

Introduction to Causal Directed Acyclic Graphs

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S-SPIRE Works in Progress
January 28, 2019

Overview

- What are DAGs & why do we need them?
- DAG rules & conventions
- How to construct a DAG
 - Which variables should be included?
 - How to determine covariates for adjustment?
- Examples: manual + DAG online tool
- **Build your own DAG**



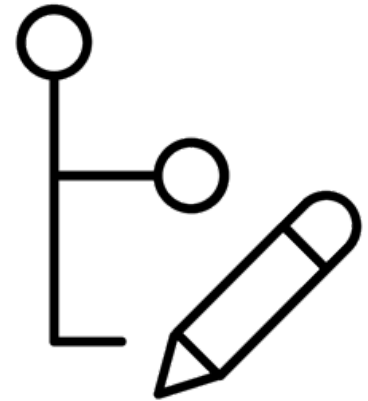
Observational Health Services Research

- Big HSR datasets are observational
 - Medicare
 - HCUP: NIS, NEDS, NRD, SIDs
 - Truven, Optum
 - EMR: STARR
 - Clinical Registries: NSQIP, VQI
- Observational comparative effectiveness ¹
 - Treatments not assigned, determined by mechanisms of routine practice
 - Actual mechanisms are often unknown
 - However researchers can (and should) speculate on the treatment assignment process or mechanism
- Problem: correlation \neq causation

¹ 2013 AHRQ *Developing a protocol for observational comparative effectiveness research: a user's guide*

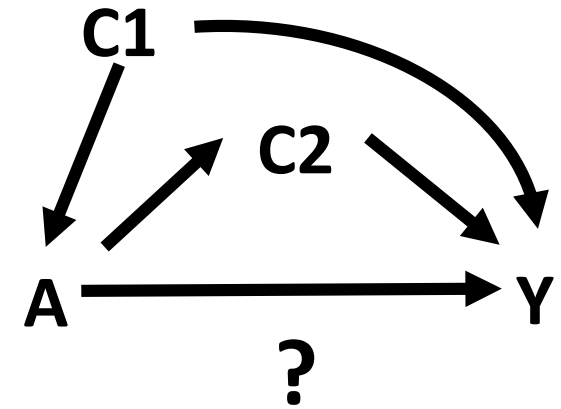
Causal Graphs: Helpful Tools

1. Illustrate sources of bias
2. Determine whether the effect of interest can be identified from available data
3. Causal graphs are based on assumptions (but so are analytic models)



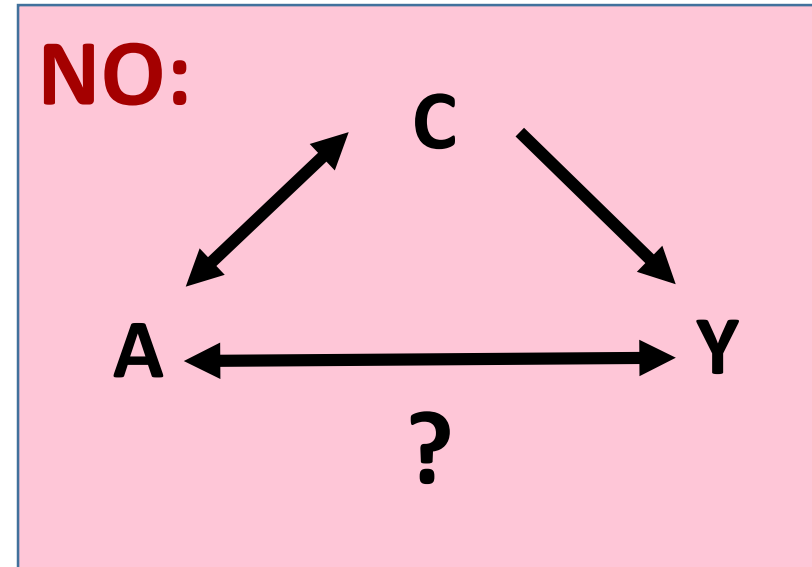
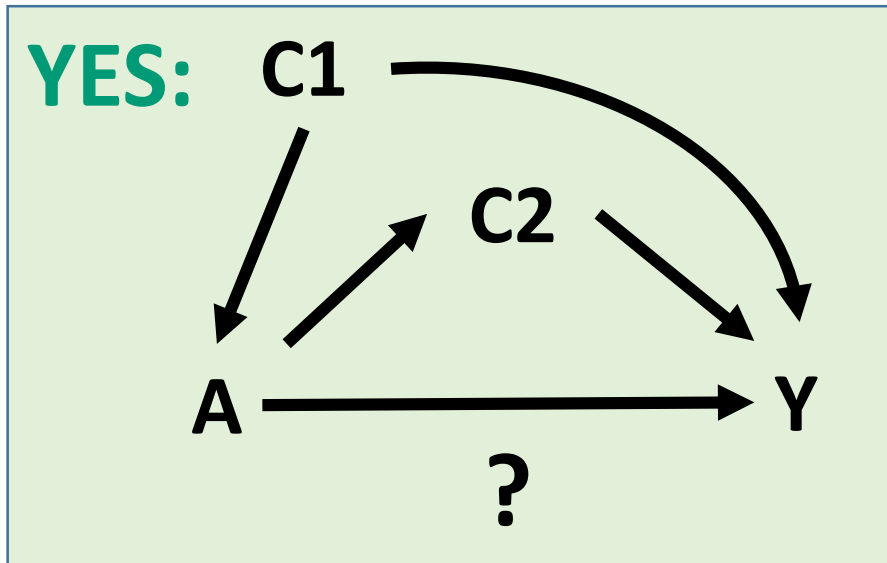
What are Directed Acyclic Graphs?

