

# AP 5301/8301

## Instrumental Methods of Analysis and Laboratory

### Lecture 11

### Ion Beam Analysis

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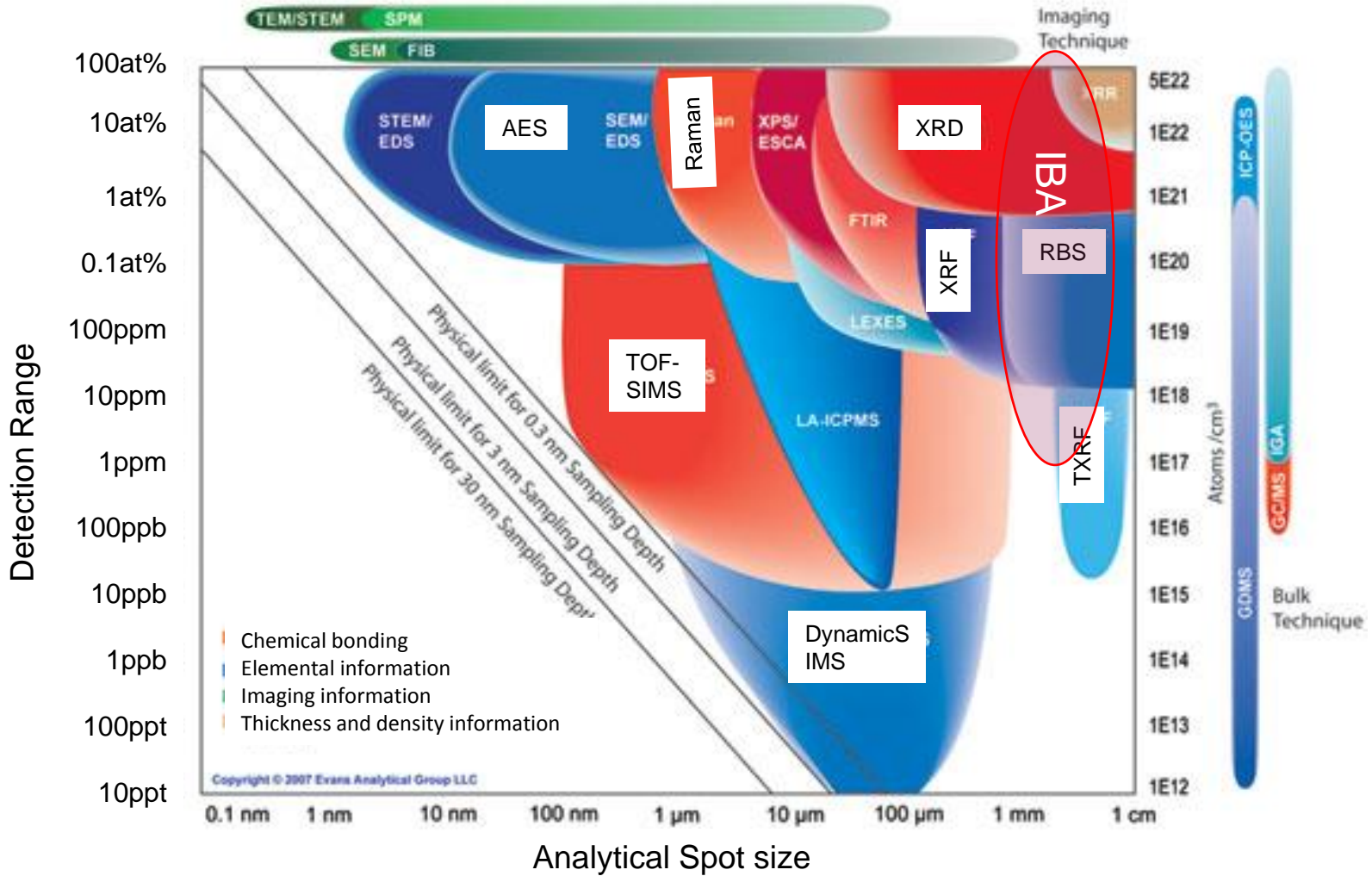
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# Lecture 8: outline

- Introduction
  - Ion Beam Analysis: an overview
- Rutherford backscattering spectrometry (RBS)
  - Introduction-history
  - Basic concepts of RBS
    - Kinematic factor (K)
    - Scattering cross-section
    - Depth scale
  - Quantitative thin film analysis
  - RBS data analysis
- Other IBA techniques
  - Hydrogen Forward Scattering
  - Particle induced x-ray emission (PIXE)
- Ion channeling
  - Minimum yield and critical angle
  - Dechanneling by defects
  - Impurity location

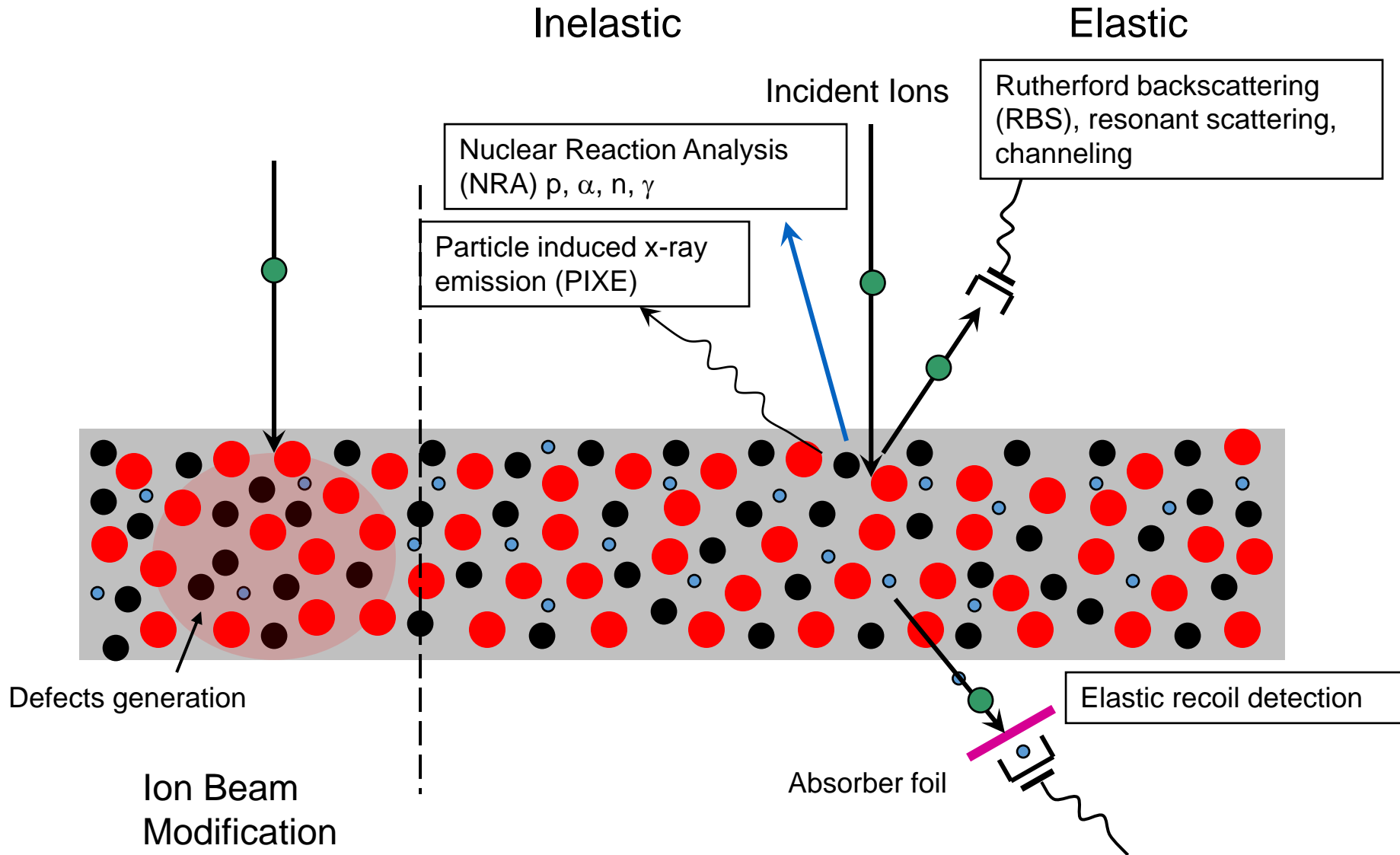
# Analytical Techniques



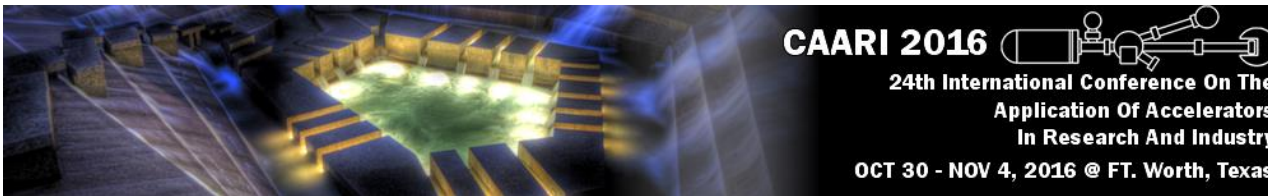
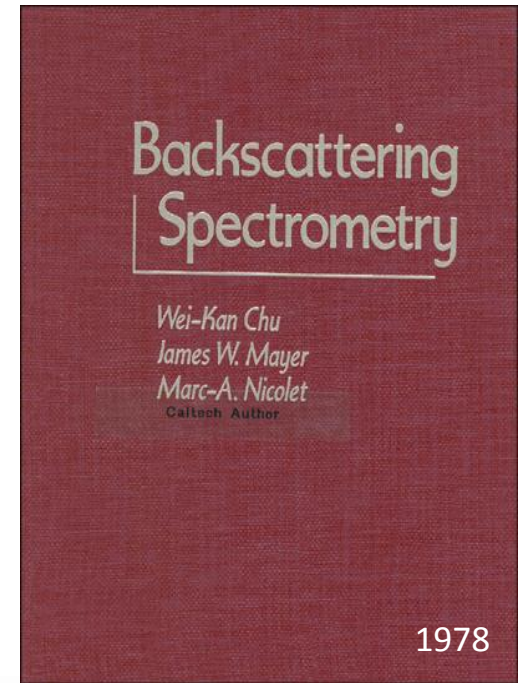
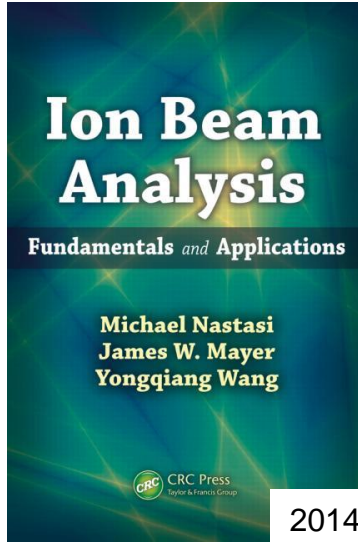
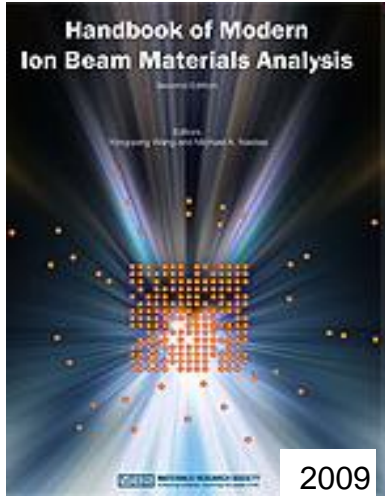
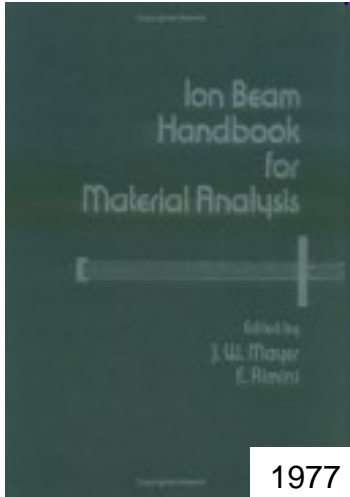
But IBA is typically quantitative and depth sensitive

<http://www.eaglabs.com>

# Ion Beam Analysis: an overview



# Ion Beam Analysis



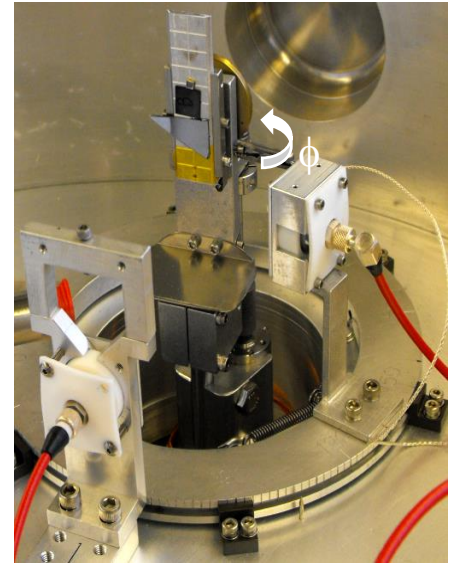
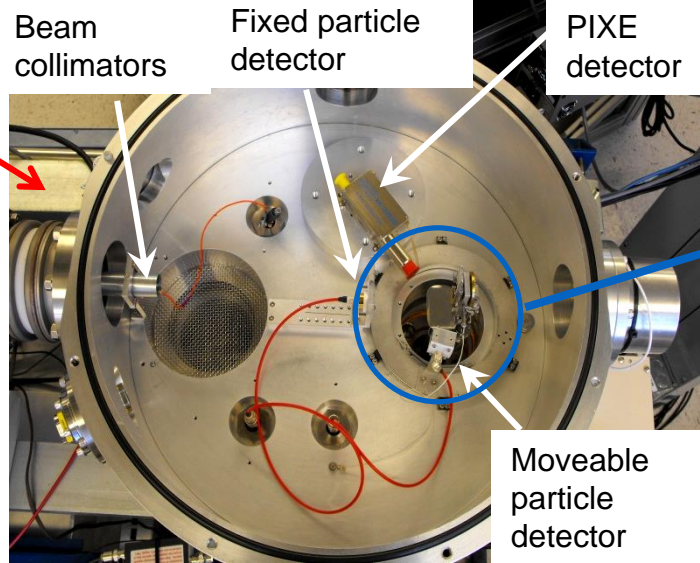
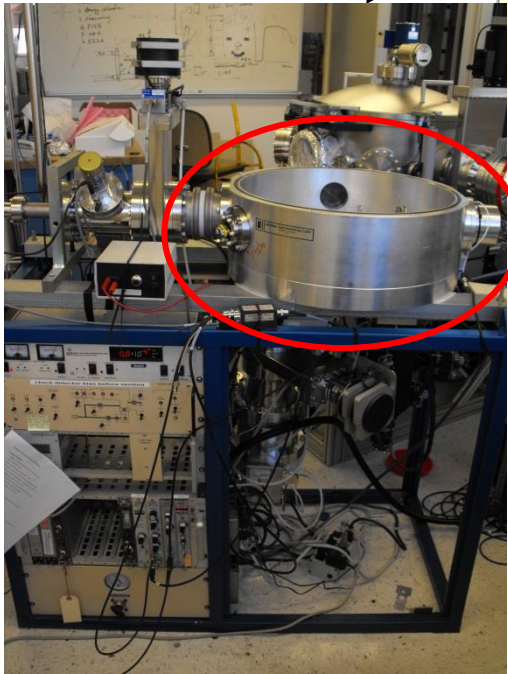
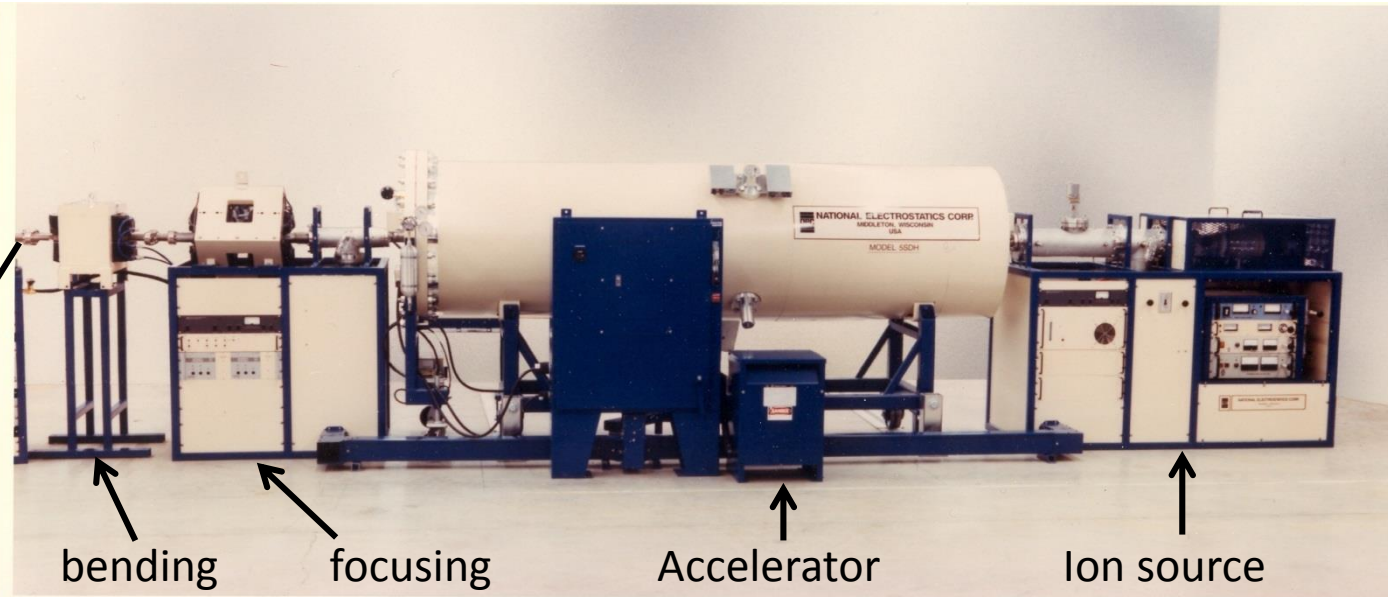
# Why IBA?

- Simple in principle
- Fast and direct
- Quantitative (without standard for RBS)
- Depth profiling without chemical or physical sectioning
- Non-destructive
- Wide range of elemental coverage
- No special specimen preparation required
- Can be applied to crystalline or amorphous materials
- Simultaneous analysis with various ion beam techniques (RBS, PIXE, NRA, channeling, etc.)
- Can obtain a lot of information in one measurement



# A typical Ion Beam Analysis Facility

Experimental chamber

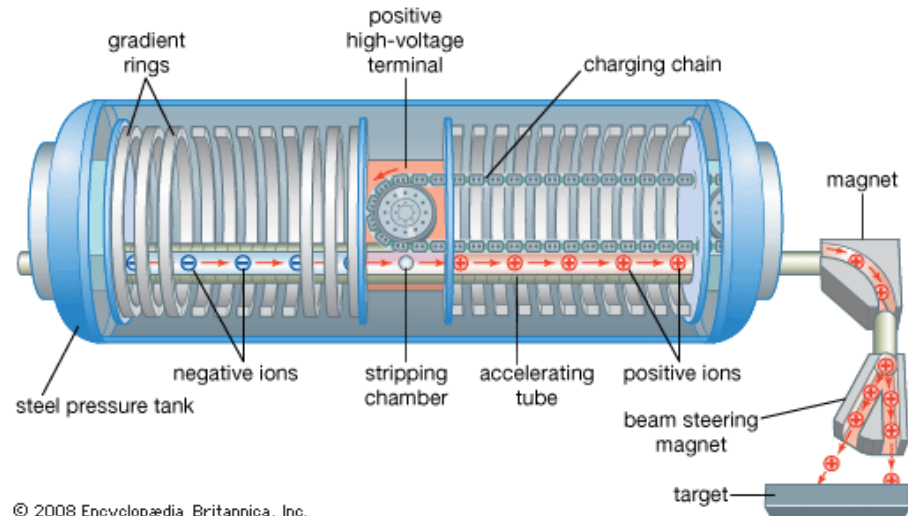


# IBA Equipment: accelerator

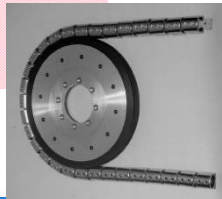
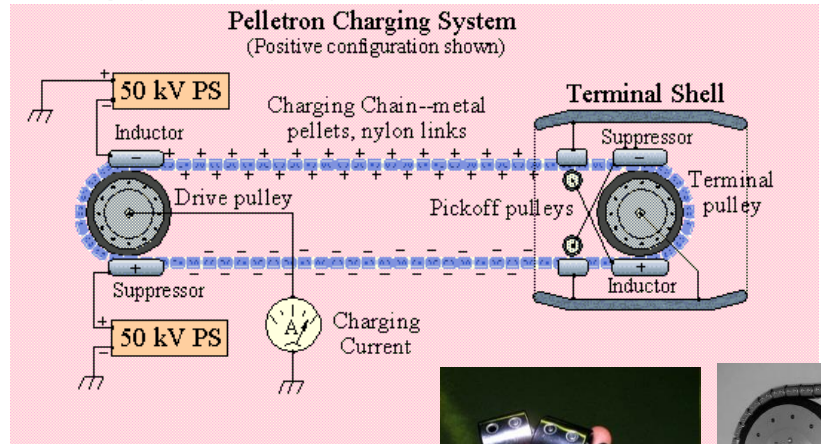
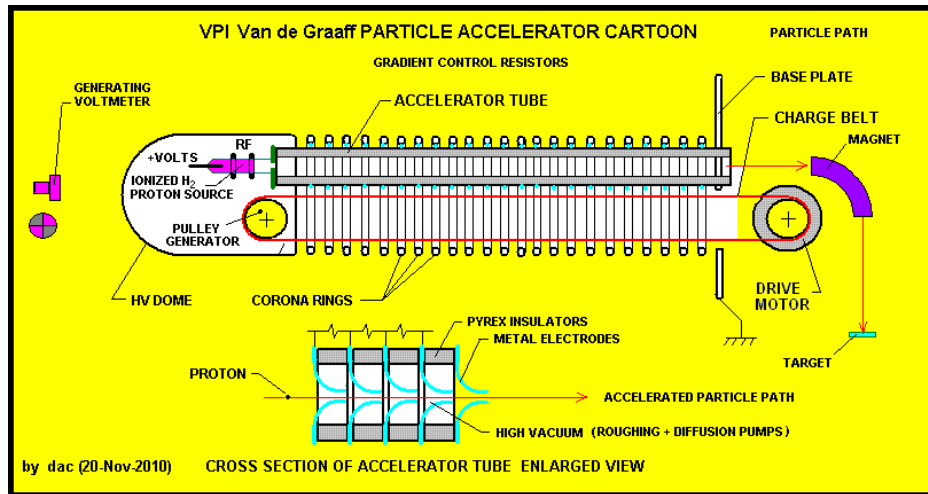
## Van de Graaff (single ended)



## Tandem Pelletron

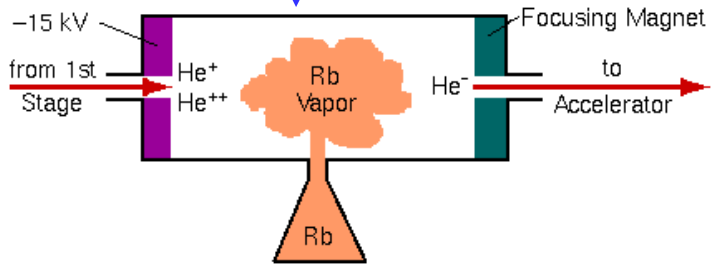
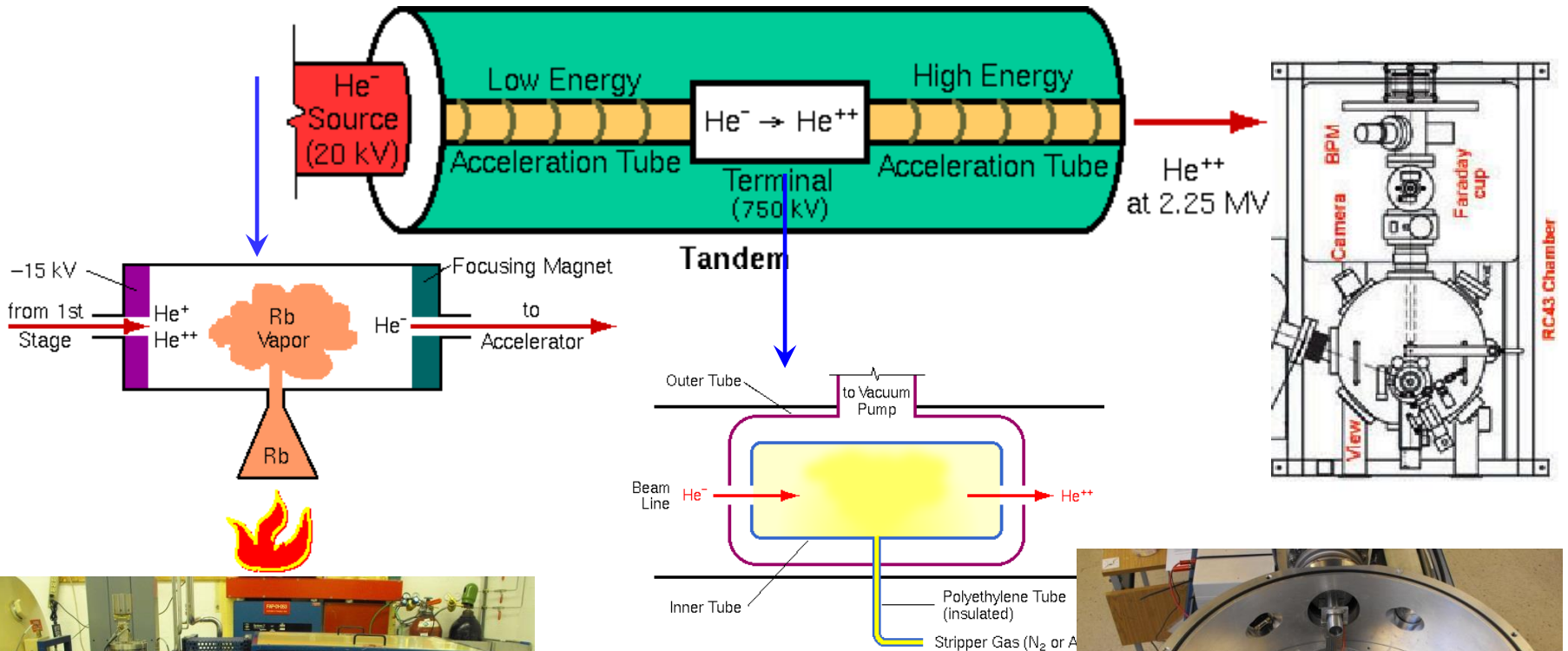


