

# Impedance Issues in SSI of Embedded and Deeply Embedded Structures

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# Outline

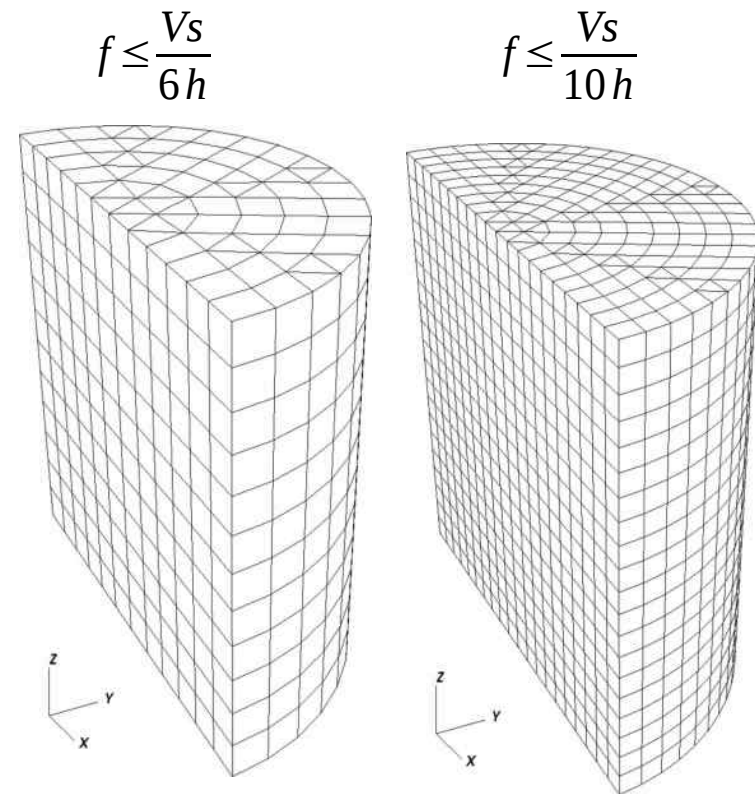
- Impedance of deeply embedded structures
- Soil box impedance
- Effect of varying wave fields

## Note:

- This talk represents a snapshot of work in progress.
- Mixed results:
  - Some good
  - Some less than acceptable
- Sharing is encouraged

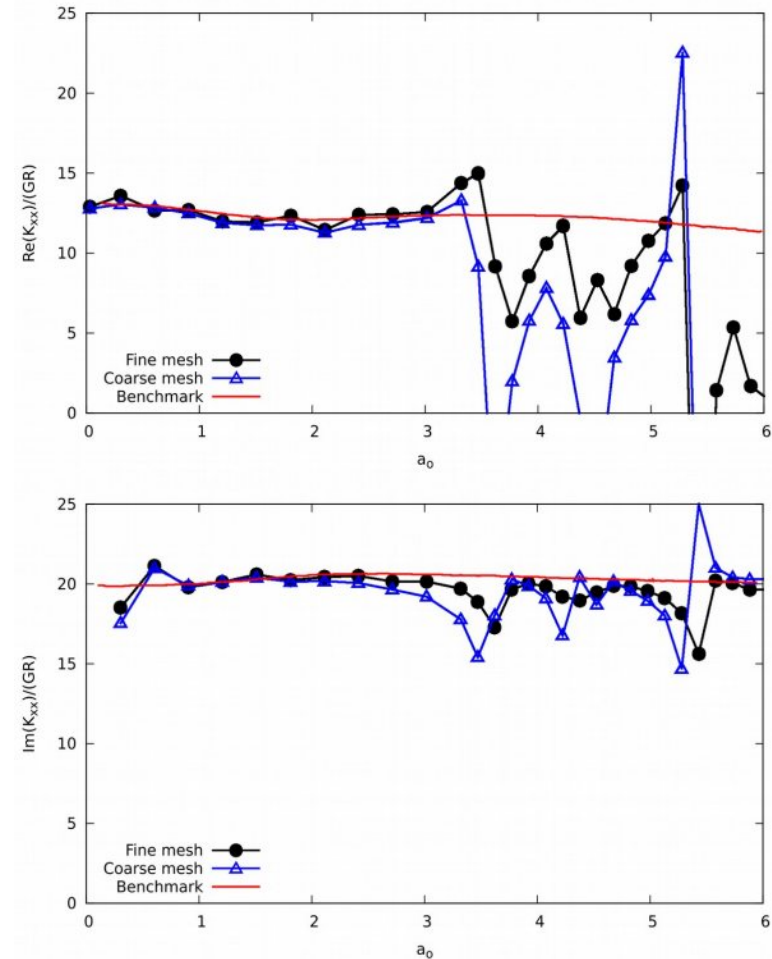
# Embedded Cylinder Impedance

- Rigid massless cylinder
- Embedment=2•radius
- Symmetry
- Direct solution
- Different meshes



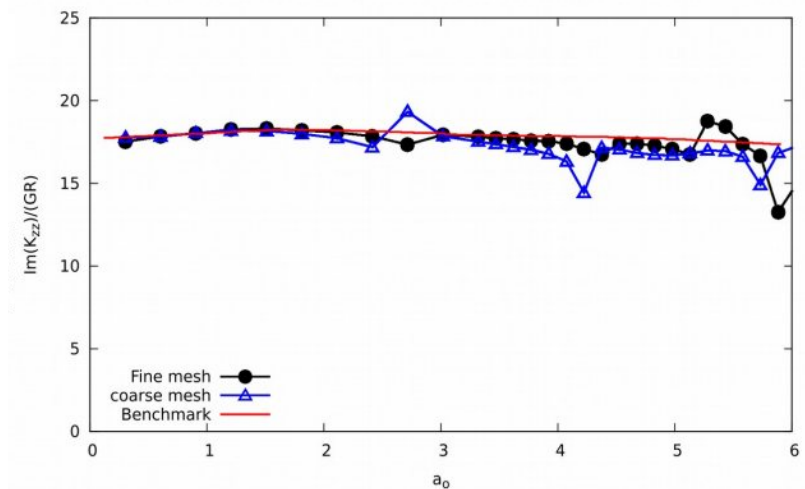
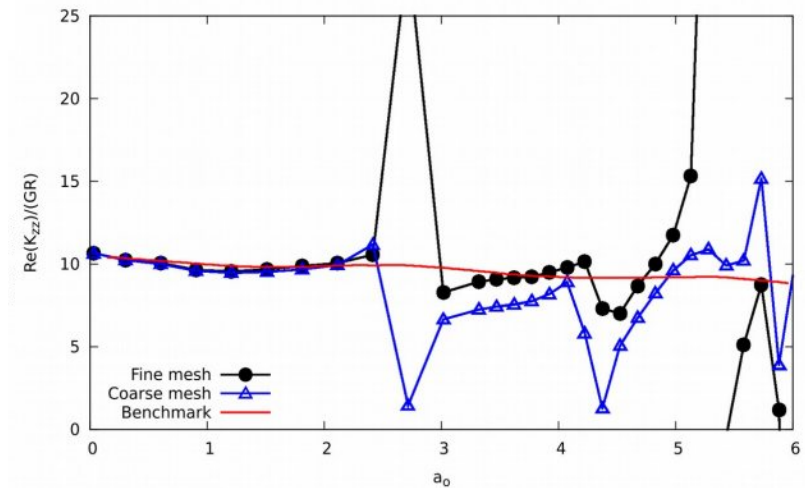
# Horizontal Impedance

