## SUBJECT : PAPER I - MATHEMATICS

## Instruction to Candidates

1. This question booklet contains 50 Objective Type Questions (Single Best Response Type) in the subject of Mathematics.
2. The question paper and OMR (Optical Mark Reader) Answer Sheet are issued to examinees separately at the beginning of the examination session.
3. Choice and sequence for attempting questions will be as per the convenience of the candidate.
4. Candidate should carefully read the instructions printed on the Question Booklet and Answer Sheet and make the correct entries on the Answer Sheet. As Answer Sheets are designed to suit the OPTICAL MARK READER (OMR) SYSTEM, special care should be taken to mark appropriate entries/answers correctly. Special care should be taken to fill QUESTION BOOKLET VERSION, SERIAL No. and Roll No. accurately. The correctness of entries has to be cross-checked by the invigilators. The candidate must sign on the Answer Sheet and Question Booklet.
5. Read each question carefully.
6. Determine the correct answer from out of the four available options given for each question.
7. Fill the appropriate circle completely like this , for answering the particular question, with Black ink ball point pen only, in the OMR Answer Sheet
8. Each answer with correct response shall be awarded two (2) marks. There is no Negative Marking. If the examinee has marked two or more answers or has done scratching and overwriting in the Answer Sheet in response to any question, or has marked the circles inappropriately e.g. half circle, dot, tick mark, cross etc, mark/s shall NOT be awarded for such answer/s, as these may not be read by the scanner. Answer sheet of each candidate will be evaluated by computerized scanning method only (Optical Mark Reader) and there will not be any manual checking during evaluation or verification.
9. Use of whitener or any other material to erase/hide the circle once filled is not permitted. Avoid overwriting and/or striking of answers once marked
10. Rough work should be done only on the blank space provided in the Question Booklet. Rough work should not be done on the Answer Sheet.
11. The required mathematical tables (Log etc.) are provided within the question booklet.
12. Immediately after the prescribed examination time is over, the Answer Sheet is to be returned to the Invigilator. Confirm that both the Candidate and Invigilator have signed on question booklet and answer sheet.
13. No candidate is allowed to leave the examination hall till the examination session is over.

## Questions and Solutions

1. The number of principal solutions of $\tan 2 \theta=1$ is
(A) One
(B) Two
(C) Three
(D) Four
2. (B)
$\tan 2 \theta=1$ (+ive)
$1^{\text {st }}$ and $3^{\text {rd }}$ quadrant
3. The objective function $z=4 x_{1}+5 x_{2}$, subject to $2 x_{1}+x_{2} \geq 7,2 x_{1}+3 x_{2} \leq 15, x_{2} \leq 3, x_{1}, x_{2} \geq 0$ has minimum value at the point
(A) On x-axis
(B) On y-axis
(C) At the origin
(D) On the line parallel to $x$-axis
4. (A)


Corner point
Value of $z=4 x_{1}+5 x_{2}$
Since two points are on $x$-axis minimum value occurs on $x$-axis.
Minimum value $=14$.
3. If $\mathrm{z}_{1}$ and $\mathrm{z}_{2}$ are z co-ordinates of the points of trisection of the segment joining the points $\mathrm{A}(2,1,4)$, $\mathrm{B}(-1,3,6)$ then $\mathrm{z}_{1}+\mathrm{z}_{2}=$
(A) 1
(B) 4
(C) 5
(D) 10
3. (D)
$\mathrm{A}(2,1,4)$


For $\quad \mathrm{Z}_{1} \rightarrow 1: 2$
For $\quad Z_{2} \rightarrow 2: 1$
(Internal division formula)

$$
\begin{aligned}
\mathrm{Z} & =\mathrm{Z}_{1}+\mathrm{Z}_{2} \\
& =\frac{(1)(6)+2(4)}{1+2}+\frac{2(6)+(1)(4)}{2+1} \\
& =\frac{6+8}{3}+\frac{12+4}{3} \\
& =\frac{14+16}{3} \\
& =\frac{30}{3} \\
& =10
\end{aligned}
$$

4. The maximum value of $f(x)=\frac{\log x}{x}(x \neq 0, x \neq 1)$ is
(A) e
(B) $\frac{1}{\mathrm{e}}$
(C) $\mathrm{e}^{2}$
(D) $\frac{1}{\mathrm{e}^{2}}$
5. (B)
$f(x)=\frac{\log x}{x}$
$f^{\prime}(x)=\frac{x \cdot \frac{1}{x}-\log x}{x^{2}}=\frac{1-\log x}{x^{2}}$
$\mathrm{f}^{\prime}(\mathrm{x})=0 \Rightarrow \frac{1-\log \mathrm{x}}{\mathrm{x}^{2}}=0$
$\log x=1$
$\mathrm{x}=\mathrm{e}$
$\max$. value $f(e)=\frac{\log e}{e}=\frac{1}{e}$
6. $\int_{0}^{1} x \tan ^{-1} x d x=$
(A) $\frac{\pi}{4}+\frac{1}{2}$
(B) $\frac{\pi}{4}-\frac{1}{2}$
(C) $\frac{1}{2}-\frac{\pi}{4}$
(D) $-\frac{\pi}{4}-\frac{1}{2}$
7. (B)

$$
\begin{aligned}
\int_{\substack{0 \\
\text { (uv rule) }}}^{1} x \tan ^{-1} x d x & =\left[\tan ^{-1} x \int x d x\right]_{0}^{1}-\int_{0}^{1}\left(\frac{d}{d x} \tan ^{-1} x \int x d x\right) d x \\
& =\left(\tan ^{-1} x \cdot \frac{x^{2}}{2} \int_{0}^{1}-\int_{0}^{1} \frac{1}{1+x^{2}} \cdot \frac{x^{2}}{2} d x\right. \\
& =\left(\frac{\pi}{4} \cdot \frac{1}{2}-0\right)-\frac{1}{2} \int_{0}^{1} \frac{1+x^{2}-1}{1+x^{2}} d x \\
& =\frac{\pi}{8}-\frac{1}{2} \int_{0}^{1}\left(1-\frac{1}{1+x^{2}}\right) d x \\
& =\frac{\pi}{8}-\frac{1}{2}\left[x-\tan ^{-1} x\right]_{0}^{1} \\
& =\frac{\pi}{8}-\frac{1}{2}\left[(1-0)-\left(\frac{\pi}{4}-0\right)\right]=\frac{\pi}{8}-\frac{1}{2}+\frac{\pi}{8}=\frac{\pi}{4}-\frac{1}{2}
\end{aligned}
$$

6. The statement pattern $(\sim \mathrm{p} \wedge \mathrm{q})$ is logically equivalent to
(A) $(p \vee q) \vee \sim p$
(B) $(p \vee q) \wedge \sim p$
(C) $(\mathrm{p} \wedge \mathrm{q}) \rightarrow \mathrm{p}$
(D) $(\mathrm{p} \vee \mathrm{q}) \rightarrow \mathrm{p}$
7. (B)
$(\sim \mathrm{p} \wedge q)$ is logically equivalent to

$$
\begin{array}{rlrl}
A \rightarrow(p \vee q) \vee \sim p & =T \vee q=T & \\
B \rightarrow(p \vee q) \wedge \sim p & =(p \wedge \sim p) \vee(q \wedge \sim p) & \ldots \text { Distributive law } \\
& =F \vee(q \wedge \sim p) & & \text {.. Complementary law } \\
& =q \wedge \sim p & & \text {.. Identify law } \\
& =\sim p \wedge q & & \text {.. Commutative law }
\end{array}
$$

7. If $g(x)$ is the inverse function of $f(x)$ and $f^{\prime}(x)=\frac{1}{1+x^{4}}$, then $g^{\prime}(x)$ is
(A) $1+[\mathrm{g}(\mathrm{x})]^{4}$
(B) $1-[\mathrm{g}(\mathrm{x})]^{4}$
(C) $1+[\mathrm{f}(\mathrm{x})]^{4}$
(D) $\frac{1}{1+[\mathrm{g}(\mathrm{x})]^{4}}$
8. (A)
$g=f^{-1}$
$f(g(x))=x$
$\mathrm{f}(\mathrm{g}(\mathrm{x}))=\mathrm{x}$
Differentiate w.r.t. $x$
$\mathrm{f}^{\prime}(\mathrm{g}(\mathrm{x})) \cdot \mathrm{g}^{\prime}(\mathrm{x})=1$

$$
\begin{aligned}
\therefore & \frac{1}{1+(\mathrm{g}(\mathrm{x}))^{4}} \cdot \mathrm{~g}^{\prime}(\mathrm{x})=1 \\
& \mathrm{~g}^{\prime}(\mathrm{x})=1+[\mathrm{g}(\mathrm{x})]^{4}
\end{aligned}
$$

8. The inverse of the matrix $\left[\begin{array}{ccc}1 & 0 & 0 \\ 3 & 3 & 0 \\ 5 & 2 & -1\end{array}\right]$ is
(A) $-\frac{1}{3}\left[\begin{array}{ccc}-3 & 0 & 0 \\ 3 & 1 & 0 \\ 9 & 2 & -3\end{array}\right\rfloor$
(B) $-\frac{1}{3}\left[\begin{array}{ccc}-3 & 0 & 0 \\ 3 & -1 & 0 \\ -9 & -2 & 3\end{array}\right]$
(C) $-\frac{1}{3}\left\lfloor\begin{array}{ccc}3 & 0 & 0 \\ 3 & -1 & 0 \\ -9 & -2 & 3\end{array}\right\rfloor$
(D) $-\frac{1}{3}\left[\begin{array}{ccc}-3 & 0 & 0 \\ -3 & -1 & 0 \\ -9 & -2 & 3\end{array}\right]$
9. (B)

$$
\begin{aligned}
\mathrm{A} & =\left[\begin{array}{ccc}
1 & 0 & 0 \\
3 & 3 & 0 \\
5 & 2 & -1
\end{array}\right] \quad|\mathrm{A}|=-3 \\
\mathrm{~A}^{-1} & =\frac{1}{|\mathrm{~A}|} \operatorname{Adj} \mathrm{A} \\
& =\frac{1}{-3}\left[\begin{array}{ccc}
-3 & 0 & 0 \\
3 & -1 & 0 \\
-9 & -2 & 3
\end{array}\right]
\end{aligned}
$$

9. If $\int \frac{1}{\sqrt{9-16 \mathrm{x}^{2}}} \mathrm{dx}=\alpha \sin ^{-1}(\beta \mathrm{x})+\mathrm{c}$, then $\alpha+\frac{1}{\beta}=$
(A) 1
(B) $\frac{7}{12}$
(C) $\frac{19}{12}$
(D) $\frac{9}{12}$
10. (A)

$$
\begin{aligned}
& \int \frac{1}{\sqrt{9-16 x^{2}}} \mathrm{dx}=\alpha \sin ^{-1}(\beta \mathrm{x})+\mathrm{c} \\
& \int \frac{1}{\sqrt{3^{2}-(4 x)^{2}}} \mathrm{dx}=\frac{1}{4} \sin ^{-1}\left(\frac{4 x}{3}\right)+\mathrm{c} \\
& \alpha=\frac{1}{4} \quad \beta=\frac{4}{3} \\
& \alpha+\frac{1}{\beta}=\frac{1}{4}+\frac{3}{4}=1
\end{aligned}
$$

10. $\mathrm{O}(0,0), \mathrm{A}(1,2), \mathrm{B}(3,4)$ are the vertices of $\triangle \mathrm{OAB}$. The joint equation of the altitude and median drawn from O is
(A) $x^{2}+7 x y-y^{2}=0$
(B) $x^{2}+7 x y+y^{2}=0$
(C) $3 x^{2}-x y-2 y^{2}=0$
(D) $3 x^{2}+x y-2 y^{2}=0$
11. (D)