- Computer science: data structure
- Markov models: visualization
- Epidemiology: Causal DAGs are systematic representation of causal relationships
- Useful tools to represent assumptions & known relationships
 - plan analytic approach
 - reduce bias



Directed & Acyclic

- Directed: point from cause to effect
 - Causal effects cannot be bidirectional
- Acyclic: no directed path can form a closed loop



Why do we need DAGs?

- Clarify study question & relevant concepts
- Explicitly identify assumptions
- Reduce bias
 - Separate individual effects
 - Ascertain appropriate covariates for statistical analysis
- Estimate required analysis time



 We can assist with DAG creation and covariate assessment

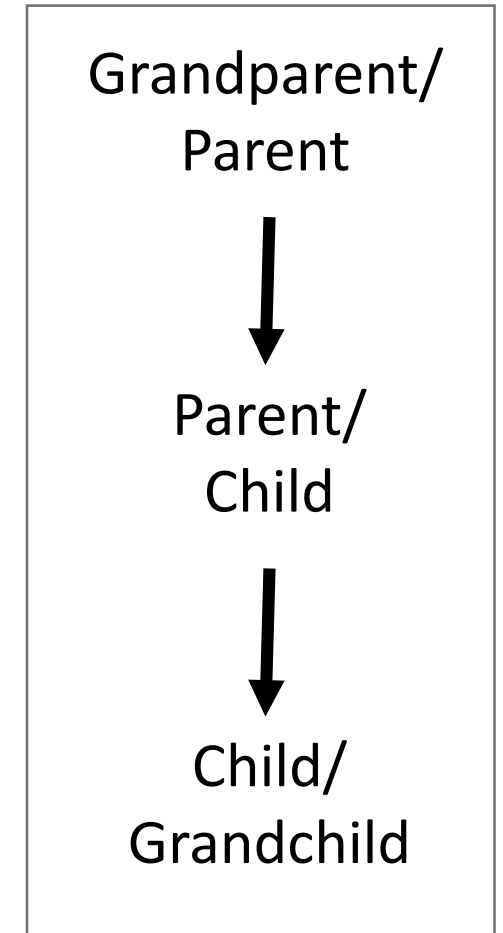
DAG Rules



- All common causes are represented
- No arrow = no causal effect
- Time flows left to right
 - A (or E) = Exposure / Treatment / Intervention / Primary IV
 - Y (or D) = Outcome
 - C = Covariates / Confounders
 - U = Unmeasured relevant variables
- Confounders can be grouped for notation

Glossary – Genealogy

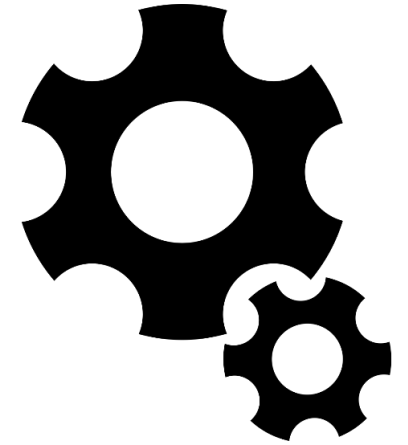
- **Parent:** a direct cause of a particular variable
- **Ancestor:** a direct cause (i.e. parent) or indirect cause (e.g. grandparent) of a particular variable
- **Child:** the direct effect of a particular variable, i.e. the child is a direct effect of the parent
- **Descendant:** a direct effect (i.e. child) or indirect effect (e.g. grandchild) of a particular variable
- **Common Cause:** a covariate that is an ancestor of two other covariates



How to Construct a DAG: Variables to Include

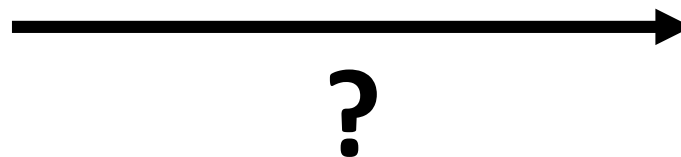
How to construct a DAG

Step 1: Articulate the research question



- Start the DAG with your:
 - A / treatment / exposure / primary IV (cause)
 - Y / dependent variable / endpoint / outcome (effect)
- Indicate the research question with a “?”