- Poor comparison for  $a_0 > 3$
- Minor improvement with mesh refinement
- At  $a_0 = 3$ , the fine mesh has  $V_s/21h$
- Something besides mesh issues are perturbing the solution



# Vertical Impedance

- Poor comparison for  $a_0 > 2.5$
- Minor improvement with mesh refinement
- Something besides mesh issues are perturbing the solution



# Embedded Cylinder Impedance

- Same problem, with an embedment of  $0.5 \cdot \text{radius}$
- Vs/6h model

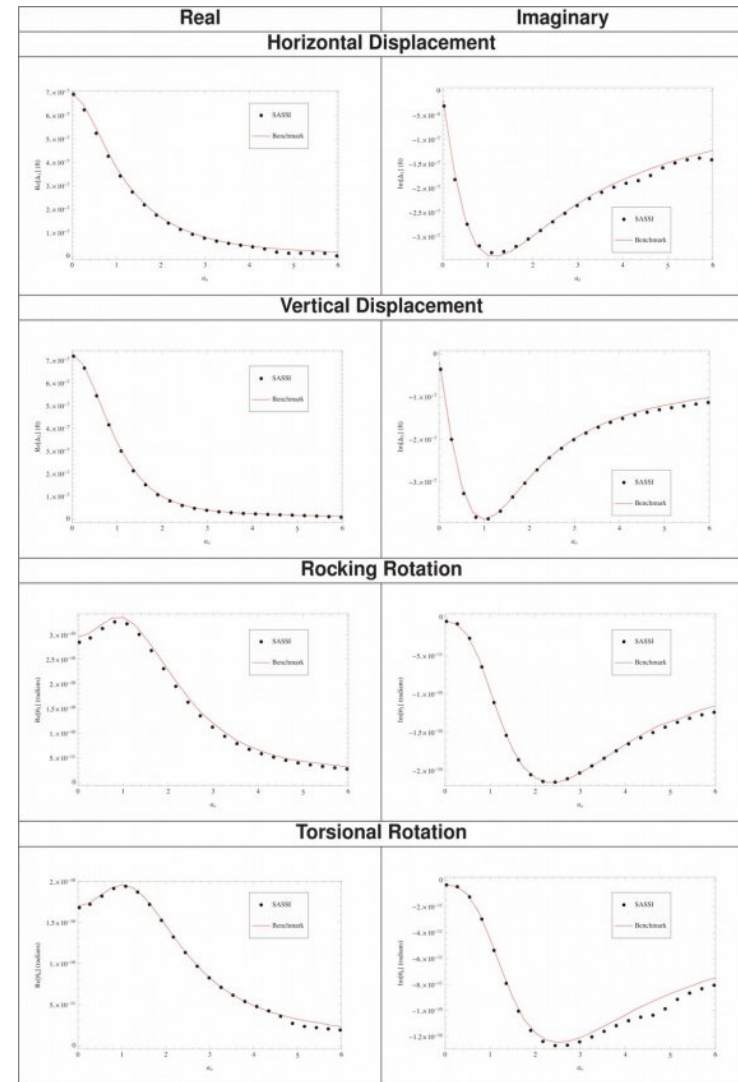
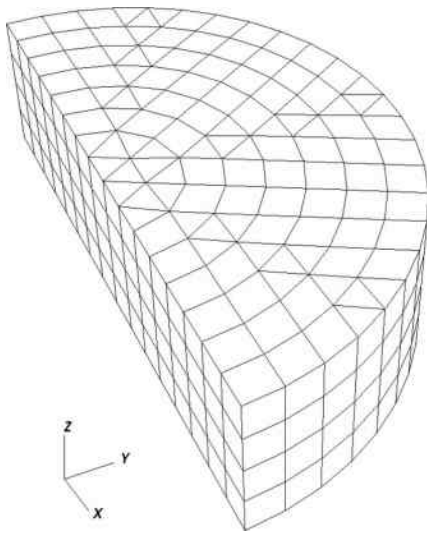


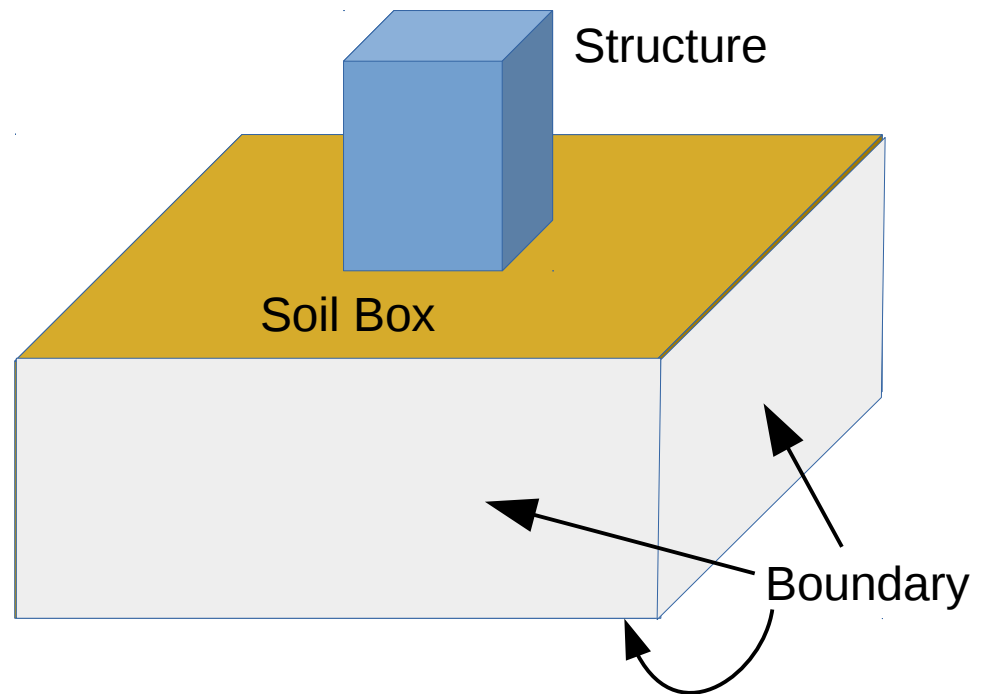
Figure 8.7: Comparison of Displacements for Problem 2a