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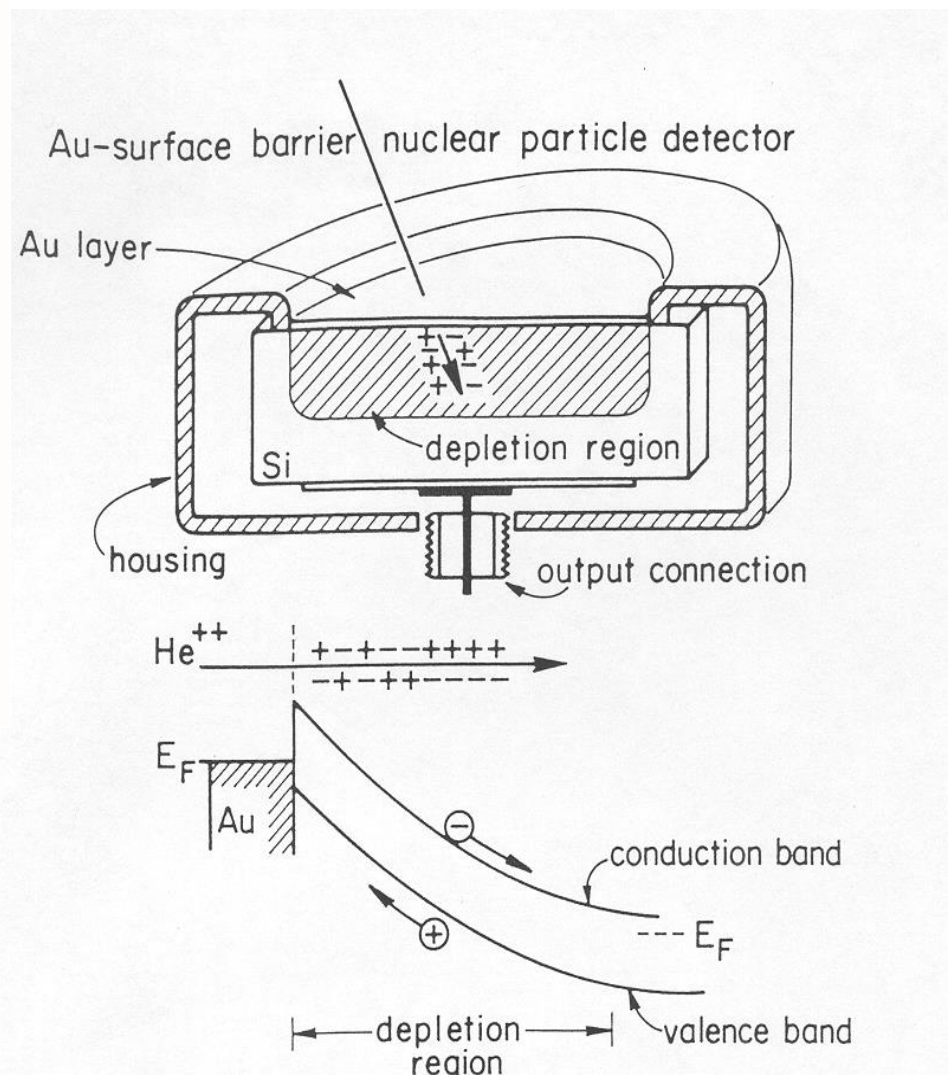
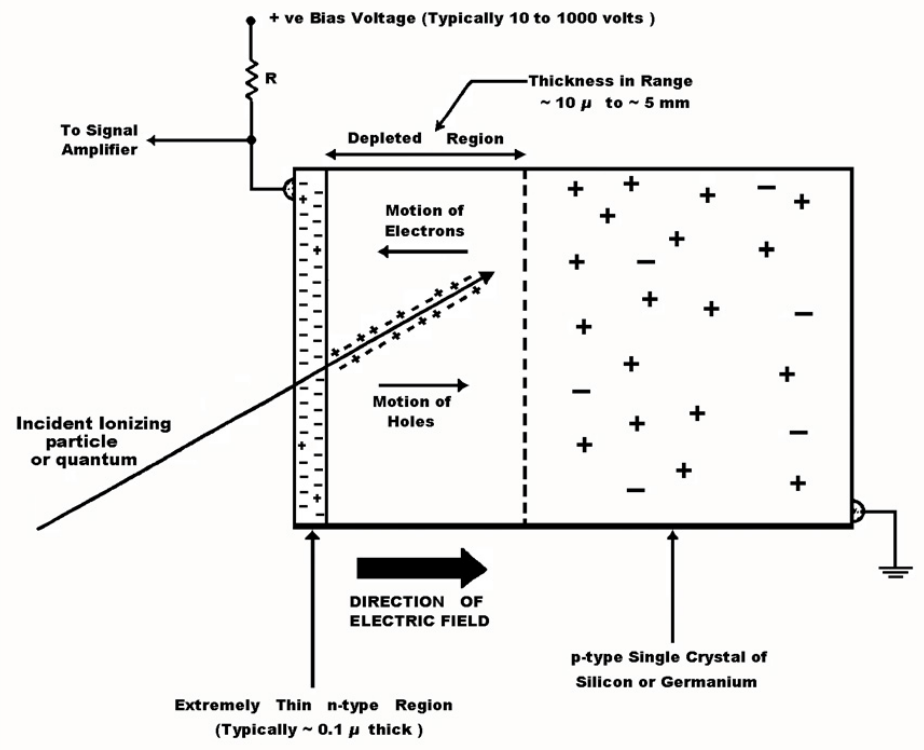




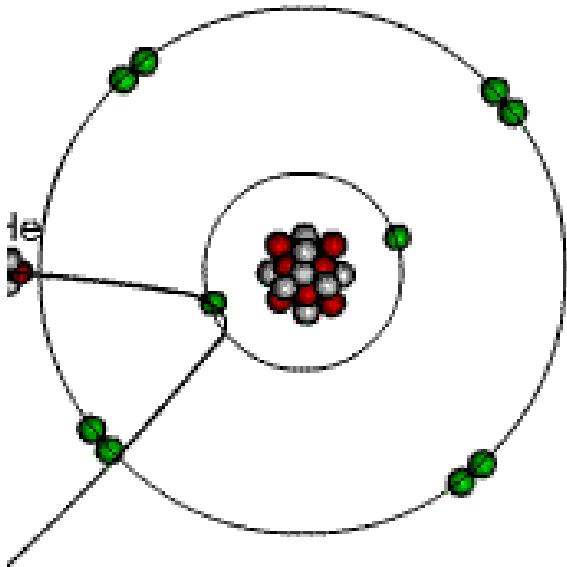
# IBA Equipment: tandem pelletron



# Equipment: particle detector



# Rutherford Backscattering Spectrometry (RBS)

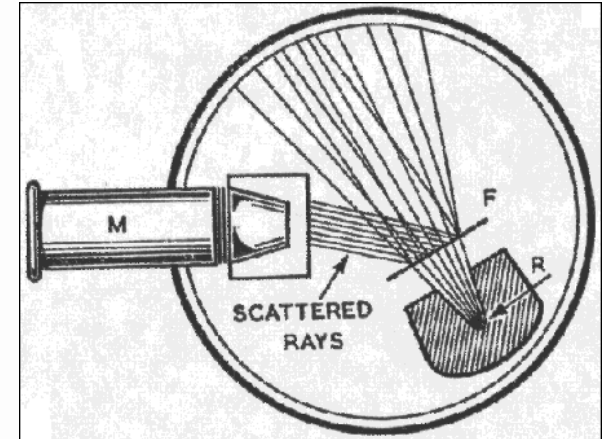
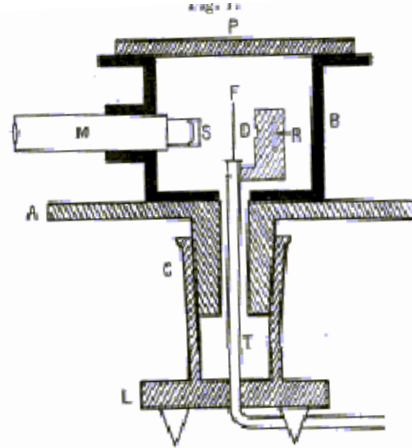


- Relatively simple physics
  - Requires some experimental skills
  - Requires some data simulation to obtain the most out of the spectrum
  - The only quantitative and absolute method to determine
    - atomic concentration with no matrix effect
    - composition variation with depth
    - layer thickness
    - damage distribution and impurity lattice location
- of multi-elemental, multi-layered films

# Rutherford Backscattering Spectrometry (RBS) a brief history



## The original experiment



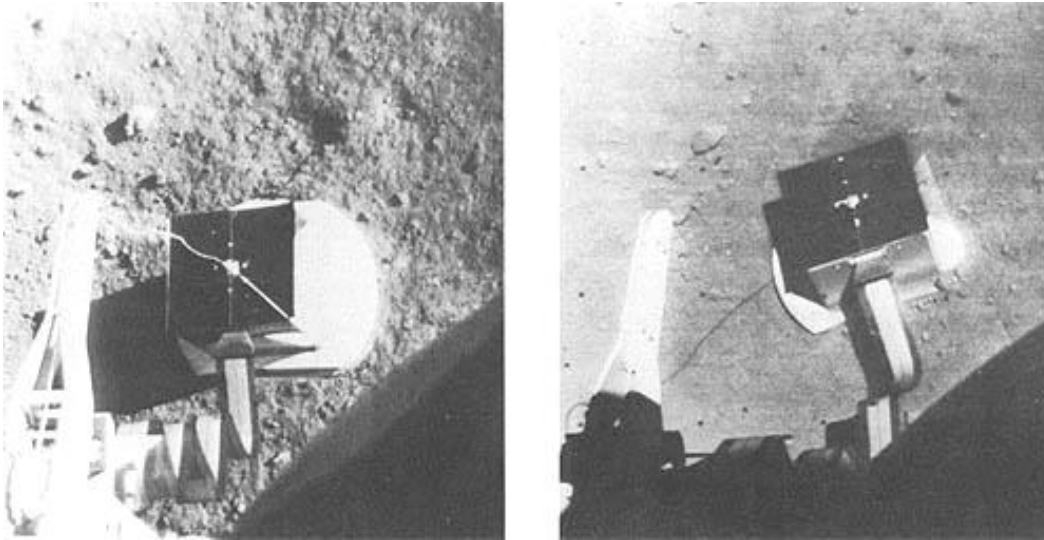
Alpha particles at a thin gold foil experiment by Hans Geiger and Ernest Marsden in 1909.

- 1) Almost all of the alpha particles went through the gold foil
- 2) Some of the alpha particles were deflected only slightly, usually  $2^\circ$  or less.
- 3) A very, very few (1 in 8000 for platinum foil) alpha particles were turned through an angle of  $90^\circ$  or more.

"We shall suppose that for distances less than  $10^{-12}$  cm the central charge and also the charge on the alpha particle may be supposed to be concentrated at a point." (1911)



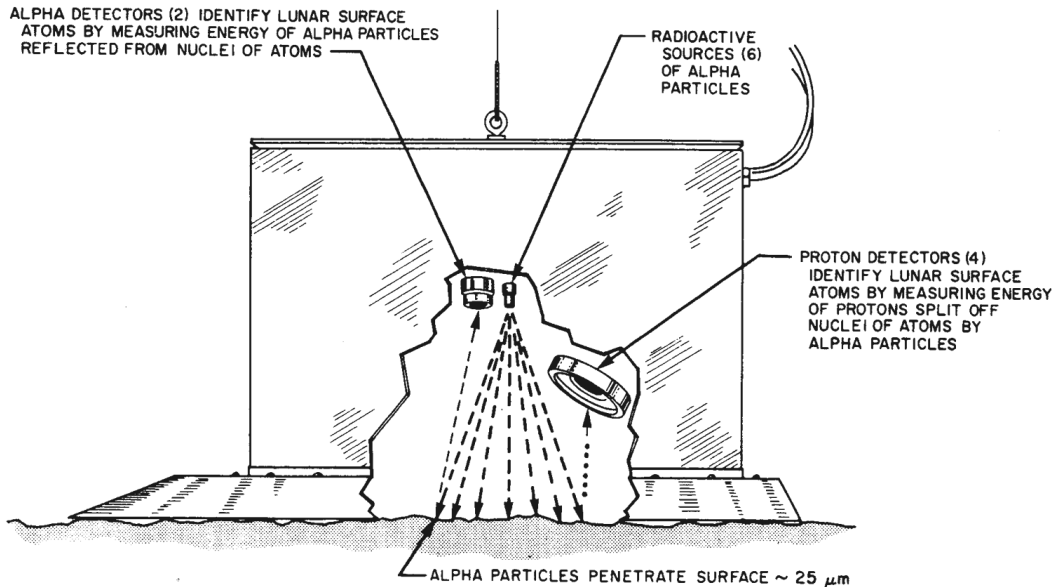
# RBS: The Surveyor V experiment



ALPHA DETECTORS (2) IDENTIFY LUNAR SURFACE ATOMS BY MEASURING ENERGY OF ALPHA PARTICLES REFLECTED FROM NUCLEI OF ATOMS

RADIOACTIVE SOURCES (6) OF ALPHA PARTICLES

PROTON DETECTORS (4) IDENTIFY LUNAR SURFACE ATOMS BY MEASURING ENERGY OF PROTONS SPLIT OFF OF NUCLEI OF ATOMS BY ALPHA PARTICLES



**Surveyor V**, first of its spacecraft family to obtain information about the chemical nature of the Moon's surface, landed in Mare Tranquillitatis on September 11, 1967.

"**Surveyor V** carried an instrument to determine the principal chemical elements of the lunar-surface material," explained ANTHONY TURKEVICH, Enrico Fermi institute and Chemistry Department, University of Chicago. "After landing, upon command from Earth, the instrument was lowered by a nylon cord to the surface of the Moon ..."

# General applications of RBS

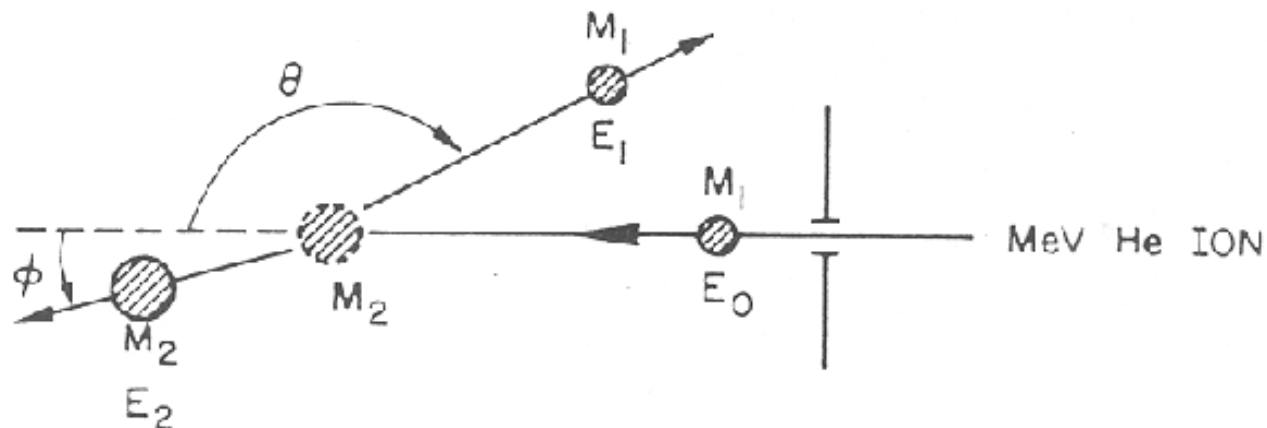
- Quantitative analysis of thin films
  - thickness, composition, uniformity in depth
  - solid state reactions
  - interdiffusion
- Crystalline perfection of homo- and heteroepitaxial thin films
- Quantitative measurements of impurities in substrates
- Defect distribution in single-crystal samples
- Surface atom relaxation in single crystals
- Lattice location of impurities in single crystals

# RBS: basic concepts

- Kinematic factor: elastic energy transfer from a projectile to a target atom can be calculated from collision kinematics
  - mass determination
- Scattering cross-section: the probability of the elastic collision between the projectile and target atoms can be calculated
  - quantitative analysis of atomic composition
- Energy Loss: inelastic energy loss of the projectile ions through the target
  - perception of depth

These allow RBS analysis to give quantitative depth distribution of targets with different masses

# Kinematic factor: $K$



Conservation of energy :

$$\frac{1}{2}m_1v^2 = \frac{1}{2}m_1v_1^2 + \frac{1}{2}m_2v_2^2$$

Conservation of momentum:

$$m_1v = m_1v_1 \cos \theta + m_2v_2 \cos \phi$$

$$m_1v_1 \sin \theta = m_2v_2 \sin \phi$$

$$K_{m_2} = \frac{E_1}{E_0} = \left[ \frac{\sqrt{(m_2^2 - m_1^2 \sin^2 \theta)} + m_1 \cos \theta}{(m_2 + m_1)} \right]^2 = K(\theta, m_2, m_1)$$



# Kinematic Factor

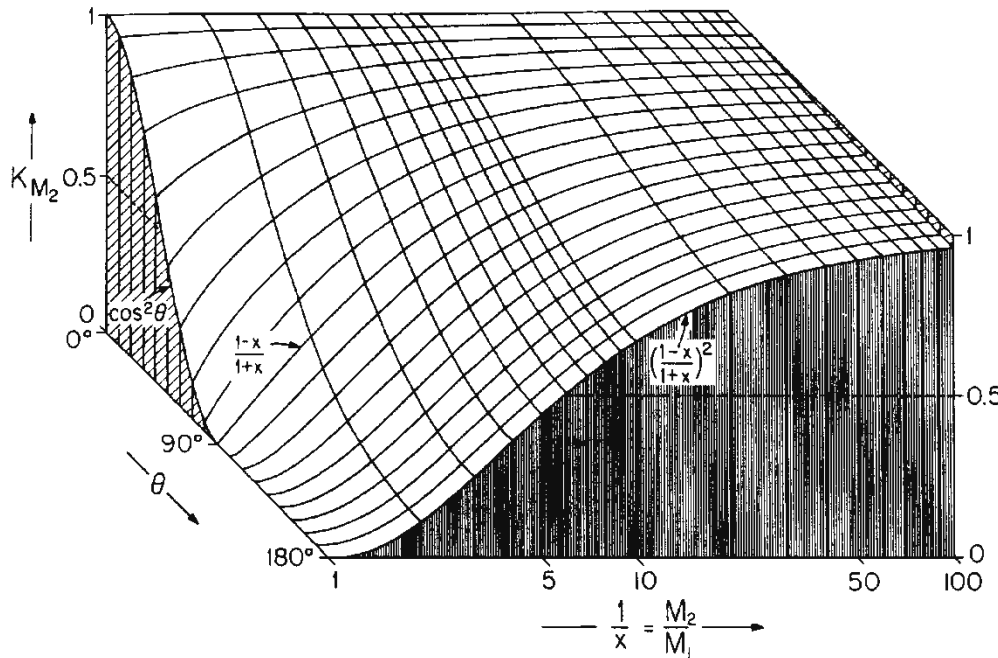
$$K_{m_2} = \frac{E_1}{E_o} = \left[ \frac{\sqrt{(m_2^2 - m_1^2 \sin^2 \theta) + m_1 \cos \theta}}{(m_2 + m_1)} \right]^2$$

$$K_{m_2}(\theta = 180^\circ) = \left[ \frac{(m_2 - m_1)}{(m_2 + m_1)} \right]^2$$

$$K_{m_2}(\theta = 90^\circ) = \frac{(m_2 - m_1)}{(m_2 + m_1)}$$

When  $m_2 \gg m_1$ :

$$K_{m_2}(\theta = 180^\circ) \sim 1$$



# Element identification

2.5 MeV He ion with  $\theta=170^\circ$

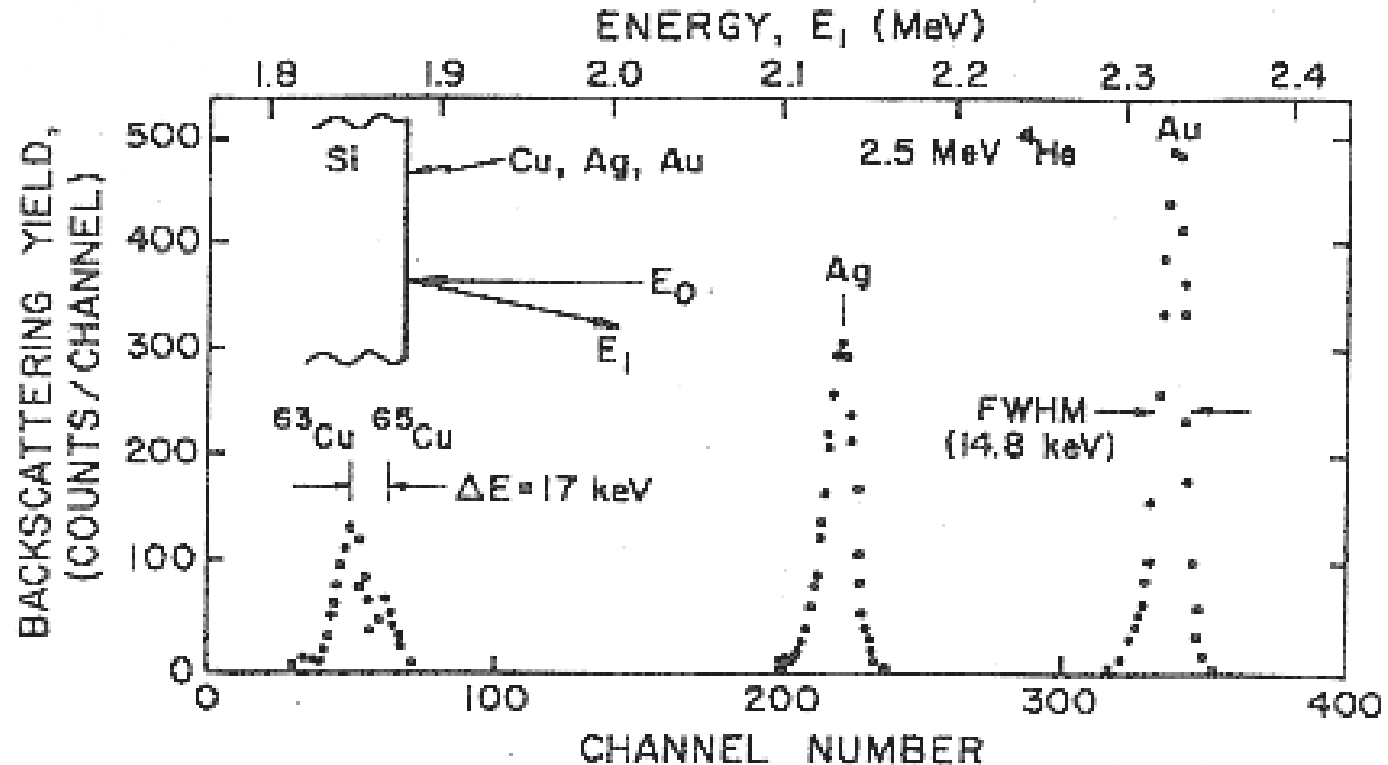
$$K(^{197}\text{Au}) = 0.923$$

$$K(^{109}\text{Ag}) = 0.864$$

$$K(^{107}\text{Ag}) = 0.862$$

$$K(^{65}\text{Cu}) = 0.783$$

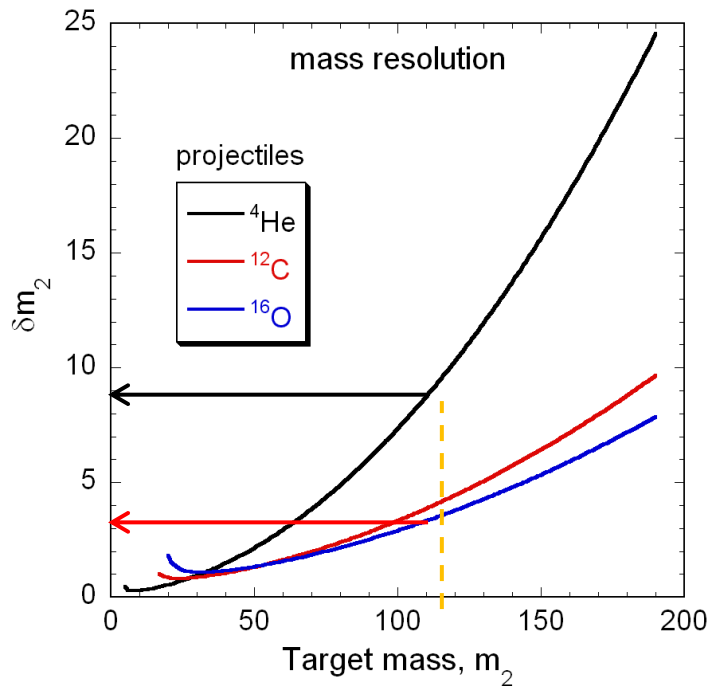
$$K(^{63}\text{Cu}) = 0.777$$



# Mass Resolution, $\delta m_2$

For 180° scattering: 
$$K_{m_2} = \frac{E_1}{E_0} = \left[ \frac{(m_2 - m_1)}{(m_2 + m_1)} \right]^2$$

$$\frac{\delta E_1}{E_0} = \delta \frac{(m_2 - m_1)^2}{(m_1 + m_2)^2}$$

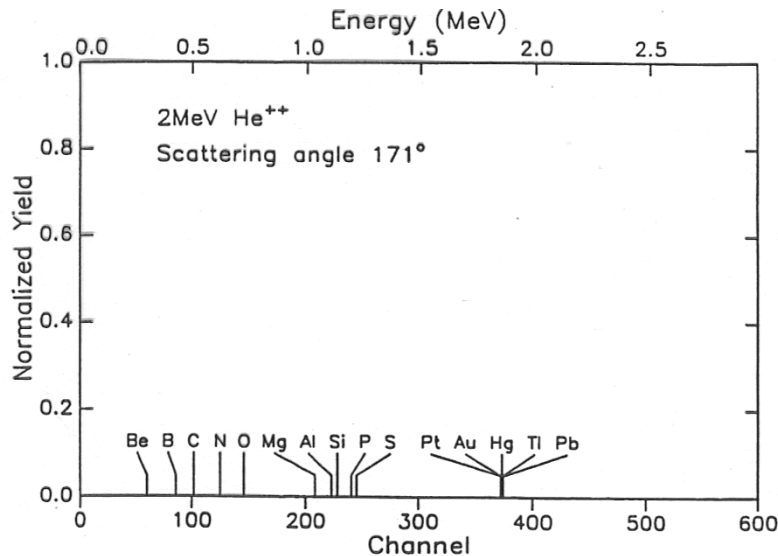


For a fixed  $\delta E_1/E_0$  ( $\sim 0.01$ ), heavier projectiles result in better mass resolution