Equation of median $O D=y=m x \Rightarrow 3=2 m$
$\Rightarrow \mathrm{m}=\frac{3}{2}$
$\therefore \mathrm{y}=\frac{3}{2} \mathrm{x} \Rightarrow 3 \mathrm{x}-2 \mathrm{y}=0$
Slope of $\mathrm{AB}=\frac{2}{2}=1 \Rightarrow$ Slope of $\mathrm{OP}=-1$
Equation of $\mathrm{OP} \Rightarrow \mathrm{y}=-\mathrm{x} \Rightarrow \mathrm{x}+\mathrm{y}=0$
Joint equation of OP and $\mathrm{OD} \Rightarrow(\mathrm{x}+\mathrm{y})(3 \mathrm{x}-2 \mathrm{y})=0$
$\Rightarrow 3 x^{2}+x y-2 y^{2}=0$
11. If the function $\mathrm{f}(\mathrm{x})=\left[\tan \left(\frac{\pi}{4}+\mathrm{x}\right)\right]^{\frac{1}{x}} \quad$ for $\mathrm{x} \neq 0 \quad$ is continuous at $\mathrm{x}=0$, then $\mathrm{K}=$ ?

$$
=\mathrm{K} \quad \text { for } \mathrm{x}=0
$$

(A) e
(B) $\mathrm{e}^{-1}$
(C) $\mathrm{e}^{2}$
(D) $\mathrm{e}^{-2}$
11. (C)
$\mathrm{f}(0)=\lim _{\mathrm{x} \rightarrow 0} \mathrm{f}(\mathrm{x})$

$$
\begin{aligned}
& =\lim _{x \rightarrow 0}\left[\tan \left(\frac{\pi}{4}+\pi\right)\right]^{\frac{1}{x}} \\
& =\lim _{x \rightarrow 0}\left(\frac{1+\tan x}{1-\tan x}\right)^{\frac{1}{x}} \\
& =\lim _{x \rightarrow 0} \frac{\left[(1+\tan x)^{\frac{1}{\tan x}}\right]^{\frac{\tan x}{x}}}{\left[(1-\tan x)^{-\frac{1}{\tan x}}\right]^{-\frac{\tan x}{x}}}
\end{aligned}
$$

taking limits

$$
=\frac{e^{1}}{e^{-1}}=e^{1} \cdot e^{1}=e^{2}
$$

12. For a invertible matrix $A$ if $A(\operatorname{adj} A)=\left[\begin{array}{cc}10 & 0 \\ 0 & 10\end{array}\right]$, then $|A|=$
(A) 100
(B) -100
(C) 10
(D) -10
13. (C)
$\mathrm{A}(\operatorname{adj} \mathrm{A})=\left[\begin{array}{cc}10 & 0 \\ 0 & 10\end{array}\right]=10\left[\begin{array}{ll}1 & 0 \\ 0 & 1\end{array}\right]=10 \mathrm{I}$
we know that $\mathrm{A}(\operatorname{adj} \mathrm{A})=|\mathrm{A}| \mathrm{I}$
$\Rightarrow|\mathrm{A}|=10$
14. The solution of the differential equation $\frac{d y}{d x}=\tan \left(\frac{y}{x}\right)+\frac{y}{x}$ is
(A) $\cos \left(\frac{y}{x}\right)=c x$
(B) $\sin \left(\frac{y}{x}\right)=c x$
(C) $\cos \left(\frac{y}{x}\right)=c y$
(D) $\sin \left(\frac{y}{x}\right)=c y$
15. (B)
$\frac{d y}{d x}=\tan \left(\frac{y}{x}\right)+\left(\frac{y}{x}\right)$
$\frac{\mathrm{y}}{\mathrm{x}}=\mathrm{v}$
$\mathrm{y}=\mathrm{vx}$
$\frac{d y}{d x}=v+x \frac{d v}{d x}$
$\therefore$ the given equation becomes

$$
\begin{aligned}
v+x \frac{d v}{d x} & =\tan v+v \\
\frac{1}{\tan v} d v & =\frac{1}{x} d x \\
\int \cot v d v & =\int \frac{1}{x} d x \\
\log |\sin v| & =\log x+\log c \\
& =\log (x c) \\
\sin v & =x c \\
\sin \left(\frac{y}{x}\right) & =x c
\end{aligned}
$$

14. In $\Delta \mathrm{ABC}$ if $\sin ^{2} \mathrm{~A}+\sin ^{2} \mathrm{~B}=\sin ^{2} \mathrm{C}$ and $\ell(\mathrm{AB})=10$, then the maximum value of the area of $\Delta \mathrm{ABC}$ is
(A) 50
(B) $10 \sqrt{2}$
(C) 25
(D) $25 \sqrt{2}$
15. (C)
$\sin ^{2} \mathrm{~A}+\sin ^{2} \mathrm{~B}=\sin ^{2} \mathrm{C}$
$\Rightarrow \mathrm{a}^{2}+\mathrm{b}^{2}=\mathrm{c}^{2}$ (Sine Rule)

$$
\begin{equation*}
\mathrm{A}(\triangle \mathrm{ABC})=\frac{1}{2} \mathrm{ab} \tag{1}
\end{equation*}
$$

From sine rule $\frac{a}{\sin A}=\frac{b}{\sin B}=\frac{c}{\sin C}$

$\Rightarrow \frac{\mathrm{a}}{\sin \mathrm{A}}=\frac{\mathrm{b}}{\sin \mathrm{B}}=\frac{10}{1}$
$\Rightarrow \mathrm{a}=10 \sin \mathrm{~A}, \mathrm{~b}=10 \sin \mathrm{~B}$
Using equation (1) $\mathrm{A}(\triangle \mathrm{ABC})=\frac{1}{2}(10 \sin \mathrm{~A})(10 \sin \mathrm{~B})$

$$
=50 \sin \mathrm{~A} \sin \mathrm{~B}
$$

But maximum value of $\sin A \sin B=\frac{1}{2}$
$\therefore \quad$ Maximum value of $\mathrm{A}(\triangle \mathrm{ABC})=50 \times \frac{1}{2}=25$

## OR

$\angle \mathrm{C}=90^{\circ} \Rightarrow \mathrm{ABC}$ is right angled triangle
$\therefore$ Area of $\Delta$ is maximum when it is $45^{\circ}-45^{\circ}-90^{\circ} \Delta$.
$\therefore \mathrm{A}(\triangle \mathrm{ABC})=\frac{1}{2} \times 5 \sqrt{2} \times 5 \sqrt{2}=25$

15. If $x=f(t)$ and $y=g(t)$ are differentiable functions of $t$ then $\frac{d^{2} y}{d x^{2}}$ is
(A) $\frac{\mathrm{f}^{\prime}(\mathrm{t}) \cdot \mathrm{g}^{\prime \prime}(\mathrm{t})-\mathrm{g}^{\prime}(\mathrm{t}) \cdot \mathrm{f}^{\prime \prime}(\mathrm{t})}{\left[\mathrm{f}^{\prime}(\mathrm{t})\right]^{3}}$
(B) $\frac{\mathrm{f}^{\prime}(\mathrm{t}) \cdot \mathrm{g}^{\prime \prime}(\mathrm{t})-\mathrm{g}^{\prime}(\mathrm{t}) \cdot \mathrm{f}^{\prime \prime}(\mathrm{t})}{\left[\mathrm{f}^{\prime}(\mathrm{t})\right]^{2}}$
(C) $\frac{g^{\prime}(t) \cdot f^{\prime \prime}(t)-f^{\prime}(t) \cdot g^{\prime \prime}(t)}{\left[f^{\prime}(t)\right]^{3}}$
(D) $\frac{g^{\prime}(t) \cdot f^{\prime \prime}(t)+f^{\prime}(t) \cdot g^{\prime \prime}(t)}{\left[f^{\prime}(t)\right]^{3}}$
15. (A)

$$
\begin{aligned}
x & =f(t) \\
y & =g(t) \\
\frac{d x}{d t} & =f^{\prime}(t) \\
\frac{d y}{d t} & =g^{\prime}(t) \\
\frac{d y}{d x} & =\frac{\frac{d y}{d t}}{\frac{d x}{d x}}=\frac{g^{\prime}(t)}{f^{\prime}(t)} \\
\frac{d^{2} y}{d x^{2}} & =\frac{d}{d x}\left(\frac{g^{\prime}(t)}{f^{\prime}(t)}\right) \\
& =\frac{f^{\prime}(t) \cdot g^{\prime \prime}(t)-g^{\prime}(t) \cdot f^{\prime \prime}(t)}{\left(f^{\prime}(t)\right)^{2}} \cdot \frac{d t}{d x} \\
& =\frac{f^{\prime}(t) \cdot g^{\prime \prime}(t)-g^{\prime}(t) \cdot f^{\prime \prime}(t)}{\left(f^{\prime}(t)\right)^{2}} \cdot \frac{1}{f^{\prime}(t)} \\
& =\frac{f^{\prime}(t) \cdot g^{\prime \prime}(t)-g^{\prime}(t) f^{\prime \prime}(t)}{\left(f^{\prime}(t)\right)^{3}}
\end{aligned}
$$

16. The equation of line equally inclined to co-ordinate axes and passing through $(-3,2,-5)$ is
(A) $\frac{x+3}{1}=\frac{y-2}{1}=\frac{z+5}{1}$
(B) $\frac{x+3}{-1}=\frac{y-2}{1}=\frac{5+z}{-1}$
(C) $\frac{\mathrm{x}+3}{-1}=\frac{\mathrm{y}-2}{1}=\frac{\mathrm{z}+5}{1}$
(D) $\frac{\mathrm{x}+3}{-1}=\frac{2-\mathrm{y}}{1}=\frac{\mathrm{z}+5}{-1}$
17. (B)

Equation of line passing through $\left(\mathrm{x}_{1}, \mathrm{y}_{1}, \mathrm{z}_{1}\right)$ and having d.c.s. $\ell, \mathrm{m}, \mathrm{n}$ is
$\frac{\mathrm{x}-\mathrm{x}_{1}}{\ell}=\frac{\mathrm{y}-\mathrm{y}_{1}}{\mathrm{~m}}=\frac{\mathrm{z}-\mathrm{z}_{1}}{\mathrm{n}}$
Here $\left(\mathrm{x}_{1}, \mathrm{y}_{1}, \mathrm{z}_{1}\right) \equiv(-3,2,-5)$
Also line is equally inclined to co-ordinate axes.
$\therefore \ell=-1, m=1, n=-1$
$\therefore$ Equation of line is $\frac{\mathrm{x}+3}{-1}=\frac{\mathrm{y}-2}{1}=\frac{\mathrm{z}+5}{-1}$
17. If $\int_{0}^{\pi / 2} \log \cos x d x=\frac{\pi}{2} \log \left(\frac{1}{2}\right)$, then $\int_{0}^{\pi / 2} \log \sec x d x=$
(A) $\frac{\pi}{2} \log \left(\frac{1}{2}\right)$
(B) $1-\frac{\pi}{2} \log \left(\frac{1}{2}\right)$
(C) $1+\frac{\pi}{2} \log \left(\frac{1}{2}\right)$
(D) $\frac{\pi}{2} \log 2$
17. (D)

$$
\begin{aligned}
\int_{0}^{\pi / 2} \log \sec x d x & =\int_{0}^{\pi / 2} \log \left(\frac{1}{\cos x}\right) d x \\
& =-\int_{0}^{\pi / 2} \log (\cos x) d x \\
& =-\frac{\pi}{2} \log (1 / 2) \quad\left(\log \left(\frac{1}{\mathrm{a}}\right)=-\log a\right)=\frac{\pi}{2} \log 2
\end{aligned}
$$

