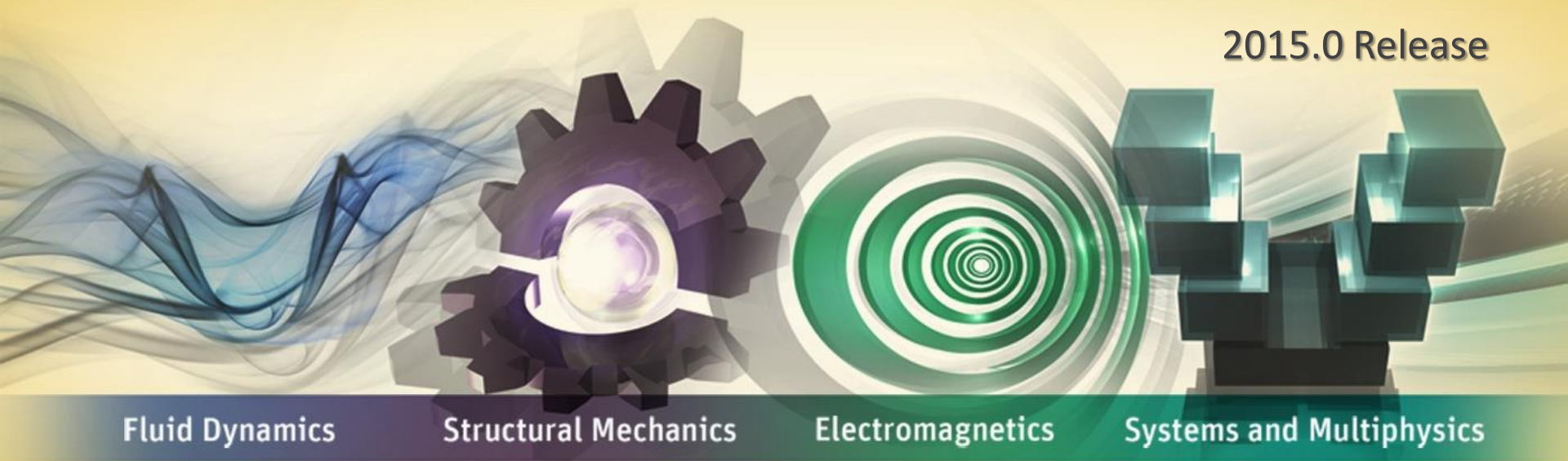


Lecture 9: Unit Cell Analysis (Infinite Array)

2015.0 Release



Fluid Dynamics

Structural Mechanics

Electromagnetics

Systems and Multiphysics

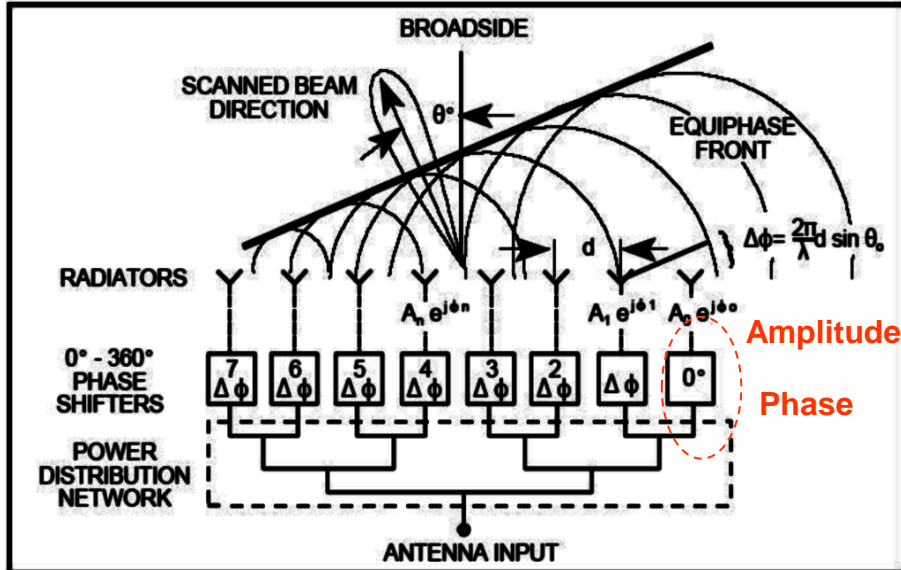
ANSYS HFSS for Antenna Design

• Phased Array

- A group of antenna elements in which the relative amplitudes and phases are varied to construct an effective radiation pattern by constructive and destructive interference

$$E_{array}(\theta_o, \phi_o, \theta, \phi) = \sum_n A_n(\theta_o, \phi_o) e^{j\psi_n(\theta_o, \phi_o)} \frac{e^{-jk_o r_n}}{r_n} E_n(\theta, \phi)$$