However,  $\delta E_1$  for heavier projectiles is higher

# Mass Resolution: examples

With system energy resolution  $\delta E = 20\text{keV}$  and  $E_0 = 2\text{MeV}$



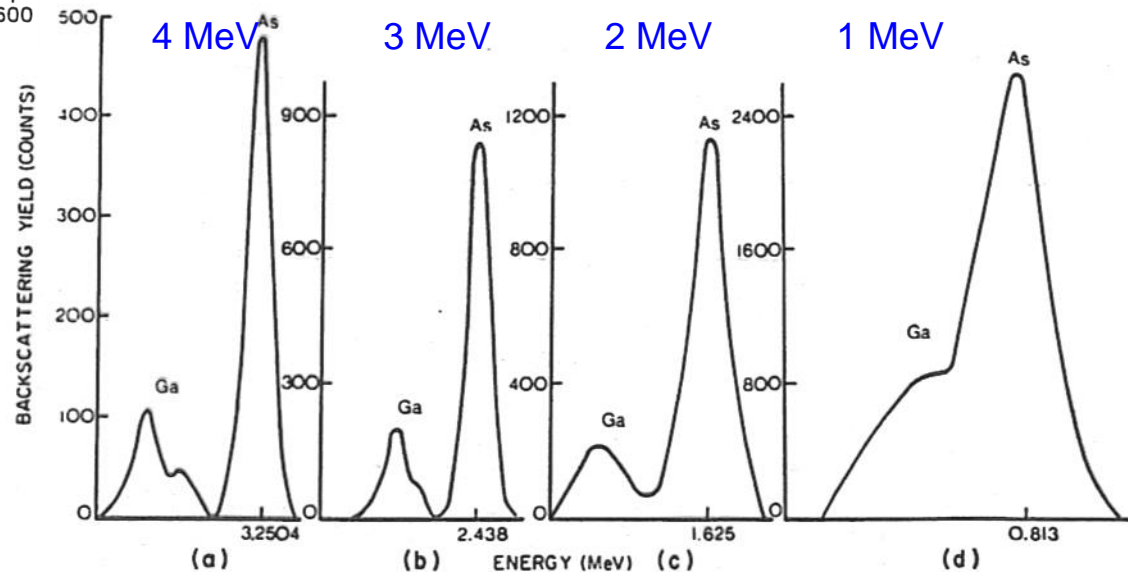
$$\text{For } m_2 = 40 \quad \delta m_2 = \frac{(40 + 4)^3}{4 \times 4(40 - 4)} \bullet \frac{20}{2000} = 1.48 a.m.u.$$

$$\text{For } m_2 = 70 \quad \delta m_2 = \frac{(70 + 4)^3}{4 \times 4(70 - 4)} \bullet \frac{20}{2000} = 3.84 a.m.u.$$

Isotopes of Ga (68.9 and 70.9 a.m.u.)  
cannot be resolved

We can also improve mass resolution by increasing  $E_0$

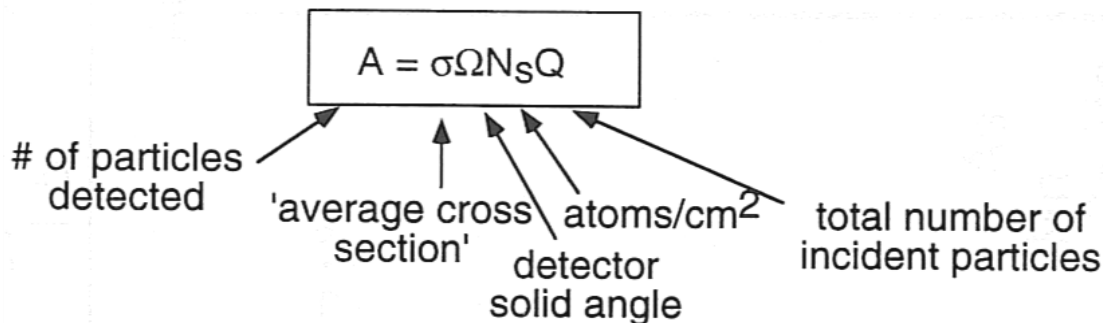
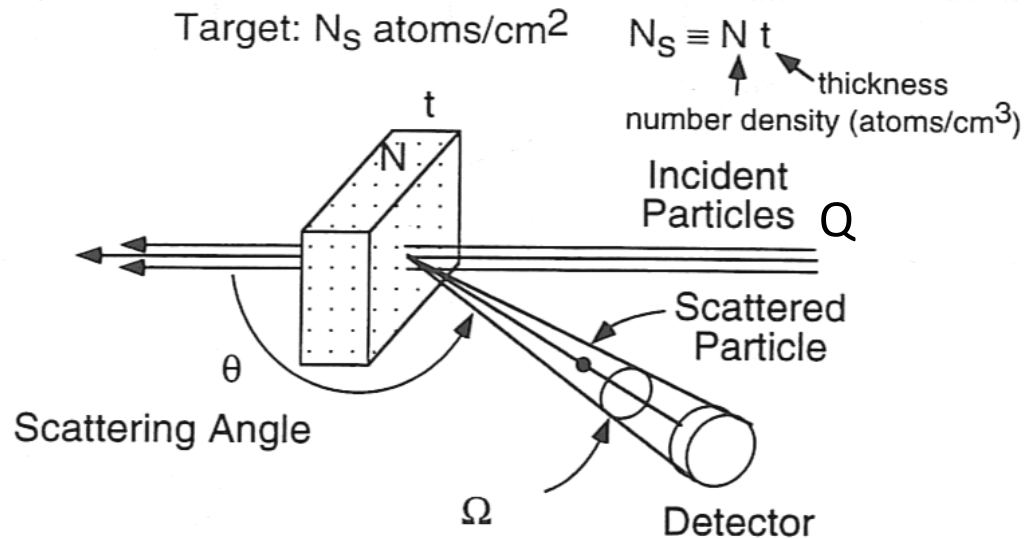
$$\therefore \delta m_2 = \frac{(m_2 + m_1)^3}{4m_1(m_2 - m_1)} \frac{\delta E_1}{E_0}$$





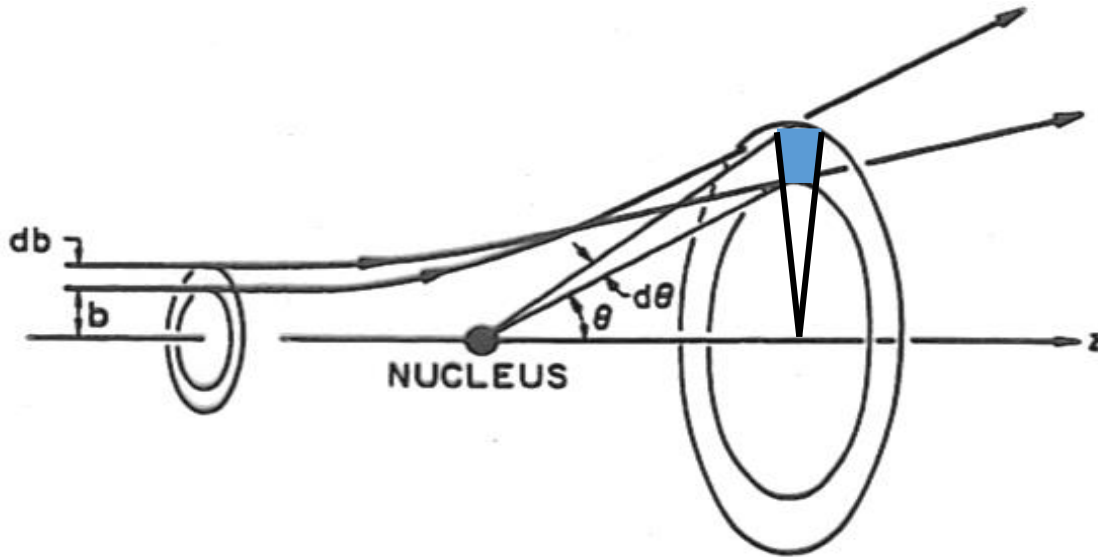
# RBS Quantification

## Backscattering Yield



- For a given incident number of particles  $Q$ , a greater amount of an element present ( $N_S$ ) should result in a greater number of particles scattered.
- Thus we need to know how often scattering events should be detected ( $A$ ) at a characteristic energy ( $E = KE_0$ ) and angle  $\theta$ , within our detector's window of solid angle  $\Omega$ .

# Scattering cross-section



If particles are coming in with impact parameters between  $b$  and  $b + db$ , they will be scattered through angles between  $\theta$  and  $\theta + d\theta$ . For central forces, we have circular symmetry.

$$2\pi b db = -\sigma(\theta) \cdot 2\pi \sin \theta d\theta$$

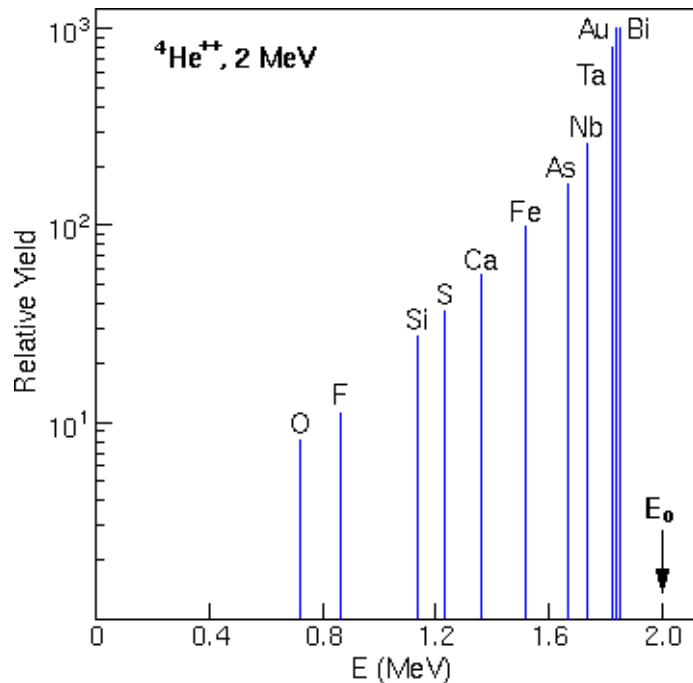
Rutherford cross-section:

$$\frac{d\sigma}{d\Omega} = \left( \frac{Z_1 Z_2 e^2}{2E_o} \right)^2 \frac{[\cos \theta + (1 - A^2 \sin^2 \theta)^{1/2}]^2}{\sin^4 \left( \frac{\theta}{2} \right) (1 - A^2 \sin^2 \theta)^{1/2}} \sim \left( \frac{Z_1 Z_2}{E_o} \right)^2 \quad A = \frac{m_1}{m_2}$$

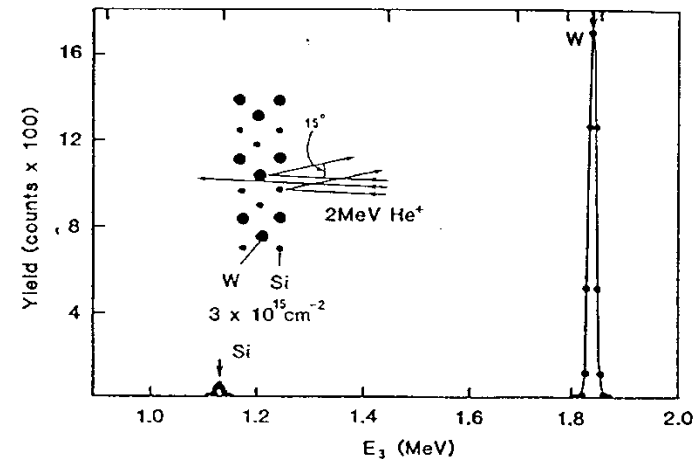
# Scattering Yield

$$\text{Yield, } Y \propto \sigma(\theta) = \left( \frac{Z_1 Z_2 e^2}{2E_0} \right)^2 \frac{[\cos \theta + (1 - A^2 \sin^2 \theta)^{1/2}]^2}{\sin^4 \theta (1 - A^2 \sin^2 \theta)^{1/2}}$$

$$\propto \left( \frac{Z_1 Z_2}{E_0} \right)^2 \sim 10^{-24} \text{ cm}^2 [\text{barn}]$$



## Example:



Mixed Si and W target analyzed by a 2 MeV He ion beam at  $165^\circ$  scattering angle.

$$\sigma(\text{Si}) = 2.5 \times 10^{-25} \text{ cm}^2/\text{str}$$

$$\sigma(\text{W}) = 7.4 \times 10^{-24} \text{ cm}^2/\text{str}$$

$$\text{Total incident ions } Q = 1.5 \times 10^{14} \text{ ions}$$

$$\Omega = 1.8 \text{ mstr}$$

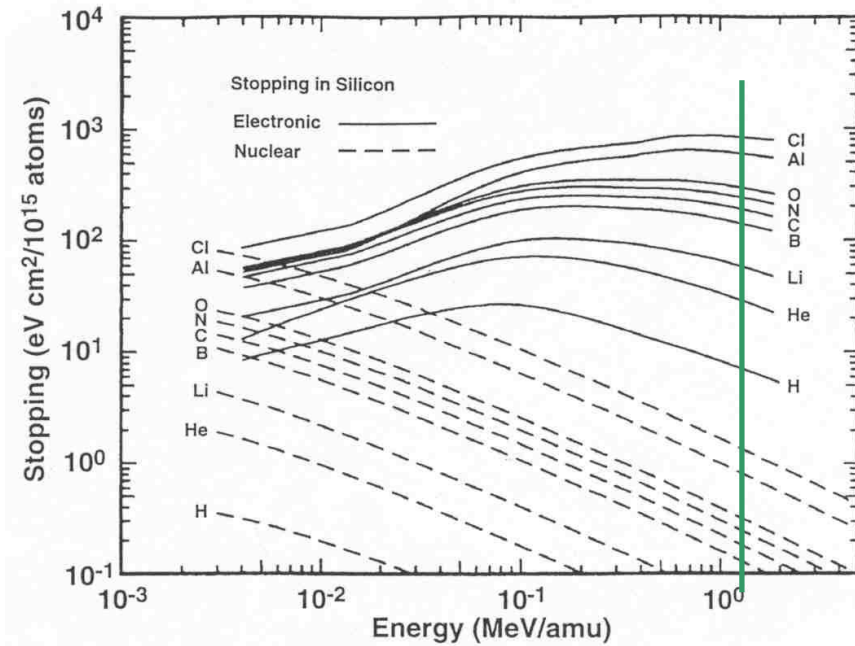
$$\text{Area under Si, } A(\text{Si}) = 200 \text{ counts}$$

$$\text{Area under W, } A(\text{W}) = 6000 \text{ counts}$$

$$(Nt)_{\text{Si}} = 3 \times 10^{15} \text{ atoms/cm}^2$$

$$(Nt)_{\text{W}} = 3 \times 10^{15} \text{ atoms/cm}^2$$

# Energy Loss



Electronic stopping  $\left. \frac{dE}{dx} \right|_{ele}$

Nuclear Stopping  $\left. \frac{dE}{dx} \right|_{nucl}$

When an He or H ion moves through matter, it loses energy through

- interactions with  $e^-$  by raising them to excited states or even ionizing them.
- Direct ion-nuclei scattering

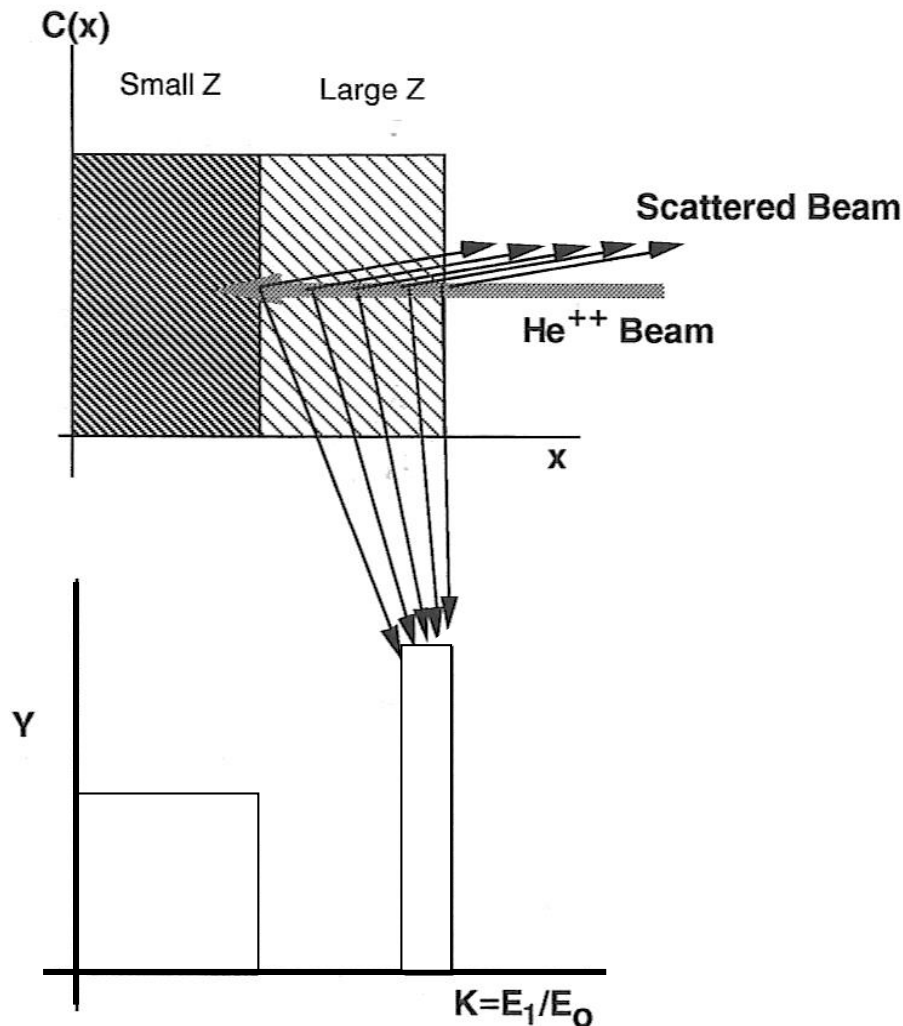
Since the radii of atomic nuclei are so small, interactions with nuclei may be neglected

$$\left. \frac{dE}{dx} \right|_{total} = \left. \frac{dE}{dx} \right|_{ele} + \left. \frac{dE}{dx} \right|_{nucl} \approx \left. \frac{dE}{dx} \right|_{ele}$$



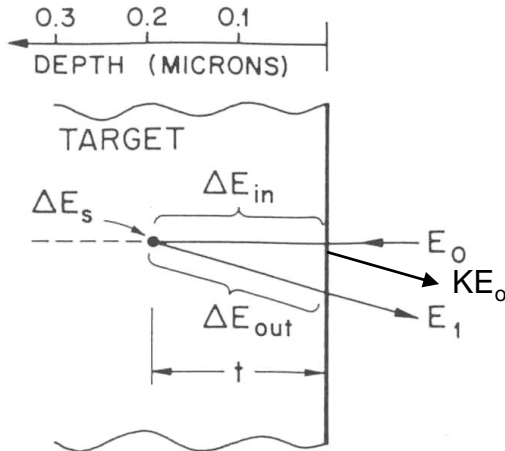
# How to read a typical RBS spectrum

A thin film on a light substrate



- Most projectile ions experience electronic stopping that results in a gradual reduction of the particle's kinetic energy ( $dE/dx$ ).
- At the same time a small fraction of projectile ions come close enough to the nucleus for large-angle scattering (KE).
- A detected backscattered particle has lost some energy during initial penetration, then lost a large fraction of its remaining energy during the large-angle scattering event, then lost more energy in leaving the solid.

# Depth Scale



ENERGY LOSS:

$$\Delta E_{in} \approx \left. \frac{dE}{dx} \right|_{E_0} \cdot t$$

$$E_t = E_0 - \Delta E_{in}$$

$$\Delta E_s = (1-K) E_t$$

$$\Delta E_{out} \approx \left. \frac{dE}{dx} \right|_{E_1} \cdot \frac{t}{\cos \theta}$$

$$E_1 = K(E_0 - \Delta E_{in}) - \Delta E_{out}$$

$$E_1 = K(E_0 - \left. \frac{dE}{dx} \right|_{E_0} \cdot t) - \left( \left. \frac{dE}{dx} \right|_{KE_0} \cdot \frac{t}{\cos \theta} \right)$$

Total energy loss  $\Delta E = KE_0 - E_1$

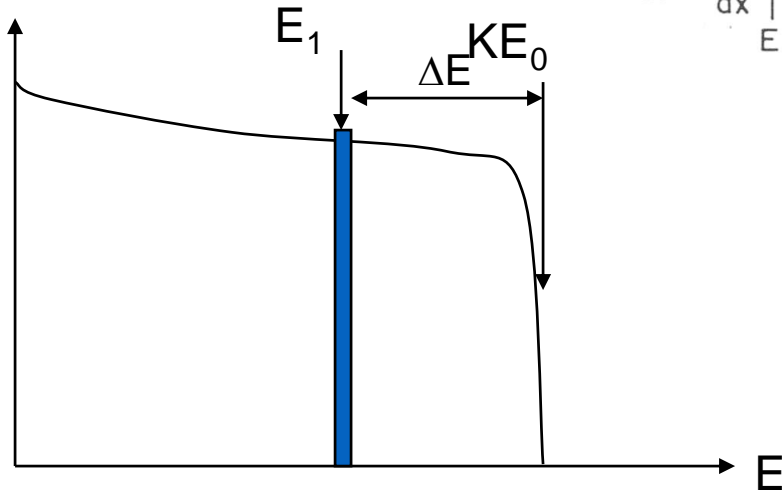
$$\Delta E = \left( \frac{K}{\cos \theta_1} \cdot \left. \frac{dE}{dx} \right|_{E_0} + \frac{1}{\cos \theta_2} \cdot \left. \frac{dE}{dx} \right|_{KE_0} \right) \cdot t = [S_o] \cdot t$$

$[S_o]$  is the effective stopping power

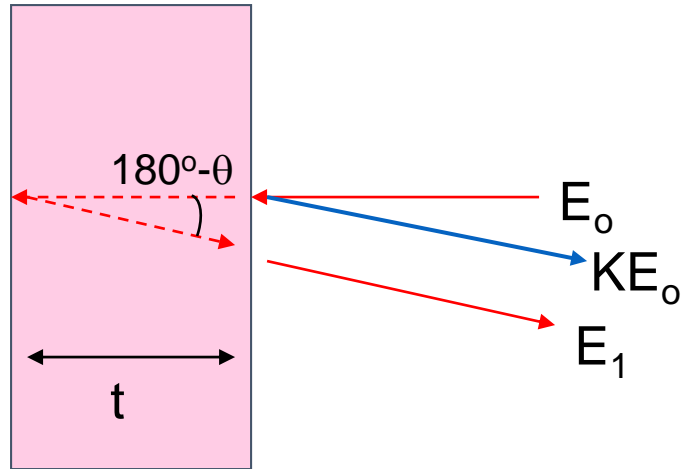
Stopping cross-section

$$\varepsilon = \frac{1}{N} \frac{dE}{dx} : \frac{\text{eV cm}^3}{\text{cm atom}} = \frac{\text{eVcm}^2}{\text{atom}}$$

$$\Delta E = \left( \frac{K}{\cos \theta_1} \cdot N \varepsilon_{in} + \frac{1}{\cos \theta_2} \cdot N \varepsilon_{out} \right) \cdot t = N[\varepsilon_o] \cdot t$$



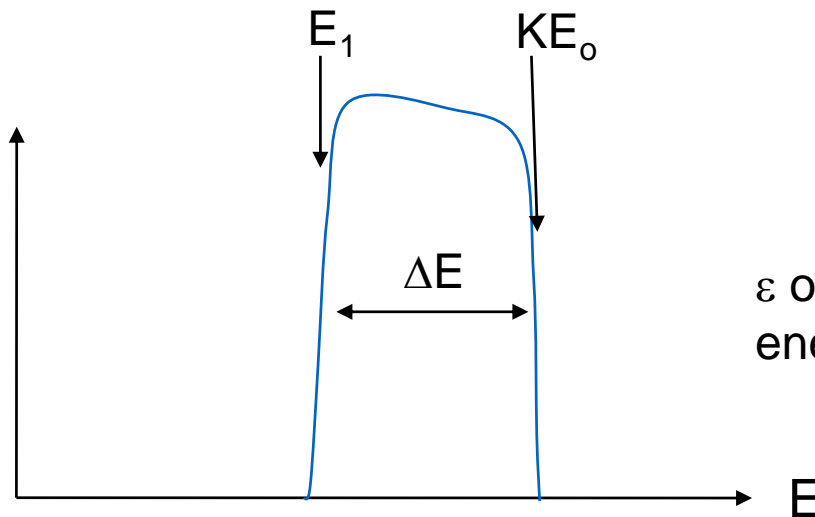
# Depth scale: thin film



Thickness of film:

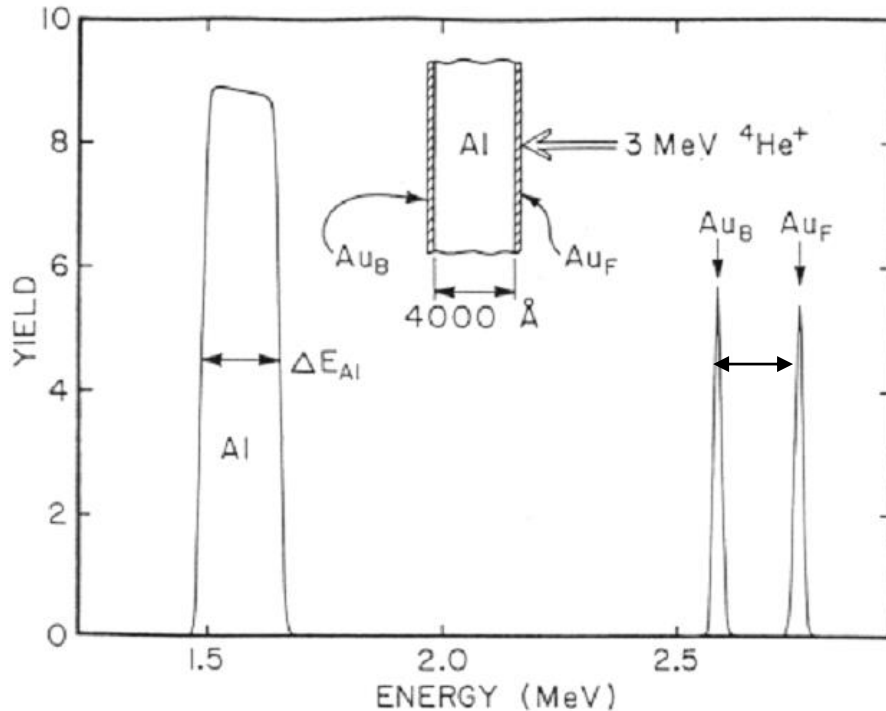
$$\Delta E = \left( K \frac{dE}{dx} \Big|_{E_0} + \frac{dE}{dx} \Big|_{KE_0} \right) \cdot t = [S_o] \cdot t$$

$$t = \frac{\Delta E}{[S_o]} = \frac{\Delta E}{N[\epsilon_o]}$$



$\epsilon$  obtained from TRIM code or empirical energy loss data fitting

# Example: layer thickness



$$\Delta E_{Al} = 165 \text{ keV}$$

$$\Delta E_{Au} = 175 \text{ keV}$$

$$K_{Au} = 0.9225$$

$$K_{Al} = 0.5525$$

consider the Au markers

$$\begin{aligned} \Delta E_{Au} &= E_{AuF} - E_{AuB} \\ &= [K_{Au} dE/dx |_{E_0 + 1 / (\cos 10^\circ)} \cdot dE/dx |_{EAuB}] \cdot t \end{aligned}$$

$$\begin{aligned} dE/dx |_{3\text{MeV}} &= N_{Al} \epsilon_{Al} |_{3\text{MeV}} \\ &= 6.02 \times 10^{22} \cdot 36.56 \times 10^{-15} \\ &= 2.2 \times 10^9 \text{ eVcm}^{-1} \end{aligned}$$

$$\begin{aligned} dE/dx |_{EAuB} &= N_{Al} \epsilon_{Al} |_{2.57\text{MeV}} \\ &= 6.02 \times 10^{22} \times 39.34 \times 10^{-15} \\ &= 2.37 \times 10^9 \text{ eVcm}^{-1} \end{aligned}$$

$$t = 3945 \text{ \AA}$$

consider the Al signals

$$\Delta E_{Al} = [K_{Al} dE/dx |_{E_0 + 1 / (\cos 10^\circ)} \cdot dE/dx |_{KE_0}] \cdot t$$

$$t = 3937 \text{ \AA}$$

# Energy Loss: Bragg's rule

For a target  $A_m B_n$ , the stopping cross-section is the sum of those of the constituent elements weighted by the abundance of the elements.

$$\epsilon^{AmBn} = m \epsilon^A + n \epsilon^B$$

Example:

the stopping cross-section  $\epsilon^{Al_2O_3}$  of  $Al_2O_3$ .

