### Lens Design Lecture #1-3

### College of Optical Sciences University of Arizona



## Tentative "syllabus":

- Microscopes, mainly objectives, some eyepiece
  - -~3 weeks
- Telecentric systems
  ~3 weeks
- Tolerancing
  - ~6 weeks
- Synopsis software
  - ~2 weeks

## Microscope objectives

# Magnification & designing backwards



# Characteristics of microscope objectives

- Historically, most microscope objectives were designed to operate at finite conjugates
  - "Infinity-corrected" becoming more prevalent
- Specified by NA in object space
  - object marginal angles tend to be large (fast)
- Must resolve fine detail or structure of SUT
- Design approach may require personalized optimization techniques
  - Modification of standard merit functions
- Important note: the object and image are reversed in design
  - Design from long conjugate to short
    - Helps the optimization process



## Microscope objective

Some design techniques:

- Petzval lens
- Aplanatic surface
- Concentric surfaces
- Sort of new: object immersion (higher NA by higher n)



# Optical systems for magnification



## Why microscopes?

Possible methods for observing small objects:

- The eye (observe directly)
- Simple magnifier AKA magnifying glass
  - Real image
  - Virtual image located at finite location
  - Virtual image at infinity
- Compound magnifier



## Motivation

### Why microscopes?:

Consider direct observation and magnifier:





## No microscope

### Just look with your eye...





### Forms a "real image" with the eye





### Simple magnifier: virtual image at finite





### Forms a virtual image at infinity

virtual image at infinity





## Magnification





If magnifier is close to the eye, s may be negligible Copyright 2017 Mary G. Turner



## Magnifying power

#### Simple magnifier: virtual image at finite distance



$$MP = \frac{\overline{u}_{mag}}{\overline{u}_{mag}} \cong \frac{h'/_{Z'}}{h/_{Z'}}$$
  
Magnifying power (MP)



Simple magnifier: virtual image at finite distance **Back into imaging** virtual image eye pupil Magnifying power (MP)  $MP = \frac{\overline{u}_{mag}}{\overline{u}_{no}} \cong \frac{h'/_{z'}}{h/_{z}} \quad \overleftarrow{z'}$ Ζ S maa  $MP = \frac{(f - z')z}{f * z'} = \frac{z}{z'} - \frac{z}{f} = \frac{-250mm}{z'} + \frac{250mm}{f}$ 



## Magnifying power (MP) & focal length

Simple magnifier 2 -> 3

Important case:

Let the image distance  $z' \rightarrow \infty$ This is the "relaxed eye" Magnifying power (MP) when  $z = -f, z' \rightarrow \infty$ So for an image at infinity  $MP = \frac{-250mm}{r'} + \frac{250mm}{f} = \frac{250mm}{f[mm]}$ 





## Magnifying power (MP) & focal length: example



Magnifying power (MP)when  $z = -f, z' \rightarrow \infty$ 

So for an image at infinity, let's try a focal length of 25mm

$$MP = \frac{250mm}{f[mm]} = \frac{250mm}{25mm} = 10X$$



# Magnifying power (MP) required to resolve by eye

Simple magnifier: virtual image versus direct view Using the *image at infinity*  $cas_{h'}$  $(z = -f, z' \to \infty)$ Magnifying power (MP) for eye t (1arc-min~0.3mrad) an object of height **h** relying on d<sub>0</sub>=250mm

 $MP = \frac{\bar{u}_{mag}}{\frac{\bar{u}_{mag}}{mag}} = \frac{0.3mrad}{h/d_0} = \frac{0.3mrad * 250mm}{h} = \frac{75um}{h[um]}$ 



## MP required to resolve by eye: example

Simple magnifier: virtual image versus direct view Using the *image at infinity* case  $(z = -f, z' \rightarrow \infty)$ , with  $d_0 = 250m$  $\overline{u}'(mag)$ Magnifying power (MP) for eye to h an object of 0.5um height

 $MP_{needed} = \frac{75um}{h[um]} = \frac{75um}{0.5um} = 150X$  needed to resolve



eye pupi

h'

### Simple magnifier, relaxed eye Simple magnifier: virtual image at infinity (relaxed eye)





## Compound magnifier (microscope

### Compound magnifier:

# Virtual image at infinity (of an intermediate objective image)





## Microscope objectives

# Magnifying Power and visual resolution



## Microscopes

- A magnifier is the simplest microscope
  - Very limited in how much it can magnify
  - ~25X absolute limit
- Compound system has two sections
  - Objective
  - Eyepiece
  - Magnification product of both
    - $MP_{microscope} = M_{objective} * MP_{eyepiece}$
    - $MP_{microscope} = -\frac{OTL}{f_{objective}} * \frac{250}{f_{eyepiece}}$
- MP of microscope called visual resolution

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## Microscope

 A magnifier consists of an objective plus an eyepiece



- Assume 25X objective, 10X eyepiece
- MP=25\*10=250

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**Optical Systems** 

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A microscope is a sophisticated magnifier consisting of an objective plus an eyepiece.