# Summary of Deeply Embedded Structures

- SASSI V&V project considered embedment depths up to 50% of the effective radius
- Preliminary results for deeper embedment are unsatisfactory
  - Additional work is required to understand existing results and path forward
- Engineers are cautioned to ensure that their V&V fully encompasses the full range of parameters being evaluated

# Soil Box Impedance

- Considering implementing time domain SSI
  - Can we implement, execute and defend analyses?
- Proposed models
  - Structure
  - Boundary
  - Soil box





# Soil Box Impedance

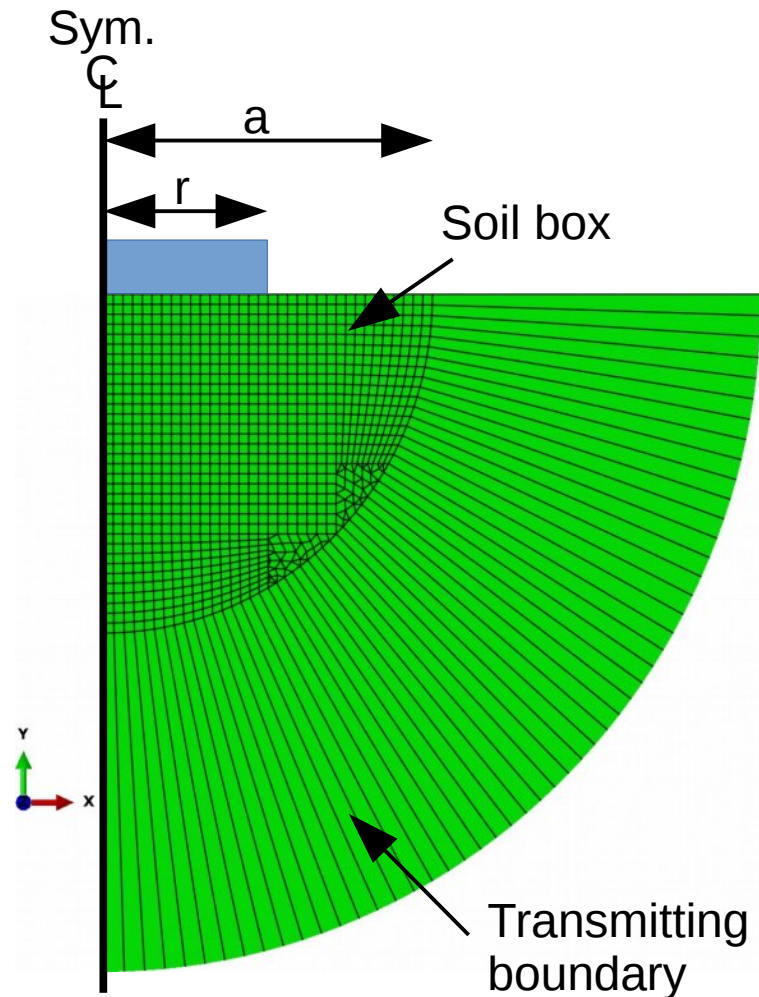
- Linear frequency domain SSI experience
  - Extensive V&V of soil impedance
    - What works
    - What doesn't work
- How does the time domain soil impedance compare with frequency domain benchmarks?

# Impedance Comparison Methodology

- Focus on boundaries and soil box size
  - Omit nonlinear soil models
- Use common damping formulation
  - Abaqus viscoelastic soil model can be equal to SASSI complex soil damping
- Limited to lumped mass matrix
- Initial comparisons in frequency domain
  - Abaqus steady state dynamics with direct option yields complex stiffness and displacement
  - Use transmitting boundary (infinite elements) to calibrate soil box size
  - Rerun with alternate boundaries
- Time domain comparison
  - Abaqus explicit

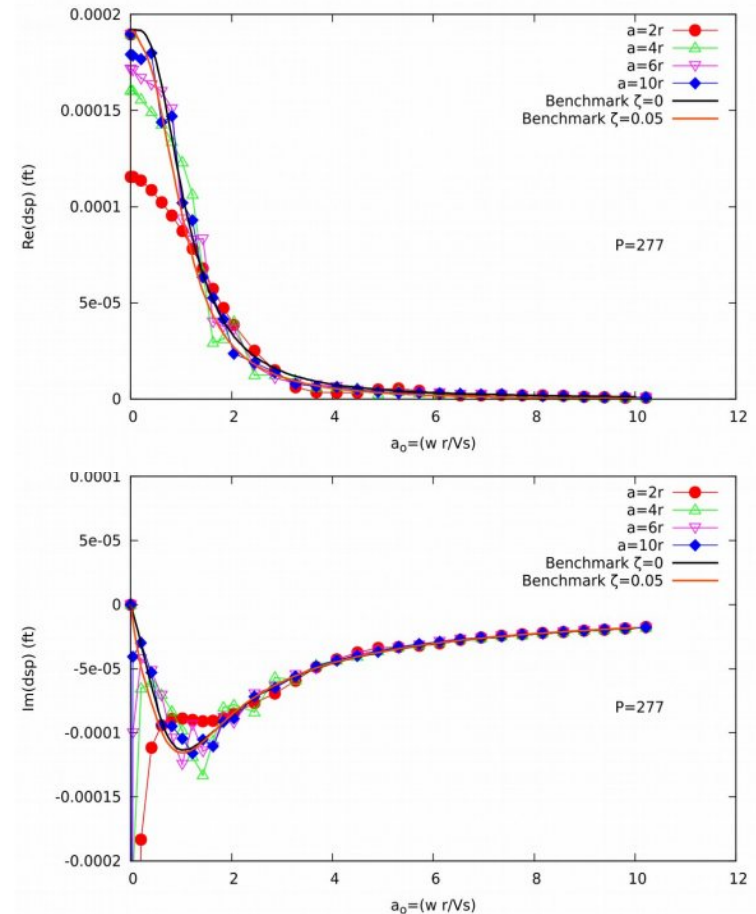
# Axisymmetric Modeling

- Exploratory
  - Quick runs
- Frequency domain
- Calibrate damping
- Transmitting boundary
  - Limited to symmetric load
  - Asymmetric infinite boundary would be helpful
- SASSI V&V Task 6 Problem 5
  - Model parameters
    - $r$  = foundation radius
    - $a$  = soil box radius