Exposure / Treatment
“Cause”
A

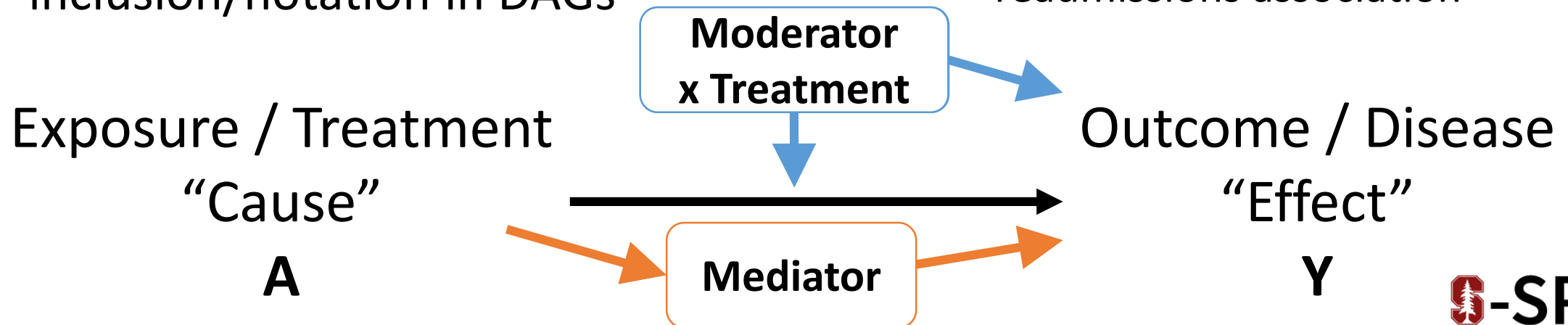


Outcome / Disease
“Effect”
Y

How to construct a DAG

Step 2: Consider important variables embedded in the question

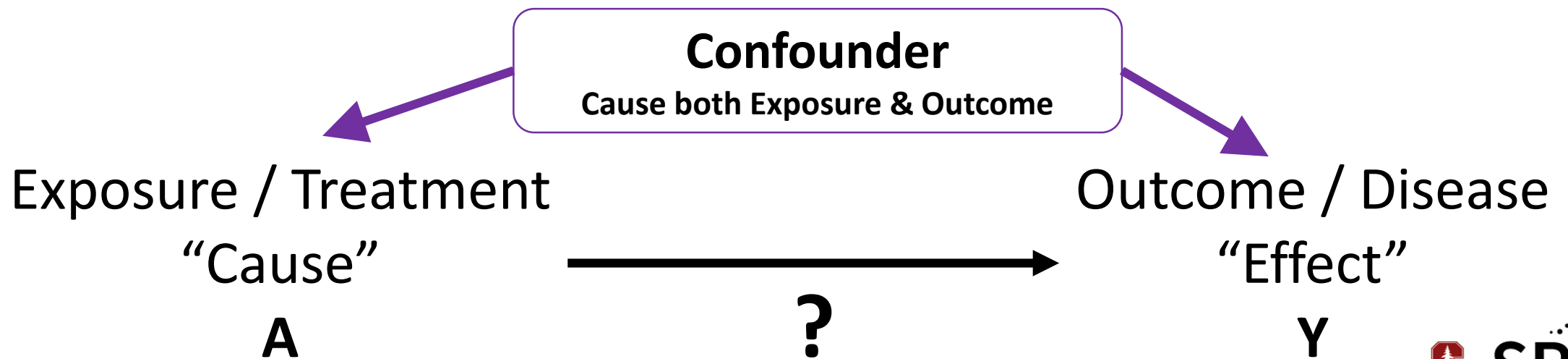
- **Moderator**: affects the direction and/or strength of the relation between A & Y (AKA effect modifier, statistical interaction)
 - e.g. **gender** differences in surgical history-opioid relationship
- Some disagreement on inclusion/notation in DAGs ²
- **Mediator**: a variable within the causal pathway between the treatment and outcome. Treatment (A) influences the mediator, which in turn influences the outcome.
 - e.g. **complications** in frailty-readmissions association



How to construct a DAG

Step 3: Consider confounding variables

- Variables that **confound** the relationship you are evaluating
- Confounders are causes of both the treatment (A) & the outcome
 - e.g. **age, gender, race, insurance**
- Add confounders to DAG, considering causal mechanism



