Image Alignment

- Image stitching is a difficult field to be innovative in.
- Noticeable number of papers only make the previous methods fancier (my point of view).

# Multiple Image Alignment

Already discussed:

- Automatic panoramic image stitching using invariant features (Brown and Lowe)
- MGRAPH: A Multigraph Homography Method to Generate Incremental Mosaics in Real-Time From UAV Swarms

In this presentation:

- Image mosaicing using sequential bundle adjustment
- A Novel Adjustment Model for Mosaicking Low-Overlap Sweeping Images
- Natural Image Stitching with the Global Similarity Prior
- Robust UAV Thermal Infrared Remote Sensing Images Stitching Via Overlap-Prior-Based Global Similarity Prior Model

# Sequential Bundle Adjustment

## Image mosaicing using sequential bundle adjustment

- Relatively an old paper.
- First paper that suggests using bundle adjustment to do image stitching (not 3D reconstruction).
- Initial and approximate orientation of the images need to be given manually.
- They show how to do bundle adjustment using points as well as lines as features.
- Key point or line locations are found by using corner detection and Hough transform respectively.
- RANSAC and initial homographies used to find correspondences.
- Variable State Dimension Filter (VSDF) is used to solve bundle adjustment.



# Sequential Bundle Adjustment

- Bundle adjustment

$$f(x) = \frac{1}{2} \sum_i \Delta Z_i(X)^\top W_i \Delta Z_i(X)$$

$$\Delta Z_i(X) = \underline{Z}_i - Z_i(X)$$

- $Z_i = Z_i(X)$ : predicted value of the feature  $i$  corresponding to the observation from parameters  $X$ .
- $\underline{Z}_i$ : observed value of feature  $i$ .
- $W_i$ : some weights.
- Solve the optimization formula

# Sequential Bundle Adjustment

## Variable State Dimension Filter (VSDF)

- Uses Levenberg Marquardt algorithm
- Updates the state vector iteratively

# Mosaicking of Low-Overlap Images

## A Novel Adjustment Model for Mosaicking Low-Overlap Sweeping Images

- This paper makes the best use of available prior knowledge.
- Works on UAV images.
- Stitching error source:
  - Camera parameters
  - Exterior orientation of the UAV
  - Projection plane in the object space
- Parameters are separated and a new error model is defined based on these error groups.
- Projection is defined by using the lat, lon, orientation(compass), pitch, yaw, and role.
- Optimization function using this error model is minimized.

# Mosaicking of Low-Overlap Images

Projection is defined as:

$$v = H_e P V \quad (1)$$

- Inputs/known parameters:
  - $v$  is the image point
  - $P$  is the projective matrix. (calculated using the given camera parameters and exterior orientation parameters)
- Outputs/Unknown parameters:
  - $H_e$  is the error homograph (error model)
  - $V$  is the 3D scene point

# Mosaicking of Low-Overlap Images

Error model: built as a homograph

$$H_e = (H_{e3}H_{e2}H_{e1})^{-1} \quad (2)$$

- $H_{e1}$ : Camera parameter error. Scale and translation.
- $H_{e2}$ : Projection plane error. (?)
- $H_{e3}$ : Exterior Orientation Error. Accounts for the error in GPS, compass information and tilts (pitch, yaw and roll).

Optimization is done by an approach similar to that of bundle adjustment (nonlinear least squares).

# Global Similarity Prior Model

## Natural Image Stitching with the Global Similarity Prior

- The proposed method is built the as-projective-as-possible paper.
- They use a mesh deformation approach to align, warp and stitch images.
- An optimization function made up of global and local alignment terms is defined and minimized to find the alignment and warping parameters.

# Global Similarity Prior Model

## Steps:

- SIFT features are detected. APAP is used to define the grid and locally align the overlapping images.
- The warped mesh from APAP is considered. The vertexes of this mesh are the new matched points which are used in this method.
- An energy function is defined which consists of the following components:
  - Alignment Term:  $\Psi_a$
  - Local Similarity Term:  $\Psi_l$
  - Global Similarity Term:  $\Psi_g$

# Global Similarity Prior Model

Alignment Term:

- Ensures the alignment quality after deformation between the images.
- Equation:

$$\Psi_a(V) = \sum_{i=1}^N \sum_{(i,j) \in J} \sum_{p_k^{ij} \in M^{ij}} \|\tilde{v}(p_k^{ij}) - \tilde{v}(\Phi(p_k^{ij}))\|^2 \quad (3)$$

- $V$  is the list of vertexes of the mesh
- $J$  is the list of overlapping images
- $M$  is the list of all matched points between  $i, j$
- $\tilde{v}$  expresses points position as a linear combination of four vertex positions that surround the keypoint.
- $\Phi$  returns the correspondence for a given keypoint.



# Global Similarity Prior Model

## Local Similarity Term:

- Locally avoids distortion on non-overlapping regions of the images.
- Ensure that each quad undergoes a similarity transform.
- Equation:

$$\Psi_l(V) = \sum_{i=1}^N \sum_{(j,k) \in E_i} \|(\tilde{\nu}_k^i - \tilde{\nu}_j^i) - S_{jk}^i(\nu_k^i - \nu_j^i)\|^2 \quad (4)$$

- $\nu_k^i$  is the location of an original vertex  $k$  in image  $i$ .
- $\tilde{\nu}_k^i$  is the position of the vertex after deformation (parameter).
- $S_{jk}^i$  is a similarity transformation for each edge. The parameters of this are expressed as linear combination of the vertexes.

# Global Similarity Prior Model

## Global Similarity Term:

- Preserves the naturalness of the stitched image.
- Ensure that each image undergoes a similarity transform.
- Equation:

$$\Psi_g(V) = \sum_{i=1}^N \sum_{e_j^i \in E_i} w(e_j^i)^2 [(c(e_j^i) - s_i \cos \theta_i)^2 + (s(e_j^i) - s_i \sin \theta_i)^2] \quad (5)$$

- $e_j^i$  is an edge in image  $i$ .
- $w$  is a weight function that assigns more weight to the edges that are far from the overlapped region.
- The rotation and scale parameters are estimated using the initial homographies from APAP (decomposition).

# Global Similarity Prior Model

They proposed different methods for finding the best rotation for the final stitched image (naturalness).

The final optimization function is:

$$\tilde{V} = \arg \min_{\tilde{V}} \Psi_a(V) + \lambda_l \Psi_l(V) + \Psi_g(V) \quad (6)$$

They use a sparse linear solver to solve this optimization function.

# Thermal Image Stitching using GSP

## **Robust UAV Thermal Infrared Remote Sensing Images Stitching Via Overlap-Prior-Based Global Similarity Prior Model**

- Very similar to the previous paper.
- It is used on Thermal IR images.
- Probability of outliers is higher than RGB.
- Simply weight the GSP formula based on the overlap ratio of the images.

# References

- Brown, Matthew, and David G. Lowe. "Automatic panoramic image stitching using invariant features." *International journal of computer vision* 74.1 (2007): 59-73.
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# Thank you for your attention

I will post the slides to my homepage at  
<http://vision.cs.arizona.edu/ariyanzareif/>