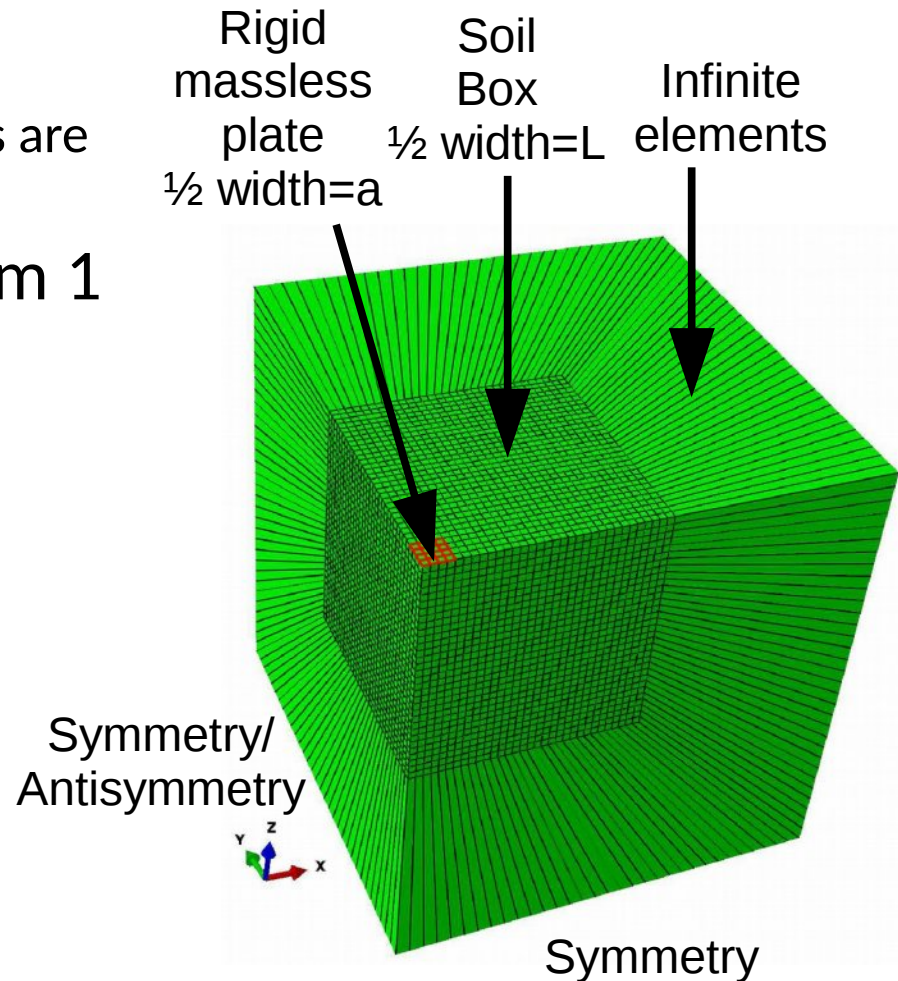
# Axisymmetric Modeling

- High frequency behavior is good
  - Mesh  $\approx Vs/(10f_{\max})$
  - Initial mesh was problematic
- Low frequency behavior is problematic
  - Wavelength,  $\lambda \approx 0.9Vs/f \approx 5.6r/a_0$ 
    - $a=2r \rightarrow \lambda=a$  at  $a_0=2.8$
    - $A=6r \rightarrow \lambda=a$  at  $a_0=0.9$
  - Response degrades when soil box radius,  $a \leq \lambda$ 
    - Mesh with infinite elements
    - Preliminary results



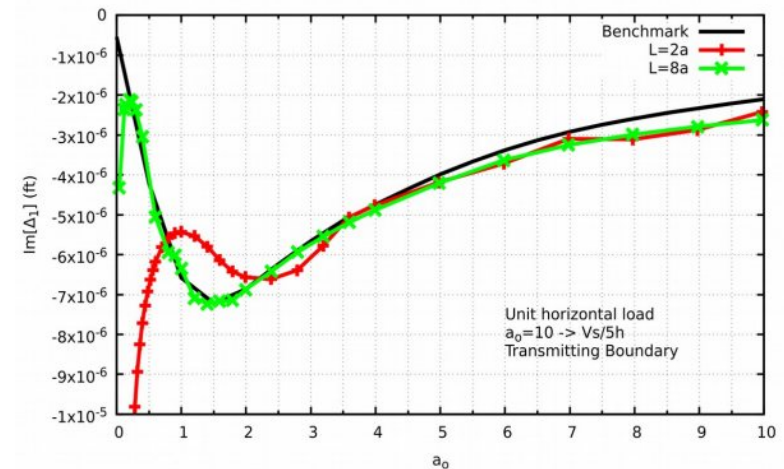
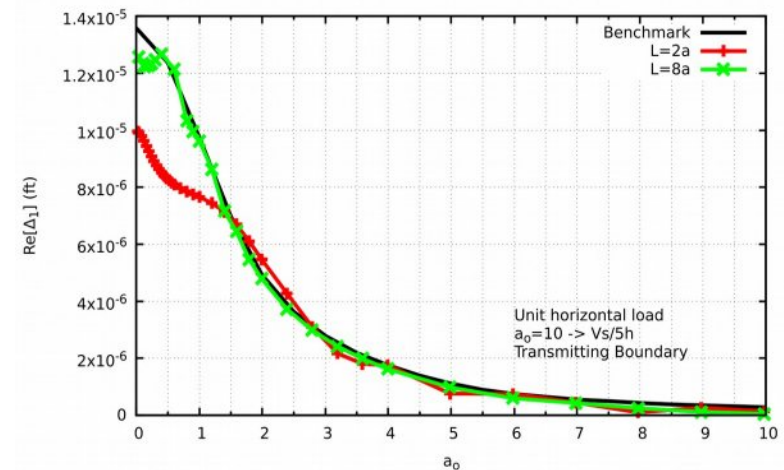
# 3D Modeling

- Quarter symmetry
  - Some frequency domain runs are slow
- SASSI V&V Task 8 Problem 1
  - Square rigid massless surface plate, half-width= $a$
  - Uniform half-space
- Cases:
  - Infinite boundary
  - Side constraint plus infinite boundary on base only



