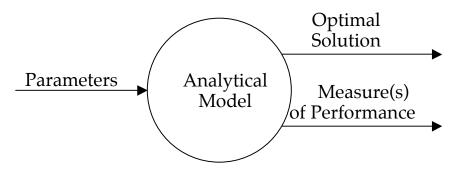
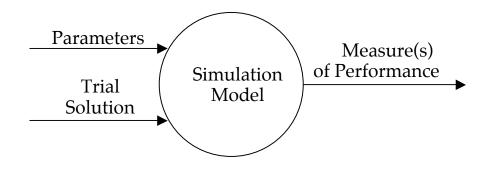
### **Introduction to Simulation**

### **Analytical Models:**



Simulation Models:



Advantages:

Disadvantages:

# **Monte-Carlo Simulation with Crystal Ball**<sup>®</sup>

To run a simulation using Crystal Ball<sup>®</sup>:

#### 1. Setup Spreadsheet

Build a spreadsheet that will calculate the performance measure (e.g., profit) in terms of the inputs (random or not). For random inputs, just enter any number.

#### 2. Define Assumptions—i.e., random variables

Define which cells are random, and what distribution they should follow.

#### 3. Define Forecast—i.e., output or performance measure

Define which cell(s) you are interested in forecasting (typically the performance measure, e.g., profit).

### 4. Choose Number of Trials

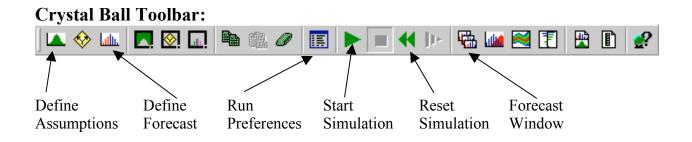
Select the number of trials. If you would later like to generate the Sensitivity Analysis chart, choose "Sensitivity Analysis" under Options in Run Preferences.

### 5. Run Simulation

Run the simulation. If you would like to change parameters and re-run the simulation, you should "reset" the simulation (click on the "Reset Simulation" button on the toolbar or in the Run menu) first.

### 6. View Results

The forecast window showing the results of the simulation appears automatically after (or during) the simulation. Many different results are available (frequency chart, cumulative chart, statistics, percentiles, sensitivity analysis, and trend chart). The results can be copied into the worksheet.



In August, Walton Bookstore must decide how many of next year's nature calendars to order. Each calendar costs the bookstore \$7.50 and is sold for \$10. After February, all unsold calendars are returned to the publisher for a refund of \$2.50 per calendar. Suppose Walton predicts demand will be somewhere between 100 and 300.

Demand = d ~ Uniform[100, 300] Order Quantity = Q (decision variable) Revenue = Cost = Refund = Profit =

#### В С D Е F 3 Data 4 Unit Cost \$7.50 5 Unit Price \$10.00 6 Unit Refund \$2.50 7 8 **Demand Distribution (Uniform)** 9 100 Minimum 10 300 Maximum 11 12 **Decision Variable** 13 Order Quantity 200 14 15 Simulation 16 Demand Revenue Cost Refund Profit 17 200 \$2,000.00 \$1,500.00 \$0.00 \$500.00

Step #	<b>#1 (</b>	Setur	) Sprea	dsheet)
Sup '	/ <b>I</b> (	Sciup	, Spi ca	usneet

	В	С	D	E	F
16	Demand	Revenue	Cost	Refund	Profit
17	200	=\$C\$5*MIN(\$C\$13,B17)	=\$C\$4*\$C\$13	=\$C\$6*MAX(\$C\$13-B17,0)	=C17-D17+E17

For random inputs, just enter any number (e.g., 200 in B17).

Calculate performance measure (Profit) as a function of the random input(s) (Demand).