Microscopes



The visual magnification is the product of the objective magnification and the eyepiece MP.

$$\begin{split} m_{OBJ} &= \frac{z'_O}{z_O} \qquad MP_{EYE} = \frac{250 \text{ mm}}{f_{EYE}} \\ m_V &= m_{OBJ} MP_{EYE} = \frac{z'_O 250 \text{ mm}}{z_O f_{EYE}} \end{split}$$

The optical tube length OTL of a microscope is defined as the distance from the rear focal point of the objective to the front focal point of the eyepiece (intermediate image). Standard values for the OTL are 160 mm and 215 mm. The OTL is a Newtonian image distance:

$$m_{OBJ} = -\frac{OTL}{f_{OBJ}}$$
  $m_V = -\frac{OTL}{f_{OBJ}}\frac{250 \text{ mm}}{f_{EYE}}$ 

The NA of a microscope objective is defined in object space by the half-angle of the accepted input ray bundle. Along with the objective magnification, the NA is inscribed on the objective barrel.

#### $NA = n\sin\theta$

Microscope objectives are often telecentric in object space. The stop is placed at the rear focal point of the objective so that the magnification does not change with object defocus.



#### Visual magnification m<sub>v</sub>



### Example: 25 X objective with 10X eyepiece

 $m_v = 25 \times 10 = 250$ 

#### Much greater than a simple magnifier Optics



Two sets of conjugate planes

- image conjugates
  - object
  - intermediate image
  - eye image



Tkaczyk , Field Guide to Microscopy



- pupil conjugates
  - objective internal stop
  - eye pupil

#### Visual magnification m<sub>v</sub>

Optical tube length is Newtonian image distance.



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## **Microscope resolution**





http://www.olympusmicro.com/primer/digitalimaging/deconvolution/deconresolution.ht ml



Rayleigh & Sparrow criteria Overlap of Airy disks to differ Rayleigh is most commonly



**Figure 6.17** The dashed lines represent the diffraction patterns of two point images at various separations. The solid line indicates the combined diffraction pattern. Case (b) is the Sparrow criterion for resolution. Case (c) is the Rayleigh criterion.

Smith, Modern Optical Engineering



- overlapping Airy disks
  - Rayleigh criterion

$$0.61 \frac{\lambda}{NA}$$

where  $NA = n \sin \theta$ 

Kidger, Intermediate Lens Design p.

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http://www.microscopyu.com/tutorials/java/objectives/nuaperture/index.ht ml

- Higher resolution requires working at higher NA or lower wavelength
  - angle  $\theta$  is limited
- Raise index in object space
  - liquid immersion: oil (cedar<sup>\*</sup>; n ~ 1.515, V ~41.5), water (n ~ 1.333)
  - solid immersion (Solid Immersion Lens, SIL, Gaten Optical Engineering



**Overlapping Airy disks** 

- Rayleigh criterion
  - $0.61 \frac{\lambda}{NA}$
  - where  $NA = n \sin \theta$



http://www.microscopyu.com/tutorials/java/objectives/nuaperture/index.ht ml

Higher resolution requires working at higher NA or lower wavelength

- angle  $\theta$  is limited

Raise index in object space

- liquid immersion: oil (cedar<sup>\*</sup>; n ~ 1.515, V ~41.5), water (n ~ 1.333)
- solid immersion (Solid Immersion Lens, SIL, GaP n >3)



## Factors in resolution

### Animations from web sites



#### Animation of microscope objective numerical aperture (Nikon)



http://www.microscopyu.com/tutorials/java/objectives/nuaperture/index.html



Animation of microscope objective numerical aperture (Nikon)

a few captures at various NA for non-video use



http://www.microscopyu.com/tutorials/java/objectives/nuaperture/index.ht ml


## Microscope objective numerical aperture (Nikon)

#### Comparing several NA values if video not





## Resolution of a cluster of points (Olympus)



http://www.olympusmicro.com/primer/java/imageformation/airyna/index.html



## Resolution of a cluster of points (Olympus)

• A few samples:





# Animation of microscope objective resolution (Olympus)



http://www.olympusmicro.com/primer/java/imageformation/rayleighdisks/index.html



## Microscope objective resolution (Olympus)



http://www.olympusmicro.com/primer/java/imageformation/rayleighdisks/index.html



# Microscope objective resolution (Olympus)

Varying only NA



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# Microscope objective resolution (Olympus)

