

Irradiance Volumes for Games

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Overview

- Introduction and Motivation
- Review

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- Radiance, Irradiance, Transfer
- Spherical Harmonics
 - Projection, Gradients, Evaluation
- Irradiance Volume
 - Uniform Subdivision, Adaptive Subdivision, Interpolation
- Summary

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Motivation

- Real-time and offline rendering have one important gap: the use of *global illumination* for physically based, realistic lighting
- Games use light mapping
 - Approximates global illumination on the surface
 - Only for static scenes!
 - Does not address dynamic objects that move through the scene
 - Result in beautifully rendered, globally illuminated scenes that contain unrealistic, locally lit dynamic objects
- Solution:

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- Precomputed Irradiance Volumes for static scenes
- Precomputed Radiance Transfer for objects within those scenes

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The Irradiance Volumes

- We aim to solve as much of the global illumination calculation during preprocess time
- A 3D light map: volume of diffuse lighting samples
 - ✓ This is what we're trying to achieve



[Greger98] gdceurope.com



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Used in *Ruby: Dangerous Curves*



- These techniques were used as a drop in replacement for diffuse lighting in the *Ruby: Dangerous Curves* demo
- At the very least, these techniques could serve as an ambient lighting solution in your games
- Before diving into the details it is necessary to have a basic familiarity with the following terms:
 - Radiance, Irradiance, and Transfer



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Demo

Ruby2: Dangerous Curves

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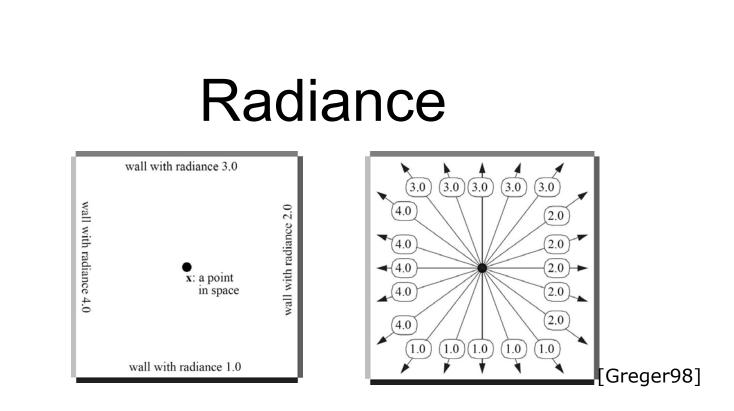
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 Radiance is the emitted energy per unit time in a given direction from a unit area of an emitting surface

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Capturing Radiance

- Capture radiance at a point for all directions
 - Place a camera at that point
 - Render the surrounding scene into a cubemap
 - Scale each texel by its projected solid angle
- The cube map represents the radiance for all directions for this point
 - Known as the radiance distribution function
 - Not necessarily continuous (Even in simple environments)
- Every point in space has a radiance distribution function
 - Radiance is a 5D function (3 spacial dimensions and 2 directional dimensions)

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Radial distance from x indicates radiance seen in that direction.

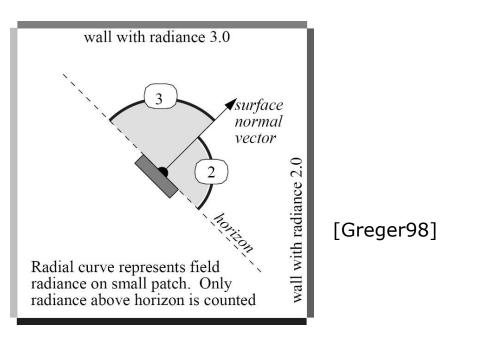
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[Greger98]





Radiance



- The radiance of a surface is a function of its BRDF and incident radiance
- The incident radiance defined on the hemisphere of incoming directions is called the *field-radiance function*



Irradiance

- The radiance of a purely diffuse surface is defined in terms of the surface's *irradiance*
- Irradiance is an *integral* of the field-radiance function multiplied by the Lambertian cosine term over a hemisphere

$$I(p, N_p) = \int_{\Omega} L(p, \vec{\omega}_i) (N_p \bullet \vec{\omega}_i) d\omega_i$$