Session #9 Simulation and Crystal Ball

### Step #2 (Define Assumptions—i.e., random variables)

Select the cell that contains the random variable (B17):

	В
16	Demand
17	200

(Note: The cell *must* contain a value before choosing Define Assumption)

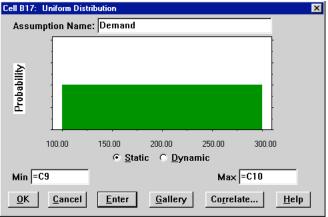
and click on the "Define Assumptions" button in toolbar (or in the Cell menu):



Select type of distribution:

Normal	<u>T</u> riangular	Poisson	<u>B</u> inomial
<u>L</u> ognormal	Uniform	<u>E</u> xponential	<u>G</u> eometric
	Beta	Hype <u>rg</u> eometric	Cu <u>s</u> tom
OK Cancel More Fit Help			

#### Provide parameters of distributions:



	В	С	
8	Demand Distrik	oution (Uniform)	
9	Minimum =	100	
10	Maximum =	300	

### Step #3 (Define Forecast—i.e., output)

Select the cell that contains the output variable to forecast (F17):

	F
16	Profit
17	\$500.00

click on the "Define Forecast" button in toolbar (or in the Cell menu),



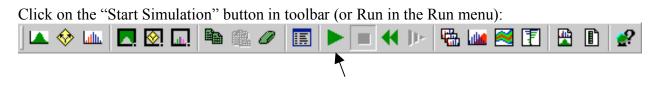
and fill in the Define Forecast dialogue box.

Cell F17: Define Fore	ecast 🔀
Forecast Name:	Profit
Units:	
Forecast Window	v Size: © Small C Large
☑ <u>D</u> isplay Wind	low Automatically C While <u>R</u> unning
	When Stopped (faster)
<u>0</u> K	<u>Cancel</u> <u>Set Default</u> <u>H</u> elp

### Step #4 (Choose Number of Trials)

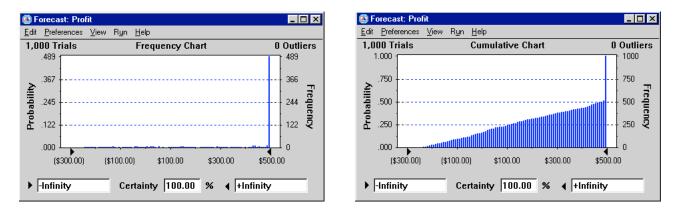
Click on the "Run Preferences" button in toolbar (or in the Run menu): 💾 🗈 2 🚸 📖 - 🕮 🥖 .... ۵ 11 T and select the number of trials to run. **Run Preferences** х Maximum Number of Trials: 1,000 <u>S</u>ampling Stopping Criteria Spee<u>d</u> Stop on Calculation Error <u>M</u>acros 🗆 Stop When Mean Std. Errors are Less Than: 0.00 Options <<u>></u>> <u>0</u>K <u>C</u>ancel <u>H</u>elp

### **Step #5 (Run Simulation)**



### Step #6 (View Results)

The results of the simulation can be viewed in a variety of different ways (frequency chart, cumulative chart, statistics, and percentiles). Choose different options under the View menu in the forecast window.



🙆 Forecast	: Profit		_ 🗆 ×		
<u>E</u> dit <u>P</u> refere	<u>E</u> dit <u>P</u> references <u>V</u> iew R <u>u</u> n <u>H</u> elp				
Cell F17	Stati	stics			
	Statistic	Value			
	Trials Mean Mode Standard Deviation Variance Skewness Kurtosis Coeff. of Variability Range Maximum Range Minimum Range Minimum Range Width Mean Std. Error	1,000 \$310.77 \$484.05 \$500.00 \$240.12 \$57,655.32 -0.88 2.26 0,77 (\$246.94) \$500.00 \$746.94 \$7.59			

<u>dit P</u> refere	ences <u>V</u> iew R <u>u</u> n <u>H</u> elp		
Cell F17	Perc	entiles	
	Percentile	Value	
	0%	(\$246.94)	
	10%	(\$85.83)	
	20%	\$33.69	
	30%	\$177.70	
	40%	\$342.59	
	50%	\$484.05	
	60% 70%	\$500.00 \$500.00	
	80%	\$500.00	
	90%	\$500.00	
	100%	\$500.00	

The results can be copied into a worksheet or Word document (choose Copy under the Edit menu in the simulation output window.