18. A boy tosses fair coin 3 times. If he gets $₹ 2 \mathrm{X}$ for X heads then his expected gain equals to ₹ ....
(A) 1
(B) $\frac{3}{2}$
(C) 3
(D) 4
19. (C)

For x heads, he gets $\mathrm{y}=2 \mathrm{x}$

| $x$ | 0 | 1 | 2 | 3 |
| :---: | :---: | :---: | :---: | :---: |
| $y$ | 0 | 2 | 4 | 6 |
| $p(y)$ | $\frac{1}{8}$ | $\frac{3}{8}$ | $\frac{3}{8}$ | $\frac{1}{8}$ |

Expected gain $=\Sigma y_{i} p_{i}$

$$
=0\left(\frac{1}{8}\right)+2\left(\frac{3}{8}\right)+4\left(\frac{3}{8}\right)+6\left(\frac{1}{8}\right)=\frac{6+12+6}{8}=3
$$

19. Which of the following statement pattern is a tautology?
(A) $p \vee(q \rightarrow p)$
(B) $\sim q \rightarrow \sim p$
(C) $(q \rightarrow p) \vee(\sim p \leftrightarrow q)$
(D) $\mathrm{p} \wedge \sim \mathrm{p}$
20. (C)

It can be done using truth table or using rules of logic.
(A) $\mathrm{p} \vee(\mathrm{q} \rightarrow \mathrm{p}) \equiv \mathrm{p} \vee(\sim \mathrm{q} \vee \mathrm{p}) \equiv \mathrm{p} \vee \mathrm{p} \vee \sim \mathrm{q}$

$$
\equiv \mathrm{p} \vee \sim \mathrm{q}
$$

(B) $\sim \mathrm{q} \rightarrow \sim \mathrm{p} \equiv \mathrm{q} \vee \sim \mathrm{p}$
(D) $\mathrm{p} \wedge \sim \mathrm{p} \equiv \mathrm{F}$

So left is (C)
(C)

| p | q | $\mathrm{q} \rightarrow \mathrm{p}$ | $\sim \mathrm{p}$ | $\sim \mathrm{p} \leftrightarrow \mathrm{q}$ | $(\mathrm{q} \rightarrow \mathrm{p}) \vee(\sim \mathrm{p} \leftrightarrow \mathrm{q})$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| T | T | T | F | F | T |
| T | F | T | F | T | T |
| F | T | F | T | T | T |
| F | F | T | T | F | T |

20. If the angle between the planes $\overline{\mathrm{r}} .(\mathrm{m} \hat{\mathrm{i}}-\hat{\mathrm{j}}+2 \hat{\mathrm{k}})+3=0$ and $\overline{\mathrm{r}} .(2 \hat{\mathrm{i}}-\mathrm{m} \hat{\mathrm{j}}-\hat{\mathrm{k}})-5=0$ is $\frac{\pi}{3}$ then $\mathrm{m}=$
(A) 2
(B) $\pm 3$
(C) 3
(D) -2
21. (C)

Direction ratios $\overline{\mathrm{n}}_{1}$ are $\mathrm{m},-1,2$
Direction ratios $\overline{\mathrm{n}}_{2}$ are $2,-\mathrm{m},-1$
$\theta=\frac{\pi}{3}$
$\cos \theta=\left|\frac{\bar{n}_{1} \cdot \overline{\mathrm{n}}_{2}}{\left|\overline{\mathrm{n}}_{1}\right|\left|\overline{\mathrm{n}}_{2}\right|}\right| \Rightarrow \frac{1}{2}=\left|\frac{2 \mathrm{~m}+\mathrm{m}-2}{\sqrt{\mathrm{~m}^{2}+5} \sqrt{\mathrm{~m}^{2}+5}}\right|$
$\frac{1}{2}=\left|\frac{3 \mathrm{~m}-2}{\mathrm{~m}^{2}+5}\right| \Rightarrow \mathrm{m}^{2}+5= \pm(6 \mathrm{~m}-4)$
$\Rightarrow \mathrm{m}^{2}+5=6 \mathrm{~m}-4, \mathrm{~m}^{2}+5=-6 \mathrm{~m}+4$
$m^{2}-6 m+9=0, m^{2}+6 m+1=0$
$(\mathrm{m}-3)^{2}=0$
$\mathrm{m}=3$
21. If the origin and the points $P(2,3,4), Q(1,2,3)$ and $R(x, y, z)$ are co-planar then
(A) $x-2 y-z=0$
(B) $x+2 y+z=0$
(C) $x-2 y+z=0$
(D) $2 x-2 y+z=0$
21. (C)
$\mathrm{O}, \mathrm{P}, \mathrm{Q}, \mathrm{R}$ are co-planar
$\left[\begin{array}{lll}\overline{\mathrm{OR}} & \overline{\mathrm{OP}} & \overline{\mathrm{OQ}}\end{array}\right]=0$
$\left|\begin{array}{lll}\mathrm{x} & \mathrm{y} & \mathrm{z} \\ 2 & 3 & 4 \\ 1 & 2 & 3\end{array}\right|=0$
$\mathrm{x}(9-8)-\mathrm{y}(6-4)+\mathrm{z}(4-3)=0$
$x-2 y+z=0$
Alternative
Points $\mathrm{P}, \mathrm{Q}$ satisfy equations given in option.
22. If lines represented by equation $\mathrm{px}^{2}-\mathrm{qy}^{2}=0$ are distinct then
(A) $\mathrm{pq}>0$
(B) $\mathrm{pq}<0$
(C) $\mathrm{pq}=0$
(D) $p+q=0$
22. (A)
$\mathrm{px}^{2}-\mathrm{qy}{ }^{2}=0$
$\mathrm{a}=\mathrm{p}, \mathrm{b}=-\mathrm{q}, \mathrm{h}=0$
lines are real and distinct is $\mathrm{h}^{2}-\mathrm{ab}>0$
$\Rightarrow 0+\mathrm{pq}>0$ $\mathrm{pq}>0$
23. Let $\square$ PQRS be a quadrilateral. If $M$ and $N$ are midpoints of the sides PQ and RS respectively then $\overline{\mathrm{PS}}+\overline{\mathrm{QR}}=$
(A) $3 \overline{\mathrm{MN}}$
(B) $4 \overline{\mathrm{MN}}$
(C) $2 \overline{\mathrm{MN}}$
(D) $2 \overline{\mathrm{NM}}$
23. (C)

$$
\begin{aligned}
& \overline{\mathrm{m}}=\frac{\overline{\mathrm{p}}+\overline{\mathrm{q}}}{2} \\
& \begin{aligned}
\overline{\mathrm{n}} & =\frac{\overline{\mathrm{r}}+\overline{\mathrm{s}}}{2} \\
\overline{\mathrm{PS}}+\overline{\mathrm{QR}} & =\overline{\mathrm{s}}-\overline{\mathrm{p}}+\overline{\mathrm{r}}-\overline{\mathrm{q}} \\
& =(\overline{\mathrm{r}}+\overline{\mathrm{s}})-(\overline{\mathrm{p}}+\overline{\mathrm{q}}) \\
& =2 \overline{\mathrm{n}}-2 \overline{\mathrm{~m}} \\
& =2(\overline{\mathrm{n}}-\overline{\mathrm{m}}) \\
& =2 \overline{\mathrm{MN}}
\end{aligned}
\end{aligned}
$$

24. If slopes of lines represented by $K x^{2}+5 x y+y^{2}=0$ differ by 1 then $K=$
(A) 2
(B) 3
(C) 6
(D) 8
25. (C)

$$
\begin{aligned}
& \mathrm{kx}^{2}+5 x y+\mathrm{y}^{2}=0 \\
& \mathrm{~m}_{1}+\mathrm{m}_{2}=-5, \mathrm{~m}_{1} \mathrm{~m}_{2}=\mathrm{k}, \mathrm{~m}_{1}-\mathrm{m}_{2}=1 \\
& \left(\mathrm{~m}_{1}-\mathrm{m}_{2}\right)^{2}=\left(\mathrm{m}_{1}+\mathrm{m}_{2}\right)^{2}-4 \mathrm{~m}_{1} \mathrm{~m}_{2} \Rightarrow 1=25-4 \mathrm{k} \Rightarrow \mathrm{k}=6
\end{aligned}
$$

25. If vector $\overline{\mathrm{r}}$ with d.c.s. $1, \mathrm{~m}, \mathrm{n}$ is equally inclined to the co-ordinate axes, then the total number of such vectors is
(A) 4
(B) 6
(C) 8
(D) 2
26. (C)
$\overline{\mathrm{r}}=|\overline{\mathrm{r}}|\left( \pm \frac{1}{\sqrt{3}} \hat{\mathrm{i}} \pm \frac{1}{\sqrt{3}} \hat{\mathrm{j}} \pm \frac{1}{\sqrt{3}} \hat{\mathrm{k}}\right)$
For equally inclined to co-ordinate axes.

$$
\begin{aligned}
& \alpha=\beta=\gamma \\
& \ell=\mathrm{m}=\mathrm{n} \\
& \ell^{2}+\mathrm{m}^{2}+\mathrm{n}^{2}=1 \\
& 3 \ell^{2}=1 \\
& \ell^{2}=\frac{1}{3}
\end{aligned}
$$

$$
\ell= \pm \frac{1}{\sqrt{3}}=\mathrm{m}=\mathrm{n} \Rightarrow \ell, \mathrm{~m}, \mathrm{n} \text { each has } 2 \text { choices. }
$$

$\therefore$ total lines $=2^{3}$
26. If $\int \frac{1}{\left(x^{2}+4\right)\left(x^{2}+9\right)} d x=A \tan ^{-1} \frac{x}{2}+B \tan ^{-1}\left(\frac{x}{3}\right)+C$ then $A-B=$
(A) $\frac{1}{6}$
(B) $\frac{1}{30}$
(C) $-\frac{1}{30}$
(D) $-\frac{1}{6}$
26. (A)
$\frac{1}{\mathrm{AB}}=\frac{1}{\mathrm{~B}-\mathrm{A}}\left(\frac{1}{\mathrm{~A}}-\frac{1}{\mathrm{~B}}\right)$

$$
\begin{aligned}
\int \frac{1}{\left(x^{2}+4\right)\left(x^{2}+9\right)} d x & =\int \frac{1}{5}\left(\frac{1}{x^{2}+4}-\frac{1}{x^{2}+9}\right) d x \\
& =\frac{1}{5}\left[\frac{1}{2} \tan ^{-1} \frac{x}{2}-\frac{1}{3} \tan ^{-1} \frac{x}{3}\right]+C \\
A & =\frac{1}{10} \quad B=-\frac{1}{15}
\end{aligned}
$$

$$
A-B=\frac{1}{10}+\frac{1}{15}=\frac{5}{30}=\frac{1}{6}
$$

27. If $\alpha$ and $\beta$ are roots of the equation $x^{2}+5|x|-6=0$ then the value of $\left|\tan ^{-1} \alpha-\tan ^{-1} \beta\right|$ is
(A) $\frac{\pi}{2}$
(B) 0
(C) $\pi$
(D) $\frac{\pi}{4}$
28. (A)

$$
\begin{aligned}
& \mathrm{x}^{2}+5|\mathrm{x}|-6=0 \\
& |\mathrm{x}|^{2}+5|\mathrm{x}|-6=0 \\
& |\mathrm{x}|^{2}+6|\mathrm{x}|-|\mathrm{x}|-6=0 \\
& |\mathrm{x}|(|\mathrm{x}|+6)-1(|\mathrm{x}|+6)=0 \\
& (|\mathrm{x}|-1)(|\mathrm{x}|+6)=0 \\
& |\mathrm{x}|=1 \quad|\mathrm{x}| \neq-6 \\
& \therefore \quad|\mathrm{x}|=1 \\
& \therefore \quad \mathrm{x}= \pm 1 \\
& \quad \alpha=1, \beta=-1 \\
& \therefore\left|\tan ^{-1} \alpha-\tan ^{-1} \beta\right|=\left|\tan ^{-1} 1-\tan ^{-1}(-1)\right| \\
& =\left|\frac{\pi}{4}-\left(-\frac{\pi}{4}\right)\right| \\
& =\left|\frac{\pi}{2}\right|
\end{aligned}
$$