# 3D Modeling – Frequency Domain

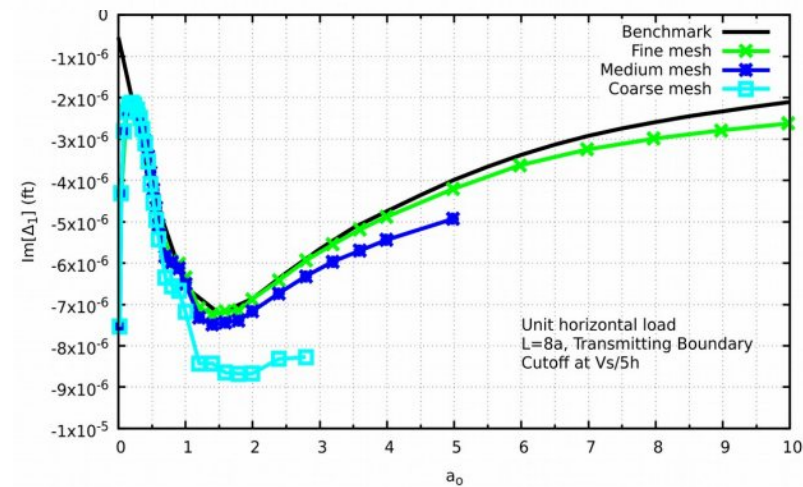
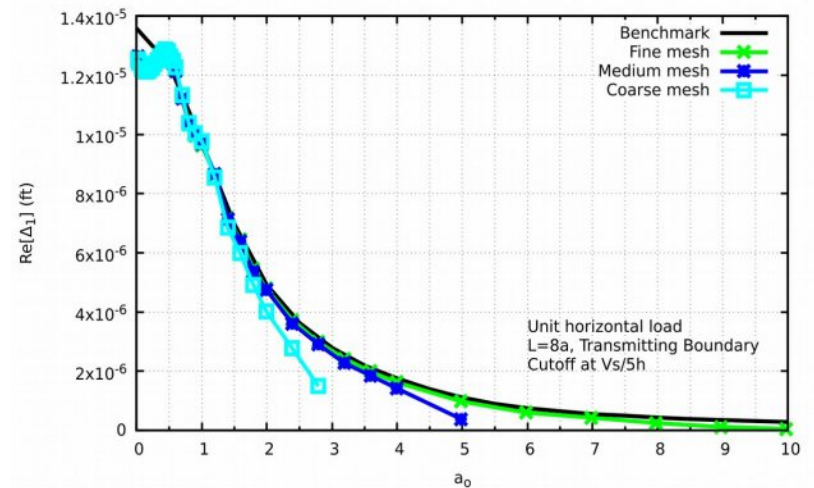
- Horizontal unit load
- Investigate soil box size
  - Low frequency problems similar to axisymmetric case
  - Response degrades when soil box width,  $L \leq \lambda$ 
    - $L=2a \rightarrow \lambda=L$  at  $a_0=2.8$
    - $L=8a \rightarrow \lambda=L$  at  $a_0=0.7$





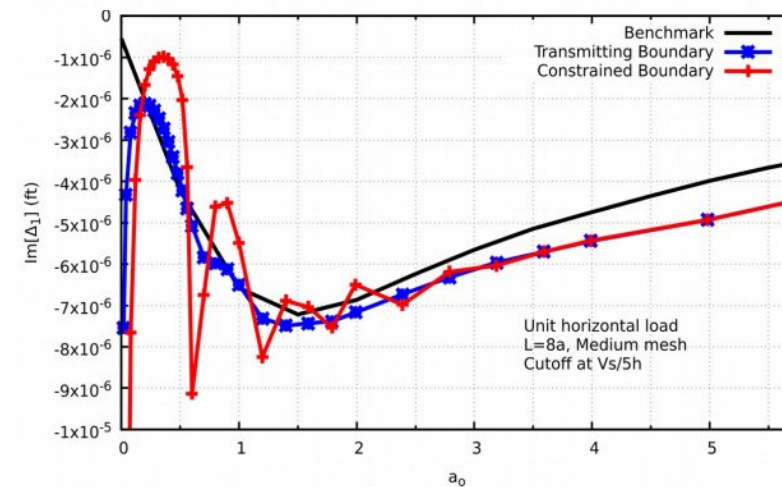
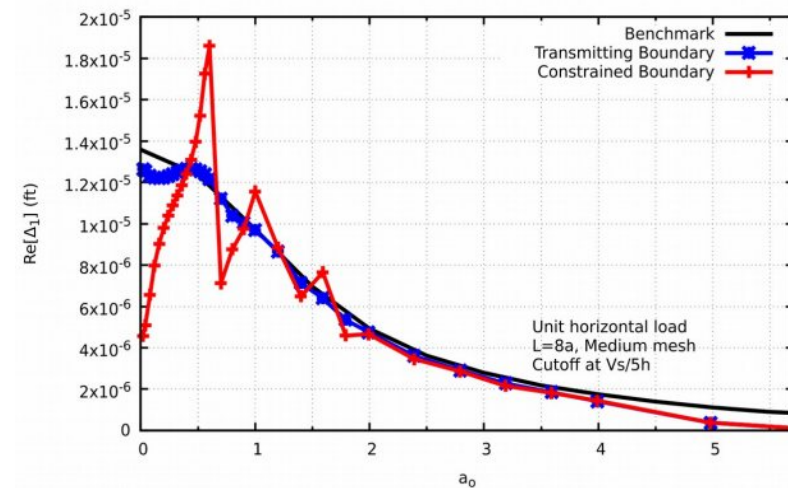
# 3D Modeling – Frequency Domain

- Horizontal unit load
- Compare soil box mesh density
  - $L=8a$  for all meshes
  - Each mesh meets  $\lambda/5$
  - Response degrades at frequencies  $> \lambda/10$
  - Note: Response is based on lumped mass matrix