• Varying only wavelength





#### **Microscope objectives**

#### **Design forms**



## In order of increasing NA

Aplanatic, concentric surfaces

• Amici-type

Immersion type

- Oil
- Water
- Solid
- CaF<sub>2</sub>
  - Control secondary color
- Fluorite elements (shaded)
  - Reduce dispersion Copyright 2017 Mary G. Turner



Figure 13.6 Microscope objectives. (a) Low-power achromatic doublet or triplet. (b)  $10 \times NA 0.25$ . (c) Amici objective  $20 \times NA 0.5$  to  $40 \times NA 0.8$ . (d) Immersion objective. (e) Apochromatic  $10 \times NA 0.3$ . Shading indicates fluorite (CaF<sub>2</sub>). (f) Apochromatic  $50 \times NA 0.95$ .

Smith, Modern Optical Engineering



#### Solid immersion

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Microscopy: Resolution Enhancement Techniques

#### Solid Immersion

- High NA Amici-like
- Immersion without the liquid
- Evanescent coupling between a hemispherical immersion optic and the object
- For thin, flat object





Tkaczyk, Field Guide to Microscopy



Solid immersion

- High NA Amici-like
  - Aplanatic & concentric
- Central homogeneous cone is concentric on bottom planar surface, resulting in plane-wave propagation
- Ring (cored cone) couples evanescently



Fig. 4. Light incident on the recording layers can be divided into two parts: the homogeneous cone and the inhomogeneous ring. In the ring, light couples evanescently into the recording layers through the gap. In the cone, light propagates directly across the gap as a homogeneous plane wave.

Roles of propagating and evanescent waves in solid immersion lens systems By Tom D. Milster, Joshua S. Jo, and Kusato Hirota APPLIED OPTICS y Vol. 38, No. 23 y 10 August 1999



Basic microscope layout

- Important issues
  - cover slip
  - working distance
  - optical tube length
  - mechanical tube length
  - pupil matching: microscope exit pupil to eye pupil



Microscopy



- In design, we will mostly talk about optical tube length
- Do not confuse mechanical tube length with optical tube length
- Objectives are marked for identification of key specifications

- The **working distance** WD is the distance from the object to the first element of the objective; can be less than 1 mm for high-power objectives.
- The **mechanical tube length** is separation between the shoulder of the threaded mount of the objective and the end of the tube into which the eyepiece is inserted. Objectives and eyepieces must be used at their design conjugates and are not necessarily interchangeable between manufacturers.



Greivenkamp, Field Guide to Geometrical Optics





#### Correction types

Lens

Doublet-

Front

ens



Common Objective Optical Correction Factors

http://micro.magnet.fsu.edu/primer/a natomy/objectives.html

Doublet

Groups

Meniscus

Lens

6 - + 6

#### 60x Plan Apochromat Objective



http://www.microscopyu.com/articles/optics/objectivespecs.html/



#### LWD Plan Infinity-Corrected Apochromat Objective



#### Continuing the tour of objectives

The hierarchy of commercial objectives begins with simple **achromats**. Next, **Fluorites** or **semi-apochromats** have similar color correction to achromats, but they correct for spherical aberration for two or three colors. The name "fluorites" was assigned to this type of objective due to the natural mineral originally used to build this type of objective. 'Fluor' (CaF2, n =1.43, V = 95!! very low dispersion). There are also **plan-achromats**, achromats with field correction. The most advanced microscope objectives are **apochromats**, which are usually chromatically corrected for three colors, with spherical aberration correction for at least two colors. They are similar in construction to fluorites but with different thicknesses and surface figures. With the correction of field curvature, they are called **plan-apochromats**.



#### **Objective Correction for Optical Aberration**

Objective Type	Spherical Aberration	Chromatic Aberration	Field Curvature
Achromat	1 Color	2 Colors	No
Plan Achromat	1 Color	2 Colors	Yes
Fluorite	2-3 Colors	2-3 Colors	No
Plan Fluorite	3-4 Colors	2-4 Colors	Yes
Plan Apochromat	3-4 Colors	4-5 Colors	Yes

Table 1

http://micro.magnet.fsu.edu/primer/a natomy/objectives.html



#### **Microscope objectives**

The Petzval lens & classic design Designing microscope objectives



### About designing microscopes

- Disclaimer:
  - This is not legal advise
- A vast array of design examples are available in the literature and from patents
- It is highly recommended that some of these be examined before starting on more complex designs
- We will start from the simplest



#### An achromat

- An "Off-the-shelf" achromat can serve as a simple microscope:
  - Use at finite conjugates