## **Using Decision Tables**

The **Decision Table** tool can be used to quickly run a simulation for many values of a decision variable (e.g., the order quantity).

Select the cell that contains the decision variable (C13):

	В	С
12		<b>Decision Variable</b>
13	Order Quantity	200

and click on the "Define Decision" button in toolbar (or in the Cell menu):



and specify the type of variable (continuous or discrete) and upper and lower bounds:

Cell C13: Define Decision Variable	2	<
Name: Order Quantity		
Variable Bounds Lower: 100 Upper: 300	Variable Type C Continuous Discrete Step: 1	
OK Cancel	Help	

# **Using Decision Tables**

Choose Decision Table from the CB Tools menu, and follow the instructions in the three dialogue boxes:

Choose the target cell (Profit in this case), and click on Next.

specify target (step 1 of 3)	<u>?</u> ×
Decision Table Crystal Ball Tool & Decisioneering 1938-2000	10.0 <th< th=""></th<>
Evaluate the effects of alternate decisions in your simulation model.	
Profit	
	-
Please enter the target cell or select from the li	st of forecasts above
[Walton.xls]Walton!\$F\$17	<u>.</u>
< Back	Cancel Help (v5.1

Specify the decision variable(s) to vary (Order Quantity in this case), and click on >> to move it to the "Chosen Decision Variables" column. Then click on Next. Note: a maximum of two decision variables can be varied at a time.

Select one or two decisions (step 2 of 3)	<u>? ×</u>
Decision Table Crystal Ball Tool & Decisioneering 1938-2000	122 134 477 527 527 528 534 477 522   103 106 437 527
Select one or two decisions to evaluate:	47 155 40 004 47 455 47 037 477 037 163 055 49 00 10 0 0 04 47 107
Available Decision Variables	Chosen Decision Variables
	Order Quantity
<back <u="">Next &gt;</back>	Cancel <u>H</u> elp

## **Using Decision Tables**

Select the number of different trial values to simulate for the decision variable. The values will be evenly distributed between the lower and upper bound for the decision variable. For example, 5 trial values with a lower bound of 100 and an upper bound of 300 will simulate order quantities of 100, 150, 200, 250, and 300. Also specify the number of trials to run for each simulation run. Then click on Start to run the simulations.

Spe	cify options (step 3 of 3)	? ×
	<b>Decision Table</b> Crystal Ball Tool ® Decisioneering 1998-2000	D.20 D.14 4.77 D.20 D.20 D.16 4.77 D.20   D.20 D.14 4.77 D.20 D.20 D.16 4.77 D.20   D.20 D.26 4.77 D.20 D.27 D.20 D.16 4.77 D.20   D.21 D.25 4.77 D.20 D.26 4.77 D.20 D.26 4.77 D.20   D.21 D.25 4.77 D.20 D.24 D.25 4.77 D.20 D.24 D.25 D.27   D.21 D.21 D.24 D.24 D.25 D.27 D.24 D.25 D.27   D.21 D.24 D.27 D.27 D.27 D.24 D.25 D.27   D.21 D.24 D.27 D.27 D.24 D.27 D.26 D.26 D.26   D.23 D.24 D.27 D.24 D.27 D.24 D.27 D.24 D.27 D.24 D.27 D.26 D.26 D
	Simulation Control Test 5 values for Order Run each simulation for 1000	r Quantity trials (maximum)
	While Running C Show forecasts as defined Show only target forecast C Hide all forecasts < Back Start	Cancel <u>H</u> elp

The resulting decision table shows the mean result of the target cell (Profit) for each value of the decision variable (order quantity). To see the complete simulation results for an order quantity, select the appropriate cell (B2, C2, D2, E2, or F2) and click on forecast chart.