Given:  $\epsilon^{Al} = 44 \times 10^{-15} \text{eVcm}^2$

$\epsilon^O = 35 \times 10^{-15} \text{eVcm}^2$

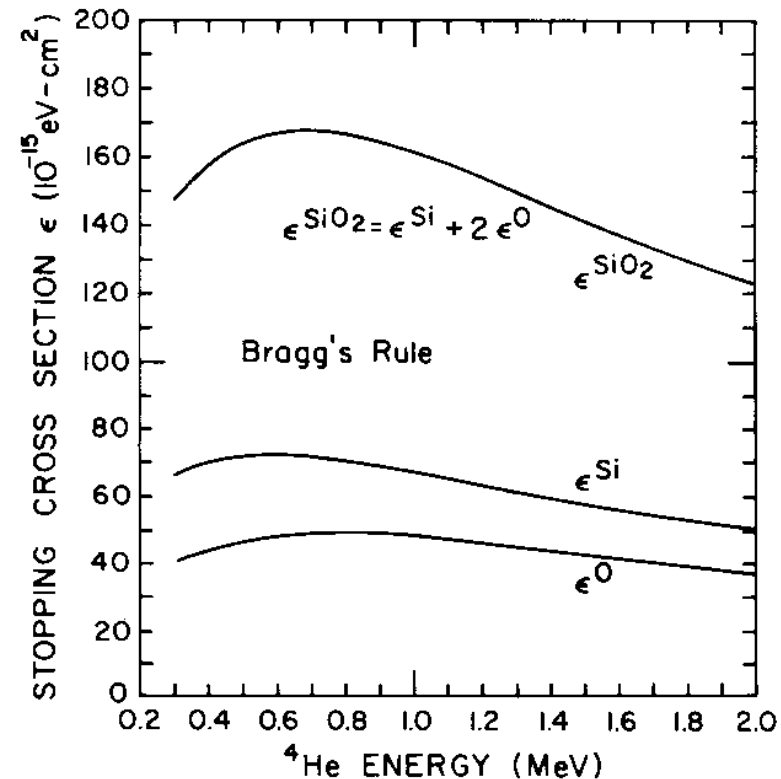
$$\epsilon^{Al_2O_3} = 2/5 \times \epsilon^{Al} + 3/5 \times \epsilon^O$$

$$= (2/5 \times 44 + 3/5 \times 35) \times 10^{-15}$$

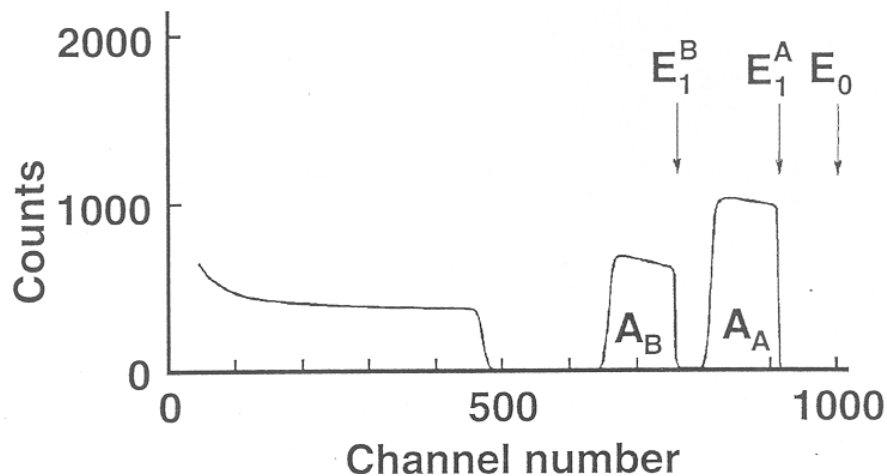
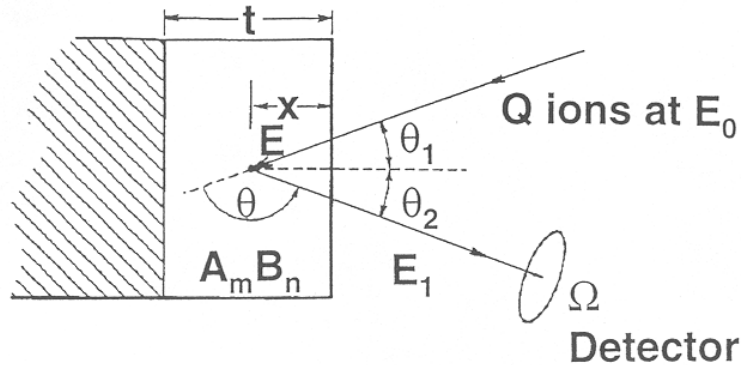
$$= 38.6 \times 10^{-15} \text{eV-cm}^2/\text{atom}$$

$$dE/dx(Al_2O_3) = N \epsilon^{Al_2O_3} = (1.15 \times 10^{22})(38.6 \times 10^{-15}) \text{eV/cm}$$

$$= 44.4 \text{ eV/\AA}$$



# Quantitative analysis: composition and thickness



$$A_A = \sigma_A \cdot \Omega \cdot Q \cdot (Nt)_A$$

$$A_B = \sigma_B \cdot \Omega \cdot Q \cdot (Nt)_B$$

$$\frac{A_A}{A_B} = \left( \frac{\sigma_A}{\sigma_B} \right) \cdot \left( \frac{(Nt)_A}{(Nt)_B} \right) = \left( \frac{Z_A}{Z_B} \right)^2 \cdot \frac{m}{n}$$

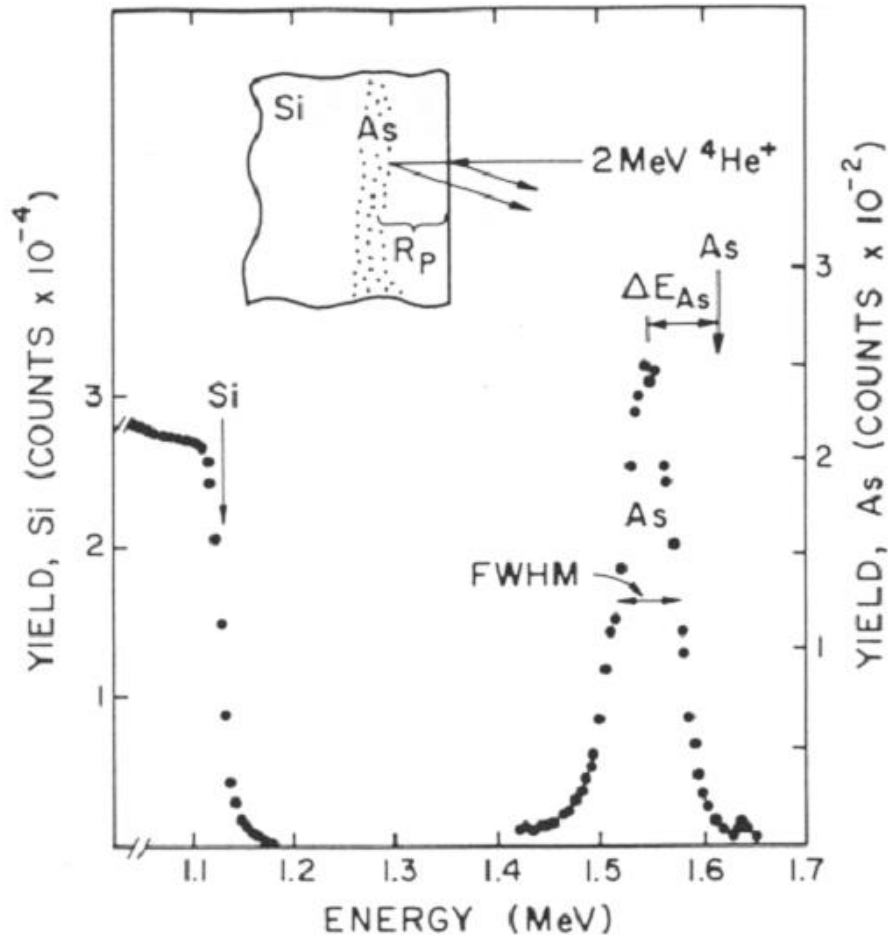
$$\frac{m}{n} = \left( \frac{A_A}{A_B} \right) \cdot \left( \frac{Z_B}{Z_A} \right)^2$$

$$t = \frac{(\Delta E)_A}{[S_o]_A^{A_m B_n}} = \frac{(\Delta E)_B}{[S_o]_B^{A_m B_n}}$$

$$t = \frac{(\Delta E)_A}{N[\epsilon_o]_A^{A_m B_n}} = \frac{(\Delta E)_B}{N[\epsilon_o]_B^{A_m B_n}}$$



# Example: As implanted Si



$$K_{As} = 0.809; K_{Si} = 0.566$$

$$[\varepsilon_o]_{Si}^{Si} = 92.6 \times 10^{-15} \text{ eV} - \text{cm}^2 / \text{atom}$$

$$[\varepsilon_o]_{As}^{Si} = 95.3 \times 10^{-15} \text{ eV} - \text{cm}^2 / \text{atom}$$

$$\Delta E_{As}^{Si} = 68 \text{ keV}$$

$$(FWHM)_{As} = 60 \text{ keV}$$

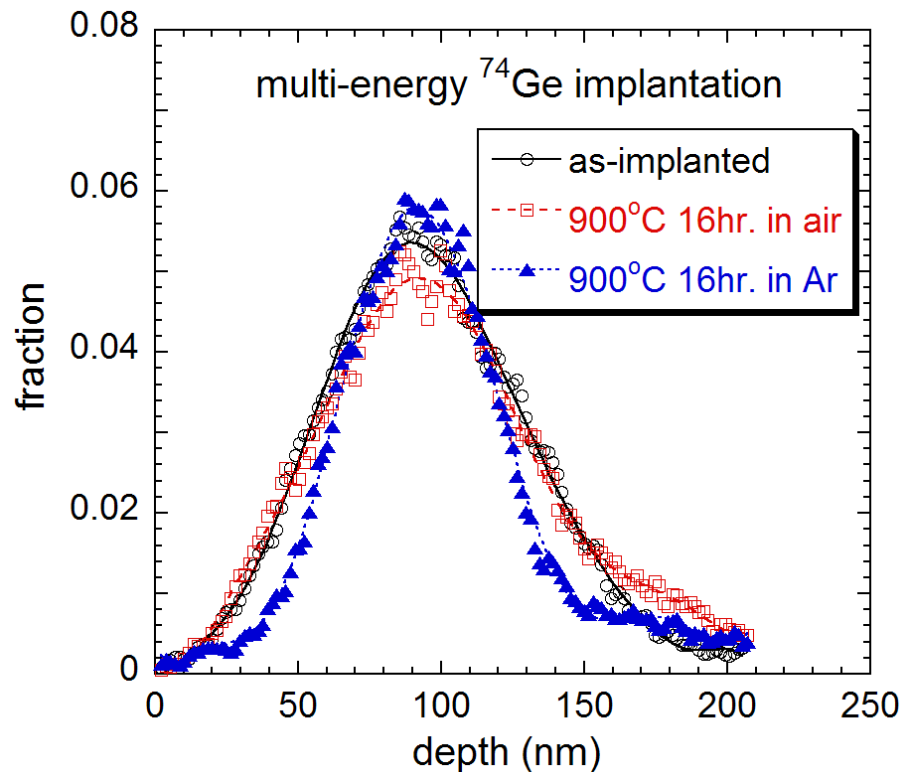
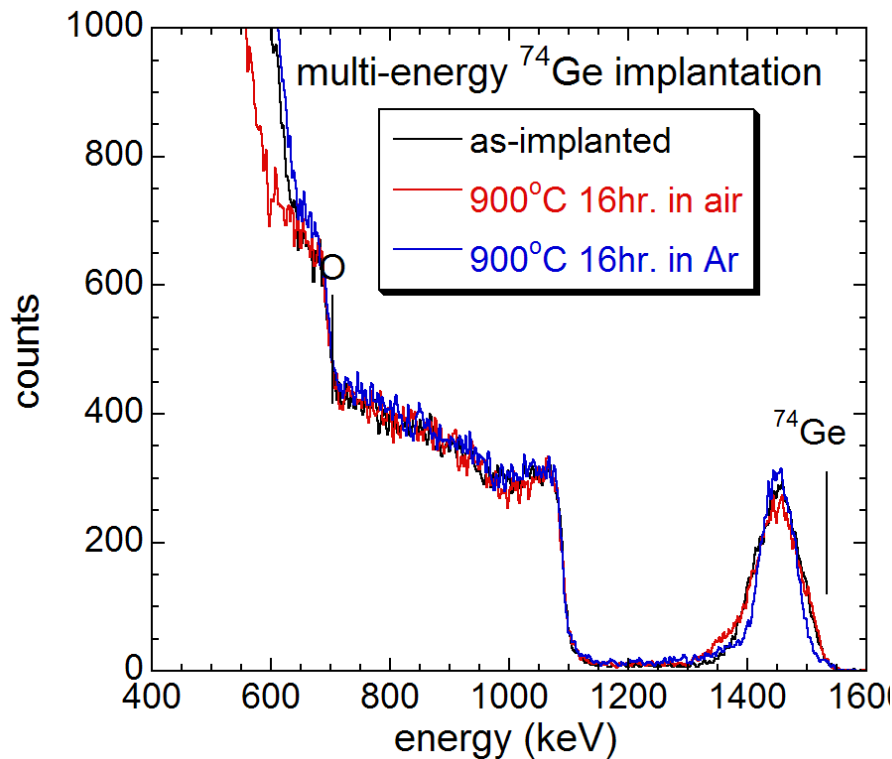
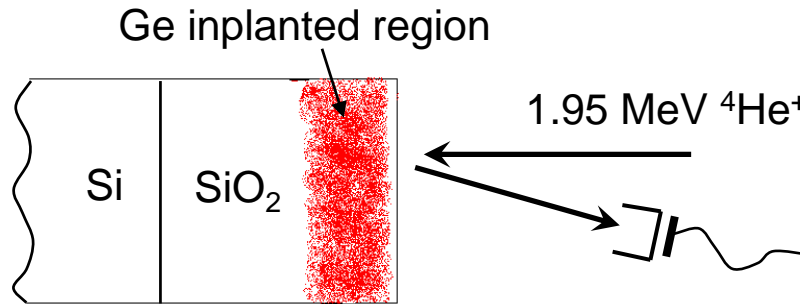
$$R_p = \frac{\Delta E_{As}^{Si}}{N[\varepsilon_o]_{As}^{Si}} = 1420 \text{ \AA}$$

$$\Delta R_p = \frac{(FWHM)_{As}}{2.355 \cdot N[\varepsilon_o]_{As}^{Si}} = 540 \text{ \AA}$$

Total As dose:

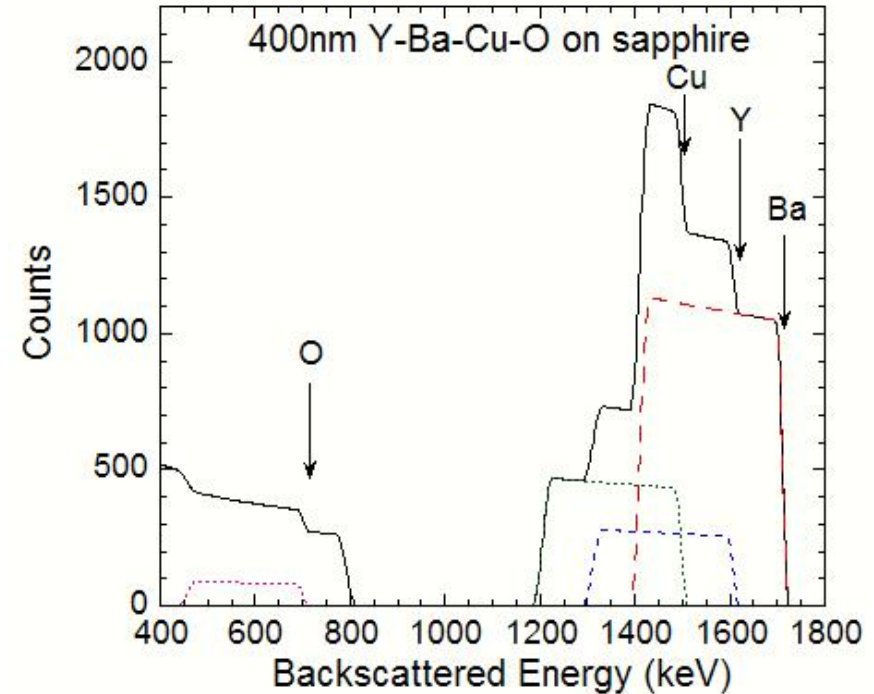
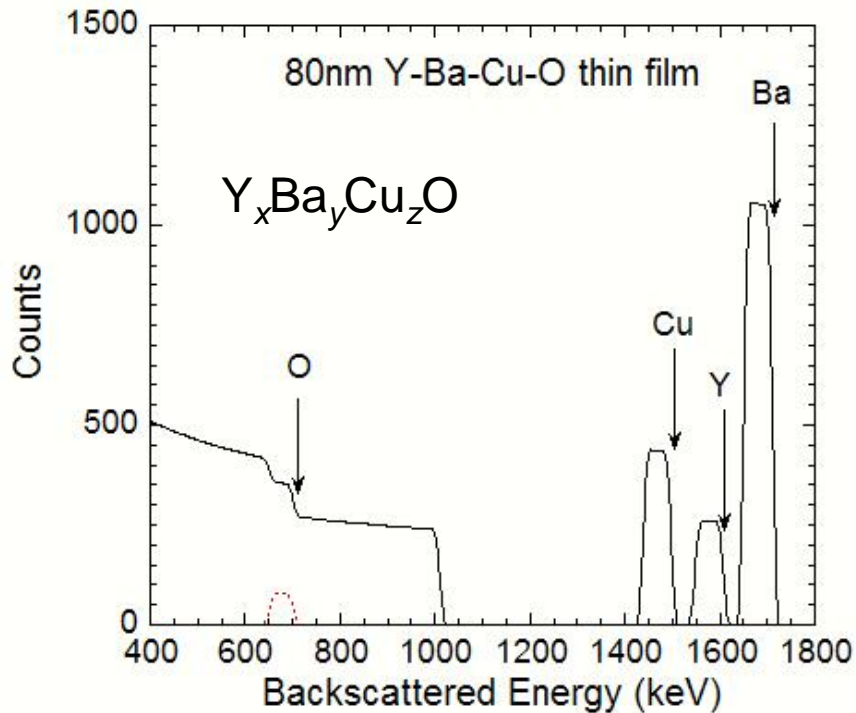
$$(Nt)_{As} = \frac{A_{As}}{(\sigma_{As} \cdot \Omega \cdot Q)}$$

# RBS Application: impurity profile



*I. Sharp et al., LBNL (2004)*

# Thin film analysis

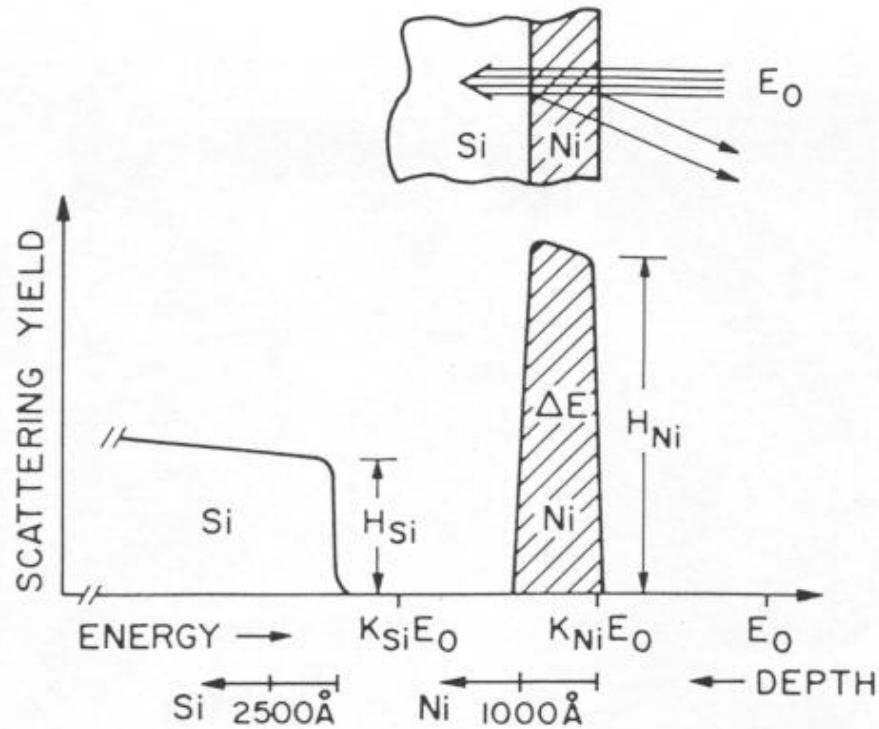


$$\frac{y}{x} = \frac{A_Y}{A_{Ba}} \cdot \left( \frac{Z_{Ba}}{Z_Y} \right)^2$$

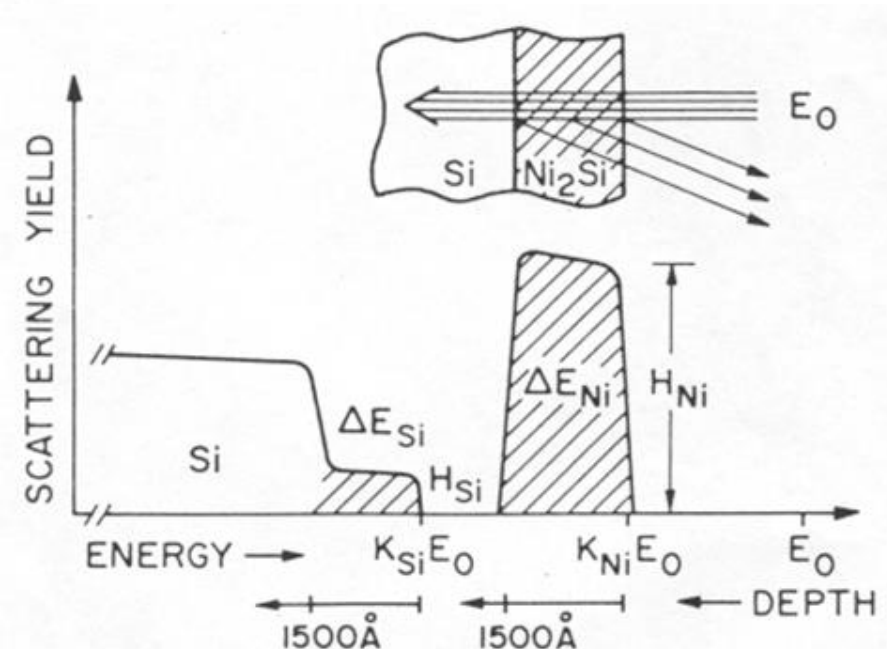
$$\frac{y}{x} \approx \frac{H_Y}{H_{Ba}} \cdot \left( \frac{Z_{Ba}}{Z_Y} \right)^2$$

# Example: silicide formation (1970-80s)

Before reaction

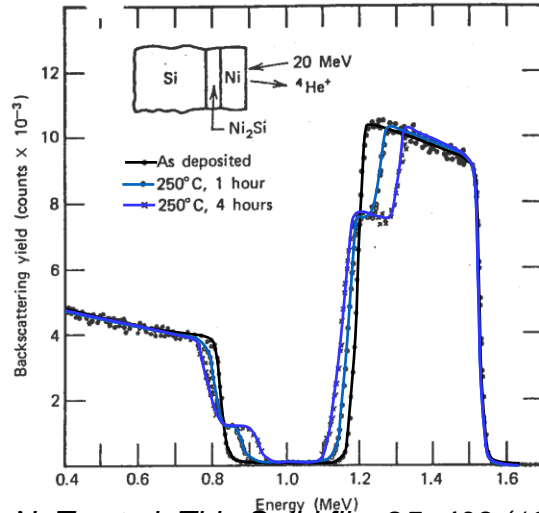


After reaction

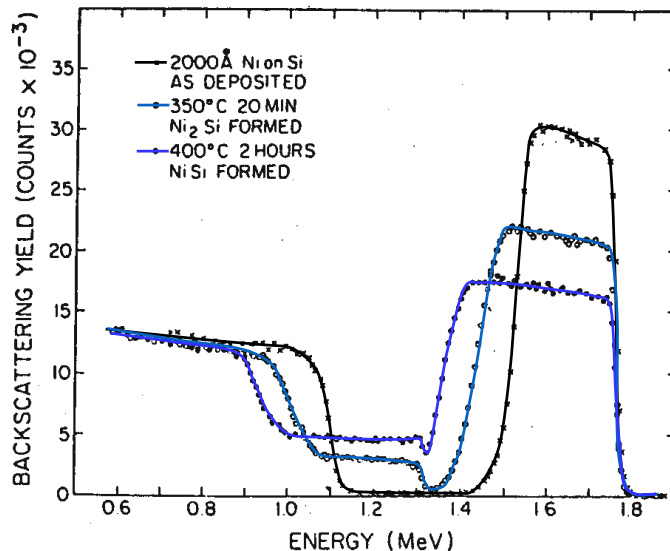


Wei-Kan Chu, James W. Mayer and Marc-A. Nicolet, *Backscattering Spectrometry*, (Academic Press, New York 1978).