How to construct a DAG

Step 4: Consider other relevant variables

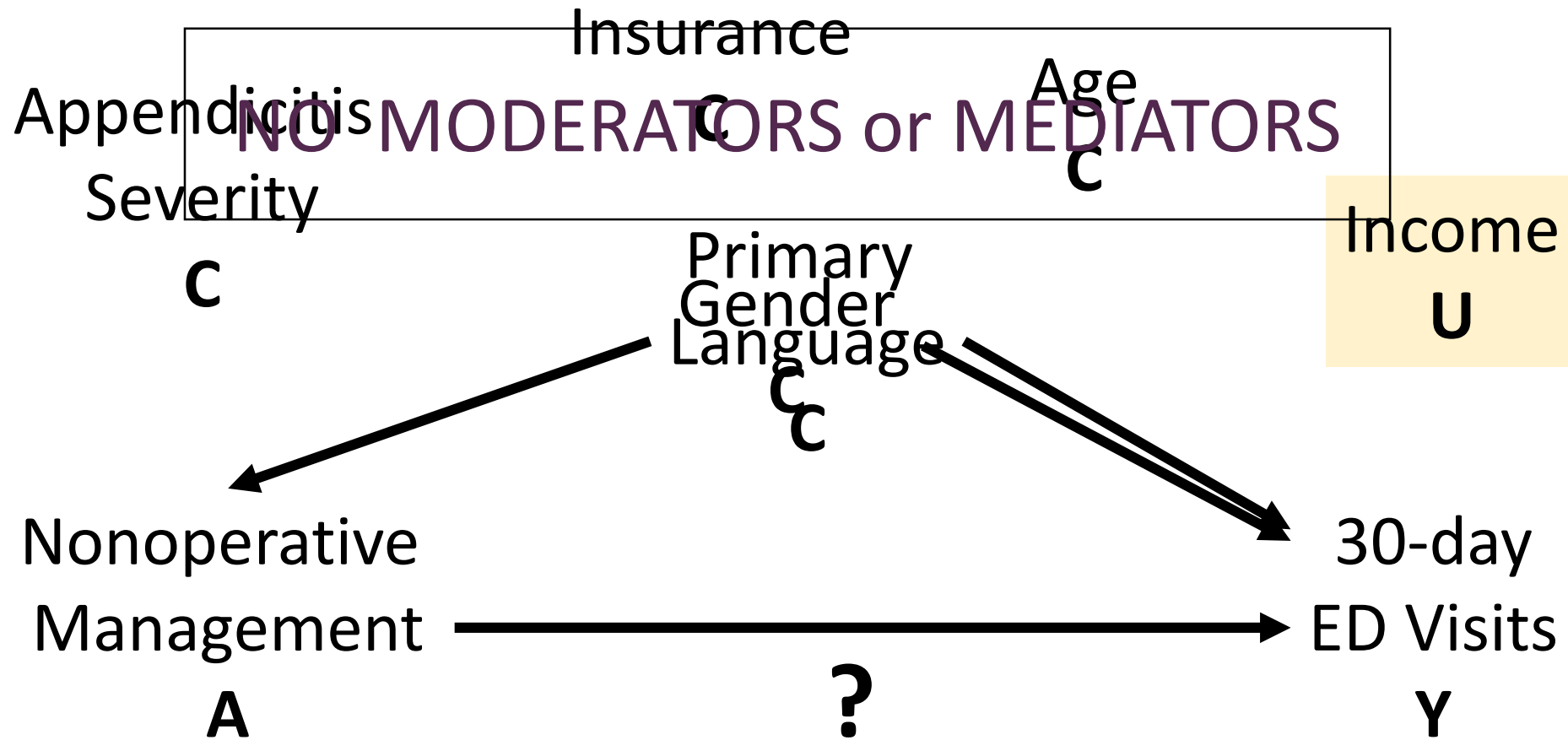
Which Variables Should be Included?

- All common causes of any 2 variables in the DAG
- Unmeasured (and unmeasurable) common causes
- Selection variables, i.e. inclusion criteria

Not Required in Causal DAGs:

- Variables that cause Y but not A
 - May be included if desired, e.g. for comparison to other studies which adjusted for the variable