# 3D Modeling – Frequency Domain

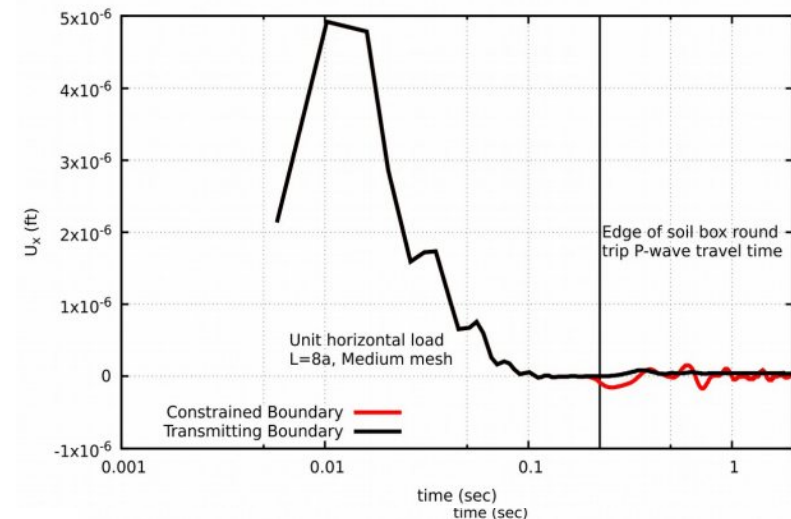
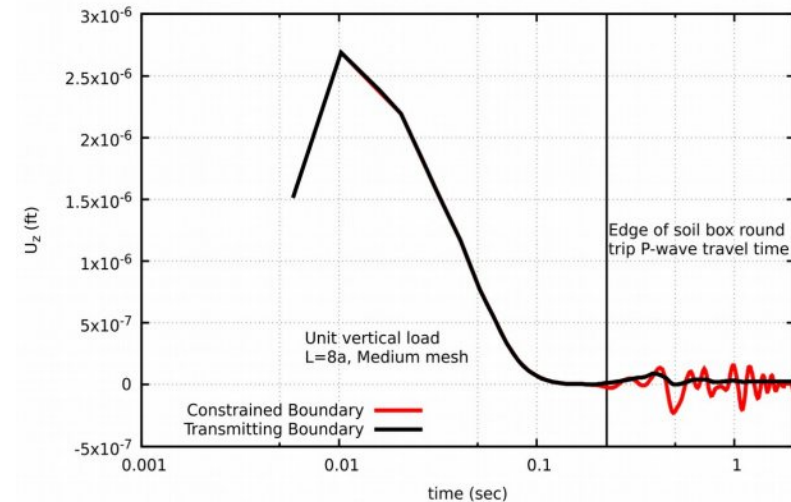
- Horizontal unit load
- Compare transmitting and restrained boundaries
  - $L=8a$
  - Each mesh meets  $\lambda/5$
  - Restrained boundary has spurious response due to reflected energy





# Time Domain Response

- Abaqus explicit
- Response to unit impulse
- Significant reflections in constrained boundary solution
- To do...
  - Refine data extraction
  - Understand high frequency noise in horizontal response
  - Extract frequency domain displacement TF and compare to benchmark



# Summary of Soil Box Impedance Study

- Preliminary results
  - Work in progress
- Abaqus transmitting boundary
  - Good comparisons with benchmark
  - 6-node wedge would be very use full
- Side constraint plus infinite boundary on base only
  - Reflections from side constraint corrupt solution at  $L=8a$
- Mesh requirements
  - High frequency: element size  $< V_s/10h$
  - Low frequency: soil box size  $> \lambda$
- Overall, promising results
  - Additional work needed before implementation on a safety basis project

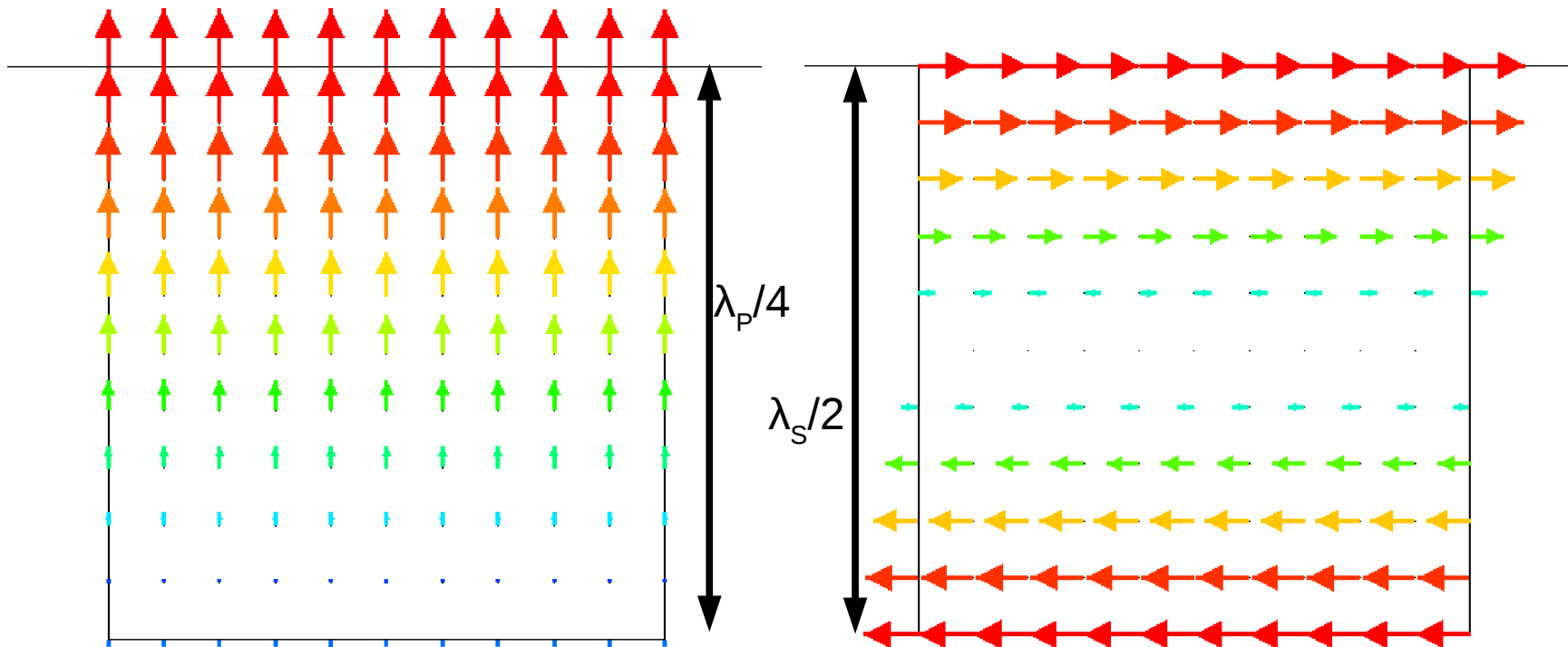
# Effect of Varying Wave Fields on SSI Loads

- Current practice
  - Analyze vertically propagating P and S-waves
    - Maximize response in a surface or shallowly embedded structure
  - Magnitude anchored to input spectra at some elevation
- Actual wave field
  - Combined body and surface waves
    - P-wave, S-wave
    - Rayleigh wave, Love wave
- Potential issues
  - Are P and S wave fields realistic for both shallow and deeply embedded structures?
  - How do we evaluate alternate wave fields?
  - Does the actual wave field impact response?