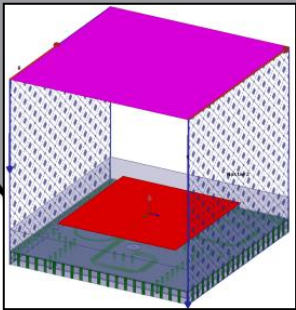
$$S_m(\theta_o, \phi_o) = \sum_n \frac{A_n(\theta_o, \phi_o) e^{j\psi_n(\theta_o, \phi_o)}}{A_m(\theta_o, \phi_o) e^{j\psi_m(\theta_o, \phi_o)}} S_{m,n}$$



- Beam shape can be controlled by adjusting the amplitude of each element
- Beam can be steered by applying a progressing phase shift across the array.
- Mutual coupling plays a key role in an element's pattern and input impedance.
- It is necessary to analyze the arrays performance over frequency and scan volume.

Unit Cell

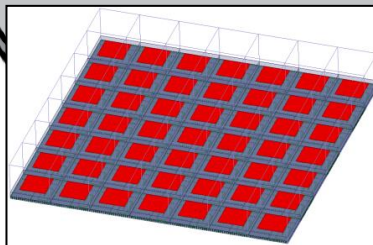
- **Uses Master/Slave boundaries**
 - models a single element as if it were in an infinite array environment
 - Infinite array environment accounted for by enforcing field periodicity through master/slave boundary pairs.
- **Reduces RAM**
- **Reduces solve time**
- **Infinite Array Approx.**
 - Edge affects ignored
 - Uniform magnitude excitation
 - Single scan angle solved at a time (Distributed Solve Option Parallelizes)



Finite Array

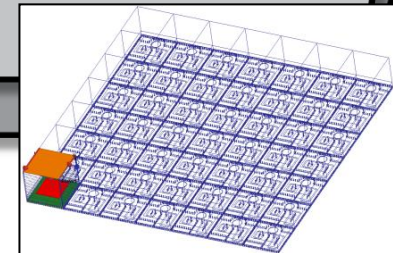
Explicit

- **Entire array analyzed**
 - Accounts for edge affects and edge treatments
 - Provides mutual coupling terms
 - Allows magnitude taper
- **Most flexible**
 - Fewest assumptions
 - Adaptive meshing performed on entire model
- **Complex Geometry**
 - Every element needs to be drawn
 - Large number of excitations
 - Complicated meshing process



Finite Array DDM

- **Entire array analyzed**
 - Accounts for edge affects
 - Provides mutual coupling terms
 - Allows magnitude taper
 - Adaptive meshing performed on single unit cell
 - Uses Domain Decomposition to minimize and distribute compute resources
- **Distributes RAM**
- **Reduces solve time**
- **Periodic assumption**
 - Geometry must be purely periodic in the XY plane



Unit Cell Analysis with Master / Slave Boundaries

Unit Cell Simplification

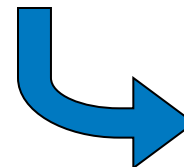
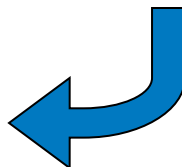
- **Unit Cell Analysis simplifies large arrays by assuming:**
 - The array is infinite
 - The pattern of each element is identical
 - The array is uniformly excited in amplitude, but not necessarily in phase.
- **This simplifies the pattern superposition equation**

$$E_{array}(\theta, \phi) = \sum_n A_n e^{j\psi_n} \frac{e^{-jk_o r_n}}{r_n} E_n(\theta, \phi)$$

$$E_{array}(\theta, \phi) = E(\theta, \phi) \underbrace{\sum_n A_n e^{j\psi_n}}_{\text{Array Factor}} \underbrace{\frac{e^{-jk_o r_n}}{r_n}}_{\text{Element Pattern}}$$

