

Introduction to Automatic Speech Recognition

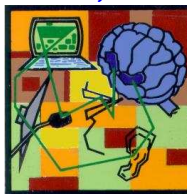
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“Automatic Speech Recognition using Sphinx and HTK”

A hands-on Workshop

18-FEB-2011

AU-KBC Research Centre, Chennai



<http://www.au-kbc.org/speech>

<http://speech.tifr.res.in>

- Overview
- Speech signal processing for feature extraction
- Recognition by Template matching
 - * Vowel recognition
 - * Classification of temporal patterns: DTW
- ASR using stochastic models
 - * Acoustic model: HMM
 - * Language model: Backoff trigram model

What is ASR?

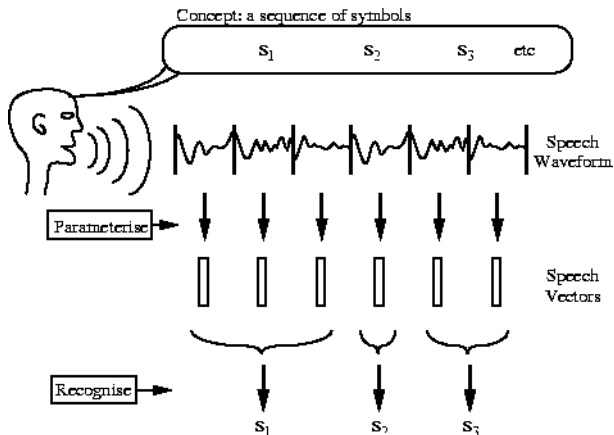


Fig. 1.1 Message Encoding/Decoding

source: HTK book

Dictation machine

Command and Control

- Speech interface to computer
- Electronic gadgets: phone, TV, VCR etc.
- Eyes and hands busy situations: Car driver, Pilot in a cockpit
- Aids to handicapped: voice operated wheel chair
- Information retrieval: bank, travel, Telco
- Keyword spotting

Types of ASR

Types of speech:

- Isolated Word Recognition (IWR)
- Connected Word Recognition (CWR)
- Continuous Speech Recognition (CSR)
- Spontaneous speech
- KeyWord Spotting (KWS)

Speaker dependence:

- speaker dependent/adaptive/independent
- multi-speaker

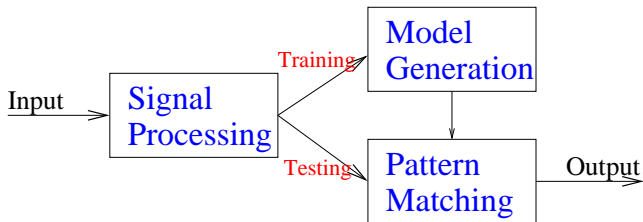
Vocabulary:

- Small (< 100 words), Medium (hundreds), Large (thousands)
- Very large (tens of thousands), Out of vocabulary (OOV)

Bandwidth:

- Wideband/desktop
- Narrowband

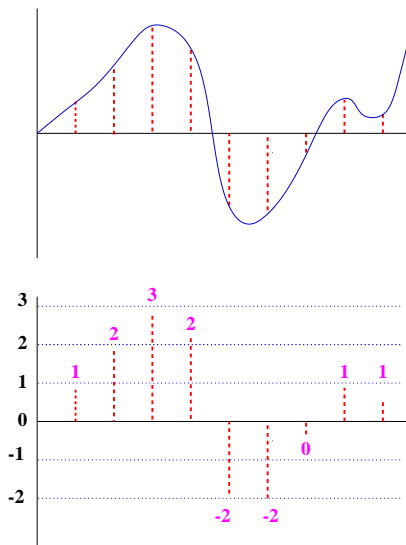
Speech Recognition is Sequential Pattern Recognition



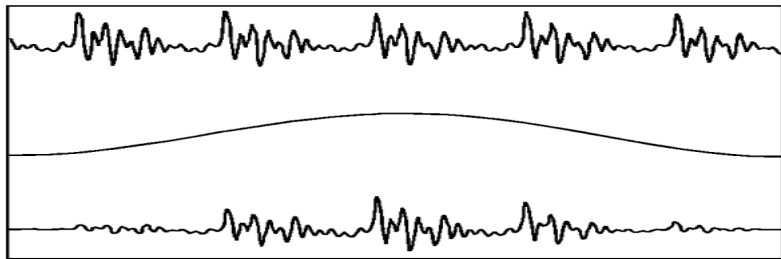
Goal: recognise the sequence of words from time waveform of speech.

Two phases: Training (learning) and Testing (recognition)

Analog to digital (A2D) conversion



Digitisation = Sampling + Quantisation
analog wave \rightarrow a sequence of integers



Blocking sequence into analysis **frames**

$$x(n) = s(m)w(n - m)$$

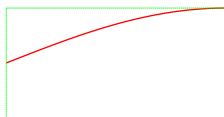
$w(n)$ is a *Tapering window*

Production of voiced sounds



vowel अ

Glottal impulses; Resonances of vocal tract



Uniform tube model

$$\nu = c/\lambda = 34000/4 * 17 = 500\text{Hz}$$



glottal vibration

vocal tract

speech wave

Formant === pole of a filter

Source-Filter model of speech production



glottal vibration

vocal tract

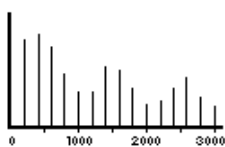
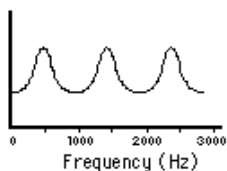
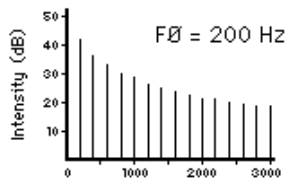
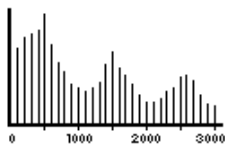
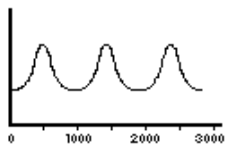
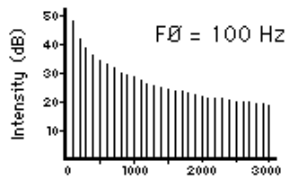
speech wave