28. If $x=a\left(t-\frac{1}{t}\right), y=a\left(t+\frac{1}{t}\right)$ where $t$ be the parameter then $\frac{d y}{d x}=$ ?
(A) $\frac{y}{x}$
(B) $\frac{-x}{y}$
(C) $\frac{x}{y}$
(D) $\frac{-\mathrm{y}}{\mathrm{x}}$
29. (C)
$x=a\left(t-\frac{1}{t}\right), \quad y=a\left(t+\frac{1}{t}\right)$

$$
\begin{aligned}
& y^{2}-x^{2}=a^{2}\left[\left(t+\frac{1}{t}\right)^{2}-\left(t-\frac{1}{t}\right)^{2}\right] \\
& y^{2}-x^{2}=4 a^{2}
\end{aligned}
$$

Differentiate w.r.t. x
$2 y \frac{d y}{d x}-2 x=0$
$\therefore \frac{d y}{d x}=\frac{x}{y}$
29. The point on the curve $\mathrm{y}=\sqrt{\mathrm{x}-1}$ where the tangent is perpendicular to the line $2 \mathrm{x}+\mathrm{y}-5=0$ is
(A) $(2,-1)$
(B) $(10,3)$
(C) $(2,1)$
(D) $(5,-2)$
29. (C)
$\frac{d y}{d x}=\frac{1}{2 \sqrt{x-1}}=m_{1}$
Slope of line $2 x+y-5=0$ is $m_{2}=-2$
For lines are perpendicular

$$
\mathrm{m}_{1} \mathrm{~m}_{2}=-1
$$

$\left(\frac{1}{2 \sqrt{x-1}}\right)(-2)=-1$
$\frac{2}{2 \sqrt{x-1}}=1$
$\sqrt{\mathrm{x}-1}=1$
Squaring both sides, $\mathrm{x}-1=1$

$$
\begin{aligned}
x & =2 \\
\therefore \quad y & =\sqrt{x-1} \\
& =\sqrt{2-1} \\
& =\sqrt{1} \\
y & =1
\end{aligned}
$$

$$
\therefore \quad(2,1)
$$

30. If $\int \sqrt{\frac{x-5}{x-7}} d x=A \sqrt{x^{2}-12 x+35}+\log \left|x-6+\sqrt{x^{2}-12 x+35}\right|+C$ then $A=$
(A) -1
(B) $\frac{1}{2}$
(C) $-\frac{1}{2}$
(D) 1
31. (D)

$$
\begin{aligned}
\int \sqrt{\frac{x-5}{x-7}} d x & =\int \frac{x-5}{\sqrt{x^{2}-12 x+35}} d x=\frac{1}{2} \int \frac{2 x-10}{\sqrt{x^{2}-12 x+35}} d x \\
& =\frac{1}{2} \int \frac{2 x-12+2}{\sqrt{x^{2}-12 x+35}} d x \\
& =\frac{1}{2} \int \frac{2 x-12}{\sqrt{x^{2}-12 x+35}} d x+\int \frac{d x}{\sqrt{x^{2}-12 x+36-1}} \\
& =\frac{1}{2} 2 \sqrt{x^{2}-12 x+35}+\int \frac{d x}{\sqrt{(x-6)^{2}-1}}+c_{1} \\
& =\sqrt{x^{2}-12 x+35}+\log \left|x-6+\sqrt{x^{2}-12 x+35}\right|+c \\
\text { A } & =1
\end{aligned}
$$

31. A r. v. $X \sim B(n, p)$. If values of mean and variance of $X$ are 18 and 12 respectively then total number of possible values of $X$ are
(A) 54
(B) 55
(C) 12
(D) 18
32. (B)

Mean $=\mathrm{np}=18$
Variance $=\mathrm{npq}=12$

$$
\begin{aligned}
& \frac{\mathrm{npq}}{\mathrm{np}}=\frac{12}{18} \\
& \mathrm{q}=\frac{2}{3} \\
& \mathrm{p}=1-\mathrm{q}=1-\frac{2}{3} \\
& \mathrm{p}=\frac{1}{3} \\
& \mathrm{np}=18 \\
& \mathrm{n}\left(\frac{1}{3}\right)=18 \\
& \mathrm{n}=54
\end{aligned}
$$

$\therefore \quad$ values of X are

$$
0,1,2, \ldots \ldots \ldots .
$$

$\therefore 55$ values.
32. The area of the region bounded by the lines $y=2 x+1, y=3 x+1$ and $x=4$ is
(A) 16 sq. unit
(B) $\frac{121}{3}$ sq. unit
(C) $\frac{121}{6}$ sq. unit
(D) 8 sq. unit
32. (D)

$\mathrm{A}($ Shaded region $)=\mathrm{A}(\triangle \mathrm{ABD})-\mathrm{A}(\triangle \mathrm{ABC})=\frac{1}{2}[4 \times 12-4 \times 8]=\frac{1}{2}(48-32)=8$ sq. units.

$$
\begin{aligned}
\mathrm{A}(\Delta \mathrm{ACD}) & =\frac{1}{2}\left|\begin{array}{ccc}
0 & 1 & 1 \\
4 & 9 & 1 \\
4 & 13 & 1
\end{array}\right| \\
& =\frac{1}{2} \times 16=8
\end{aligned}
$$

33. A box contains 6 pens, 2 of which are defective. Two pens are taken randomly from the box. If r.v. X : Number of defective pens obtained, then standard deviation of $X=$
(A) $\pm \frac{4}{3 \sqrt{5}}$
(B) $\frac{8}{3}$
(C) $\frac{16}{45}$
(D) $\frac{4}{3 \sqrt{5}}$
34. (D)
x : no. of defective pens
Two pens are taken from box
$\therefore \quad \mathrm{x}$ can take values $0,1,2$

$$
\begin{aligned}
& \mathrm{p}(\mathrm{x}=0)=\frac{{ }^{4} \mathrm{C}_{2}}{{ }^{6} \mathrm{C}_{2}}=\frac{4 \times 3}{6 \times 5}=\frac{2}{5}=\frac{6}{15} \\
& \mathrm{p}(\mathrm{x}=1)=\frac{{ }^{2} \mathrm{C}_{1} \times{ }^{4} \mathrm{C}_{1}}{{ }^{6} \mathrm{C}_{2}}=\frac{2 \times 4 \times 2 \times 1}{6 \times 5}=\frac{8}{15} \\
& \mathrm{p}(\mathrm{x}=2)=\frac{{ }^{2} \mathrm{C}_{2}}{{ }^{6} \mathrm{C}_{2}}=\frac{1 \times 2 \times 1}{6 \times 5}=\frac{1}{15}
\end{aligned}
$$

| x | p | $\mathrm{x}_{\mathrm{i}} \mathrm{p}_{\mathrm{i}}$ | $\mathrm{x}_{\mathrm{i}}^{2} \mathrm{p}_{\mathrm{i}}$ |
| :---: | :---: | :---: | :---: |
| 0 | $\frac{6}{15}$ | 0 | 0 |
| 1 | $\frac{8}{15}$ | $\frac{8}{15}$ | $\frac{8}{15}$ |
| 2 | $\frac{1}{15}$ | $\frac{2}{15}$ | $\frac{4}{15}$ |

$$
\begin{aligned}
\mathrm{E}(\mathrm{x}) & =\frac{10}{15} \\
& =\frac{2}{3} \\
\mathrm{E}\left(\mathrm{x}^{2}\right) & =\frac{12}{15} \\
& =\frac{4}{5}
\end{aligned}
$$

Standard deviation $=\sqrt{E\left(x^{2}\right)-[E(x)]^{2}}$

$$
\begin{aligned}
\text { Standard devivation } & =\sqrt{\left(\frac{4}{5}\right)-\left(\frac{2}{3}\right)^{2}} \\
& =\sqrt{\frac{4}{5}-\frac{4}{9}} \\
& =\sqrt{\frac{4 \times 4}{45}} \\
& =\frac{4}{3 \sqrt{5}}
\end{aligned}
$$

34. If the volume of spherical ball is increasing at the rate of $4 \pi \mathrm{cc} / \mathrm{sec}$ then the rate of change of its surface area when the volume is $288 \pi \mathrm{cc}$ is
(A) $\frac{4}{3} \pi \mathrm{~cm}^{2} / \mathrm{sec}$
(B) $\frac{2}{3} \pi \mathrm{~cm}^{2} / \mathrm{sec}$
(C) $4 \pi \mathrm{~cm}^{2} / \mathrm{sec}$
(D) $2 \pi \mathrm{~cm}^{2} / \mathrm{sec}$
35. (A)
$\mathrm{V}=\frac{4}{3} \pi \mathrm{r}^{3} \Rightarrow \frac{\mathrm{dv}}{\mathrm{dt}}=4 \pi \mathrm{r}^{2} \frac{\mathrm{dr}}{\mathrm{dt}}$
When $\mathrm{V}=288 \pi$
$288 \pi=\frac{4}{3} \pi r^{3} \Rightarrow \quad r=6$
$\frac{\mathrm{dv}}{\mathrm{dt}}=4 \pi$
$\therefore 4 \pi \mathrm{r}^{2} \frac{\mathrm{dr}}{\mathrm{dt}}=4 \pi=\frac{\mathrm{dr}}{\mathrm{dt}}=\frac{1}{\mathrm{r}^{2}}$
$\mathrm{A}=$ Surface area $=4 \pi \mathrm{r}^{2}$
$\therefore \frac{\mathrm{dA}}{\mathrm{dt}}=8 \pi \mathrm{r} \frac{\mathrm{dr}}{\mathrm{dt}}=8 \pi \mathrm{r} \times \frac{1}{\mathrm{r}^{2}}=\frac{8 \pi}{\mathrm{r}}=\frac{8 \pi}{6}=\frac{4 \pi}{3}$
36. If $f(x)=\log \left(\sec ^{2} x\right)^{\cot ^{2} x} \quad$ for $x \neq 0$
is continuous at $x=0$ then $K$ is
(A) $e^{-1}$
(B) 1
(C) e
(D) 0
37. (B)

$$
\begin{aligned}
\mathrm{f}(0) & =\lim _{\mathrm{x} \rightarrow 0} \log \left(\sec ^{2} \mathrm{x}\right)^{\cot 2 \mathrm{x}} \\
\mathrm{k} & =\lim _{\mathrm{x} \rightarrow 0} \cot ^{2} \mathrm{x} \cdot \log \left(1+\tan ^{2} \mathrm{x}\right) \\
& =\lim _{\mathrm{x} \rightarrow 0} \frac{\log \left(1+\tan ^{2} \mathrm{x}\right)}{\tan ^{2} \mathrm{x}} \\
\mathrm{k} & =1
\end{aligned}
$$

36. If $c$ denotes the contradiction then dual of the compound statement $\sim p \wedge(q \vee c)$ is
(A) $\sim p \vee(q \wedge t)$
(B) $\sim \mathrm{p} \wedge(\mathrm{q} \vee \mathrm{t})$
(C) $\mathrm{p} \vee(\sim \mathrm{q} \vee \mathrm{t})$
(D) $\sim p \vee(q \wedge c)$
37. (A)

