Lecture 11

Single Stage FET Amplifiers: Common Source (CS) Amplifier

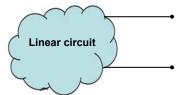
The Building Blocks of Analog Circuits - I

In this lecture you will learn:

- General amplifier concepts (in terms of the two-port models)
 Common source amplifier (CS)
- Small signal models of amplifiers

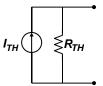
Reminder: Thevenin and Norton Equivalent Circuits

Consider an arbitrary linear circuit:



It can be represented by any two of the following equivalent circuits:





 $V_{TH} = I_{TH}R_{TH}$

Types of Linear Amplifiers

There are four basic types of amplifiers that we will study in this course:

1) Voltage to Voltage Amplifiers (or just Voltage Amplifiers)



2) Voltage to Current Amplifiers (or Transconductance Amplifiers)

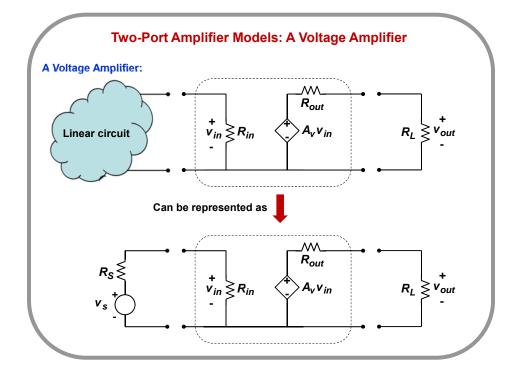


3) Current to Current Amplifiers (or just Current Amplifiers)



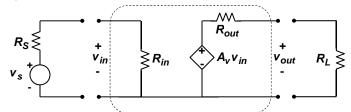
4) Current to Voltage Amplifiers (or Transimpedance Amplifiers)





Two-Port Amplifier Models: A Voltage Amplifier

A Voltage Amplifier:



$$\frac{v_{out}}{v_s} = A_v \left(\frac{R_{in}}{R_{in} + R_S} \right) \left(\frac{R_L}{R_{out} + R_L} \right)$$

Requirements:

Large input resistance R_{in} Small output resistance R_{out}

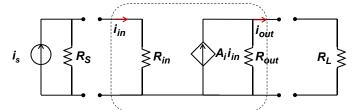
Input voltage divider Ouput voltage divider

Open circuit output voltage gain (i.e. when $R_L = \infty$):

$$\frac{v_{out}}{v_{in}} = A_v = \text{Voltage gain}$$

Two-Port Amplifier Models: A Current Amplifier

A Current Amplifier:



$$\frac{i_{out}}{i_s} = A_i \left(\frac{R_S}{R_S + R_{in}}\right) \left(\frac{R_{out}}{R_{out} + R_L}\right)$$

Requirements:

Small input resistance R_{in} Large output resistance R_{out}

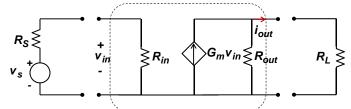
Input Ouput current current divider divider

Short circuit output current gain (i.e. when $R_L = 0$):

$$\frac{i_{out}}{i_{in}} = A_i = \text{Current gain}$$

Two-Port Amplifier Models: A Transconductance Amplifier

A Transconductance Amplifier (or a Voltage-to-Current Amplifier):



$$\frac{i_{\text{out}}}{v_{\text{S}}} = G_m \left(\frac{R_{in}}{R_{\text{S}} + R_{in}}\right) \left(\frac{R_{\text{out}}}{R_{\text{out}} + R_L}\right)$$

Requirements:

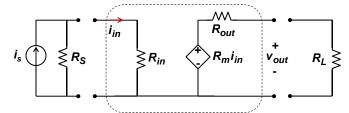
Large input resistance R_{in} Large output resistance R_{out} Input Ouput voltage current divider divider

Short circuit output current and transconductance gain (i.e. when $R_L = 0$):

$$\frac{i_{out}}{v_{in}} = G_m = \text{Transconductance gain}$$

Two-Port Amplifier Models: A Transimpedance Amplifier

A Transimpedance (or a Transresistance) Amplifier (or a Current-to-Voltage Amplifier):



$$\frac{\mathbf{v}_{out}}{i_s} = R_m \left(\frac{R_S}{R_S + R_{in}} \right) \left(\frac{R_L}{R_{out} + R_L} \right)$$

divider

Requirements:

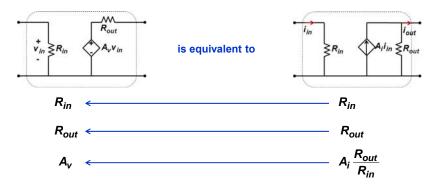
Small input resistance R_{in} Small output resistance R_{out} Input Ouput current voltage

divider

Open circuit output voltage and transimpedance gain (i.e. when $R_L = \infty$):

$$\frac{v_{out}}{i_{in}} = R_m = \text{Transimpedance gain}$$

Two-Port Amplifier Models: General Concepts



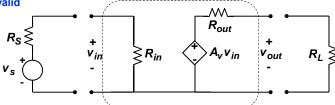
The two-port models are equivalent (inter-convertible)

The designation of an amplifier as a voltage, current, transconductance, or transimpedance amplifier depends on the values of the input and output resistances

Need to find the input resistance, output resistance, open circuit voltage gain, and short circuit current gain to characterize an amplifier

Unilateral Networks and Two-Port Amplifier Models

For many circuits and amplifiers, the kind of two-port models described here are not strictly valid



Reasons:

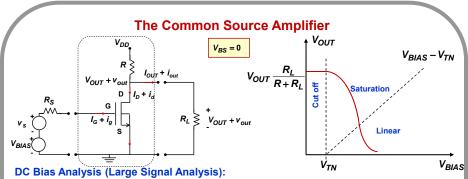
The input resistance R_{in} can depend on the load resistance R_{L} The output resistance R_{out} can depend on the source resistance R_{s}

Circuits in which the above does not happen, and for which the two-port models described here are strictly valid, are unilateral

In many cases, even for non-unilateral networks, two-port models described here tend to be good approximations for <u>hand-calculations</u>

The Common Source Amplifier V_{DD} $V_{BS} = 0$ $V_{BS} = 0$ V_{BIAS} V_{DD} V_{DD} V_{DD} $V_{DUT} + i_{out}$ $V_{DUT} + i_{out}$ $V_{DUT} + i_{out}$ $V_{DUT} + v_{OU}$

The source terminal is "common" between the input and the output



Make sure the output load resistance R_L is included in the DC bias analysis

Start by assuming the FET is in saturation (and then later verify):

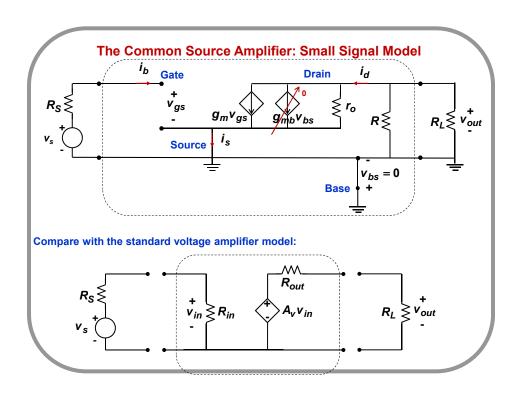
$$V_{DD} - (I_{OUT} + I_D)R = V_{OUT}$$

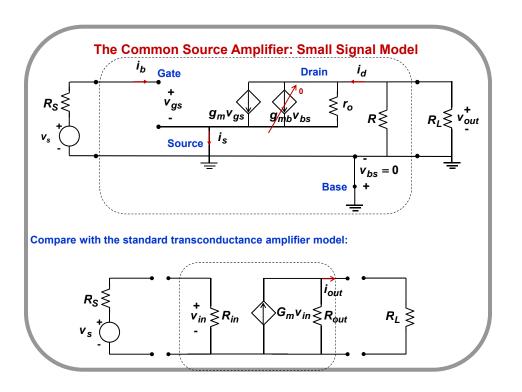
$$\Rightarrow V_{DD} - \left(\frac{V_{OUT}}{R_L} + I_D\right)R = V_{OUT}$$

$$\Rightarrow V_{OUT} = (V_{DD} - I_D R) \frac{R_L}{R + R_L}$$

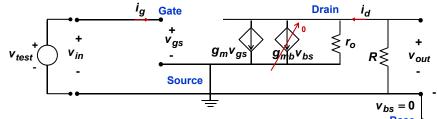
$$I_D = \frac{k_n}{2} (V_{BIAS} - V_{TN})^2 (1 + \lambda_n V_{OUT})$$

$$I_D \approx \frac{k_n}{2} (V_{BIAS} - V_{TN})^2$$





The Common Source Amplifier: Open Circuit Voltage Gain



Open circuit voltage gain and transimpedance gain:

To find the open circuit voltage gain or the transimpedance gain one must:

- Remove the load resistance R_L at the output that the circuit will drive
- Then apply a test voltage source at the input
- iii) Then find the resulting open circuit output voltage
- iv) Take the ratio of the output voltage and the input voltage to find the open circuit voltage gain:

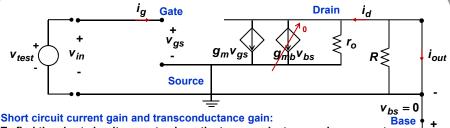
$$A_{v} = \frac{v_{out}}{v_{in}} = -\frac{i_{d}R}{v_{in}} = -g_{m}(r_{o} \mid\mid R)$$

Or take the ratio of the output voltage and the input current to find the transimpedance gain:

$$R_m = \frac{V_{out}}{i_{in}} = -\infty$$

This result is somewhat artificial since at non-zero frequencies there will be a finite input current due to capacitances

The Common Source Amplifier: Short Circuit Current Gain



To find the short circuit current gain or the transconductance gain one must:

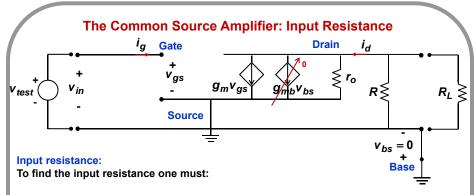
- Short the load resistance R_L at the output that the circuit will drive
- Then apply a test voltage source at the input
- iii) Then find the resulting current at the shorted output
- iv) Take the ratio of the output and the input currents to find the short circuit current

$$A_i = \frac{i_{out}}{i_g} = -\frac{g_m v_{gs}}{0} = \infty \qquad \qquad \underset{\text{(at DC)}}{\longrightarrow} \text{ for the CS amplifier}$$
This result is somewhat artificial since at non-zero frequencies

there will be a finite input current due to capacitances

Or take the ratio of the output current and the input voltage to find the transconductance gain:

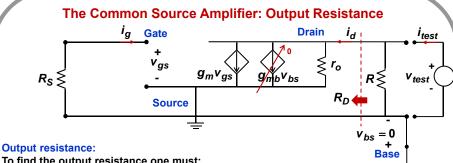
$$G_m = \frac{i_{out}}{v_{in}} = -\frac{g_m v_{gs}}{v_{in}} = -g_m$$



- Make sure the load resistance R_L that the circuit will drive is in place at the output
- Then apply a test voltage source at the input
- iii) Then find the resulting current at the input
- iv) Then take the ratio of the input voltage and the input current

$$R_{in} = \frac{v_{in}}{i_g} = \infty$$
 \longrightarrow of for the CS amplifier (at DC)

This result is somewhat artificial since at non-zero frequencies there will be a finite input current due to capacitances



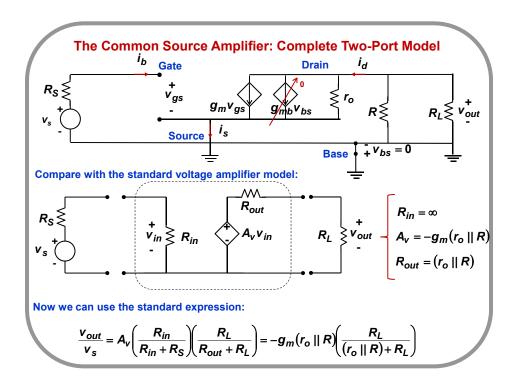
- To find the output resistance one must:
- Remove the load resistance R_{L} and put a test voltage source in its place
- Make sure the source resistance $R_{\rm S}$ is in place at the input
- Then find the resulting test current at the output
- iv) Then take the ratio of the test voltage and the test current

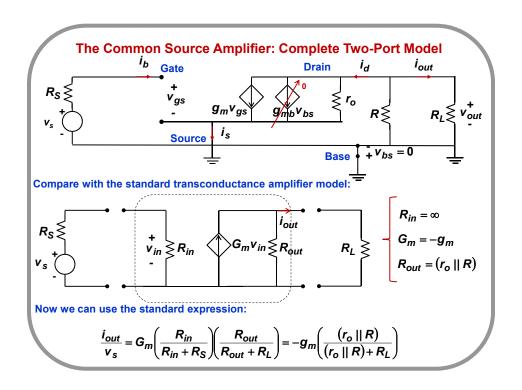
$$R_{out} = \frac{v_{test}}{i_{test}} = r_o || R$$
 Fairly large for the CS amplifier

Analysis shows that CS is a good transconductance amplifier!