Element Pattern **Array Factor**

Solved using HFSS's Unit Cell Analysis with Master / Slave Boundaries

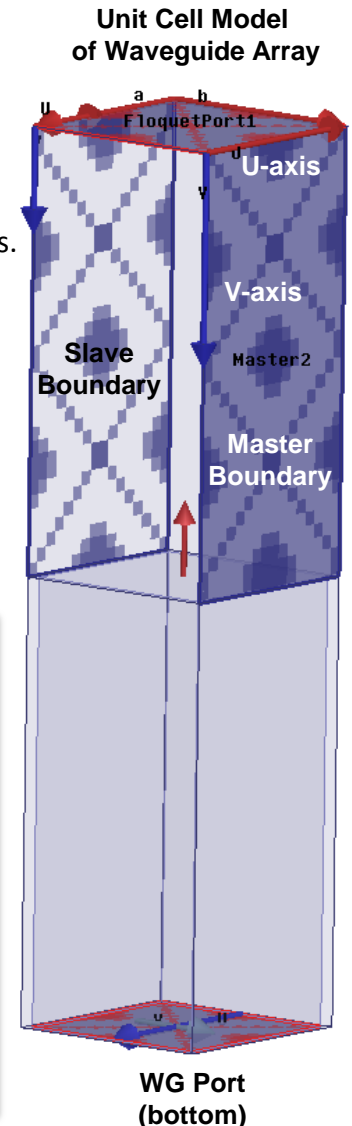
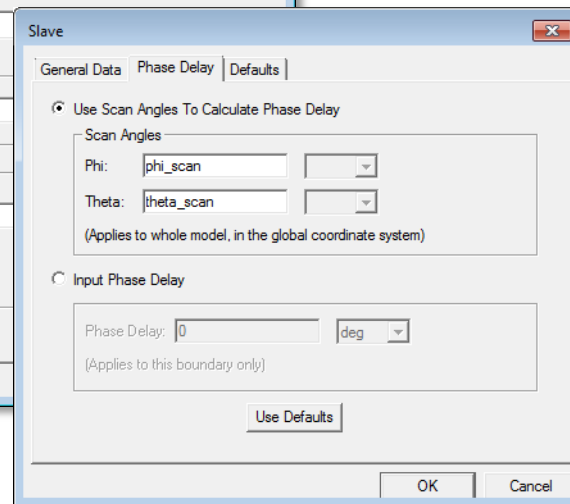
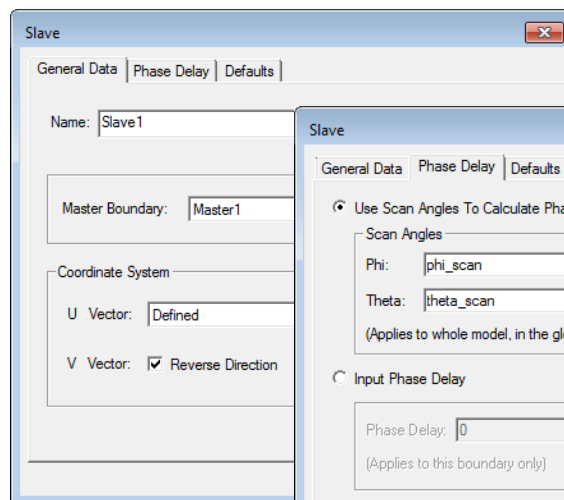
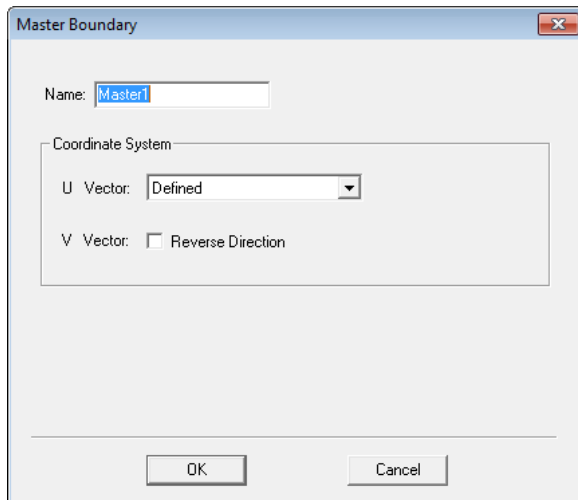


Determined by:

1. the array's lattice
2. the element's amplitude distribution
3. the progressive phase shift