Dual of $\sim P \wedge(q \vee c)=\sim P \vee(q \wedge t)$
37. The differential equation of all parabolas whose axis is $y$-axis is
(A) $x \frac{d^{2} y}{d x^{2}}-\frac{d y}{d x}=0$
(B) $x \frac{d^{2} y}{d x^{2}}+\frac{d y}{d x}=0$
(C) $\frac{d^{2} y}{d x^{2}}-y=0$
(D) $\frac{d^{2} y}{d x^{2}}-\frac{d y}{d x}=0$
37. (A)
axis $=y$ axis
vertex is $(0, k)$
Equation of parabola is
$(x-0)^{2}=4 a(y-k)$
$x^{2}=4 a y-4 a k$
Differentiate w.r.t $x$

$$
\begin{array}{r}
2 x=4 a \frac{d y}{d x} \\
x=2 a \frac{d y}{d x} \\
\therefore \quad \frac{1}{2 a}=\frac{1}{x} \frac{d y}{d x}
\end{array}
$$

Differentiate w.r.t $x$,
$\frac{d}{d x}\left(\frac{1}{x} \cdot \frac{d y}{d x}\right)=\frac{d}{d x}\left(\frac{1}{2 a}\right)$
$\frac{1}{x} \cdot \frac{d^{2} y}{d x^{2}}+\frac{d y}{d x}\left(-\frac{1}{x^{2}}\right)=0$
$\therefore \quad x \frac{d^{2} y}{d x^{2}}-\frac{d y}{d x}=0$
38. $\int_{0}^{3}[x] d x=$ $\qquad$ , where $[\mathrm{x}]$ is greatest integer function.
(A) 3
(B) 0
(C) 2
(D) 1
38. (A)

$$
\begin{aligned}
\int_{0}^{3}[x] d x & =\int_{0}^{1} 0 d x+\int_{1}^{2} 1 d x+\int_{2}^{3} 2 d x \\
& =[x]_{1}^{2}+2[x]_{2}^{3} \\
& =(2-1)+2(3-2) \\
& =1+2 \\
& =3
\end{aligned}
$$

39. The objective function of LPP defined over the convex set attains its optimum value at
(A) At least two of the corner points
(B) All the corner points
(C) At least one of the corner points
(D) None of the corner points
40. (C)
41. If the inverse of the matrix $\left[\begin{array}{ccc}\alpha & 14 & -1 \\ 2 & 3 & 1 \\ 6 & 2 & 3\end{array}\right]$ does not exist then the value of $\alpha$ is
(A) 1
(B) -1
(C) 0
(D) -2
42. (D)
$\mathrm{A}=\left[\begin{array}{ccc}\alpha & 14 & -1 \\ 2 & 3 & 1 \\ 6 & 2 & 3\end{array}\right]$
$|\mathrm{A}|=7 \alpha+14$
$\mathrm{A}^{-1}$ does not exists if $|\mathrm{A}|=0$
$\Rightarrow 7 \alpha+14=0 \Rightarrow \alpha=-2$
43. If $f(x)=x$ for $x \leq 0$

$$
=0 \text { for } x>0 \text { then } f(x) \text { at } x=0 \text { is }
$$

(A) Continuous but not differentiable
(B) Not continuous but differentiable
(C) Continuous and differentiable
(D) Not continuous and not differentiable
41. (A)

Continuity at $\mathrm{x}=0$
$\lim _{x \rightarrow 0^{-}} f(x)=\lim _{x \rightarrow 0} x=0$
$\lim _{x \rightarrow 0^{+}} f(x)=0$
$f(0)=0$
$\therefore$ continuous at $\mathrm{x}=0$
For differentiable

$$
\begin{aligned}
\mathrm{f}^{\prime}(\mathrm{x}) & =1 & & \mathrm{x} \leq 0 \\
& =0 & & \mathrm{x}>0
\end{aligned}
$$

$\therefore$ not differentiable

## Alternative



It has sharp edge at $\mathrm{x}=0$
$\therefore$ not differentiable but continuous
42. The equation of the plane through $(-1,1,2)$, whose normal makes equal acute angles with co-ordinate axes is
(A) $\overline{\mathrm{r}} \cdot(\hat{\mathrm{i}}+\hat{\mathrm{j}}+\hat{\mathrm{k}})=2$
(B) $\overline{\mathrm{r}} \cdot(\hat{\mathrm{i}}+\hat{\mathrm{j}}+\hat{\mathrm{k}})=6$
(C) $\overline{\mathrm{r}} \cdot(3 \hat{\mathrm{i}}-3 \hat{\mathrm{j}}+3 \hat{\mathrm{k}})=2$
(D) $\overline{\mathrm{r}} \cdot(\hat{\mathrm{i}}-\hat{\mathrm{j}}+\hat{\mathrm{k}})=3$
42. (A)

Equation plane passing through
$\mathrm{A}(\overline{\mathrm{a}}) \& \perp$ to $\overline{\mathrm{n}}$ is
$\overline{\mathrm{r}} . \overline{\mathrm{n}}=\overline{\mathrm{a}} . \bar{n}$
Here $\quad \overline{\mathrm{a}}=-\hat{\mathrm{i}}+\hat{\mathrm{j}}+2 \hat{\mathrm{k}}, \quad \overline{\mathrm{n}}=\hat{\mathrm{i}}+\hat{\mathrm{j}}+\hat{\mathrm{k}}$
$\therefore \quad \overline{\mathrm{r}} .(\hat{\mathrm{i}}+\hat{\mathrm{j}}+\hat{\mathrm{k}})=(-\hat{\mathrm{i}}+\hat{\mathrm{j}}+2 \hat{\mathrm{k}}) \cdot(\hat{\mathrm{i}}+\hat{\mathrm{j}}+\hat{\mathrm{k}})=2$
43. Probability that a person will develop immunity after vaccination is 0.8 . If 8 people are given the vaccine then probability that all develop immunity is =
(A) $(0.2)^{8}$
(B) $(0.8)^{8}$
(C) 1
(D) ${ }^{8} \mathrm{C}_{6}(0.2)^{6}(0.8)^{2}$
43. (B)
$(0.8)^{8}$
44. If the distance of points $2 \hat{i}+3 \hat{j}+\lambda \hat{k}$ from the plane $\bar{r} \cdot(3 \hat{i}+2 \hat{j}+6 \hat{k})=13$ is 5 units then $\lambda=$
(A) $6,-\frac{17}{3}$
(B) $6, \frac{17}{3}$
(C) $-6,-\frac{17}{3}$
(D) $-6, \frac{17}{3}$
44. (A)

Equation of plane $\bar{r} \cdot(3 \hat{i}+2 \hat{j}+6 \hat{k})=13$
i.e. $3 x+2 y+62-13=0$

Given point ( $2,3, \lambda$ )
distance of plane from the point $=\left|\frac{a x_{1}+b y_{1}+c z_{1}+d}{\sqrt{a^{2}+b^{2}+c^{2}}}\right|$

$$
\begin{array}{ll} 
& 5=\left|\frac{3(2)+2(3)+6 \lambda-13}{\sqrt{9+4+36}}\right| \\
\therefore & 5=\left|\frac{6 \lambda-1}{7}\right| \\
\Rightarrow & 6 \lambda-1= \pm 35 \\
\Rightarrow & 6 \lambda=36,6 \lambda=-34 \\
& \lambda=6, \lambda=-\frac{17}{3}
\end{array}
$$

45. The value of $\cos ^{-1}\left(\cot \left(\frac{\pi}{2}\right)\right)+\cos ^{-1}\left(\sin \left(\frac{2 \pi}{3}\right)\right)$ is
(A) $\frac{2 \pi}{3}$
(B) $\frac{\pi}{3}$
(C) $\frac{\pi}{2}$
(D) $\pi$
46. (A)

$$
\begin{aligned}
\cos ^{-1}\left(\cot \frac{\pi}{2}\right)+\cos ^{-1}\left(\sin \frac{2 \pi}{3}\right) & =\cos ^{-1}(0)+\cos ^{-1}\left(\frac{\sqrt{3}}{2}\right) \\
& =\frac{\pi}{2}+\cos ^{-1}\left(\cos \frac{\pi}{6}\right)
\end{aligned}
$$

$$
\begin{aligned}
& =\frac{\pi}{2}+\frac{\pi}{6} \\
& =\frac{4 \pi}{6} \\
& =\frac{2 \pi}{3}
\end{aligned}
$$

46. The particular solution of the differential equation $x d y+2 y d x=0$, when $x=2, y=1$ is
(A) $x y=4$
(B) $x^{2} y=4$
(C) $x y^{2}=4$
(D) $x^{2} y^{2}=4$
47. (B)
$x d y+2 y d x=0$
$\Rightarrow \frac{\mathrm{dy}}{\mathrm{y}}+\frac{2 \mathrm{dx}}{\mathrm{x}}=0$
on Integrating

$$
\int \frac{d y}{y}+2 \int \frac{d x}{x}=C_{1}
$$

$$
\log y+2 \log x=\log C
$$

$$
\therefore \quad x^{2} y=C
$$

When $\mathrm{x}=2, \mathrm{y}=1, \mathrm{C}=4$
$\therefore$ Particular solution is $x^{2} y=4$
47. $\triangle \mathrm{ABC}$ has vertices at $\mathrm{A} \equiv(2,3,5), \mathrm{B} \equiv(-1,3,2)$ and $\mathrm{C} \equiv(\lambda, 5, \mu)$. If the median through A is equally inclined to the axes, then the values of $\lambda$ and $\mu$ respectively are
(A) 10,7
(B) 9,10
(C) 7,9
(D) 7, 10
47. (D)

$$
\begin{aligned}
\mathrm{D} & \equiv\left(\frac{\lambda-1}{2}, \frac{5+3}{2}, \frac{\mu+2}{2}\right) \\
& \equiv\left(\frac{\lambda-1}{2}, 4, \frac{\mu+2}{2}\right)
\end{aligned}
$$

Direction ratios of AD are $\frac{\lambda-1}{2}-2,4-3, \frac{\mu+2}{2}-5$

$$
\begin{aligned}
& \text { i.e. } \frac{\lambda-1-4}{2}, 1, \frac{\mu+2-10}{2} \\
& \text { i.e. } \frac{\lambda-5}{2}, 1, \frac{\mu-8}{2}
\end{aligned}
$$


go by options (since the line AD is equally inclined to coordinate axes, its direction ratios are in ratio $\pm 1: \pm 1: \pm 1)$
48. For the following distribution function $F(x)$ of a r.v.X

| $x$ | 1 | 2 | 3 | 4 | 5 | 6 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{~F}(\mathrm{x})$ | 0.2 | 0.37 | 0.48 | 0.62 | 0.85 | 1 |

$P(3<x \leq 5)=$
(A) 0.48
(B) 0.37
(C) 0.27
(D) 1.47
48. (B)

| x | 1 | 2 | 3 | 4 | 5 | 6 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathrm{f}(\mathrm{x})$ | 0.2 | 0.37 | 0.48 | 0.62 | 0.85 | 1 |
| $\mathrm{p}(\mathrm{x})$ | 0.2 | 0.17 | 0.11 | 0.14 | 0.23 | 0.15 |
| $\mathrm{p}(3<\mathrm{x} \leq 5)$ |  | $=\mathrm{p}(\mathrm{x}=4)+\mathrm{p}(\mathrm{x}=5)$ |  |  |  |  |
|  |  |  |  |  |  |  |
|  | $=0.14+0.23$ |  |  |  |  |  |
|  |  | $=0.37$ |  |  |  |  |

49. The lines $\frac{x-1}{2}=\frac{y+1}{2}=\frac{z-1}{4}$ and $\frac{x-3}{1}=\frac{y-k}{2}=\frac{z}{1}$ intersect each other at point
(A) $(-2,-4,5)$
(B) $(-2,-4,-5)$
(C) $(2,4,-5)$
(D) $(2,-4,-5)$
50. (B)