# RBS application: silicide formation

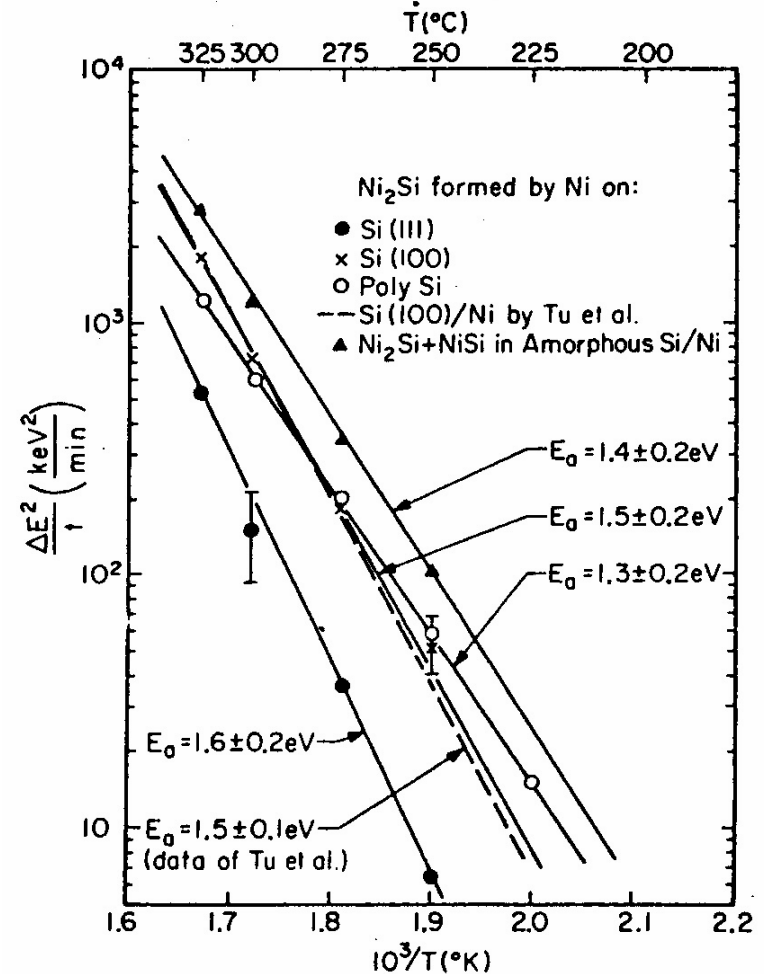


K. N. Tu et al. *Thin Solid film* 25, 403 (1975).



K. N. Tu et al. *Japn, J. Appl. Phys. Suppl.* 2 Pt 1 669 (1974).

## Reaction kinetics:



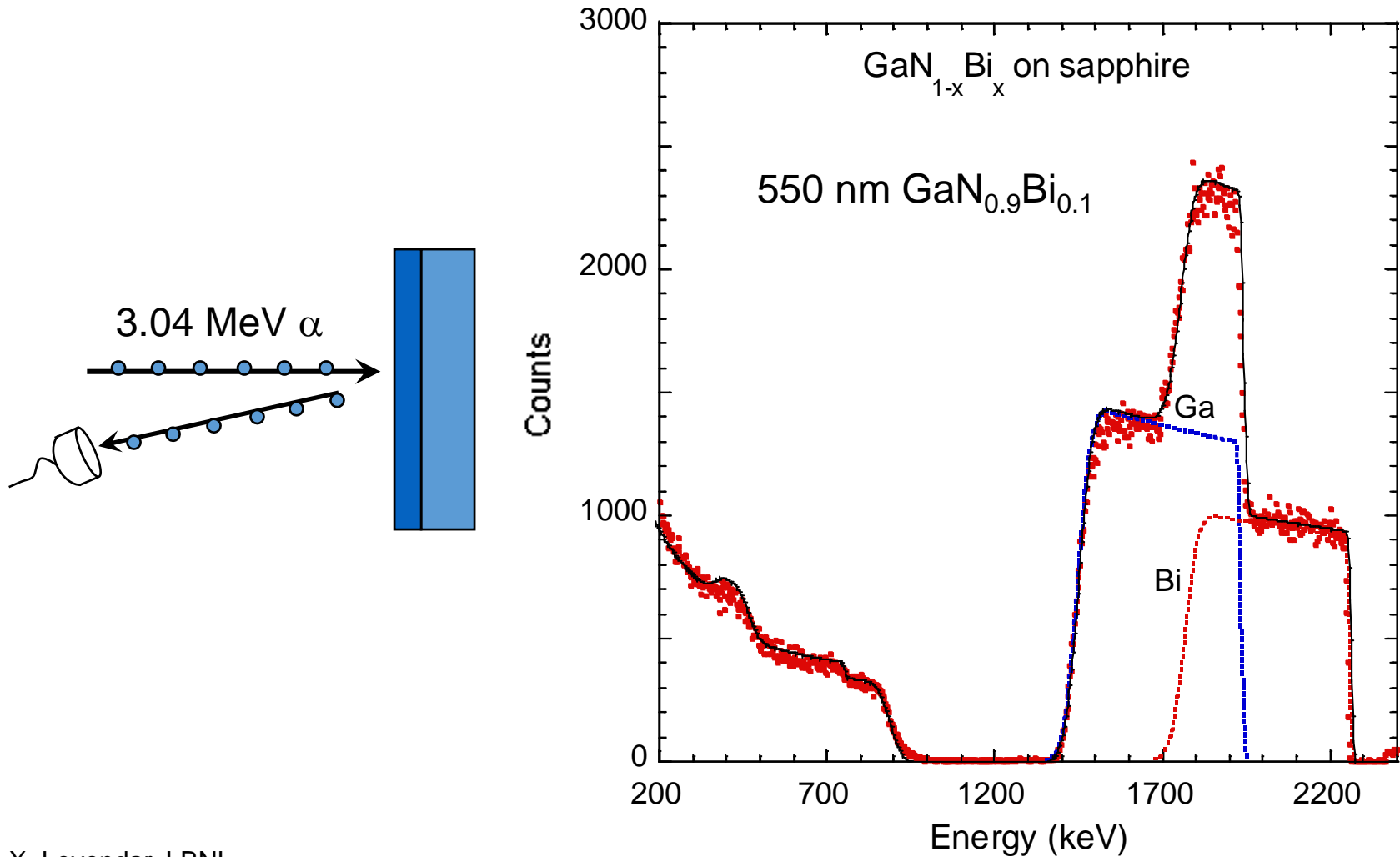
J. O. Olowolafe et al. *Thin Solid film* 38, 143 (1976).

# IBA Data Analysis

- Starts with a simple guess sample structure (film thickness and composition)
- Simulates spectrum and directly compare to experimental data
- Iterates simulated structure to fit experimental data (either automatically or manually)
- An ideal software:
  - able to handle different data files
  - have large data base for various ion-solid interaction: resonant scattering, nuclear reaction, etc.
  - User friendly interface
  - Fast simulation
  - Can simulate sample non-uniformity (roughness, compositional gradient, etc.)
  - Able to correct for electronic errors (pile up, dead time, charge up, etc)

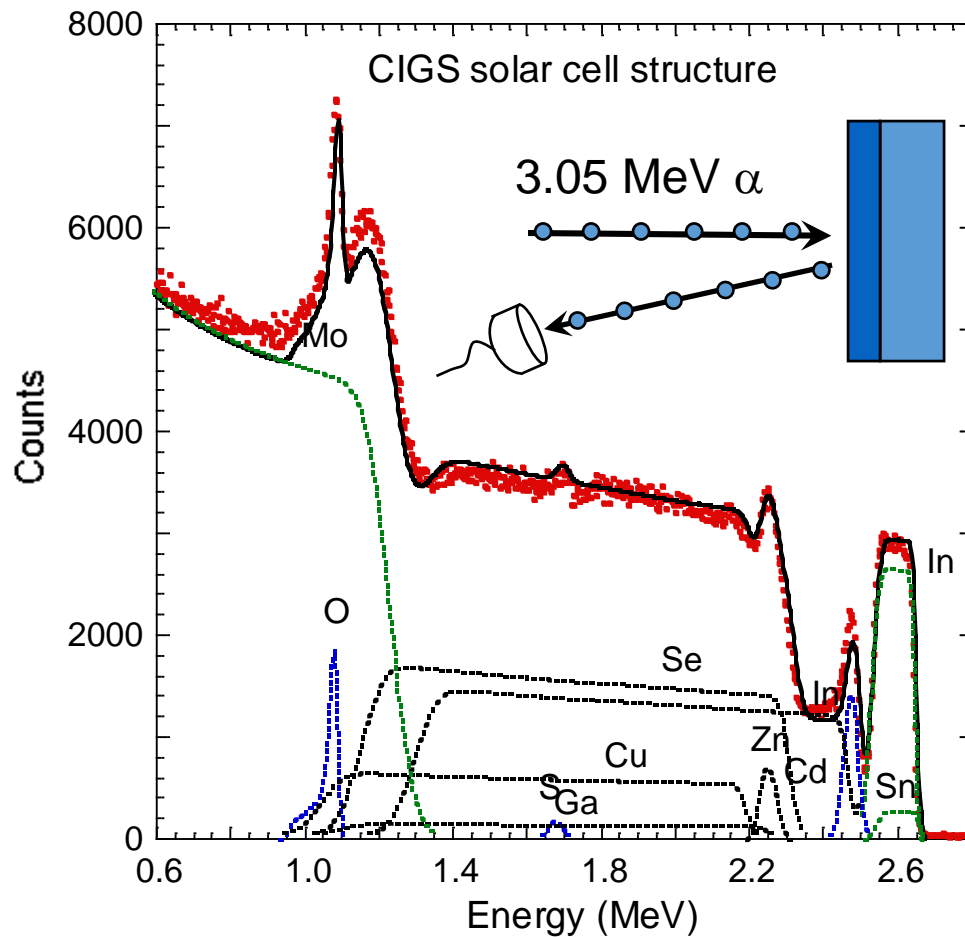


# Thin Film Analysis: single layer

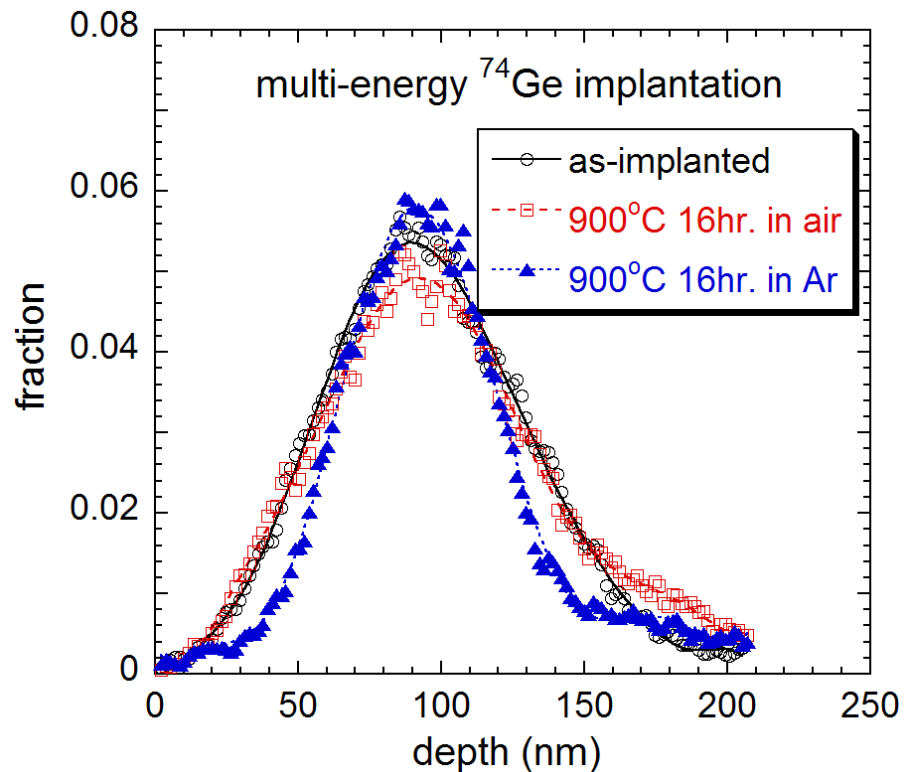
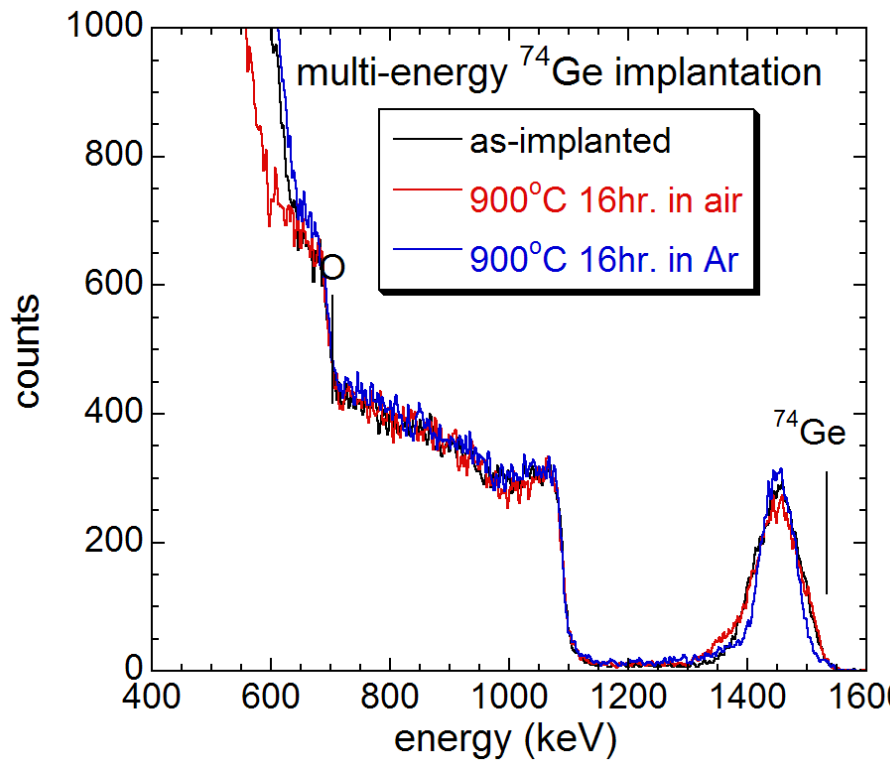
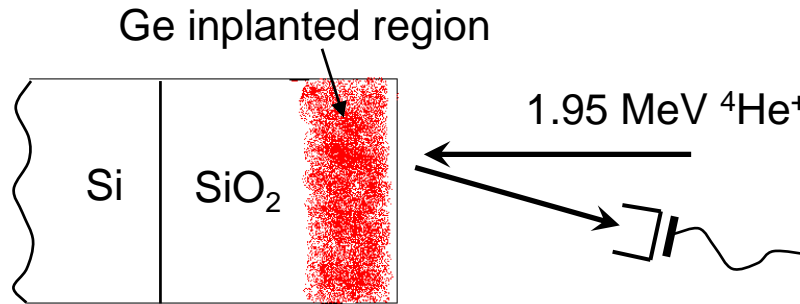


A.X. Levendar, LBNL

# Thin film analysis: multilayers



# Impurity profile



*I. Sharp et al., LBNL (2004)*

# Strengths of RBS

- Simple in principle
- Fast and direct
- Quantitative without standard
- Depth profiling without chemical or physical sectioning
- Non-destructive
- Wide range of elemental coverage
- No special specimen preparation required
- Can be applied to crystalline or amorphous materials
- Simultaneous analysis with various ion beam techniques (PIXE, PIGE, channeling, etc.)

# Weaknesses of RBS

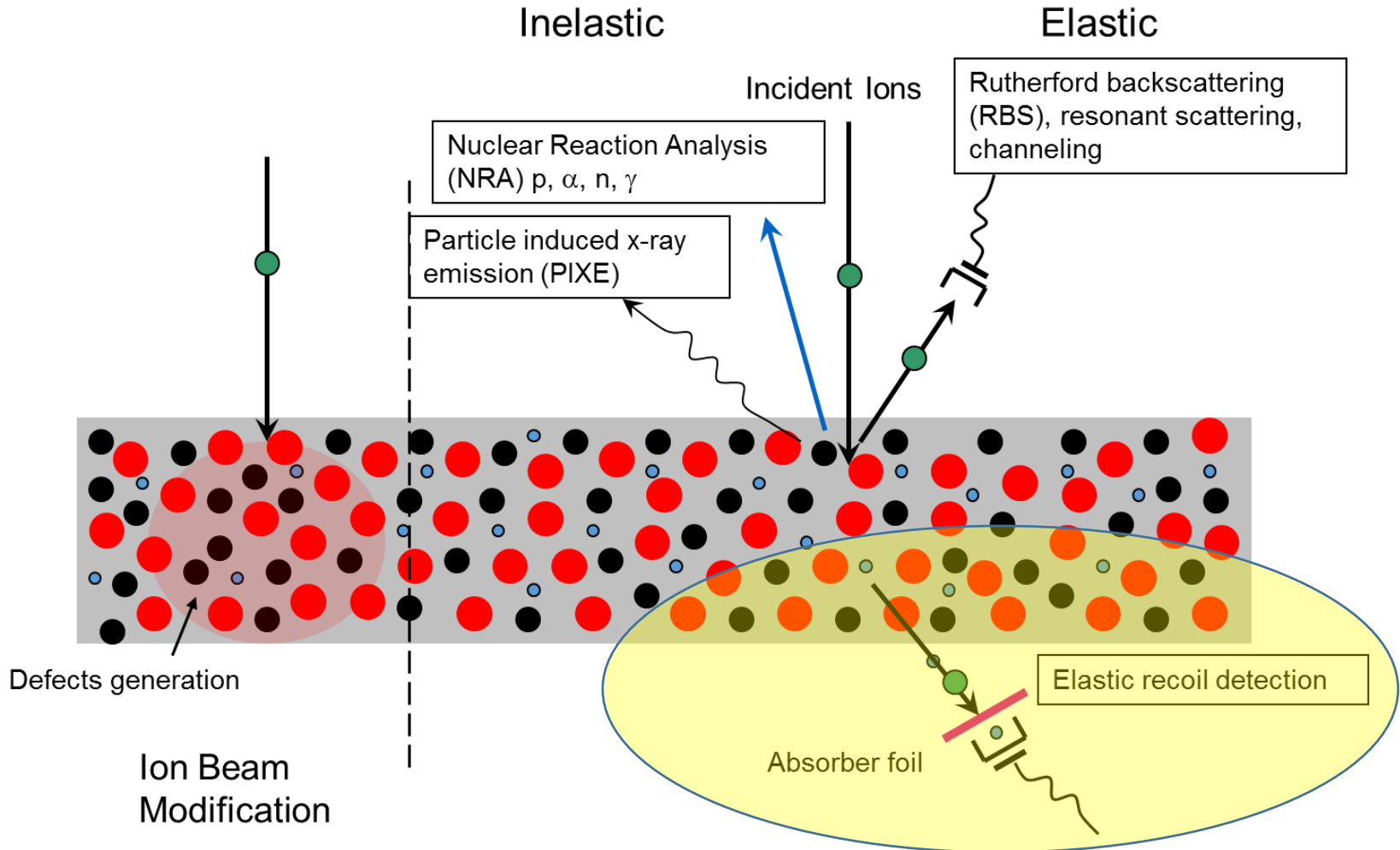
- Poor lateral resolution ( $\sim 0.5\text{-}1\text{mm}$ )
- Moderate depth resolution ( $>50\text{\AA}$ )
- No microstructural information
- No phase identification
- Poor mass resolution for target mass heavier than  $70\text{amu}$  (PIXE)
- Detection of light impurities more difficult (e.g. Li, B, C, O, etc) (non-Rutherford scattering, Nuclear Reaction Analysis)
- Data may not be obvious: require knowledge of the technique (simulation software)

# Hydrogen Forward Scattering (HFS) (Elastic Recoil Detection Analysis ERDA)



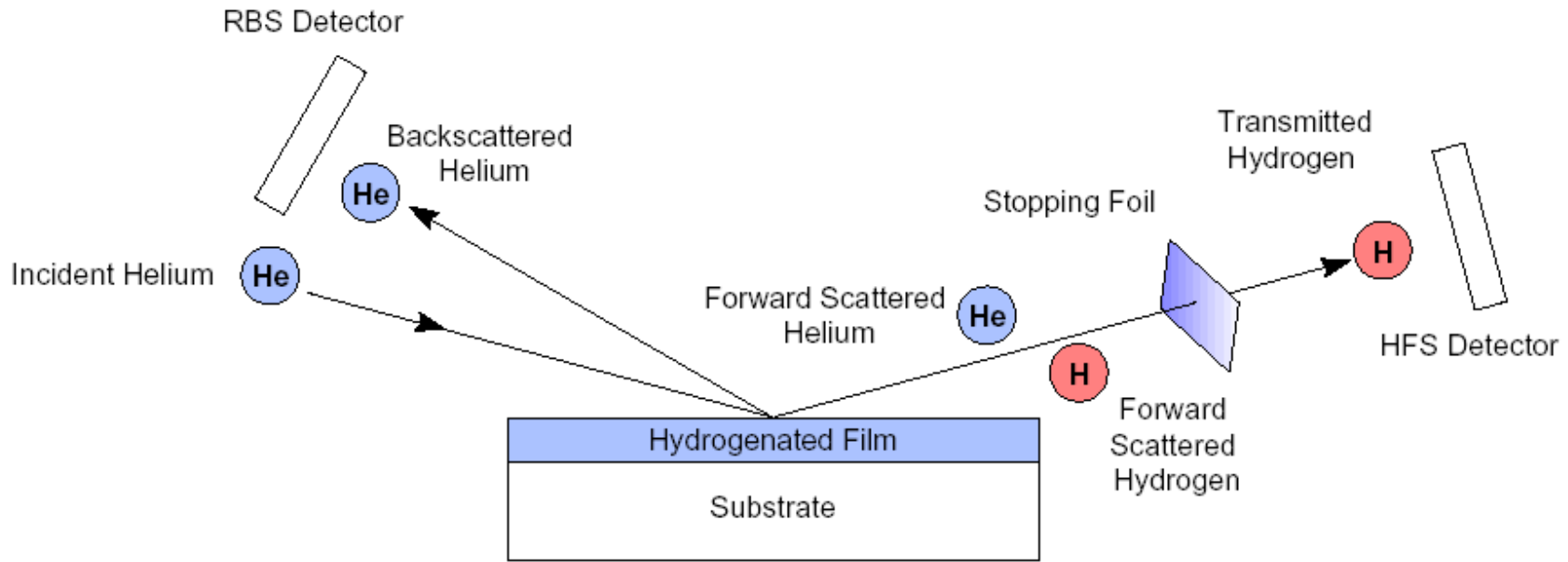
# Hydrogen Forward Scattering (HFS)

Generally known as elastic recoil detection analysis (ERDA)



# Hydrogen Forward Scattering (HFS)

Generally known as Elastic Recoil Detection (ERD)