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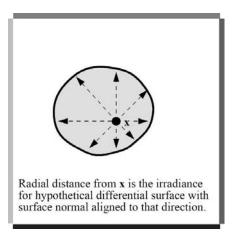
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Irradiance



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- We could compute irradiance at a point for *all* possible orientations of a small patch:
 - For each orientation, compute a convolution of the field radiance with a cosine kernel
- The result of this convolution for all orientations would be an irradiance distribution function
- The irradiance distribution function looks like a radiance distribution function except much blurrier because of the averaging process (convolution with cosine kernel)
- The irradiance distribution function is continuous over directions



Irradiance

- The irradiance distribution function can be computed for every point in space: irradiance is a 5D function (3 spatial dimensions and 2 directional dimensions)
- Evaluating the irradiance distribution function in the direction of a surface normal gives us irradiance at that surface location
- Computing irradiance distribution functions on demand is possible but can be costly. An obvious optimization is to precompute irradiance distribution functions for a scene at preprocess time and then use this precomputed data at runtime

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Rendering with Irradiance

- The Irradiance Distribution Function at a point can be stored using a "Diffuse Cube Map"
- The cube map is indexed with an object's surface normal





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Efficient Storage of Irradiance

- We need an irradiance distribution function for objects moving in the scene
- Capture the lighting environment at many points in the scene
 - At preprocess time
 - Then we'll have a volume of irradiance distribution functions
- But! We're still left with the cost of storing tons of cubemaps
 - For all the points in the scene
 - And the bandwidth overhead of indexing these maps at render time
- Instead! Compress irradiance maps
 - Represent each as a vector of spherical harmonic coefficients
 - Reduces both storage and bandwidth costs



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Spherical Harmonics

- Infinite series of spherical functions
- Can be used as basis functions
 - Stores a frequency space approximation of an environment map
- Use Microsoft DirectX SDK for spherical harmonics computations
 - Includes functions for projecting a cubemap into a representative set of spherical harmonic coefficients
 - Also functions for scaling and rotating spherical harmonics – important if your object is moving
- For code snippets that will help your write your own spherical harmonic helper functions, see Robin Green's Spherical Harmonic Lighting: The Gritty Details

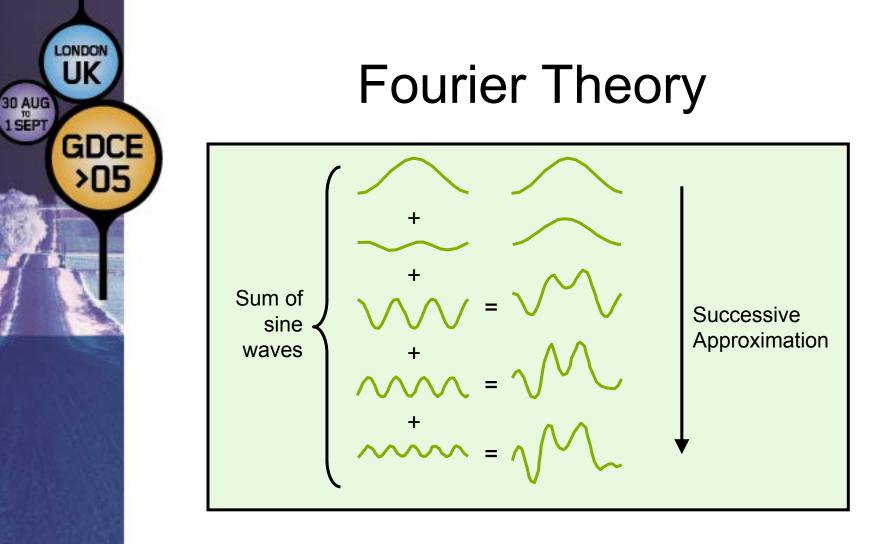
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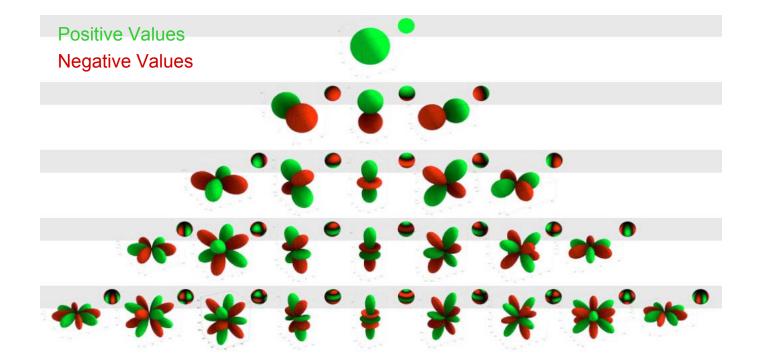
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- Recall that it is possible to represent any 1D signal as a sum of appropriately scaled and shifted sine waves
- Spherical harmonics are the same idea on a sphere!