Go by options, only (B) option satisfies the first line.
50. $\int \frac{\sec ^{8} x}{\operatorname{cosec} x} d x=$
(A) $\frac{\sec ^{8} x}{8}+c$
(B) $\frac{\sec ^{7} \mathrm{x}}{7}+\mathrm{c}$
(C) $\frac{\sec ^{6} x}{6}+c$
(D) $\frac{\sec ^{9} \mathrm{x}}{9}+\mathrm{c}$
50. (B)

$$
\begin{aligned}
\int \frac{\sec ^{8} x}{\operatorname{cosec} x} d x & =\int \frac{\sin x}{\cos ^{8} x} d x \\
= & \int \tan x \cdot \sec ^{7} x d x \\
= & \int \sec ^{6} x \cdot \sec x \tan x d x \\
& \sec x=t \\
& =\int t=\sec x \cdot \tan x \cdot d x \\
& =\frac{t^{7}}{7}+c \\
& =\frac{\sec ^{7} x}{7}+c
\end{aligned}
$$

LOGARITHMS

|  | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 50 | 6990 | 6998 | 7007 | 7016 | 7024 | 7033 | 7042 | 7050 | 7059 | 7067 | 1 | 2 | 3 | 3 | 4 | 5 | 6 | 7 | 8 |
| 51 | 7076 | 7084 | 7093 | 7101 | 7110 | 7118 | 7126 | 7135 | 7143 | 7152 | 1 | 2 | 3 | 3 | 4 | 5 | 6 | 7 |  |
| 52 | 7160 | 7168 | 7177 | 7185 | 7193 | 7202 | 7210 | 7218 | 7226 | 7235 | 1 | 2 | 2 | 3 | 4 | 5 | 6 | 7 |  |
| 53 | 7243 | 7251 | 7259 | 7267 | 7275 | 7284 | 7292 | 7300 | 7308 | 7316 | 1 | 2 | 2 | 3 | 4 | 5 | 6 | 6 | 7 |
| 54 | 7324 | 7332 | 7340 | 7348 | 7356 | 7364 | 7372 | 7380 | 7388 | 7396 | 1 | 2 | 2 | 3 | 4 | 5 | 6 | 6 | 7 |
| 55 | 7404 | 7412 | 7419 | 7427 | 7435 | 7443 | 7451 | 7459 | 7466 | 74 | 1 | 2 | 2 | 3 | 4 | 5 | 5 | 6 | 7 |
| 56 | 7482 | 7490 | 7487 | 7505 | 7513 | 7520 | 7528 | 7536 | 7543 | 7551 | 1 | 2 | 2 | 3 | 4 | 5 | 5 | 6 | 7 |
| 57 | 7559 | 7566 | 7574 | 7582 | 7589 | 7597 | 7604 | 7612 | 7619 | 7627 | 1 | 2 | 2 | 3 | 4 | 5 | 5 | 6 | 7 |
| 58 | 7634 | 7642 | 7649 | 7657 | 7664 | 7672 | 7679 | 7686 | 7694 | 7701 | 1 | 1 | 2 | 3 | 4 | 4 | 5 | 6 | 7 |
| 59 | 7709 | 7716 | 7723 | 7731 | 7738 | 7745 | 7752 | 7760 | 7767 | 777 | 1 | 1 | 2 | 3 | 4 | 4 | 5 | 6 | 7 |
| 60 | 7782 | 7789 | 7796 | 7803 | 7810 | 7818 | 7825 | 7832 | 7839 | 7846 | 1 | 1 | 2 | 3 | 4 | 4 | 5 | 6 | 6 |
| 61 | 7853 | 7860 | 7868 | 7875 | 7882 | 7889 | 7896 | 7903 | 7910 | 7917 | 1 | 1 | 2 | 3 | 4 | 4 | 5 | 6 | 6 |
| 62 | 7924 | 7931 | 7938 | 7945 | 7952 | 7959 | 7966 | 7973 | 7980 | 7987 | 1 | 1 | 2 | 3 | 3 | 4 | 5 | 6 | 6 |
| 63 | 7993 | 8000 | 8007 | 8014 | 8021 | 8028 | 8035 | 8041 | 8048 | 8055 | 1 | 1 | 2 | 3 | 3 | 4 | 5 | 5 | 6 |
| 64 | 8062 | 8069 | 8075 | 8082 | 8089 | 8096 | 8102 | 8109 | 8116 | 8122 | 1 | 1 | 2 | 3 | 3 | 4 | 5 | 5 | 6 |
| 65 | 8129 | 8136 | 8142 | 8149 | 8156 | 8162 | 8169 | 8176 | 8182 | 8189 | 1 | 1 | 2 | 3 | 3 | 4 | 5 | 5 | 6 |
| 66 | 8195 | 8202 | 8209 | 8215 | 8222 | 8228 | 8235 | 8241 | 8248 | 8254 | 1 | 1 | 2 | 3 | 3 | 4 | 5 | 5 | 6 |
| 67 | 8261 | 8267 | 8274 | 8280 | 8287 | 8293 | 8299 | 8306 | 8312 | 8319 | 1 |  | 2 | 3 | 3 | 4 | 5 | 5 | 6 |
| 68 | 8325 | 8331 | 8338 | 8344 | 8351 | 8357 | 8363 | 8370 | 8376 | 8382 | 1 | 1 | 2 | 3 | 3 | 4 | 4 | 5 | 6 |
| 69 | 8388 | 8395 | 8401 | 8407 | 8414 | 8420 | 8426 | 8432 | 8439 | 8445 | 1 | 1 | 2 | 2 | 3 | 4 | 4 | 5 | 6 |
| 70 | 8451 | 8457 | 8463 | 8470 | 8476 | 8482 | 8488 | 8494 | 8500 | 8506 | 1 | 1 | 2 | 2 | 3 | 4 | 4 | 5 | 6 |
| 71 | 8513 | 8519 | 8525 | 8531 | 8537 | 8543 | 8549 | 8555 | 8561 | 8567. | 1 | 1 | 2 | 2 | 3 | 4 | 4 | 5 | 5 |
| 72 | 8573 | 8579 | 8585 | 8591 | 8597 | 8603 | 8609 | 8615 | 8621 | 8627 | 1 | 1 | 2 | 2 | 3 | 4 | 4 | 5 | 5 |
| 73. | 8633 | 8639 | 8645 | 8651 | 8657 | 8663 | 8669 | 8675 | 8681 | 8686 | 1 | 1 | 2 | 2 | 3 | 4 | 4 | 5 | 5 |
| 74 | 8692 | 8698 | 8704 | 8710 | 8716 | 8722 | 8727 | 8733 | 8739 | 8745 | 1 | 1 | 2 | 2 | 3 | 4 | 4 | 5 | 5 |
| 75 | 8751 | 8756 | 8762 | 8768 | 8774 | 8779 | 8785 | 8791 | 8797 | 8802 | 1 | 1 | 2 | 2 | 3 | 3 | 4 | 5 | 5 |
| 76 | 8808 | 8814 | 8820 | 8825 | 8831 | 8837 | 8842 | 8848 | 8854 | 8859 | 1 | 1 | 2 | 2 | 3 | 3 | 4 | 5 | 5 |
| 77 | 8865 | 8871 | 8876 | 8882 | 8887 | 8893 | 8899 | 8904 | 8910 | 8915 | 1 | 1 | 2 | 2 | 3 | 3 | 4 | 4 | 5 |
| 78 | 8921 | 8927 | 8932 | 8938 | 8943 | 8949 | 8954 | 8960 | 8965 | 8971 | 1 | 1 | 2 | 2 | 3 | 3 | 4 | 4 | 5 |
| 79 | 8976 | 8982 | 8987 | 8993 | 8998 | 9004 | 9009 | 9015 | 9020 | 9025 | 1 | 1 | 2 | 2 | 3 | 3 | 4 | 4 | 5 |
| 80 | 9031 | 9036 | 9042 | 9047 | 9053 | 9058 | 9063 | 9069 | 9074 | 9079 | 1 | 1 | 2 | 2 | 3 | 3 | 4 |  | 5 |
| 81 | 9085 | 9090 | 9096 | 9101 | 9106 | 9112 | 9117 | 9122 | 9128 | 9133 | 1 | 1 | 2 | 2 | 3 | 3 | 4 | 4 | 5 |
| 82 | 9138 | 9143 | 9149 | 9154 | 9159 | 916 | 9170 | 9175 | 9180 | 9186 | 1 | 1 | 2 | 2 | 3 | 3 | 4 | 4 | 5 |
| 83 | 9191 | 9196 | 9201 | 9206 | 9212 | 9217 | 9222 | 9227 | 9232 | 9238 | 1 | 1 | 2 | 2 | 3 | 3 | 4 | 4 | 5 |
| 84 | 9243 | 9248 | 9253 | 9258 | 9263 | 9269 | 9274 | 9279 | 9284 | 9289 | 1 | 1 | 2 | 2 | 3 | 3 | 4 | 4 | 5 |
| 85 | 9294 | 9299 | 9304 | 9309 | 9315 | 9320 | 9325 | 9330 | 9335 | 9340 | 1 | 1 | 2 | 2 | 3 | 3 | 4 |  | 5 |
| 86 | 9345 | 9350 | 9355 | 9360 | 9365 | 9370 | 9375 | 9380 | 9385 | 9390 | 1 | 1 | 2 | 2 | 3 | 3 | 4 | 4 | 5 |
| 87 | 9395 | 9400 | 9405 | 9410 | 9415 | 9420 | 9425 | 9430 | 9435 | 9440 | 0 | 1 | 1 | 2 | 2 |  | 3 | 4 | 4 |
| 88 | 9445 | 9450 | 9455 | 9460 | 946 | 9469 | 9474 | 9479 | 9484 | 9489 | 0 | 1 | 1 | 2 | 2 | 3 | 3 | 4 | 4 |
| 89 | 9494 | 949 | 9504 | 9509 | 9513 | 9518 | 9523 | 9528 | 9533 | 9538 | 0 | 1 | 1 | 2 | 2 | 3 | 3 | 4 | 4 |
| 90 | 9542 | 9547 | 9552 | 9557 | 9562 | 9566 | 9571 | 9576 | 9581 | 9586 | 0 | 1 | 1 | 2 | 2 | 3 | 3 | 4 | 4 |
| 91 | 9590 | 9595 | 9600 | 9605 | 9609 | 9614 | 9619 | 9624 | 9628 | 9633 | 0 | 1 | 1 | 2 | 2 | 3 | 3 |  | 4 |
| 92 | 9638 | 9643 | 9647 | 9652 | 9657 | 9661 | 9666 | 9671 | 9675 | 9680 | 0 | 1 | 1 | 2 | 2 | 3 | 3 | 4 | 4 |
| 93 | 9685 | 9689 | 9694 | 9699 | 9703 | 9708 | 9713 | 9717 | 9722 | 9727 | 0 | 1 | 1 | 2 | 2 | 3 | 3 | 4 | 4 |
| 94 | 9731 | 9736 | 9741 | 9745 | 9750 | 9754 | 9759 | 9763 | 9768 | 9773 | 0 | 1 | 1 | 2 | 2 | 3 | 3 | 4 | 4 |
| 95 | 9777 | 9782 | 9786 | 9791 | 9795 | 9800 | 9805 | 9809 | 9814 | 9818 | 0 | 1 | 1 | 2 | 2 | 3 | 3 | 4 | 4 |
| 98 | 9823 | 9827 | 9832 | 9836 | 9841 | 9845 | 9850 | 9854 | 9859 | 9863 | 0 | 1 | 1 | 2 | 2 | 3 | 3 | 4 | 4 |
| 97 | 9868 | 9872 | 9877 | 9881 | 9886 | 9890 | 9894 | 9899 | 9903 | 9908 | 0 | 1 | 1 | 2 | 2 | 3 | 3 | 4 | 4 |
| 98 | 9912 | 9917 | 9921 | 9926 | 9930 | 9934 | 9939 | 9943 | 9948 | 9952 | 0 | 1 | 1 | 2 | 2 | 3 | 3 | 4 | 4 |
| 99 | 9956 | 9961 | 9965 | 9969 | 9974 | 9978 | 9983 | 9987 | 9991 | 9996 | 0 | 1 | 1 | 2 | 2 | 3 | 3 | 3 | 4 |