# P and S Wave Fields

$V_p \approx 2000$  fps  
 $\lambda_p = 400$  ft @ 5hz

$V_s = 1000$  fps  
 $\lambda_s = 200$  ft @ 5hz



- Embedment,  $e=100'$ , Radius,  $r=50'$ ,  $e/r=2$
- Control point at surface
- Seismic input averaged over the depth of embedment is much less than a surface foundation.

# Evaluation of Alternate Wave Field

- Wave field generation
  - Active R&D
  - Current study uses PUNCH to generate plane strain waves
- Analysis
  - Seismic load vector  $F=K \Delta$
  - Use PUNCH to develop free field displacement,  $\Delta$
  - Use SASSI for soil impedance,  $K$
  - Import frequency dependent load vector into SASSI
  - Solve using traditional frequency domain approach

# Wave field generation

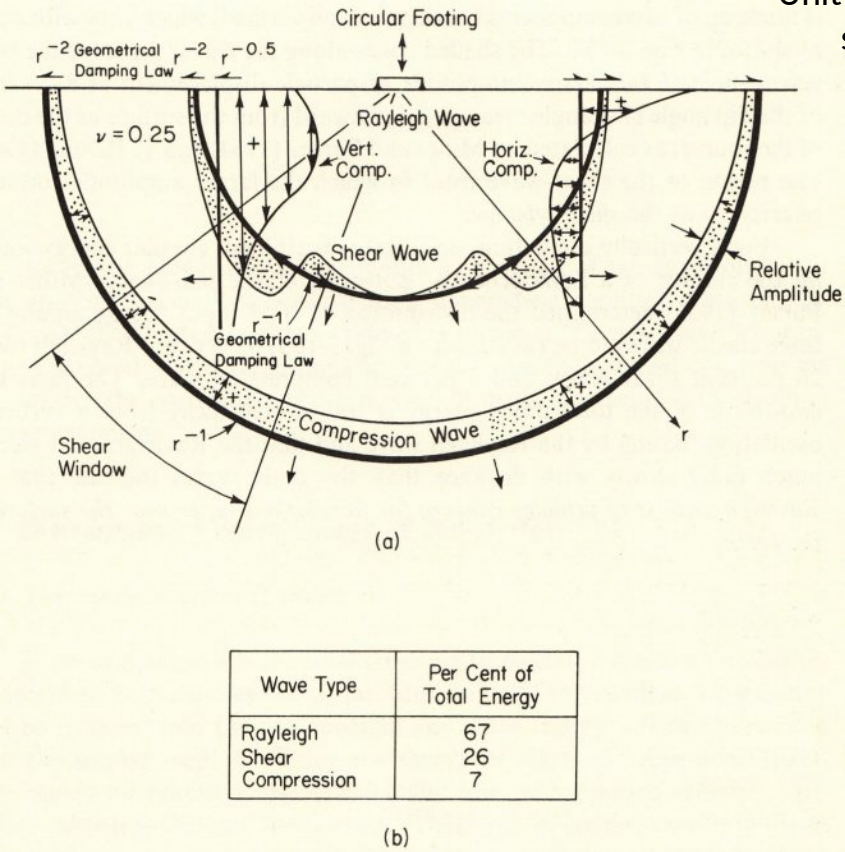
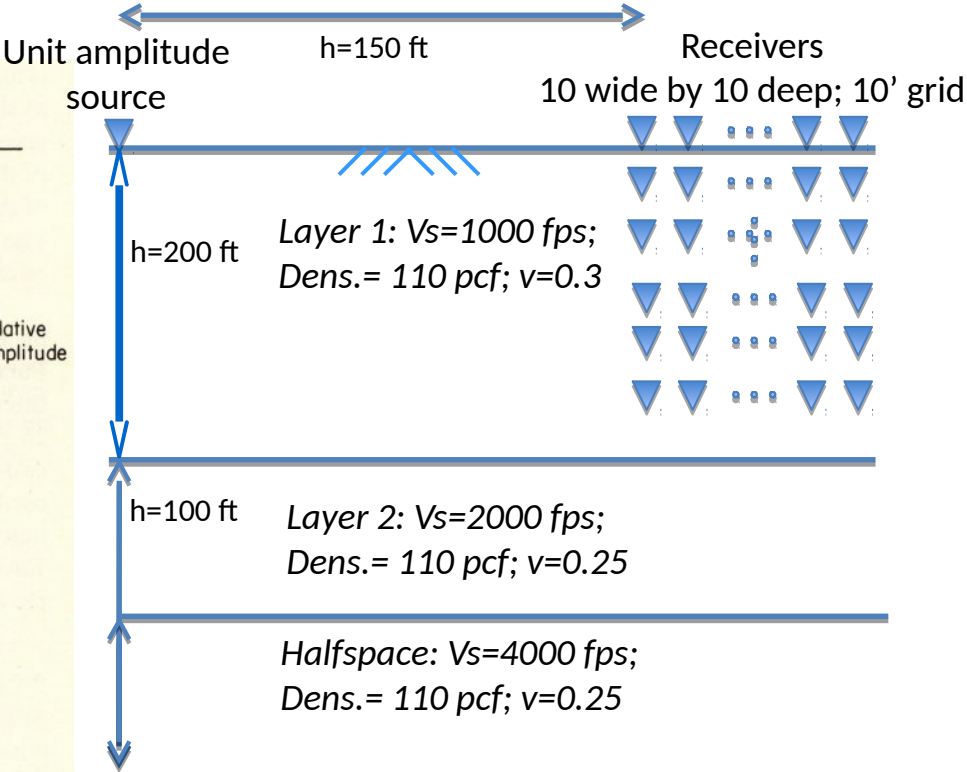
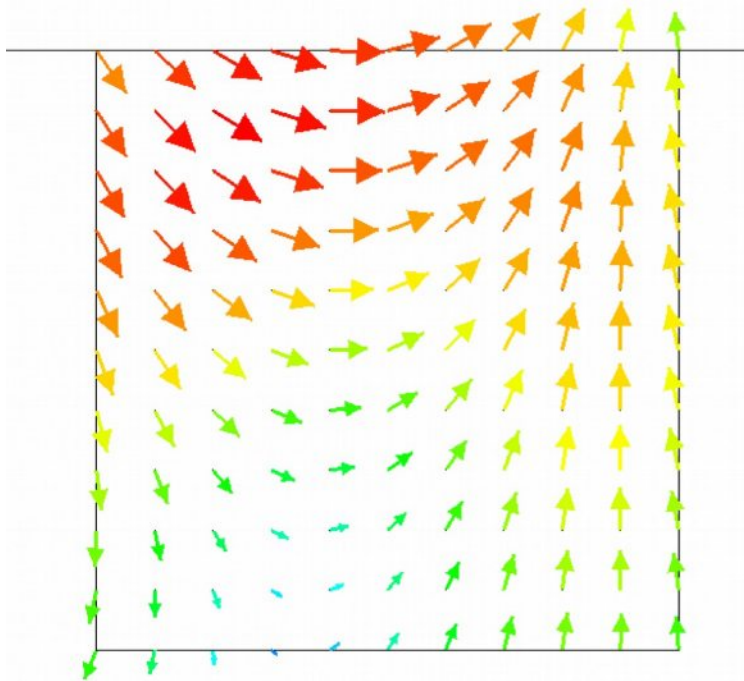


Figure 3-16. Distribution of displacement waves from a circular footing on a homogeneous, isotropic, elastic half-space (from Woods, 1968).