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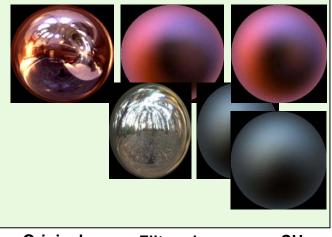
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From [Green] gdceurope.com

Spherical Projection: Storage and Computation



[Ramamoorthi]

Original Filtered SH Environment Environment Representation Map Map

- Map Map
 Projecting an environment map into 3rd order spherical harmonics effectively gives you the irradiance distribution function [Ramamoorthi]
- Projection into 3rd order SH is not only a storage win but a preprocessing win too since SH projection is much faster than convolving an environment map with a cosine kernel for all possible normal orientations



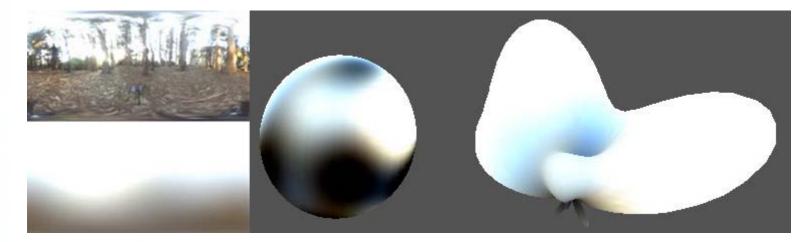
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Spherical Harmonics

- Once an environment map has been projected into spherical harmonics, the coefficients can be used to evaluate the original map in a given direction
- Storing these coefficients VS constants allows us to compute irradiance per-vertex rather than having to sample a cubemap per-pixel





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SH Evaluation With Normal

float4 cAr; // first 4 red irradiance coefficients
float4 cAg; // first 4 green irradiance coefficients
float4 cAb; // first 4 blue irradiance coefficients
float4 cBr; // second 4 red irradiance coefficients
float4 cBg; // second 4 green irradiance coefficients
float4 cBb; // second 4 blue irradiance coefficients
float4 cC; // last 1 irradiance coefficient for red, blue and green

float3 x1, x2, x3;

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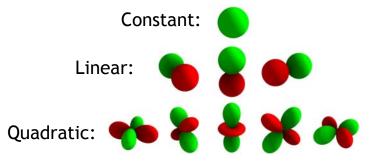
```
// Linear + constant polynomial terms
x1.r = dot(cAr, vNormal);
x1.g = dot(cAg, vNormal);
x1.b = dot(cAb, vNormal);
```

```
// 4 of the quadratic polynomials
float4 vB = vNormal.xyzz * vNormal.yzzx;
x2.r = dot(cBr, vB);
x2.g = dot(cBg, vB);
x2.b = dot(cBb, vB);
```

```
// Final quadratic polynomial
float vC = vNormal.x*vNormal.x - vNormal.y*vNormal.y;
x3 = cC.rgb * vC;
```

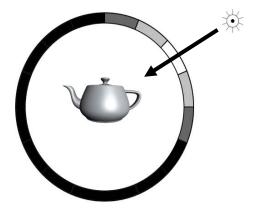
Output.Diffuse.rgb = x1 + x2 + x3;