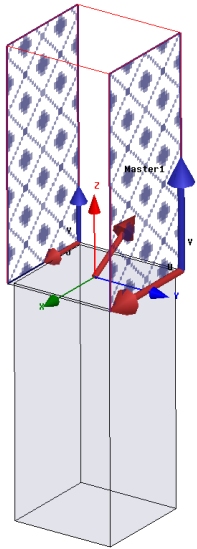
Master/Slave Boundaries

- Used to model unit cell of periodic structures
- Master and slave boundaries are always paired
 - Fields on master surface are mapped to slave surface with a phase shift enforcing a periodicity in the fields.
- Constraints
 - Master and slave surfaces must be identical in shape and size
 - Coordinate systems must be created to identify point-to-point correspondence



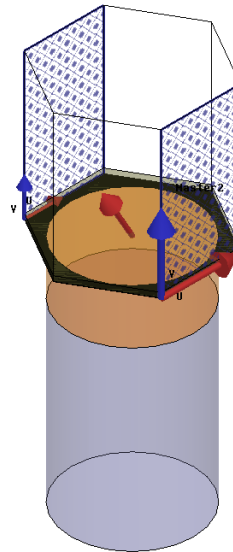
- **Unit Cell shape describes the array's lattice**
 - The shape should recreate the array's periodicity

Rectangular Lattice

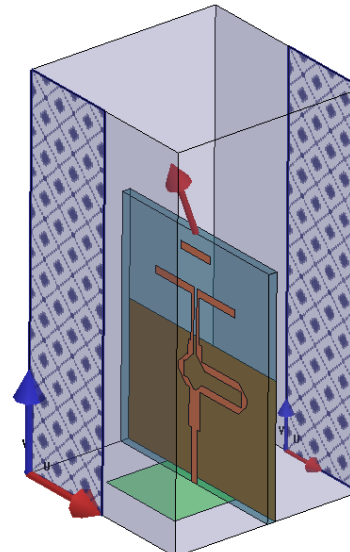


Rectangle

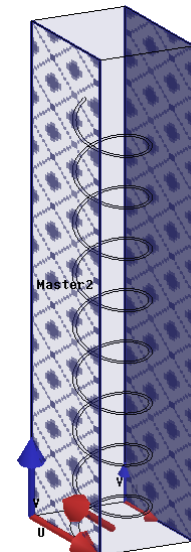
Triangular Lattice



Hexagon



Rectangle

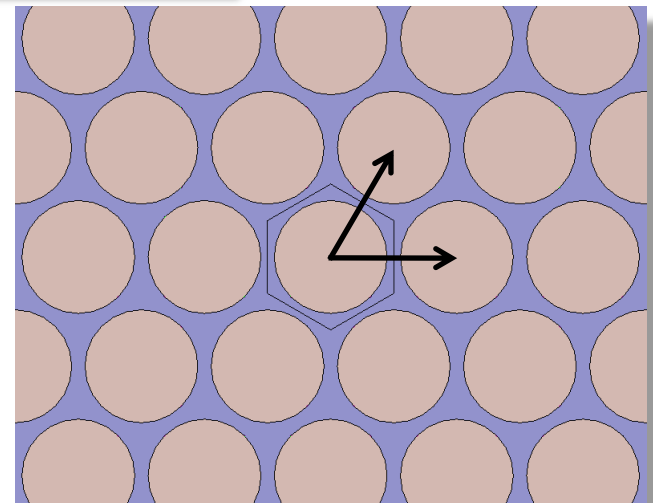
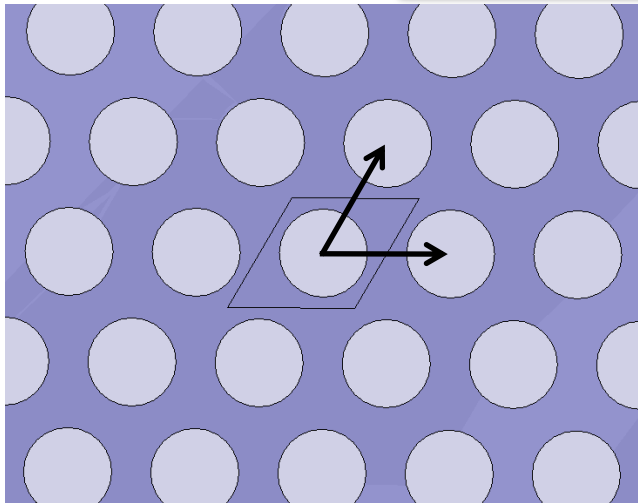
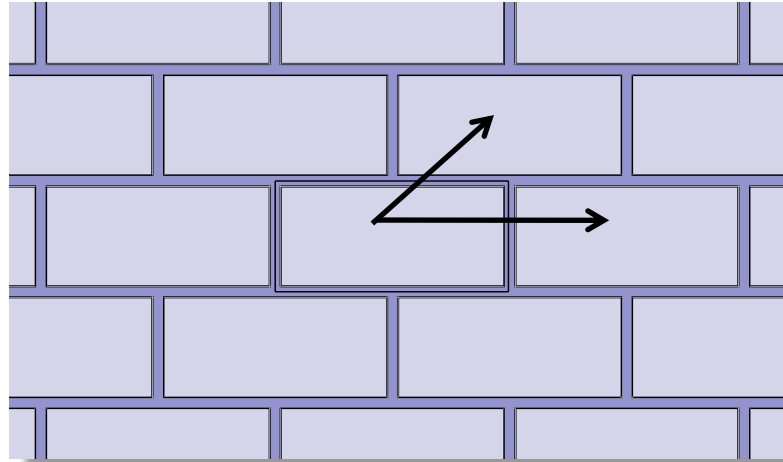