ANTILOGARITHMS

|  | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.00 | 1000 | 1002 | 1005 | 1007 | 1009 | 1012 | 1014 | 1016 | 1019 | 1021 | 0 | 0 | 1 | 1 | 1 | 1 | 2 | 2 | 2 |
| 0.01 | 1023 | 1026 | 1028 | 1030 | 1033 | 1035 | 1038 | 1040 | 1042 | 1045 | 0 | 0 | 1 | 1 | 1 | 1 | 2 | 2 | 2 |
| 0.02 | 1047 | 1050 | 1052 | 1054 | 1057 | 1059 | 1062 | 1064 | 1067 | 1069 | 0 | 0 | 1 | 1 | 1 | 1 | 2 | 2 | 2 |
| 0.03 | 1072 | 1074 | 1076 | 1079 | 1081 | 1084 | 1086 | 1089 | 1091 | 1094 | 0 | 0 | 1 | 1 | 1 | 1 | 2 | 2 | 2 |
| 0.04 | 1096 | 1099 | 1102 | 1104 | 1107 | 1109 | 1112 | 1114 | 1117 | 1119 | 0 | 1 | 1 | 1 | 1 | 2 | 2 | 2 | 2 |
| 0.05 | 1122 | 1125 | 1127 | 1130 | 1132 | 1135 | 1138 | 1140 | 1143 | 1146 | 0 | 1 | 1 | 1 | 1 | 2 | 2 | 2 | 2 |
| 0.06 | 1148 | 1151 | 1153 | 1156 | 1159 | 1161 | 1164 | 1167 | 1169 | 1172 | 0 | 1 | 1 | 1 | 1 | 2 | 2 | 2 | 2 |
| 0.07 | 1175 | 1178 | 1180 | 1183 | 1186 | 1189 | 1191 | 1194 | 1197 | 1199 | 0 | 1 | 1 | 1 | 1 | 2 | 2 | 2 | 2 |
| 0.08 | 1202 | 1205 | 1208 | 1211 | 1213 | 1216 | 1219 | 1222 | 1225 | 1227 | 0 | 1 | 1 | 1 | 1 | 2 | 2 | 2 | 3 |
| 0.09 | 1230 | 1233 | 1236 | 1239 | 1242 | 1245 | 1247 | 1250 | 1253 | 1256 | 0 | 1 | 1 | 1 | 1 | 2 | 2 | 2 | 3 |
| 0.10 | 1259 | 1262 | 1265 | 1268 | 1271 | 1274 | 1276 | 1279 | 1282 | 1285 | 0 | 1 | 1 | 1 | 1 | 2 | 2 | 2 | 3 |
| 0.11 | 1288 | 1291 | 1294 | 1297 | 1300 | 1303 | 1306 | 1309 | 1312 | 1315 | 0 | 1 | 1 | 1 | 2 | 2 | 2 | 2 | 3 |
| 0.12 | 1318 | 1321 | 1324 | 1327 | 1330 | 1334 | 1337 | 1340 | 1343 | 1346 | 0 | 1 | 1 | 1 | 2 | 2 | 2 | 2 | 3 |
| 0.13 | 1349 | 1352 | 1355 | 1358 | 1361 | 1365 | 1368 | 1371 | 1374 | 1377 | 0 | 1 | 1 | 1 | 2 | 2 | 2 | 3 | 3 |
| 0.14 | 1380 | 1384 | 1387 | 1390 | 1393 | 1396 | 1400 | 1403 | 1406 | 1409 | 0 | 1 | 1 | 1 | 2 | 2 | 2 | 3 | 3 |
| 0.15 | 1413 | 1416 | 1419 | 1422 | 1426 | 1429 | 1432 | 1435 | 1439 | 1442 | 0 | 1 | 1 | 1 | 2 | 2 | 2 | 3 | 3 |
| 0.16 | 1445 | 1449 | 1452 | 1455 | 1459 | 1462 | 1466 | 1469 | 1472 | 1476 | 0 | 1 | 1 | 1 | 2 | 2 | 2 | 3 | 3 |
| 0.17 | 1479 | 1483 | 1486 | 1489 | 1493 | 1496 | 1500 | 1503 | 1507 | 1510 | 0 | 1 | 1 | 1 | 2 | 2 | 2 | 3 | 3 |
| 0.18 | 1514 | 1517 | 1521 | 1524 | 1528 | 1531 | 1535 | 1538 | 1542 | 1545 | 0 | 1 | 1 | 1 | 2 | 2 | 2 | 3 | 3 |
| 0.19 | 1549 | 1552 | 1556 | 1560 | 1563 | 1567 | 1570 | 1574 | 1578 | 1581 | 0 | 1 | 1 | 1 | 2 | 2 | 3 | 3 | 3 |
| 0.20 | 1585 | 1589 | 1592 | 1596 | 1600 | 1603 | 1607 | 1611 | 1614 | 16.18 | 0 | 1 | 1 | 1 | 2 | 2 | 3 | 3 | 3 |
| 0.21 | 1622 | 1626 | 1629 | 1633 | 1637 | 1641 | 1644 | 1648 | 1652 | 1656 | 0 | 1 | 1 | 2 | 2 | 2 | 3 | 3 | 3 |
| 0.22 | 1660 | 1663 | 1667 | 1671 | 1675 | 1679 | 1683 | 1687 | 1690 | 1694 | 0 | 1 | 1 | 2 | 2 | 2 | 3 | 3 | 3 |
| 0.23 | 1698 | 1702 | 1706 | 1710 | 1714 | 1718 | 1722 | 1726 | 1730 | 1734 | 0 | 1 | 1 | 2 | 2 | 2 | 3 | 3 | 4 |
| 0.24 | 1738 | 1742 | 1746 | 1750 | 1754 | 1758 | 1762 | 1766 | 1770 | 1774 | 0 | 1 | 1 | 2 | 2 | 2 | 3 | 3 | 4 |
| 0.25 | 1778 | 1782 | 1786 | 1791 | 1795 | 1799 | 1803 | 1807 | 1811 | 1816 | 0 | 1 | 1 | 2 | 2 | 2 | 3 | 3 | 4 |
| 0.26 | 1820 | 1824 | 1828 | 1832 | 1837 | 1841 | 1845 | 1849 | 1854 | 1858 | 0 | 1 | 1 | 2 | 2 | 3 | 3 | 3 | 4 |
| 0.27 | 1862 | 1866 | 1871 | 1875 | 1879 | 1884 | 1888 | 1892 | 1897 | 1901 | 0 | 1 | 1 | 2 | 2 | 3 | 3 | 3 | 4 |
| 0.28 | 1905 | 1910 | 1914 | 1919 | 1923 | 1928 | 1932 | 1936 | 1941 | 1945 | 0 | 1 | 1 | 2 | 2 | 3 | 3 | 4 | 4 |
| 0.29 | 1950 | 1954 | 1959 | 1963 | 1968 | 1972 | 1977 | 1982 | 1986 | 1991 | 0 | 1 | 1 | 2 | 2 | 3 | 3 | 4 | 4 |
| 0.30 | 1995 | 2000 | 2004 | 2009 | 2014 | 2018 | 2023 | 2028 | 2032 | 2037 | 0 | 1 | 1 | 2 | 2 | 3 | 3 | 4 | 4 |
| 0.31 | 2042 | 2046 | 2051 | 2056 | 2061 | 2065 | 2070 | 2075 | 2080 | 2084 | 0 | 1 | 1 | 2 | 2 | 3 | 3 | 4 | 4 |
| 0.32 | 2089 | 2094 | 2099 | 2104 | 2109 | 2113 | 2118 | 2123 | 2128 | 2133 | 0 | 1 | 1 | 2 | 2 | 3 | 3 | 4 | 4 |
| 0.33 | 2138 | 2143 | 2148 | 2153 | 2158 | 2163 | 2168 | 2173 | 2178 | 2183 | 0 | 1. | 1 | 2 | 2 | 3 | 3 | 4 | 4 |
| 0.34 | 2188 | 2193 | 2198 | 2203 | 2208 | 2213 | 2218 | 2223 | 2228 | 2234 | 1 | 1 | 2 | 2 | 3 | 3 | 4 | 4 | 5 |
| 0.35 | 2239 | 2244 | 2249 | 2254 | 2259 | 2265 | 2270 | 2275 | 2280 | 2286 | 1 | 1 | 2 | 2 | 3 | 3 | 4 | 4 | 5 |
| 0.36 | 2291 | 2296 | 2301 | 2307 | 2312 | 2317 | 2323 | 2328 | 2333 | 2339 | 1 | 1 | 2 | 2 | 3 | 3 | 4 | 4 | 5 |
| 0.37 | 2344 | 2350 | 2355 | 2360 | 2366 | 2371 | 2377 | 2382 | 2388 | 2393 | 1 | 1 | 2 | 2 | 3 |  | 4 | 4 | 5 |
| 0.38 | 2399 | 2404 | 2410 | 2415 | 2421 | 2427 | 2432 | 2438 | 2443 | 2449 | 1 | 1 | 2 | 2 | 3 | 3 | 4 | 4 | 5 |
| 0.39 | 2455 | 2460 | 2466 | 2472 | 2477 | 2483 | 2489 | 2495 | 2500 | 2506 | 1 | 1 | 2 | 2 | 3 | 3 | 4 | 5 | 5 |
| 0.40 | 2512 | 2518 | 2523 | 2529 | 2535 | 2541 | 2547 | 2553 | 2559 | 2564 | 1 | 1 | 2 | 2 | 3 | 4 | 4 | 5 | 5 |
| 0.41 | 2570 | 2576 | 2582 | 2588 | 2594 | 2600 | 2606 | 2612 | 2618 | 2624 | 1 | 1 | 2 | 2 | 3 | 4 | 4 | 5 | 5 |
| 0.42 | 2630 | 2636 | 2642 | 2649 | 2655 | 2661 | 2667 | 2673 | 2679 | 2685 | 1 | 1 | 2 | 2 | 3 | 4 | 4 | 5 | 6 |
| 0.43 | 2692 | 2698 | 2704 | 2710 | 2716 | 2723 | 2729 | 2735 | 2742 | 2748 | 1 | 1 | 2 | 3 | 3 | 4 | 4 | 5 | 6 |
| 0.44 | 2754 | 2761 | 2767 | 2773 | 2780 | 2786 | 2793 | 2799 | 2805 | 2812 | 1 | 1 | 2 | 3 | 3 | 4 | 4 | 5 | 6 |
| 0.45 | 2818 | 2825 | 2831 | 2838 | 2844 | 2851 | 2858 | 2864 | 2871 | 2877 | 1 | 1 | 2 | 3 | 3 | 4 | 5 | 5 | 6 |
| 0.46 | 2884 | 2891 | 2897 | 2904 | 2911 | 2917 | 2924 | 2931 | 2938 | 2944 | 1 | 1 | 2 | 3 | 3 | 4 | 5 | 5 | 6 |
| 0.47 | 2951 | 2958 | 2965 | 2972 | 2979 | 2985 | 2992 | 2999 | 3006 | 3013 | 1 | 1 | 2 | 3 | 3 | 4 | 5 | 5 | 6 |
| 0.48 | 3020 | 3027 | 3034 | 3041 | 3048 | 3055 | 3062 | 3069 | 3076 | 3083 | 1 | 1 | 2 | 3 | 4 | 4 | 5 | 6 | 6 |
| 0.49 | 3090 | 3097 | 3105 | 3112 | 3119 | 3126 | 3133 | 3141 | 3148 | 3155 | 1 | 1 | 2 | 3 | 4 | 4 | 5 | 6 | 6 |