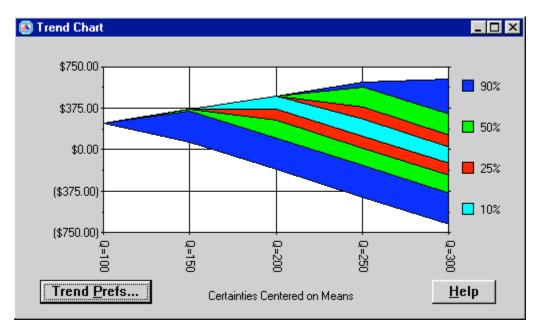
	А	В	С	D	E	F
	Trend Chart	Order (	Order (	Order (	Order (	Order (
	Overlay Chart	Quantity (100)	Quantity	Quantity	Quantity	Quantity (300)
1	Forecast Charts	(100)	r (150)	(200)	(250)	(300)
2		\$250.00	\$328.13	\$312.49	\$202.77	-\$0.49
3		1	2	3	4	5

# **Trend Charts**

A trend chart can be used to show trends across a range of values for the decision variable. To generate a trend chart, select the entire set of results for all of the decision variables (B2:F2)

	A	В	С	D	E	F
	Trend Chart	Order G	Order Q	Order Q	Order Q	Order Q
	Overlay Chart	luantii	Quantity	luantii	Quantity	Quantity
1	Forecast Charts	Quantity (100)	y (150)	Quantity (200)	y (250)	y (300)
2		\$250.00	\$328.13	\$312.49	\$202.77	-\$0.49
3		1	2	3	4	5

and then click on Trend Chart.



This chart gives "certainty bands" (similar to a confidence interval) for the forecast cells. 10% of the time, the project duration will fall within the inner band (light blue), 25% of the time within the  $2^{nd}$  band (red), 50% of the time within the third band (green), and 90% of the time within the outside band (dark blue).

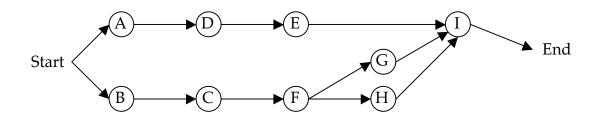
### **Project Management—Global Oil**

Global Oil is planning to move their credit card operation to Des Moines, Iowa from their home office in Dallas. The move involves many different divisions within the company. Real estate must select one of three available office sites. Personnel has to determine which employees from Dallas will move, how many new employees to hire, and who will train them. The systems group and treasurer's office must organize the new operating procedure and make financial arrangements. The architects will have to design the interior space, and oversee needed structural improvements. Each site is an existing building with sufficient open space, but office partitions, computer facilities, furnishings, and so on, must all be provided.

A complicating factor is that there is an interdependence of activities. In other words, some parts of the project cannot be started until other parts are completed. For example, Global cannot construct the interior of an office before it has been designed. Neither can it hire new employees until it has determined its personnel requirements.

The necessary activities and their necessary predecessors (due to interdependence) are listed below. Three estimates are made for the completion time of each activity—the minimum time, most likely time, and maximum time.

		Immediate	Time Estimates (days)		
Activity	Description	Predecessor	Minimum	Most Likely	Maximum
А	Select Office Site	—	21	21	21
В	Create Org. & Fin. Plan	—	20	25	30
С	Determine Personnel Req.	В	15	20	30
D	Design Facility	A, C	20	28	42
E	Construct Facility	D	40	48	66
F	Select Personnel to Move	С	12	12	12
G	Hire New Employees	F	20	25	32
Н	Move Key Employees	F	28	28	28
Ι	Train New Personnel	Е, G, H	10	15	24



