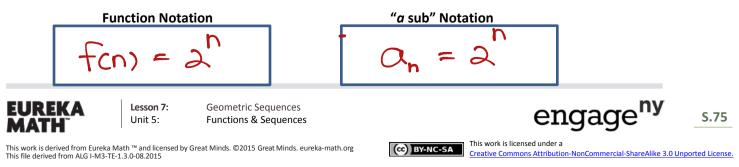


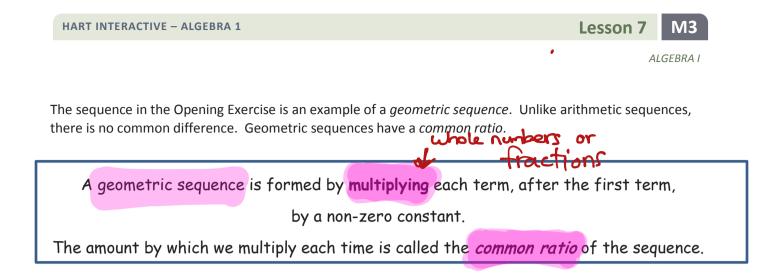
1. A. **PREDICTION** If we fold a rectangular piece of paper in half multiple times and count the number of rectangles created, what pattern do you expect in the number of rectangles?

B. **TRY IT!** Use the table below to record the number of rectangles in the paper folding experiment.

Term number	Sequence	Sketch of Unfolded Paper
(number of folds)	(number of rectangles)	
1	2	fold line
2	Ч	
3	8	
4	16	
5	32	
6	64	
n	بر بر	

C. Write an explicit formula for this sequence.





The sequence in the Opening Exercise was fairly simple and you saw something similar to it in Lesson 3 with Aunt Lucy's Plan 4. Let's look at more challenging sequences and determine the pattern for the explicit formula.

- 2. Consider the sequence: 2, 6, 18, ...
 - A. Write the next three terms.

2,6,18,54,62,486

B. Why isn't this an arithmetic sequence?

Because there's no common difference.

C. What is the pattern? What is the common ratio?

Multiply each term by 3 = common ratio

D. Fill in the table below.

n	1	2	3	4	5	6	
f(n)	2	6	18	54	162	486	
Pattern	2	2(<mark>3</mark>)	2(<u>3)(3</u>)	Q.33.3	2.3333	2.3.3.3.3.3	3
Exponential form	2.3	2.3	2.3	2.3	2.34	2·3 ⁵	
$f(n) = 2 \cdot 3^{n-1}$							
UREKA Less MATH	on 7: Terr	netric Sequences tions & Sequence	s V	mmon	This work is licensed	engag	e

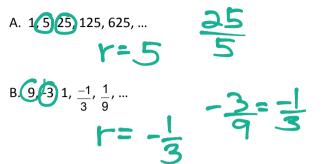
					<u>(</u> 6, ^L	186)
HART INTERACTIVE – ALGEBRA 1			Lessor	n 7 🛛 🛛	VI3	
8 ارد) (عرد) (حرا))	((5ر+	4 ALGEE	ر6 ^ل ر M3 BRA(5)	162)
E. Plot the points on the graph. What type of graph do the points	500					_
make?	480					1
IIIdKe!	460					4
	440					4
	420					Н
	400					Η
	380 360					-
	340					
	320					_
F. Write the explicit formula for this sequence based on the	300					4
pattern in the table.	280					-
	260					-
1	240					-
n-1	220					-
	200 180					1
Γ , γ γ	160					
$f(n) = 2 \cdot 3$	140					_
	120					4
	100					-
	80					-
	60			1		-
	40					1
	20					1
	() 1	2	3 4	4 5	6

3. We can now say that . . .

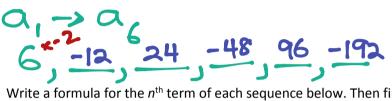
Arithmetic sequences are modeled by $\underline{\qquad}$	near functions.
Geometric sequences are modeled by	
common ratio=	r
4. To find the general term, $f(n)$ or a_n , of a geometric seque	ence you need the first term, $f(1)$, and the
$f(n) = \frac{f(n)}{f(n)} $ or	$a_n = \underline{a_1} \cdot \underline{r}$
EUREKA Lesson 7: Geometric Sequences Unit 5: Functions & Sequences	CCOBY-NC-SA This work is licensed under a Creative Commons Attribution-NonCommercial-ShareAlike 3.0 Unported License



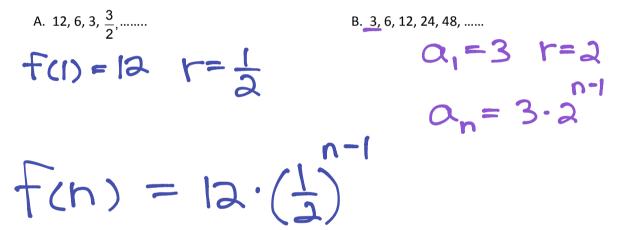
5. Find the common ratio for the following geometric sequences:



6. Write the first six terms of the geometric sequence with first term 6 and common ratio -2.



7. Write a formula for the n^{th} term of each sequence below. Then find f(8).





Geometric Sequences Functions & Sequences





Lesson Summary

A *geometric sequence* is a sequence in which each term after the first is obtained by multiplying the preceding term by a fixed non-zero constant. The amount by which we multiply each time is called the *common ratio* of the sequence.