Example: Uncomplicated Appendicitis³



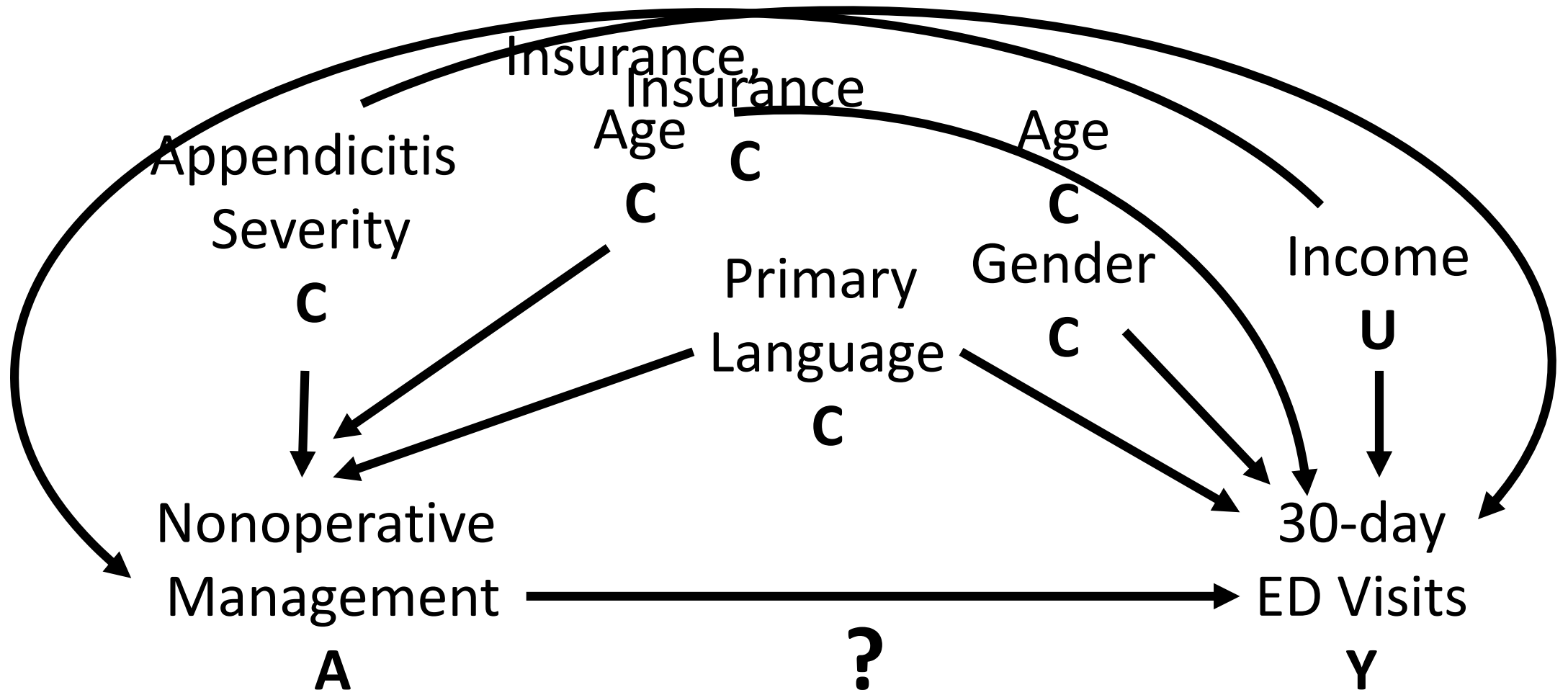
Step 1:
Research Q

Step 2:
Med/Mods

Step 3:
Confounds

Step 4:
Others

Example: Uncomplicated Appendicitis³



Keep in mind

- Assumptions must be made
- Every analysis has built-in assumptions
- DAGs make them explicit, represent *your* model of relationships between variables
- Often more than 1 appropriate DAG
- Alternate DAGs can make excellent sensitivity analyses



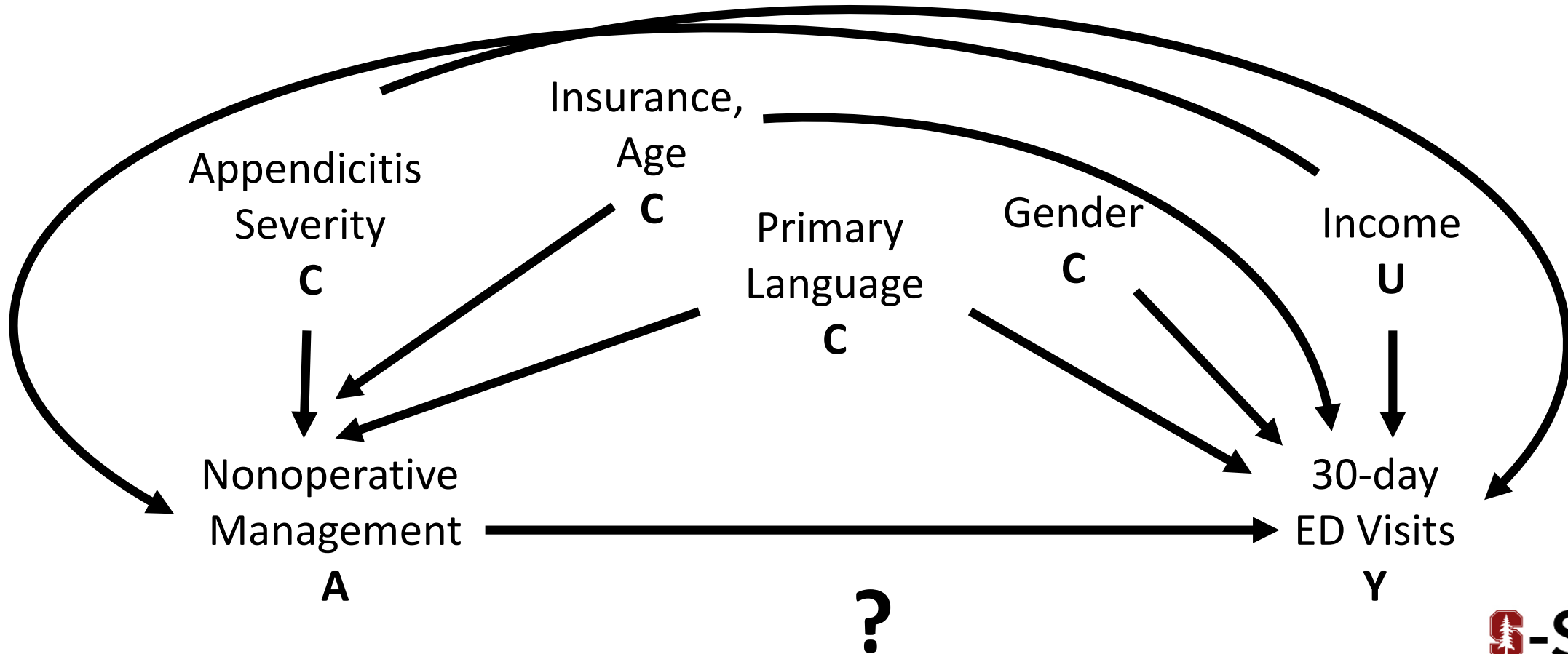
How to Construct a DAG: Determine Covariates for Adjustment

Glossary – Causes, Effects, Associations

- **Back Door Path:** a connection between A & Y that does not follow the path of the arrows.
- **Common Effect** (also known as **Collider**): a covariate that is a descendant of two other covariates. The term collider is used because the two arrows from the parents "collide" at the descendant node.
- **Conditioning:** Conditioning on a variable means using either sample restriction, stratification, adjustment or matching to examine the association of A & Y within levels of the conditioned variable.
 - Other terms "adjusting" or "controlling" suggest a misleading interpretation of the statistical model. ⁴