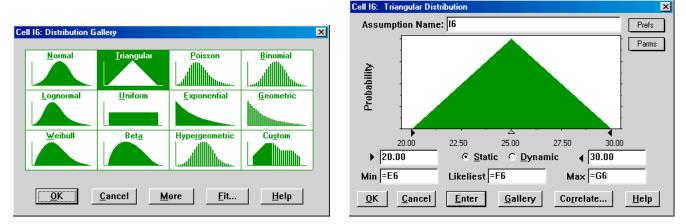
### **Step #1 (Setup Spreadsheet)**

	В	С	D	E	F	G	Н	I	J
2				Activity	/ Time (Tria	ngular)			
3			Immediate		Most		Start	Activity	Finish
4	Activity	Description	Predecessors	Minimum	Likely	Maximum	Time	Time	Time
5	Α	Select Site	-	21	21	21	0	21	21
6	В	Create Org. & Fin. Plan	-	20	25	30	0	25	25
7	С	Determine Personnel Req.	В	15	20	30	25	20	45
8	D	Design Facility	A, C	20	28	42	45	28	73
9	Е	Construct Facility	D	40	48	66	73	48	121
10	F	Select Personnel to Move	С	12	12	12	45	12	57
11	G	Hire New Employees	F	20	25	32	57	25	82
12	Н	Move Key Employees	F	28	28	28	57	28	85
13	Ι	Train New Personnel	E, G, H	10	15	24	121	15	136
14									
15						Project Completion Time			136.00

	Н	I	J
3	Start	Activity	Finish
4	Time	Time	Time
5	0	21	=H5+I5
6	0	25	=H6+I6
7	=J6	20	=H7+I7
8	=MAX(J5,J7)	28	=H8+I8
9	=J8	48	=H9+I9
10	=J7	12	=H10+I10
11	=J10	25	=H11+I11
12	=J10	28	=H12+I12
13	=MAX(J9,J11,J12)	15	=H13+I13
14			
15		Project Completion Time	=J13

### Step #2 (Define Assumptions—i.e., random variables)

Each of the random activity times (B, C, D, E, G, and I) is assumed to follow the triangular distribution.



# **Global Oil Simulation with Crystal Ball**<sup>®</sup>

### Step #3 (Define Forecast—i.e., output)

Cell J15 is the forecast cell:

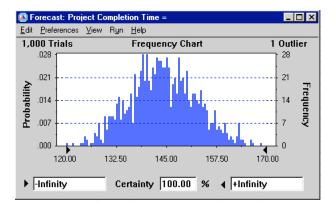
	Н		J
15	Project Co	mpletion Time	136.00

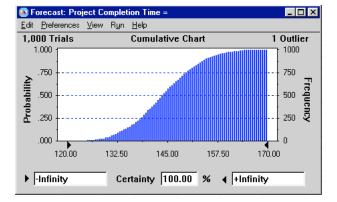
### **Step #4 (Choose Number of Trials)**

1000 trials were run. In addition, Sensitivity Analysis was enabled in the Options of the Run Preferences dialogue box. This allows for the generation of sensitivity analysis results later.

### **Step #5 (Run Simulation)**

### Step #6 (View Results)





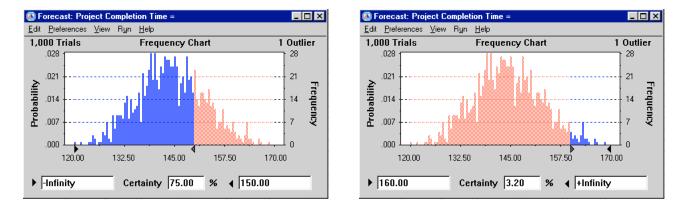
🙆 Forecast	: Project Completion Time	=	_ 🗆 🗡
<u>E</u> dit <u>P</u> refere	nces <u>V</u> iew R <u>u</u> n <u>H</u> elp		
Cell J15	Stati		
	Statistic	Value	
	Trials Mean Median Mode Standard Deviation Variance Skewness Kurtosis Coeff. of Variability Range Maximum Range Maximum Range Midth Mean Std. Error	1,000 144,33 144,03  8,30 68,95 0,12 2,83 0,06 120,10 174,17 54,08 0,26	

	ices <u>V</u> iew R <u>u</u> n	Help			
Cell J15		Percen	tiles		_
	Percenti	e	Value	•	
	0%			120.10	
	10%			133.25	
	20%			137.41	
	30%			139.76	
	40%			142.02	
	50%			144.03	
	60%				
	70%				
	80%			151.55	
	90%			154.93	
	100%			174.17	