ANTILOGARITHMS

|  | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 1 | 2 | 3 | 4 | 6 | 6 | 7 | 8 | $\theta$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.50 | 3162 | 3170 | 3177 | 3184 | 3192 | 3199 | 3206 | 3214 | 3221 | 3228 | 1 |  | 2 | 3 | 4 | 4 | 5 | 6 | 7 |
| 0.51 | 3236 | 3243 | 3251 | 3258 | 3266 | 3273 | 3281 | 3289 | 3296 | 3304 | 1 | 2 | 2 | 3 | 4 | 5 | 5 | 6 | 7 |
| 0.62 | 3311 | 3319 | 3327 | 3334 | 3342 | 3350 | 3357 | 3365 | 3373 | 3381 | 1 | 2 | 2 | 3 | 4 | 5 | 5 | 6 | 7 |
| 0.63 | 3388 | 3396 | 3404 | 3412 | 3420 | 3428 | 3436 | 3443 | 3451 | 3459 | 1 | 2 | 2 | 3 | 4 | 5 | 6 | 6 | 7 |
| 0.64 | 3467 | 3475 | 3483 | 3491 | 3498 | 3508 | 3516 | 3524 | 3532 | 3540 |  | 2 | 2 | 3 | 4 | 5 | 6 | 6 | 7 |
| 0.65 | 3548 | 3556 | 3565 | 3573 | 3581 | 3589 | 3597 | 3606 | 3614 | 3622 | 1 | 2 | 2 | 3 | 4 | 5 | 6 | 7 | 7 |
| 0.68 | 3631 | 3639 | 3648 | 3656 | 3664 | 3673 | 3681 | 3690 | 3698 | 3707 | 1 | 2. | 3 | 3 | 4 | 5 | 6 | 7 | 8 |
| 0.67 | 3715 | 3724 | 3733 | 3741 | 3750 | 3758 | 3767 | 3776 | 3784 | 3793 | 1 | 2 | 3 | 3 | 4 | 5 | 6 | 7 | 8 |
| 0.58 | 3802 | 3811 | 3819 | 3828 | 3837 | 3846 | 3855 | 3864 | 3873 | 3882 | 1 | 2 | 3 | 4 | 4 | 5 | 6 | 7 | 8 |
| 0.68 | 3890 | 3899 | 3908 | 3917 | 3926 | 3936 | 3945 | 3854 | 3963 | 3972 | 1 | 2 | 3 | 4 | 5 | 5 | 6 | 7 | 8 |
| 0.80 | 3981 | 3890 | 3999 | 4009 | 4018 | 4027 | 4036 | 4046 | 4055 | 4064 | 1 | 2 | 3 | 4 | 5 | 6 | 6 | 7 | 8 |
| 0.6 | 4074 | 4083 | 4093 | 4102 | 4111 | 4121 | 4130 | 4140 | 4150 | 4159 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
| 0.62 | 4169 | 4178 | 4188 | 4198 | 4207 | 4217 | 4227 | 4236 | 4246 | 4256 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
| 0.63 | 4286 | 4276 | 4285 | 4295 | 4305 | 4315 | 4325 | 4335 | 4345 | 4355 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
| 0.64 | 4365 | 4375 | 4385 | 4396 | 4408 | 4416 | 4426 | 4436 | 4446 | 4457 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 8 |
| 0.65 | 4487 | 4477 | 4487 | 4498 | 4508 | 4618 | 4529 | 4539 | 4550 | 4560 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
| 0.66 | 4571 | 4581 | 4582 | 4803 | 4613 | 4624 | 4634 | 4645 | 4656 | 4667 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 9 | 10 |
| 0.67 | 4677 | 4888 | 4698 | 4710 | 4721 | 4732 | 4742 | 4753 | 4764 | 4775 | 1 | 2 | 3 | 4 | 5 | 7 | 8 | 9 | 10 |
| 0.68 | 4786 | 4797 | 4808 | 4819 | 4831 | 4842 | 4853 | 4864 | 4875 | 4887 | 1 | 2 | 3 | 4 | 6 | 7 | 8 | 9 | 10 |
| 0.69 | 4898 | 4909 | 4920 | 4932 | 4843 | 4955 | 4986 | 4877 | 4989 | 5000 | 1 | 2 | 3 | 5 | 6 | 7 | 8 | 9 | 10 |
| 0.70 | 5012 | 5023 | 5035 | 5047 | 5058 | 5070 | 5082 | 5083 | 5105 | 5117 | 1 | 2 | 4 | 5 | 6 | 7 | 8 | 9 | 11 |
| 0.71 | 5129 | 5140 | 5152 | 5164 | 5178 | 5188 | 5200 | 5212 | 5224 | 5238 | 1 | 2 | 4 | 5 | 6 | 7 | 8 | 10 | 11 |
| 0.72 | 5248 | 5260 | 5272 | 5284 | 5297 | 5309 | 5321 | 5333 | 5346 | 5348 | 1 | 2 | 4 | 5 | 6 | 7 | 9 | 10 | 11 |
| 0.73 | 5370 | 5383 | 5395 | 5408 | 5420 | 5433 | 5445 | 5458 | 5470 | 5483 | 1 | 3 | 4 | 5 | 6 | 8 | 9 | 10 | 11 |
| 0.74 | 5495 | 5508 | 5521 | 5534 | 5546 | 5559 | 5572 | 5585 | 5598 | 5610 | 1 | 3 | 4 | 5 | 6 | 8 | 9 | 10 | 12 |
| 0.76 | 5623 | 5836 | 5649 | 5662 | 5675 | 5689 | 5702 | 5715 | 5728 | 5741 | 1 | 3 | 4 | 5 | 7 | 8 | 9 | 10 | 12 |
| 0.76 | 5754 | 5768 | 5781 | 5794 | 5808 | 5821 | 5834 | 5848 | 5861 | 5875 | 1 | 3 | 4 | 5 | 7 | 8 | 9 | 11 | 12 |
| 0.77 | 5888 | 5902 | 5816 | 5929 | 5943 | 6957 | 5970 | 5884 | 5998 | 6012 | 1 | 3 | 4 | 5 | 7 | 8 | 10 | 11 | 12 |
| 0.78 | 6026 | 6039 | 6053 | 6067 | 6081 | 6095 | 6109 | 6124 | 6138 | 6152 | 1 | 3 | 4 | 6 | 7 | 8 | 10 | 11 | 13 |
| 0.79 | 8166 | 6180 | 6194 | 6209 | 6223 | 6237 | 6252 | 6286 | 6281 | 6295 | 1 | 3 | 4 | 6 | 7 | 8 | 10 | 11 | 13 |
| 0.80 | 6310 | 6324 | 6339 | 6353 | 6368 | 6383 | 6397 | 6412 | 6427 | 6442 | 1 | 3 | 4 | 6 | 7 | 9 | 10 | 12 | 13 |
| 0.81 | 6457 | 6471 | 6486 | 6501 | 6516 | 6531 | 6546 | 6581 | 6577 | 6592 | 2 | 3 | 5 | 6 | 8 | 9 | 11 | 12 | 14 |
| 0.82 | 6607 | 6622 | 6637 | 6653 | 6868 | 6883 | 6899 | 6714 | 6730 | 6745 | 2 | 3 | 5 | 6 | 8 | 9 | 11 | 12 | 14 |
| 0.83 | 6761 | 6776 | 6792 | 6808 | 6823 | 6839 | 6855 | 6871 | 6887 | 8902 | 2 | 3 | 5 | 6 | 8 | 9 | 11 | 13 | 14 |
| 0.84 | 6918 | 6934 | 6950 | 6966 | 6982 | 6998 | 7015 | 7031 | 7047 | 7083 | 2 | 3 | 5 | 6 | 8 | 10 | 11 | 13 | 15 |
| 0.85 | 7079 | 7096 | 7112 | 7129 | 7145 | 7161 | 7178 | 7194 | 7211 | 7228 | 2 | 3 | 5 | 7 | 8 | 10 | 12 | 13 | 15 |
| 0.88 | 7244 | 7261 | 7278 | 7295 | 7311 | 7328 | 7345 | 7362 | 7378 | 7398 | 2 | 3 | 5 | 7 | 8 | 10 | 12 | 13 | 15 |
| 0.87 | 7413 | 7430 | 7447 | 7464 | 7482 | 7499 | 7516 | 7534 | 7551 | 7568 | 2 | 3 | 5 | 7 | 9 | 10 | 12 | 14 | 16 |
| 0.88 | 7588 | 7803 | 7621 | 7638 | 7858 | 7674 | 7681 | 7709 | 7727 | 7745 | 2 | 4 | 5 | 7 | 8 | 11 | 12 | 14 | 16 |
| 0.88 | 7782 | 7780 | 7798 | 7816 | 7834 | 7852 | 7870 | 7889 | 7807 | 7925 | 2 | 4 | 5 | 7 | $\theta$ | 11 | 13 | 14 | 16 |
| 0.90 | 7943 | 7982 | 7980 | 7888 | 8017 | 8035 | 8054 | 8072 | 8091 | 8110 | 2 | 4 | 6 | 7 | 9 | 11 | 13 | 15 | 17 |
| 0.81 | 8128 | 8147 | 8168 | 8185 | 8204 | 8222 | 8241 | 8260 | 8279 | 8290 | 2 | 4 | 6 | 8 | $\theta$ | 11 | 13 | 15 | 17 |
| 0.92 | 8318 | 8337 | 8356 | 8375 | 8305 | 8414 | 8433 | 8453 | 8472 | 8492 | 2 | 4 | 6 | 8 | 10 | 12 | 14 | 15 | 17 |
| 0.93 | 8611 | 8531 | 8551 | 8670 | 8590 | 8810 | 8830 | 8850 | 8870 | 8680 | 2 | 4 | 6 | 8 | 10 | 12 | 14 | 16 | 18 |
| 0.94 | 8710 | 8730 | 8750 | 8770 | 8790 | 8810 | 8831 | 8851 | 8872 | 8882 | 2 | 4 | 6 | 8 | 10 | 12. | 14 | 16 | 18 |
| 0.88 | 8913 | 8933 | 8964 | 8974 | 8895 | 9016 | 9036 | 9057 | 9078 | 8089 | 2 | 4 | 6 | 8 | 10 | 12 | 16 | 17 | 10 |
| 0.98 | 9120 | 9141 | 9162 | 8183 | 9204 | 9220 | 0247 | 9288 | 9290 | 9311 | 2 | 4 | 6 | 8 | 11 | 13 | 15 | 17 | 10 |
| 0.07 | 9333 | 8364 | 9378 | 9397 | 9419 | 0441 | 9482 | 9484 | 9508 | 9528 | 2 | 4 | 7 | 8 | 11 | 13 | 15 | 17 | 20 |
| 0.98 | 8850 | 9672 | 9594 | 9816 | 8838 | 9881 | 9883 | 9705 | 9727 | 9750 | 2 | 4 | 7 | 0 | 11 | 13 | 16 | 18 | 20 |
| 0.08 | 9772 | 9795 | 9817 | 9840 | 8863 | 9886 | 8808 | 8931 | 9954 | 9977 | 2 | 5 | 7 | 8 | 11 | 14 | 18 | 18 | 20 |