$$s(n) = e(n) * h(n)$$

$$S(k) = E(k)H(k)$$

$$\log(|S(k)| ** 2) = \log(|E(k)| ** 2) + \log(|H(k)| ** 2)$$

Illustration in spectral domain



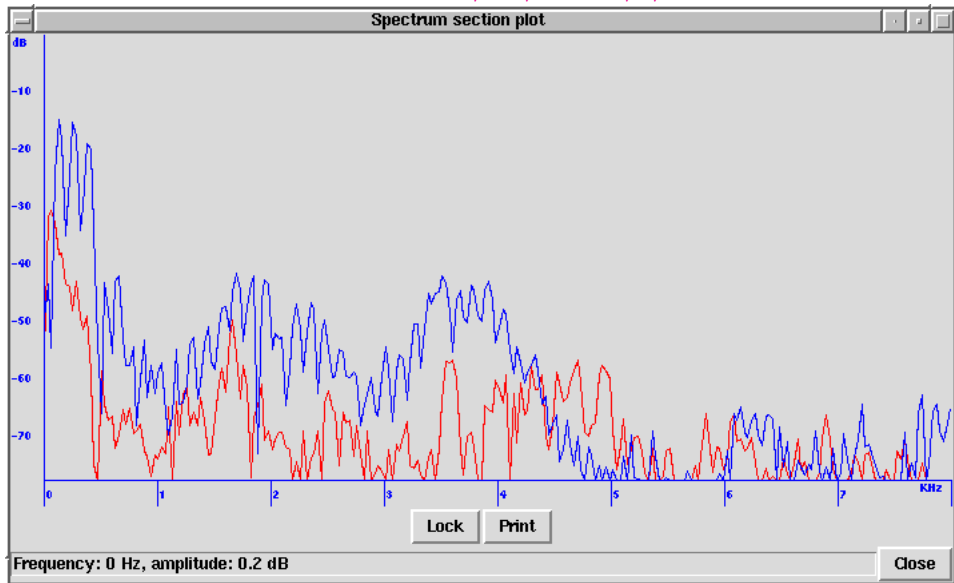
SOURCE SPECTRUM

FILTER FUNCTION

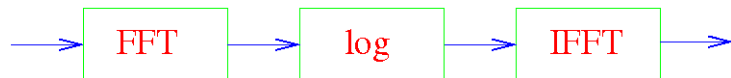
OUTPUT ENERGY SPECTRUM

source: <http://www.haskins.yale.edu/haskins/HEADS/MMSP/acoustic.html>

Speech Spectra of /th/ and /i/ sounds

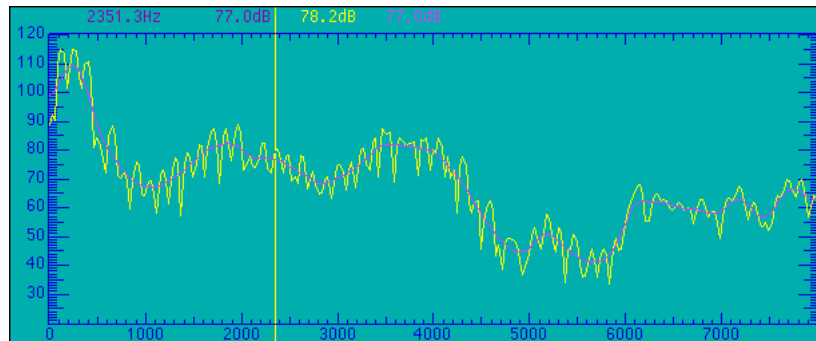


Cepstral Analysis



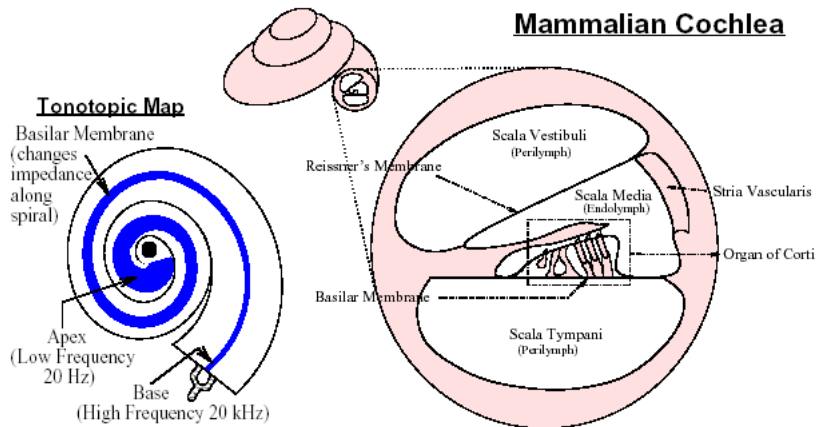
Waveform Power spectrum Log spectrum Cepstrum

$$cep(q) = IFFT\{log(|S(k)| ** 2)\} \quad q = 0, 1, \dots, N - 1$$



Captures not only resonances but also anti-resonances.

Mammalian Cochlea



Basilar membrane: Bark/mel scale

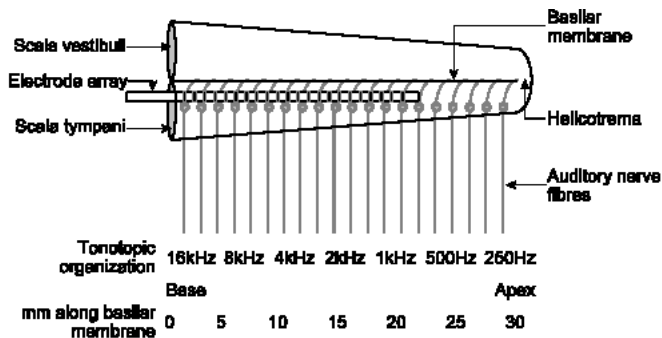
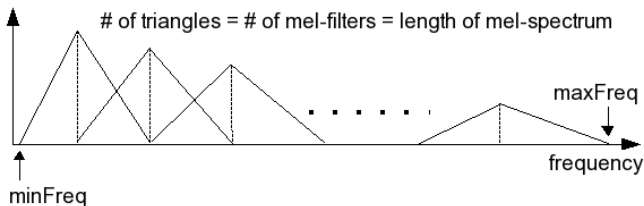


Figure 1.1. A simplified unrolled representation of the cochlea showing the auditory nerve fibres, the tonotopic organization of these nerve fibres and an intracochlear electrode array in the scala tympani.

Critical band phenomenon

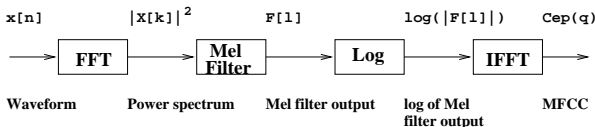
Non-linearities along amplitude and frequency

MFCC



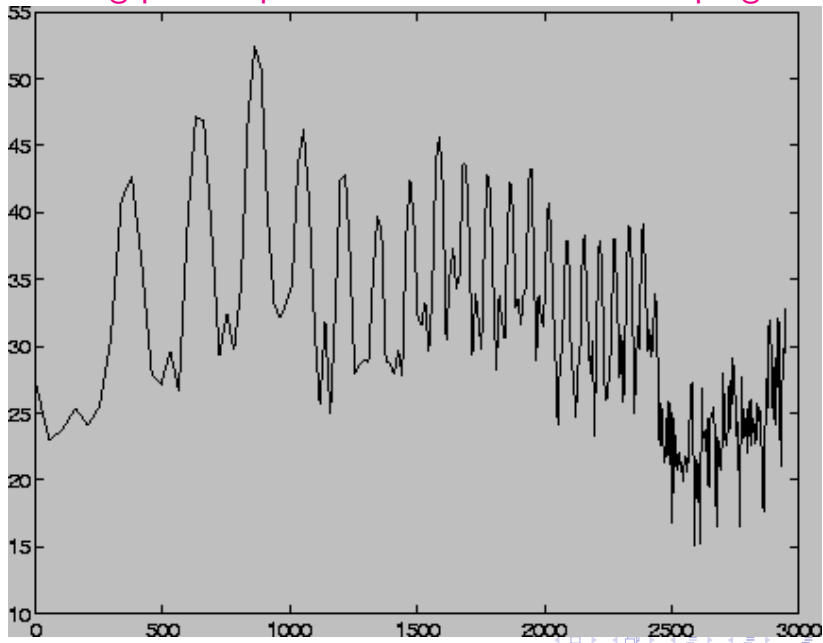
$$B(m) = \sum_{k=lo(m)}^{hi(m)} |X(k)|^2$$

$$cep(q) = IFFT\{\log(|B(m)|^2)\} \quad q = 0, 1, \dots, N$$



Mel Frequency Cepstral Coefficients

Log power spectrum after mel scale warping



Phones and Phonemes

Phone: A sound generated by human vocal apparatus and used for human communication in a language.

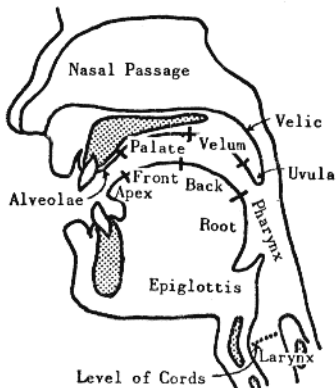
Phoneme: Smallest meaningful contrastive unit in the phonology of a language.

Allophones: “p” and “ph” are allophones of one phoneme /p/ in English, are two distinct phonemes in Hindi

Minimal pair:

पल vs फल

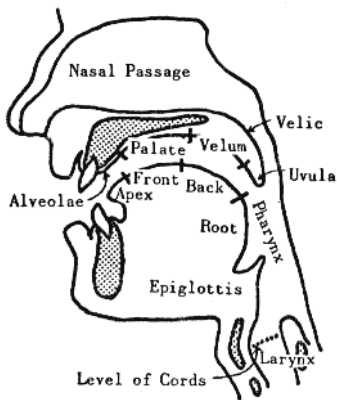
Place and Manner of articulation



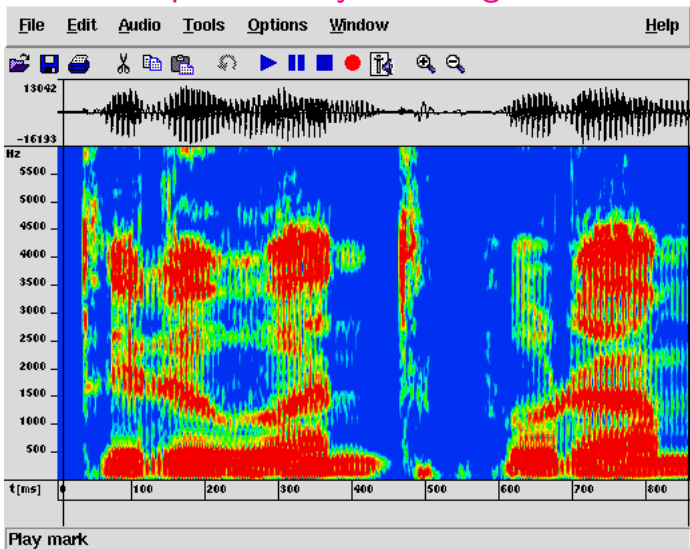
अ	आ	इ	ई	उ	ऊ	ए	ऐ	ओ	औ
<i>a</i>	<i>A</i>	<i>i</i>	<i>I</i>	<i>u</i>	<i>U</i>	<i>e</i>	<i>E</i>	<i>o</i>	<i>O</i>

क	ख	ग	घ	ङ
<i>k</i>	<i>kh</i>	<i>g</i>	<i>gh</i>	<i>ng</i>
च	छ	ज	झ	ञ
<i>c</i>	<i>ch</i>	<i>j</i>	<i>jh</i>	<i>nj</i>
ट	ठ	ड	ढ	ण
<i>T</i>	<i>Th</i>	<i>D</i>	<i>Dh</i>	<i>N</i>
त	थ	द	ध	न
<i>t</i>	<i>th</i>	<i>d</i>	<i>dh</i>	<i>n</i>
प	फ	ब	भ	म
<i>p</i>	<i>ph</i>	<i>b</i>	<i>bh</i>	<i>m</i>

य	र	ल	व	श	ष	स	ह
<i>y</i>	<i>r</i>	<i>l</i>	<i>w</i>	<i>sh</i>	<i>S</i>	<i>s</i>	<i>h</i>



Speech: a dynamic signal



Formant: frequency of resonance: F_1 , F_2 , F_3 , ...