# Additional Results Available with Crystal Ball<sup>®</sup>

Slide the triangles below the histograms to determine the probability that the output (project duration) is less than a certain value (e.g., a deadline), greater than a certain value, or between any two values (by sliding both triangles).

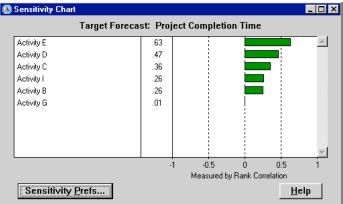
Alternatively, you can type in values for the lower bound or upper bound to determine the probability. You can also type in a probability (in "Certainty"), and it will determine the range that has that probability.



There is a 75% chance the project will be completed within 150 days. There is a 3.2% chance that the project will take more than 160 days.

### **Sensitivity Chart**

Choose "Open Sensitivity Chart" in the Run menu. Note that this chart is only available if you selected the "Sensitivity Analysis" option under Run Preferences. This chart gives an indication as to which random variables (activity times) have the greatest impact on the output cell (project completion time).



Variability in activity E has the greatest impact on overall project duration, followed by activity D, C, I, and B. Variability in activity G has almost no impact.

# Fitting a Distribution

Crystal Ball can be used to "fit" a distribution to data.

The following data has been collected for the previous 100 phone calls to a mailorder house:

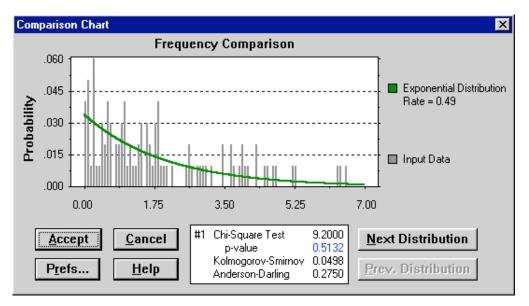
	A	В	С	D	E	F	G	H	
1	Pho	ne Data							
2									
3			Arrival	Interarrival	Length of Call			Interarrival	Length of Call
4		<u>Customer #</u>	(minutes)	<u>Time</u>	(minutes)			Time	(minutes)
5		1	8.22	8.22	3.77		Averages	2.004	4.51
6		2	12.25	4.03	4.53				
7		3	12.27	0.02	4.04				
8		4	16.26	3.98	3.70		Simulation	2	4
9		5	18.06	1.81	5.38				
10		6	18.87	0.81	4.36				
11		7	23.46	4.58	4.41				
12		8	23.53	0.08	5.14				
13		9	28.73	5.20	4.76				
14		10	30.56	1.83	4.68				
15		11	32.36	1.80	5.06				
16		12	36.90	4.54	5.75				
17		13	43.30	6.40	4.06				
18		14	43.88	0.57	3.25				
19		15	45.17	1.29	3.57				
99		95	194.02	0.28	4.26				
100		96	195.48	1.46	3.37				
101		97	195.87	0.38	4.45				
102		98	196.84	0.98	5.06				
103		99	197.81	0.97	5.20				
104		100	200.43	2.61	4.25				

# Fitting Data to a Distribution

### Using Crystal Ball<sup>®</sup> to fit data to a distribution

- 1. Select a spreadsheet cell.
- 2. Choose Define Assumption.
- 3. Click the Fit button, then select the source of the fitted data.
- 4. Click the Next button, then select the distributions to try to fit.
- 5. Click OK.

### **Interarrival Time**



**Service Time** 