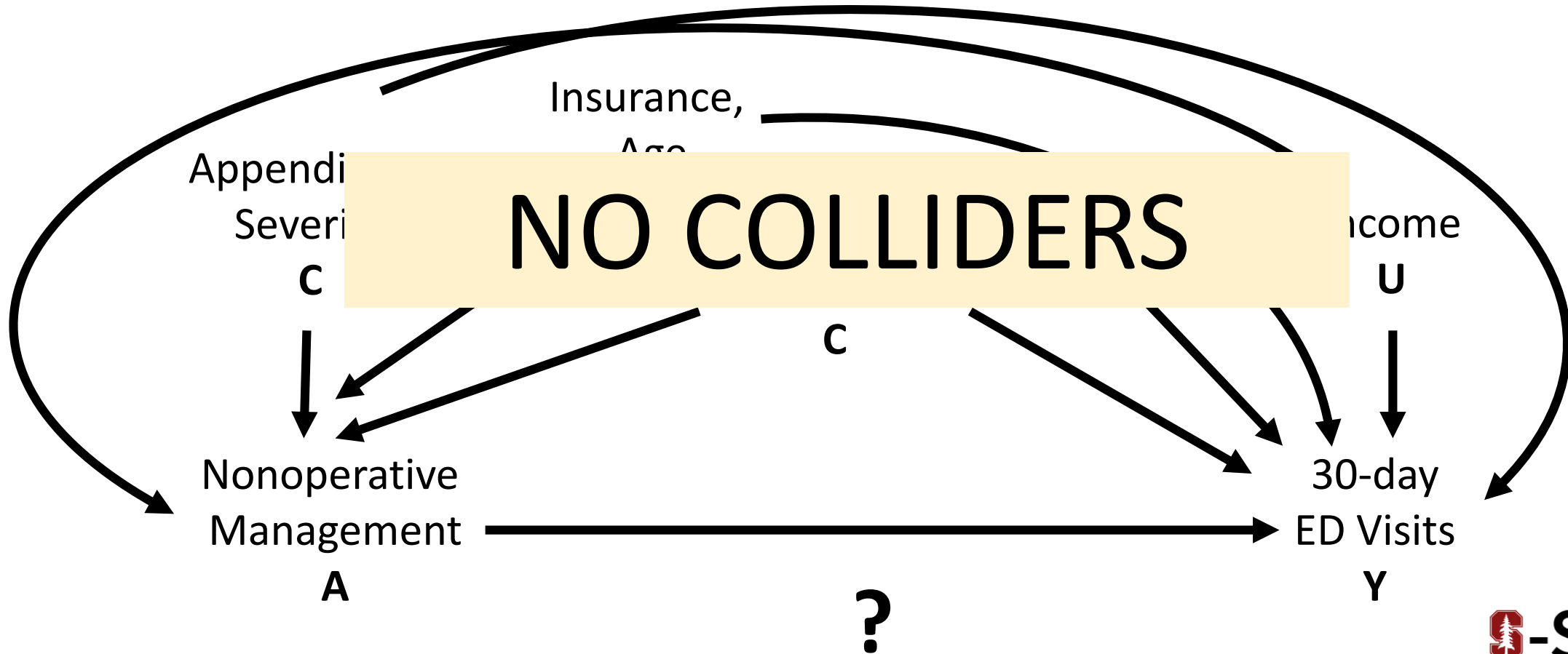
Back Door Path

- A connection between A & Y that does not follow the path of the arrows.
- Open back door path → confounding bias, i.e. association b/t A & Y ≠ causal effect



Common Effect or Collider

- A covariate descendant of two other covariates.
- Two arrows from the parents "collide" at the descendant node.



Conditioning

Conditioning can mean:

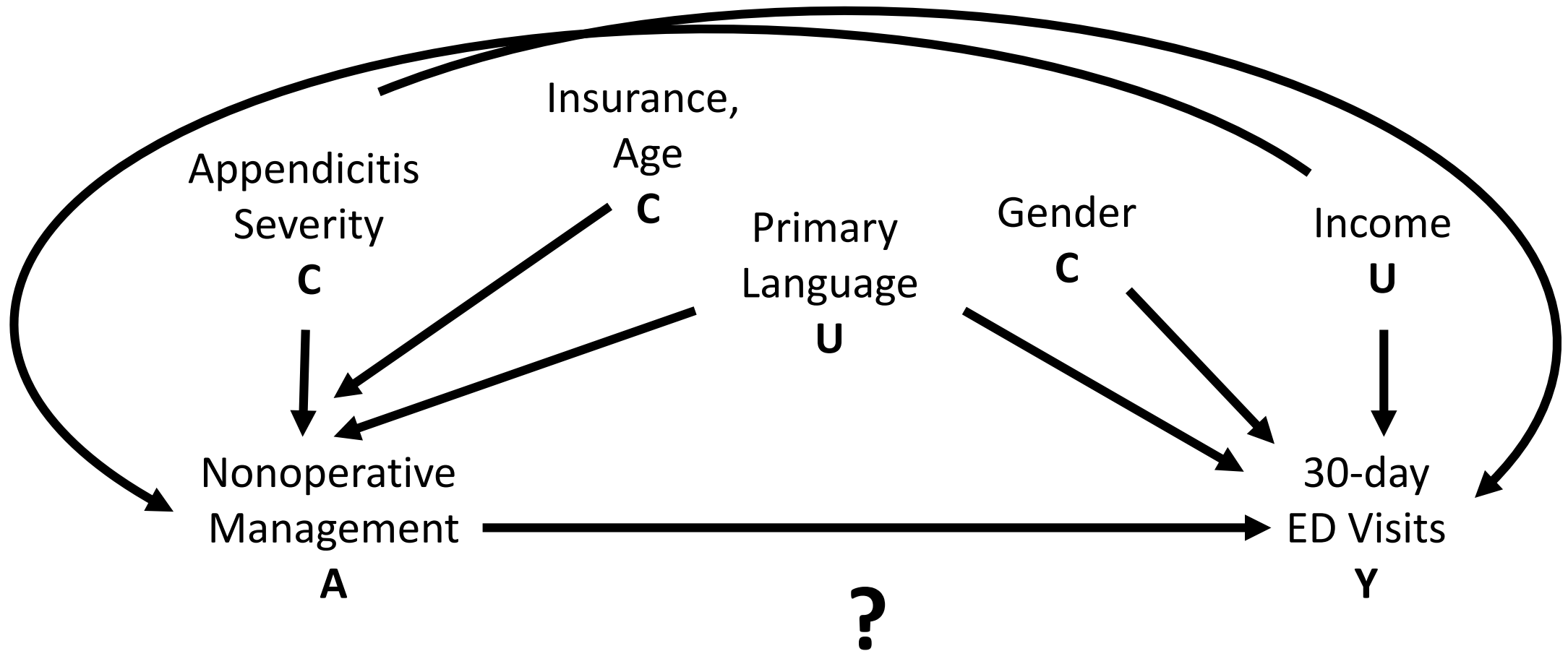
- adjusting, restricting, stratifying, matching

Draw a box around the conditioned variables

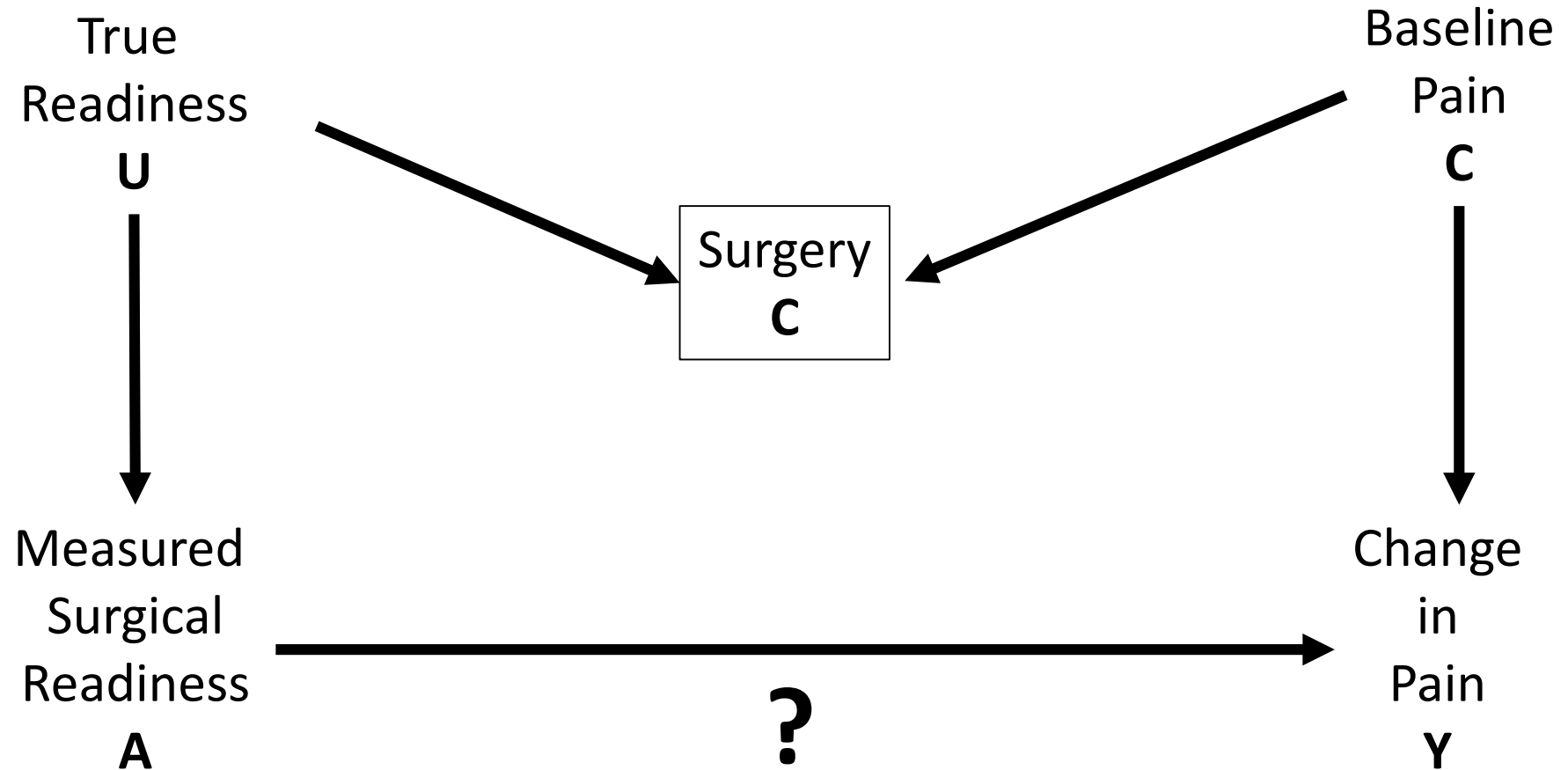
1. Conditioning on a variable in an open backdoor path removes the non-causal association (i.e. controls for confounding)
2. Conditioning on a collider opens the path that the collider was blocking
3. Conditioning on a variable in the causal pathway (mediator) removes part of the causal effect