Slope and curvature of trajectory

Delta coefficients: $y(x) = m x + c$

If $Cep(n, l)$ is the n^{th} cepstral coefficient at time (frame) index l , we can define

$$\Delta Cep(n, l) = \frac{\sum_{l=-L}^L l Cep(n, l)}{\sum_{l=-L}^L l^2}$$

Delta-delta (acceleration) coefficients

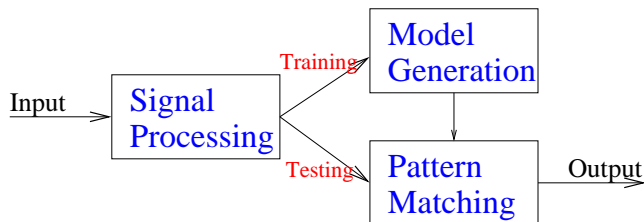
$$\Delta^2 Cep(n, l) = \frac{\sum_{l=-L}^L l \Delta Cep(n, l)}{\sum_{l=-L}^L l^2}$$

Speech signal \Rightarrow Sequence of feature vectors

Speech Signal Processing (Feature Extraction)

- ▶ Digitisation of analog speech signal
- ▶ Blocking signal into frames
- ▶ FFT \rightarrow mel filter \rightarrow log \rightarrow IFFT \Rightarrow MFCC
- ▶ Slope and curvature
- ▶ Sequence of feature vectors : x_1, x_2, \dots, x_T
: o_1, o_2, \dots, o_T

Recognition of (static) patterns

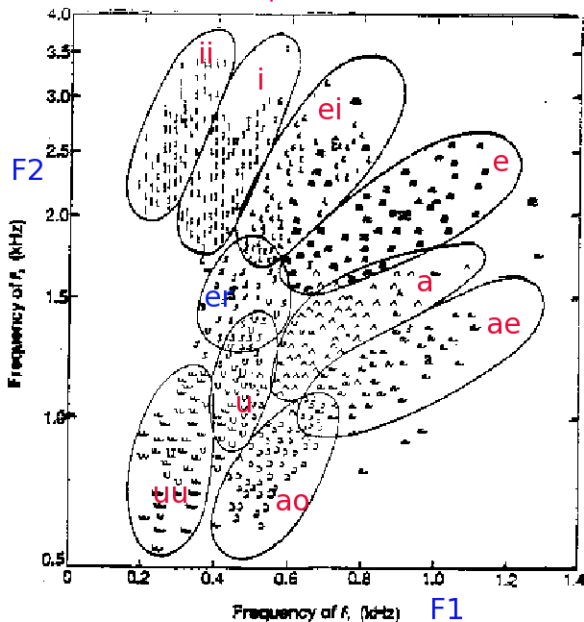


Signal Processing \Rightarrow Sequence of feature vectors

Pattern Recognition

Illustration: Vowel recognition with the first 2 Formant frequencies as features

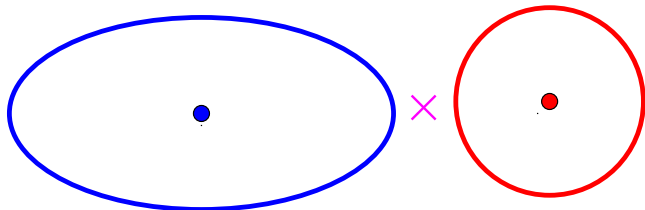
Formant space of vowels



Classification criterion

* Euclidean Distance

$$x \in C_k \quad \text{if } (x - \mu_k)^2 \leq (x - \mu_j)^2 \quad \forall j$$



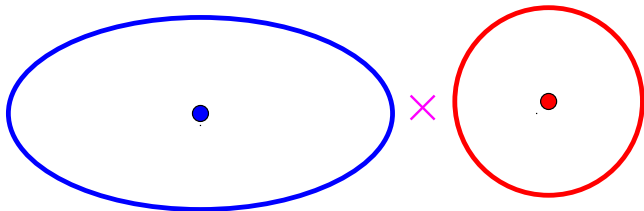
* Weighted Euclidean distance

$$d^k = \sqrt{\left(\frac{x - \mu^k}{\sigma^k}\right)^2}$$

Classification criterion

* Euclidean Distance

$$x \in C_k \quad \text{if } (x - \mu_k)^2 \leq (x - \mu_j)^2 \quad \forall j$$



* Weighted Euclidean distance

$$d^k = \sqrt{\left(\frac{x - \mu^k}{\sigma^k}\right)^2}$$

* Extension to multiple features

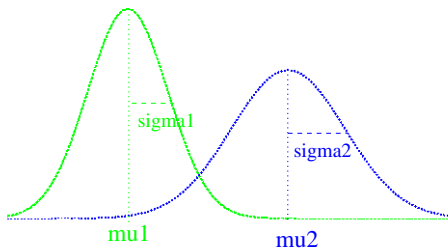
$$d^k = \sqrt{\sum_i \left(\frac{x_i - \mu_i^k}{\sigma_i^k}\right)^2}$$

$d(\bar{x}, \bar{\mu}_k)$

Two class problem

Normal Distribution: $N(\mu; \sigma)$

$$p(x) = \frac{1}{\sqrt{2\pi\sigma^2}} \exp \left\{ -\frac{1}{2} \left(\frac{x - \mu}{\sigma} \right)^2 \right\}$$

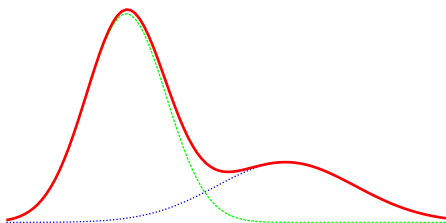


Maximum Likelihood classification criterion:

$$x \in C_k \quad \text{if} \quad p(x|N(\mu_k; \sigma_k)) \geq p(x|N(\mu_j; \sigma_j)) \quad \forall j$$

Refer to vowel F1-F2 diagram

Gaussian Mixture Model(GMM)



$$p(x|GMM(k)) = \alpha p(x : N[\mu_1; \sigma_1]) + (1 - \alpha) p(x : N[\mu_2; \sigma_2])$$

Maximum Likelihood classification criterion for GMM case:

$$x \in C_k \text{ if } p(x|GMM(k)) \geq p(x|GMM(j)) \quad \forall j$$

Extension to Multi-dimensional space

Classification of Temporal patterns

Isolated Word Recognition:

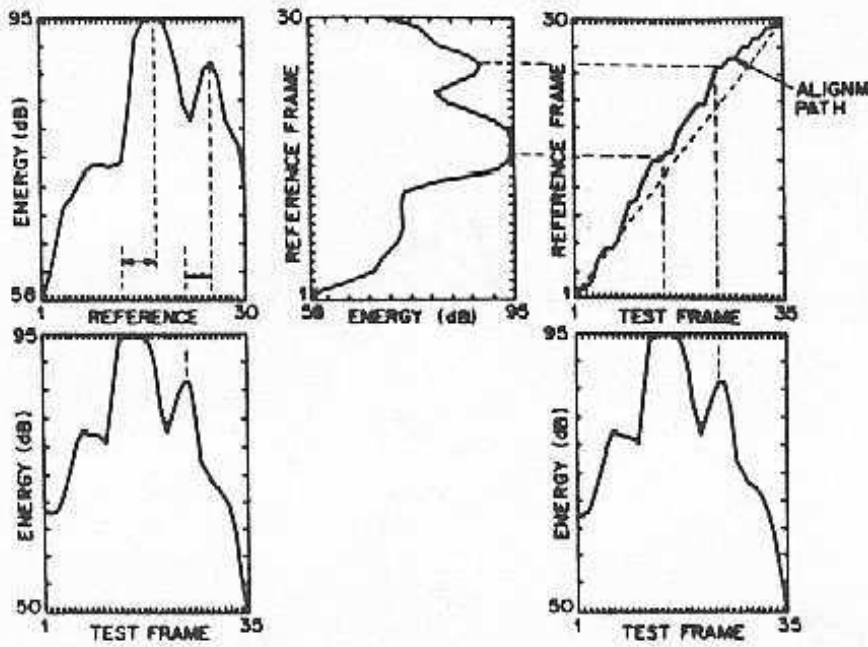
Example: name dialling

Match a sequence of test feature vectors x_1, x_2, \dots, x_N
with a sequence of reference feature vectors r_1, r_2, \dots, r_M