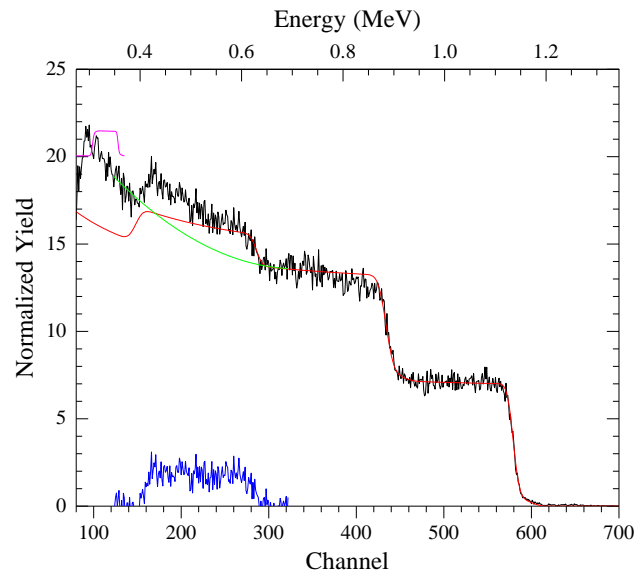


*Charles Evans and Assoc., RBS APPLICATION SERIES NO. 3*

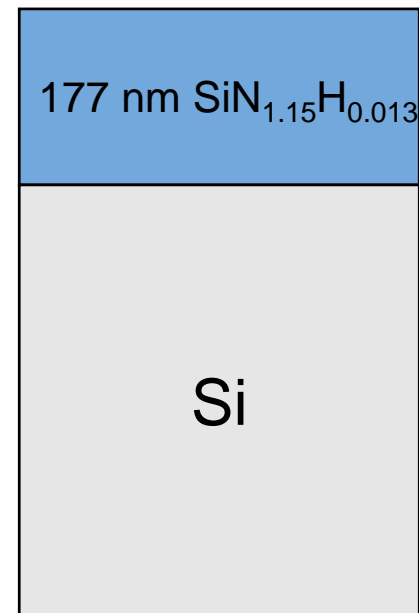
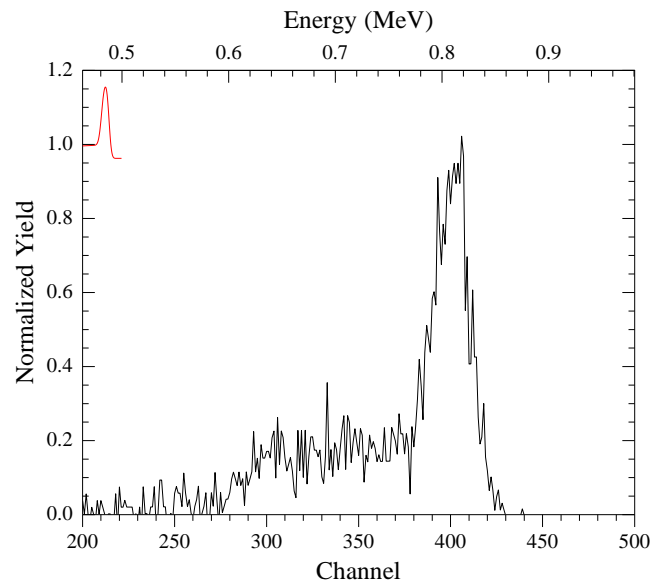
- Quantitative hydrogen and deuterium profiling
- Good sensitivity ( $\sim 0.01\text{at\%}$  of H)
- Can be performed simultaneously with RBS and PIXE
- Profiling with any light element in solid (using heavy ion beam, ERD)

# HFS: a-SiN:H film

RBS



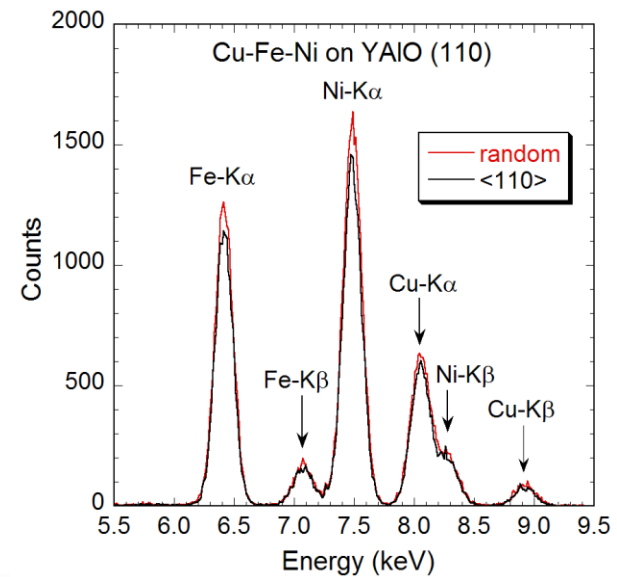
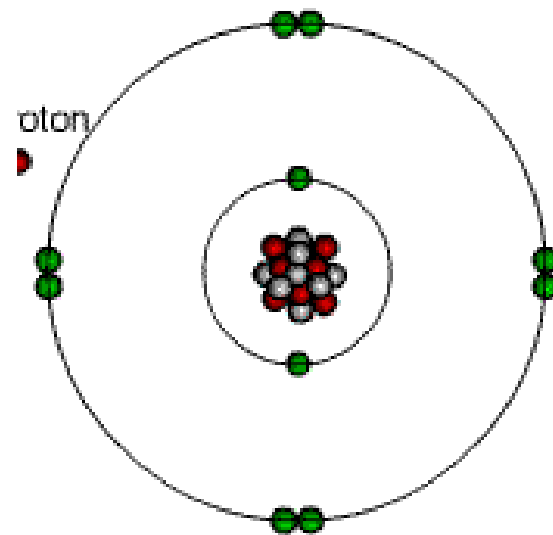
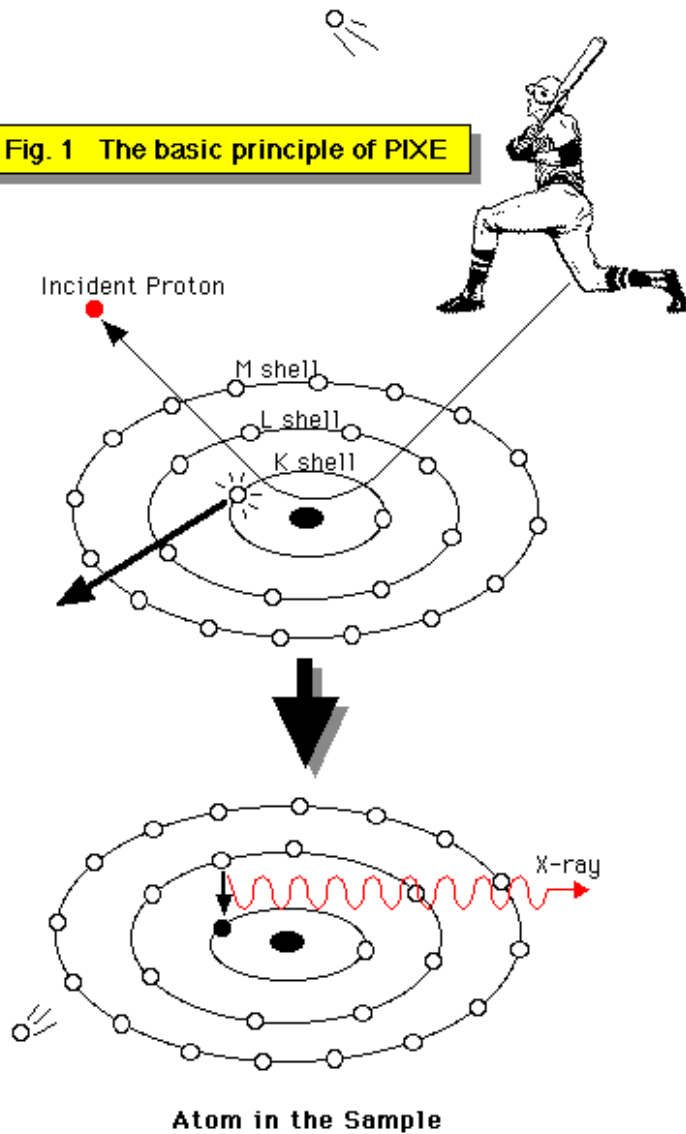
HFS



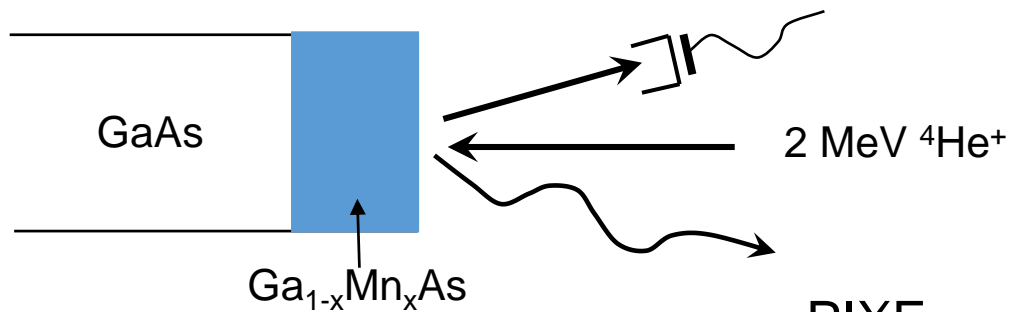
Courtesy: F. Hellman group, 2008

# Particle Induced X-ray Emission (PIXE)

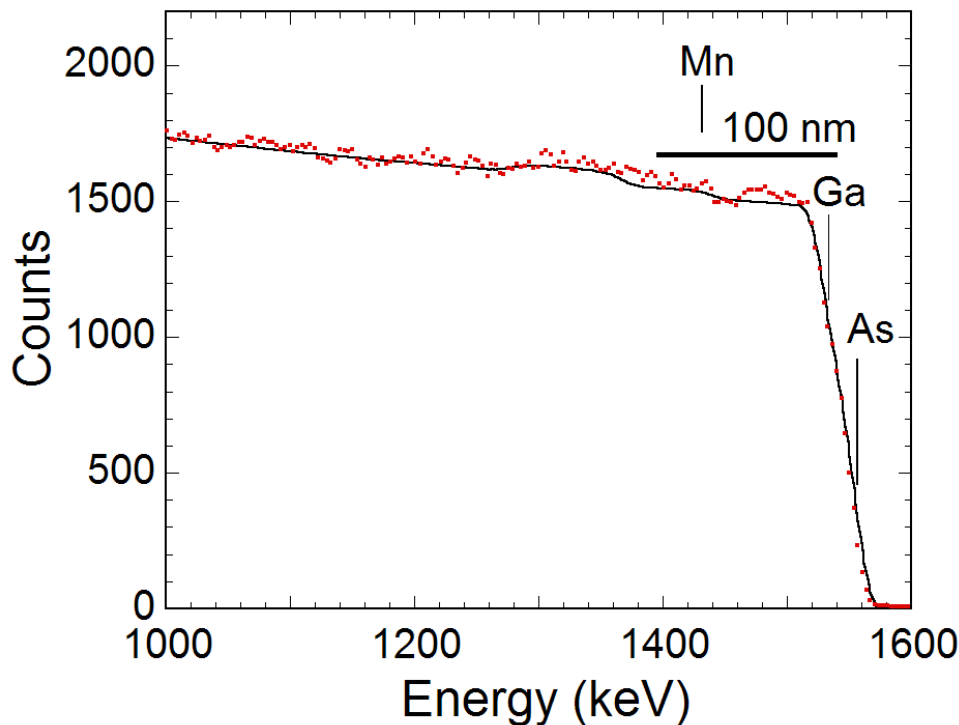
Fig. 1 The basic principle of PIXE



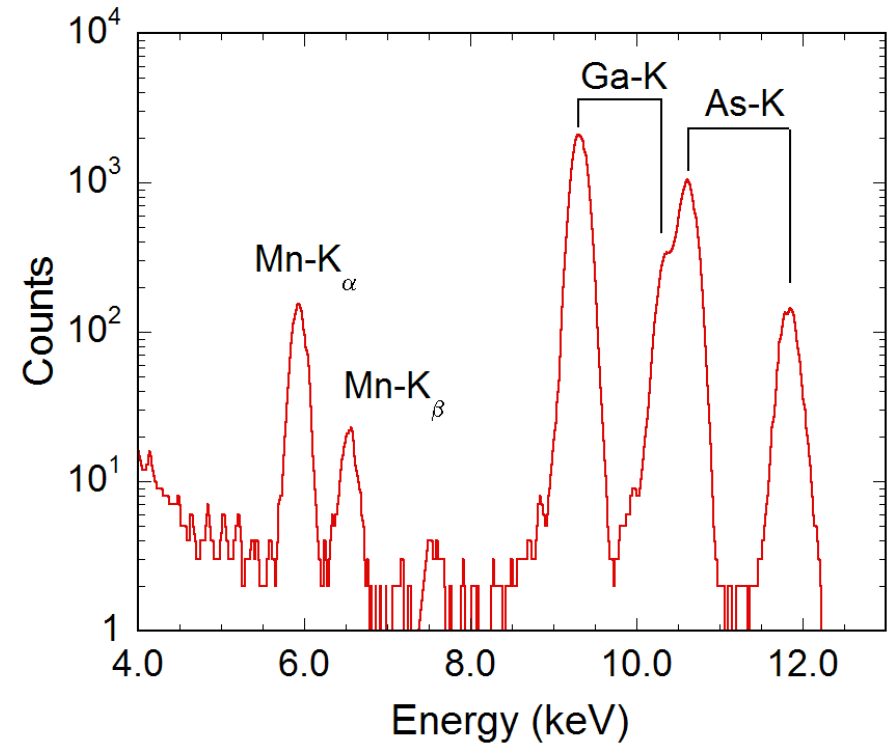
# PIXE: Light impurity in heavy matrix



RBS

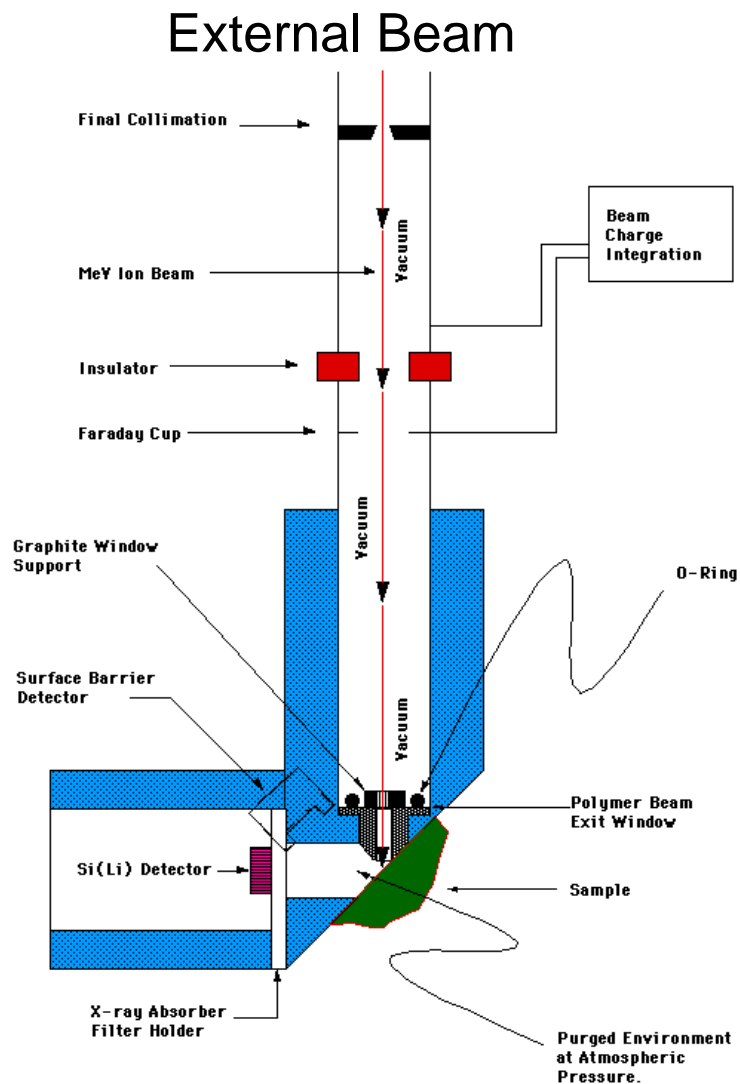


PIXE



*K. M. Yu et al. 2002.*

# PIXE Application: Geology, Art, Archeology, Biology



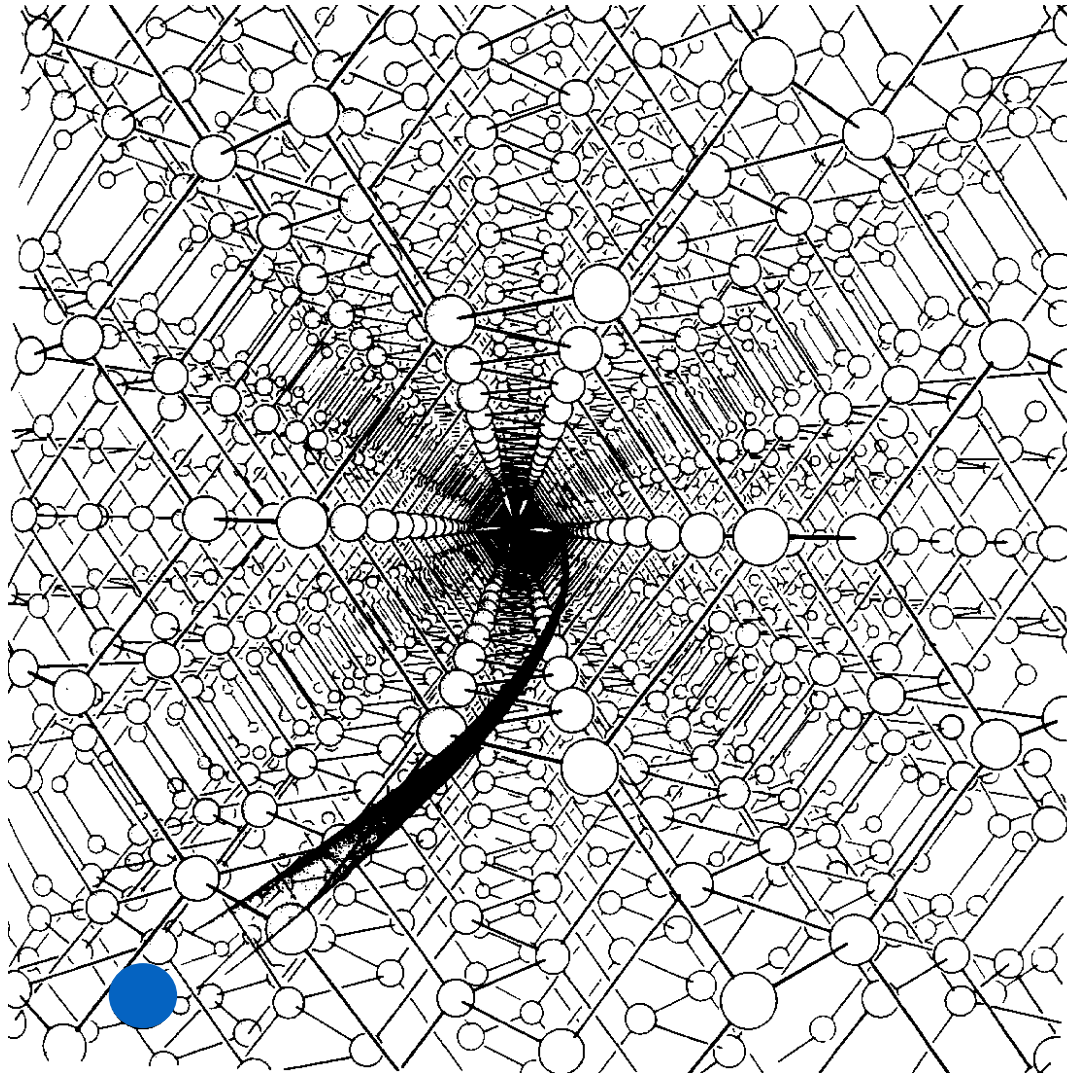
HARVARD PIXE SYSTEM



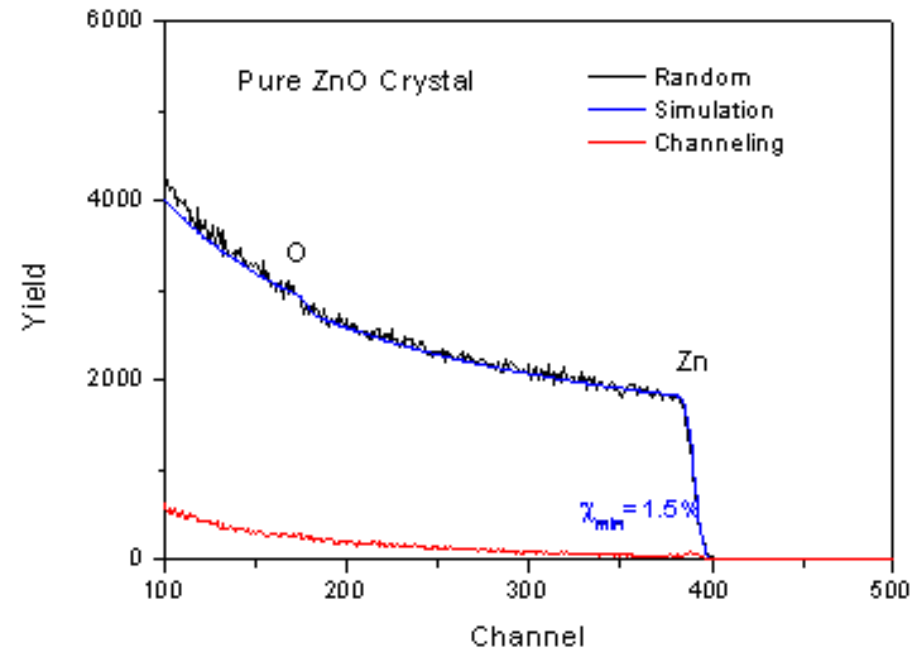
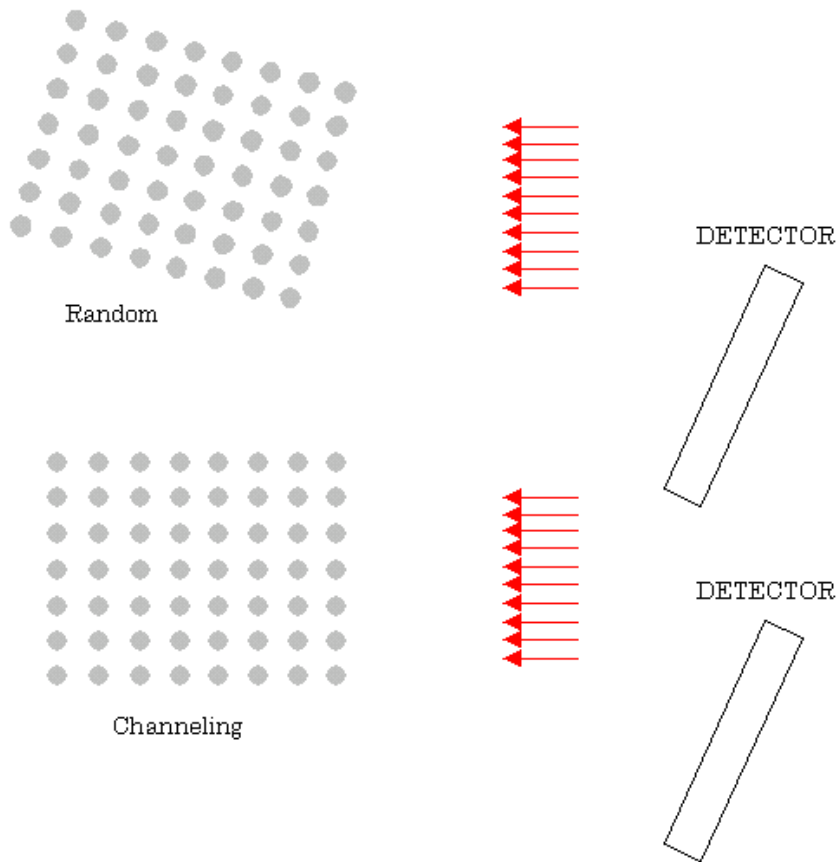
Figure 1. External PIXE set-up at IOP.