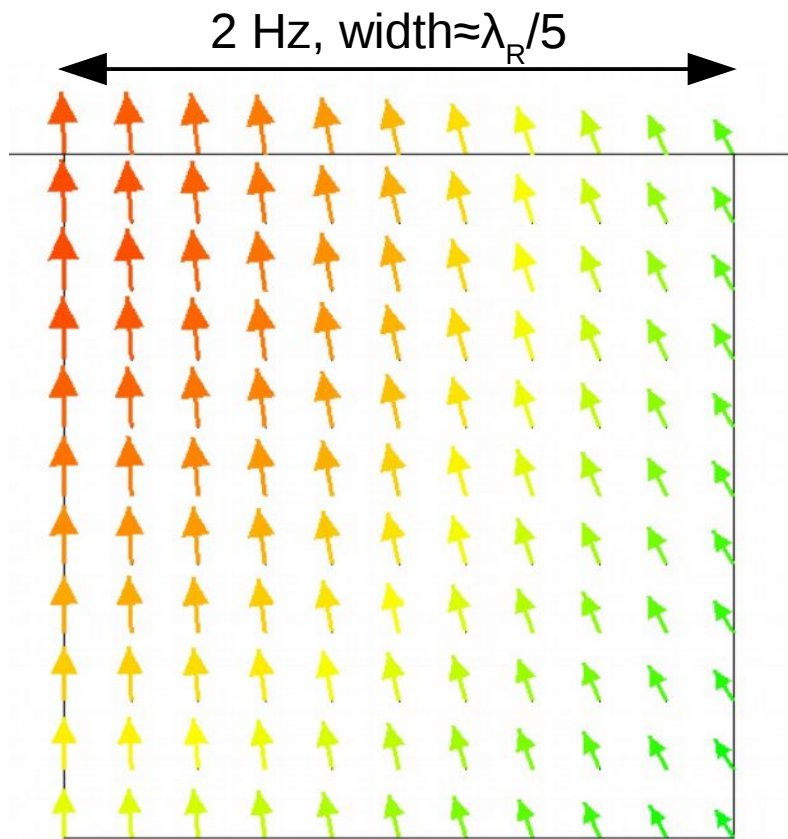
# 5 Hz Wave From Vertical Surface Input



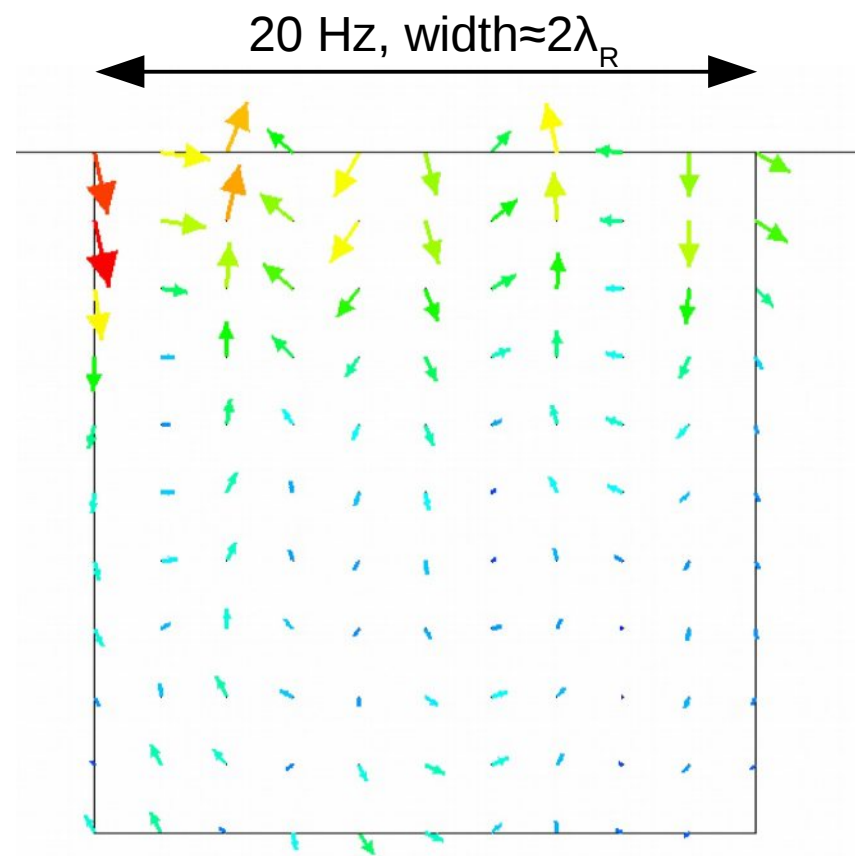
- Primarily Rayleigh wave

- $\lambda_R \approx 180'$
- $\lambda_R/2 \approx$  building width
- Input is down on left side, up on right side with coupled translation
- Direction and amplitude of input changes with phase angle

# 2 and 20 Hz Excitation



Loads in phase, greater total load than traditional analysis assumptions



Loads out of phase, smaller total load than traditional analysis assumptions

Out of phase loading can have a significant impact on structural response.



# Effect of Wave Fields

- Vertically propagating P-Wave
  - Analytical idealization
    - Yields spurious results in 1D convolution analyses
    - PSHA & Site studies use empirical V/H ratios
- Surface Waves
  - Combined vertical and horizontal input
  - Coherent building input when  $\lambda_R >$  building width
    - More total load for deeply embedded structures
  - Incoherent building input when  $\lambda_R <$  building width
    - Less total load for all structures at high frequencies
    - Excite building responses not observed in traditional analyses.

# Summary for Varying Wave Fields on SSI Loads

- Surface waves are a viable alternative to traditional seismic input
  - Provide better insight into actual seismic response
    - Coherent low frequency input
    - Incoherent high frequency input
  - Superposition of multiple waves could be used to develop ground motions meeting target spectra
    - Additional work required to develop design motion
- Surface waves can be evaluated using existing analysis tools