[Shader Code From DirectX SDK]

One Irradiance Sample: A Point in Space



- Irradiance samples only store irradiance for a single point in space
- This really only works well if the lighting environment is infinitely distant (just like a cubic environment map)
- This error can be very noticeable when the lighting environment isn't truly distant



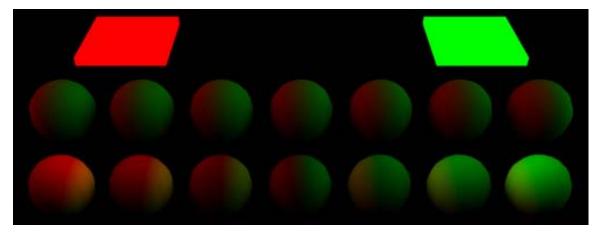
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Spherical Harmonic Irradiance Gradients

- If an irradiance sample is used to shade the surface of an object, the potential error increases the further we move away from the point at which the irradiance sample was generated
- Irradiance gradients allow us to store the rate at which irradiance changes with respect to translations about the sample





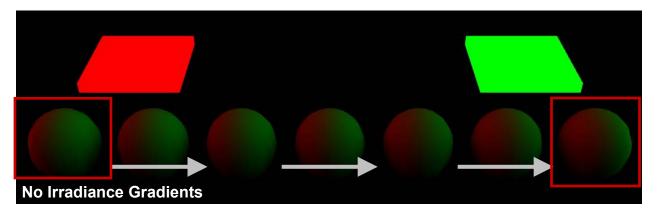
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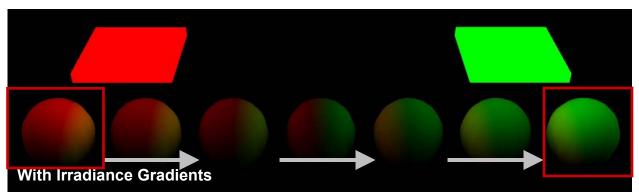
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If irradiance varies greatly near a sample point, can store irradiance gradients along with each irradiance sample. [Ward 92][Annen04] **Game**Developers gdceurope.com



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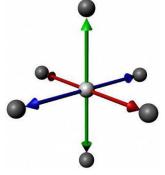
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Spherical Harmonic Irradiance Gradients

- Translational gradients for spherical harmonic irradiance samples may be computed in a number of ways [Annen]...
- One simple way to find the gradients is to use central differencing to estimate the partial derivatives of the spherical harmonic irradiance coefficients
- Project 6 additional irradiance functions into spherical harmonics and perform central differencing on each of the coefficients



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Central Differencing $d \nabla_y = \frac{y_{+1} - y_{-1}}{d}$

- Subtract the coefficients for samples taken at a small offset in the +Y and –Y directions
- Divide by distance between the samples
- This gives you an estimate of the partial derivative with respect to y for each coefficient
- Do this for the other two axes as well...
- You now have a 3D gradient vector for each spherical harmonic coefficient



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First-Order Taylor Expansion

- At render time, the gradient may be used to extrapolate a new irradiance function
- Compute world space vector from the location at which the sample was generated to the point being rendered
- This vector is then dotted with the gradient vector and added to the original sample to extrapolate a new irradiance function

$$I'_i = I_i + (\nabla I_i \cdot d)$$

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• *li'* is the *i*th spherical harmonic coefficient of the extrapolated irradiance function, *li* is the *i*th spherical harmonic coefficient of the stored irradiance sample, is the irradiance gradient for the *i*th irradiance coefficient and *d* is a non-unit vector from the original sample location to the point being rendered