Parallelogram

What if the Lattice is Triangular

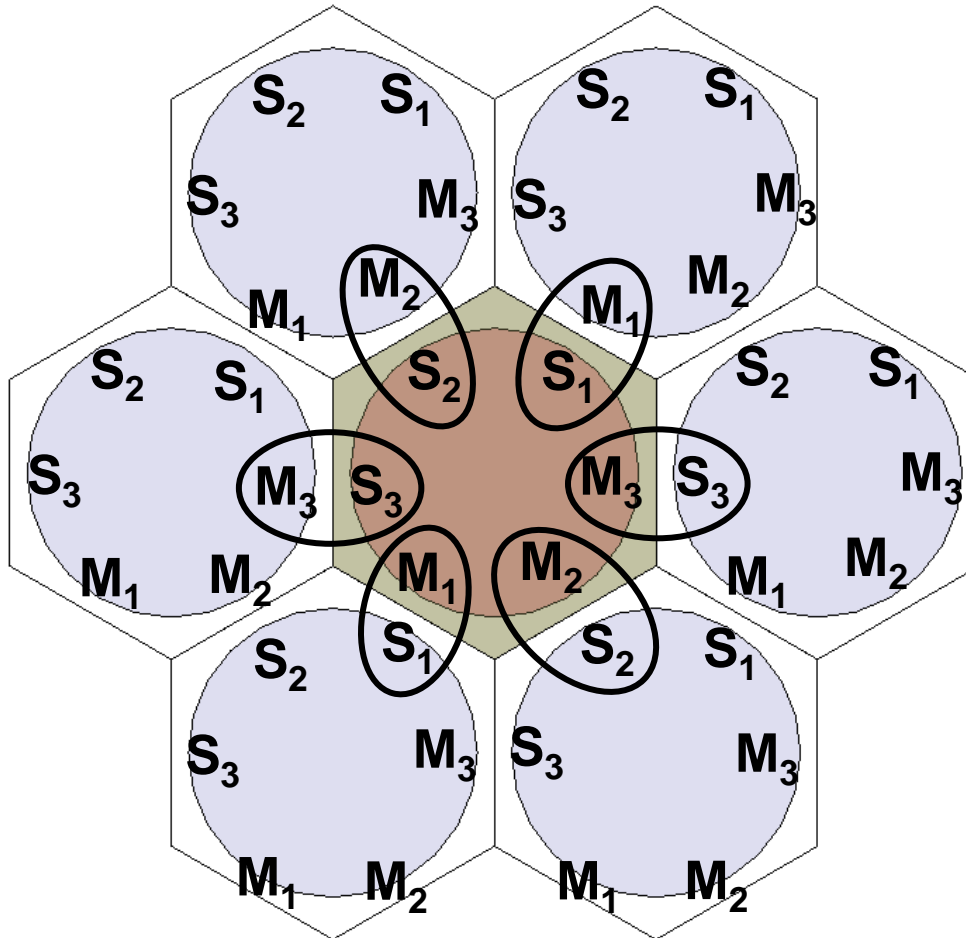
- **Triangular Lattice**

- A and B vectors should point from one element to the next adjacent element.
- Alternatively they should point from a master boundary to its corresponding slave boundary (or visa versa).