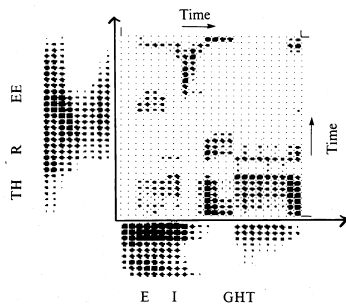
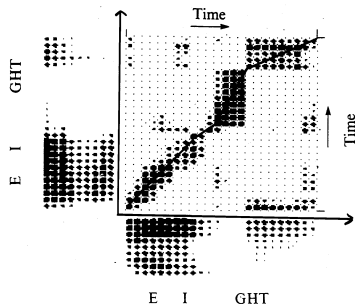
Reasons for $N \neq M$

- ▶ End-point detection errors
- ▶ speaking rate variations
- ▶ Within word variations

Linear vs Non-linear Time-warping



Optimal alignment path



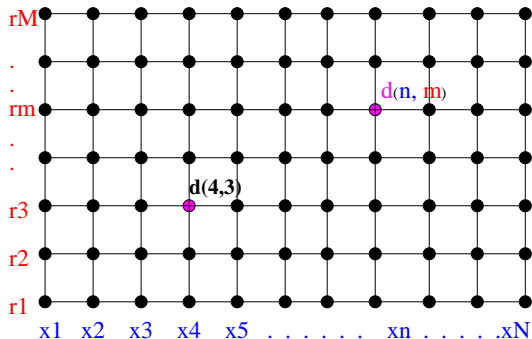
From: Holmes book

Bigger the dark blob, greater the similarity (lesser distance).

“eight” versus “eight”: A path along diagonal exists

“eight” versus “three”: A path along diagonal **does not** exist.

Dynamic Programming

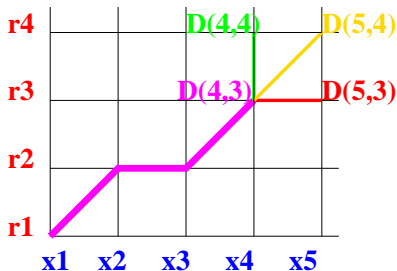


Test feature vector sequence

Goal: To find the **optimal alignment path** from the grid point $(1, 1)$ to the grid point (N, M) . There are exponential number (M^N) of paths. In order to reduce the number of computations from exponential to linear, we use the **Dynamic Programming** whose foundation is the “principle of optimality”.

Principle of optimality: The best path from (1, 1) to any given point on the grid is independent of what happens beyond that point.

So, if two paths share a partial path starting from (1, 1), the cost of this shared partial path need to be computed only once and stored in a table for later use.



DP Algorithm: Define

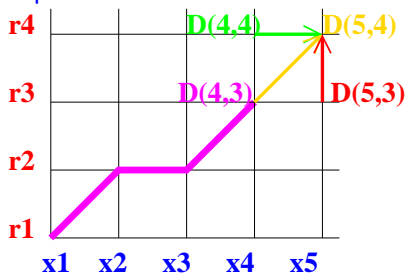
$d(n, m)$: the **local** distance between the n^{th} test frame and m^{th} reference frame.

$D(n, m)$: the **accumulated** distance of the optimal path starting from the grid point (1, 1) and ending at the grid point (n, m).

Dynamic Time Warping

Applying the *Principle of optimality*, $D(n, m)$ is the sum of the local cost, and the cost of cheapest path to it

$$D(5,4) = d(5,4) + \min \begin{cases} D(4,4) \\ D(4,3) \\ D(5,3) \end{cases}$$



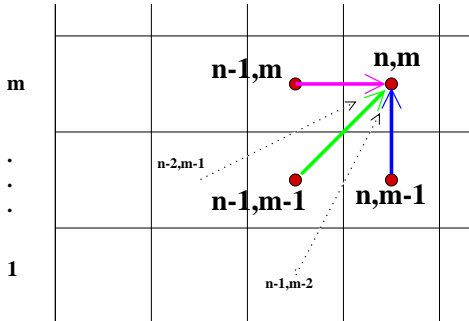
$$D(n, m) = d(n, m) + \min \begin{cases} D(n-1, m) \\ D(n-1, m-1) \\ D(n, m-1) \end{cases}$$

* Compute $D(n, m)$ for each “allowed” pair of (n, m) .

Remember the “best” predecessor point.

* $D(N, M)$ is the cost of the optimal path.

* From (N, M) , start backtracing to identify the optimal path.



$$D(n, m) = d(n, m) + \min \begin{cases} D(n-1, m) \\ D(n-1, m-1) \\ D(n, m-1) \end{cases}$$

- * Compute $D(n, m)$ for each “allowed” pair of (n, m) . Remember the “best” predecessor point.
- * $D(N, M)$ is the cost of the optimal path.
- * From (N, M) , start backtracing to identify the optimal path.

Global constraints: left- and down-paths are prohibited.

Local constraints: path $(n, m-1) \rightarrow (n, m)$ not allowed.

Spell checking: Application of Dynamic Programming

Reference (correct spelling)

n	1	1	2			1	1	0
r	1	1	2	1	2	0	0	1
e	2	2	1	2	1	2	2	2
t	1	1	2	0	2	1	1	
a	1	1	2	0	2	1	1	
p	2	2	0	2	0	2		
	0	0	2		2	1		
	p	p	a	t	a	r	r	n

$$d(v, c) = 2$$

$$d(v1, v2) = 1$$

$$d(c1, c2) = 1$$

Test sequence (just typed in text)

p a t t e r n

1	8	1	2			1	2	1	2	0	1	
1	7	1	2	1	2	3	0	1	0	1	1	2
2	6	2	1	2	2	1	1	2	3	2	2	
1	4	1	4	2	4	0	0	2	2	1	1	
1	3	1	3	2	2	0	0	2	2	1	1	
2	2	2	2	0	0	2	2	0	2	2		
0	0	0	0	2	2	4	2	2	1			

p p a t a r r n

Test sequence (just typed in text)

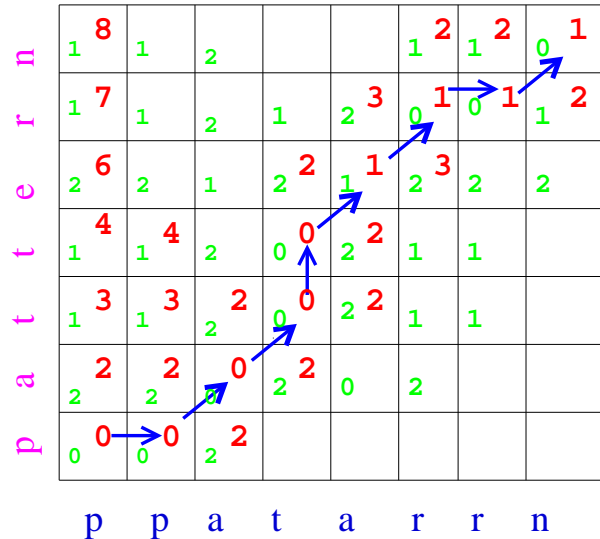
$$d(v, C) = 2$$

$$d(v_1, v_2) = 1$$

$$d(C_1, C_2) = 1$$

$$D(x, y) = d(x, y)$$

$$+\min \begin{cases} D(x-1, y-1) \\ D(x-1, y) \\ D(x, y-1) \end{cases}$$



$$d(v, c) = 2$$

$$d(v_1, v_2) = 1$$

$$d(c_1, c_2) = 1$$

$$D(x, y) = d(x, y)$$

$$+ \min \begin{cases} D(x-1, y-1) \\ D(x-1, y) \\ D(x, y-1) \end{cases}$$

p a t t e r n

1	8	1	2			1	2	1	2	0	1
1	7	1	2	1	2	3	0	1	0	1	2
2	6	2	1	2	2	1	1	2	3	2	2
1	4	1	4	2	0	0	2	2	1	1	
1	3	1	3	2	2	0	0	2	2	1	1
2	2	2	2	0	2	2	0	2			
0	0	0	2	2							