 ∇I_i



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```
shaded
float3 vSampleOffset = (vPos - vIrradianceSamplePosWS);
// Arrays for the extrapolated 4th order (16 coefficients per color channel) spherical
    harmonic irradiance
float4 vIrradNewRed[4]; float4 vIrradNewGreen[4]; float4 vIrradNewBlue[4];
// Extrapolate new irradiance for 4th order spherical harmonic irradiance sample
for ( int index = 0; index < 4; index++ )
ł
    vIrradNewRed[index] = float4( dot(vSampleOffset, vIrradianceGradientRedOS[index*4 + 0]),
                                  dot(vSampleOffset, vIrradianceGradientRedOS[index*4 + 1]),
                                  dot(vSampleOffset, vIrradianceGradientRedOS[index*4 + 2]),
                                  dot(vSampleOffset, vIrradianceGradientRedOS[index*4 + 3])
    );
    vIrradNewGreen[index] = float4( dot(vSampleOffset, vIrradianceGradientGreenOS[index*4 +
    0]),
                                    dot(vSampleOffset, vIrradianceGradientGreenOS[index*4 +
    11),
                                    dot(vSampleOffset, vIrradianceGradientGreenOS[index*4 +
    2]),
                                    dot(vSampleOffset, vIrradianceGradientGreenOS[index*4 +
    31) );
    vIrradNewBlue[index] = float4( dot(vSampleOffset, vIrradianceGradientBlueOS[index*4 +
    0]),
                                   dot(vSampleOffset, vIrradianceGradientBlueOS[index*4 +
    1]),
                                   dot(vSampleOffset, vIrradianceGradientBlueOS[index*4 +
    2]),
                                   dot(vSampleOffset, vIrradianceGradientBlueOS[index*4 +
    31) );
    vIrradNewRed[index] = vIrradNewRed[index] + vIrradianceSampleRed[index];
```

// Compute vector from original irdiance sample position to the position that is being