Conditioning

Remaining potential confounding due to unmeasured language & income



Collider Bias Example: Surgery for Low Back Pain



Glossary – Structural Approach to Bias

- **Confounding bias:** common cause of A & Y that is not "blocked" by conditioning on other specific covariates
- **Collider bias:** general phenomenon involving conditioning on common effects.
- **Selection bias:** a particular type of collider bias in which the common effect is selection into the study; occurs when a common effect is conditioned such that there is now a conditional association between A & Y (e.g. Berkson's Bias, loss to f/u, missing data, healthy worker bias)
- **Berkson's bias:** a particular type of selection bias in which selection of cases into the study depends on hospitalization, and the treatment is another disease, or a cause of another disease, which also results in hospitalization ⁵

Online Tool ⁶ www.dagitty.net

Save your [code!](#)
(.docx or .txt)

Diagram style

- classic
- SEM-like

View mode

- normal
- moral graph
- correlation graph

Coloring

- causal paths
- biasing paths
- ancestral structure

Effect analysis

- atomic direct effects

Legend

- ▶ exposure
- I outcome
- ancestor of exposure
- ancestor of outcome
- ancestor of exposure and outcome
- adjusted variable
- unobserved (latent)

Model | **Examples** | **How to ...** | **Layout** | **Help**

Causal effect identification

Adjustment (total effect) ▾

Minimal sufficient adjustment sets containing C: Appendicitis Severity, C: Insurance, Age, C: Gender for estimating the total effect of A: nonop mgmt on Y: ED visits:

- **C: Appendicitis Severity, C: Insurance, Age, C: Gender, U: Income, U: Primary Language**

Testable implications

The model implies the following conditional independences:

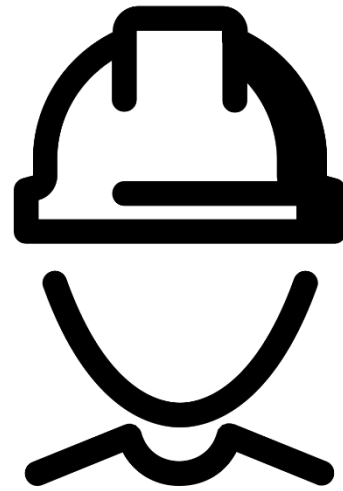
- A: nonop mgmt ⊥ C: Gender
- C: Appendicitis Severity ⊥ C: Insurance, Age
- C: Appendicitis Severity ⊥ C: Gender
- C: Appendicitis Severity ⊥ U: Income
- C: Appendicitis Severity ⊥ U: Primary Language
- C: Insurance, Age ⊥ C: Gender
- C: Insurance, Age ⊥ U: Income
- C: Insurance, Age ⊥ U: Primary Language

Summary: AHRQ CER User's Guide ⁷

Guidance	Key Considerations
Develop a simplified DAG to illustrate concerns about bias.	<ul style="list-style-type: none">• Use a DAG to illustrate and communicate known sources of bias, such as important well known confounders and causes of selection bias.
Develop complete DAG(s) to identify a minimal set of covariates.	<ul style="list-style-type: none">• Construction of DAGs should not be limited to measured variables from available data; they must be constructed independent of available data.• The most important aspect of constructing a causal DAG is to include on the DAG any common cause of any other 2 variables on the DAG.• Variables that only causally influence 1 other variable (exogenous variables) may be included or omitted from the DAG, but common causes must be included for the DAG to be considered causal.• Identify a minimal set of covariates that blocks all backdoor paths and does not inadvertently open closed pathways by conditioning on colliders or descendants.

*Sauer, VanderWeele. "Supplement 2: Use of directed acyclic graphs." (2013).

Questions?



Build your own DAG!

References

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Additional Resources

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2. Williams TC, Bach CC, Matthiesen NB, Henriksen TB, Gagliardi L. Directed acyclic graphs: a tool for causal studies in paediatrics. *Pediatric research*. 2018 Jun 4.
3. Suttorp MM, Siegerink B, Jager KJ, Zoccali C, Dekker FW. Graphical presentation of confounding in directed acyclic graphs. *Nephrology Dialysis Transplantation*. 2014 Oct 16;30(9):1418-23.
4. Baron RM, Kenny DA. The moderator–mediator variable distinction in social psychological research: Conceptual, strategic, and statistical considerations. *Journal of personality and social psychology*. 1986 Dec;51(6):1173.