$$d(v, c) = 2$$

$$d(v1, v2) = 1$$

$$d(c1, c2) = 1$$

$$D(x, y) = d(x, y) + \min \begin{cases} D(x-1, y-1) \\ D(x-1, y) \\ D(x, y-1) \end{cases}$$

p p a t a r r n

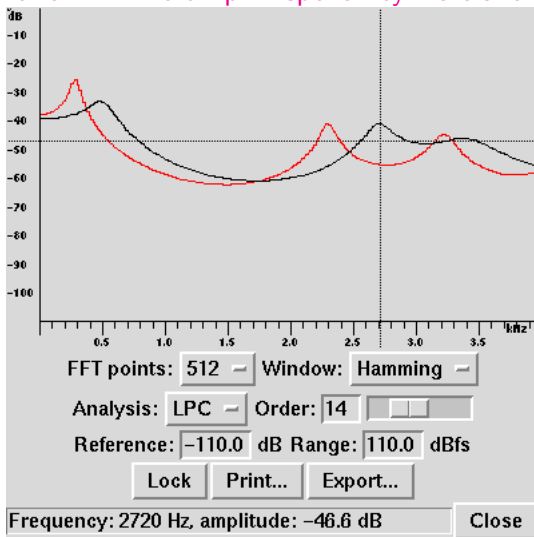
- Training: Viterbi (forced) alignment to get phoneme boundaries
- Reference template generation: average frames belonging same phoneme
- Recognition: Viterbi traceback to retrieve phoneme sequence

Why speech recognition is difficult?

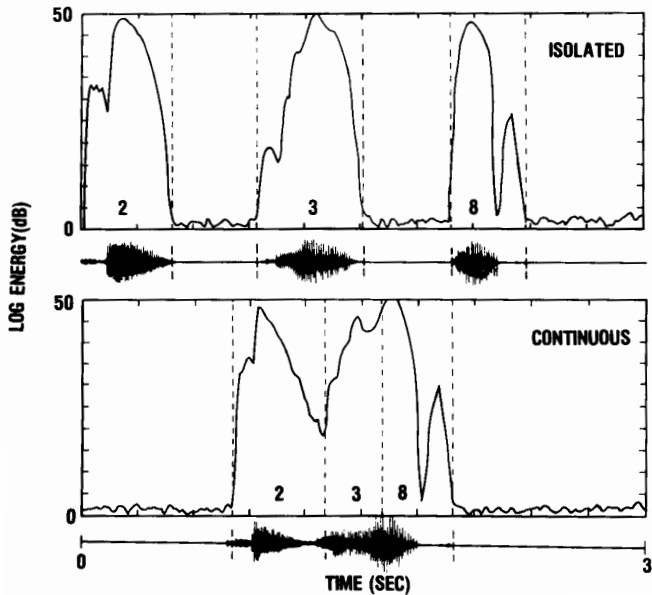
Sources of variabilities

- ▶ **Speaker specific**: physiological, emotional, cultural
- ▶ **Continuous signal**: no well defined boundaries between linguistic units
- ▶ **Ambience**: noise, Lombard effect, room acoustics
- ▶ **Channel**: additive/convolutional noise, compression
- ▶ **Transducer**: omni/uni-directional, carbon/electret mic
- ▶ **Phonetic context**

Spectra of the vowel 'i' in word "pin" spoken by male and female speakers



No well defined boundaries between linguistic units



Diversity of transduction characteristics of microphones

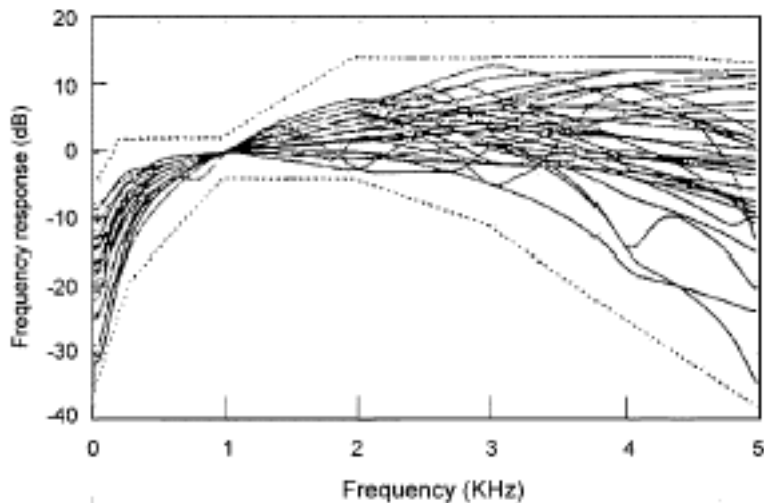
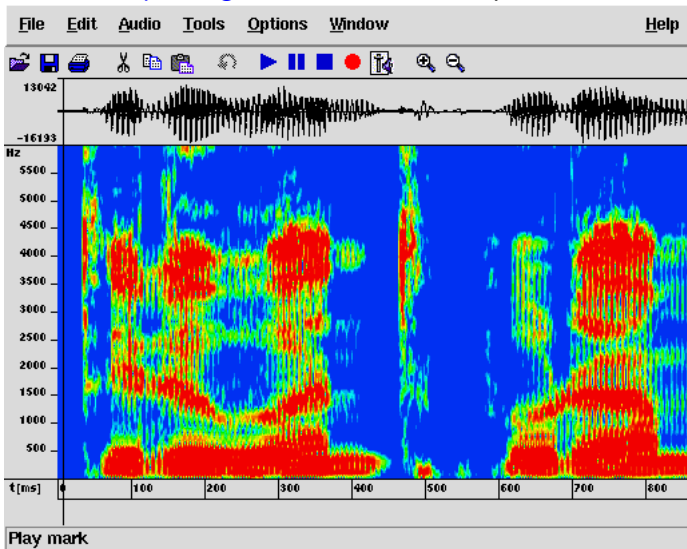


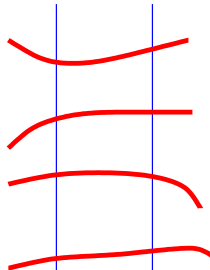
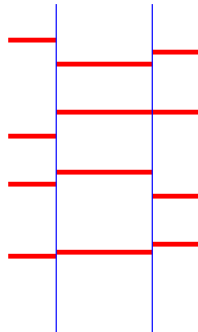
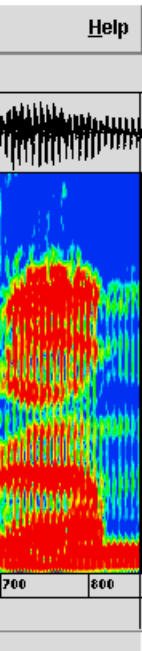
Fig. 6. Diversity of transducer characteristics in telephone set [25].

Spectrogram of thiruvananthapuram

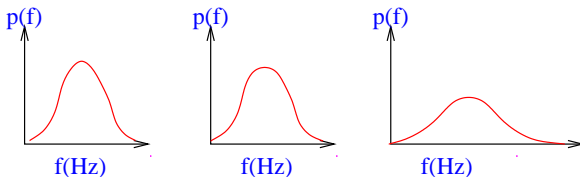
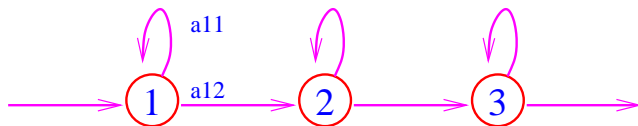
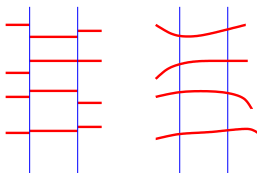


t i r u w a n t h p u r a m

Formant trajectories

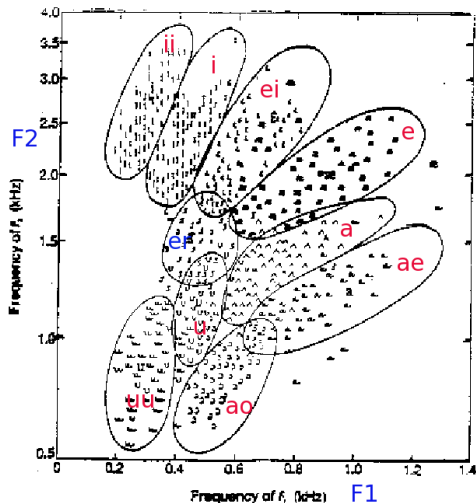


hidden Markov model (HMM)



Parameters of a HMM: A , B , π

What is hidden in hidden Markov model?