```
vIrradNewGreen[index] = vIrradNewGreen[index] + vIrradianceSampleGreen[index];
vIrradNewBlue[index] = vIrradNewBlue[index] + vIrradianceSampleBlue[index];
```



}

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What About Self Occlusion or Bounced Lighting?

- Gradients improve the usefulness of each sample but we still haven't solved all our problems...
- One limitation of irradiance mapping is that it doesn't account for an object's self occlusion or for bounced lighting from the object itself
- This additional light transport complexity can be accounted for by generating pre-computed radiance transfer (PRT) functions for points on the object's surface



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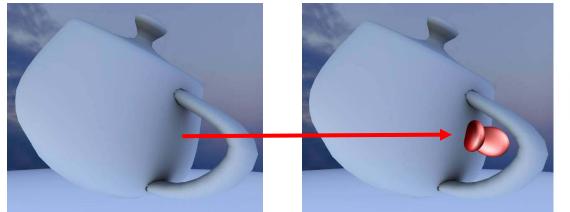
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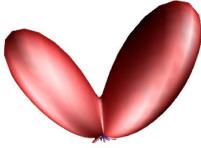
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Precomputed Radiance Transfer

- Radiance Transfer maps incident radiance to reflected radiance
- PRT require incident radiance, we're dealing will irradiance?!
 - If you project an environment map into 3rd order SH and evaluate with a surface normal then the SH data represents irradiance
 - If you project an environment map into SH and integrate the product of the environment and transfer functions then the SH data represents low-frequency incident radiance (where "lowfrequency" is relative to the order of the SH projection)
 - As long as we're assuming low-frequency, the data is the same... the difference is semantic
- If stored as SH, the integral of (Incident Radiance * Transfer) reduces to a dot product of two vectors (the vectors contain SH coefficients for incident radiance and transfer)







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Handling Rotation

- If using samples for irradiance distribution, the surface normal used for finding irradiance should be transformed into world space (skinned) before evaluating the SH function
- If using the samples for PRT, the transfer function can not be easily rotated on the GPU so instead rotate the lighting environment by the inverse model transform on the CPU







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Irradiance Volume: Background

- Irradiance volumes have been used by the film industry as an acceleration technique for high quality, photorealistic offline rendering
- The volumes store irradiance distribution functions for points in space by utilizing a spatial partitioning structure that serves as a cache
- Sampling the volume allows the for the global illumination of a point in space to be quickly calculated
- Spherical harmonics allow irradiance volumes to be efficiently stored and evaluated
- These volumes are compatible with precomputed radiance transfer and allow for fast, efficient and realistic rendering in real time applications such as games



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The Irradiance Volume



From [Greger]

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- A grid of irradiance samples is taken throughout the scene
- At render time, the volume is queried and near-by irradiance samples are interpolated to estimate the global illumination at a point in the scene



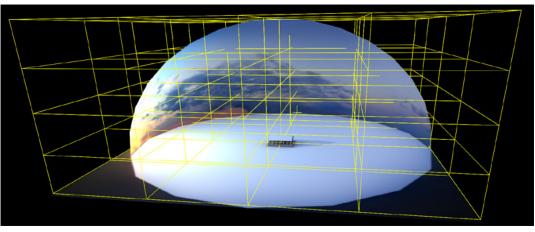
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Uniform Volume Subdivision



- Subdividing a scene into evenly spaced voxels is one way to generate and store irradiance samples
- Irradiance samples should be computed for each of the eight corners of all the voxels
- A uniform grid is easy to implement but quickly becomes unwieldy for large, complex scenes that require many levels of subdivision



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Adaptive Volume Subdivision



- Choosing an adaptive subdivision scheme such as an octree will allow you to only subdivide the volume where subdivision is beneficial
 - For a given scene, some areas will have slowly changing irradiance and can be subdivided coarsely
 - Areas with quickly changing irradiance will need to be subdivided more finely



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Demo

Irradiance Volumes with Irradiance Gradients Computed Using Adaptive Subdivision

Adaptive Octree Subdivision

- Knowing which areas of your scene need further subdivision is a challenging problem
- For example, a character standing just inside a house will appear shadowed on a sunny day but if the character moves over the threshold of the door and into the sunlight they should appear much brighter; irradiance can change very quickly

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• We need a way to find areas of rapidly changing irradiance so that these areas can be more finely subdivided



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Adaptive Subdivision