# Ion channeling

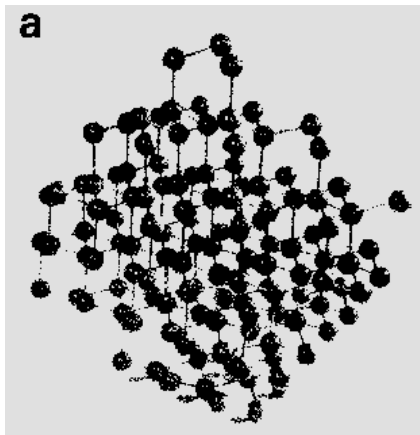
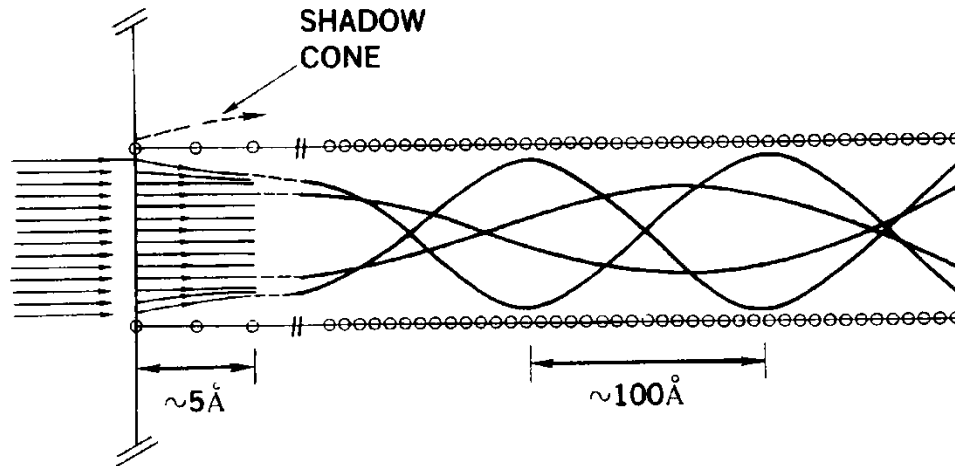


# Ion Channeling

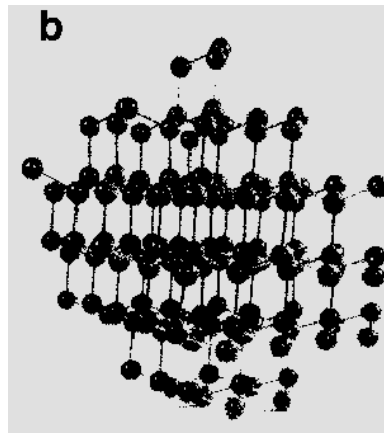


Kobelco Steel Group

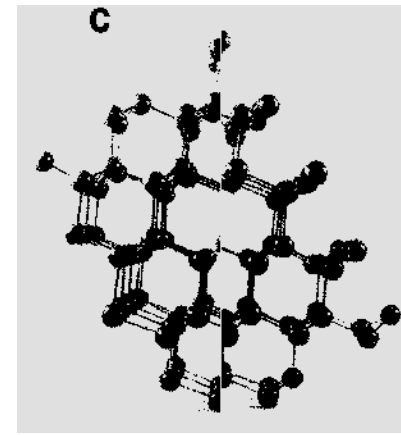
# Ion Channeling



random



Planar channel



Axial channel

# Ion Channeling:

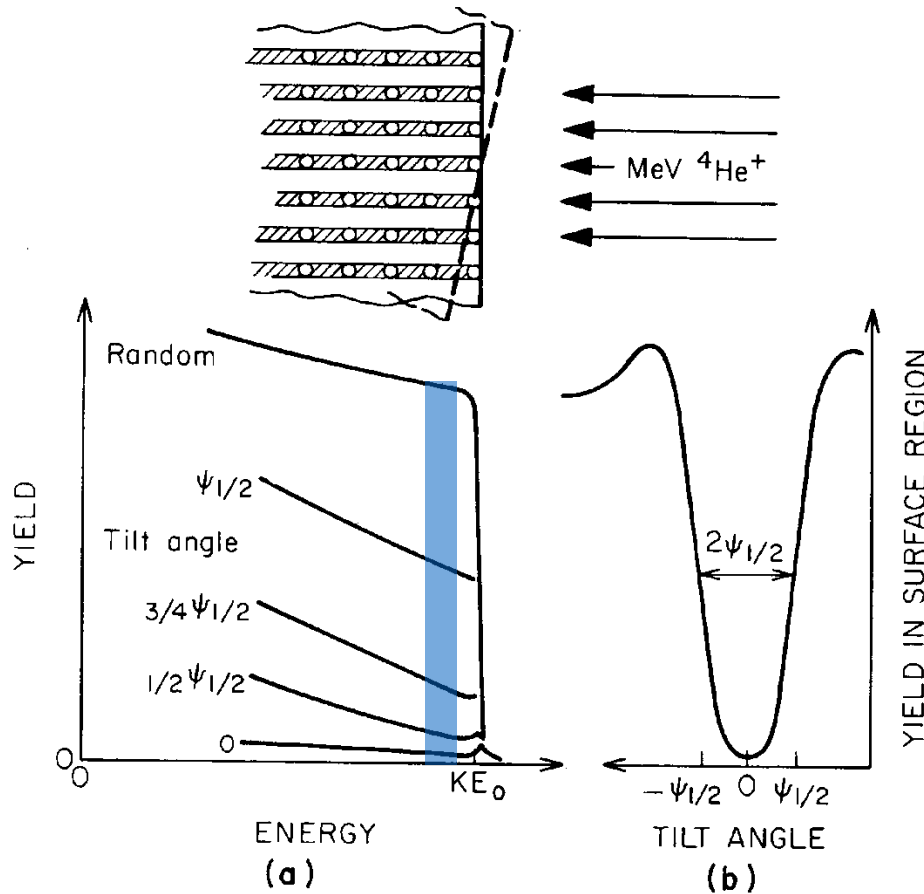
## minimum yield and critical angle

Two important parameters to characterize channeling results:

1. Minimum yield:

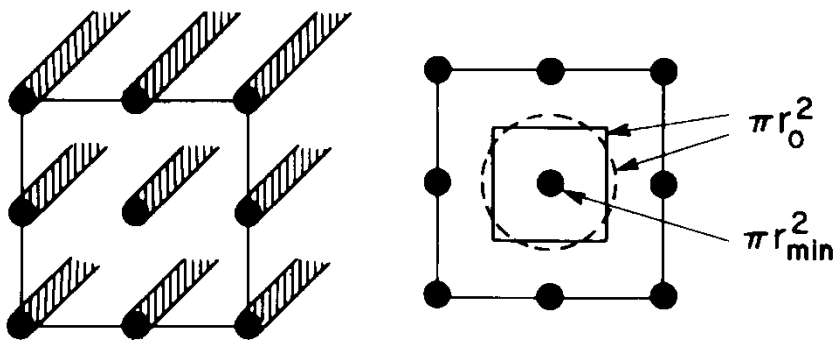
$$\chi_{\min} = \frac{Y_{\text{channeled}}}{Y_{\text{random}}} \sim 0.02-0.06$$

2. Critical half-angle,  $\psi_{1/2}$  indicates presence of defects responsible for beam dechanneling



# Ion Channeling: minimum yield and critical angle

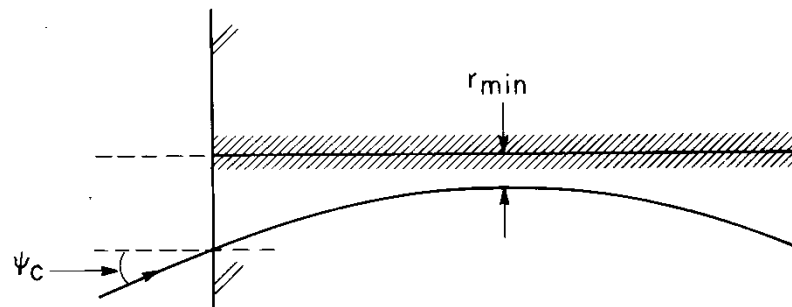
Minimum Yield,  $\chi_{\min}$



$$\chi_{\min} = \frac{Y_{\text{channeled}}}{Y_{\text{random}}}$$

$$\chi_{\min} \approx \frac{\pi r_{\min}^2}{\pi r_o^2} \sim 0.02 - 0.05$$

Critical half-angle,  $\Psi_{1/2}$

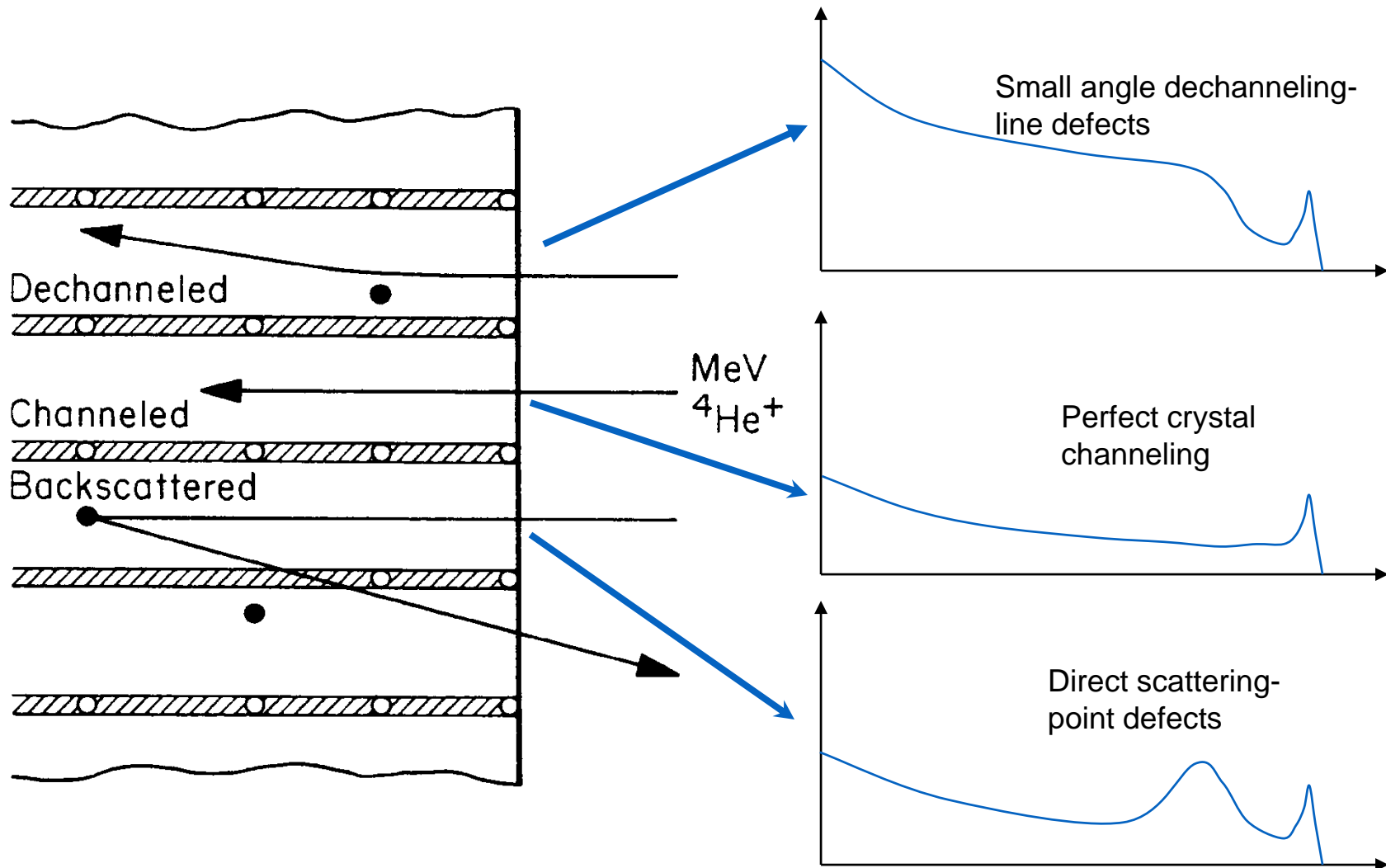


$$\Psi_c = \frac{1}{\sqrt{2}} \left( \frac{2Z_1 Z_2 e^2}{Ed} \right)^{1/2} \left\{ \ln \left[ \left( \frac{Ca}{\rho} \right)^2 + 1 \right] \right\}^{1/2}$$

where  $d$  is the distance of atoms in a row,  
 $a$  is the Thomas-Fermi screening distance,  $r$   
is rms thermal vibration

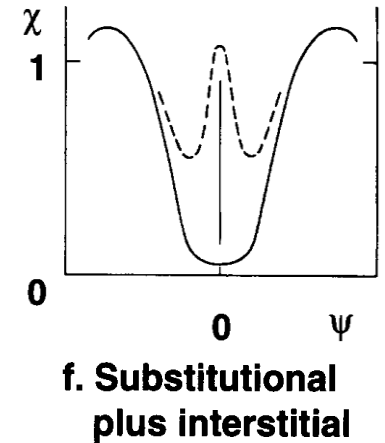
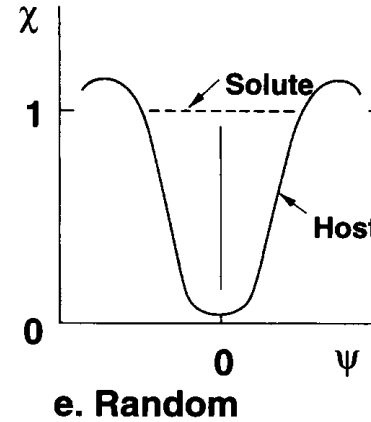
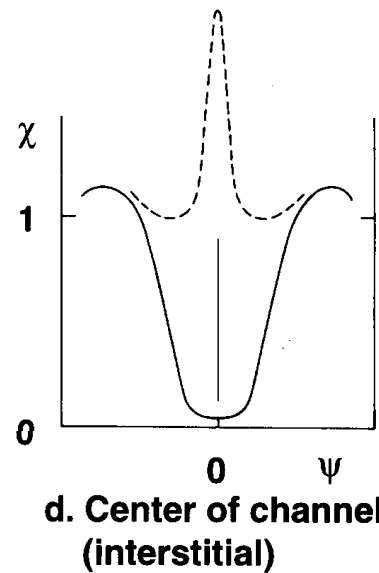
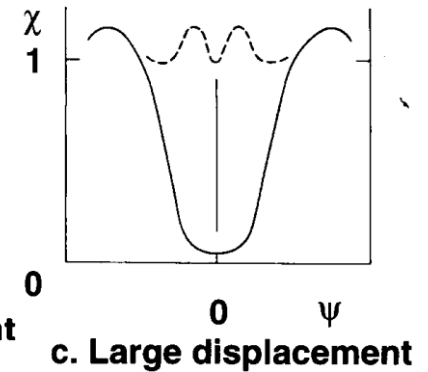
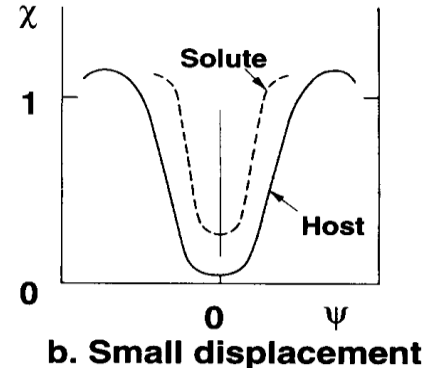
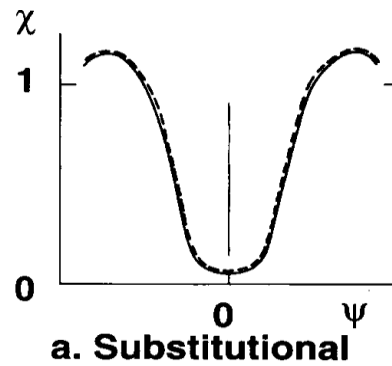
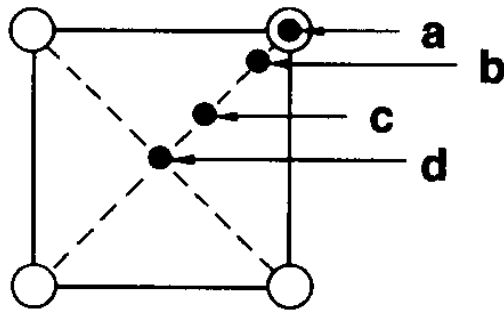
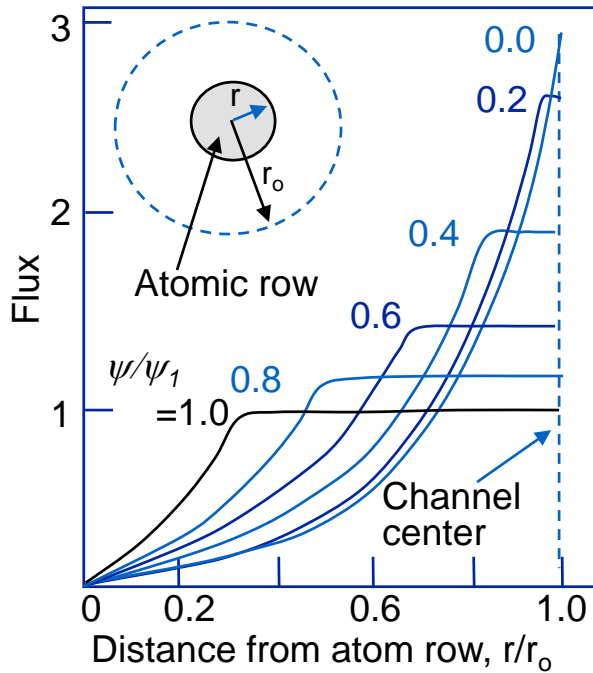
$$\Psi_{1/2} \sim \Psi_c \sim \left( \frac{2Z_1 Z_2}{E} \right)^{1/2} \sim 0.5 - 1^\circ$$

# Dechanneling by defects



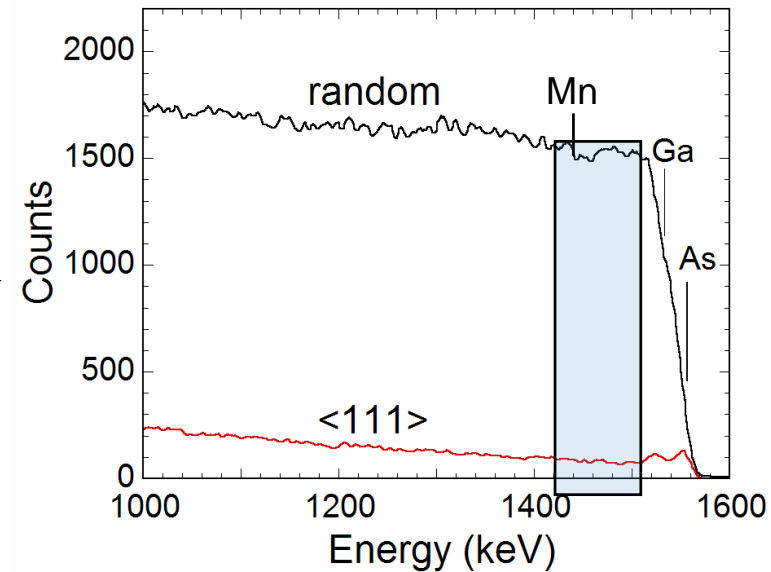
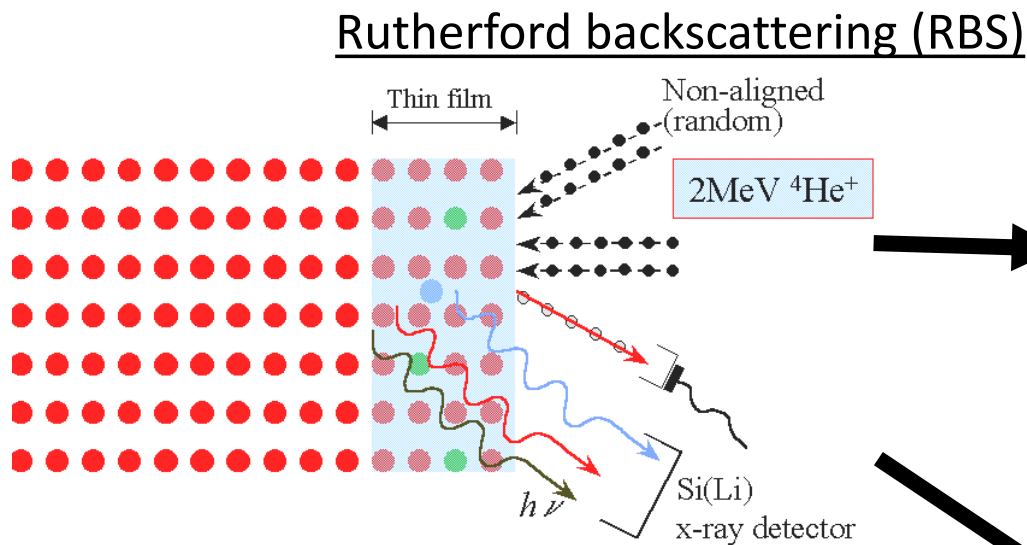


# Channeling: Impurity Lattice Location

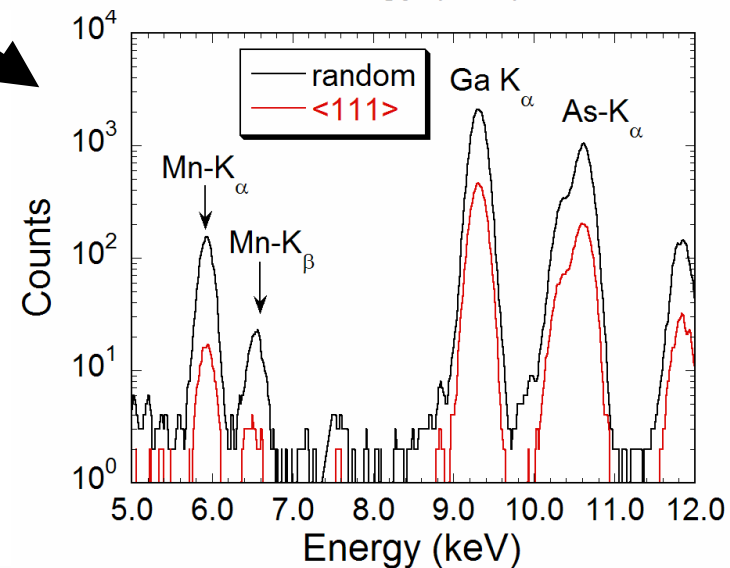


**Channel cross section**

# Experimental techniques : combined channeling RBS/PIXE



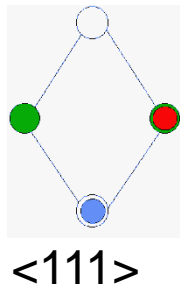
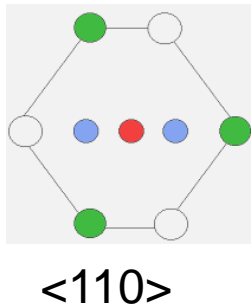
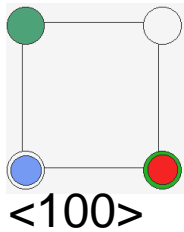
Particle-induced x-ray emission (PIXE)



**c-RBS:** crystalline quality of film  
(from GaAs backscattering yields)

**c-PIXE:** substitutionality of Mn  
atoms w.r.t. host GaAs

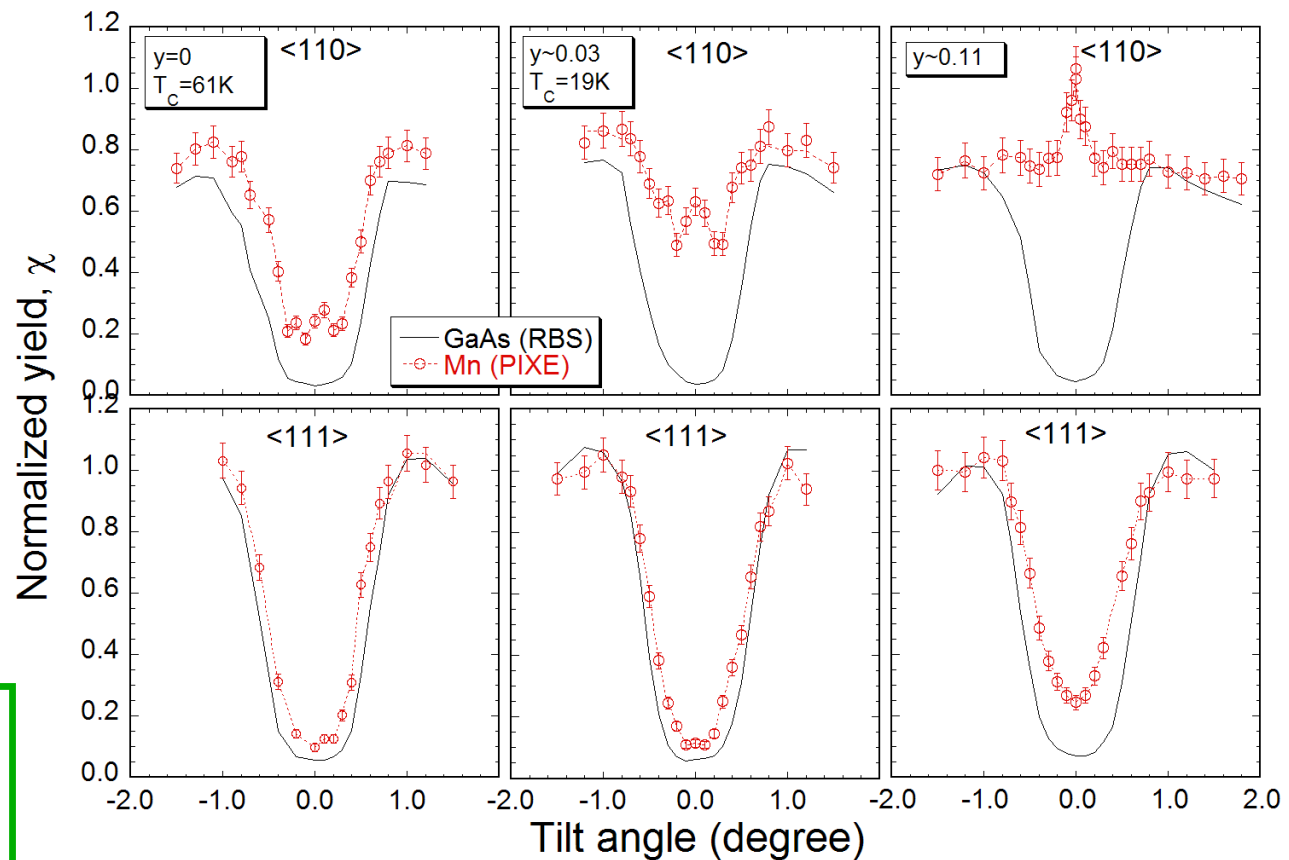
# Channeling: $\text{Ga}_{1-x-y}\text{Be}_y\text{Mn}_x\text{As}$



- Cation
- Anion
- Tetrahedral interstitials
- Hexagonal interstitials

Channeling RBS/PIXE:

- presence of interstitial Mn in GaAs
- $[\text{Mn}_i]$  increases with Be doping
- $\text{Mn}_i$  reduces  $T_c$