Geometric sequences can be modeled by exponential functions.

The common ratio, r, is found by dividing any term after the first term by the term that directly precedes it.

General Term of a Geometric Sequence

The nth term (the general term) of a geometric sequence with first term f(1) or a_1 and common ratio r is

$$f(n) = f(1)r^{n-1}$$
 or $a_n = a_1 \cdot r^{n-1}$

Example: Find f(8) of the geometric sequence when f(1) = -4 and the common ratio is -2.

$$f(n) = -4 \cdot (-2)^{n-1}$$
$$f(8) = -4 \cdot (-2)^{8-1}$$
$$= -4 \cdot (-2)^{7}$$
$$= -4 \cdot (-128)$$
$$= 512$$



Geometric Sequences Functions & Sequences



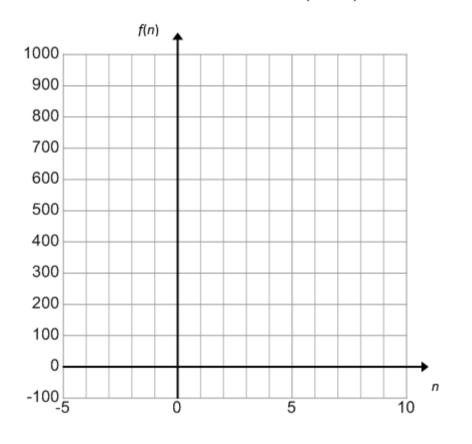
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Homework Problem Set

- 1. Consider a sequence that follows a times 5 pattern: 1, 5, 25, 125,
 - a. Write a formula for the n^{th} term of the sequence. Be sure to specify what value of n your formula starts with.
 - b. Using the formula, find the 10^{th} term of the sequence.

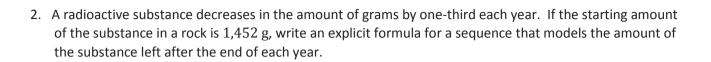
c. Graph the terms of the sequence as ordered pairs (n, f(n)) on a coordinate plane.





Lesson 7: Unit 5: Geometric Sequences Functions & Sequences





3. Write the first five terms of each geometric sequence.

A.
$$f(1) = 20$$
, $r = \frac{1}{2}$
B. $a_1 = 4$, $r = 3$

Use the formula for the general term (n^{th} term) of a geometric sequence to find the indicated term of each sequence with the given first term, f(1) or a_1 , and common ratio, r.

5. Find a_{12} when $a_1 = 5$, r = -2. 4. Find f(8) when f(1) = 6, r = 2.

6. Find a_{22} when $a_1 = 1000$, $r = -\frac{1}{2}$.

7. Find
$$f(15)$$
 when $f(1) = 9000$, $r = -\frac{1}{3}$



Geometric Sequences Functions & Sequences



Lesson 7

M3

ALGEBRA I



Write a formula for the n^{th} term of each geometric sequence. Then use the formula to find f(7).

9. 18,6,2,²/₃,.... 8. 3, 12, 48, 192,

Find the first 5 terms of the following function.

11. $f(n) = 3^{n-2}$ 10. $a_n = 1^n$

Write a formula for the general term (the n^{th} term) of each geometric sequence. Then use the formula for *f*(*n*) to find *f*(9).

12. 5, -1, $\frac{1}{5}$, $-\frac{1}{25}$,.... 13. 0.07, 0.007, 0.0007, 0.00007, ...



Geometric Sequences Functions & Sequences





14. A mine worker discovers an ore sample containing 500 mg of radioactive material. It is discovered that the radioactive material has a half life of 1 day. (This means that each day, half of the material decays, and only half is left.) Find the amount of radioactive material in the sample at the beginning of the 7th day.

15. A culture of bacteria doubles every 2 hours. If there are 500 bacteria at the beginning, how many bacteria will there be after 24 hours?

16. You complain that the hot tub in your hotel suite is not hot enough. The hotel tells you that they will increase the temperature by 10% each hour. If the current temperature of the hot tub is 75° F, what will be the temperature of the hot tub after 3 hours, to the nearest tenth of a degree?



Geometric Sequences Functions & Sequences



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CHALLENGE PROBLEMS

- 17. Find the common ratio and an explicit form in each of the following geometric sequences.
 - A. 4, 12, 36, 108, ...
 - B. 162, 108, 72, 48, ...
 - C. $\frac{4}{3}, \frac{2}{3}, \frac{1}{3}, \frac{1}{6}, \dots$
 - D. $xz, x^2z^3, x^3z^5, x^4z^7, ...$
- 18. The first term in a geometric sequence is 54, and the 5th term is $\frac{2}{3}$. Find an explicit form for the geometric sequence.
- 19. If 2, a, b, -54 forms a geometric sequence, find the values of a and b.

20. Find the explicit form f(n) of a geometric sequence if f(3) - f(1) = 48 and $\frac{f(3)}{f(1)} = 9$.







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