- Since irradiance sampling is done as a preprocess, one option is to use a brute force method that starts by super-sampling irradiance using a highly subdivided uniform grid
- After this super-sampled volume is found, redundant voxels may be discarded by comparing irradiance samples at child nodes using some error tolerance to determine if a voxel was unnecessarily subdivided
- This brute force method isn't perfect though because it assumes you know the maximum level of subdivision or supersampling that is needed for a given scene
- Instead, certain heuristics may be used to detect voxels that might benefit from further subdivision



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Subdivision Heuristics

- Measuring irradiance gradients and flagging voxels where the irradiance is known to change quickly with respect to translation (large gradient) is one way to test if further subdivision is necessary
- Testing gradients isn't perfect though, because this will only subdivide areas where you know that irradiance changes rapidly. There may still be areas that have small gradients but contain sub-regions with quickly changing irradiance
- Subdivide any voxels that contain scene geometry [Greger98]
- Find the **harmonic mean** of scene depth at a sample point to determine when subdivision is needed [Pharr04]
- The idea is that areas that contain a lot of geometry will have more rapidly changing irradiance
 - Not a bad assumption, the more geometry surrounding a sample point the more opportunities for shadows, bounced lighting, etc...
 - In the center of a room, lighting doesn't change much. As one approaches the walls things get interesting.



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Harmonic Mean of Scene Depth

- Shoot a bunch of rays out from the irradiance sample's position
- Compute the harmonic mean of distance traveled by all rays before intersection

$$HM = \frac{N}{\sum_{i=1}^{N} \frac{1}{d_i}}$$

- *N* is the total number of rays fired, and d*i* is the distance that the *i*th ray traveled before intersecting scene geometry
- The harmonic mean is then used as an upper-bound for the sample's usefulness. If the neighboring irradiance samples are further away than this upper-bound, then their associated voxels should be subdivided
- The harmonic mean is chosen over the arithmetic mean (or linear average) because large depth values—due to infinite depth if no geometry exists in a given direction—would quickly bias the arithmetic mean to a large value



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Using the GPU: Harmonic Mean of Scene Depth

- For each sample location, render the scene into each face of a floating point cubemap
- The scene should be drawn with a shader that outputs: 1/depth
- Read the cubemap back into system memory and find the harmonic mean

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Using the GPU: Voxel Contains Scene Geometry

- If you're already reading back scene depth for the harmonic mean test, you can also use this data to determine if any scene geometry exists inside the voxel
 - Scene depth is sampled at the voxel corners, so only some of the cubemap texels should be used to test for scene intersection
- Alternatively, you could use occlusion queries:
 - Place the camera at the center of a voxel
 - Render into each face of a cubemap
 - First draw quads for each face of the voxel
 - Second draw the scene
 - If any of the scene's draw calls pass the occlusion query, a part of the scene is inside the voxel



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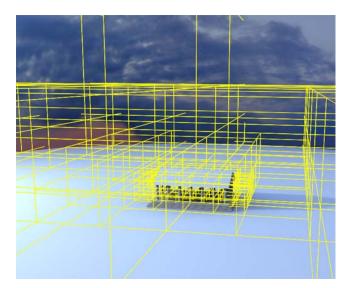
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- Specify a Min and Max level of subdivision
- Allow thresholds to be specified for each subdivision heuristic
- After you've fully sampled the volume, go back and reject any redundant samples: if a voxel has been subdivided and it's children don't differ enough from the parent, these samples may be culled

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Sampling the Volume

- If you're using an octree, search the tree for the voxel that contains the object's centroid
- Use the surrounding samples to determine irradiance
 - Interpolate surrounding samples (trilinear)
 - Find a weighted sum of surrounding samples (weighted by 1/distance)

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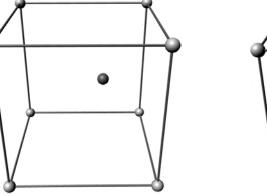
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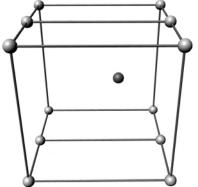
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Trilinear Interpolation







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- Seven LERPs of the spherical harmonic coefficients
- Works well for uniformly subdivided volumes