Verifying the Unit Cell Geometry

- When an element is duplicated along a periodicity the Master boundary should make contact with the adjacent cell's slave boundary



• Floquet Port

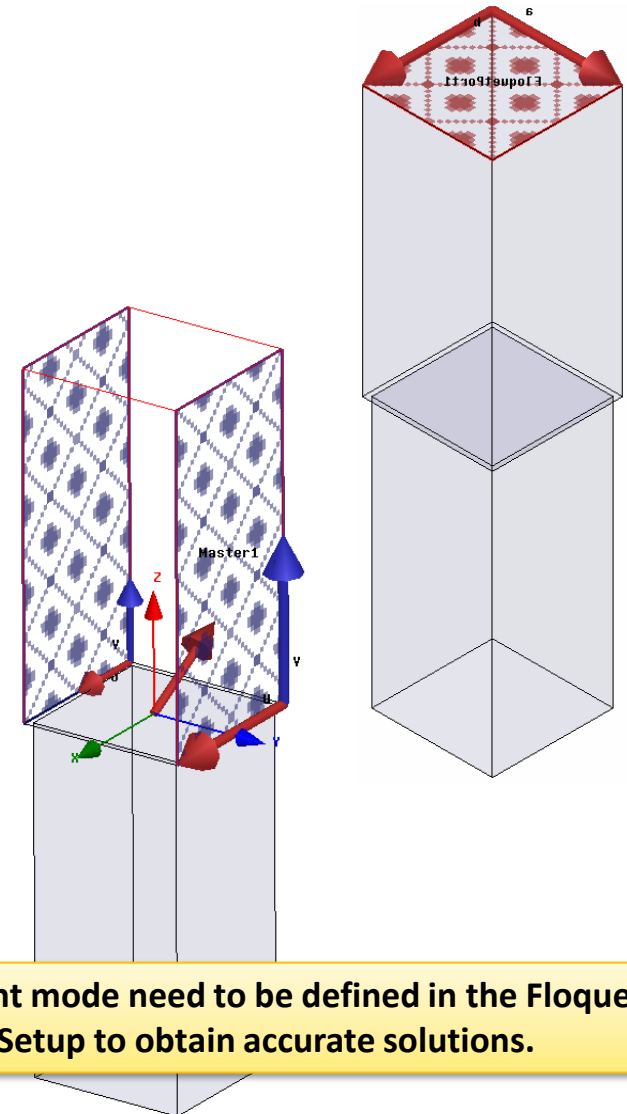
- Excites and terminates waves propagating down the unit cell
- Always Linked to Master/Slave Boundaries
 - Establishes field periodicity of the array
- Only for surfaces exposed to the background
- Replaces radiation boundary and PML for free space field absorption

• How do Floquet Ports Excite and Terminate Power

- Decomposes the fields on the Floquet Port into Floquet Modes
 - Set of TE and TM modes in which the power travels
 - Similar concept to Waveguide Modes
- Floquet Ports only absorb the modes that are defined on the port
 - All other modes are short circuited back into the model

• Post-Processing Floquet Ports

- Supports multiple modes and de-embedding
- Computes Generalized S-Parameters
 - Frequency dependent characteristic impedance (Z_0)
 - Frequency dependent propagation constant
 - Perfectly matched at every frequency and every scan angle