3 problems in HMM

- ▶ How to compute the likelihood of a trained model generating a test observation sequence?
Solution: forward algorithm (uses DP)
- ▶ How to find the optimal state sequence?
Solution: Viterbi algorithm (similar to DTW)
- ▶ How to estimate the parameters of the model: $\lambda = (A, B, \pi)$?
Solution: Forward-backward (Baum-Welch) algorithm

DP and HMM: Viterbi algorithm

In case of template matching (DTW), we decided on the optimal path that **minimised distance** between a test feature sequence and a reference template. The key optimisation equation was

$$D(n, m) = d(n, m) + \min \begin{cases} D(n-1, m) \\ D(n-1, m-1) \\ D(n, m-1) \end{cases}$$

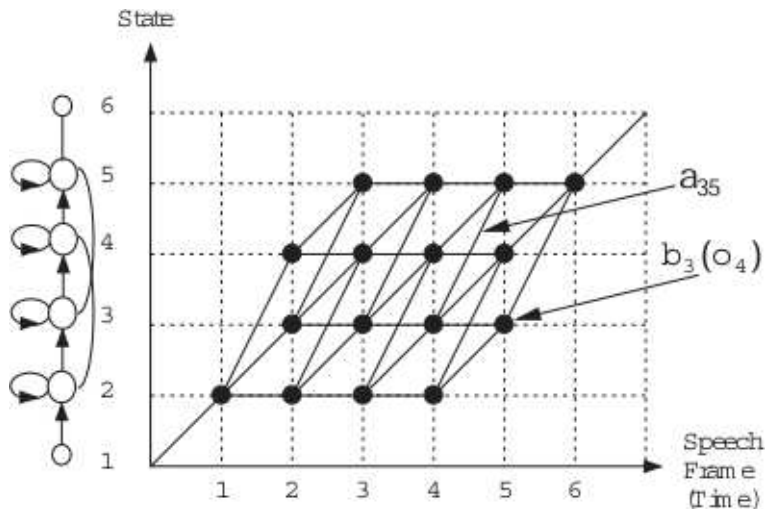
In case of a probabilistic model, we want to **maximise the probability** of a test feature sequence matching a HMM.

In the log probability domain, the DP equation for matching a test sequence with the best HMM state sequence (**Viterbi algorithm**) is

$$\psi_j(t) = \log(b_j(\mathbf{o}_t)) + \max_i \{ \psi_i(t-1) + \log(a_{ij}) \}$$

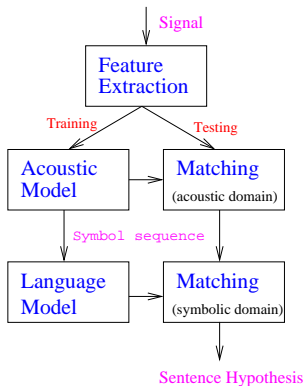
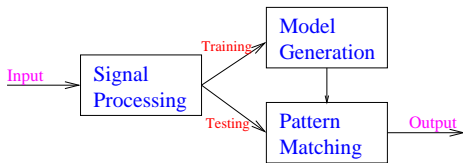
$$\text{Initial conditions: } \psi_1(1) = 0; \psi_j(1) = \log(a_{1j}) + \log(b_j(\mathbf{o}_1))$$

DP and HMM: Viterbi algorithm



source: The HTK Book

The HMM can represent even a sentence!



Recognition of a spoken sentence (a sequence of words)

Phone sequence/phone hypothesis lattice
==> Sentence hypothesis

Lexicon

man

mna

Syntax

Some man brought the apple.

Apple the brought man some.

Phone sequence/phone hypothesis lattice
==> Sentence hypothesis

Lexicon

man
mna

Syntax

Some man brought the apple.
Apple the brought man some.

Semantics

Time flies like an arrow
Fruit flies like banana

Pragmatics

Turn left for the nearest chemist

Combining Acoustic and Language Models

Let Y : Acoustic feature sequence

W : Word sequence

$$\hat{\mathbf{W}} = \underset{\mathbf{W}}{\operatorname{argmax}} P(\mathbf{W}|\mathbf{Y})$$

Combining Acoustic and Language Models

Let Y : Acoustic feature sequence

W : Word sequence

$$\hat{W} = \underset{W}{\operatorname{argmax}} P(W|Y)$$

Bayes' rule:

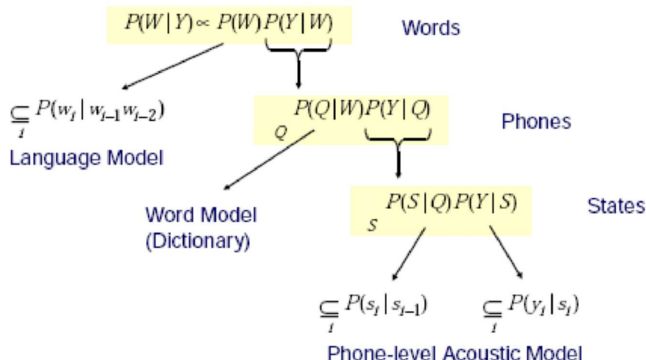
$$P(W|Y) = \frac{P(Y|W)P(W)}{P(Y)}$$

$$\hat{W} = \underset{W}{\operatorname{argmax}} \frac{P(Y|W)P(W)}{P(Y)}$$

CSR: Acoustic model, Language model and Hypothesis search

Hierarchy of Units

$$\hat{W} = \underset{W}{\operatorname{argmax}} \frac{P(Y|W)P(W)}{P(Y)}$$



"Beads on a string model"

Source: "State of the Art in ASR (and beyond)", Steve Young

Basic units of HMM (phone-like units)

अ	आ	इ	ई	उ	ऊ	ए	ऐ	ओ	औ
<i>a</i>	<i>A</i>	<i>i</i>	<i>I</i>	<i>u</i>	<i>U</i>	<i>e</i>	<i>E</i>	<i>o</i>	<i>O</i>

क	ख	ग	घ	ङ
<i>k</i>	<i>kh</i>	<i>g</i>	<i>gh</i>	<i>ng</i>
च	छ	ज	झ	ञ
<i>c</i>	<i>ch</i>	<i>j</i>	<i>jh</i>	<i>nj</i>
ट	ठ	ड	ढ	ण
<i>T</i>	<i>Th</i>	<i>D</i>	<i>Dh</i>	<i>N</i>
त	थ	द	ध	न
<i>t</i>	<i>th</i>	<i>d</i>	<i>dh</i>	<i>n</i>
प	फ	ब	भ	म
<i>p</i>	<i>ph</i>	<i>b</i>	<i>bh</i>	<i>m</i>

य	र	ल	व	श	ष	स	ह
<i>y</i>	<i>r</i>	<i>l</i>	<i>w</i>	<i>sh</i>	<i>S</i>	<i>s</i>	<i>h</i>

Pronunciation dictionary

- * Representing a word as a sequence of units of recognition
- * Pronunciation rules can be used
- * Manual verification is necessary

kalam vs kamal

karnaa, pahale, Bhaartiya

pause

aage aa g e

aa ja aa j

aba a b

abbaasa a bb aa s

aatxha aa t'h

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Multiple pronunciations

vij~nAna v i j n aa n

vij~nAna(2) v i g y aa n

Examples of pronunciation variability

Feature spreading in coalescence:

c ae n t — > c ae t where ae is nasalised

Assimilation causing changes in place of articulation:

n — > m before labial stop as in input, can be, grampa

Asynchronous articulation errors causing stop insertions:

warm[p]th, ten[t]th, on[t]ce, leng[k]th

Fast speech:

probably — > probly

r-insertion in vowel-vowel transitions:

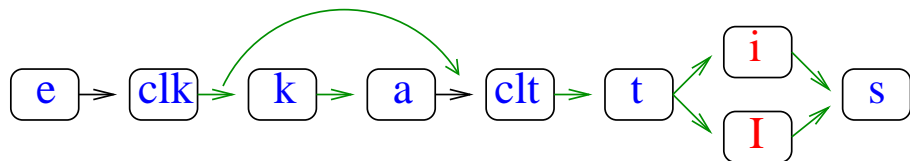
stir [r]up, director [r]of

Context dependent deletion:

nex[t] week

Source: "State of the Art in ASR (and beyond)", Steve Young

phone HMM \rightarrow word HMM \rightarrow sentence HMM



e clk k a clt t I s
e clk k a clt t i s

e clk clt t I s
e clk clt t i s

- * "probabilities" of pronunciations can be estimated
- * many pronunciations \rightarrow higher word confusions
 \rightarrow performance degradation
- * Dialect and Accent (native/non-native speakers)
- * seek a dynamic speaker specific pron dictionary.

Training subword HMMs

An iterative algorithm (Baum-Welch, also known as Forward-Backward) is used. The Maximum Likelihood approach guarantees increase of the likelihood of the trained model matching with training data with each iteration. To begin with, an initial estimation of parameters of HMMs (A, B, π) is required.