- Adaptively subdivided volumes require slightly more care



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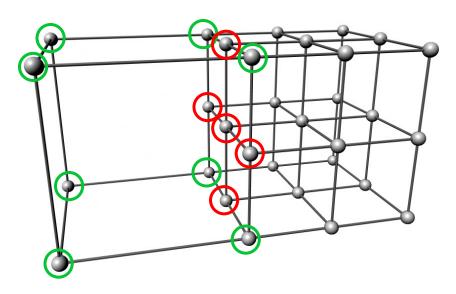
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Trilinear Interpolation



- When transitioning between voxels that have been adaptively subdivided, naïve trilinear interpolation can produce popping artifacts
- As an object moves from finely subdivided voxels to coarsely subdivided voxels, some of the sample data will suddenly be ignored



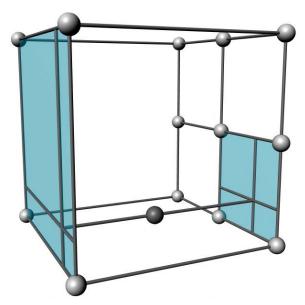
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Trilinear Interpolation



- To prevent popping, continue using samples from subdivided neighbors for interpolation
- Each octree node should store pointers to samples that lie on each face



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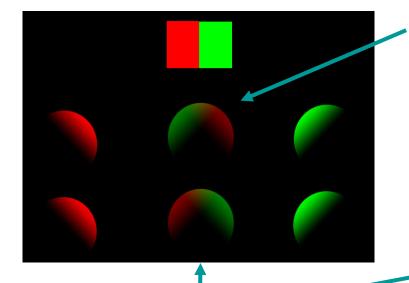
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Using Gradients for Interpolation



Linear interpolation between left and right samples

Gradients used for first-order Taylor expansion before interpolation

• Before using a sample for interpolation, evaluate the first-order Taylor expansion, then interpolate as usual.



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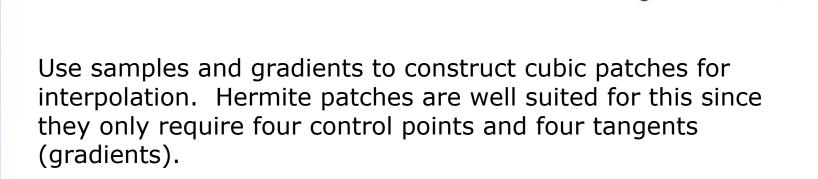
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Tricubic Interpolation



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	6 th order SH approximation for R, G and B: 108 floats 6 th order SH gradients for R, G, and B: 324 floats 432 floats / sample
	3 rd order SH approximation for R, G, and B: 27 floats 3 rd order SH gradients for R, G, and B: 81 floats

Modern GPUs can typically store 1024 to 2048 floats in VS constant store

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GPU Memory Requirements (Constant Store)

- If you have enough constant store available, you can send all nearby samples and their gradients to the vertex shader and do the interpolation per-vertex
- If this is too costly for you, interpolate on the CPU and send a single interpolated sample and interpolated gradient to the vertex shader
 - We did this for *Ruby: Dangerous Curves* and were very pleased with the results

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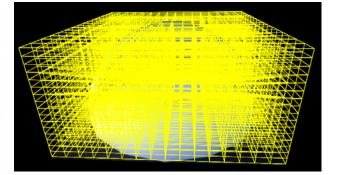
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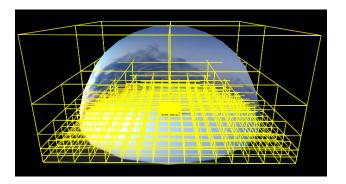
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System Memory Requirements



Uniform Subdivision Scene: 4913 Unique Samples 3rd Order SH + Gradients: ~2MB 6th Order SH + Gradients: ~8.2MB



Adaptive Subdivision Scene: 2301 Unique Samples 3rd Order SH + Gradients: ~970kB 6th Order SH + Gradients: ~3.8MB



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Pros:

- Fast, efficient global illumination: A 3D light map for characters
- Much smaller memory cost compared to diffuse cubemaps
- Scalable: use higher/lower order SH approximations depending on needs
- Compatible with lower-end hardware



- Doesn't handle dynamic lighting well
- Articulated characters are tricky
 - Works fine if evaluating irradiance samples with a vertex normal but PRT can be problematic
 - Instead of using Spherical Harmonic basis functions...
 - Valve uses a Cartesian basis in HalfLife2 (Ambient cube): <u>http://www2.ati.com/developer/gdc/D3DTutorial10_Half-Life2_Shading.pdf</u>
 - Zonal Harmonics are more GPU rotation friendly. See Microsoft's GDC 2004 talk on LDPRT



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Conclusion

- A lighting technique for dynamic characters in static scenes
- Compact storage of diffuse lighting functions using Spherical Harmonics for many points in a scene
- First order derivatives are used for Taylor series expansion of the incident lighting functions to increase the accuracy of each sample
- Adaptive scheme using an octree for efficiently subdividing a scene
- Interpolation between samples



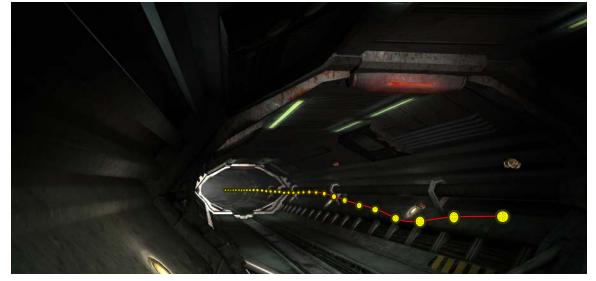
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Irradiance Samples Along a Path



- We used a technique, similar to the one presented today, for diffuse lighting in *Ruby: Dangerous Curves*
- We cheated a little though, rather than storing an entire volume, we only stored samples along each character's animation spline
- Rather than parameterize the samples by position, we parameterized by time



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- [Pharr04[*Physically Based Rendering*, Pharr, M., Humphreys, G., Morgan Kaufmann, San Francisco, 2004.
- See also Richard Huddy's truly awesome material elsewhere, even if it is on other subjects like cats, chickens and performance malarkey...



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СМР

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