K. M. Yu et al. 2003.

# Homo- and Heteroepitaxy

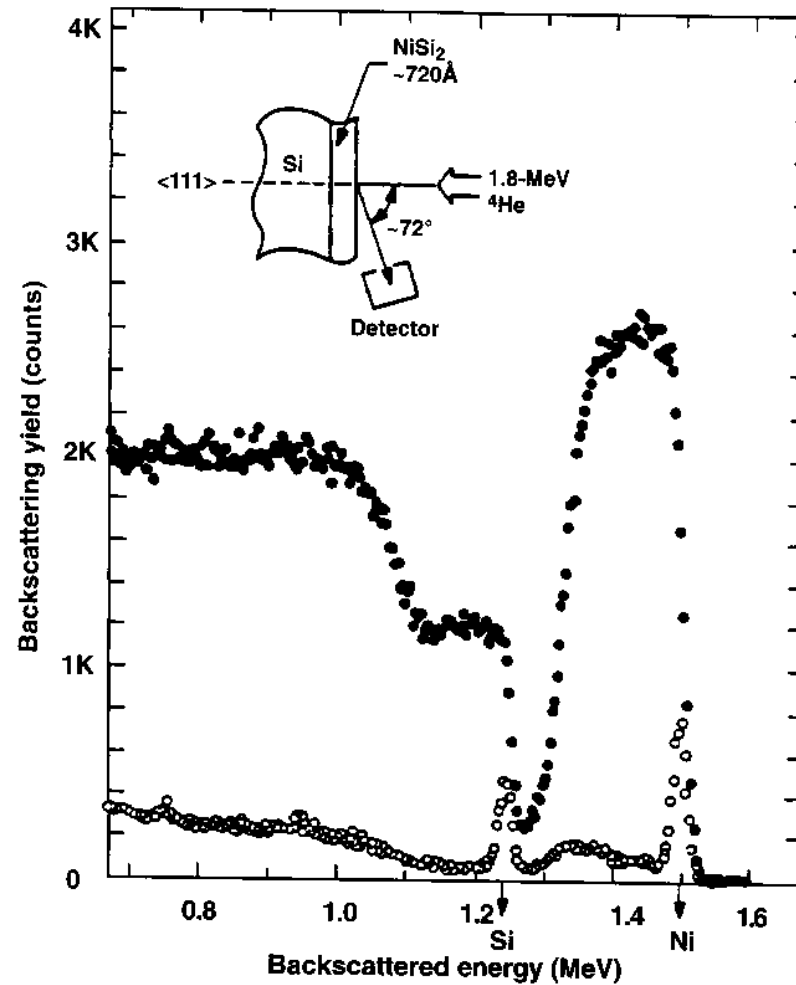
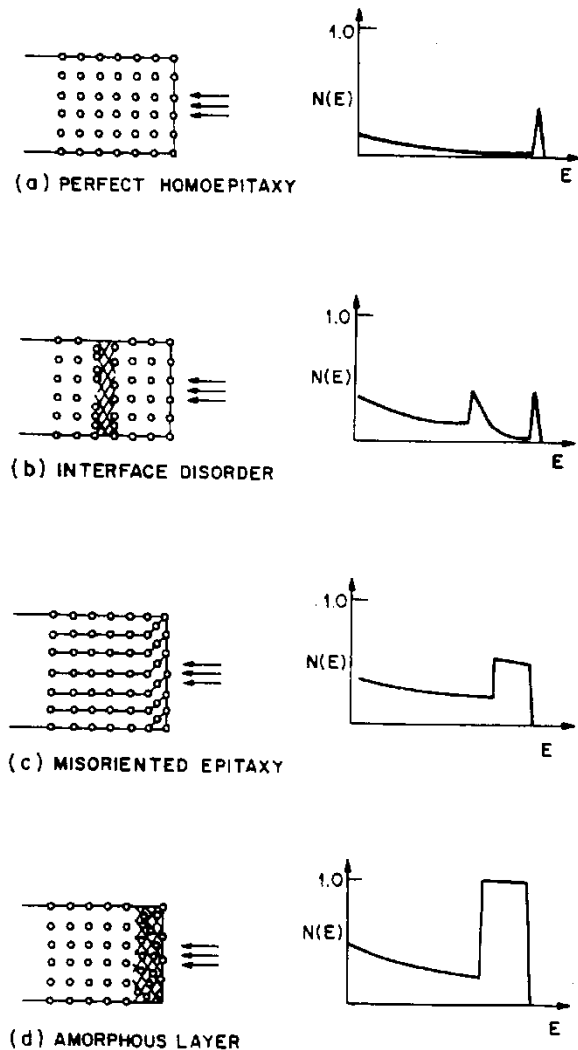
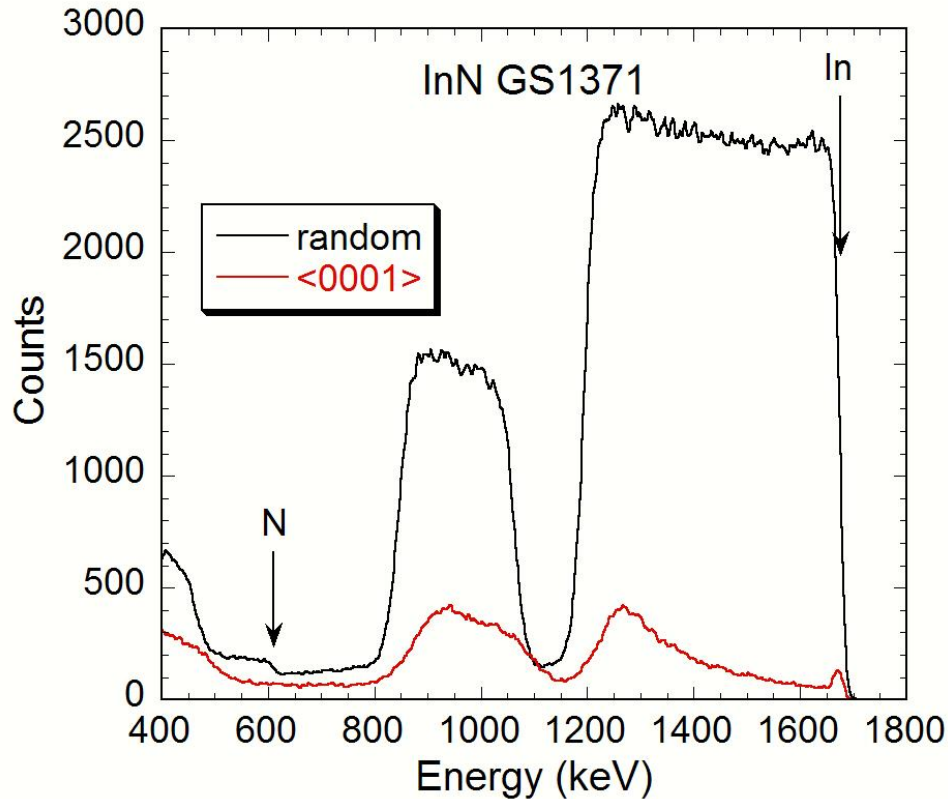


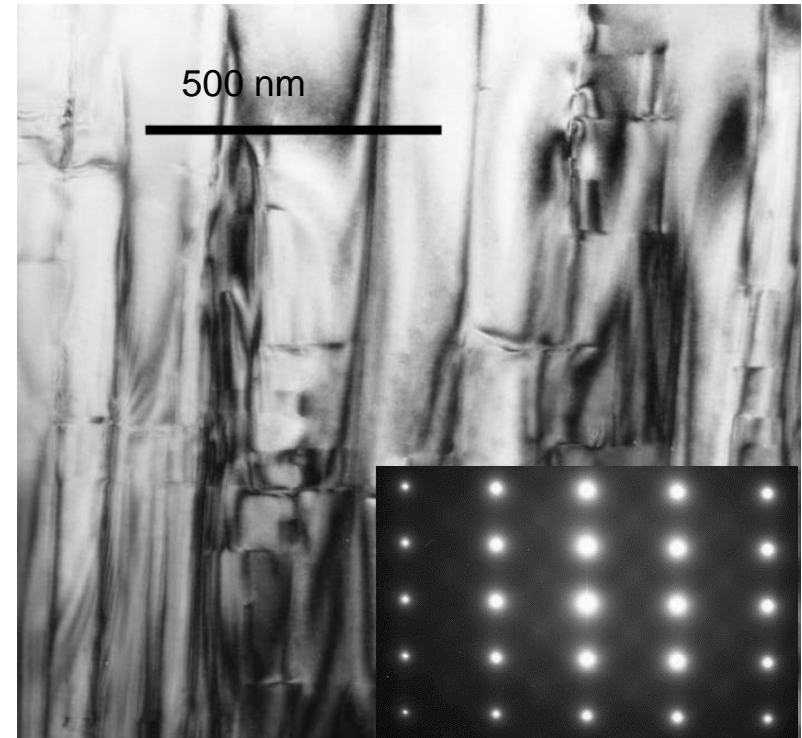
FIG. 10.24. Random and  $\langle 111 \rangle$  channeling spectra for a 72 nm  $\text{NiSi}_2$  epitaxial film on a  $\langle 111 \rangle$  Si substrate (from Chiu *et al.*, 1980).

# Channeling: Heteroepitaxy



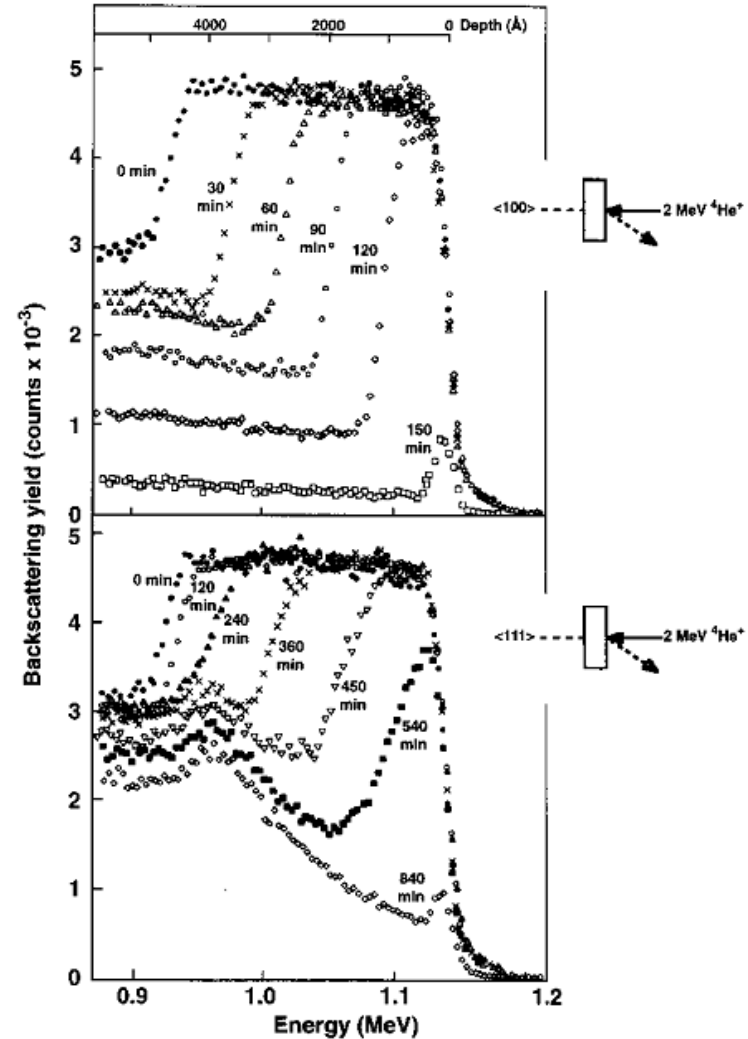
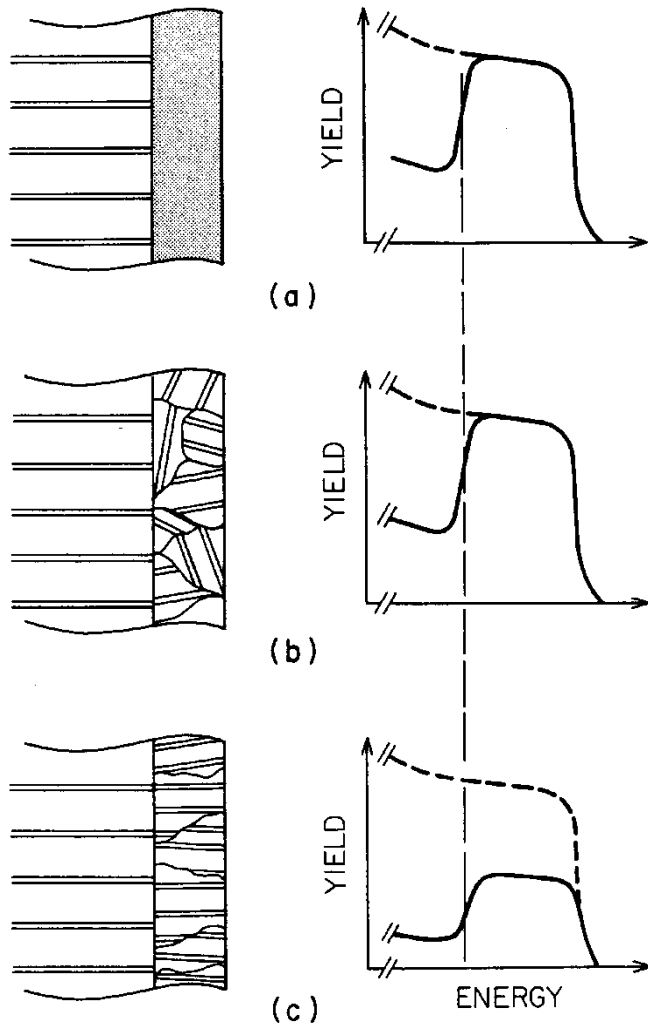
~530nm InN on 210 nm GaN

*K. M. Yu et al., LBNL 2004.*



*Z. Liliental-Weber*

# Amorphous layer analysis





# Strengths of Ion Beam Analysis Techniques

- Simple in principle
- Fast and direct
- Quantitative (without standard for RBS)
- Depth profiling without chemical or physical sectioning
- Non-destructive
- Wide range of elemental coverage
- No special specimen preparation required
- Can be applied to crystalline or amorphous materials
- Simultaneous analysis with various ion beam techniques (RBS, PIXE, channeling, etc.)

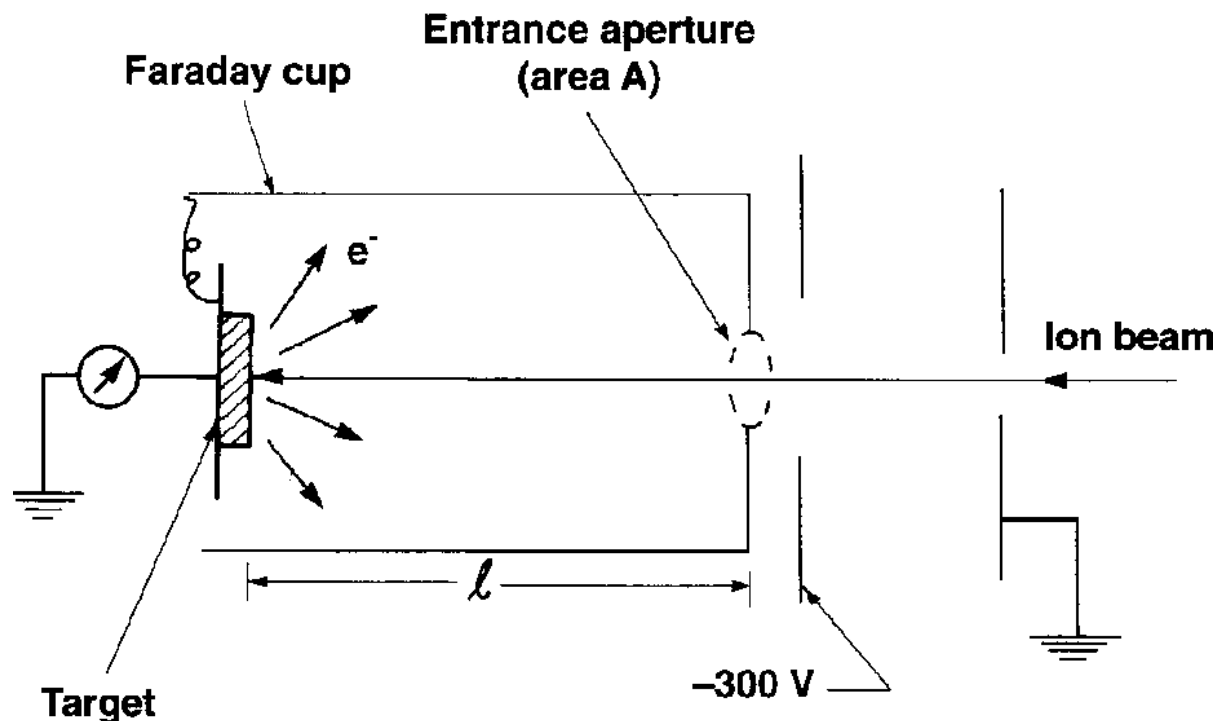
# Pitfalls in IBA

$$\text{Yield: } Y_i = N_i \left( \frac{d\sigma(E, \dots)}{d\Omega} \right) * Q\Omega$$

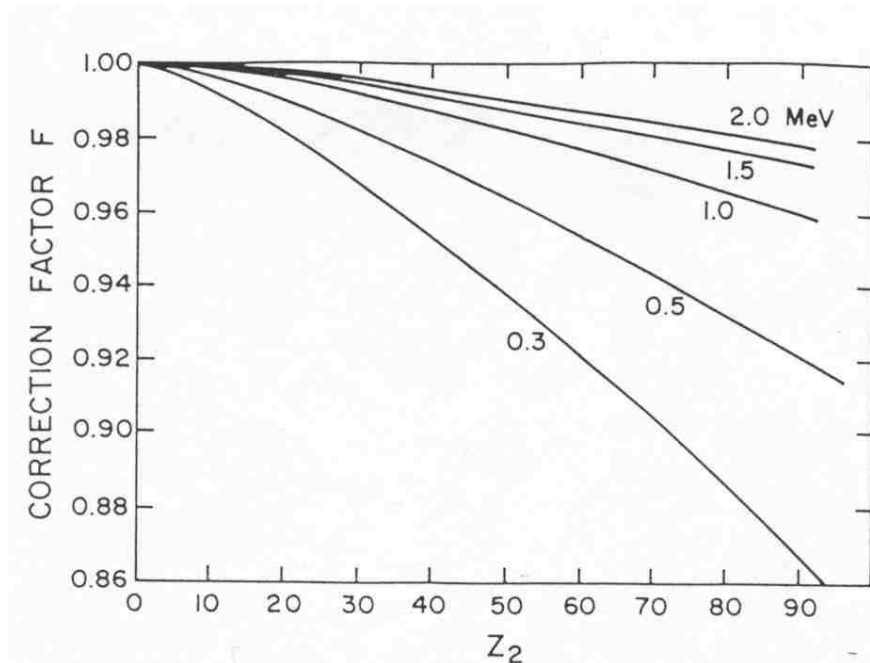
- Q-total charge
  - accurate charge integration
- $\Omega$ -solid angle
  - $d\sigma/d\Omega$ - detection angle, double/plural scattering
- Other issues:
  - Radiation damage
  - Sputtering
  - Detector response
  - Surface roughness
  - Non-uniformity
  - Charging on insulators
  - Count rate effects

# Charge integration

- Charge Integration
  - Accurate charge integration is important for absolute quantitative measurements
    - Good faraday cup design



# Deviation from Rutherford scattering



Correction factor  $F$ , which describes the deviation from pure Rutherford scattering due to electron screening for  $\text{He}^+$  scattering from atoms,  $Z_2$ , at variety of incident kinetic energies.

Electronic screening

Rutherford

Nuclear Interaction

Energy 

- At very high energy and very low energy, scattering will deviate from the Rutherford type.
- At low energy : screening of  $e^-$  must be considered
- At high energy : nuclear short range force will enhance the cross-section, the so-called “resonance scattering.”

# Charging effect for insulating samples

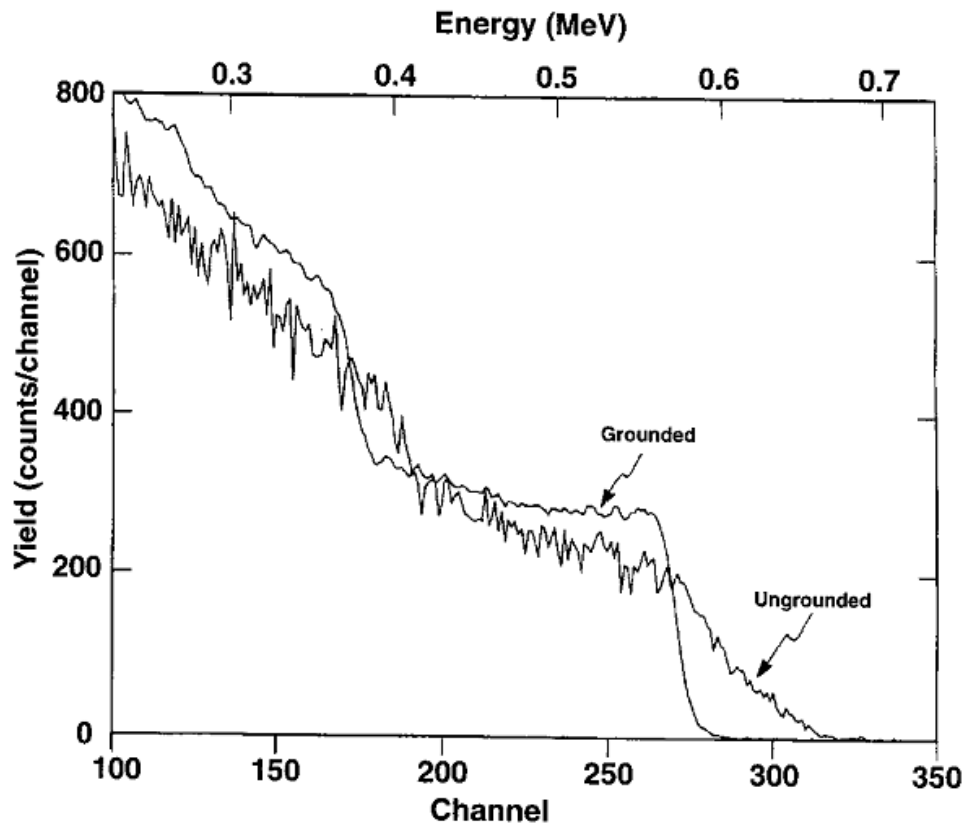


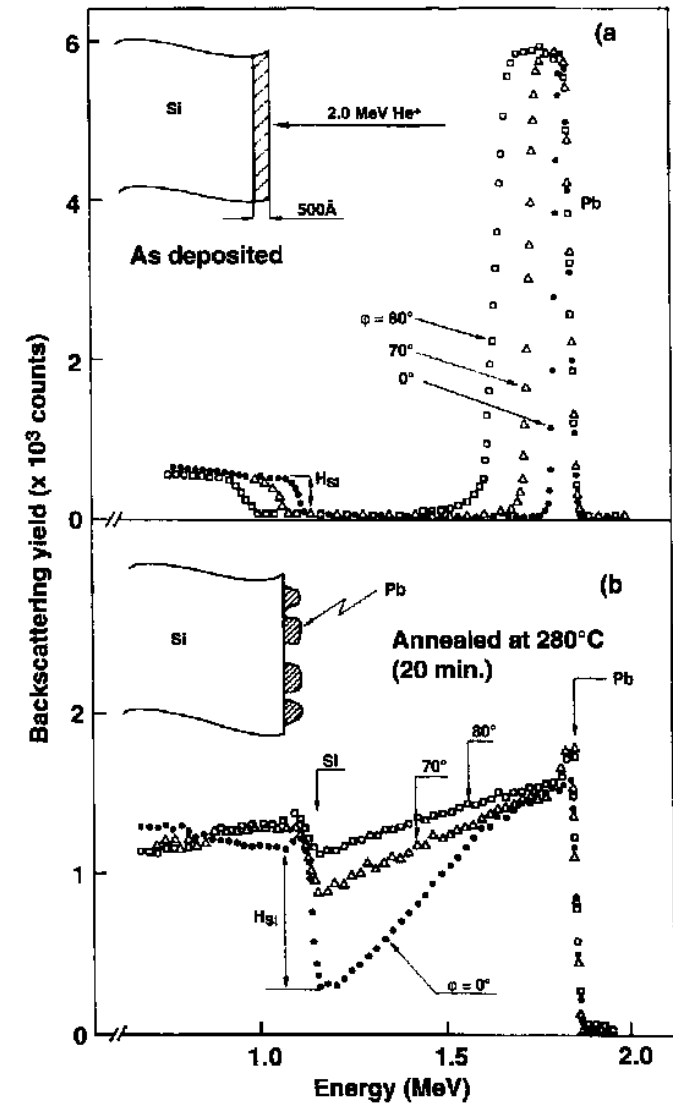
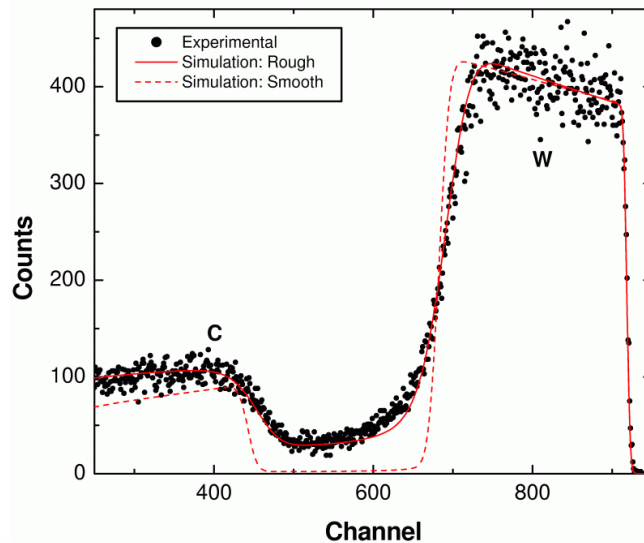
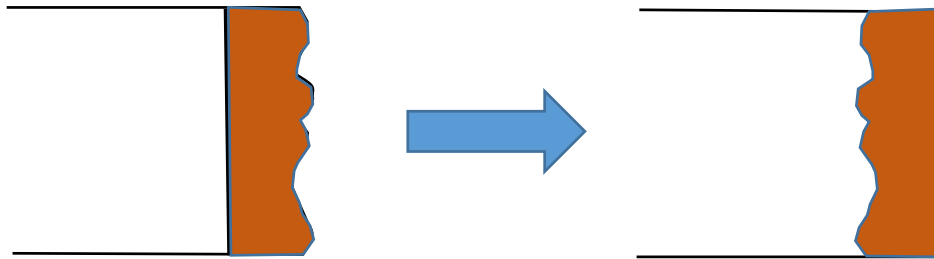
FIG. 12.8. Surface charging effect. Comparison of RBS spectra from a quartz target using 1 MeV  $^4\text{He}$ : a) ungrounded; b) grounded via a thin conductive surface layer of graphite by rubbing a pencil lightly across the surface (Almeida and Macauley-Newcombe, 1991).

Severely distort the RBS spectrum

- Provide a supply of low-E electrons from a small, hot filament located nearby
- Coating the surface with a very thin layer of conducting material

# Target non-uniformity

- Surface roughness and interface roughness cannot be distinguished
- Target non-uniformity will resemble diffusion



Campisano et al., 1978