Q: How to get an initial estimation of ($\lambda = \{A, B, \pi\}$)?

A: We can estimate parameters if we know the boundaries of every subword HMM in training utterances.

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A: We can estimate parameters if we know the boundaries of every subword HMM in training utterances.

Practical solution: Assume that the durations of all units (phones) are equal. If there are N phones in a training utterance, divide the feature vector sequence into N equal parts. Assign each part, to a phoneme in the phoneme sequence corresponding to the transcription of the utterance. Repeat for all training utterances.

Initial estimation of HMM parameters: an illustration

Let the transcription of the 1st wave file be the following sequence of words: mera bhaarat mahaan

Let the relevant lines in the dictionary be as follows:

bhaarata bh aa r a t

mahaana m a h aa n

mera m e r aa

The phonemeHMM sequence (of length 16) corresponding to this sentence is sil m e r aa bh aa r a t m a h aa n sil

Initial estimation of HMM parameters: an illustration

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```
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mahaana   m a h aa n
mera      m e r aa
```

The phonemeHMM sequence (of length 16) corresponding to this sentence is sil m e r aa bh aa r a t m a h aa n sil

If the duration of the wavefile is 1.0sec, there will 98 feature vectors (frame shift = 10msec and frame size = 25msec).

Assign the first 6 feature vectors to “sil” HMM; the next 6 (7 through 12) to “m”; the next 6 (13 through 18) to “e”; ... ; the last 8 feature vectors to “sil”. If HMM has 3 states, assign 2 feature vector to each state; compute mean,SD.

Assume $a_{i,j}=0.5$ if $j=i$ or $j=i+1$; else assign 0.

Decoding: Generation of word hypotheses

Generation of word hypotheses can result in

- * a single sequence of words,
- * in a collection of the n-best word sequences,
- * in a lattice of partially overlapping word hypotheses.

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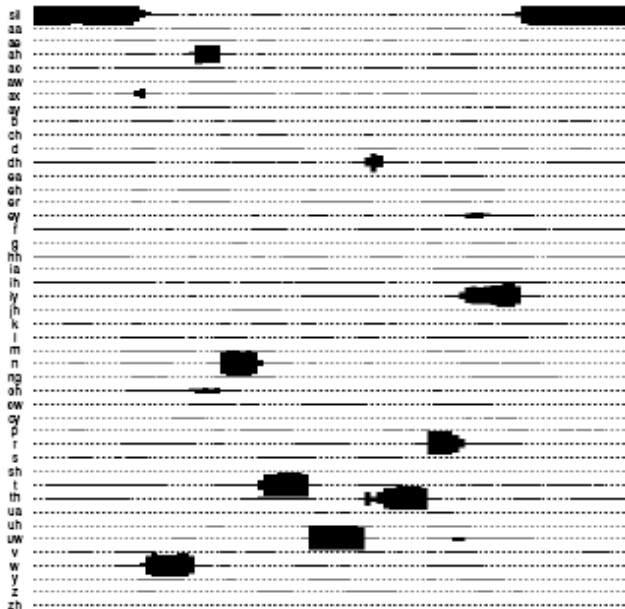
- * a single sequence of words,
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- * in a lattice of partially overlapping word hypotheses.

Goal: Find the path with the least cost (most likely word sequence)

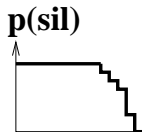
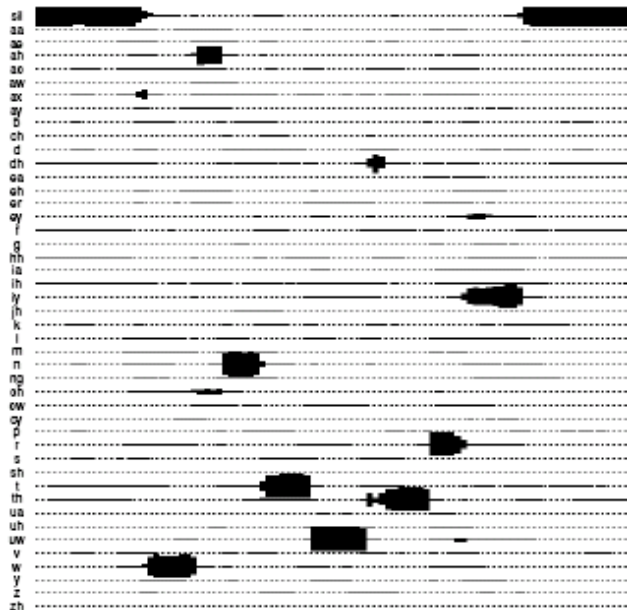
Acoustic evidence \rightarrow Word lattice \rightarrow DAG

Given a graph with N nodes and E edges, the least-cost path can be found in time proportional to $N+E$

Probabilities of phones at various time instants



Probabilities of phones at various time instants



sil **ah**



w **n**

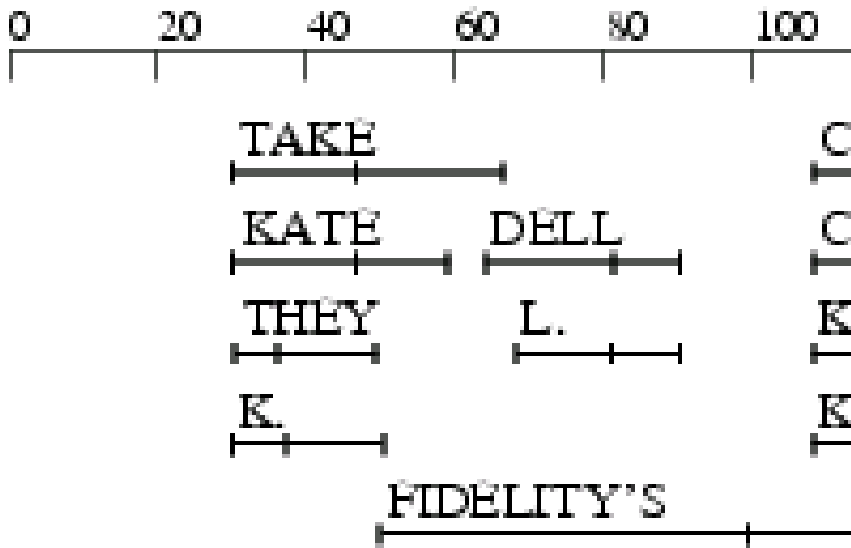
ax **oh**



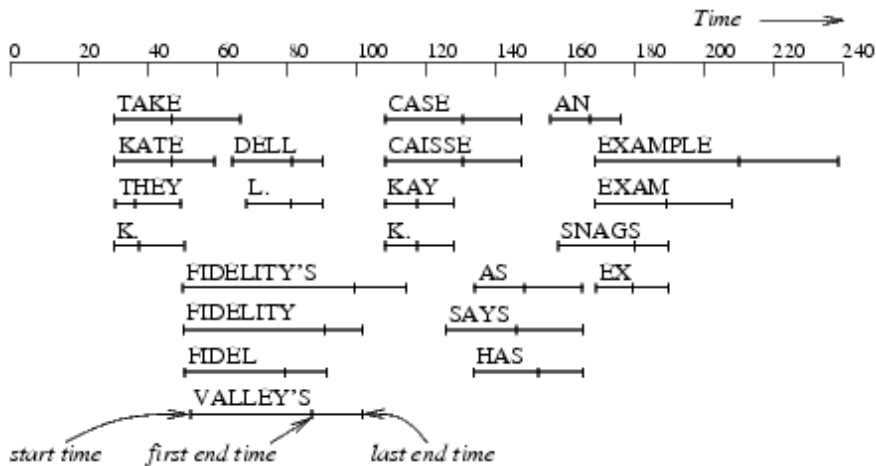
one



Lattice of phone hypotheses → lattice of word hypotheses



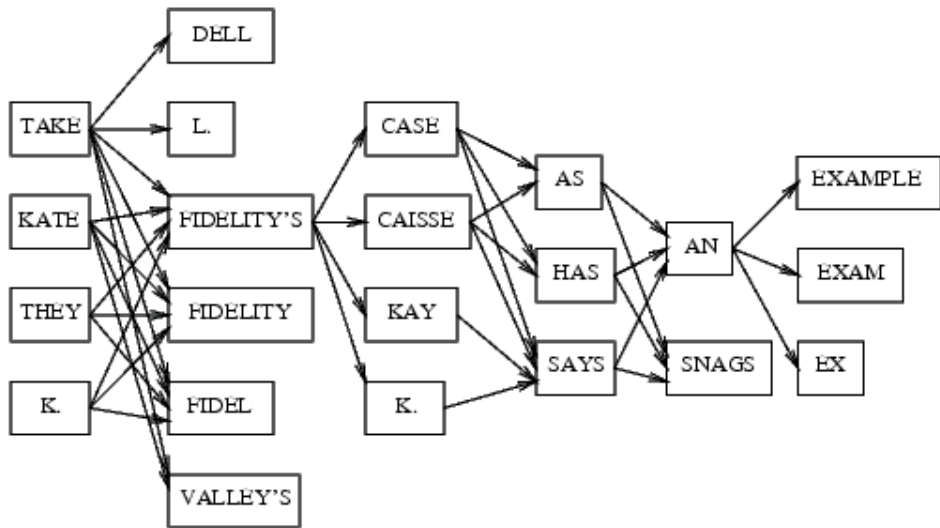
Word hypotheses at various time instants



Take Fidelity's case as an example

Source: "Efficient algorithms for Speech Recognition", M.K.Ravishankar, PhD thesis: CMU-CS-96-143

Word Lattice as a Directed Acyclic Graph



Incorporation of syntax

Backus-Naur Form (BNF) grammar is useful for ASR in a specific task domain.

[क्या] **Trainname** (का | मे) [**Digit**] (रिजर्वेशन
| **Class** का टिकट) **Aaj** के लिए **Milegaa** [क्या]?;

Integration of syntax, semantics and domain knowledge

Probability of a word sequence

Let \mathbf{W} denote the word sequence w_1, w_2, \dots, w_i .

$$p(\mathbf{W}) = p(w_1) \times p(w_2 | w_1) \times p(w_3 | w_1, w_2) \times \dots \times p(w_i | w_{i-1}, w_{i-2}, \dots, w_1)$$

Not practical due to 'unlimited history':
too many parameters for even a short \mathbf{W}

Markovian assumption:

- ▶ Disregard 'very old' history (short memory)
- ▶ remember only 'n-1' previous words: **n-gram** model

Parameter Estimation

Maximum Likelihood Estimation: relative frequencies
Use counts from training data.

unigram:

$$p(w) = C(w)/|V|$$

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n-gram:

$$p(w_n|w_1 w_2 \cdots w_{n-1}) = \frac{C(w_1, w_2, \cdots, w_{n-1}, w_n)}{C(w_1, w_2, \cdots, w_{n-1})}$$

Data sparsity \Rightarrow Smoothing of probability distributions

Example: 1000 word vocabulary corpus divided into training set of size 1,500,000 words and test set of size 300,000 words.

Observation: 23% of the trigrams occurring in test data never occurred in the training subset!

Similar observation with a 38 million word newspaper corpus.

Robust parameter estimation is needed

Eliminating Zero Probabilities

From the same training data, derive revised n-grams such that no n-gram is zero.

Discounting: Take away some counts from 'high count words' and distribute them among 'zero/low count words'.

Good-Turing Discounting

Let N_c denote the number of bigrams that occurred c times in the corpus.

For bigrams that **never** occurred, the revised count is

$$c^* = \frac{N_1}{N_0}$$

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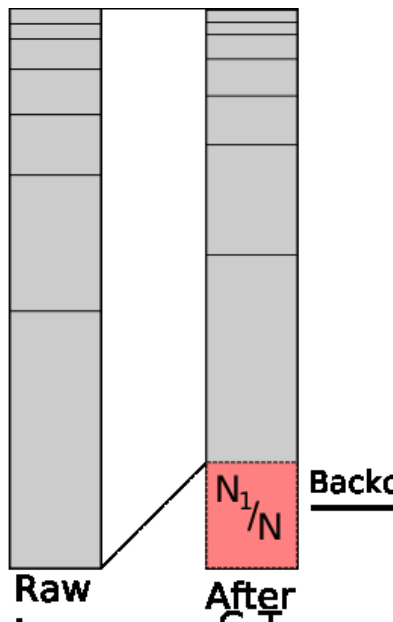
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In general,

$$c^* = (c + 1) \frac{N_{c+1}}{N_c}$$

- * Proper normalization is needed.
- * Suitable for estimation from large data.

Good-Turing Discounting: Illustration



Using n-gram 'hierarchy': Combining frequencies

Linear interpolation of n-grams

$$\hat{p}(w_3|w_1, w_2) = \lambda_1 p(w_3|w_1, w_2) + \lambda_2 p(w_3|w_2) + \lambda_3 p(w_3)$$

with $\lambda_i > 0$; $\sum_i \lambda_i = 1.0$

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with $\lambda_i > 0$; $\sum_i \lambda_i = 1.0$

Backoff trigram

if trigram count > 0 no interpolation

Backoff to bigram otherwise

We “backoff” to a lower order n-gram only if we have zero evidence for a higher order n-gram.

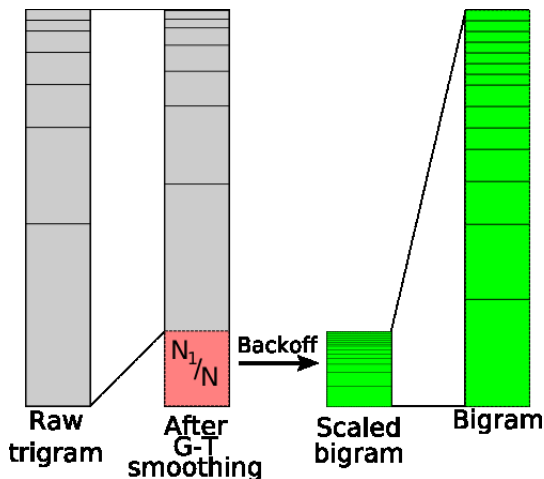
A non-linear method of combining counts.

The backoff trigram grammer is computed as