Resistance looking into the drain end of a FET:

$$R_D = r_o$$





The Common Source Amplifier: g_m vs g_o

In saturation:

$$g_m = k_n (V_{GS} - V_{TN})(1 + \lambda_n V_{DS})$$

$$g_o = \frac{k_n}{2} (V_{GS} - V_{TN})^2 \lambda_n$$

Therefore:

$$\frac{g_m}{g_o} = g_m r_o = \frac{2(1 + \lambda_n V_{DS})}{(V_{GS} - V_{TN})^2 \lambda_n} \approx \frac{2}{(V_{GS} - V_{TN}) \lambda_n}$$

Rough Estimates:

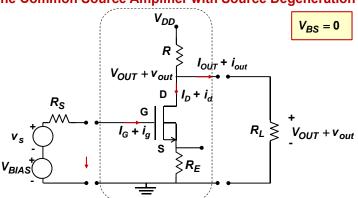
$$(V_{GS} - V_{TN}) \sim 0.5 - 1.0 V$$

 $\lambda_n \sim 0.05 - 0.10 V^{-1}$

Therefore:

$$\frac{g_m}{g_o} = g_m r_o \approx \frac{2}{(V_{GS} - V_{TN})\lambda_n} \sim 20 - 80$$

The Common Source Amplifier with Source Degeneration



$$V_{DD} - (I_{OUT} + I_D)R = V_{OUT}$$

$$V_{DD} - (I_{OUT} + I_D)R = V_{OUT}$$

$$\Rightarrow V_{DD} - \left(\frac{V_{OUT}}{R_L} + I_D\right)R = V_{OUT}$$

$$\Rightarrow V_{OUT} = (V_{DD} - I_DR)\frac{R_L}{R + R_L}$$

$$I_D = \frac{k_n}{2}(V_{GS} - V_{TN})^2(1 + \lambda_n V_{OUT})$$

$$I_D \approx \frac{k_n}{2}(V_{GS} - V_{TN})^2$$

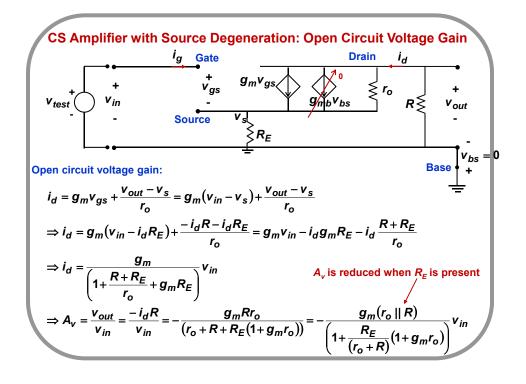
$$V_{GS} = V_{BIAS} - I_DR_E$$

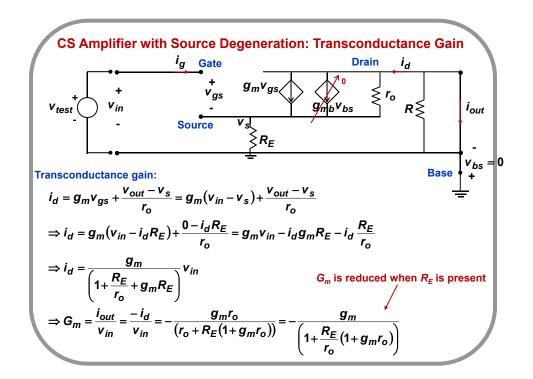
$$\Rightarrow V_{OUT} = (V_{DD} - I_D R) \frac{R_L}{R + R_L}$$

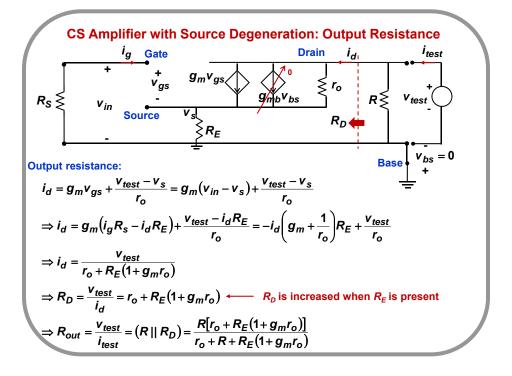
$$I_D = \frac{k_n}{2} \left(V_{GS} - V_{TN} \right)^2 \left(1 + \lambda_n V_{OUT} \right)$$

$$I_D \approx \frac{k_n}{2} (V_{GS} - V_{TN})^2$$

$$V_{GS} = V_{BIAS} - I_D R_E$$







Relations to Remember

For any small signal amplifier model, the following always hold:

(Transconductance) X (Output resistance) = (Open circuit voltage gain)

(Transimpedance) / (Output resistance) = (Short circuit current gain)

The above follows from the equivalent Thevenin and Norton models of the amplifier

***All quantities must be calculated assuming the same value of R_s (typically zero)