### The Petzval objective

#### A more useful design is based on the

#### Petzval objective For system focal length f<sub>P</sub>

• Front group has focal length  $f_1 = f_P * 2$ 

- Rear group has focal length  $f_2 = f_P * 1$
- spacing between groups
- Back focal length



rear group: achromatized pair using Celor equations



f2

BFL

#### The Petzval objective

• Start with  $a_{t_2}$  Petzval lens of focal length  $f_P$ 





#### Starting point for designing objective



overall focal length  $f_P$ 

- Two positive lenses
- increased NA
- weaker surfaces share ray bending





#### The Lister objective



#### Again with the math.... $\phi_1 = \frac{1}{f_1} = \frac{1}{2f_p} = \frac{1}{2}\phi$ $\phi_2 = \frac{1}{f_2} = \frac{1}{f_2} = \phi$ $\phi = \phi_1 + \phi_2 - \phi_1 \phi_2 \tau$ $=\phi_{1}+\phi_{2}-\phi_{1}\phi_{2}t$ $f_1 = 2 \cdot f_P$ В $=\frac{1}{2}\phi + \phi - \frac{1}{2}\phi^{2}t$ $f_2 = f_P$ $=\frac{3}{2}\phi - \frac{1}{2}\phi^{2}t$ $t = f_{P}$ $2\phi = 3\phi - \phi^2 t$ $B = \frac{f_P}{2}$ $\Rightarrow$ $t = \frac{1}{\phi} = f_P$ $\phi = \phi^2 t$



#### Petzval into Lister





## Lister 10X microscope objective

Start with perfect optics

FL(objective) = 17 mm  $FL_1 = 2 * FL = 34 mm$   $FL_2 = FL = 17 mm$  t = FL = 17 mm







### Now add real optics

- Achromatic doublet for front lens:
  - 34mm FL
    - Use N-BK7 and N-SF6.
    - N-BK7: n = 1.51680, V = 64.17

• N-SF6: n = 1.80518, V = 25.36  

$$\varphi_1 = \frac{64.17}{64.17 - 25.36} \cdot \left[\frac{1}{34}\right] = 0.04863 = 2(n-1)/R1$$

$$\varphi_2 = \frac{25.36}{25.36} \cdot [1/34] = -0.01922$$

Let R1=-R2=-R3= 21.25mm (1<sup>st</sup> element symmetric)

$$R4 = -43.14$$
mm



## Finish adding lenses

- Achromatic doublet for the back:
  - 17mm FL
    - Use N-BK7 and N-SF6.
    - N-BK7: n = 1.51680, V = 64.17

• N-SF6: n = 1.80518, V = 25.36  

$$\varphi_1 = \frac{64.17}{64.17 - 25.36} \cdot [1/17] = 0.09726$$

$$\varphi_2 = \frac{25.36}{25.36} \cdot [1/17] = -0.03844$$

- Let R1=-R2=-R3= 10.63mm (1<sup>st</sup> element symmetric)
  - R4 = -21.57mm



# Now put it into the design program

- Start with "thin" lenses
  - Lens thickness not useful
  - PMAG: -0.10 (10X)
  - u': 0.25





FL(objective) = 17mm

$$FL_1 = 2 * FL = 34mm$$
$$FL_2 = FL = 17mm$$
$$t = FL = 17mm$$

10X, 0.25NA



## Optimize





10X, 0.25NA



Lister 10X microscope objective

(Petzval objective) typical optimized results

10X, 0.25NA



$$FL(objective) = 17mm$$

$$FL_1 = 2 * FL = 34mm$$

$$FL_2 = FL = 17mm$$

$$t = FL = 17mm$$



## Final design

- Constrain glass thickness
- Allow glass selecti

   Restrict choices:
  - Preferred, inexper





#### Amici modification



# Comparing "conventional" objective to Amici

- Comparable form, ignoring the Amici hemisphere
  - -10X, 0.25 NA conventional
  - -20X NA 0.5 40X NA 0.8 Am
- Amici
  - Aplanatic surface
  - -Greater NA, MP
  - -Small working distance





Smith, Modern Optical Engineering



### Modified Lister objective

- Element added:
  - increase NA (40X, NA 0.65)



Field pos.: 1

\_\_\_\_\_

Figure 7.1 Classical Lister objective with aplanatic element.

Kidger, Intermediate Lens Design



#### Modified Lister: Zemax

- Zemax layout
  - Stretched in Y to show some detail
  - Some/ slight vignetting seen



Object in Zemax (Intermediate image plane)

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Image in Zemax (Actually the Object)



### Lister with Amici modification

- Isolate the Amici optic:
  - First surface: "Almost" aplanatic
  - Second surface: Concave Petzval corrector




## Complex objective designs

Examples of correction by section



Gross, Handbook of Optical System, V.3

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