```
if (trigramCount(xyz)) > 0) {  
    // compute trigramProb(z|xy)  
else if (bigramCount(yz)) > 0){  
    trigramProb = a1(xy) * bigramProb(z|y)  
} else {  
    trigramProb = a2(y) * unigramProb(z)  
}
```

a_1 and a_2 are positive scale factors that can even be > 1 (for a lucid explanation, see <http://www.speech.cs.cmu.edu/sphinxman/FAQ.html>).

Backoff trigram grammar with Good-Turing Discounting



[http://www.inf.ed.ac.uk/teaching/courses/fnlp/lectures/9/index.html.xml#\(4\)](http://www.inf.ed.ac.uk/teaching/courses/fnlp/lectures/9/index.html.xml#(4))

Requirements for Implementation of an ASR system

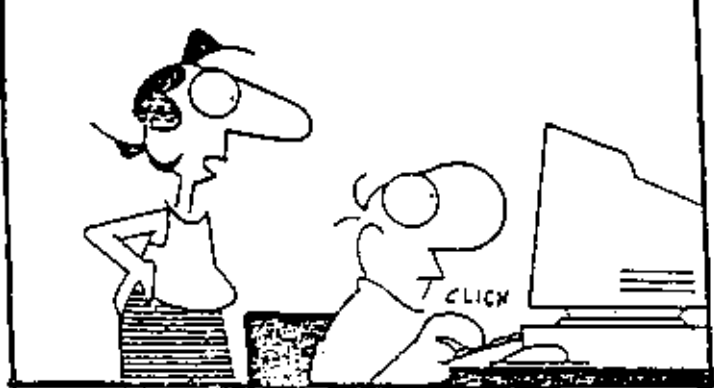
- ▶ Knowledge of spoken language recognition
- ▶ ASR toolkit
- ▶ Speech data
- ▶ Transcription (sequence of 'words' in an utterance)
- ▶ Pronunciation dictionary
- ▶ Language model (can be generated automatically)
- ▶ Knowledge of shell scripts and perl helps
- ▶ Lots of patience and perseverance

A Short list of Relevant Books

1. "Speech Communications : Human and Machine", D. O'Shaughnessy University press, Hyderabad; price: Rs. 575.
2. "Fundamentals of Speech Recognition", by Lawrence R. Rabiner, B. H. Juang and B.Yegnanarayana, Pearson Education India, 2008, Rs. 450; ISBN:9788177585605
3. "Statistical Methods for Speech Recognition", Frederick Jelinek, The MIT Press, 1997.
4. "Spoken Language Processing : A Guide to Theory, Algorithm and System Development", by Xuedong Huang, Alex Acero, Hsiao-Wuen Hon Year 2001, Prentice Hall PTR; ISBN: 0130226165; Price: \$91.
5. "Speech and Language Processing: An Introduction to Natural Language Processing, Computational Linguistics, and Speech Recognition", By Daniel Jurafsky and J.H.Martin, ISBN 8178085941 Pearson Education Asia, 2000. Price Rs. 425
6. "Spoken Language Understanding — An Introduction to the Statistical Framework" Y. Wang, L. Deng, and A. Acero, In IEEE Signal Processing Magazine, Vol 27 No. 5. Sepetmber 2005.

More links at <http://speech.tifr.res.in/>





"What good is a faster computer, faster modem and faster printer if you're still using the same old slow fingers?"

Times of India, 19-OCT-1998