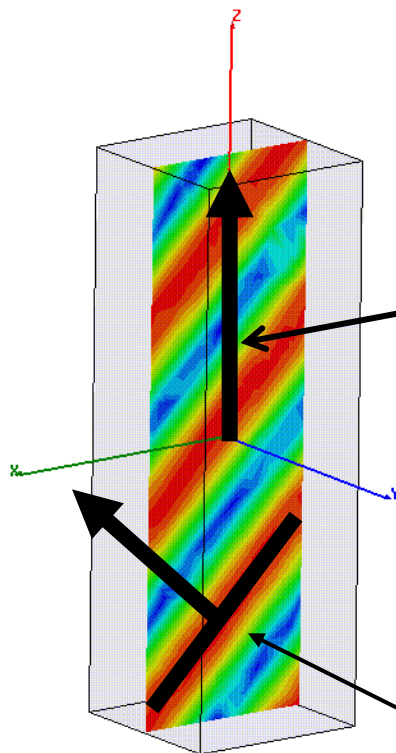


Floquet Mode Visualization

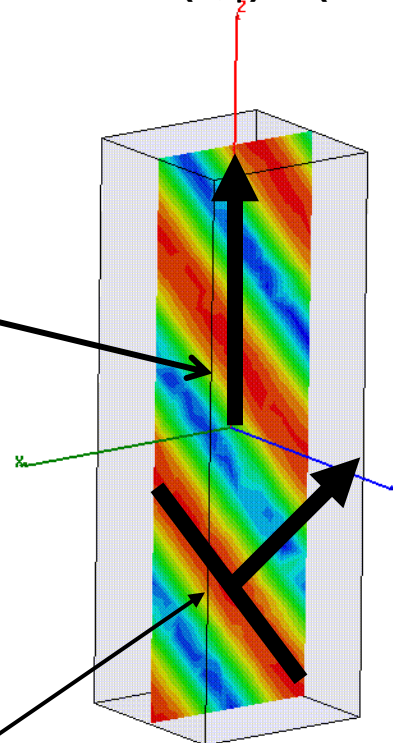
- Each floquet mode:

1. is a plane wave propagating in a given direction
2. represents a main beam or grating lobe of the array

**Dominant Mode
(Main Beam)**
Scanned to $(\theta, \phi) = (45^\circ, 0^\circ)$



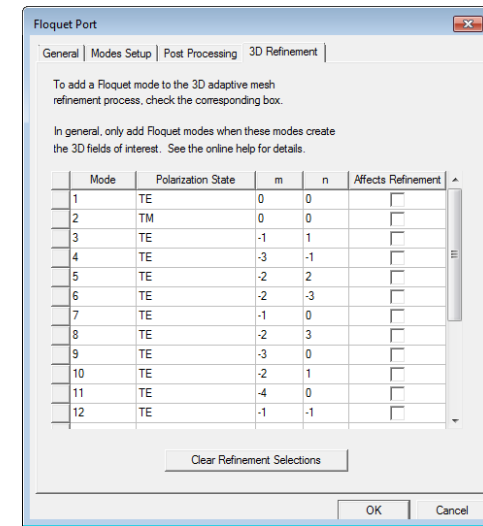
**Higher Order Mode
(Grating Lobe)**
Scanned to $(\theta, \phi) = (-45^\circ, 0^\circ)$



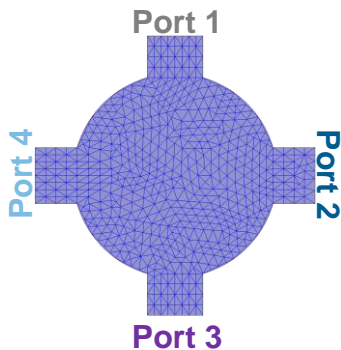
Floquet Port Setup

• Affects 3D Refinement

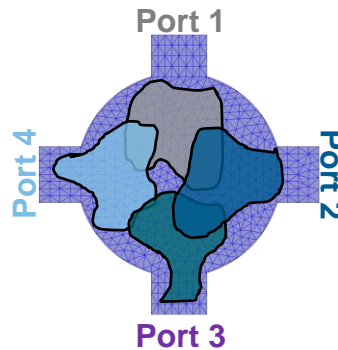
- Determines which modes are excited during 3D Refinement
 - Modes excluded have NO impact on the mesh density
- Eliminating an excitation from the 3D Refinement Process
 - Simplifies the analysis
 - Can overcome convergence issues



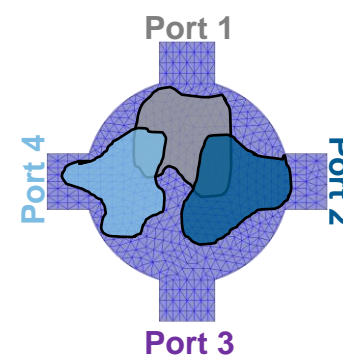
Mesh for Random Multiport Device



Regions Requiring Mesh Refinement



Regions Requiring Mesh Refinement with Port 3 Excluded



- For phased array element analysis uncheck all the modes.
 - The primary purpose of the Floquet Port is to terminate the array's radiated power and determine how the element transmits power to different Floquet Modes.
 - The transmission terms from the antenna to the Floquet Modes will be accurate because the antenna's ports are always included in the 3D Refinement process.
 - The only questionable results will be the transmission and reflection terms where the power emanates from the Floquet Port itself.